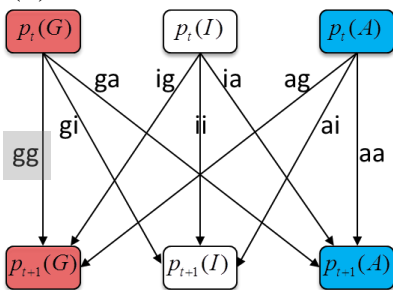


(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

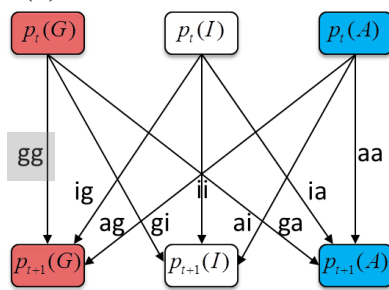
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(I)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers*_{*t*} (at time *t*)

$p_t(A)$ – proportion of *Absentees*_{*t*} (at time *t*)

$p_{t+1}(I)$ = proportion of *Irregulars*_{*t+1*}

gg – *Goers*_{*t*} who stay *Goers*_{*t+1*}

gi – *Goers*_{*t*} who become *Irregulars*_{*t+1*}

ga – *Goers*_{*t*} who become *Absentees*_{*t+1*}

ig – *Irregulars*_{*t*} who become *Goers*_{*t+1*}

ii – *Irregulars*_{*t*} who stay *Irregulars*_{*t+1*}

ia – *Irregulars*_{*t*} who become *Absentees*_{*t+1*}

ag – *Absentees*_{*t*} who become *Goers*_{*t+1*}

ai – *Absentees*_{*t*} who become *Irregulars*_{*t+1*}

aa – *Absentees*_{*t*} who stay *Absentees*_{*t+1*}

gg

gi

ga

ig

ii

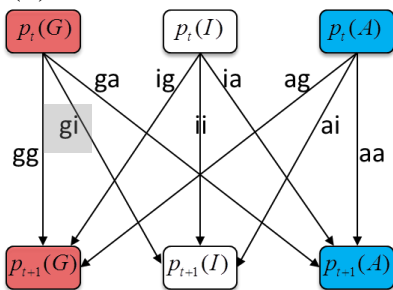
ia

ag

ai

aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - \text{gi} - \text{ga} + \text{ig} + \text{ag}$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - \text{ag} - \text{ai} + \text{ga} + \text{ia}$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = \text{gg} + \text{gi} + \text{ga}$$

$$p_t(I) = \text{ig} + \text{ii} + \text{ia}$$

$$p_t(A) = \text{ag} + \text{ai} + \text{aa}$$

(d) Next year

$$p_{t+1}(G) = \text{gg} + \text{ig} + \text{ag}$$

$$p_{t+1}(I) = \text{ii} + \text{gi} + \text{ai}$$

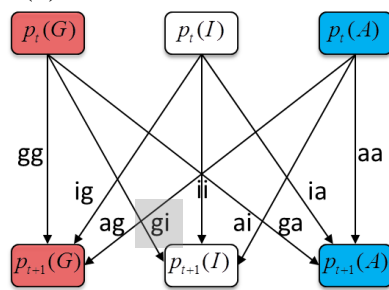
$$p_{t+1}(A) = \text{aa} + \text{ga} + \text{ia}$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$\text{gg} = (p_t(G) - \text{gi} - \text{ga})$$

$$\text{aa} = (p_t(A) - \text{ag} - \text{ai})$$

$$\text{ii} = 1 - \text{gg} - \text{gi} - \text{ga} - \text{ia} - \text{aa} - \text{ig} - \text{ag} - \text{ai}$$

(h) Diffusion predicts transitions:

$$\text{gi} = k_{gi} p_t(G)$$

$$\text{ga} = k_{ga} p_t(I)$$

$$\text{ig} = k_{ig} p_t(I)$$

$$\text{ia} = k_{ia} p_t(I)$$

$$\text{ag} = k_{ag} p_t(A)$$

$$\text{ai} = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

aa – *Absentees_t* who stay *Absentees_{t+1}*

gg

gi

ga

ig

ii

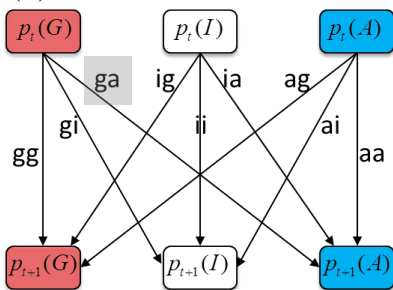
ia

ag

ai

aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

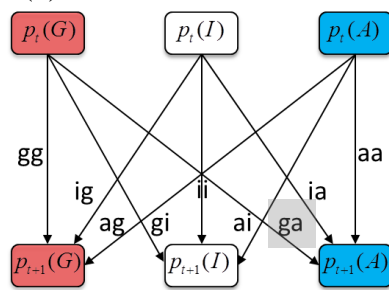
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers*_t (at time *t*)

$p_t(A)$ – proportion of *Absentees*_t (at time *t*)

$p_{t+1}(I)$ = proportion of *Irregulars*_{t+1}

gg – *Goers*_t who stay *Goers*_{t+1}

gi – *Goers*_t who become *Irregulars*_{t+1}

ga – *Goers*_t who become *Absentees*_{t+1}

ig – *Irregulars*_t who become *Goers*_{t+1}

ii – *Irregulars*_t who stay *Irregulars*_{t+1}

ia – *Irregulars*_t who become *Absentees*_{t+1}

ag – *Absentees*_t who become *Goers*_{t+1}

ai – *Absentees*_t who become *Irregulars*_{t+1}

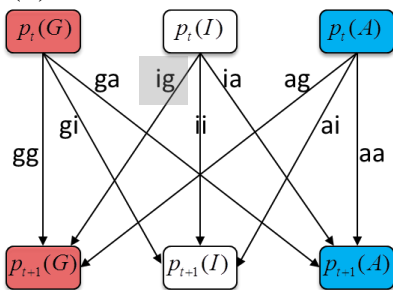
aa – *Absentees*_t who stay *Absentees*_{t+1}

gg *gi* *ga*

ig *ii* *ia*

ag *ai* *aa*

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

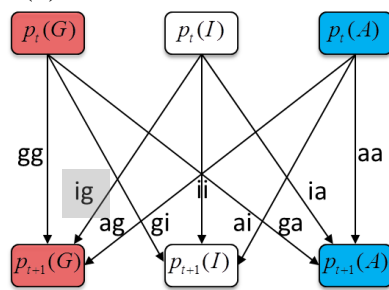
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

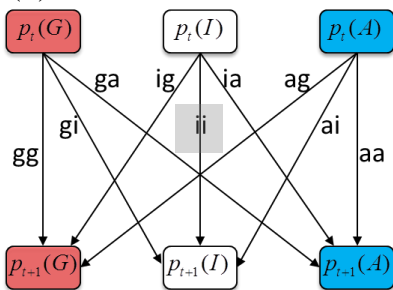
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

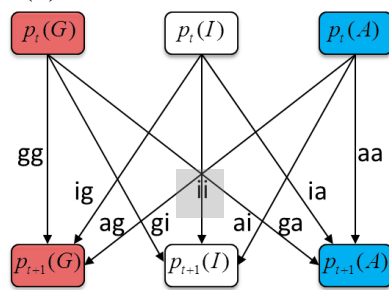
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(I)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

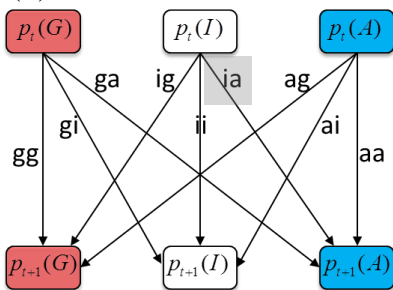
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

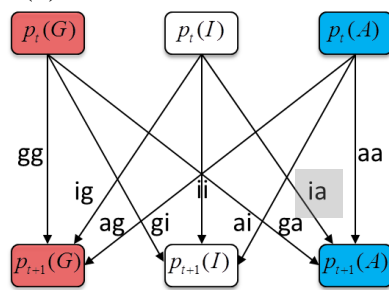
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(I)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

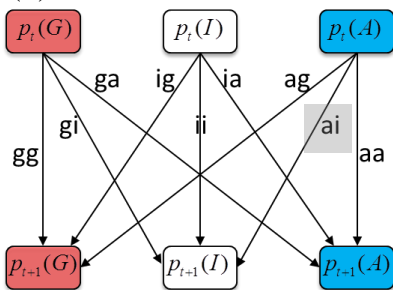
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

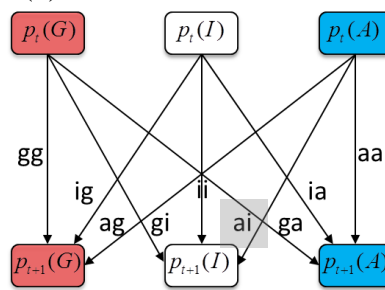
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(I)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

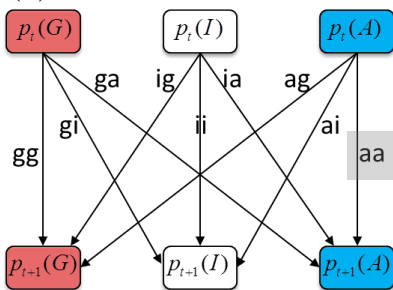
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Diffusion

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + k_{ig} p_t(I) + k_{ag} p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - k_{ag} p_t(A) - k_{ai} p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

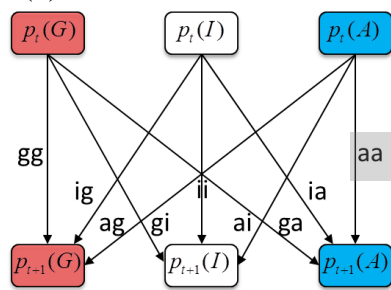
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Diffusion predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(I)$$

$$ig = k_{ig} p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = k_{ag} p_t(A)$$

$$ai = k_{ai} p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

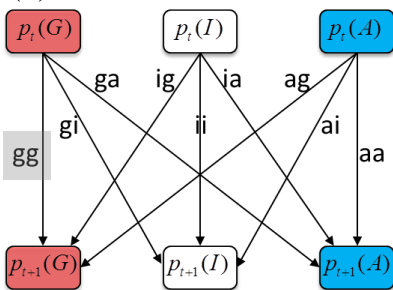
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A) + T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I) + T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

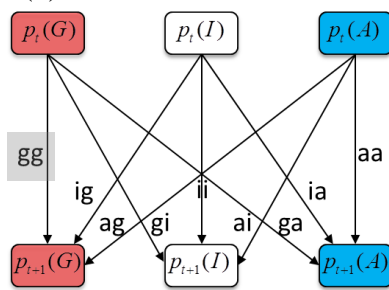
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

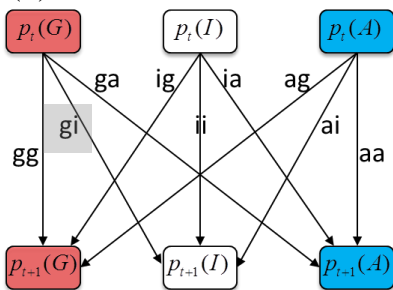
$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}* gg gi ga ig ii ia ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A) + T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I) + T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

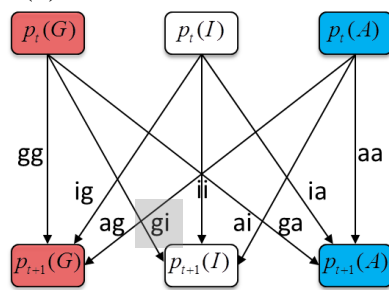
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

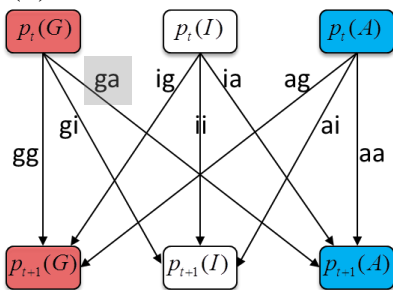
$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}* gg gi ga ig ii ia ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A) + T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I) + T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

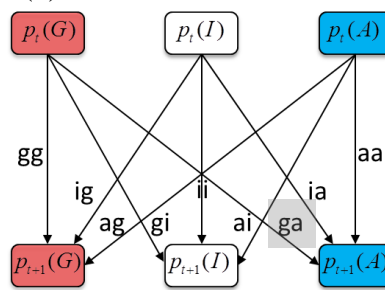
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

$p_t(G)$ = proportion of *Goers*_{*t*} (at time *t*)

$p_t(A)$ – proportion of *Absentees*_{*t*} (at time *t*)

$p_{t+1}(I)$ = proportion of *Irregulars*_{*t+1*}

gg – *Goers*_{*t*} who stay *Goers*_{*t+1*}

gi – *Goers*_{*t*} who become *Irregulars*_{*t+1*}

ga – *Goers*_{*t*} who become *Absentees*_{*t+1*}

ig – *Irregulars*_{*t*} who become *Goers*_{*t+1*}

ii – *Irregulars*_{*t*} who stay *Irregulars*_{*t+1*}

ia – *Irregulars*_{*t*} who become *Absentees*_{*t+1*}

ag – *Absentees*_{*t*} who become *Goers*_{*t+1*}

ai – *Absentees*_{*t*} who become *Irregulars*_{*t+1*}

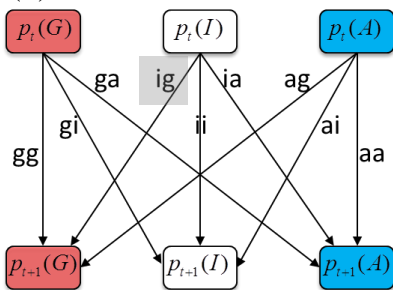
aa – *Absentees*_{*t*} who stay *Absentees*_{*t+1*}

gg *gi* *ga*

ig *ii* *ia*

ag *ai* *aa*

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga$$

$$+ ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai$$

$$+ ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A)$$

$$+ T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I)$$

$$+ T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

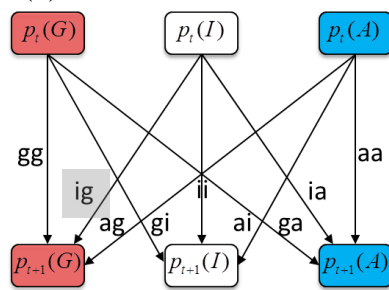
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia$$

$$- aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

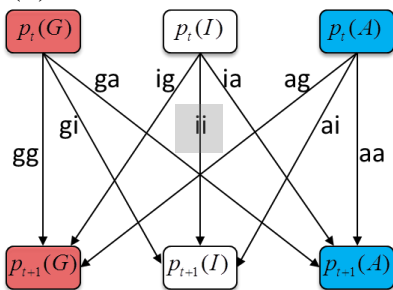
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A) + T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I) + T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

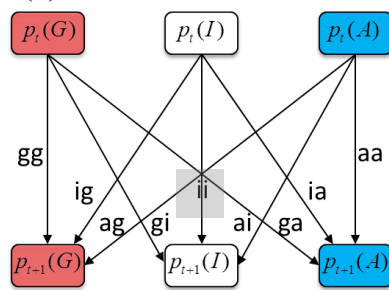
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

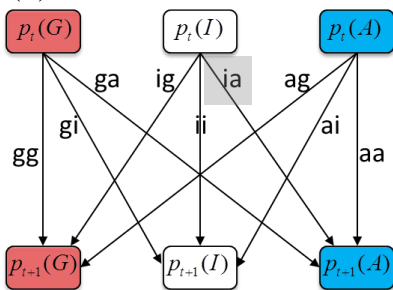
 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga$$

$$+ ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai$$

$$+ ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A)$$

$$+ T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I)$$

$$+ T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

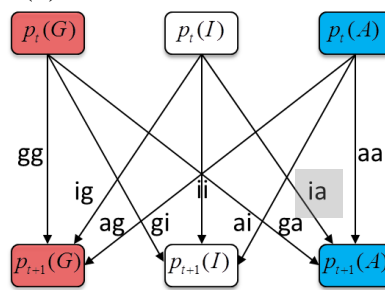
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia$$

$$- aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

$p_t(G)$ = proportion of *Goers*_{*t*} (at time *t*)

$p_t(A)$ – proportion of *Absentees*_{*t*} (at time *t*)

$p_{t+1}(I)$ = proportion of *Irregulars*_{*t+1*}

gg – *Goers*_{*t*} who stay *Goers*_{*t+1*}

gi – *Goers*_{*t*} who become *Irregulars*_{*t+1*}

ga – *Goers*_{*t*} who become *Absentees*_{*t+1*}

ig – *Irregulars*_{*t*} who become *Goers*_{*t+1*}

ii – *Irregulars*_{*t*} who stay *Irregulars*_{*t+1*}

ia – *Irregulars*_{*t*} who become *Absentees*_{*t+1*}

ag – *Absentees*_{*t*} who become *Goers*_{*t+1*}

ai – *Absentees*_{*t*} who become *Irregulars*_{*t+1*}

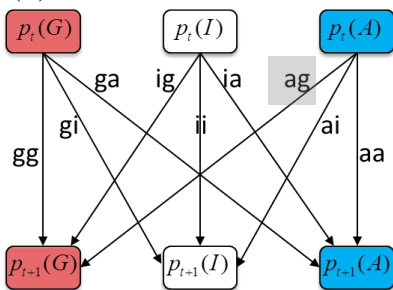
aa – *Absentees*_{*t*} who stay *Absentees*_{*t+1*}

gg *gi* *ga*

ig *ii* *ia*

ag *ai* *aa*

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga$$

$$+ ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai$$

$$+ ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A)$$

$$+ T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I)$$

$$+ T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

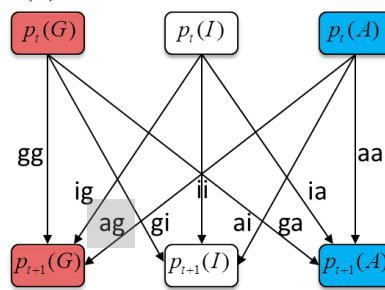
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia$$

$$- aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

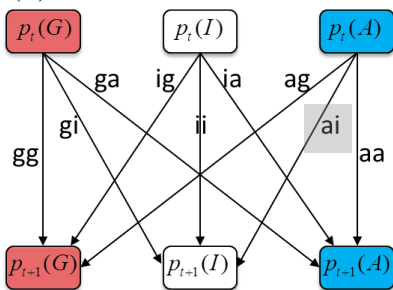
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga \\ + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai \\ + ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A) \\ + T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I) \\ + T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

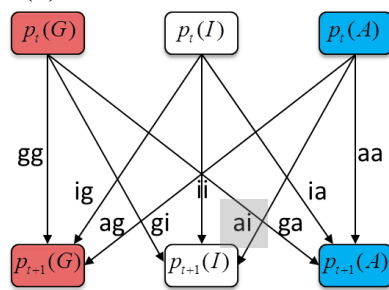
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia \\ - aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

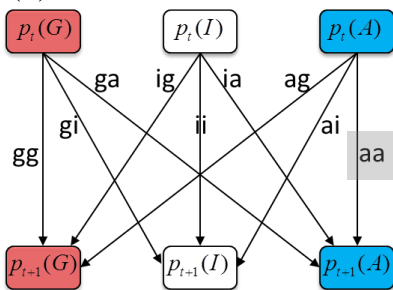
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga$$

$$+ ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai$$

$$+ ga + ia$$

(g) Counting with Contagion

$$p_{t+1}(G) = p_t(G) - T_{gi} p_t(G) p_t(I) - T_{ga} p_t(G) p_t(A)$$

$$+ T_{ig} p_t(I) p_t(G) + T_{ag} p_t(A) p_t(G)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(G) - T_{ai} p_t(A) p_t(I)$$

$$+ T_{ga} p_t(G) p_t(A) + T_{ia} p_t(I) p_t(A)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

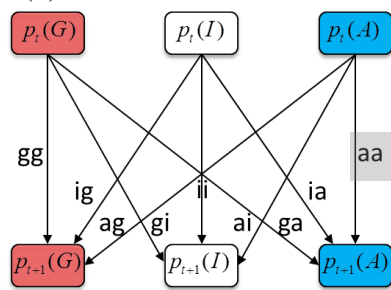
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia$$

$$- aa - ig - ag - ai$$

(h) Contagion predicts transitions:

$$gi = T_{gi} p_t(G) p_t(I)$$

$$ga = T_{ga} p_t(G) p_t(A)$$

$$ig = T_{ig} p_t(I) p_t(G)$$

$$ia = T_{ia} p_t(I) p_t(A)$$

$$ag = T_{ag} p_t(A) p_t(G)$$

$$ai = T_{ai} p_t(A) p_t(I)$$

$p_t(G)$ = proportion of *Goers*_{*t*} (at time *t*)

$p_t(A)$ – proportion of *Absentees*_{*t*} (at time *t*)

$p_{t+1}(I)$ = proportion of *Irregulars*_{*t+1*}

gg – *Goers*_{*t*} who stay *Goers*_{*t+1*}

gi – *Goers*_{*t*} who become *Irregulars*_{*t+1*}

ga – *Goers*_{*t*} who become *Absentees*_{*t+1*}

ig – *Irregulars*_{*t*} who become *Goers*_{*t+1*}

ii – *Irregulars*_{*t*} who stay *Irregulars*_{*t+1*}

ia – *Irregulars*_{*t*} who become *Absentees*_{*t+1*}

ag – *Absentees*_{*t*} who become *Goers*_{*t+1*}

ai – *Absentees*_{*t*} who become *Irregulars*_{*t+1*}

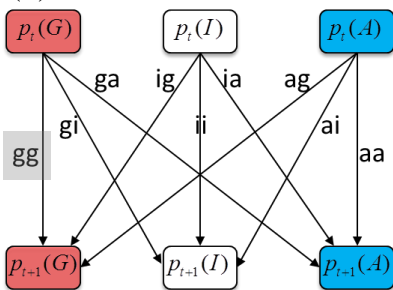
aa – *Absentees*_{*t*} who stay *Absentees*_{*t+1*}

gg *gi* *ga*

ig *ii* *ia*

ag *ai* *aa*

(a) Those who leave



(e) Counting transitions

$$\begin{aligned}
 p_{t+1}(G) &= p_t(G) - gi - ga \\
 &\quad + ig + ag \\
 p_{t+1}(I) &= 1 - p_{t+1}(G) - p_{t+1}(A) \\
 p_{t+1}(A) &= p_t(A) - ag - ai \\
 &\quad + ga + ia
 \end{aligned}$$

(g) Counting with Resilience

$$\begin{aligned}
 p_{t+1}(G) &= p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) \\
 &\quad + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A) \\
 p_{t+1}(I) &= 1 - p_{t+1}(G) - p_{t+1}(A) \\
 p_{t+1}(A) &= p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) \\
 &\quad + k_{ga} p_t(G) + k_{ia} p_t(I)
 \end{aligned}$$

(c) This year

$$\begin{aligned}
 p_t(G) &= gg + gi + ga \\
 p_t(I) &= ig + ii + ia \\
 p_t(A) &= ag + ai + aa
 \end{aligned}$$

(d) Next year

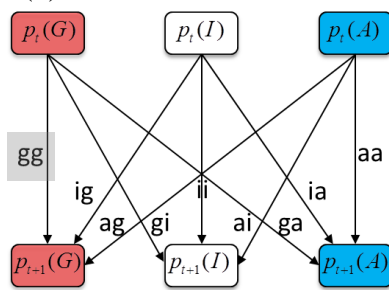
$$\begin{aligned}
 p_{t+1}(G) &= gg + ig + ag \\
 p_{t+1}(I) &= ii + gi + ai \\
 p_{t+1}(A) &= aa + ga + ia
 \end{aligned}$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$\begin{aligned}
 gg &= (p_t(G) - gi - ga) \\
 aa &= (p_t(A) - ag - ai) \\
 ii &= 1 - gg - gi - ga - ia \\
 &\quad - aa - ig - ag - ai
 \end{aligned}$$

(h) Resilience predicts transitions:

$$\begin{aligned}
 gi &= k_{gi} p_t(G) \\
 ga &= k_{ga} p_t(G) \\
 ig &= T_{ig} p_t(I) p_t(I) \\
 ia &= k_{ia} p_t(I) \\
 ag &= T_{ag} p_t(A) p_t(A) \\
 ai &= T_{ai} p_t(A) p_t(A)
 \end{aligned}$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

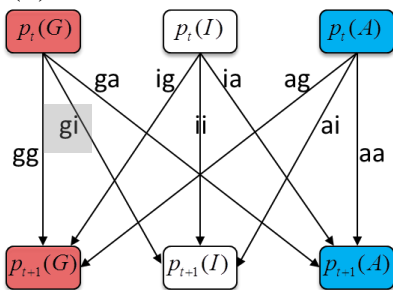
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - \text{gi} - \text{ga} + \text{ig} + \text{ag}$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - \text{ag} - \text{ai} + \text{ga} + \text{ia}$$

(g) Counting with Resilience

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = \text{gg} + \text{gi} + \text{ga}$$

$$p_t(I) = \text{ig} + \text{ii} + \text{ia}$$

$$p_t(A) = \text{ag} + \text{ai} + \text{aa}$$

(d) Next year

$$p_{t+1}(G) = \text{gg} + \text{ig} + \text{ag}$$

$$p_{t+1}(I) = \text{ii} + \text{gi} + \text{ai}$$

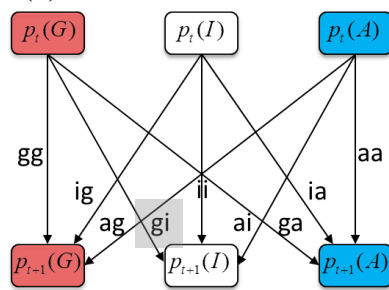
$$p_{t+1}(A) = \text{aa} + \text{ga} + \text{ia}$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$\text{gg} = (p_t(G) - \text{gi} - \text{ga})$$

$$\text{aa} = (p_t(A) - \text{ag} - \text{ai})$$

$$\text{ii} = 1 - \text{gg} - \text{gi} - \text{ga} - \text{ia} - \text{aa} - \text{ig} - \text{ag} - \text{ai}$$

(h) Resilience predicts transitions:

$$\text{gi} = k_{gi} p_t(G)$$

$$\text{ga} = k_{ga} p_t(G)$$

$$\text{ig} = T_{ig} p_t(I) p_t(I)$$

$$\text{ia} = k_{ia} p_t(I)$$

$$\text{ag} = T_{ag} p_t(A) p_t(A)$$

$$\text{ai} = T_{ai} p_t(A) p_t(A)$$

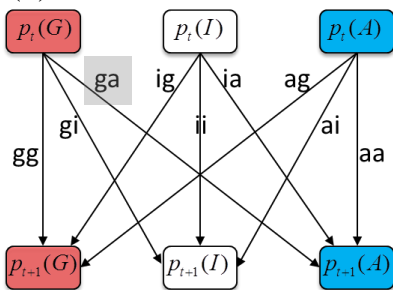
 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Resilience

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

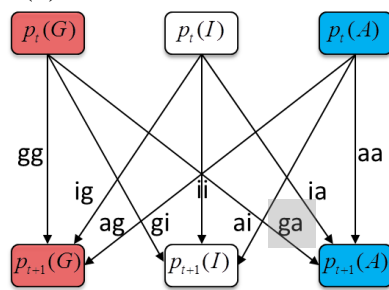
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Resilience predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = T_{ig} p_t(I) p_t(I)$$

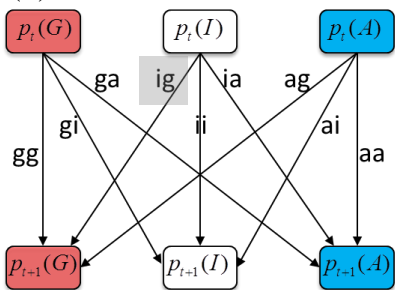
$$ia = k_{ia} p_t(I)$$

$$ag = T_{ag} p_t(A) p_t(A)$$

$$ai = T_{ai} p_t(A) p_t(A)$$

 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}* gg gi ga ig ii ia ag ai aa

(a) Those who leave



(e) Counting transitions

$$\begin{aligned}
 p_{t+1}(G) &= p_t(G) - gi - ga \\
 &\quad + ig + ag \\
 p_{t+1}(I) &= 1 - p_{t+1}(G) - p_{t+1}(A) \\
 p_{t+1}(A) &= p_t(A) - ag - ai \\
 &\quad + ga + ia
 \end{aligned}$$

(g) Counting with Resilience

$$\begin{aligned}
 p_{t+1}(G) &= p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) \\
 &\quad + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A) \\
 p_{t+1}(I) &= 1 - p_{t+1}(G) - p_{t+1}(A) \\
 p_{t+1}(A) &= p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) \\
 &\quad + k_{ga} p_t(G) + k_{ia} p_t(I)
 \end{aligned}$$

(c) This year

$$\begin{aligned}
 p_t(G) &= gg + gi + ga \\
 p_t(I) &= ig + ii + ia \\
 p_t(A) &= ag + ai + aa
 \end{aligned}$$

(d) Next year

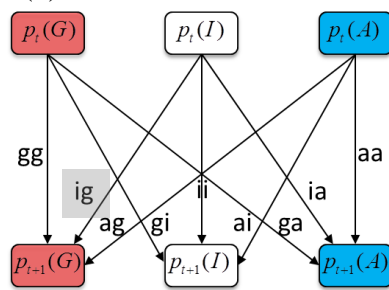
$$\begin{aligned}
 p_{t+1}(G) &= gg + ig + ag \\
 p_{t+1}(I) &= ii + gi + ai \\
 p_{t+1}(A) &= aa + ga + ia
 \end{aligned}$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$\begin{aligned}
 gg &= (p_t(G) - gi - ga) \\
 aa &= (p_t(A) - ag - ai) \\
 ii &= 1 - gg - gi - ga - ia \\
 &\quad - aa - ig - ag - ai
 \end{aligned}$$

(h) Resilience predicts transitions:

$$\begin{aligned}
 gi &= k_{gi} p_t(G) \\
 ga &= k_{ga} p_t(G) \\
 ig &= T_{ig} p_t(I) p_t(I) \\
 ia &= k_{ia} p_t(I) \\
 ag &= T_{ag} p_t(A) p_t(A) \\
 ai &= T_{ai} p_t(A) p_t(A)
 \end{aligned}$$

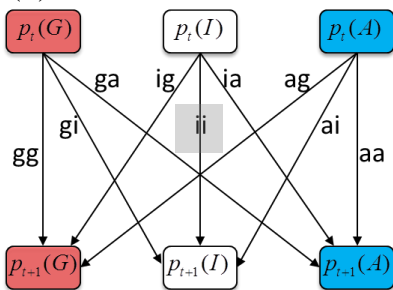
 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga$$

$$+ ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai$$

$$+ ga + ia$$

(g) Counting with Resilience

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) \\ + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) \\ + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

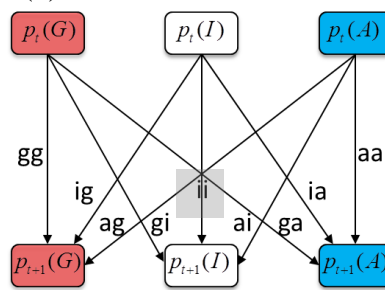
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia \\ - aa - ig - ag - ai$$

(h) Resilience predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = T_{ig} p_t(I) p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = T_{ag} p_t(A) p_t(A)$$

$$ai = T_{ai} p_t(A) p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

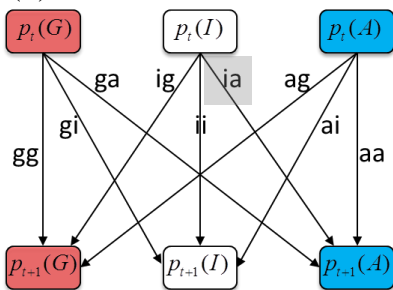
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Resilience

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

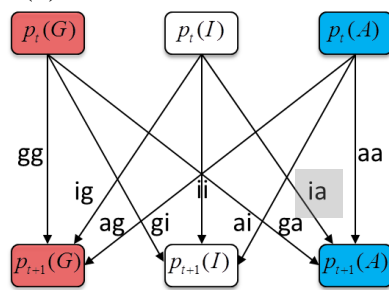
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Resilience predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = T_{ig} p_t(I) p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = T_{ag} p_t(A) p_t(A)$$

$$ai = T_{ai} p_t(A) p_t(A)$$

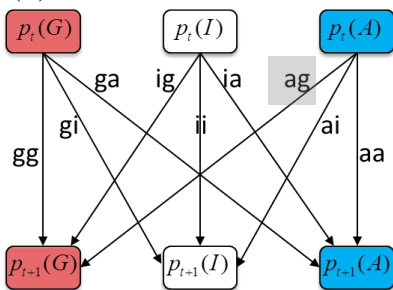
 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Resilience

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

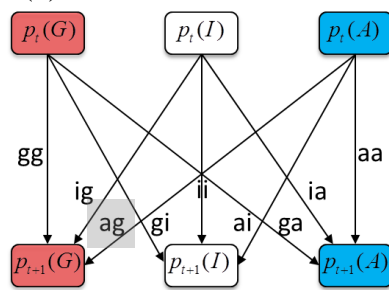
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Resilience predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = T_{ig} p_t(I) p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = T_{ag} p_t(A) p_t(A)$$

$$ai = T_{ai} p_t(A) p_t(A)$$

$p_t(G)$ = proportion of *Goers_t* (at time t)

$p_t(A)$ – proportion of *Absentees_t* (at time t)

$p_{t+1}(I)$ = proportion of *Irregulars_{t+1}*

gg – *Goers_t* who stay *Goers_{t+1}*

gi – *Goers_t* who become *Irregulars_{t+1}*

ga – *Goers_t* who become *Absentees_{t+1}*

ig – *Irregulars_t* who become *Goers_{t+1}*

ii – *Irregulars_t* who stay *Irregulars_{t+1}*

ia – *Irregulars_t* who become *Absentees_{t+1}*

ag – *Absentees_t* who become *Goers_{t+1}*

ai – *Absentees_t* who become *Irregulars_{t+1}*

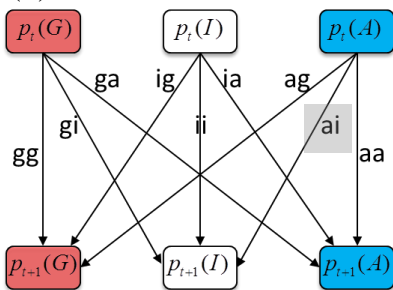
aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$\begin{aligned}
 p_{t+1}(G) &= p_t(G) - gi - ga \\
 &\quad + ig + ag \\
 p_{t+1}(I) &= 1 - p_{t+1}(G) - p_{t+1}(A) \\
 p_{t+1}(A) &= p_t(A) - ag - ai \\
 &\quad + ga + ia
 \end{aligned}$$

(g) Counting with Resilience

$$\begin{aligned}
 p_{t+1}(G) &= p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) \\
 &\quad + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A) \\
 p_{t+1}(I) &= 1 - p_{t+1}(G) - p_{t+1}(A) \\
 p_{t+1}(A) &= p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) \\
 &\quad + k_{ga} p_t(G) + k_{ia} p_t(I)
 \end{aligned}$$

(c) This year

$$\begin{aligned}
 p_t(G) &= gg + gi + ga \\
 p_t(I) &= ig + ii + ia \\
 p_t(A) &= ag + ai + aa
 \end{aligned}$$

(d) Next year

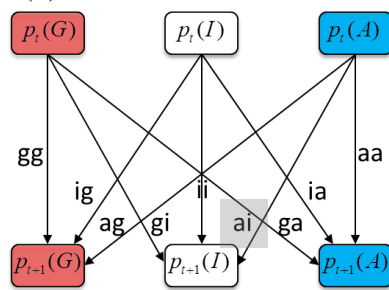
$$\begin{aligned}
 p_{t+1}(G) &= gg + ig + ag \\
 p_{t+1}(I) &= ii + gi + ai \\
 p_{t+1}(A) &= aa + ga + ia
 \end{aligned}$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$\begin{aligned}
 gg &= (p_t(G) - gi - ga) \\
 aa &= (p_t(A) - ag - ai) \\
 ii &= 1 - gg - gi - ga - ia \\
 &\quad - aa - ig - ag - ai
 \end{aligned}$$

(h) Resilience predicts transitions:

$$\begin{aligned}
 gi &= k_{gi} p_t(G) \\
 ga &= k_{ga} p_t(G) \\
 ig &= T_{ig} p_t(I) p_t(I) \\
 ia &= k_{ia} p_t(I) \\
 ag &= T_{ag} p_t(A) p_t(A) \\
 ai &= T_{ai} p_t(A) p_t(A)
 \end{aligned}$$

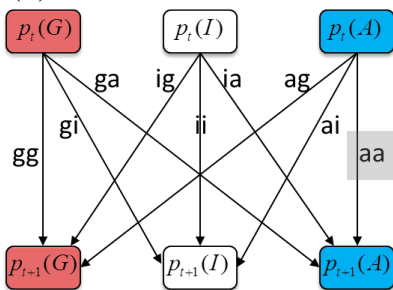
 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa

(a) Those who leave



(e) Counting transitions

$$p_{t+1}(G) = p_t(G) - gi - ga + ig + ag$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - ag - ai + ga + ia$$

(g) Counting with Resilience

$$p_{t+1}(G) = p_t(G) - k_{gi} p_t(G) - k_{ga} p_t(G) + T_{ig} p_t(I) p_t(I) + T_{ag} p_t(A) p_t(A)$$

$$p_{t+1}(I) = 1 - p_{t+1}(G) - p_{t+1}(A)$$

$$p_{t+1}(A) = p_t(A) - T_{ag} p_t(A) p_t(A) - T_{ai} p_t(A) p_t(A) + k_{ga} p_t(G) + k_{ia} p_t(I)$$

(c) This year

$$p_t(G) = gg + gi + ga$$

$$p_t(I) = ig + ii + ia$$

$$p_t(A) = ag + ai + aa$$

(d) Next year

$$p_{t+1}(G) = gg + ig + ag$$

$$p_{t+1}(I) = ii + gi + ai$$

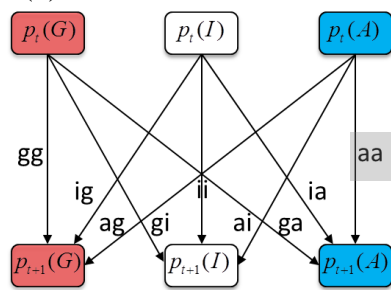
$$p_{t+1}(A) = aa + ga + ia$$

Diffusion

Contagion

Hybrid

(b) Those who come



(f) Redundancy/Constraints

$$gg = (p_t(G) - gi - ga)$$

$$aa = (p_t(A) - ag - ai)$$

$$ii = 1 - gg - gi - ga - ia - aa - ig - ag - ai$$

(h) Resilience predicts transitions:

$$gi = k_{gi} p_t(G)$$

$$ga = k_{ga} p_t(G)$$

$$ig = T_{ig} p_t(I) p_t(I)$$

$$ia = k_{ia} p_t(I)$$

$$ag = T_{ag} p_t(A) p_t(A)$$

$$ai = T_{ai} p_t(A) p_t(A)$$

 $p_t(G)$ = proportion of *Goers_t* (at time t) $p_t(A)$ – proportion of *Absentees_t* (at time t) $p_{t+1}(I)$ = proportion of *Irregulars_{t+1}* gg – *Goers_t* who stay *Goers_{t+1}* gi – *Goers_t* who become *Irregulars_{t+1}* ga – *Goers_t* who become *Absentees_{t+1}* ig – *Irregulars_t* who become *Goers_{t+1}* ii – *Irregulars_t* who stay *Irregulars_{t+1}* ia – *Irregulars_t* who become *Absentees_{t+1}* ag – *Absentees_t* who become *Goers_{t+1}* ai – *Absentees_t* who become *Irregulars_{t+1}* aa – *Absentees_t* who stay *Absentees_{t+1}*

gg gi ga

ig ii ia

ag ai aa