Metrics

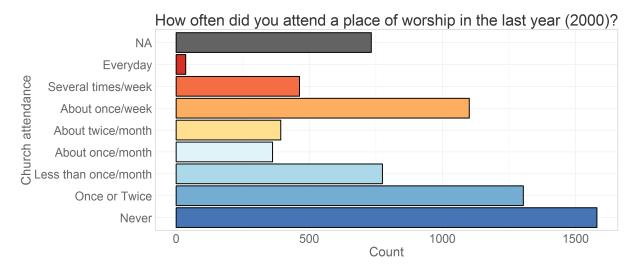
Andriy Koval Tuesday, June 24, 2014

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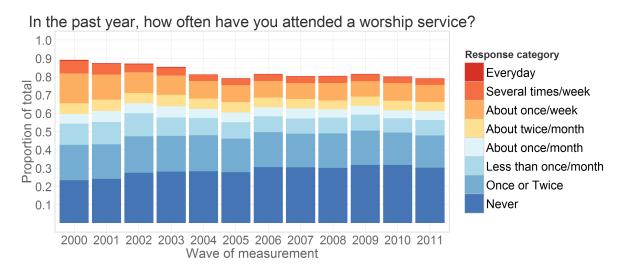
Mapping Church Attendance in Time

Cross-Sectional View

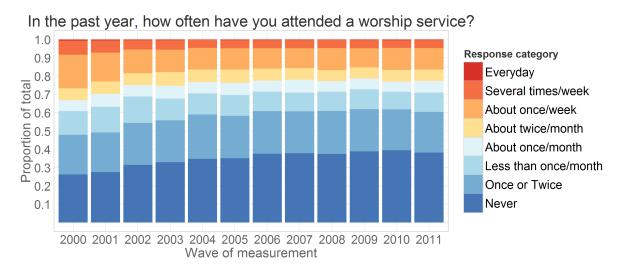
The focal variable of interest is **attend**, an item measuring church attendance in the current year. The questionnaire recorded the responses on the ordinal scale.



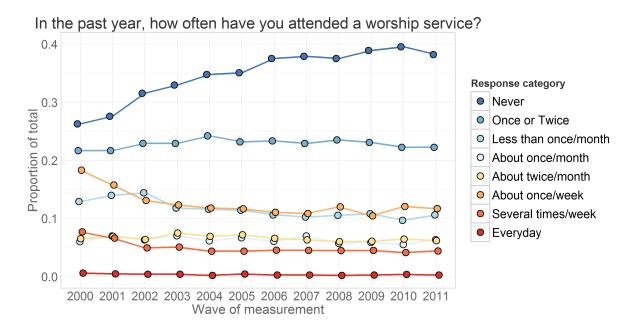
Creating frequency distributions for each of the measurement wave we have:



Missing values are used in the calculation of total responses to show the natural attrition in the study. Assumming that attrition is not significantly associated with the outcome measure, we can remove missing values from the calculation of the total and look at prevalence of endorsements over time.



Tracing the rate of change of prevalence in a line graph, we see more clearly which categores increase over time (e.g. "Never"), which decline (e.g. "About once/week), and which stay relatively stable (e.g. "About twice/month")



Longitudinal View

Graphs above shows change in the cross-sectional distribution of responses over the years. Modeling the change in these response frequencies is handled well by Markov models. LCM, however, works with longitudinal data, modeling the trajectory of each individual and treating attendance as a continuous outcome.

To demonstrate mapping of individual trajectories to time, let's select a dataset that would include personal identifyer (id), cohort indicator (byear), wave of measurement (year) and the focal variable of interest - worship attendance (attend).

| attendF | attend | year | byear | id | |
|----------------------|--------|------|-------|----|----|
| About twice/month | 5 | 2000 | 1982 | 47 | 1 |
| Once or Twice | 2 | 2001 | 1982 | 47 | 2 |
| About once/month | 4 | 2002 | 1982 | 47 | 3 |
| Once or Twice | 2 | 2003 | 1982 | 47 | 4 |
| Less than once/month | 3 | 2004 | 1982 | 47 | 5 |
| Once or Twice | 2 | 2005 | 1982 | 47 | 6 |
| Once or Twice | 2 | 2006 | 1982 | 47 | 7 |
| Less than once/month | 3 | 2007 | 1982 | 47 | 8 |
| Once or Twice | 2 | 2008 | 1982 | 47 | 9 |
| Never | 1 | 2009 | 1982 | 47 | 10 |
| Never | 1 | 2010 | 1982 | 47 | 11 |
| Never | 1 | 2011 | 1982 | 47 | 12 |
| | | | | | |

The view above lists attendance data for subjust with id = 47. Mapping his attendance to time we have



where vertical dimension maps the outcome value and the horizontal maps the time. There will be a trajecory for each of the

```
length(unique(dsL$id))
```

[1] 8983

subjects in total. Unless specified otherwise, only individuals from the cross-sample will be used in the model to increase external validity.

```
ds<- dsL %>% dplyr::filter(sample==1)
```

Each of such trajectories imply a story, a life scenario. Why one person grows in his religious involvement, while other declines, or never develops an interest in the first place? To demostrate how interpretations of trajectories can vary among individuals consider the following scenario.

Attendance trajectories of subjects with ids 4, 25, 35, and 47 are plotted in the next graph



The respondent **id**=35 reported attending no worship services in any of the years, while respodent **id**=25 seemed to frequent it, indicating weekly attendance in 8 out of the 12 years. Individual **id**=47 started as a fairly regular attendee of religious services in 2000 (5= "about twice a month"), then gradually declined his involvement to nill in 2009 and on. Respondent **id**=4, on the other hand started off with a rather passive involvement, reporting attended church only "Once or twice" in 2000, maintained a low level of participation throughout the years, only to surge his attendance in 2011. Latent curve models will describe intraindividual trajectories of change, while summarizing the interindividual similarities and trends.

Previous research in religiousity indicated that age might be one of the primary factors explaining interindividual differences in church attendance. To examine the role of age, we change the metric of time from waves of measurement, as in the previous graph, to biological age. There are, however, a number of ways information about age was recorded.

```
ds<- dsL %>% dplyr::filter(id %in% c(4,25,35,47),year %in% c(2000:2011)) %>%
    dplyr::select(idF,attend, year, byear, ageyear, agemon, ageyear) %>%
    mutate(time=year-2000, age=(year-byear+1), ageCurrent = agemon/12)
print(ds[ds$idF==25,])
```

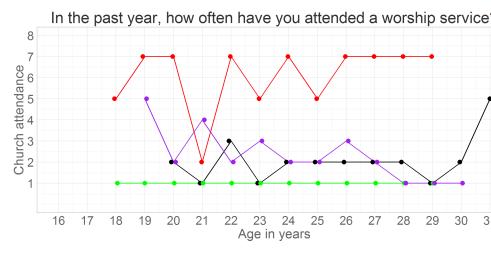
```
idF attend year byear ageyear agemon time age ageCurrent
13
    25
             5 2000
                      1983
                                 17
                                       214
                                               0
                                                   18
                                                            17.83
    25
             7 2001
                      1983
                                        226
                                                   19
                                                            18.83
14
                                 18
                                               1
15
    25
             7 2002
                      1983
                                 19
                                       236
                                               2
                                                   20
                                                            19.67
             2 2003
                                               3
16
    25
                      1983
                                 21
                                       254
                                                   21
                                                            21.17
17
    25
             7 2004
                      1983
                                 21
                                       261
                                               4
                                                   22
                                                            21.75
18
    25
             5 2005
                      1983
                                 22
                                        272
                                               5
                                                   23
                                                            22.67
19
    25
             7 2006
                      1983
                                 23
                                       284
                                               6
                                                   24
                                                            23.67
                                               7
                                                   25
20
    25
             5 2007
                      1983
                                 24
                                        295
                                                            24.58
    25
             7 2008
                                 25
                                        307
                                                   26
                                                            25.58
21
                      1983
                                               8
22
    25
             7 2009
                      1983
                                 26
                                        319
                                               9
                                                   27
                                                            26.58
23
    25
             7 2010
                      1983
                                 27
                                        332
                                              10
                                                   28
                                                            27.67
24
    25
             7 2011
                                 28
                                                   29
                                                            28.50
                      1983
                                        342
                                               11
```

ds

| | idF | ${\tt attend}$ | year | byear | ageyear | agemon | time | age | ageCurrent |
|---|-----|----------------|------|-------|---------|--------|------|-----|------------|
| 1 | 4 | 2 | 2000 | 1981 | 19 | 238 | 0 | 20 | 19.83 |
| 2 | 4 | 1 | 2001 | 1981 | 20 | 251 | 1 | 21 | 20.92 |
| 3 | 4 | 3 | 2002 | 1981 | 21 | 262 | 2 | 22 | 21.83 |
| 4 | 4 | 1 | 2003 | 1981 | 22 | 276 | 3 | 23 | 23.00 |

| 5 | 4 | 2 | 2004 | 1981 | 23 | 287 | 4 | 24 | 23.92 |
|----|----|---|------|------|----|-----|----|----|-------|
| 6 | 4 | 2 | 2005 | 1981 | 24 | 297 | 5 | 25 | 24.75 |
| 7 | 4 | 2 | 2006 | 1981 | 25 | 309 | 6 | 26 | 25.75 |
| 8 | 4 | 2 | 2007 | 1981 | 26 | 320 | 7 | 27 | 26.67 |
| 9 | 4 | 2 | 2008 | 1981 | 27 | 336 | 8 | 28 | 28.00 |
| 10 | 4 | 1 | 2009 | 1981 | 28 | 344 | 9 | 29 | 28.67 |
| 11 | 4 | 2 | 2010 | 1981 | 29 | 357 | 10 | 30 | 29.75 |
| 12 | 4 | 5 | 2011 | 1981 | 30 | 368 | 11 | 31 | 30.67 |
| 13 | 25 | 5 | 2000 | 1983 | 17 | 214 | 0 | 18 | 17.83 |
| 14 | 25 | 7 | 2001 | 1983 | 18 | 226 | 1 | 19 | 18.83 |
| 15 | 25 | 7 | 2002 | 1983 | 19 | 236 | 2 | 20 | 19.67 |
| 16 | 25 | 2 | 2003 | 1983 | 21 | 254 | 3 | 21 | 21.17 |
| 17 | 25 | 7 | 2004 | 1983 | 21 | 261 | 4 | 22 | 21.75 |
| 18 | 25 | 5 | 2005 | 1983 | 22 | 272 | 5 | 23 | 22.67 |
| 19 | 25 | 7 | 2006 | 1983 | 23 | 284 | 6 | 24 | 23.67 |
| 20 | 25 | 5 | 2007 | 1983 | 24 | 295 | 7 | 25 | 24.58 |
| 21 | 25 | 7 | 2008 | 1983 | 25 | 307 | 8 | 26 | 25.58 |
| 22 | 25 | 7 | 2009 | 1983 | 26 | 319 | 9 | 27 | 26.58 |
| 23 | 25 | 7 | 2010 | 1983 | 27 | 332 | 10 | 28 | 27.67 |
| 24 | 25 | 7 | 2011 | 1983 | 28 | 342 | 11 | 29 | 28.50 |
| 25 | 35 | 1 | 2000 | 1983 | 17 | 216 | 0 | 18 | 18.00 |
| 26 | 35 | 1 | 2001 | 1983 | 18 | 227 | 1 | 19 | 18.92 |
| 27 | 35 | 1 | 2002 | 1983 | 19 | 239 | 2 | 20 | 19.92 |
| 28 | 35 | 1 | 2003 | 1983 | 20 | 250 | 3 | 21 | 20.83 |
| 29 | 35 | 1 | 2004 | 1983 | 21 | 264 | 4 | 22 | 22.00 |
| 30 | 35 | 1 | 2005 | 1983 | 22 | 274 | 5 | 23 | 22.83 |
| 31 | 35 | 1 | 2006 | 1983 | 23 | 286 | 6 | 24 | 23.83 |
| 32 | 35 | 1 | 2007 | 1983 | 24 | 297 | 7 | 25 | 24.75 |
| 33 | 35 | 1 | 2008 | 1983 | 25 | 310 | 8 | 26 | 25.83 |
| 34 | 35 | 1 | 2009 | 1983 | 26 | 320 | 9 | 27 | 26.67 |
| 35 | 35 | 1 | 2010 | 1983 | 27 | 334 | 10 | 28 | 27.83 |
| 36 | 35 | 1 | 2011 | 1983 | 28 | 345 | 11 | 29 | 28.75 |
| 37 | 47 | 5 | 2000 | 1982 | 18 | 220 | 0 | 19 | 18.33 |
| 38 | 47 | 2 | 2001 | 1982 | 19 | 233 | 1 | 20 | 19.42 |
| 39 | 47 | 4 | 2002 | 1982 | 20 | 243 | 2 | 21 | 20.25 |
| 40 | 47 | 2 | 2003 | 1982 | 21 | 257 | 3 | 22 | 21.42 |
| 41 | 47 | 3 | 2004 | 1982 | 22 | 266 | 4 | 23 | 22.17 |
| 42 | 47 | 2 | 2005 | 1982 | 23 | 280 | 5 | 24 | 23.33 |
| 43 | 47 | 2 | 2006 | 1982 | 24 | 292 | 6 | 25 | 24.33 |
| 44 | 47 | 3 | 2007 | 1982 | 25 | 302 | 7 | 26 | 25.17 |
| 45 | 47 | 2 | 2008 | 1982 | 26 | 315 | 8 | 27 | 26.25 |
| 46 | 47 | 1 | 2009 | 1982 | 27 | 326 | 9 | 28 | 27.17 |
| 47 | 47 | | 2010 | 1982 | 28 | | 10 | 29 | 28.25 |
| 48 | 47 | 1 | 2011 | 1982 | 29 | 351 | 11 | 30 | 29.25 |

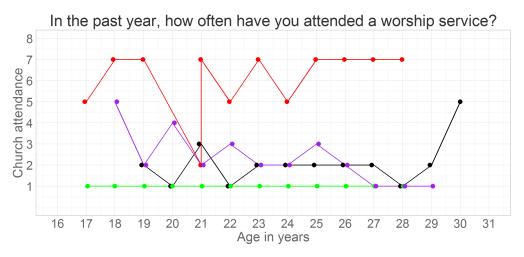
Note that for person **id** = 25 the age was recorded as 21 years for both 2003 and 2004. However, when you examine age in months (**agemon**) you can see this is rounding issue that disappears once a more precise scale is used. To avoid this potentially confusing peculiarity, age in years will be either calculated as (**age** = **year** - **byear** + 1)



Plotting age, caclulated as age = year - byear + 1

```
ds<- dsL %>% dplyr::filter(id %in% c(4,25,35,47),year %in% c(2000:2011)) %>%
    dplyr::select(idF,year,attend,agemon,ageyear) %>%
    mutate(time=year-2000, age=ageyear)
head(ds,12)
```

| | idF | year | attend | agemon | ageyear | time | age |
|----|-----|------|--------|--------|---------|------|-----|
| 1 | 4 | 2000 | 2 | 238 | 19 | 0 | 19 |
| 2 | 4 | 2001 | 1 | 251 | 20 | 1 | 20 |
| 3 | 4 | 2002 | 3 | 262 | 21 | 2 | 21 |
| 4 | 4 | 2003 | 1 | 276 | 22 | 3 | 22 |
| 5 | 4 | 2004 | 2 | 287 | 23 | 4 | 23 |
| 6 | 4 | 2005 | 2 | 297 | 24 | 5 | 24 |
| 7 | 4 | 2006 | 2 | 309 | 25 | 6 | 25 |
| 8 | 4 | 2007 | 2 | 320 | 26 | 7 | 26 |
| 9 | 4 | 2008 | 2 | 336 | 27 | 8 | 27 |
| 10 | 4 | 2009 | 1 | 344 | 28 | 9 | 28 |
| 11 | 4 | 2010 | 2 | 357 | 29 | 10 | 29 |
| 12 | 4 | 2011 | 5 | 368 | 30 | 11 | 30 |



Plotting age, caclulated as age = ageyear

Plotting age, caclulated as age = agemon/12

```
ds<- dsL %>% dplyr::filter(id %in% c(4,25,35,47),year %in% c(2000:2011)) %>%
    dplyr::select(idF,year,attend,agemon,ageyear,byear) %>%
    mutate(time=year-2000, age=agemon/12)
head(ds,12)
```

| | idF | year | ${\tt attend}$ | agemon | ageyear | byear | time | age |
|----|-----|------|----------------|--------|---------|-------|------|-------|
| 1 | 4 | 2000 | 2 | 238 | 19 | 1981 | 0 | 19.83 |
| 2 | 4 | 2001 | 1 | 251 | 20 | 1981 | 1 | 20.92 |
| 3 | 4 | 2002 | 3 | 262 | 21 | 1981 | 2 | 21.83 |
| 4 | 4 | 2003 | 1 | 276 | 22 | 1981 | 3 | 23.00 |
| 5 | 4 | 2004 | 2 | 287 | 23 | 1981 | 4 | 23.92 |
| 6 | 4 | 2005 | 2 | 297 | 24 | 1981 | 5 | 24.75 |
| 7 | 4 | 2006 | 2 | 309 | 25 | 1981 | 6 | 25.75 |
| 8 | 4 | 2007 | 2 | 320 | 26 | 1981 | 7 | 26.67 |
| 9 | 4 | 2008 | 2 | 336 | 27 | 1981 | 8 | 28.00 |
| 10 | 4 | 2009 | 1 | 344 | 28 | 1981 | 9 | 28.67 |
| 11 | 4 | 2010 | 2 | 357 | 29 | 1981 | 10 | 29.75 |
| 12 | 4 | 2011 | 5 | 368 | 30 | 1981 | 11 | 30.67 |

