

### Optimal control – Assignment 3

The state vector are inputted as the following :

```

x0=[ 0 0 -1.52 0];

A=[ 0 1 0 0
    0 -0.4 0 -0.01
    0 0 0 1
    9.8 -1.43 0 -0.02 ];

B=[ 0
    6
    0
    9.8 ];

C=[ 1 0 0 0
    0 0 1 0 ];

D=[ 0
    0 ];

```

After that, with the initial Q and R, the height and pitch of the helicopter was computed as follows.

```

Q=diag([1000 1 50 1]);
R=0.001;

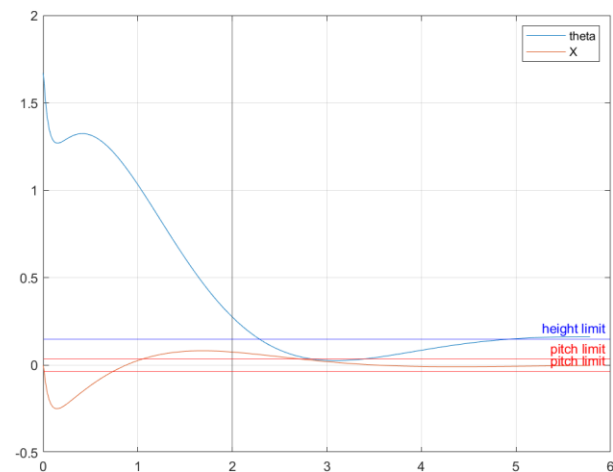
[Ko, Mo, E]=lqr(A, B, Q, R);

sysCL=ss(A-B*Ko, [B zeros(4,1)], [ zeros(1,4) ;C2],zeros(2,2));
[y,t,e]=initial(sysCL, x0');
n=size(t,4);

Xdt = [0 0 0.15 0] ;
Xd = repelem(Xdt,n,1);
X=Xd-e ;
u=Ko*e';

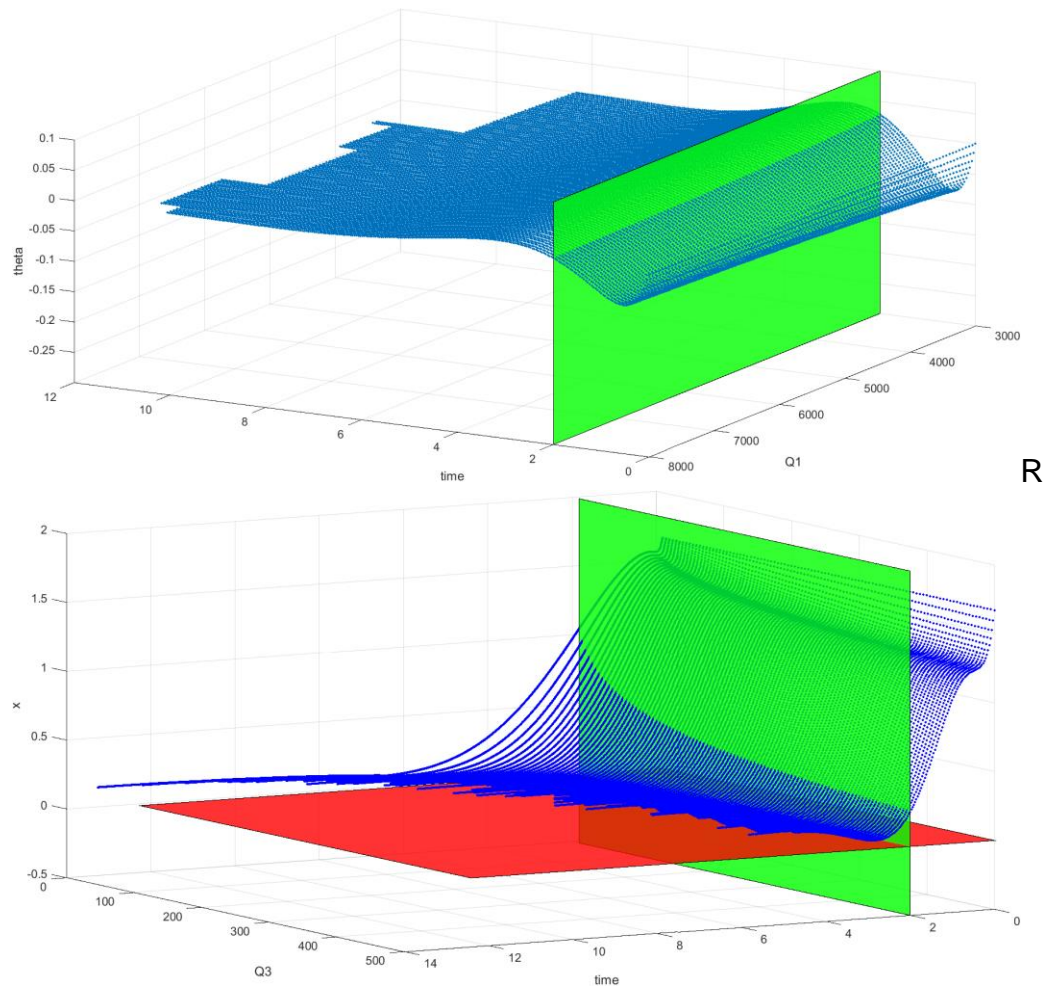
X1=X(1:end,1);
X3=X(1:end,3);

```



the resulted plot suggested that the helicopter went above height limit just after 2 seconds limit and briefly after 5 second. The pitch also still outside the limit after 2.5 seconds. Therefore, the system still need optimization.

Various solution has been tried to get the optimal value of Q and R. including brute forcing the value using for loop for x1 and x3 in Q resulting in this 3D graph.



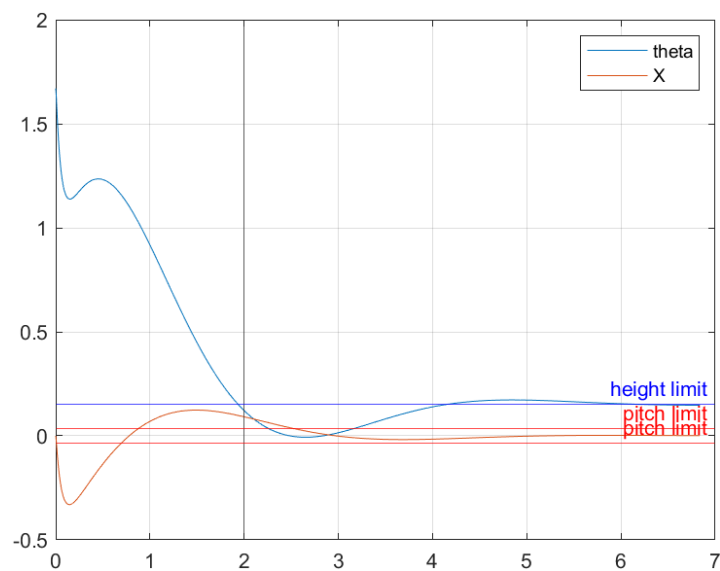
The closest value that has been attempted is

$$Q = \begin{bmatrix} 820 & 1 & 85 & 1 \end{bmatrix}$$

$$R = 0.001$$

Which resulting in this graph.

The helicopter manage to reach the height target before 2 second but it went above it again after 4 second.



At the end I did not manage to reach the specification. I suspect that I made mistake in the computation of the state space. Otherwise, its simply my lack of understanding and experience.