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COSC 3020

Lab\_04 Time complexity

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|---|----------------|
| 1. If the array has 0 or 1 element the array is sorted, stop. | $T(1)$         |
| 2. Go through all permutations until sorted array is found.   | $T(n * n - 1)$ |
| 3. Test to find an array that is sorted.                      | $T(n)$         |

Recurrence Relation:

$$T(n) = \begin{cases} 1 & \text{if } n = 0 \\ 1 & \text{if } n = 1 \\ (n * n - 1) & \text{if } n > 1 \end{cases}$$

Solve by substitution

$$T(n) = T(n * n - 1)$$

$$= 2T(n * n - 1)$$

$$= 3T(n * n - 1)$$

...

$$= 1^i T(n * n - 1^i)$$

For  $i = n$

$$= T(1) + n + (n * n - 1) = 1 + n + (n * n - 1) \in \Theta(n!)$$

The best-case scenario would be to find the sorted array on the first permutation. It would have a time complexity of  $\Theta(n)$ .

The worst-case scenario is a time complexity of  $\Theta(n!)$

If using a randomly generated permutation to find a sorted array the worst case scenario would be  $\Theta(\infty)$ . This is due to the fact that it is entirely possible to never find the sorted permutation if the permutations are randomly generated.