

# Ghid recapitulare – Sortari & Order Statistics

## Sortari prin comparatii

- **Insertion Sort**
  - Bun pt. vectori mici / aproape sortati.
  - Worst-case:  $O(n^2)$ .
- **Merge Sort**
  - Divide et impera: divide  $\rightarrow$  conquer  $\rightarrow$  merge.
  - Complexitate:  $O(n \log n)$  mereu.
  - Nu e in-place (foloseste memorie suplimentara).
- **Heap Sort**
  - Foloseste max-heap.
  - BuildHeap:  $O(n)$ .
  - Sortare:  $n$  apeluri Heapify  $\rightarrow O(n \log n)$ .
  - In-place, worst-case tot  $O(n \log n)$ .
  - Practic: mai lent decat Quicksort.
- **Quick Sort**
  - Divide et impera cu pivot.
  - Average:  $O(n \log n)$ .
  - Worst-case:  $O(n^2)$  (ex. sir sortat daca pivot prost).
  - Randomizare pivot  $\rightarrow$  elimina caz prost.
  - Cel mai rapid in practica.

## Limite teoretice

- Toate sortarile prin comparatii au limita  $\Omega(n \log n)$ .
- Dovada: arborele de decizie ( $n!$  permutari  $\rightarrow$  inaltime minima  $\log(n!) \approx n \log n$ ).

## Sortari liniare (fara comparatii)

- **Counting Sort**:  $O(n + k)$ . Necesita interval mic de valori ( $1..k$ ). Nu e in-place.
- **Radix Sort**:  $O(d \cdot (n+k))$ , cu Counting Sort pe cifre. Devine  $O(n)$  daca  $d$  constant si  $k=O(n)$ . Stabil.

- **Bucket Sort**: pentru valori uniforme in  $[0,1)$ . Expected  $O(n)$ .

## Order Statistics

- **Minim / Maxim**:  $O(n)$ .
- **Min + Max impreuna**: 3 comparatii pentru 2 elemente  $\rightarrow \sim 1.5n$  comparatii.
- **Selectia (al i-lea cel mai mic)**:
- Naiv: sortezi  $\rightarrow O(n \log n)$ .
- Randomized Select  $\rightarrow O(n)$  in medie.
- Median of Medians  $\rightarrow O(n)$  worst-case (teoretic, nu prea folosit practic).

## De stiut la examen:

- Diferente cheie intre sortari (merge vs quick, quick vs heap).
- Cand putem face mai bine de  $O(n \log n)$  (Counting / Radix / Bucket).
- Cum gasim rapid min, max, mediana.
- De ce limitele  $\Omega(n \log n)$  NU se aplica la Counting/ Radix (nu folosesc comparatii).