A common solution to R_D anomalies and Dark Matter

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Abstract

The anomalies observed by LHCb in flavor observables suggest the breakdown of lepton flavor universality. We study how a vanilla leptoquark solution to the $R_{D^{(*)}}$ anomalies can also explain the measured relic abundance, if the leptoquark mediates between the visible sector and the dark sector. We find that [something awesome].

1. INTRODUCTION

The current LHC dataset has not shown any significant deviation from the SM expectations, except for the $R_{K^{(*)}}$ [1, 2] and $R_{D^{(*)}}$ [3, 4, 5] anomalies. While many models have been considered to explain these observations, the consensus is that two classes of models can accommodate these results: leptoquarks and Z' models (for a recent review see e.g [6] and references therein). It is thus interesting to consider the interplay between these solutions and dark matter (DM), which essentially requires to add an additional decay of the leptoquark into the dark sector, studied previously in [7, 8]. As this will reduce the visible decays of the leptoquarks, this naively allows to lower the current expectation of $m_{LQ} \gtrsim 1$ TeV with $\mathcal{O}(1)$ couplings, thus opening up novel parameter space and increasing the opportunities to probe this model at the LHC in the near future.

For our study we built a simplified model featuring the minimal ingredients to explain the charged current flavor anomalies $R_{D^{(*)}}$ and dark matter simultaneously, limiting ourselves to the couplings strictly

necessary to explain the anomaly. We study how the different phenomenological constrains affect the parameter space: LHC searches for leptoquarks and dark matter, relic density and direct detection. We pay particular attention to the existing CMS search for a resonant leptoquark plus mssing energy: while this search might not alway be the golden channel for discovery, its importance lies in the fact that this is indeed probing the $R_{D(*)}$ -DM connection (RDM).

2. THE MODEL

[JZ: Text taken from Benj, except for last paragraph.]

We consider a simplified model in which we supplement the Standard Model by one scalar leptoquark field S_1 and two extra fermionic fields, a Majorana fermion χ_0 and a Dirac fermion χ_1 . The S_1 and χ_1 fields are electrically-charged coloured weak singlets lying in the $(\mathbf{3},\mathbf{1})_{-1/3}$ representation of the Standard Model gauge group. In contrast, χ_0 is a dark matter candidate and therefore a non-coloured electroweak singlet. In our FeynRules implementation, we consider all potential interactions of the new sector with the Standard Model sector, the corresponding Lagrangian being written as

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_{kin} + \left[\lambda_{\mathbf{R}} \ \bar{u}_{R}^{c} \ \ell_{R} \ S_{1}^{\dagger} + \lambda_{\mathbf{L}} \ \bar{Q}_{L}^{c} \cdot L_{L} \ S_{1}^{\dagger} + y_{\chi} \bar{\chi}_{1} \chi_{0} S_{1} + \text{h.c.} \right]. \tag{1}$$

In this expression, all flavour indices are understood for simplicity and the dot stands for the SU(2)-invariant product of two fields lying in its fundamental representation. In addition, $\mathcal{L}_{\mathrm{SM}}$ is the Standard Model Lagrangian and $\mathcal{L}_{\mathrm{kin}}$ contains gauge-invariant kinetic and mass terms for all new fields, the χ_1 state being assumed vector-like. The Q_L and L_L spinors stand for the $SU(2)_L$ doublets of left-handed quarks and leptons respectively, whilst u_R and ℓ_R stand for the $SU(2)_L$ singlets of right-handed down-type quarks and charged leptons, respectively. As can be derived from the omitted flavour structure, the λ_L and λ_R couplings are 3×3 matrices in the flavour space, that are considered real in the following. Moreover, in our conventions, the first index i of any λ_{ij} element refers to the quark generation whilst the second one j refers to the lepton generation.

The field content of the new physics sector of our simplified model is presented in table 1, together with the corresponding representation under the gauge and Poincaré groups, the potential Majorana nature of the different particles, the adopted symbol in the FeynRules implementation and the PDG identifier that has been chosen for each particle. The new physics coupling parameters are collected in table 2, in which we additionally include the name used in the FeynRules model and the Les Houches blocks in which the numerical values of the different parameters can be changed by the user when running tools like MG5_AMC or MICROMEGAS.

Field	Spin	Repr.	Self-conj.	FEYNRULES name	PDG code
S_1	0	$(3,1)_{-1/3}$	no	LQ	42
χ_0	1/2	$({f 1},{f 1})_0$	yes	chi0	5000521
χ_1	1/2	$(3,1)_{-1/3}$	no	chi1	5000522

Table 1: New particles supplementing the Standard Model, given together with the representations under $SU(3)_c \times SU(2)_L \times U(1)_Y$. We additionally indicate whether the particles are Majorana particles, their name in the FEYNRULES implementation and the associated Particle Data Group (PDG) identifier.

Coupling	FEYNRULES name	Les Houches block		
$(\lambda_{\scriptscriptstyle L})_{ij}$	lamL	LQLAML		
$(\lambda_R)_{ij}$	lamR	LQLAMR		
y_χ	уDМ	DMINPUTS		

Table 2: Couplings of the new particles, given together with the associated FEYNRULES symbol and the Les Houches block of the parameter card.

In a nutshell, our model needs three new masses and several new couplings. The R_D anomalies can be solved with only $(\lambda_L)_{33} \equiv \lambda_L^{-1}$ and $(\lambda_R)_{23} \equiv \lambda_R$. Finally, the dark matter phenomenology requires the coupling y_χ . Hence these 6 parameters span our parameter space. In what follows we will study how the flavor anomalies, dark matter phenomenology and collider searches constrain this parameter space, showing the currently allowed parameter space and commenting on the future prospects.

3. LEPTOQUARK SOLUTIONS TO R_D ANOMALIES

As mentioned in the previous chapter, a minimal solution of the R(D) anomalies can be obtained with just a left-handed (33) and a right-handed (32) couplings to S_1 . We note that the 33 coupling is forced to be left-handed due to the presence of the neutrino 2 . The choice of having a right-handed coupling for the 32 interaction is due to the large contributions that a left-handed coupling would generate to the $B \to X_s \nu \nu$ process, which in turn would require the addition of another leptoquark state [10, 11, 12, 13]. We perform a global fit of the model with the two couplings $(\lambda_L)_{33}$ and $(\lambda_R)_{23}$ as free parameters. The relevant observables included in the fit are: R_D , R_D^* , $\text{Br}(B_c \to \tau \nu)$, deviations in the Z couplings to τ_L and τ_R , effective number of neutrinos from Z decays, lepton flavour universality test in τ decays. For more details on this fit see e.g. [11, 12, 9]. A contribution to $D^0 - \bar{D}^0$ mixing is generated at one loop, but it is strongly CKM-suppressed and does not provide a strong constraint. The results of a scan in the two parameters of the model, for $m_{S_1} = 1.5 \text{TeV}$, where all points are within 1σ of the best-fit point, is shown in the plane of the R_D and R_D^* anomalies in the left panel of figure 1. The corresponding preferred region in the two couplings is presented in the right panel of figure 1.

From the figure we can establish two working points. We pick the first one to obtain the lowest possible $BR(S_1 \to c\tau)$, which corresponds to (x,y)=(0.6,0.5). For the second one we do not want to pick extreme values of λ_R , as we could run into the regime of a "fat" leptoquark, namely having a width comparable to its mass. So we restrict ourselves to the best fit point (0.16,2.0) that already gives a negligible branching fraction into the third generation states. We thus use these working points to generate concrete benchmarks by picking two values for the leptoquark mass: $m_{S_1}=500$ GeV and $m_{S_1}=1000$ GeV. We show the corresponding values of the couplings and branching ratios in Table 3, where we have assumed a negligible coupling of S_1 to the dark sector. We note that the solution of the $R_{D^{(*)}}$ anomalies, being an off-shell interference with the SM amplitude, will not be affected by diluting the leptoquark visible decays,

¹As the neutrino flavor is not tagged, in principle the second index is not constrained. For simplicity we restrict it here to the third generation.

²Alternatively one could consider a right handed by explicitly introducing a right-handed neutrino that could serve as a dark matter candidate, see e.g [9].

³Defining $x = \lambda_L/m_{S_1}$ and $y = \lambda_R/m_{S_1}$ we have that the anomalies would scale with the product xy. Other constraints scale instead like x^2 or y^2 .

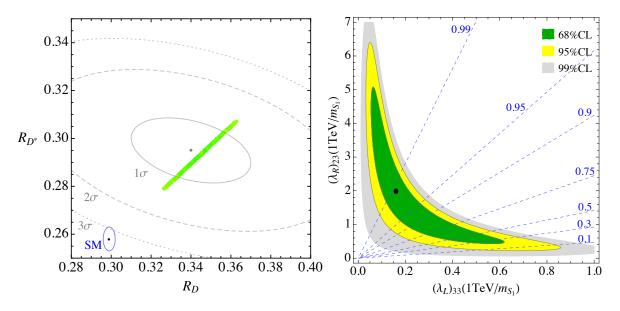


Fig. 1: Left: flavor fit to the charged current anomalies for $m_{S_1}=1.5$ TeV (1σ region). The gray lines represent the present status in the measurements of the two observables, compared with the SM point (blue point and contour). Right: Viable parameter space from the fit of flavor and precision observables as function of λ/m_{S_1} . Blue dashed lines are iso-lines of the branching ratio $B(S_1 \to c_R \tau_R)$ assuming $y_\chi \ll (\lambda_L)_{33}$, $(\lambda_R)_{23}$ and $m_{S_1} \gg m_t$. The black dot represents the best-fit point.

m_{S_1} [GeV]	λ_L	λ_R	$BR(S_1 \to b\nu)$	$BR(S_1 \to t\tau)$	$BR(S_1 \to c\tau)$	$\Gamma(S_1)/m_{S_1}$
500	0.30	0.25	0.4049	0.3139	0.2812	4.42E-3
1000	0.6	0.5	0.3794	0.3571	0.2635	1.89E-2
500	0.08	1.0	0.0063	0.0049	0.9887	3.4E-2
1000	0.16	2.0	0.0063	0.0059	0.9877	8.06E-2

Table 3: Benchmark points compatible with the flavour anomalies. Here we have assumed negligible decays into the dark sector. Note the wide range of possibilities for the $c-\tau$ channel (from 25 % to roughly 100%) while the b and top decays have an upper bound of about 40 and 30 % respectively, and can actually become at the sub-percent level.

but it would rather loose the constraints coming from direct searches of S_1 , which we discuss in detail in Section 5..

Having established the parameter space in the λ_L, λ_R and m_{S_1} we will focus in the next section on the constraints given by dark matter observables: relic density, direct detection and indirect detection.

4. DARK MATTER CONSTRAINTS

In this section we study how the measured relic density and the null results of direct detection impact on our model. We start by noting that the direct detection rate is suppressed at 1-loop [JZ: draw box diagrams], however given the current σ_{SI} exclusions this suppression might not be enough to discard this observable. For the relic density we consider two distinct scenarios. On one hand we study the (co)-annihilation case, as done in [8], while on the other hand we also consider the conversion-driven freeze-out (CDFO) scenario [14], also known as co-scattering [15]. The main idea behind this mechanism is that the self-annihilation of the dark matter candidate is negligible: the dark matter abundance arises instead from conversion processes

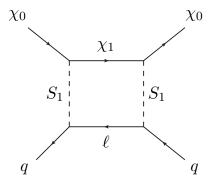


Fig. 2: Feynman diagram for the direct detection of dark matter in our model at the lowest order in perturbation theory.

within the dark sector. Hence, this scenario requires small/tiny interactions between the SM and the DM candidate $(y_{DM}$ in our case), thus rendering the $BR(S_1 \to \chi_1 \chi_0)$ negligible. This will thus affect the relevance of the collider signatures, that are discussed in detail in section 5.

4.1 Direct Detection

The scattering of χ_0 on a nucleon proceeds via a 1-loop diagram, which we show in figure 2. The loop include two leptoquark masses and the χ_1 mass, which are already heavy enough compared with the typical momentum transfer, so that would naively induce a mass suppression. [JZ: What follows is highly speculative] We can obtain a rough estimate of the size of this contribution by first integrating out the S_1 . We then would end with a 1-loop diagram with χ_1 and a lepton propagating in the loop. The effective 4-fermion coupling of the $\chi_1 - \chi_0 - l - q$ vertex would be $y_{DM} * \lambda L, R/m_{S_1}^2$, and hence the full diagram would scale as

$$y_{DM}^4 \lambda_{L,R}^2 \lambda_{L,R}^2 m_{S_1}^{-8}$$
 (2)

On top of this strong suppression of the LQ mass, we also have to consider that we need specific quarks from the nucleon, and hence we will pay an additional price. Note that while the λ_L coupling will let us access b quarks inside the proton and λ_R will give us access to c_R , the coupling to u quarks proceeds via CKM mixing, so an additional chirality flip is needed, which then comes with a charm Yukawa ($y_c \sim 0.09$) thus giving an overall suppression of $y_c^2 \sim 8 \times 10^{-2}$. We can then focus only on bottom or charm quarks in the initial and final state, and then pay a form factor suppression of $f_{Tq}(n,p)^4$ which is about 0.06 for bottom and charm quarks, thus leading to an overall suppression of $(0.066)^4 \sim 1.9 \times 10^{-5}$. [JZ: end of speculation]

[JZ: Under study by GB, AG, DS, JB]

4.2 Relic Density

[JZ: Coannihilation done with Micromegas, CDFO: Under study by GB, JH, AL, AG, JB]

Preliminary results using the LQ solution to the flavor anomalies and satisfying the correct relic density are displayed in Fig. 3.

⁴[JZ: A quick estimation from MSSM neutralinos gave me $f_{T,q}^{(n,p)} = 2/27(1 - sum_{u,d,s}f_{T,q}^{(n,p)}) \sim 2/27(1 - 0.107) \sim 0.066$].

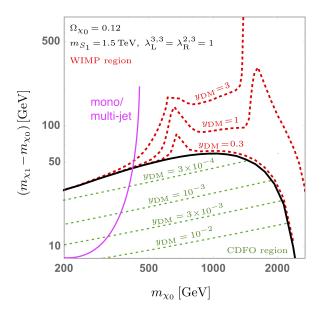


Fig. 3: Parameters space in the $m_{\chi_0} - \Delta = m_{\chi_1} - m_{\chi_0}$ plane satisfying $\Omega h^2 = 0.12$. The solid black line denotes the boundary between the coannihilation (CA) and the conversion-driven freeze-out (CDFO) regimes. The dashed lines also indicate the specific value of Y_{dm} . We also overlay a naive hand-waving estimate of the mono-jet reach (see Section 5.2).

4.3 Indirect Detection

[JZ: JH and AG want to write something about it.]

Indirect detection constitutes an important probe of the self-annihilating nature of dark matter. In the considered model annihilation today dominantly takes place either via the $2 \to 2$ process $\chi^0 \chi^0 \to S_1 S_1$, if $m_{S_1} < m_{\chi^0}$, or via $2 \to 4$ or loop-induced $2 \to 2$ processes otherwise. [Right?] Figure 6 shows an exemplary $2 \to 4$ annihilation diagram. As these processes are suppressed by the off-shell S_1 propagator (or loop-suppressed) we expect small annihilation rates. In particular, if annihilation during freeze-out proceeds dominantly via $\chi^0 \chi^\pm$ co-annihilation or pair-annihilation of χ^\pm , the relic density constraint does not require the dark matter self-annihilation rate to be large and hence we expect it to fall below the sensitivity of indirect detection experiments.

In Figure 5 we show an exemplary gamma-ray and antiproton spectra per annihilation for a benchmark point with $m_{\chi^0}=150\,\mathrm{GeV}$, $m_{\chi^\pm}=600\,\mathrm{GeV}$ and $m_{S_1}=1\,\mathrm{TeV}$. Note that as long as $m_{S_1}>m_{\chi^0}$ (and, of course, $m_{\chi^\pm}>m_{\chi^0}$) the masses m_{S_1} and m_{χ^\pm} are not expected to have a significant effect on the shape of the spectrum but mainly change the annihilation cross section, *i.e.* the total normalization of the signal. We also compare the spectra to the ones for annihilation into $b\bar{b}$ which is an often quoted reference channel in the literature (choosing the same dark matter mass). While the gamma-ray spectrum is very similar to the one for $b\bar{b}$, the antiproton spectrum is slightly more peaked. However, it does not exhibit a distinct feature that is expected to alter the constraints with respect to the case of $b\bar{b}$ drastically. Accordingly, we can use the limits on $b\bar{b}$ for an order-of-magnitude estimate of indirect detection limits in our model and use them to asses their relevance. [Just as a proposal. Needs to be further checked, of course.]

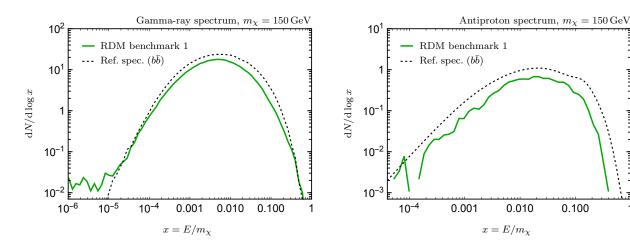


Fig. 4: Exemplary gamma-ray (left panel) and antiproton spectra (right panel) for dark matter annihilation of the benchmark point with $m_{\chi^0}=150\,{\rm GeV},\,m_{\chi^\pm}=600\,{\rm GeV}$ and $m_{S_1}=1\,{\rm TeV}$ (green curves). For comparison we show the corresponding reference spectra for annihilation into $b\bar{b}$ (black dotted curves).

0.100

LHC CONSTRAINTS

Our model contains three new fields that are probed by several LHC searches, which generically fall into two categories. On one hand, we have direct searches for leptoquarks (S_1) , both for single and double production. On the other hand we have the full spectrum of missing energy searches targeting dark matter observables, in our case driven by pair production of χ_1 via gauge interarctions. As a hybrid of both categories, the CMS search for leptoquark plus dark matter [16], inspired by the Coannihilation Codex [8], gives not only interesting constraints on the parameter space, but moreover it would allow to establish the connection between flavor anomalies and dark matter, in a post-discovery scenario.

In each of the categories described above, we will consider both a) existing searches and b) novel searches (for instance, the aforementioned LQ + MET search of Ref [16] only applies if the leptoquark decays to muons, but it is not applicable for e.g. electron decays).

We note that the actual mechanism underlying the production of the dark matter abundance has phenomenological implications. Two distinct scenarios arise, depending on the size of y_{DM} versus $\lambda_{L,R}$. For y_{DM} comparable to the S_1 couplings to leptons and quarks all S_1 decay modes $b\nu, c\tau, t\tau, \chi_1\chi_0$ have comparable branching fractions, hence all three kind of searches (LQ, MET, LQ + MET) are relevant, and the combination of all searches would allow to establish this model and measure its parameters. In the case of CDFO, we have seen from Figure 3 that $y_{DM} \lesssim 10^{-2}$ and hence we would have only the signatures in LQ searches and in MET searches. However, if in the $\chi_1 o \chi_0 lq$ decay one could resolve the final state lepton and quarks, one would have an additional handle to make the link between apparently uncorrelated signals in LQ and MET searches.

Leptoquark searches

[JZ: Under study by JB, GP, PP, JZ, AJ]

5.11 LQ pair searches

Pair production of LQs at the LHC proceeds via gauge couplings, as shown in the left panel of Fig 7.

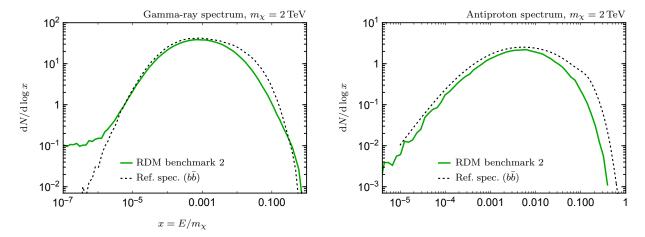


Fig. 5: Exemplary gamma-ray (left panel) and antiproton spectra (right panel) for dark matter annihilation of the benchmark point with $m_{\chi^0}=2\,{\rm TeV},\,m_{\chi^\pm}=2.5\,{\rm TeV}$ and $m_{S_1}=1.5\,{\rm TeV}$ (green curves). For comparison we show the corresponding reference spectra for annihilation into $b\bar{b}$ (black dotted curves).

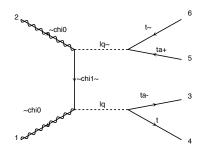


Fig. 6: Exemplary $2 \rightarrow 4$ dark matter annihilation diagram.

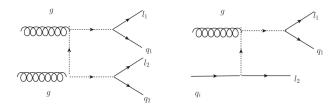


Fig. 7: Leptoquark production at the LHC: single (left) and double (right), considering visible decays.

5.12 LQ associated production (with lepton and/or jet)

[JZ: In charge: JZ, AB, DS, AJ]

A single leptoquark can also be produced in association with a SM fermion, as shown in the right panel of Fig 7. For our particular choice of couplings, we expect that one can have some sensitivity if this fermion is a charged lepton, hence if $l_2 = e, \mu, \tau$.

5.2 Dark matter (missing energy) searches

Since the χ_1 particle is the lightest new particle with non-trivial SM quantum numbers, its production is strongly constrained by LHC searches, and it can only be "hidden" if χ_1 and χ_0 are close in mass. The LHC production is depicted in Fig. 8. The usual strategy against a compressed spectra is to boost the system with additional radiation, leading to the mono-X (typically jet) signals.

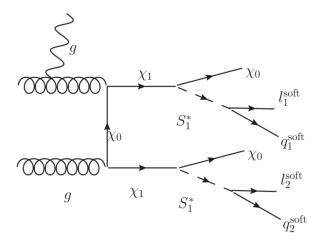


Fig. 8: Monojet (plus soft leptons and quarks) signatures.

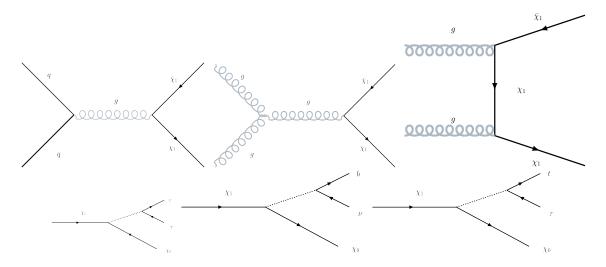


Fig. 9: Production and decay channels for χ_1 .

However, if the SM decay products in the $\chi_1 \to \chi_0$ are soft enough to be reconstructed (but probably not to triggered on) the LHC sensitivity gets greatly enhanced, as shown in e.g. [17] for MSSM electroweakinos and soft-leptons. However, the mass gap can be small enough such that the soft decay products fail to pass the reconstruction thresholds, in which case the pair production of χ particles can only be constrained by mono-jet searches. We stress that this is an unavoidable bound, that, for a given Δ , sets a lower mass on the dark sector masses. We will thus ignore here the MET searches that also include resolved (soft or hard) leptons. [JZ: This last sentence needs to be revisited depending on what is available in MadAnalysis, CheckMATE or similar].

5.3 Resonant lepto-quark + MET search

[JZ: Benj wants to recast the CMS study, [16]. AJ will help him.].

6. CONCLUSIONS

The charged-current flavor anomalies hint at the present of leptoquarks near or at the TeV scale. Here we have studied the connection between these models and dark matter, which necessarily requires to add new particles and couplings. Employing a simplified model with only 6 parameters we have scanned the parameter space vis-a-vis the aformentioned flavor anomalies, relic density, direct detection and LHC constraints.

We have seen that when taken all these constraints simultaneously [JZ: SOMETHING]. We thus encourage the LHC collaborations to ... [JZ: DO A NEW SEARCH THAT MIGHT BE IMPORTANT / CONVINCE ATLAS OF DOING THE LQ RESONANT + MET STUDY]. Naively rescaling our results for the HL-LHC we find that (HOPEFULLY) the parameter space favored by the flavor anomalies will be fully covered with just 1000 fb⁻¹ of data. [JZ: Maybe we will leave the projections for the paper.]

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A Appendix A

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