

Recent Advances in Potentiometric Scanning Electrochemical Microscopy

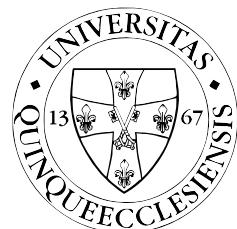
PhD Dissertation Draft

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Preface

The work presented here was performed mainly at the *Department of General and Physical Chemistry* in the *Doctoral School of Chemistry* at the *University of Pécs*, during the years 2011-2016, under the supervision of Professor Géza Nagy. Some of the work was done at the *Department of Physical Chemistry* of the *La Laguna University* in Tenerife, Spain, under the joint supervision of Professor Géza Nagy, and Professor Ricardo M. Souto. This thesis is based almost entirely on the following publications, which are referred to in the text by their Roman numerals.

I. András Kiss, Ricardo M. Souto, Géza Nagy

Investigation of Mg/Al alloy sacrificial anode corrosion with Scanning Electrochemical Microscopy

Periodica Polytechnica Chemical Engineering 57, no. 1-2 (2013): 11-14.

IF.: 0.30, cited by: 2

II. Javier Izquierdo, András Kiss, Juan José Santana, Lívia Nagy, István Bitter, Hugh S. Isaacs, Géza Nagy, Ricardo M. Souto

Development of Mg^{2+} ion-selective microelectrodes for potentiometric scanning electrochemical microscopy monitoring of galvanic corrosion processes

Journal of The Electrochemical Society 160, no. 9 (2013): C451-C459.

IF.: 3.27, cited by: 14

III. Ricardo M. Souto, András Kiss, Javier Izquierdo, Lívia Nagy, István Bitter, Géza Nagy

Spatially-resolved imaging of concentration distributions on corroding magnesium-based materials exposed to aqueous environments by SECM

Electrochemistry Communications 26 (2013): 25-28.

IF.: 4.85, cited by: 20

IV. András Kiss, Géza Nagy

New SECM scanning algorithms for improved potentiometric imaging of circularly symmetric targets

Electrochimica Acta 119 (2014): 169-174.

IF.: 4.50, cited by: 5

V. András Kiss, Géza Nagy

Deconvolution in Potentiometric SECM

Electroanalysis 27, no. 3 (2015): 587-590.

IF.: 2.14, cited by: 1

VI. András Kiss, Géza Nagy

Deconvolution of potentiometric SECM images recorded with high scan rate

Electrochimica Acta 163 (2015): 303-309.

IF.: 4.50, cited by: 3

Contribution statement

Publications **I**, and **IV-VI** are entirely my own work including the original idea, the experimental work, the simulations, the calculations, the written text and the figures. They were done under the guidance of my doctoral supervisor, Professor Géza Nagy, in Pécs, at the Department of General and Physical Chemistry of the University of Pécs. Publications **II** and **III** are mostly my work. The work published therein was done at the University of La Laguna, Tenerife, under the supervision of Professor Ricardo M. Souto and Professor Géza Nagy. In **II** and **III**, I prepared the electrodes, did the electrode characterization and the majority of the SECM scans.

Not included in the thesis

- (a) Zsuzsanna Őri, **András Kiss**, Anton Alexandru Ciucu, Constantin Mihailciuc, Cristian Dragos Stefanescu, Livia Nagy, Géza Nagy

Sensitivity enhancement of a „bananatrode” biosensor for dopamine based on SECM studies inside its reaction layer

IF.: 4.10, cited by: 4

Sensors and Actuators B: Chemical 190 (2014): 149-156.

- (b) Javier Izquierdo, Bibiana M Fernández-Pérez, Dániel Filotás, Zsuzsanna Őri, **András Kiss**, Romen T Martín-Gómez, Lívia Nagy, Géza Nagy, Ricardo M Souto

Imaging of Concentration Distributions and Hydrogen Evolution on Corroding Magnesium Exposed to Aqueous Environments Using Scanning Electrochemical Microscopy

IF.: 2.471

Electroanalysis (2016).

- (c) A. El Jaouhari, Dániel Filotás, **András Kiss**, M. Laabd, E. A. Bazaarui, Lívia Nagy, Géza Nagy, A. Albourine, J. I. Martins, R. Wang

SECM investigation of electrochemically synthesized polypyrrole from aqueous medium

IF.: 2.223

Journal of Applied Electrochemistry, (2016).

Published prior PhD

András Kiss, László Kiss, Barna Kovács, Géza Nagy

Air Gap Microcell for Scanning Electrochemical Microscopic Imaging of Carbon Dioxide Output. Model Calculation and Gas Phase SECM Measurements for Estimation of Carbon Dioxide Producing Activity of Microbial Sources

Electroanalysis 23, no. 10 (2011): 2320-2326.

IF.: 2.14, cited by: 1

Published in non-refereed journal

Lívia Nagy, Gergely Gyevai, **András Kiss**, Ricardo Souto, Javier Izquierdo, Géza Nagy

Speciális célra szolgáló mikroelektródok kifejlesztése és alkalmazása

Magyar Kémiai Folyóirat 119, 2-3. (2013): 104-109.

Book chapter

Ricardo M. Souto, Javier Izquierdo, Juan J. Santana, **András Kiss**, Lívia Nagy, Géza Nagy

Progress in Scanning Electrochemical Microscopy by coupling Potentiometric and Amperometric Measurement Modes

Current Microscopy Contributions to Advances in Science and Technology (A. Méndez-Vilas, Ed.), Formatex, (2012): 1407-1415.

Presentations

Posters

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I am thankful to Professor Johan Bobacka, Ricardo M. Souto, Frank-Michael Matysik, Petr Skládal and Mohammed Bazzaoui for welcoming me in their laboratories.

I am also thankful to all the anonymous referees who gave meaningful feedback about my work as part of the peer review process.

Pécs, March, 2017.

András Kiss

Motivation

I started my doctoral studies at the Department of General and Physical Chemistry at the University of Pécs in 2011 under the supervision of Professor Géza Nagy. By that time, I've already spent 3 years there as an undergraduate student, culminating in my MSc thesis, which I successfully defended in 2011. The original title of my PhD research was „*Application of potentiometric microelectrodes in Scanning Electrochemical Microscopy to study the corrosion of magnesium and its alloys*”. I started the work with great enthusiasm, but soon discovered, that the potentiometric SECM had one major limitation which prevented me from pursuing my studies in corrosion science. The method was too slow to complete a relevant portion of the scan before the system has completely changed. Corrosion is highly localized, and the location and size of the anodic and cathodic spots are quick to change. On the other hand, when one increases scanning speed, the image becomes distorted. This is because the time allowed for the potentiometric cell to reach equilibrium potential is getting closer to RC, the time constant of the cell, or more specifically $4 \times RC$, which is the least amount of time necessary to reach equilibrium potential to a reasonable extent. In order to use SECM more effectively in corrosion studies, one has to speed up the method, *and* lower, or at least not increase imaging distortion.

Efforts have already been made at the Department of General and Physical Chemistry to lower the resistance of the electrodes used as SECM measuring probes. By using novel solid contact instead of the conventional liquid contact as interface between the metallic conductor and the ion selective cocktail, resistance, and therefore the RC time constant could be decreased by a factor of ten. Building on the new electrodes, several papers have been published about successful research collaborations with neurophysiologists, botanists, and in particular, corrosion scientists.

I joined the research in the hopes of a worthwhile contribution to the technique of potentiometric SECM, which eventually might lead to new possibilities in corrosion science and other areas. My PhD research was slowly turning into a methodological study, exploring ideas to improve the technique.

In 2012 I was lucky enough to be able to participate in the biggest conference of „SECM and related techniques” held annually, which in 2012, was held in Ein

Gedi, Israel. I've realized, that other research groups are also struggling with the difficulties of potentiometric SECM, and the problem is not limited to corrosion science. In fact, most of the studies are done in amperometric mode, which, based on discussions with participants, might be exactly due to these difficulties. Also in 2012 I was able to spend a month at the Department of Physical Chemistry of the La Laguna University in Tenerife under the supervision of Professor Ricardo M. Souto. We used the very same solid contact magnesium-ion selective electrodes I prepared in Pécs to map magnesium-ion concentration above corroding magnesium and magnesium alloy samples. They worked unexpectedly well, and we were able to take high-speed, low distortion images of the samples for the first time. We published the results. I was very happy with the two papers done in cooperation between our research groups, and the methodological aspect of them fitted nicely in my research topic.

When I returned home, I immediately started working on a new idea I had when I was in Tenerife. Since the majority of the targets in SECM studies are, or can be made circular, it makes sense to use a scanning pattern based on the polar coordinate system instead of the conventional 2D raster based on the Cartesian coordinate system. With new scanning patterns and algorithms, I managed to further decrease distortion and increase scanning speed at the same time.

While working on the final touches of the paper about the new scanning algorithms, I had another idea. The transient response of the potentiometric cell due to concentration changes is described by a relatively simple function. It's not necessary to wait $4 \times RC$ to find out the equilibrium potential at a given sampling point. From the initial potential, and the potential at time t , it's possible to calculate it. One has to know the response characteristics of the cell, but that can be easily measured. I managed to increase scanning speed even further. My PhD thesis is mainly about these three improvements to the potentiometric SECM.

In May 2016, I was lucky enough to be invited to the Analytica 2016 conference in München, by Professor Frank-Michael Matysik. I presented my work, and got precious feedback from the audience, including two of the most prominent researchers working in the field; Professors Michael Mirkin and Eric Bakker. The discussions with them shed some light on a few issues I faced writing my thesis.

The author hopes that he managed to contribute to the field of Scanning Electrochemical Microscopy with this thesis. Please forgive the rather lengthy discussion about the role of biologists in the development of microelectrodes, but the author graduated as a biologist himself, and takes pride in the achievements of the early pioneers of electrophysiology.

Chapter 1

Introduction

Since the invention of Scanning Tunnelling Microscopy (STM) in 1981 by Binnig and Rohrer, surface analysis has seen tremendous growth. The fact that they received the Nobel Prize in 1986, only five years later, is an indication of the importance of their pioneering work. STM was but the first of a family of techniques, called Scanning Probe Microscopy (SPM), with many more to come in the following years. Their basic element is a local experiment, which is repeated sequentially at the pre-defined points of a raster grid. Then, the gathered information is presented by plotting the measured parameter as a function of their coordinate. The most important advantage of them over the conventional optical microscopy is their incredible resolution. Even individual atoms can be „seen”, because they are not limited by Abbes’ formula. Modifications of the original STM followed quickly. For instance, Atomic Force Microscopy was invented in 1982 by the same researchers.

In 1989, not long after the introduction of the STM, electrochemists invented the Scanning Electrochemical Microscope (SECM), the electrochemical version of SPM. It is based on the same concept, except the scanning probe is a microelectrode. With this technique, highly resolved chemical information can be gathered about a wide range of surfaces. One of the biggest disadvantages of the SPM techniques in general is their low speed, due to the scanning process. The entire image is recorded with the same measuring tip, as opposed to optical techniques, where there is usually a sensor array. As a consequence of this, the more data points are in an image, the longer it will take to record it. This is especially a problem in the potentiometric operation mode of the SECM. The response time of the measuring cell is determined by the time constant, which in turn, depends mainly on the resistance of the measuring microelectrode. Due to the small size of the microelectrodes, their resistance can even reach the $G\Omega$ range, resulting in imaging times that can be measured in minutes. There are other contributors to the delayed response of the potentiometric cell, such as transport limitation and the complexation reaction between the ion and the

ionophore. Usually only one of these steps will determine the response of a particular cell. That step is called the *rate determining step*.

Other SPM techniques have received significant improvement during the last few decades, and their imaging speed can even reach video framerates. Low speed, however, is an often overlooked limitation of the SECM, and prevents the quick recording of highly resolved images. That is, one has to choose between high resolution and quick imaging. The image will either be quickly completed but distorted, or high quality but asynchronous, because the points of the image will not only have different spatial, but different temporal coordinates as well.

My thesis is mostly devoted to the investigation of this problem, and three possible solutions to it:

1. Use of novel, low-resistance solid contact electrodes instead of conventional ones. Based on publications [I-III](#).
2. Optimization of scanning patterns and algorithms. Based on publication [IV](#).
3. Deconvolution of distorted potentiometric SECM images recorded with high scanrate. Based on publications [V-VI](#).

The first approach I took is to lower the resistance of the measuring microelectrode. By using a conducting polymer based solid internal contact instead of the conventional liquid contact, electrode resistance, therefore RC time-constant of the entire potentiometric circuit can be decreased. Conducting polymers have been used in macroelectrodes before, but never where it is crucial to have a small resistance despite the small probe diameter: SECM investigation of corroding surfaces.

The second approach is to optimize scanning patterns. Many studied systems have a certain symmetry which can be exploited to achieve lower distortion. I chose a simple, yet very common symmetry, the radial symmetry, and came up with optimized scanning patterns and algorithms.

The third technique is image processing. The relationship between cell potential difference and time is relatively simple, and by measuring some basic parameters of the microelectrode and the potentiometric cell, a deconvolution function can be obtained. With this, the equilibrium potential can be calculated for each data acquisition point of the raster grid, and distortion can be removed from the image.

To investigate the performance of these techniques, I've used simple model systems, then, I've applied them in corrosion studies as an example where they can be useful. During collaborations with colleagues, I used these techniques on several occasions, and I've included some of those results in my thesis.

Additionally, I investigated the undesired effect of electric field generated in certain SECM experiments. In some cases, where there is a potential difference between two points in the electrolyte, a relatively strong electric field can be formed. For instance during galvanic corrosion there is a large potential difference between the surfaces of the metals constituting the galvanic couple. The local electric field at the tip of the measuring electrode might influence the measured potential. I investigated this contribution to the measured value, and tried to isolate the effect of the electric field.

Chapter 2

Theory and principles

2.1 Microelectrodes

2.1.1 Pioneers of using microelectrodes

In this section I look at the motivation behind electrode miniaturization, and the difficulties the researchers encountered during the early development of microelectrodes. By decreasing electrode diameter, new challenges had to be faced. These challenges always lead to a compromise between several competing desired properties, which can never truly be solved, only alleviated to a certain point, to make a particular study possible. Researchers that first used microelectrodes faced the same problems as todays researchers, the difference lies in the severity of the compromise. The fundamental problem of potentiometry with microelectrodes hasn't changed. Therefore, I reviewed the literature going back to the first appearances of such electrodes in an effort to better understand the reasons and potential solutions of some of the problems in microelectrode potentiometry.

For the first few decades, the development of microelectrodes was related closely, almost exclusively to neurophysiology. The main merit of the work of the early pioneers from the standpoint of the electrochemist, is the foundation of the micropipette techniques, including preparation, instrumentation, and basic characterization.

First efforts to miniaturize electrodes originally were made by biologists, electrophysiologists in particular. Microelectrodes were necessary to carry out experiments at the cellular level on single neurons. Even though the largest possible neuron cells (*Loligo forbesii* or veined squid, *Architeuthis spp.* or giant squid) were used in the early days of neurophysiology, the electrodes of those days in the 1930's weren't small enough for single cell experiments. This initiated the miniaturization of electrodes. The first successful experiments were done by the famous pioneers of the field, *Sir Alan Lloyd Hodgkin*, *Sir Andrew Huxley* and *Sir John Eccles* (Fig. 2.1),



Figure 2.1: Sir Alan L. Hodgkin, Sir Andrew Huxley and Sir John Eccles, the pioneers of electrophysiology, first to use microelectrodes.

who were awarded the Nobel Prize in Physiology and Medicine „*for their discoveries concerning the ionic mechanisms involved in excitation and inhibition in the peripheral and central portions of the nerve cell membrane*”, in 1963.

They have found that the best subject for electroneurophysiological studies is the giant squid axon. The large diameter of the axon provided a great experimental advantage for Hodgkin and Huxley; this species has large enough axons to allow the intracellular insertion of voltage clamp electrodes. But as Graham and Gerard writes [1]:

„*The giant fiber, up to a millimeter in diameter is admirable for internal exploration with a microelectrode, since this can be inserted longitudinally and the tip pushed far from the region of penetration and damage. These fibers are available, however, only at restricted seasons and localities and after painstaking preparation.*”

Interestingly, the Second World War might have accelerated the miniaturization of the microelectrodes, because it restricted the availability of the giant squid. Webb and Young wrote in their 1940 paper [2]:

„*Unfortunately the work was terminated by the outbreak of war, which rendered the capture of further squids impossible, so that the number of fibres dealt with is much smaller than might have been wished.*”

Another species, the much more accessible longfin inshore squid (*Loligo paelii*) had to be used, which has much smaller axons. In order to carry out voltage clamp

experiments on neurons of this species, the intracellular microelectrodes had to be miniaturized further.

The basic experimental setup for an early neurophysiological study employed several electrodes. To measure the potential difference across the cell membrane, an intra- and an extracellular electrode is necessary. This technique has been used to measure the resting potential in the axon of the squid [3, 4]. A microelectrode consisting of a long glass capillary was pushed into one end of the axon until it reached a distance of 10 – 30 mm. To avoid causing damage to the cell membrane, great care had to be taken during this step. The small diameter of most nerve and muscle fibres made it extremely difficult to use this technique. The breakthrough came when Graham and Gerard showed that a very small electrode can be inserted perpendicularly into a muscle fiber without causing damage or unintentional excitation [1, 5]. But, in order to obtain successful results, the microelectrodes should have had an external diameter of less than 0.5 μm . Such a small electrode diameter however introduced additional difficulties associated to the inevitable increase in electric resistance. From that point on, the further development of microelectrodes depended on the development of the recording apparatus, as its properties combined with those of the microelectrode together determine the response characteristics. At that time, the state of the art amplifiers were of valve types. A few years later, advances in electronics and the technique in general made it possible to record both action, and resting potentials with these kind of electrodes [6, 7].

In 1950, Ling and Gerard published their findings in *Nature* about the dependence of resting membrane potential on external potassium ion concentration [8]. The resulting plot resembled the calibration plots of ion-selective electrodes that will come a few years later.

The next big advancement in the development of microelectrodes was the introduction of the so-called *patch-clamp* technique by *Erwin Neher* and *Bert Sakmann* [9, 10]. They received their Nobel Prize in 1991 „*for their discoveries concerning the function of single ion channels in cells*”, also in Physiology and Medicine. With this technique, single ion channels were possible to observe. The problem that had to be solved in order to be able to conduct these experiments was the large background noise. Eher and Sakmann wrote in their original Nature paper [9]:

„*Clearly, it would be of great interest to refine techniques of conductance measurement in order to resolve discrete changes in conductance which are expected to occur when single channels open or close. This has not been possible so far because of excessive extraneous background noise.*”

To solve this problem, they measured transmembrane ionic current only on a small, isolated area of the cell membrane. This was achieved by pushing the tip of a $d_o = 3 - 5 \mu\text{m}$ glass micropipette onto the cell membrane, and limiting the measurement to a small patch of the membrane, ideally featuring only a single ion channel. By measuring the current in this way, the two states of a single ion channel – closed and open – were possible to distinguish. Eher and Sakmann were able to detect the discrete conductance changes of the ion channel associated to the acetylcholine receptor in the neuromuscular junction.

2.1.2 Glass-based electrodes and microelectrodes

Analytical potentiometry started with the discovery and development of the glass pH-electrode. It is the best electrochemical sensor, and one of the best sensor ever made, with a linear response over more than 13 orders of magnitude, and excellent selectivity. Because of its importance, and because pH measurement is used throughout the work described in this thesis, the basic concepts of pH measurement will be introduced through the example of the glass electrode.

It was in 1906, when a botanist named Max Cremer discovered that the potential difference across a thin glass membrane is a function of pH when opposite sides of the membrane are in contact with solutions containing different concentrations of H_3O^+ [11, 12]. Three years later, in 1909, Sørensen introduced the concept of pH [13]. He defined it as the negative logarithm of the concentration of H_3O^+ :

$$\text{pH} = -\lg c_{\text{H}_3\text{O}^+} \quad (2.1)$$

This however, is not entirely true, because pH depends on the *activity* of H_3O^+ , rather than its concentration:

$$\text{pH} = -\lg a_{\text{H}_3\text{O}^+} \quad (2.2)$$

And since pH is dimensionless, a better way to define pH is:

$$\text{pH} = -\lg(\gamma_{\text{H}_3\text{O}^+} m_{\text{H}_3\text{O}^+} / m^\theta) \quad (2.3)$$

or

$$\text{pH} = -\lg(\gamma_{\text{H}_3\text{O}^+} c_{\text{H}_3\text{O}^+} / c^\theta) \quad (2.4)$$

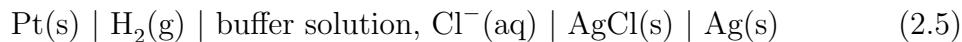
where $m^\theta = 1 \text{ mol}\cdot\text{kg}^{-1}$ and $c^\theta = 1 \text{ mol}\cdot\text{dm}^{-3}$ are the standard states, and $\gamma_{\text{H}_3\text{O}^+}$ is the activity coefficient of H_3O^+ .



Figure 2.2: The Gold Standard of pH measurement, the Harned cell (at the Danish National Metrology Institute).

The current, internationally accepted definition of pH is an instrumental definition, based on an electrochemical cell known as the *Harned Cell* [14] (Fig. 2.2). To measure the pH in such a cell, a conventional procedure was developed at NBS (National Bureau of Standards) [15] and recommended at present by the last IUPAC (International Union of Pure and Applied Chemistry) Recommendations [16]. NIST (National Institute of Standards and Technology) in the U.S. and PTB (Physikalisch-Technische Bundesanstalt) in Germany have presented pH values using the Harned Cell.

The Harned Cell is described by the following cell diagram:



To calculate the potential of the half-cells, the *Nernst-equation* can be used:

$$E = E^\theta - \frac{RT}{z_i F} \ln a_i \quad (2.6)$$

where E^θ is the standard potential difference of the cell, R the universal gas constant, F the Faraday constant, T the thermodynamic temperature, z_i is the valence and a_i is the activity of ion species i . The potential difference E of the cell 2.5 is described by the *Nernst-equation* as:

$$E = E^\theta - \frac{RT \ln 10}{F} \lg \left(\frac{a_{\text{H}_3\text{O}^+} m_{\text{Cl}^-} \gamma_{\text{Cl}^-}}{m^\theta} \right) \quad (2.7)$$

After expressing the pH:

$$\text{p}(a_{\text{H}_3\text{O}^+} \gamma_{\text{Cl}^-}) = -\lg(a_{\text{H}_3\text{O}^+} \gamma_{\text{Cl}^-}) = \frac{E - E^\theta}{(RT/F) \ln 10} + \lg \left(\frac{m_{\text{Cl}^-}}{m^\theta} \right) \quad (2.8)$$

where γ_{Cl^-} is the molal activity coefficient of the chloride ions at the molality m_{Cl^-} .

By extrapolating on the equation obtained with least square fitting, the value of the acidity function at zero chloride ion molality $\text{pa}_0 = -\lg(a_{\text{H}^+} \gamma_{\text{Cl}^-}) m_{\text{Cl}^- \rightarrow 0}$ can be determined. Applying the Bates-Guggenheim convention [17], the trace activity coefficient of chloride ions $\gamma_{\text{Cl}^- \rightarrow 0}$ at $m_{\text{Cl}^- \rightarrow 0}$ can be calculated:

$$\lg \gamma_{\text{Cl}^- \rightarrow 0} = \frac{AI^{1/2}}{1 + 1.5I^{1/2}} \quad (2.9)$$

where A is the Debye-Hückel temperature-dependent limiting slope and I the ionic strength of the buffer solution calculated by $I = (1/2)\sum c_i z_i^2$, where c_i and z_i are the molar concentration and electric charge of ionic species i .

Haber and Klemensiewicz gave a full account of the response of the glass electrode in their 1909 paper [18, 19]. The next advance towards the microelectrodes was the miniaturization of the glass electrode by Caldwell in 1954 [20]. He used it to measure intracellular pH in crab muscle fibers. Hinke created ion-selective electrodes for potassium and sodium using the respective sensitive glasses developed by Eisenmann, Rudin and Casby two years earlier [21], based on the work of Lengyel [22] published in 1934. He used them to show the correlation between sodium ion concentration in blood, and blood pressure [23, 24]. Also, similarly to what Caldwell did with the glass electrode, Hinke created sodium and potassium ion-selective microelectrodes in 1959 [25] using the same type of ion selective glasses. With his revolutionary ***ion-selective microelectrodes*** (Fig. 2.3), Hinke was able to perform the first true intracellular ion-selective measurements, and determined the potassium and sodium ion concentration in the muscle cells of the propodite of crab and lobster (*Carcinus mænus* and *Homarus vulgaris*). His microelectrodes originally had a tip cross section of $20 \mu\text{m} \times 150 \mu\text{m}$, with a wall thickness of $1 - 4 \mu\text{m}$, and a resistance of $10^{10} - 10^{11} \Omega$.



Figure 2.3: The first true ion-selective microelectrodes, created by Hinke to measure intracellular sodium, and potassium ion concentration. As published in his 1959 *Nature* paper [25].

2.1.3 Liquid ion exchanger membrane based microelectrodes

While Hinke was able to eventually decrease the tip diameter of his ion-selective microelectrodes to 1 μm or less, the sensitive area was too large ($\sim 10 \mu\text{m}$ in length, and $\geq 5 \mu\text{m}$ in diameter). In order to measure intracellular ion activity, it was necessary to push the entire sensitive part into the cell, causing significant damage. In addition to the problem of size, they were difficult to fabricate.

By that time, liquid ion exchangers have been used in liquid-liquid ion extraction processes in industry and, and as models for biological membranes [26,27]. Sandblom, Eisenmann and Walker published two papers in 1971 about a rather exhaustive theoretical treatment of such liquid ion exchanger (LIX) membranes [28, 29]. Also in 1971, Walker was able to prepare a miniaturized version of the electrodes based on the LIX membranes [30]. He writes in [30]:

„A liquid ion exchanger is composed of an organic electrolyte dissolved in a water-immiscible solvent, usually an organic solvent with a low dielectric constant. Owing to the low dielectric constant of the exchanger, inorganic ions have a very low solubility in the exchanger and, consequently, a membrane made of a liquid ion exchanger is much more permeable to ions whose valence sign is opposite to that of the organic ion than to ions of the same valence sign because of ion pair formation with the organic ion.“

Walker also added a crucial step to the fabrication of these microelectrodes: the silanization of the inner surface of micropipette. The surface of the glass pipette is highly hydrophilic owing to the silanol groups, and the sensing membrane in the pipette tip is hydrophobic. To improve the adhesion of the two, and to prevent the electrolyte from creeping along the pipette wall from either side, Walker silanized the surface. This step improved stability and life-time of these microelectrodes drastically.

He used the new LIX ion-selective microelectrodes to measure chloride, and potassium ion activity in *Aplysia* neurons. He estimated the resistance for his electrodes from their response time in the range of 10^9 to 10^{10} Ω . He also performed selectivity measurements on the microelectrode, using the Nicolsky-equation [31]:

$$E = E^\theta + \frac{RT}{z_i F} \ln \left[a_i + \sum_j \left(k_{ij} a_j^{z_i/z_j} \right) \right] \quad (2.10)$$

where E is the open circuit potential, E^θ the standard electrode potential, z and a are the valency and the activity of the ionic species i and j . k_{ij} is the selectivity coefficient with respect to j . These microelectrodes were surpassed by the following generation of ion-selective microelectrodes, based on the ionophores.

2.1.4 Ionophore based microelectrodes

The ion-selective microelectrodes used today are based on the ionophores. These are carriers for specific ions, and act as complexing ligands. Štefanac and Simon published their work concerning the use of nonactin, a lipophilic antibiotic, as ionophore in ion-selective membranes [32, 33]. Their cell consisted of the following elements:



They dissolved nonactin and nonactin homologs in carbon tetrachloride, and transferred onto sintered glass discs to form a membrane. Their cell showed a selectivity for certain cations, especially potassium and ammonium ions [32, 33].

For quite some time after the discovery that ionophores can be used in ion selective electrodes, the LIX membrane based ion selective microelectrodes were used instead. The reason for this is the relatively high resistance of the membranes employing the neutral carrier ionophores. They had however, a great advantage over the LIX membranes: their selectivity. In cases, as Amman writes in his 1987 paper [34] it reached a factor of 5000:

„[With the valinomycin based microelectrodes ...] extremely high K⁺ selectivities are obtained, e.g. a rejection of Na⁺ by a factor of 5000 and of acetylcholine by a factor of 3400. At a constant background of 140 and 500 mM Na⁺, the detection limit of the K⁺ sensor is at 1.6×10^{-5} and at 2.5×10^{-5} M K⁺, respectively.”

and

„Valinomycin-based microelectrodes will find increasing application only if their electrical resistances can be further reduced without inducing a loss in K⁺ selectivity.”

Oehme and Simon did a comparison of the two types much earlier, in 1976 [35], and already realized the major difference between the two. A slightly improved version by Wuhrmann [36] found only limited use in physiology. In both of these papers, valinomycin based microelectrodes with a very high resistance ($R = 10^{11} \Omega$) are described. Such high resistances of course result in very long response times ($\tau > 30$ s).

The big breakthrough came when Ammann realized, that the resistance of neutral carrier-based membranes can be lowered drastically if both lipophilic salts and polar membrane solvents are added to the membrane [34]. With this improvement, he lowered the resistance and essentially got the same as the LIX membranes had at the time, but managed to maintain the extremely high selectivity.

The first synthesized ionophores were introduced in 1969 by Kimura and co-workers [37]. Since then, many research groups synthesized ionophores for many different ions.

pH and blood gases have been measured routinely since Severinghaus and Bradley developed the blood gas analyzer for CO₂ and O₂ in 1958 [38]. These are not based on ionophores, but will be described here briefly because they are related closely to the metal/metal-oxide microelectrodes used in this dissertation. To measure oxygen, they used Clarks electrode [39], and for carbon-dioxide, they developed a gas gas sensor, which since has been known as the „Severinghaus-electrode”. It is based on pH measurement in a thin membrane on the surface of a glass pH-electrode. Carbon-dioxide diffuses to the membrane, dissolves in the thin film, and lowers the pH. The cell has been miniaturized by several research groups [40–44]. The cited papers are all using an improved, miniaturized, microelectrode version of the original electrode. I used a similar, antimony based miniaturized Severinghaus-electrode in my masters

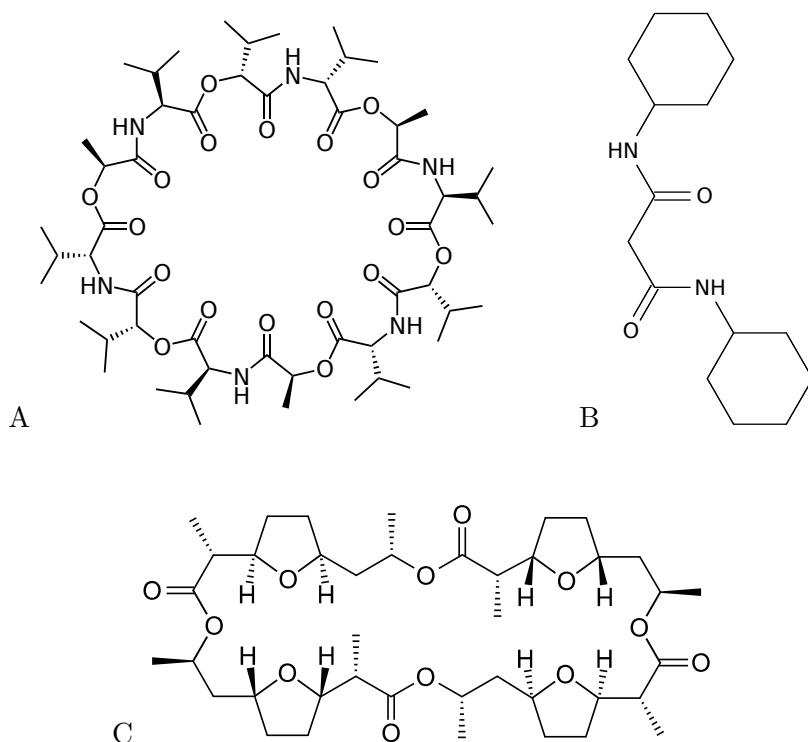


Figure 2.4: (A) Valinomycin, (B) bis-N,N-dicyclohexyl-malonamide, and (C) nonactin, ionophores for potassium, magnesium, and ammonium ions, respectively.

thesis [45], and published spatially resolved CO₂ measurements – with the same electrode – of living yeast colonies in [46].

A big advancement in the field of ion-selective electrodes was the elimination of the internal filling solution from the conventional ion-selective electrodes. This resulted in the so-called *solid-contact* electrodes. The first of these were unstable, because there was no reversible and fast ion-to-electron transducer [47]. Solid-contact electrodes had already been around since the 1970s with the invention of the coated-wire electrode (CWE) [48]. The instability was solved by the electropolymerization of a thin layer of conductive polymer onto the solid contact, that showed a mixed electronic and ionic conductivity, thereby providing a stable ion-to-electron interface [49–52]. A wide range of conductive polymers are used, including polypyrroles [53], polythiophenes [54], and polyanilins [55]. In this thesis, the ion-to-electron interface in the solid-contact ion-selective microelectrodes is PEDOT (poly(3,4-ethylenedioxythiophene)), first used for this purpose by Johan Bobacka and coworkers [54]. Solid-contact electrodes were used in the work done in our laboratory earlier [56–58].

An interesting application of solid-contact microelectrodes is described in [59]. An array of electrochemical sensors, including 27 microelectrodes were used to determine

the concentration of certain ions in the martian soil. This is a good demonstration of how little and simple instrumentation is enough to carry out potentiometric measurements. During Mars missions it is extremely important that the carried instruments are reliable, robust, and light. The reason behind the choice of microelectrodes in this case wasn't based solely on the scale of the measurement – the solvent had to be carried to Mars by the vessel in its „wet chemistry cells” –, but also the mass of the payload carried by the vessel.

The „golden age” of ion selective microelectrodes was certainly during the period of 1960 – 1980. One of the most prominent research groups in that time was lead by Professor Pungor. After this period the next big advancement in the field came at the end of the 1990s by better understanding the theory behind the ion selective microelectrodes, and a consequent lowering of their lower detection limit. The lower limit of detection of ion-selective electrodes has usually not been lower than 10^{-6} M. Several research groups have achieved better results recently by optimizations [60]. Lower limit can be achieved by drastically reducing zero-current ion fluxes from the membrane in the direction of the sample [61]. Such ion fluxes have notoriously prevented achieving better detection limits and selectivities with such sensors [62].

The above mentioned models are improvements over the previous, Phase Boundary Model (PBM). This model is assuming local equilibrium between the adjacent phases (aqueous/organic/aqueous) – and therefore throughout the whole system. Equilibrium in charged systems regarding an ion is realized when the electrochemical potential of that ion in the phases of the system is equal. The electrochemical potential of a phase can be given by the equation that was first introduced by Guggenheim [63, 64]:

$$\bar{\mu}_i = \mu_i + z_i F \phi = \mu_i^0 + RT \ln a_i + z_i F \phi \quad (2.12)$$

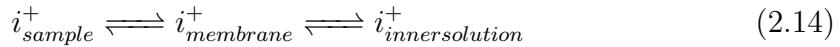
where ϕ is the Galvani potential. The PB model neglects any kinetic parameter, for instance the mobilities of ions. The model is summarized by the following equation:

$$E_{PB} = \frac{RT}{z_i F} \ln k_i + \frac{RT}{z_i F} \ln \frac{a_i(aq)}{a_i(org)} \quad (2.13)$$

where $a_i(aq)$ and $a_i(org)$ are the activity of ion i in the aqueous and the organic phase, z_i is its charge. k_i is a function of the relative free energies of solvation in both the sample and the membrane phase [65].

To account for the influence of kinetic parameters in a wide range of phenomena involving charged particles – including the behaviour of ion selective electrodes –, the Nernst-Planck-Poisson (NPP) model [66–68] can be used. This model successfully accounts for several parameters of ion selective electrodes, including their selectivity

[69] and lower detection limit [70]. The model has recently been adopted for the theoretical description of ion selective electrodes employing neutral ionophores by Lewenstam et al. [71]. The description therein is an improvement of the NPP model. Besides the transport of ion i^+ between the three phases:



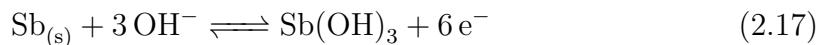
the reaction between the measured ion and the ligand – complexing the ion – is considered as well:



Previously this reaction has been regarded infinitely fast. However by considering this process, a more accurate model can be obtained. The rate of this reaction can be an additional factor determining the response characteristics of an ion selective microelectrode.

2.1.5 Metal/metal-oxide pH microelectrodes

Since the glass electrode cannot be effectively miniaturized due to the reasons detailed in the previous sections, intensive research has been conducted for several decades to improve metal/metal-oxide electrodes. One of the most often used type of these is the Ir/IrO₂ electrode [44]. The oldest is certainly the Sb/Sb₂O₃ electrode, its initial characterization dating back to 1923 [72]. It is based on the equilibrium between antimony and the antimony-oxide on its surface. It is pH sensitive because hydrogen ions participate in the equilibrium:



Using the Nernst-equation to describe the relationship between [Sb³⁺] and the measured electrode potential [73]:

$$E = E^\theta - \frac{RT}{3F} \ln a_{\text{Sb}^{3+}} \quad (2.18)$$

Which can be rewritten by using K_W , the water ion product, and K_L , the solubility product of antimony hydroxide as [73]:

$$E = E^\theta - \frac{RT}{3F} \ln \frac{K_L}{K_W} + \frac{RT}{F} \ln a_{\text{H}^+} = E^{\theta'} - \frac{RT}{0.4343F} \text{pH} \quad (2.19)$$

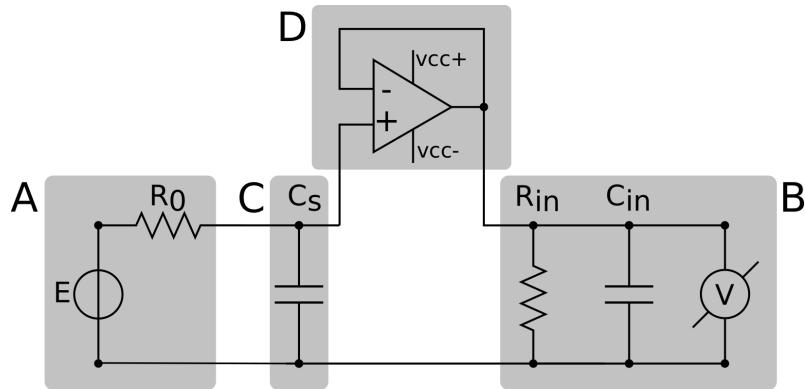
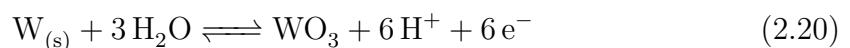


Figure 2.5: The model of the potentiometric measurement. The circuit is constituted by 4 parts: (A) voltage source, the potential difference between the reference and the measuring electrodes with an R_0 output resistance. (B) The measuring circuit, which can be split into 3 elements: a voltmeter, a resistance R_{in} to account for current flowing through the terminals of the voltmeter, and an input capacitance C_{in} . (C) The electrical connection between the voltage generator and the measuring circuit, with a capacitance C_s . (D) Unity gain current buffer built from an operational amplifier in the non-inverting voltage follower configuration.

because $[\text{Sb}^{3+}] = [\text{H}^+] \cdot K_L / K_W$.

The main reason this particular electrode is so popular is that the melting point of antimony and the softening point of borosilicate glass are similar ($T_{m,\text{Sb}} = 630.63^\circ\text{C}$, $T_{m,\text{glass}} \approx 700^\circ\text{C}$), and manufacturing them is relatively easy with standard glass blowing techniques.

Another very popular metal/metal-oxide electrode used for pH measurements is the tungsten electrode. Its function is also based on the equilibrium between the metal and its oxide:



2.1.6 The potentiometric measurement

The generation and measurement of the voltage in the potentiometric cell are closely related. Unfortunately, as with any other technique, the measurement itself influences the investigated system, and therefore the measured value. This effect is especially strong in potentiometry. Fig. 2.5 shows the circuit diagram of the generation and measurement of the voltage. First it will be discussed as if the amplifier wasn't present in the circuit. Without the amplifier, it can be split into three parts [74]:

(A) *Source of the voltage.* The potential difference V is developed across the output of an ideal voltage source E in series with a large output resistance R_0 . In the potentiometric cell, R_0 is the resistance of the measuring electrode, and E

is the potential of the measuring electrode with respect to the reference electrode. Although E is regarded perfect in this model, and its voltage is independent of the current drawn, the output voltage V is smaller than E , because of the ohmic drop $iR_0 = E - V$. Since the resistance of a microelectrode can be in the range of mega-, or even gigaohms, very large errors may result from very small currents.

(B) *The measuring circuit* consist of three elements. The first element is the voltmeter V with infinitely large input impedance. It draws no current, since $i = U/\infty = 0$. It doesn't have any input capacitance (C_{in} is modeled separately), therefore it responds to the input voltage without any delay. The second element is a resistance R_{in} to account for the imperfection of real voltmeters, the current flowing through its terminals as a consequence of the potential difference between them. The third element is the input capacitance of the voltmeter, modeled by the capacitor C_{in} . The current flowing through R_{in} is $i_{R_{in}} = V/R_{in}$. It equals to the difference between the input and the output of the circuit, the error of the measurement of E :

$$E - V = i_{R_{in}} R_0 = \frac{R_0 V}{R_{in}} \quad (2.21)$$

The ratio of the two can be calculated by the formula for the voltage divider:

$$\frac{V}{E} = \frac{R_{in}}{R_0 + R_{in}} \quad (2.22)$$

Input resistance R_{in} of a typical voltmeter is in the range of $1 - 10 \text{ M}\Omega$. This relatively low resistance can cause a large distortion, because $R_{in}/(R_0 + R_{in})$ approaches 1 only if R_{in} approaches infinity, or R_0 approaches zero. Since R_0 is a given property of the circuit, the only way the error can be lowered is by increasing R_{in} . For example, the input resistance of a microelectrode amplifier is about $10^{12} \Omega$, and of a pH meter $\sim 10^{14} \Omega$. Based on Eq. 2.21 it is very important that $R_{in} \gg R_0$ to minimize the error in potential measurements. The effect of input capacitance C_{in} is discussed in the next section (*Response characteristics*).

(C) *The connection* between the voltage source E and the measuring instrument V . This element influences the measurement in two ways. First, it delays the voltage across V compared to E , the effect which is detailed in the next section (*Response characteristics*). The other effect is a consequence of a very small current, induced by stray capacitance. The cable between E and V acts as the plate of a capacitor. The other plate can be anything in the environment. If the capacitance of the element constituted by these two plates changes – by objects moving around in the environment, or charge transfer occurring – small current will flow through the cable. Since the overall resistance of the circuit is quite high due to the measuring microelectrode, even if very small currents are induced by the stray capacitance, large amount of

noise can be added to V , because $V = iR_0$. This effect can be minimised by using shielded cables to decrease stray capacitance, and using as short connections between the high impedance elements and the amplifier as possible. Stray capacitance of a typical shielded (braided) cable is $\sim 100 - 200 \text{ pF/m}$.

(D) *Operational amplifiers* are used to solve several of the issues described above. They are introduced between the measuring electrode and the measuring circuit as seen in Fig. 2.5. The operational amplifier is used as a *unity gain current buffer*. It is achieved by connecting the output of the amplifier to the inverting input. In this configuration, the output is tied back to the inverting input, while the potential to be measured (with respect to ground) is connected to the non-inverting input. Since the operational amplifier does everything it can to keep the two inputs at the same voltage, and one of the output is fed back to one of the inputs, the output will be the same as the other input. The name of this circuit is *non-inverting voltage follower*. It comes from the fact that the output V_{out} follows V_{in} , and the sign of the two equal, as opposed to the inverting configuration, when $V_{out} = -V_{in}$. In other words, the circuit has unity ($\times 1$) gain: it does not amplify potential difference. The reason this circuit is used as an interface between the high impedance source and the low impedance measuring circuit is that because of its high input impedance, it draws no current from the source. Therefore there is no loading error on its high impedance side. On the other hand, they have a low output impedance, and can drive the measuring instrument, with minimal R_0 of their own, and therefore there is no loading error on the low impedance side either. The input impedance of a typical opamp used for this purpose is around $1 - 10 \text{ T}\Omega$, so $R_{in}/(R_{in} + R_0)$ is unity, and the measured V is almost identical to the source E , because V/E is also 1.

2.1.7 Response characteristics

2.1.7.1 Possible contributors determining the potentiometric response

There are several steps constituting the potentiometric response that can be responsible for a delay:

1. Transport of the measured ion to the sensitive surface.
2. Flux of the measured ion through the phase boundary.
3. Complexation reaction between the measured ion and its ligand.
4. RC delay.

Usually only one of these can be observed in the response of a particular type of electrode. That is because that one process – called the rate determining step – is

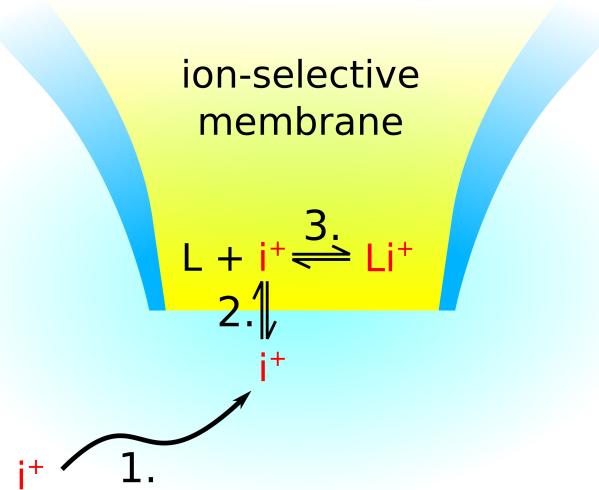


Figure 2.6: The possible contributors to the delayed response of the potentiometric cell. 1) Transport of the measured ion to the sensitive surface. 2) Flux of the measured ion through the phase boundary. 3) Complexation reaction between the measured ion and its ligand.

much slower. Figure 2.6. illustrates steps 1–3. During the first step, the measured ion has to be transported to the phase boundary. Depending on whether there is stirring or not, this can either be realized by convection and diffusion, or diffusion alone. In cases where this step is the rate determining, stirring should decrease the response time of the cell.

In the second step, the ion has to cross the phase boundary between the sample solution and the ion-selective membrane. The lower the activity of the measured ion in the sample, the lower this flux will be. In the case of an ion-selective micropipette employing a neutral ionophore, the next step is the complexation reaction between the ion and the ligand. This step has already been mentioned previously in section 2.1.4, more specifically by Eq. 2.15. If the concentration in the membrane is constant, this reaction can be regarded a first order reaction, and as such its behaviour can be described by the function e^{-kt} , k being the rate constant.

And finally, there is an RC delay associated with the potentiometric cell, described in the next section.

2.1.7.2 RC delay

In this section the response delay associated with the RC time constant is considered. Because the RC time-constant plays a central role in my thesis, I give a detailed derivation of it here. The potentiometric cell can be modeled as a series

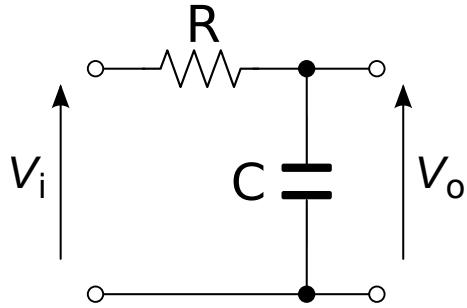


Figure 2.7: The series RC circuit.

RC circuit (Fig. 2.7). Kirchhoff's second law states that the directed sum of the electrical potential differences (voltages) around any closed network is zero [75]:

$$\sum_{k=1}^n V_k = 0 \quad (2.23)$$

where n is the total number of voltages measured across the loop. This must be true for the energy to be conserved. Using Ohm's law to express the voltage across the resistor as iR and Kirchhoff's second circuit law on the series RC circuit, we get:

$$V_{in} - iR - V_{out} = 0 \quad (2.24)$$

where i is the current flowing through any two points of the circuit clockwise. Since i is nothing but the change of charge in time, $i = dq/dt$, and $V_{out} = q/C$, Eq. 2.24 can be rewritten as

$$V_{in} - \frac{dq}{dt}R - \frac{q}{C} = 0 \quad (2.25)$$

This can be rearranged to

$$\frac{dq}{dt} = \frac{1}{R} \left(V_{in} - \frac{q}{C} \right) \quad (2.26)$$

After cross multiplication we get

$$\frac{dq}{V_{in} - \frac{q}{C}} = \frac{dt}{R} \quad (2.27)$$

Rearranging it leads to

$$\frac{dq}{q - CV_{in}} = -\frac{dt}{RC} \quad (2.28)$$

To get q as a function of t , we need to integrate. At $t = 0$ the capacitor is not charged, so $q = 0$. Then, as we apply the voltage V_{in} , the capacitor slowly starts charging, until we arrive at a charge q :

$$\int_0^q \frac{dq}{q - CV_{in}} = \int_0^t -\frac{dt}{RC} \quad (2.29)$$

or

$$\ln(q(t) - CV_{in}) \Big|_0^q = -\frac{t}{RC} \Big|_0^t \quad (2.30)$$

After solving we get

$$\ln \left(\frac{q(t) - CV_{in}}{-CV_{in}} \right) = -\frac{t}{RC} \quad (2.31)$$

If we raise both sides to the natural exponent, we get

$$\frac{q(t) - CV_{in}}{-CV_{in}} = e^{-t/RC} \quad (2.32)$$

Solving for $q(t)$:

$$q(t) = CV_{in}(1 - e^{-t/RC}) \quad (2.33)$$

Since the voltage across the capacitor is $V_{out} = q/C$, dividing both sides by C leads us to

$$V_{out}(t) = V_{in}(1 - e^{-t/RC}) \quad (2.34)$$

This is the general expression to the voltage across a charging capacitor at any time instance t . To find the expression for the voltage when the capacitor is discharging, very much the same way we get:

$$V_{out}(t) = V_{in}e^{-t/RC} \quad (2.35)$$

RC is the time constant of the series RC circuit, denoted as τ in general. Observing Eqs. 2.34-2.35, it is the time that it takes to charge the capacitor by 63.2% ($1 - e^{-1} = 0.632$), or to discharge it by 36.8% ($e^{-1} = 0.368$). Fig. 2.8 shows the response to a *Heaviside step-function* input. After about $5 \times RC$, the output voltage practically reaches the input voltage (99+%). It is useful to note the relation between the 95% response time $t_{95\%}$ and the time constant. In $3 \times RC$ time, the capacitor is charged by about 95%, therefore $t_{95\%} \approx 3 \times RC$.

To make Eqs. 2.34-2.35 useful in electrochemistry, we need to further modify

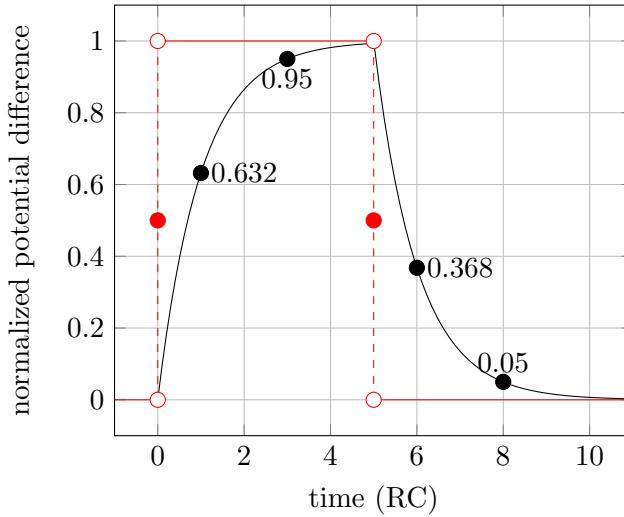


Figure 2.8: Charging and discharging the series RC circuit. Red: normalized input voltage (V_{in}) to the series RC circuit, two consecutive *Heaviside step functions*, the second one is inversed and shifted $5RC$ to the right. Black: normalized output voltage (V_{out}) of the series RC circuit.

them. In potentiometry, the important parameter is the potential of the measuring electrode. We always speak in terms of electrode potential, but it must be born in mind that it is measured with respect to the reference electrode, hence it is always a potential difference. But since we will take the difference between these differences as well, we just use the expression *potential* to refer to the state of the potentiometric cell at any time instance t . In the generalized expression we substitute V_{out} for $E_{cell}(t)$, and V_{in} for $E_{cell}(\infty)$. Also, it is useful to generalize it for changes starting, and ending at any potential value, not just 0 or E_{out} . After these generalizations, from both equations we get:

$$E_{cell}(t) = E_{cell}(\infty) + [E_{cell}(0) - E_{cell}(\infty)]e^{-t/RC} \quad (2.36)$$

This equation [76] will be modified later in the thesis to estimate $E_{cell}(\infty)$ based on the other variables.

2.1.8 On the use of the expression „equilibrium”

Throughout my dissertation I use the expression *equilibrium* to describe a steady potential difference between the two terminals of the cell, the electrical contact of the measuring and the reference electrodes. However, this state of course cannot be regarded an equilibrium, since given enough time, the potential difference will reach zero eventually. The resistance of the whole cell is finite, and if there is a potential difference between any two points in the cell, current will flow. Two phenomena have

to be distinguished. The first is the electrochemical process, which is in equilibrium *only* if cell potential difference have reached zero, i.e. the cell is depleted. The other process is the charging or discharging of a capacitance modeled by C in Fig. 2.7. This is the total capacitance of the measuring system, including the capacitance of the cables, and the amplifier input as well. If we accept the model described in the previous section, this can be regarded a purely physical process, which is in true equilibrium if the voltage across the capacitor C is the same as the voltage of the input ($V_i = V_o$). This state is what I refer to by equilibrium.

It must be kept in mind however, that the source of the potential difference in fact *does* change over time for a given electrolyte composition as a consequence of the very small current flowing through the cell (fA range). Therefore it is not an equilibrium, only a steady state.

2.2 Scanning Electrochemical Microscopy

2.2.1 Origins of the technique

Scanning Electrochemical Microscopy (SECM) is a branch of the Scanning Probe Microscopic techniques (SPM), of which the first was the Scanning Tunnelling Microscopy (STM), invented by Binnig and Rohrer in 1982 [77] building on their previous studies of controlled vacuum tunnelling published in 1981 [78, 79]. They received the Nobel Prize in 1986 „*for their design of the scanning tunneling microscope*”. It was a revolutionary technique, the first of its kind, and a pioneer for the other scanning techniques that followed. STM is capable of incredible resolution, down to the atomic scale. Optical techniques do not have the resolving power to distinguish details at the atomic level, since they are limited by the wavelength of photons [80]. For instance, wavelength of visible light is in the range of 390 – 700 nm, while the atomic radii range from 30 pm to 300 pm. On the other hand, the probes used in STM are extremely sharp, usually just a few atoms at their tip. There is a potential difference between the tip of the probe and the sample. As a consequence, a small current will flow between them. The magnitude of this current depends on the probe – sample distance. The image is created by plotting the registered current as a function of the spatial coordinate of each measurement.

The next SPM technique, the Atomic Force Microscopy (AFM), was introduced not long after, in 1986 by Binnig [81, 82]. He writes in [81]:

„The atomic force microscope is a combination of the principles of the scanning tunneling microscope and the stylus profilometer. It incorporates a probe that does not damage the surface. Our preliminary results in air demonstrate a lateral resolution of 30 Å and a vertical resolution less than 1 Å. ... We envision a general-purpose device that will measure any type of force; not only the interatomic forces, but electromagnetic forces as well.”

Indeed, since its invention, AFM has found many applications, and became an invaluable tool of surface analysis. After these two techniques were established, many more SPM variants followed in a relatively quick succession. Here a few are mentioned in chronological order:

- MFM, magnetic force microscopy (1988) [83]
- SICM, scanning ion-conductance microscopy (1989) [84]

- BEEM, ballistic electron emission microscopy (1990) [85]
- EFM, electrostatic force microscopy (1991) [86]
- KPFM, kelvin probe force microscopy (1991) [87]
- SHPM, scanning Hall probe microscopy (1992) [88]
- SThM, scanning thermal microscopy (1994) [89]
- SVM, scanning voltage microscopy (1998) [90]

The electrochemical version of SPM, the Scanning Electrochemical Microscope (SECM¹) was introduced in 1989 by Allen J. Bard [91], „*the father of modern electrochemistry*”, main author and editor of the monography about SECM [92]². It must be mentioned however, that the notion of spatially resolved chemical information was first proposed by Engstrom, three years earlier, in 1986. He published a paper about measurements with a microelectrode in the diffusion layer of another electrode, using a bipotentiostat and a micro-manipulator [94]. He writes in 1989 [95] referring to his 1986 paper [94]:

„The concept behind what has come to be called SECM was first demonstrated in 1986, when microelectrodes were used to amperometrically detect chemical species produced at a specimen electrode.”

But the term „*Scanning Electrochemical Microscope*” was coined by Allen J. Bard, and he and his coworkers generalized the idea to three dimensions, and layed down the foundations and theory of the technique.

The two main variants of the technique are the amperometric and the potentiometric modes. For the first few years, the SECM was only used in amperometric mode. The next step towards obtaining true chemical information, not just surface topography and conductivity, was the combination of potentiometry and the SECM. Although several papers have been published already about spatially resolved potentiometric scans, the first potentiometric SECM images appeared on the pages of the paper of Horrocks and Bard written in cooperation with my doctoral supervisor, Professor Géza Nagy [96]. I used very similar antimony microelectrodes as SECM probes to measure local pH throughout my work, and prepared them in the same way as described in that paper.

¹The acronym „SECM” is used for referring to both the technique (Scanning Electrochemical Microscopy) and the instrument itself (Scanning Electrochemical Microscope).

²Recently, a new version of the book has been published [93].

2.2.2 Potentiometric SECM

The potentiometric probe is passive, it does not generate or collect, and it can be described as „*substrate generates / substrate collects – tip detects*” staying with the original naming scheme. In this mode, similar to the other modes, the probe is scanned through the points of a raster grid (Fig. 2.9). But instead of an amperometric measurement, the potential of the probe is measured against a reference electrode, immersed in the same electrolyte at a fixed location. For the reasons detailed in the section „The potentiometric measurement”, a voltage follower is introduced between the electrometer and the measuring electrode. The first complete work featuring potentiometric SECM images were published in 1993 [96]. In that work, the authors successfully measured pH on a microscale with an antimony microelectrode.

Later, potentiometric SECM found an application in corrosion science. Researchers in that field are curious about the concentration of certain ions in the electrolyte adjacent of the corroding sample. Ion-selective electrodes and the SECM are good tools to study the dissolution of these ions. Concentration profiles of zinc [97], magnesium [98–100] and hydrogen ions [98] were recorded by several research groups.

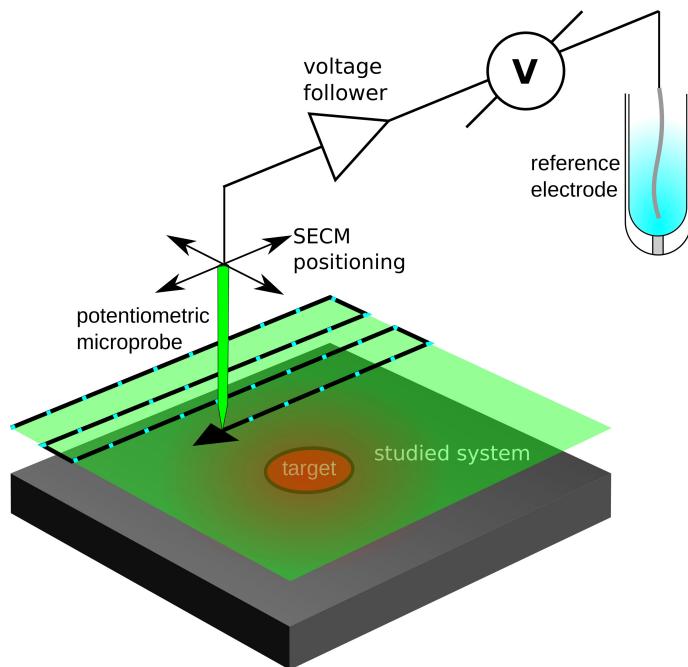


Figure 2.9: A typical potentiometric SECM setup. The probe is scanned through the points of a 2D raster at a constant height above the studied surface. The probe is stopped at every sampling points (here blue dots), and the potential against a reference electrode is recorded. For potentiometric microelectrodes, the use of a voltage follower is necessary to avoid loading error and reduce noise.

2.2.3 Distortion and image processing in SECM

Signal processing techniques has been widely used in optical microscopy [101], and in scanning probe microscopy to decrease imaging distortion. Distortion is any difference between the obtained image and reality. It is caused by the imperfection of the measuring system, which can be modeled as a measurement transfer function, or convolution function F , such that the output $y(t)$ can be written as a function of the input x as

$$y(t) = F(x(t)) \quad (2.37)$$

If F is known, the inverse function F^{-1} can be found and used as deconvolution function.

There are many sources of SPM imaging distortion. In atomic force microscopy, and scanning tunnelling microscopy, it is usually a consequence of the tip-sample interaction, causing the various artefacts [102]. Broadening of nanometer-scale features by up to three times is a common occurrence in STM [103]. The deconvolution function in this case is closely related to the geometry of the tip and its angle compared to the sample. If these are known, image restoration is possible by deconvoluting in the spatial domain [104–106]. Time, and frequency domain deconvolution is also commonly used in SPM techniques to remove time-dependent image artefacts, usually caused by the relatively long response time compared to scanning speed [107].

Deconvolution of images obtained with the scanning electrochemical microscope has also been reported by the Bard group [108]. In that work, amperometric images have been restored (deblurred) by a linear combination of Laplacian and Gaussian filtering. The main source of distortion in amperometric SECM imaging is the feature broadening caused by diffusion. The deconvolution function was derived from Fick's law of diffusion, and used as a calculation kernel to cycle through the data points of the 2D raster and obtain the deblurred image.

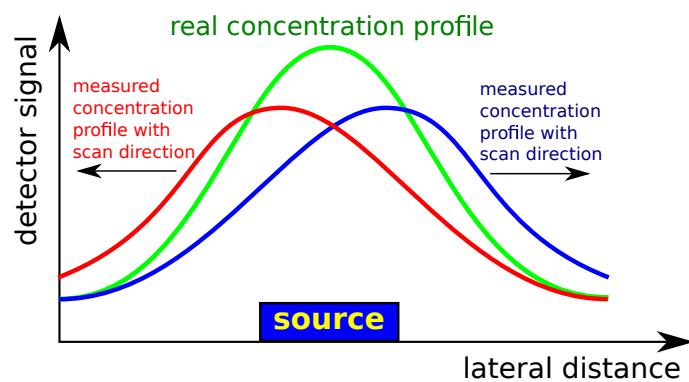


Figure 2.10: The distortive effect of potentiometric SECM imaging when scanning at relatively high speed. The effective speed of the probe is too high, and therefore the time available for the potentiometric cell is too short to reach equilibrium before recording the potential difference at a given point. The image is blurred along the scan line in the direction of the scan.

Chapter 3

Materials and Methods

3.1 Ion-selective microelectrodes

I used two kinds of ion-selective microelectrodes in my thesis: metal/metal-oxide microelectrodes and ion-selective micropipette electrodes. To measure pH on a microscale, I used metal/metal-oxide type microelectrodes. They are based on the equilibrium between the metal and their oxide. Hydrogen ions participate in the equilibrium, therefore the electrode potential will shift when pH changes. The ion-selective micropipettes on the other hand, are based on the ionophores, which are specific to certain ions, ensuring their selectivity. If an ion-exchange membrane is prepared with a particular ionophore, the crossmembrane potential depends only on the activity of the particular ion which the ionophore is selective to. I used several types of ion-selective microelectrodes as SECM measuring tips. For pH-microscopy, I used an antimony and tungsten microelectrodes. To map local K^+ and Mg^{2+} ion concentration, I used ion-selective micropipette electrodes with the appropriate ion-selective cocktails. I used traditional liquid-contact micropipettes, and new, low resistance solid contact micropipettes as well.

3.1.1 Preparation of the microelectrodes

3.1.1.1 Metal/metal-oxide electrodes

Antimony pH-sensitive microelectrode The antimony microelectrode fabrication process is based on the original work of Bard [96]. To create such electrodes, antimony powder (Szkarabeusz, Pécs, Hungary) was melted in a ceramic crucible over a Bunsen burner. Then the molten antimony was pulled into a thick walled borosilicate glass tube ($d_i=2$ mm, $d_o=10$ mm) by applying vacuum using an aspirator on the back opening of the tube. In this way, a continuous column of solid antimony was sealed into the glass tube. Then, the glass tube with the antimony in-

side was melted again. Since the melting points of antimony and the softening point of the borosilicate glass are very similar, they could be pulled together with standard glass blowing techniques. After the glass became soft, an antimony containing portion of it was suddenly pulled using tweezers. With this method, very fine, glass-sealed antimony microwires could be obtained. After this step, the diameter of the antimony wires was typically around $30\text{ }\mu\text{m}$. If it was necessary, the microwires were pulled even further with a vertical puller (Sutter Instrument, 1 Digital Dr, Novato, CA 94949). After the pulling stage, the wires were broken into pieces with a length of $3 - 4$ centimeters. Then, they were investigated under an optical microscope to select pieces with a continuous antimony wire inside. Due to the fragile nature of these microelectrodes, they often broke, and several of them were used through the course of my work. The diameter of the antimony microelectrode used in a particular experiment is always specified in the discussion of that experiment. To make electrical contact between the measuring instruments and the antimony microwires, a thin copper wire was glued to the glass shielding of antimony wire with conductive silver-epoxy (Amepox Microelectronics, Ltd. 90-268 Lodz Jaracza, Poland), making sure that the epoxy also covered the exposed antimony wire. After curing the conductive glue for 1 hour at a temperature of $200\text{ }^{\circ}\text{C}$, the antimony microelectrodes were ready. Then the whole assembly was inserted into an empty glass capillary ($d_i = 1\text{ mm}$). The remaining space in the capillary was filled with regular epoxy. This last step increased the mechanical stability of the microelectrode. All electrodes were tested before usage by calibration in three buffer solutions ($\text{pH} = 4, 7, 10$).

Antimony pH-sensitive combined macroelectrode Home-made antimony/silver combined macroelectrodes were used to study the effect of stirring on the delay in potentiometric measurements with antimony electrodes in general. To make these electrodes, copper wires were soldered to one end of a $\sim 5\text{ mm}$ long silver and antimony wires ($d = 1\text{ mm}$). Antimony wires with such diameter were made by pulling molten antimony into a $d_i = 1\text{ mm}$ glass capillary, the same way that is described in the previous section. Then, the glass was broken to acquire the antimony wire, which was then trimmed to $\sim 5\text{ mm}$ length.

Both solder joints were strengthened mechanically by small segments of heat-shrink tubes. The obtained electrodes were carefully pushed down into a glass tube ($d_o = 5\text{ mm}$, $d_i = 4\text{ mm}$) until they both reached the end of the glass tube. Then, the remaining space in the tube was filled with non-conductive epoxy resin. Finally, after the resin was cured, the end plate was sanded down to 4000 grit, and polished on three different fiber cloths (Buehler), containing alumina slurry with decreasing particle size; $1\text{ }\mu\text{m}$, $0.3\text{ }\mu\text{m}$ and finally $0.05\text{ }\mu\text{m}$. The endresult is depicted in Fig. 3.1.



Figure 3.1: Home-made antimony/silver pH-sensitive combined macroelectrodes. Left side: top view of two examples, right side: front view, displaying the antimony and silver electrodes. This type of electrode was used to investigate the effect of buffer stirring on response time.

Tungsten pH-sensitive microelectrode Since tungsten has the highest melting point of all the elements ($3422\text{ }^{\circ}\text{C}$), the method described in the previous paragraph cannot be used. Instead, tungsten microwire with a diameter of $30\text{ }\mu\text{m}$ (Element-explorer, Montreal, Canada) were sealed into a borosilicate glass capillary ($d_i = 1.12\text{ mm}$, $d_o = 2\text{ mm}$, no filament, World Precision Inc., Sarasota, Florida, USA). To seal the microwire, one end of the capillary was closed with flame. Then, a 1 cm long tungsten microwire was inserted from the other end, and pushed down to the sealed end. The sealed end was melted again while vacuum was being applied from the open end. The capillary was kept in the flame until $4 - 5\text{ mm}$, about half of the microwire was sealed into the glass. To make electrical contact between the microwire and the measuring instruments, a small piece of solder was inserted into the capillary. The solder was melted in flame, and pushed down to the sealed end of the capillary by a sudden shake of the wrist. While the solder was still melted, a copper wire was inserted into the solder. After the solder had cooled down, the electrodes were ready to be used. Microelectrodes with $30\text{ }\mu\text{m}$ tungsten filaments from a 100 W Tungsram incandescent lightbulb were also prepared, using the same method. Fig. 3.2 shows the tip of the finished tungsten microelectrodes.

3.1.1.2 Micropipette ion-selective electrodes

To prepare the ion selective microelectrodes, micropipettes were prepared by pulling borosilicate glass capillaries B100-50-10 (Sutter, Novato, CA, USA). The glass capillaries were first cleaned from organic contaminants with „piranha solution”, then thoroughly washed with deionized water and isopropyl alcohol, and dried in oven at $105\text{ }^{\circ}\text{C}$. Micropipettes were pulled from the capillaries by using a vertical pipette puller (Sutter Instruments, type P-30, Novato, CA, USA). The surface of the micropipette tips were hydrophobized by exposing them to dimethyldichlorosilane

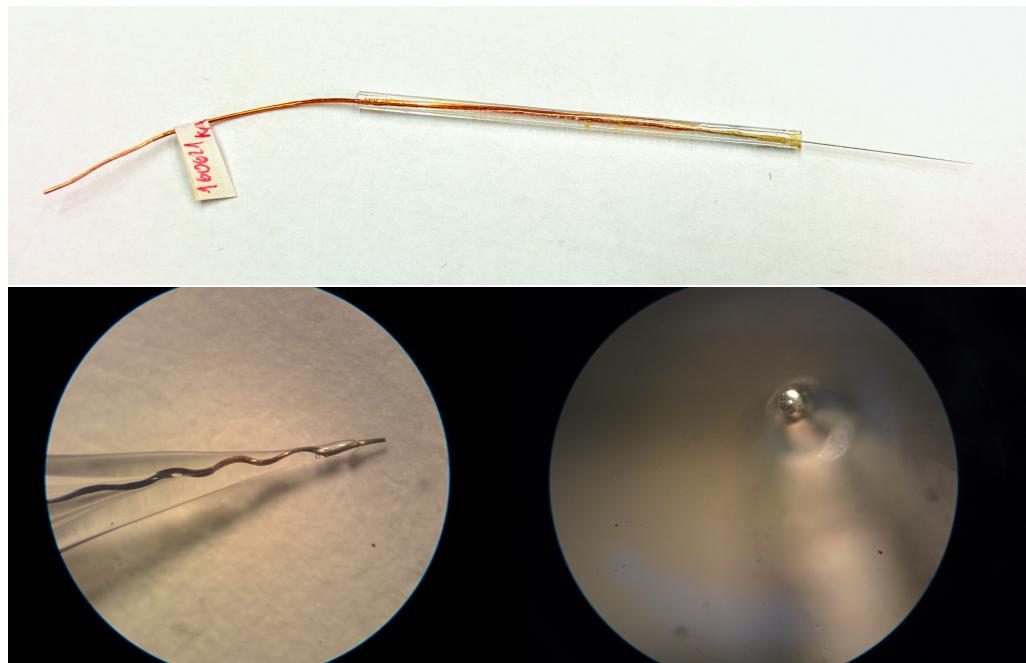


Figure 3.2: Antimony and tungsten microelectrodes for local pH measurements. Side view of the microelectrodes prepared from commercial 30 μm tungsten microwires (C) and from 100 W Tungsram filaments (D). Front view of the same electrodes (C and D).

in a closed Petri dish. 200 μm of dimethyldichlorosilane was pipetted into a Petri dish that contained 20 micropipettes. Then, the Petri dish was put in an oven at a temperature of 200 °C for 30 minutes. The ionophore cocktail was front filled into the micropipette tip under vacuum applied at the back side. The vacuum was provided by a 20 ml syringe, that was connected to the capillary with silicone tubing. Two kinds of ionophores were used. Bis-N,N-dicyclohexyl-malonamide – synthesized at the Budapest University of Economics and Technology [109] – and valinomycin – purchased from Sigma-Aldrich – for Mg^{2+} , and K^+ , respectively. Selectivity coefficients of the Mg^{2+} ionophore toward several different ions, including Na^+ and H^+ ions, are available in [109]. The composition of the ion selective cocktail is detailed in Table 3.1. All components in the ionophore cocktail were purchased from Sigma-Aldrich (St. Louis, MO), except the Mg^{2+} ionophore. After the cocktail was introduced into the tip of the micropipettes, it was cured for 24 hours in a closed Petri dish, to allow the THF to be slowly evaporated.

Liquid-contact ion-selective microelectrodes For the liquid contact version, an internal solution was backfilled with the assistance of a microsyringe. This step required great patience, as the inner surface of the pipettes was previously hydrophobicized – for reasons explained in 2.1.3 –, which made it extremely difficult to eliminate

Table 3.1: Composition Mg^{2+} and K^+ ion selective cocktails to create the membranes in the microelectrodes. As ionophore, either bis-N,N-dicyclohexyl-malonamide or valinomycin was used.

Component	Quantities for 200 μL of the mixture	
	Content	wt%
Tetrahydrofuran (THF)	100 μL	-
Poly(vinyl chloride) (PVC)	7.68 mg	5.06
bis-N,N-dicyclohexyl-malonamide	2.23 mg	1.47
valinomycin	2.23 mg	1.47
Potassium tetrakis(4-chlorophenyl)-borate (PTCB)	2.13 mg	1.40
2-nitrophenyl octyl ether (oNPOE)	139.79 mg	92.07

the small air bubble that was trapped between the membrane and the filling solution. The internal filling solution was 10 mM $MgCl_2$ and 0.25 M KCl in the case of a Mg^{2+} ion-selective electrode, and 10 mM KCl for a K^+ ion-selective electrode. The internal reference electrode for both liquid contact electrodes was a chlorinated silver wire. To chlorinate silver wires, they were submerged into 1 M $FeCl_3$ solution for a few seconds, and cleaned from traces of Fe^{3+} with cc. HCl. Schematic diagram and close up picture of the liquid-contact ion selective microelectrode are shown in Fig. 3.3A.

Solid-contact ion-selective microelectrodes The solid-contact ion-selective microelectrodes were built using the same components employed for the fabrication of the conventional ISME, except in this case instead of the internal solution and chlorinated silver wire, the ion-to-electron interface was provided by PEDOT (poly(3,4-ethylenedioxythiophene)) polymerized onto a 33 μm diameter carbon fiber, a generous gift from Specialty Materials Inc. (1449 Middlesex Street Lowell, Massachusetts 01851). The modified carbon fiber was pushed from the back opening of the pipette as close to the orifice as possible to minimize the thickness of the membrane between the solid contact and the sample, and therefore electrode resistance [56]. A micrograph of the resulting microelectrode is depicted in Fig. 3.3B.

Preparation of the solid contact A copper wire was attached to the carbon fiber trimmed to ~ 35 mm length, using silver-epoxy adhesive, to provide electrical contact. The portion of the fiber to be in contact with the ionophore cocktail was then coated with PEDOT conductive polymer in an electrochemical cell consisting of the carbon fiber as working electrode, a chlorinated, 2 mm thick silver wire immersed in the electrolyte as quasi-reference electrode, and a platinum wire as the auxiliary electrode. The 3,4-ethylenedioxythiophene monomer was dissolved in $BMIM^+PF_6^-$ (1-butyl-3-methylimidazolium hexafluorophosphate) ionic liquid [56].

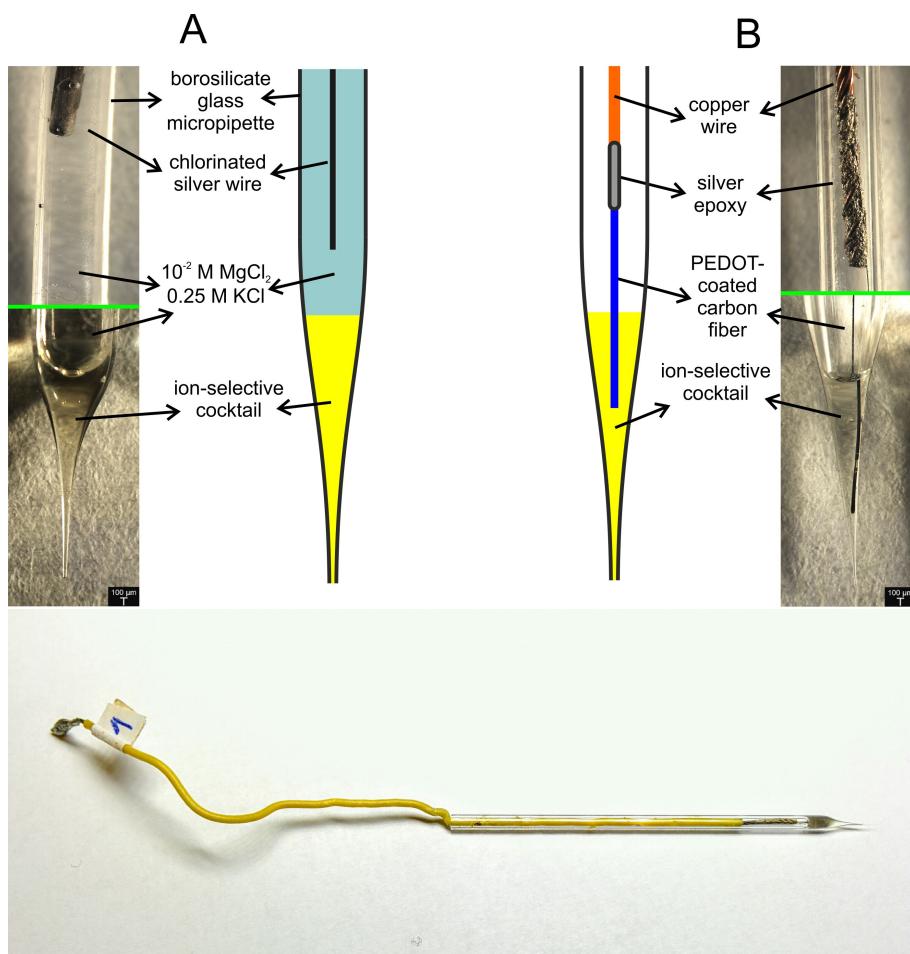


Figure 3.3: Schematic diagram and close up photo of the micropipette electrodes for the selective detection of Mg²⁺ ions. (A) liquid-contact, and (B) solid-contact version. The K⁺ solid contact micropipettes were identical in construction, except the composition of the ion-selective cocktail and the internal filling solution for the conventional electrodes, which was valinomycin, and 10⁻² M KCl, respectively.

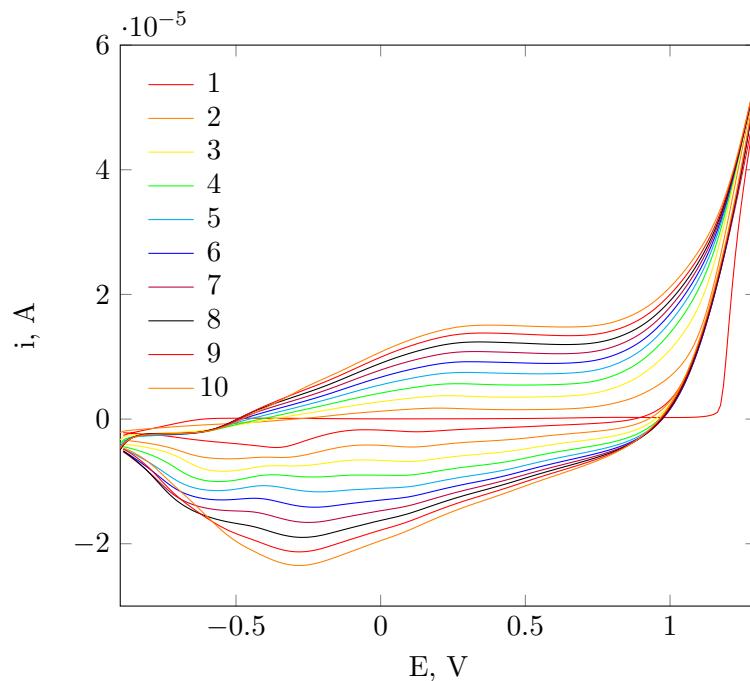


Figure 3.4: Cyclic voltammetric electropolymerization of PEDOT onto the carbon fiber to create the solid internal contact for the ion-selective microelectrodes. Top left inset indicates the order of the consecutive cycles.

Oxygen was purged from the EDOT-solution with nitrogen gas before and during the polymerization. Then, PEDOT was polymerized onto the working electrode with 10 consecutive cycles from -1.0 V to 1.5 V with a scanrate of 100 mV/s (Fig. 3.4).

3.1.2 Instrumentation for the microelectrodes

Microelectrodes have high resistance, therefore, to avoid loading error, some sort of impedance matching is necessary. This is also crucial to minimize noise caused by stray capacitance. Where the measuring apparatus lacked the high input impedance, a TL082 operational amplifier (Texas Instruments, Texas, USA) based unity gain voltage follower was used between the microelectrode and the measuring apparatus. To record the potential difference between the measuring microelectrode and the reference electrode, either one of these instruments were used:

- MeTeX Instruments M-3640D 3 1/2 Digit digital multimeter with the TL082 voltage follower,
- Autolab Electrochemical Workstation (Metrohm, Herisau, Switzerland) with the TL082 voltage follower,

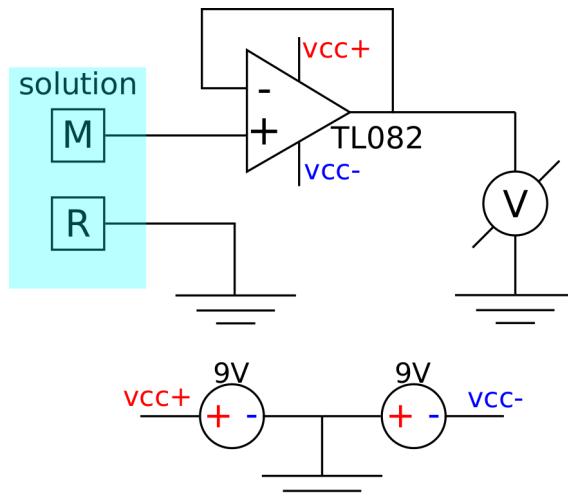


Figure 3.5: The potentiometric cell with the TL082 voltage follower. M: measuring electrode, R: reference electrode, V: voltage meter, $vcc+$ and $vcc-$: positive and negative rail of the power supply for the operational amplifier.

- eDAQ Ecoder 402 Electrochemical Workstation with the eDAQ pH/ISE isoPod (eDAQ Pty Ltd, Australia),
- eDAQ pH/ISE isoPod USB (eDAQ Pty Ltd, Australia),
- Home made, Arduino based DAQ.

A 25 cm long, shielded coaxial cable was used between the amplifier and the microelectrode. Unshielded cable length was always minimized to less than a centimeter, excluding the length of the microelectrode itself. Connection was always provided by BNC connectors. The TL082 operational amplifier was powered by two 9 V batteries, providing ± 9 V, and a convenient ground node (Fig. 3.5).

3.1.2.1 Home-made, Arduino based DAQ

The instrument is based on an DIP30 Arduino Nano, with an ATmega328 microcontroller (5V, 16MHz, Arduino AG, 2016, www.arduino.cc). A Texas Instruments ADS1115 16 bit analog-digital converter was connected to the microcontroller board through I²C interface. A virtual ground between 0 and 5 V was established by a voltage divider circuit. The virtual ground was driven by an OPA342 low voltage, rail-to-rail, high input impedance operational amplifier, provided by Texas Instruments as a generous gift. The virtual ground was connected to the reference electrode, and one of the differential inputs of the AD1115. The measuring electrode was connected to the other differential input through a TI TL082 high input impedance operational amplifier. The recommended supply voltage for this amplifier is ± 18 V, but it worked

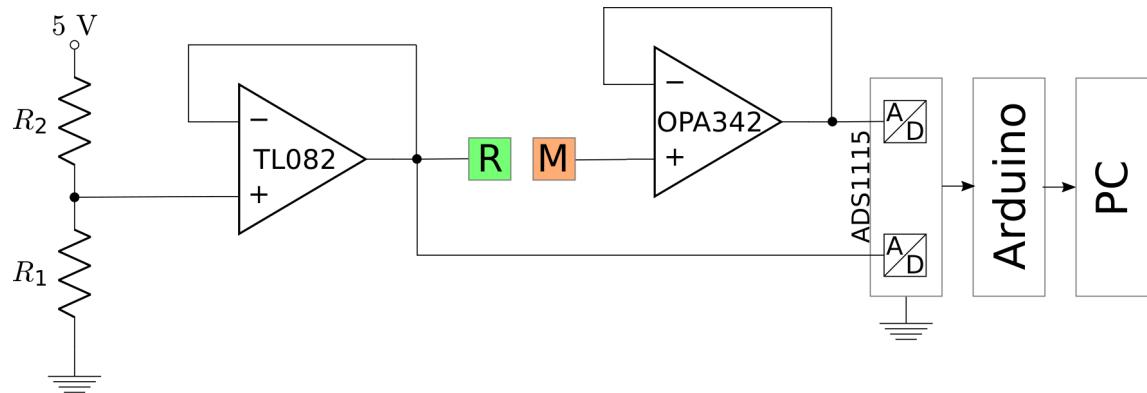


Figure 3.6: Circuit diagram of the home-made Arduino-based DAQ. [R] = reference electrode, [M] = measuring electrode. $R_1 = R_2 = 10 \text{ k}\Omega$.

surprisingly well with the ± 2.5 V provided by the split 5 V of the USB port. The circuit diagram of the instrument can be seen in Fig. 3.6. The microcontroller ran the following program, a modified version of [110]:

```
#include <Wire.h>
#include <I2Cdev.h>
#include <ADS1115.h>

ADS1115 adc0(ADS1115_ADDRESS_ADDR_GND);
float scalefactor = 0.03125;
float time;

uint16_t currentADCreadings;

void setup(void)
{
    Serial.begin(115200);
    Wire.begin();
    adc0.initialize();
    // initialize ADS1115 16 bit A/D chip
    adc0.showConfigRegister();
    adc0.setRate(ADS1115_RATE_860);
    // 860 samples/sec
    adc0.setMode(ADS1115_MODE_CONTINUOUS);
    // continuous sampling
    adc0.setGain(ADS1115_PGA_1P024);
    // 4x gain, +/- 1.024 V, 1 bit = 0.03125 mV, 2.4 MΩ
```

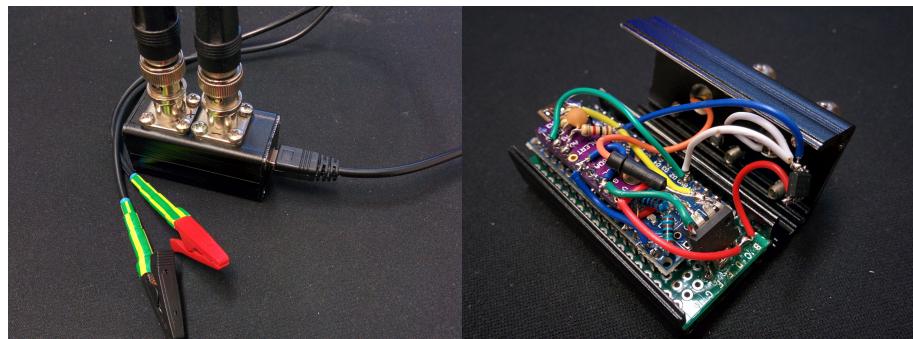


Figure 3.7: The home-made, Arduino based DAQ.

```

adc0.setMultiplexer(ADS1115_MUX_P0_N1);
// sets mux to differential
}

void loop(void)
{
    time = 0.001 * millis();
    currentADCreadings=adc0.getConversion();
    Serial.print(time,4);
    Serial.print(' ');
    Serial.println(adc0.getMilliVolts(),4);
}

```

While on the PC side (running Debian Linux 9.x) the serial port was continuously monitored for incoming data using the terminal client *screen*, which was stored in the file *data.dat*:

```

screen -d -m -S ads /dev/ttyUSB0 115200
screen -S ads -X logfile data.dat
screen -S ads -X log

```

The file was plotted live with the help of GNUPlot:

```

#!/bin/sh
echo set grid
while true; do
    echo set yrang [-1000:1000]
    echo set xlabel "time,s"
    echo set ylabel "E,mV"
    echo plot <<(tail -n -1000000 &&
        data.dat | sed -e '$d' | &&

```

```

sed -e '1_d' \)"\"
with lines lc rgb "\red\" notitle
sleep 1
done

```

The GNU tools *sed*, and *tail* was used to plot the last 1000000 data points only, ignoring the very last data point, which could potentially be incomplete at the time the plotting command is issued.

3.1.3 Characterization of the microelectrodes

3.1.3.1 Calibration

For the micropipette ion-selective electrodes, calibration was performed in $MgCl_2$ and KCl dilution series, ranging from 10^{-6} M to 10^{-1} M. The measuring and reference electrodes were submersed sequentially in each solution from lowest to highest concentration. Potential was continuously measured against an Ag/AgCl/3M KCl reference electrode with a high input impedance eDAQ pH/ISE isoPod USB (eDAQ Pty Ltd, Australia).

Metal/metal-oxide microelectrodes were calibrated by measuring their potential in nine buffer solutions. The typical calibration procedure was performed by introducing the microelectrode in a sequence of buffer solutions initiated with the most alkaline solution. In this way, the tip was exposed to solutions of increasing acidity.

3.1.3.2 Internal resistance

The voltage divider method was used to measure the resistance of the microelectrodes using 1 mM $MgCl_2$ + 1 mM NaCl solution. The electrochemical cell consisted of an Ag/AgCl/3M KCl reference electrode and an ion selective microelectrode as measuring electrode. The measuring electrode was connected to the voltage follower as shown in Fig. 3.8. After a steady reading was achieved, the input terminals of the voltage follower and the reference were connected through a precision resistor R . The experiment was performed with two different precision resistors with values of 0.5 and 1.0 G Ω .

The resistance of the antimony microelectrodes were also measured directly by attaching one probe of a high precision multimeter to the microelectrode, while submersing the other probe and the tip of the microelectrode into a beaker containing mercury.

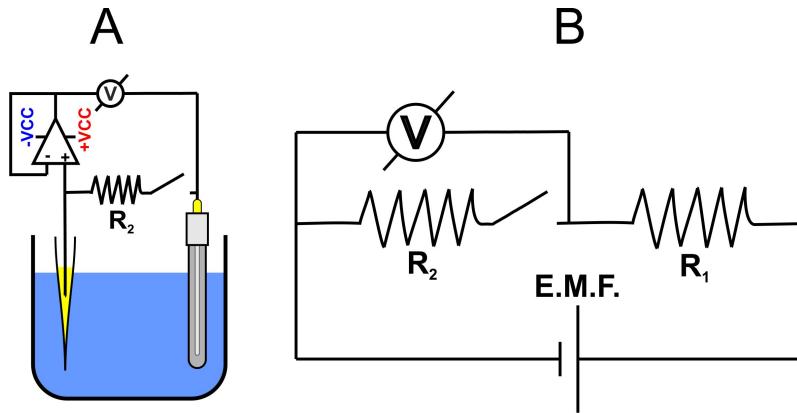


Figure 3.8: Voltage divider circuit to measure electrode resistance. The connection between the measuring and the reference electrodes through R_2 could be turned on and off with a switch.

3.1.3.3 Response time

The response time of the microelectrodes was measured by recording the response to a sudden change in ion activity. The method is based on a modified version of the dual drop cell method [99], called the „*hanging drop method*”. The tip of the measuring electrode was positioned in the close vicinity of the ceramic frit of the reference electrode. Both electrodes were in contact with the same drop of solution, that was hanging from the reference electrode. This arrangement is depicted in Fig. 3.9.

When the equilibrium potential was reached, the first solution was removed. Then, the surface of the second solution – contained in a beaker – was slowly approached to the remaining drop of the first solution that was hanging from the reference electrode, with the help of a laboratory stand with an adjustable height. When the surface of the second solution reached the drop of the previous solution, a sudden jump in ion activity was realized, corresponding to the difference between the ion activities of the first, and the second solution. This method was employed in the response characterization of the antimony microelectrodes.

The response of the antimony/silver combined macroelectrodes were conducted in a similar manner. But in this case, the antimony measuring electrode and the silver quasi reference electrode were embedded in the same epoxy body, therefore the drop that was hanging from the endplate was always in contact with both electrodes.

To measure the response time of the Mg^{2+} ion selective electrodes, they were immersed in a solution of 0.1 M $MgCl_2$ + 1 mM NaCl and then moved to the second solution of 0.01 M $MgCl_2$ + 1 mM NaCl after a stable potential was reached in about 3 minutes. The time needed to reach 95% of the total potential change caused



Figure 3.9: The hanging drop method to measure response time. The tip of the measuring electrode is touching the ceramic frit of the reference electrode. They are both in contact with a small drop of solution that is hanging from the reference electrode. In this way, the potentiometric cell is intact even while the solution is being exchanged, but at the same time, a sudden activity step can also be realized.

by the change in Mg^{2+} ion concentration was regarded as response time τ_{95} (Fig. 3.10).

3.1.3.4 RC time constant

RC time constant was determined with two different methods. For the antimony and tungsten pH-electrodes, *RC* time constant was measured directly from the response curve using the activity step method. The transient response curve of the potentiometric cell was recorded while the buffer was changed from pH 6 to pH 4, then Eq. 4.2 was fitted on the curve. In the fitted function, *RC* is the only variable parameter, and can be directly obtained.

For the micropipette electrodes, a different method was used. Resistance and capacitance of the potentiometric circuit was measured individually. Resistance of the measuring electrode was determined with the voltage divider method described in the previous section. In this case however, an $R = 50 \text{ M}\Omega$ 1% precision resistor was inserted between the measuring and reference electrodes, then the cell potential difference was continuously measured in 10^{-2} M MgCl_2 solution. After arriving at equilibrium potential difference, the resistor was removed, and the measurement was continued until a new equilibrium signal was reached. Electrode resistance can be calculated with the formula:

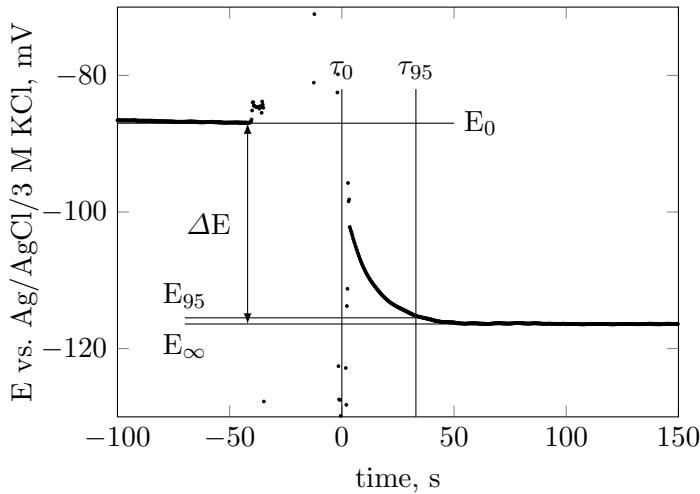


Figure 3.10: Illustration of the quantities used for the determination of response time. E_0 : electrode potential prior to change in the activity (of the measured ion), E_{eq} : equilibrium electrode potential after the change in activity. ΔE : total difference between E_{eq} and E_{eq} , E_{95} : electrode potential when 95% of the total change has occurred. τ_0 : time instance when the change occurs, τ_{95} : time instance when E_{95} is reached. $\Delta\tau_{95}$: difference between τ_{95} and τ_0 .

$$R_{ISME} = R \frac{E_{OCP} - U_R}{U_R} \quad (3.1)$$

where R_{ISME} is the resistance of the ion-selective microelectrode, R is $50 \text{ M}\Omega$, E_{OCP} is the open circuit potential difference, and U_R is the potential difference between the electrodes while the resistor is introduced in the circuit.

The capacitance of the circuit is mainly due to the capacitance of the input amplifier, and the capacitance of the cable leading from the electrodes to the amplifier input. The capacitance of the amplifier input was measured by applying a low impedance -1.5 V step between the inputs of the amplifier through a $50 \text{ M}\Omega$ resistor, and the time necessary to reach 63% of the total change in potential difference ($\tau = R \times C$) was measured. Then, the input capacitance could be calculated with the $C = \tau / 50 \text{ M}\Omega$ formula.

3.2 SECM targets

With the exception of the micropipette ion source, the model targets were created by embedding graphite rods, metal wires, or metal ribbons in an Epofix (Struers, Ballerup, Denmark) disk-shaped ($d \approx 3 \text{ cm}$) epoxy resin sleeve.

3.2.1 Magnesium- and potassium-ion source pipette model targets

Spherical Mg²⁺ and K⁺ ion concentration distribution was created in 10⁻³ M NaCl supporting electrolyte using simple model systems. They consisted of an embedded micropipette target facing upwards with a pore diameter of $d = 100 \mu\text{m}$, and filled with 0.1 M MgCl₂ and 0.1 M KCl aqueous solutions respectively, with an addition of 10⁻³ M NaCl and 4 % agar-agar to hinder diffusion (Fig. 3.11).

3.2.2 Molded model targets

The model targets described here are prepared by moulding the samples with Epofix resin. The mould was prepared by using a cut-off portion of a Falcon-tube as moulding. The samples were placed upside down into the empty mould, then the resin was poured in. After curing, the front side – which was facing downwards during the curing process – was sanded off until the sample surfaces were exposed. Then, the surface was polished with sandpapers with increasingly higher grit, from 600 to 4000. Then polishing was continued with alumina slurry on wet polishing cloth. Alumina particle size was 1 μm , 0.3 μm and 0.05 μm . Finally, the surface was cleaned and degreased with absolute ethanol. Fig. 3.12 depicts a sketch of the model targets prepared with this method, and the SECM setup used with these targets. While scanning, the front side of the mould – that featured the exposed samples – faced upwards, and was surrounded laterally by the the cut-off portion of the Falcon tube, creating a tight seal. The small container prepared in this way held about 5 cm³ of electrolyte solution. In this way, only the well-defined cross section of the samples were exposed to the electrolyte. A regular size Ag/AgCl/3M KCl reference electrode could be easily introduced into the container without obstructing the movement of the microelectrode that was used as an SECM measuring tip.

3.2.2.1 Iron – magnesium galvanic couple

A magnesium – iron galvanic couple was used as model corroding system. An iron wire with a diameter of 760 μm and a magnesium ribbon with a cross section of 200 $\mu\text{m} \times 800 \mu\text{m}$ were embedded in the Epofix resin disk. Corrosive electrolyte was 1 mM NaCl.

3.2.2.2 Iron – AZ63 galvanic couple

Scans were also performed on an epoxy resin sleeve holding 760 μm diameter wires of pure iron and AZ63 magnesium alloy, manufactured from a boyler sacrificial anode with a high-precision lathe. The composition of the alloy was determined (in wt.%)

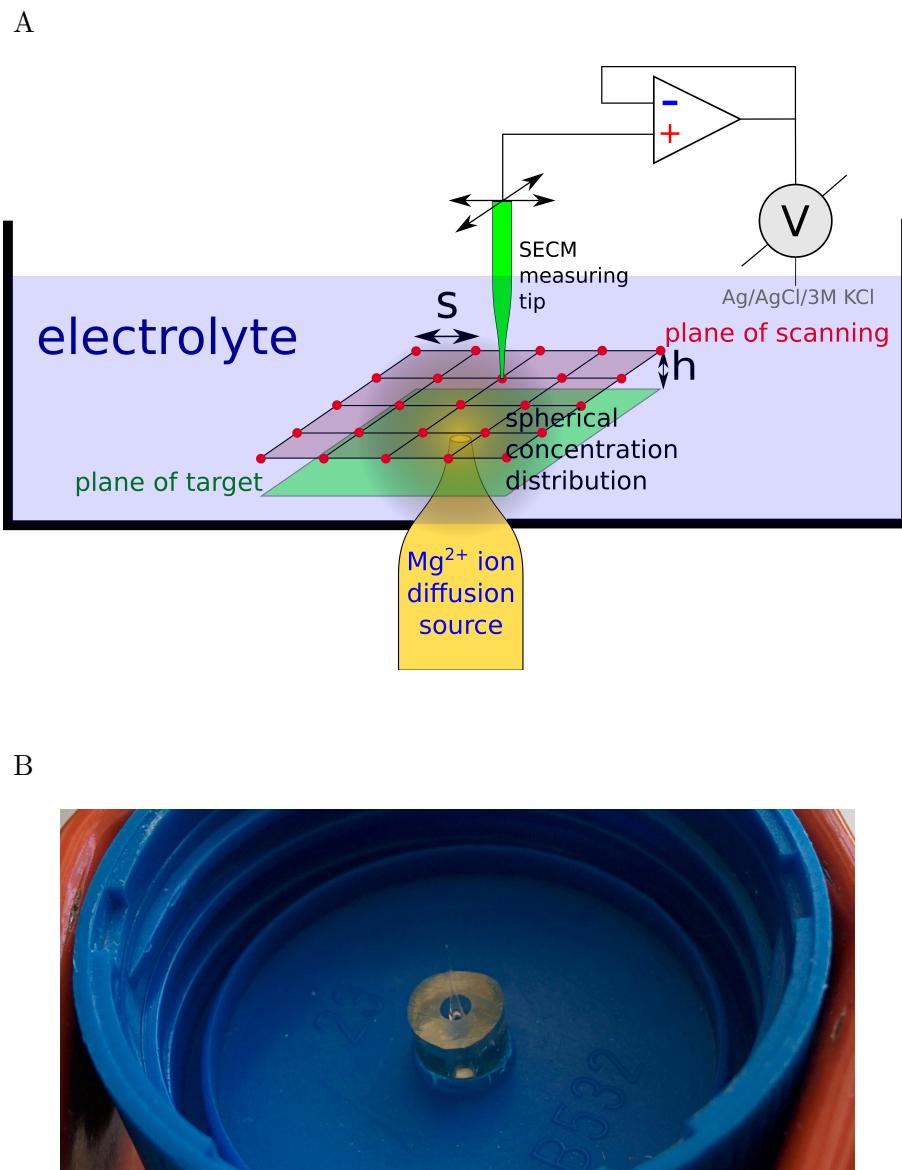


Figure 3.11: Sketch (A) and photo (B) of the model system with the embedded glass pipette Mg²⁺ or K⁺ ion diffusion source, and the SECM scan setup. "h" is height of scan, the distance between the plane of the target (pipette orifice) and the SECM tip. "s" is the step size, that is the distance between two neighbouring data aquisition points. Red dots indicate the data aquisition points of the 2D raster scan pattern. Not drawn to scale.

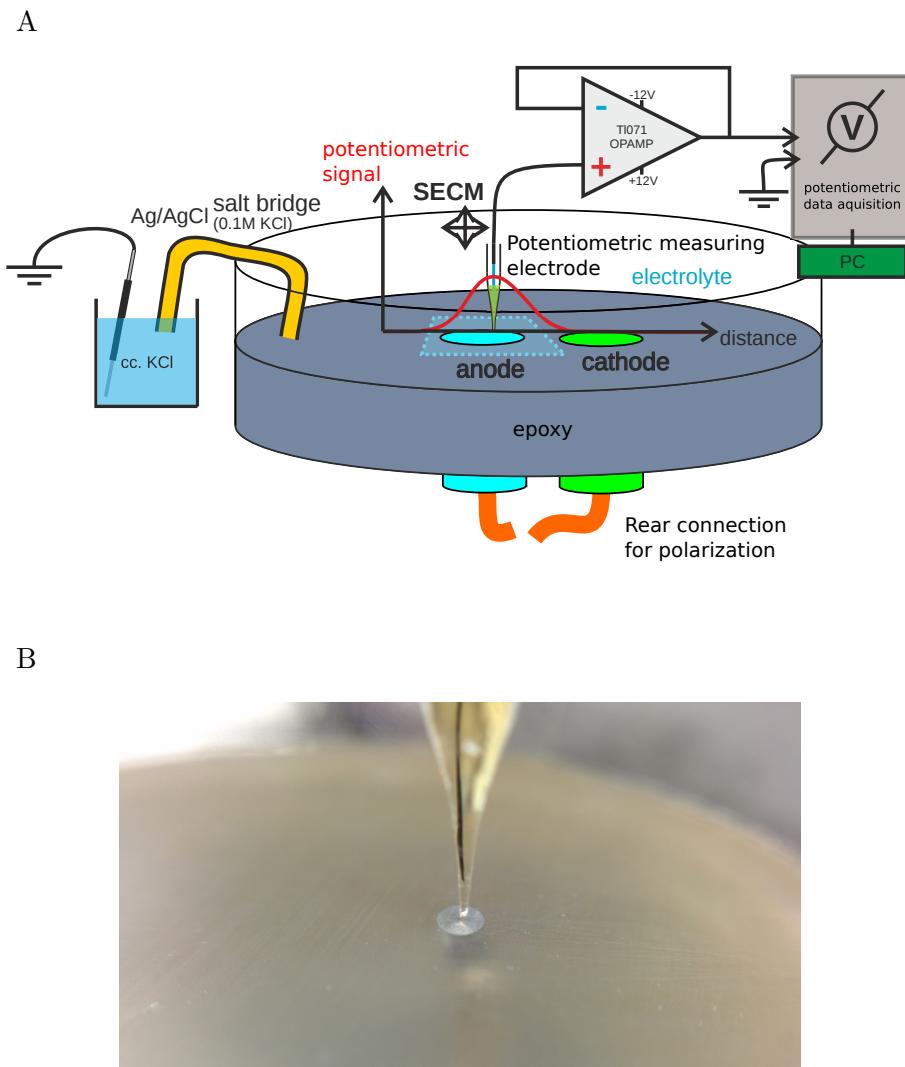


Figure 3.12: (A) Sketch of the moulded model targets and the SECM scan setup used for these targets. (B) Close-up photograph of the Mg^{2+} ion selective microelectrode above the AZ63 sample. For better visibility, the picture was taken without the electrolyte in the cell.



Figure 3.13: The water heater sacrificial anode made of the AZ63 magnesium-aluminium-zinc alloy. The sample was prepared from such an anode by a precision lathe.

by colleagues from the *University of La Laguna, Spain*, by emission spectrometry (ICP-OES): Al 5.74, Zn 2.88, Cu < 0.005, Fe < 0.005, Ni < 0.005, Si < 0.005, Mg balance [111]. Tests were conducted in 1 mM NaCl solution that was saturated with air.

3.2.2.3 Carbon steel

The embedded sample in this case was a carbon steel ($A \approx 0.2 \text{ cm}^2$) JIS G3131 SPHC specimen with the composition, C: 0.04%, Mn: 0.15%, P: 0.026%, S: 0.005%, and Si: 0.02% [112].

3.2.2.4 Graphite model target

To demonstrate and compare the performance of the new scanning algorithms, pH-dependent potential images images recorded $h = 100 \mu\text{m}$ above a graphite disc anode, set to 2 V versus another, identical graphite electrode. $d = 350 \mu\text{m}$ mechanical graphite pencil leads (Rotring, Hamburg, Germany) were used for the anode and cathode as well. They were both embedded in the epoxy resin sleeve with about 1 cm separation. At this potential difference, pH of the electrolyte will decrease at the anode, and increase at the cathode, as a consequence of water electrolysis. Electrolyte was unbuffered 10^{-3} M NaCl solution. Potential image was recorded after 10 minutes of electrolysis. During the imaging, the electrolysis cell was disconnected to avoid the electric field generated by the applied voltage affecting the image. In this way a spherical concentration distribution was generated above the target.

3.3 SECM routines

3.3.1 For the comparison of solid and liquid contact microelectrodes

2D scans were performed $100 \mu\text{m}$ above the micropipette and the magnesium ribbon target. Scanrate was $12.5 \mu\text{m}/\text{s}$ in both cases. Step size in X and Y direction was

25 and 50 μm . Scanned area was $1000 \mu\text{m} \times 1500 \mu\text{m}$ ($X \times Y$). To compare the performance of the solid contact and the liquid contact electrodes employing the same membrane, Mg^{2+} ion-selective micropipettes were used. A Sensolytics SECM system was used, potential was recorded with an Autolab Electrochemical workstation. The TL082 voltage based follower was inserted between the measuring microelectrode and the Autolab to provide impedance matching. The voltage follower was powered by two 9 V batteries in series. Reference node was between the connected opposite terminals of the two batteries. Reference electrode was an $\text{Ag}/\text{AgCl}/3 \text{ M KCl}$ electrode.

3.3.2 Optimization of scanning patterns and algorithms

3.3.2.1 Cartesian coordinate-system based patterns and algorithms

The three conventional scanning algorithms are called the „meander”, the „comb”, and the „fast comb”. In all three algorithms a sequence of linescans are performed. After finishing with one line, the scan is continued on the starting position of the next line, until the last point of the last line is reached, when the image is completed. Y usually denotes the coordinate of the line, while X denotes the position of an individual point in the line. Using the meander algorithm, the probe travels through all of the raster coordinates by alternating the X scan direction from line to line, resulting in a characteristic „meander” pattern. In this way, the probe never covers the same point twice within an image. This algorithm is considered to be the most economical for this reason. It covers the raster points as fast as possible, without any repetition or wasted movement.

In the comb pattern, the probe sweeps through each scan line twice in opposite directions. Then the two scans are averaged to get the final linescan.

The fast comb algorithm scans only in one direction, and before advancing in the Y direction, the probe quickly travels back to the starting position of the next scan line without measuring or stopping at all.

If it is not noted otherwise, the used scanning parameters were the following. In the meander, fast-comb, and comb algorithms, total scanned area was $2000 \mu\text{m} \times 2000 \mu\text{m}$, resolution was $100 \mu\text{m} \times 100 \mu\text{m}$, and consequently $21 \times 21 = 441$ raster points altogether.

Both in the experimental and simulated SECM scans, for each point, 1 second was split between probe movement, resting period, and signal sampling. One measurement was performed at every point after the equilibration period, before positioning the probe to the next point. Probe movement speed was $312.5 \mu\text{m/s}$. The starting position was $x = -1000 \mu\text{m}$, $y = -1000 \mu\text{m}$.

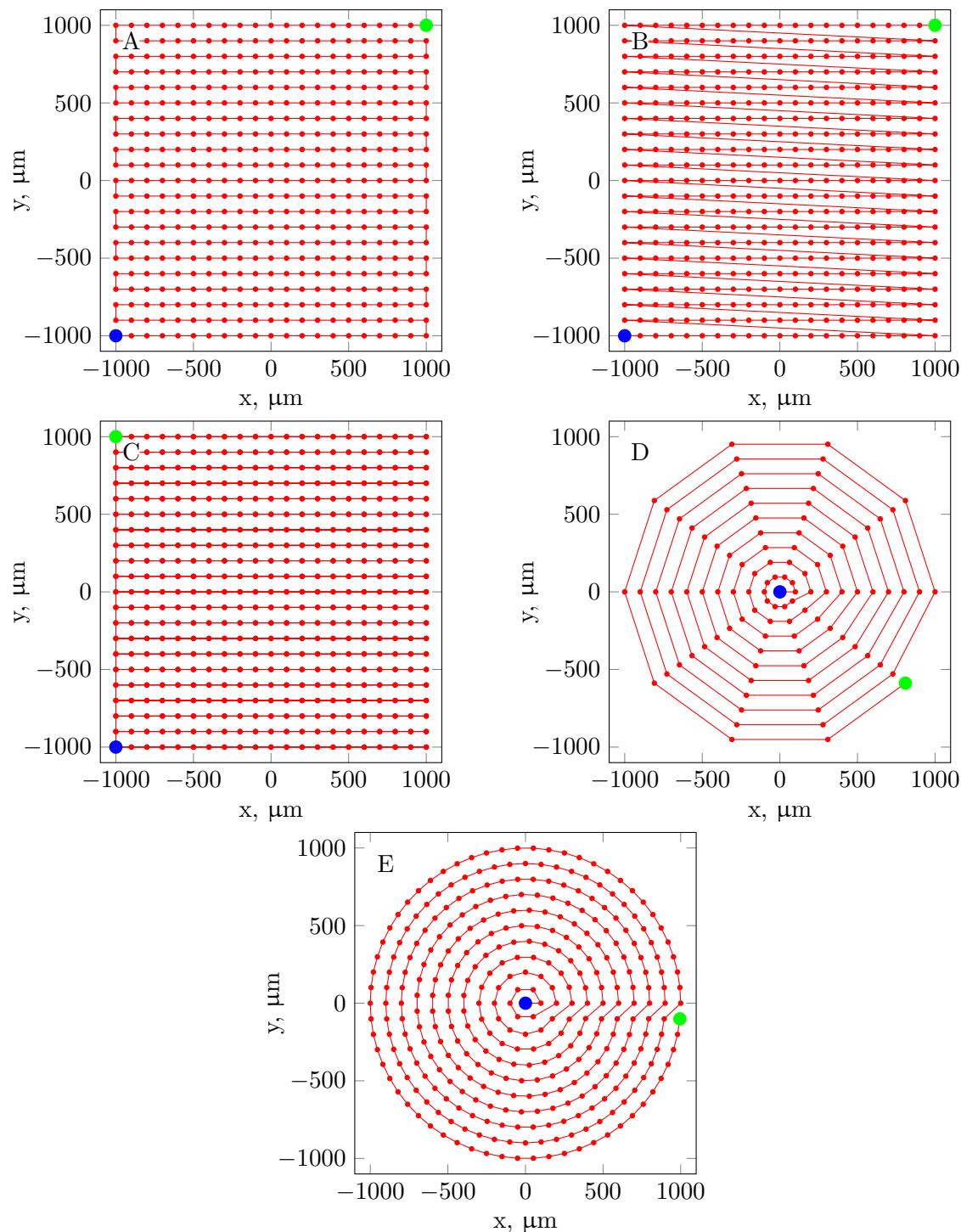


Figure 3.14: The conventional (A) meander, (B) fast comb and (C) comb, and the new, proposed (D) web, and (E) arc SECM scanning patterns for circularly symmetric targets. Red dots indicate sampling points, red line shows the probe path. Blue and green dots indicate starting and finishing positions, respectively.

3.3.2.2 Circular, polar-coordinate system based patterns and algorithms

The two new scanning patterns proposed in this thesis are called the „web” and the „arc” patterns. They are both based on a polar-coordinate system. In the web pattern, sampling points are located on concentric circles with radii increasing in regular intervals. On each circle, there are equal number of points. The first point in each circle has the angular coordinate of 0° , which increases at regular intervals with the rest of the points. Using this pattern, resolution decreases as radius increases. The arc pattern is very similar, except that the points on the circles are separated by equally long arcs, so that with increasing radius, the number of points increases, and resolution is maintained. The scanning patterns can be seen in Figure 3.14.

In the web algorithm, the radius of the scanned area was always $r = 1000 \mu\text{m}$, with $\Delta r = 100 \mu\text{m}$, and $\Delta\alpha = 2\pi/10$ radians, resulting in 10 points on each circle, and a total of 110 points. In the arc pattern r and Δr was the same as in the web pattern, arc distance between adjacent points along the circles was $100 \mu\text{m}$, with a total of 341 points.

Starting position was $x = 0 \mu\text{m}$, $y = 0 \mu\text{m}$ relative to the target center for both algorithms.

The images obtained with the two polar coordinate-based algorithms were interpolated to the grid points of the 2D raster used by the other algorithms to allow similar visualization.

3.3.3 SECM routines for the deconvolution study

3.3.3.1 Linescans

To examine the effect of equilibration interval length on the image distortion, and for easy comparison of raw and deconvoluted data, line scans were recorded with three different time intervals allocated for each data acquisition point: 0.5 s, 2 s, and 5 s. Probe movement speed was $1000 \mu\text{m}/\text{s}$, and therefore probe movement interval was 0.1 s, resulting in equilibration interval lengths (t_e) of 0.4 s, 1.9 s, and 4.9 s, respectively. Step size was $100 \mu\text{m}$, scan distance was $2000 \mu\text{m}$ with the source center in the middle. 8 consecutive line scans (4 forward and 4 reverse scans) were performed in each case to confirm repeatability.

3.3.3.2 2D scans

To confirm the effect of deconvolution on 2D image quality, 2D raster scans were performed with four different equilibration interval lengths (4.9 s, 1.9 s, 0.9 s, 0.4 s), and two different scanning algorithms; the meander and the fast comb. In

meander, the probe travels through all of the raster coordinates without repetition and wasted movement, by alternating the X scan direction from line to line, resulting in a characteristic „meander” pattern. The fast comb algorithm scans only in one direction, and before advancing in the Y direction, the probe travels back to the beginning of the scan line without measuring or stopping at all (paper IV).

Starting position was $X = -1000 \mu\text{m}$, $Y = -1000 \mu\text{m}$. Both algorithms used horizontal scanning. Initial scan direction for the meander algorithm, and scan direction for the fast comb algorithm was left to right. Step size was $100 \mu\text{m}$, scanned area was $2000 \mu\text{m} \times 2000 \mu\text{m}$, resulting in overall scanning times of 2205 s, 882 s, 441 s, and 220.5 s.

In the experiments with the micropipette sources, the $X = 0 \mu\text{m}$, $Y = 0 \mu\text{m}$ reference position was established by positioning the measuring tip $100 \mu\text{m}$ above the orifice center of the diffusion source, with the aid of a camera. Then, the tip was positioned at the starting coordinates, and the electrolyte was introduced to the cell. 10 minutes later, the scan was started.

3.3.4 Backlash compensation

To rule out additional distortion caused by the SECM apparatus, backlash of the linear stages was measured and found to be below $1 \mu\text{m}$ after software compensation. To measure backlash, a microscope slide with a micrometer scale was fixed on the linear stage, then the stage was moved $1000 \mu\text{m}$ to one direction, to make sure the momentary backlash in that direction is zero. After taking a photo, the stage was moved $100 \mu\text{m}$ to the same direction, and another photo was taken. Then, the stage was moved $100 \mu\text{m}$ to the opposite direction, and a photo was taken again. The difference between the first and last photo is the backlash of the particular stage. Fig. 3.15 shows the photos for each stage of the home-made SECM.

3.4 Deconvolution of potentiometric SECM images

The potentiometric signal-time response function to change in analyte activity can be characterized with the time constant. It is the time required for the cell potential difference to change from its initial value by the fraction $1 - e^{-1} = 0.63$ of the final value [113]. The cell can be modeled as a simple RC low-pass filter arranged serially between the signal input and the output [74]. In this case, time constant is $\tau = RC$, where R is the resistance of the cell with the largest contribution from the measuring electrode, and C is the capacitance of the cell with the largest contribution from the input amplifier and the cable between the amplifier and the electrodes.

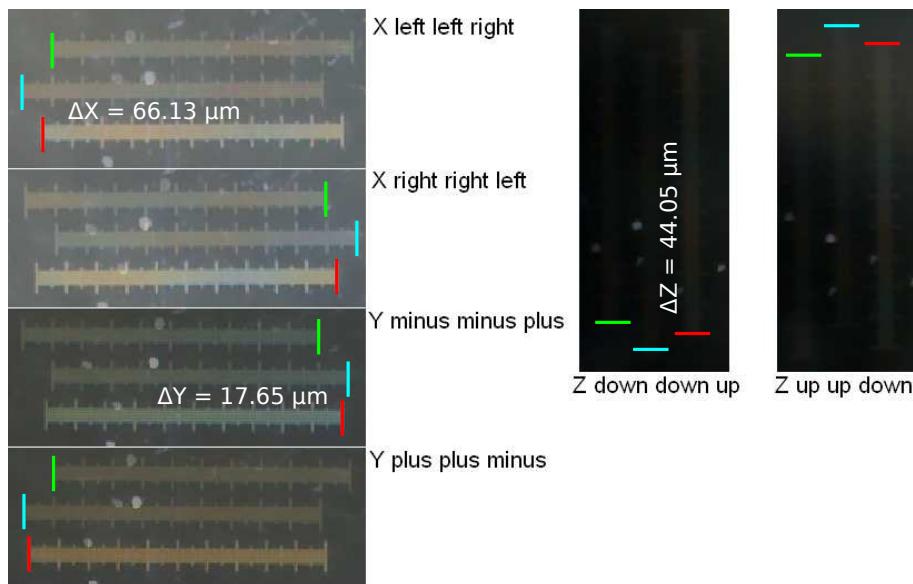


Figure 3.15: Microphotos for the backlash compensation measurements for the home-made SECM. The photos show a microscope slide with a micrometer scale fixed on the microelectrode holder. Labels ("left", "right") indicate the direction of the slide unit movement prior to taking the microphoto. First, the slide unit was moved 1000 μm , then a photo was taken. Then, it was moved 100 μm in the same direction, and another photo was taken. Finally, it was moved in the opposite direction 100 μm , and a photo was taken. The difference between the second and the third photo is the backlash, which was compensated through the control software.

Eq. 4.2 describes the transient cell response when the measuring electrode is brought to contact with a solution of different analyte activity.

$$E_{cell}(t) = E_{cell}(\infty) + [E_{cell}(0) - E_{cell}(\infty)]e^{-t/RC} \quad (3.2)$$

where $E_{cell}(t)$ is the cell potential difference at time t , $E_{cell}(\infty)$ is the equilibrium cell potential difference, $E_{cell}(0)$ is the cell potential difference prior to the change. From this, $E_{cell}(\infty)$ can be expressed as:

$$E_{cell}(\infty) = \frac{E_{cell}(t) - E_{cell}(0)e^{-t/RC}}{1 - e^{-t/RC}} \quad (3.3)$$

This can be used as a deconvolution function for potentiometric SECM images, substituting the time that elapses between two consecutive measurements in the SECM scan for t to calculate each equilibrium $E_{cell}(\infty)$ from the respective observed $E_{cell}(t)$ potential difference values.

When the tip advances from the i th data acquisition point to the $(i+1)$ th, cell potential difference changes from the initial $E_{cell}(t, i)$ to $E_{cell}(t, i+1)$. Therefore, for every point, $E_{cell}(0, i)$ will be equal to $E_{cell}(t, i-1)$. To deconvolute the raw image, the following calculation kernel was cycled through the data matrix points in the same order as they were recorded in the scan:

$$E_{cell}(\infty, i) = \frac{E_{cell}(t, i) - E_{cell}(t, i-1)e^{-t/RC}}{1 - e^{-t/RC}} \quad (3.4)$$

RC time constant in Eq. 3.3 was substituted with the value calculated from $R \times C$, obtained in the measurements described in the previous subsection. A FORTRAN program was written to perform the deconvolution:

```

program deconvolution
implicit none
integer :: i, j, stat
real rc, e0, conv
real t
rc=0.85
open(1, file='data.txt')
open(2, file='data_deconvoluted.txt')
read(1, *) i, j, e0
do
  read(1, *, iostat=stat) i, j, conv
  if (stat /= 0) exit
  write(2, *) i, j, ((conv - e0*rc)/(1-rc))
end

```

```

e0=conv
end do
close(1)
close(2)
end program deconvolution

```

3.5 Simulation of the SECM measurements

3.5.1 3D numerical simulation of diffusion from a disk source

For the diffusion simulation, the „*point*” variant of the finite difference method was used as described in [114]. In potentiometric SECM, the tip is a passive probe, it does not generate or collect, therefore it does not alter the concentration profile of the species generated at the substrate. The model target can be implemented in simulation by a disk surface with a constant flux of the generated species, H_3O^+ . Since the probe is passive, the concentration profile is only affected by the magnitude of the flux, and the diffusion coefficient of the species. The time dependent diffusion problem is described by *Fick’s Second Law of Diffusion*:

$$\frac{\partial c}{\partial t} = D \nabla^2 c \quad (3.5)$$

where c is the concentration, t is time, D is the diffusion coefficient. For three dimensions, Equation 3.5 can be expressed in discrete form for solving with the finite difference method as

$$\frac{c'_{i,j,k} - c_{i,j,k}}{\delta t} = \frac{D}{h^2} (c_{i,j+1,k} + c_{i-1,j,k} + c_{i+1,j,k} + c_{i,j-1,k} + c_{i,j,k-1} + c_{i,j,k+1} - 6c_{i,j,k}) \quad (3.6)$$

where h is the distance between the adjacent points in space, $c_{i,j,k}$ is the concentration at the grid point with the coordinates of i, j, k , and $c'_{i,j,k}$ is the same, but in the previous cycle, at the time instance $t - \delta t$. This can be solved numerically for a given time instance by iterating Equation 3.6 on every point of a 3D matrix, which represents the diffusion system.

The simulation model consisted of a cubic diffusion field with an edge length of 20 mm, and a resolution of 10 μm on all three axes. The top and side faces had Dirichlet boundary condition with $c = 0$, representing the bulk solution. The bottom face had a disc shaped source with a diameter of $d = 350 \mu\text{m}$, with Neumann boundary condition, to model the graphite anode, where H_3O^+ was being generated.

The rest of the bottom surface had Neumann boundary condition with a constant $j = 0$ flux, modeling epoxy resin which embedded the graphite electrolysis electrode. A FORTRAN program was written to calculate the potential profile for $t = 600$ s. A 2D section of the solved 3D diffusion matrix was taken at $h = 100 \mu\text{m}$, and it was normalized to c_{max} . This was the input matrix for the SECM scanning simulation.

3.5.2 SECM scan simulation

The SECM scan simulations were performed on a normalized 2D section of the solved 3D diffusion matrix. The following calculation kernel was cycled through the data points using the same scanning algorithms as in the experimental SECM scans:

$$C_i = c_i + (C_{i-1} - c_i) \times T \quad (3.7)$$

where C_i and c_i are the values of the i -th point in the output, and input matrices, respectively, C_{i-1} is the value at the previous point, at $i - 1$, and T is a constant, equivalent of expression $e^{-t/RC}$ in Equation 4.2. A value of 0.7 was set for T . For $i = 1$, C_i was set to c_i , assuming the potentiometric cell was in equilibrium in the beginning of the scan simulation.

3.6 Scanning Electrochemical Microscope

Throughout my work, I used three different SECMS. One was supplied by Sensolytics (Bochum, Germany). The instrument was built around an Autolab (Metrohm, Herisau, Switzerland) electrochemical interface, controlled with a personal computer. A voltage follower based on a $10^{12} \Omega$ input impedance operational amplifier (TL082, Texas Instruments) was introduced in the measuring circuit. The cell voltages were measured with the Autolab instrument and collected by the PC. The scanning system (Applicable Electronics Inc, New Haven, CT, USA) used a 3D micropositioner driven by precision stepping motors.

The other two SECM were custom built at the University of Pécs. While using these microscopes, potential was measured against an Ag/AgCl/3M KCl reference electrode with a high input impedance eDAQ pH/ISE isoPod USB (eDAQ Pty Ltd, Australia).

3.6.1 Z axis referencing

Z axis referencing is a notoriously hard problem in potentiometric SECM, because the measured signal is not a function of the distance from the surface per se, but the concentration of the measured ion(s). $Z = 0$ was used as a reference point in

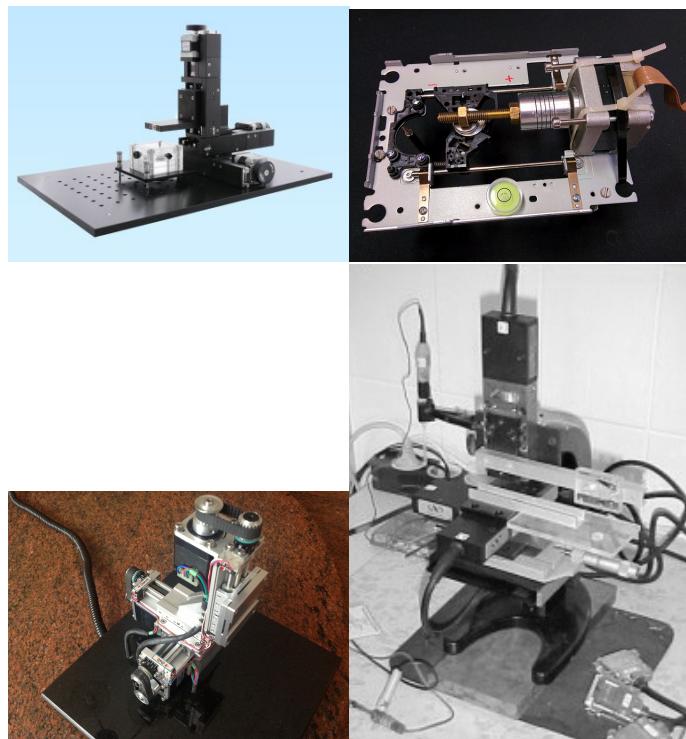


Figure 3.16: The Scanning Electrochemical Microscopes I used in my work. (A) Sensolytics SECM, (B) home-made SECM using Newport slide units, (C) home-made SECM using Domiline slide units driven with Nema 17 stepper motors, and (D) low cost, home-made 1D SECM using a slide unit from a DVD burner, driven by a stepper motor taken from a 5.25" floppy drive.

the SECM measurements. This position was established by gently approaching the ISME towards the surface of the epoxy resin while observing the distance by eye. The surface of the target and the SECM $X - Y$ plane were leveled with a bubble leveler, therefore the resin was at the same height as the AZ63 sample, compared to the tip. Once the distance could not be judged anymore by the naked eye, the ISME was approached to the surface in $1 \mu\text{m}$ increments. A video camera assisted during this stage. After every increment, the ISME was moved $100 \mu\text{m}$ laterally and the tip movement was observed. Movement along such a distance can be easily detected even by the naked eye, yet it does not break the tip if it is already touching the surface, owing to its flexibility. This was repeated until the tip of the ISME didn't move during the translation, i.e. it touched the surface ($Z = 0$). Then, the ISME was moved to the opposite direction laterally, where it originally touched the surface, and lifted $100 \mu\text{m}$ upwards on the Z axes. Since the positioning repeatability of the SECMS used in this thesis is much better than $1 \mu\text{m}$, no collision with the target was possible. Indeed, this was confirmed by the optical inspections of the target after each measurement. No evidence of mechanical interaction with the sample surface was found throughout the work.

3.6.2 Homemade SECM

Two microscopes out of the three I used during my work are homemade. The first one was built from 3 Newport M-MFN25PP linear stages equipped with UE166PP stepper motors. Controller and driver was home-made from parts available in the local electronics store. The very same microscope has been introduced in [115]. The other home made SECM was built from Domiline 15 linear stages. Stepper motors for these were 3 Nema 17. Motors were coupled to the shafts by ribbed belts. The motors were controlled by a SD4DX USB Controller (Peter Norberg Consulting, Inc. 117 South Clay Ave. Ferguson, MO, USA), and driven by a Gecko step-and-direction driver board (Geckodrive, Inc. 14662 Franklin Ave, Santa Ana, CA.). The control software was written in Java by the author. This instrument was used in for the experiments published in IV-V and for the experiments used in the investigation of the effect of the electric field on the potentiometric SECM images.

3.7 Measuring corrosion current between a galvanic couple

Corrosion current between a galvanic couple cannot be measured directly by connecting the terminals of ammeter to the galvanic pair, since the measurement itself would influence the magnitude of the current. An ideal ammeter has zero resistance. A real ammeter has a finite resistance, prohibiting the unhindered flow of current be-

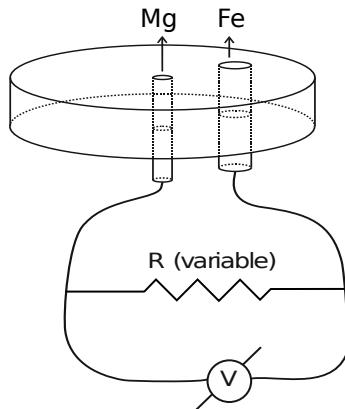


Figure 3.17: Circuit for measuring corrosion current between a galvanic couple.

tween the anode and the cathode. However, it is possible to calculate it by measuring the voltage drop on the two sides of a variable resistor, that connects the two metals constituting the galvanic pair (Fig. 3.17). Plotting the voltage over the resistance (E/R) with respect to resistance, the "y," interception will be $1/i$ at $R = 0$. It is very important to use a high input impedance voltmeter in this experiment to avoid adding any parallel conductor to the shunt resistor R . For this purpose, a MeTeX multimeter was used. Impedance matching between the circuit and the multimeter was provided by a voltage follower based on the TL082 operational amplifier. After reciprocating, corrosion current is obtained. Using Faraday's law of electrolysis, Mg^{2+} ion flow rate from the Mg/Al sample was estimated. This is a well known technique applied when a limiting quantity is to be determined, but measuring this quantity is technically challenging or theoretically impossible. An example for the latter would be the determination of the absolute zero temperature.

3.8 Estimating ion-flux based on approaching curves

To estimate the flux of Mg^{2+} ions from the surface of the AZ63 sample, lateral scans at constant height across 5 mm, and retracting scans from $h = 0 \mu\text{m}$ to $h = 1000 \mu\text{m}$ were performed above the AZ63 sample. The SECM scanning tip was a solid contact Mg^{2+} ISME electrode. The reference half cell was $\text{Ag}/\text{AgCl}/3 \text{ M KCl}$. Height of lateral scans was 100 μm , step size was 5 μm , lateral distance was 5 mm with the AZ63 sample in the centre. Retracting curves were recorded at $t = 10, 20, 30, 40, 50, 60$ minutes after introduction of the corrosive media, step size was 5 μm . Ionselective electrodes of this size have high resistance compared to the low input resistance of potentiometers To avoid loading the potentiometric sensor, a homemade high impedance voltage follower circuit was used as current

buffer based on the TL082 operational amplifier (Texas Instruments). The potential was measured with a MeTeX potentiometer (MeTeX M-3630D) connected to a PC, the signal was recorded with the software provided by MeTeX. Scans were performed both during galvanic coupling of the pair, and during the spontaneous corrosion of AZ63. Corrosive media was deionized water saturated with air.

Chapter 4

Results and Discussion

I've tried three approaches to alleviate the compromise between low distortion and short scanning time in the potentiometric SECM. The problem stems from the high RC time-constant. For a sufficiently small microelectrode, the resistance R can be so high, that the time-constant is measured in seconds. To arrive at the equilibrium potential of the measuring electrode, about $4 \times RC$ time must be allowed for the cell. Such high equilibration period is not practical, since a high number of sampling points must be included in the image raster to achieve the desired high resolution, and the $4 \times RC$ equilibration period must be waited at every sampling point. This means, for an image to be recorded with a step size of s (μm), image side length of L (μm), probe translation speed of v ($\mu\text{m}/\text{s}$), and an equilibration period of t_e (s), it takes t (s) time to complete the image, calculated with the following equation:

$$t = (L/s + 1)^2 \times (s/v + t_e) \quad (4.1)$$

For instance, if $R = 1 \text{ G}\Omega$ and $C = 500 \text{ pF}$, then $RC = 0.5 \text{ s}$, and $t = 882 \text{ s}$, or about 16 min, since about $t_e = 4 \times RC$ is necessary to obtain the equilibrium electrode potential with good approximation. To decrease the overall scanning time, there are a number of possibilities. If L or t_e is decreased or v or s is increased, then t is decreased. But, if the scanned area or resolution cannot be decreased further, then manipulating L and s is not a viable option. The parameters left are t_e and v . To decrease t_e and maintain image quality, RC must be decreased simultaneously. This is the first approach I took, and is detailed in Section 4.1.

In the second and third approaches I exploit the properties of the potentiometric response function:

$$E_{cell}(t_e) = E_{cell}(\infty) + [E_{cell}(0) - E_{cell}(\infty)]e^{-t_e/RC} \quad (4.2)$$

where $E_{cell}(t)$ is the cell potential difference at time t_e , $E_{cell}(\infty)$ is the equilibrium cell potential difference, $E_{cell}(0)$ is the cell potential difference prior to the change. The more different $E_{cell}(0)$ and $E_{cell}(\infty)$ are, the more the difference between $E_{cell}(\infty)$ and $E_{cell}(t_e)$ will be. Distortion of an image can be measured as an average of the differences between $E_{cell}(\infty)$ and $E_{cell}(t_e)$ at each point. It can be lowered by carefully optimizing scanning patterns and algorithms, so that the probe passes through borders between regions of high and low concentrations as few times as possible. This approach is detailed in Section 4.2.

In the third approach, I use the inverse of the potentiometric response function (Eq. 4.2) as deconvolution function. Since the relationship between t_e , $E_{cell}(0)$, $E_{cell}(t_e)$ and $E_{cell}(\infty)$ is known, a prediction for the only unknown $E_{cell}(\infty)$ can be calculated. This approach is detailed in Section 4.3.

Additionally, to increase the probe translation speed v and maximize the time available for cell potential equilibration (t_e), a custom SECM was built at our department, and used in the second and third approach. Increasing v has practical limitations, for a probe moving too fast between sampling points might stir the electrolyte. Scanning speeds of commercially available SECM devices however, haven't reached this limit, and are in the range of several tens of micrometers per second at best, due to hardware or software restrictions. With the custom built microscope, translation speeds up to 1000 $\mu\text{m}/\text{s}$ are possible.

4.1 Using solid-contact electrodes as potentiometric SECM probes

Solid-contact electrodes have lower resistance, compared to their otherwise identical, liquid-contact counterparts. This is due to two reasons. The solid contact can be pushed down very close to the micropipette orifice, shortening the thickness of the highly resistive ion-selective membrane, and decreasing the overall electrode resistance. The other reason is that instead of the internal solution – which has high resistance –, a modified carbon fiber – which has low resistance – is used as the ion-to-electron transducer. If R is lower, RC is lower, and the potentiometric cell becomes faster.

4.1.1 Electrode characterization and SECM images of a model system

I constructed two Mg^{2+} -ion selective electrodes. One used a liquid contact, and the other a solid contact. Besides this difference, they were prepared identically. Basic characterisation was performed for both. Fig. 4.1A and 4.1B shows the calibration plots for the liquid, and solid contact electrode, respectively. Sensitivities towards the primary ion (Mg^{2+}) were close to nernstian and very similar, 29.12 mV and 33.44 mV for the liquid and solid contact electrode, respectively. The solid contact electrode had a slightly wider dynamic range, reaching below 10^{-5} M. Selectivity coefficients, characterization of the potassium ion-selective electrode, and further characterization of the magnesium ion-selective electrode can be found in [116].

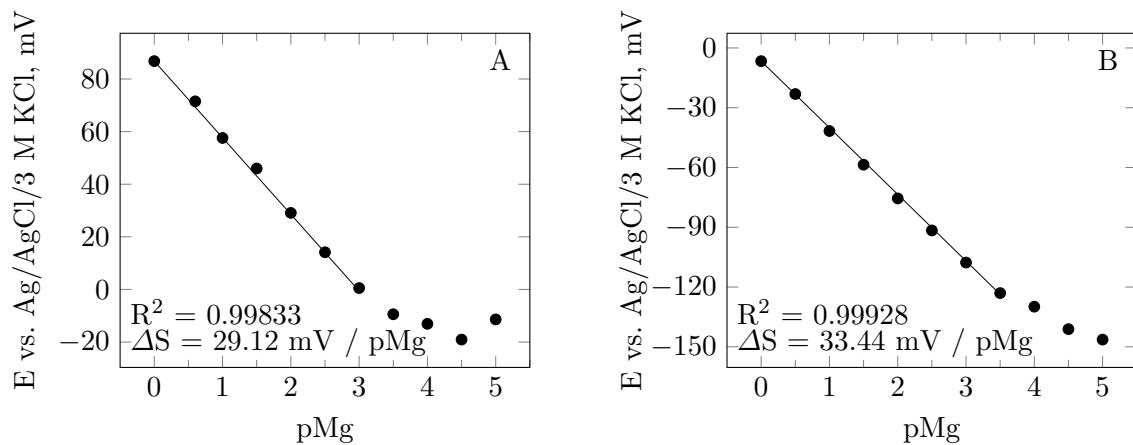


Figure 4.1: Calibration plots for the Mg^{2+} ISME in 1 mM NaCl solutions containing varying amounts of $MgCl_2$ ($pMg^{2+} = -\log_{10}[Mg^{2+}]$). (A) Liquid-contact, and (B) solid-contact.

Response characteristics were investigated by measuring the electrode resistance

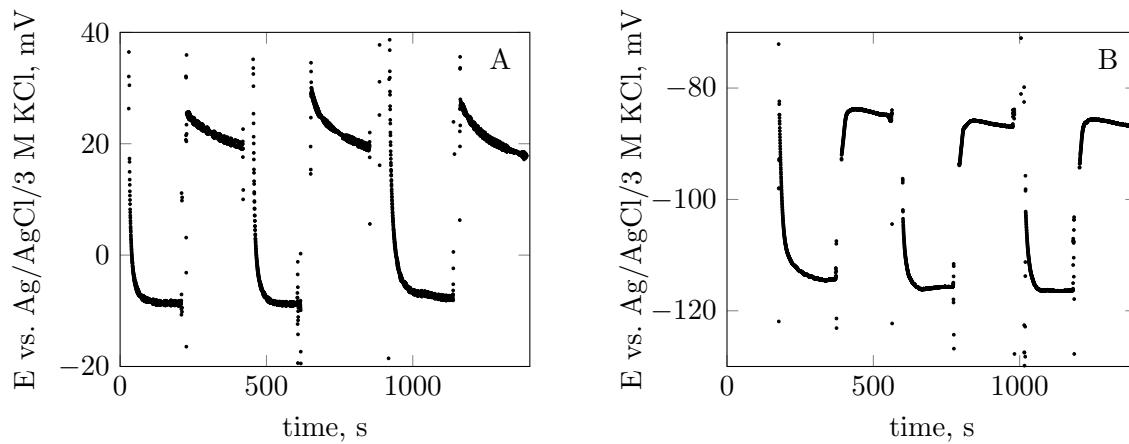


Figure 4.2: Dynamic response curves obtained for response time measurements to changes in MgCl_2 concentrations of 10^{-1} M and 10^{-2} M, in 10^{-3} M NaCl. (A) liquid-contact, and (B) solid-contact Mg^{2+} ISME.

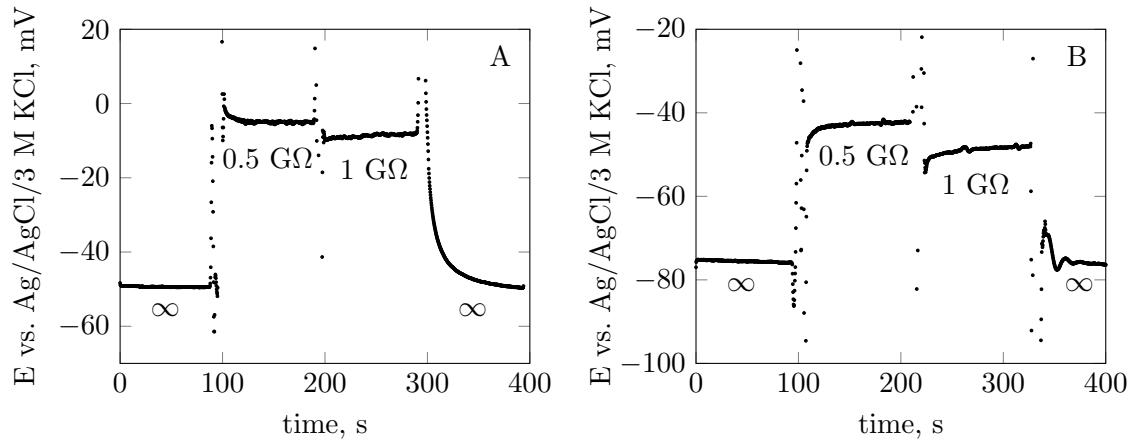


Figure 4.3: Response of ISME to shorting resistors for the voltage divider method: (A) Liquid-contact, and (B) solid-contact.

R , and the τ_{95} response time. The two parameters are related: $1 - e^{-3RC/RC} = 1 - e^{-3} \approx 0.95$. This means, that $3 \times RC \approx \tau_{95}$, because in $3 \times RC$, equilibrium electrode potential is reached by about 95%. Calculated from the voltage divider measurements (Fig. 4.2, Table 4.2), electrode resistance was $4.8 \text{ G}\Omega$ and $0.56 \text{ G}\Omega$ for the liquid, and solid contact electrodes, respectively. The measured τ_{95} parameters were 71.1 s, and 27.7 s, respectively (Fig. 4.3). Based on these values, the solid contact electrode was expected to produce less distorted images with the same scanning parameters.

To confirm it, a Mg^{2+} ion diffusion source model system was created, and the plane 100 μm above the pipette orifice was scanned with both electrodes. Fig. 4.4 shows the ISME images obtained using a liquid-contact (A), and a solid-contact (B),

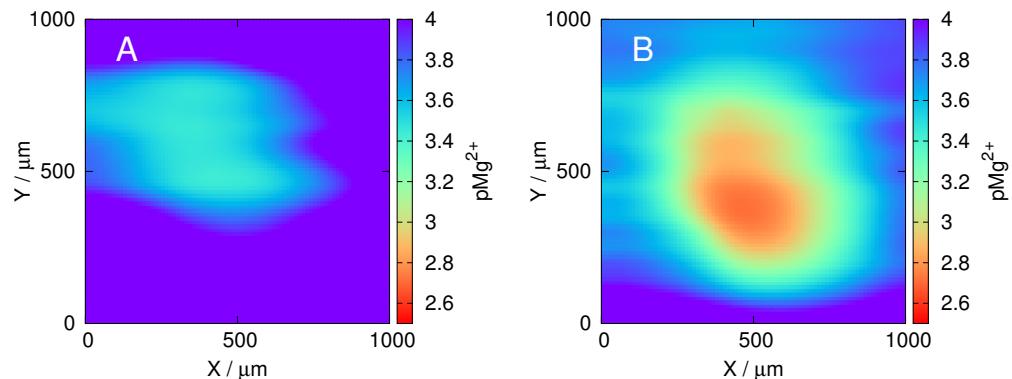


Figure 4.4: SECM images displaying the Mg^{2+} ion concentrations 100 μm above the tip of a centered pipette source. (A) liquid-contact, and (B) solid-contact. Scan rate: 12.5 $\mu\text{m}/\text{s}$.

micropipette electrode. Both 2D ISME maps were recorded at a scan rate of 12.5 $\mu\text{m}/\text{s}$. The same pipette holding the 0.1 M MgCl_2 agar solution was used in the measurements plotted in Figs. 4.4A and 4.4B. Visual inspection of the two images clearly shows significant image distortion in the X-direction with the liquid-contact ISME due its slower response as expected based on its higher resistance. It can also be observed in the image scanned with the solid-contact electrode, although to a much less extent. The overlayed isoconcentric countour lines are more circular, and not as elongated in the X-direction as in the case of the image prepared with the conventional electrode. Another important feature to note in the images is the difference in the highest magnesium ion concentration observed with the two electrodes. With the solid-contact microelectrode it's about $10^{-2.5}$ M. On the other hand, with the conventional liquid-contact electrode, highest observed magnesium ion concentration is only about $10^{-3.4}$ M. One possible reason for this is that the cell equipped with the liquid-contact electrode cannot keep up with the changes of the magnesium ion concentration at the micropipette orifice. That is, it passes over the area with the highest concentration so quickly, that by the time the cell would reach the potential corresponding to that concentration, the probe is already at another location, with a lower concentration. Potential starts dropping, while it approaches the new equilibrium potential.

4.1.2 Applications

4.1.2.1 Investigation of galvanic and homogeneous corrosion of magnesium

In paper (II), we used the Mg^{2+} ion-selective electrodes to image Mg^{2+} ion concentration above the corroding samples and compared the results. Based on the

Table 4.1: Resistance measurements for the two kinds of Mg^{2+} ion-selective micropipette electrodes conducted in 1 mM $MgCl_2$ 1 mM NaCl solution.

Parameter	ISME	
	Liquid-contact	Solid-contact
E_{OCP} / mV	-49.5	-75.5
R / GΩ	1	1
U_R / mV	-8.53	-48.41
R_{ISME} / GΩ	4.80	0.56

pipette source model target experiment and the resistivity measurements, it was expected that the cell equipped with the solid-contact electrode would yield less distorted images. Fig. 4.5 shows the four scans. Inspecting the images about the uncoupled magnesium (Fig. 4.5A1-A2), it is clear that the image scanned with the liquid-contact electrode is more distorted. The individual scanlines are blurred in the X direction, just like in the previous experiment with the pipette source. The same can be said about the images of the galvanically coupled magnesium. The one scanned with the solid-contact electrode is less distorted. Also, higher peak values can be observed, corresponding to magnesium dissolution. These anodic spots are resolved much better by the solid-contact electrode.

4.1.2.2 Estimation of corrosion current based on vertical SECM scans

Mg^{2+} ion concentration profiles above the Mg sample were recorded by SECM scans. Vertical Mg^{2+} ion concentration distribution was determined at different instants in time of the corrosion process, with, and without coupling the Mg/Al and Fe samples. About ten times more Mg^{2+} is being formed with coupling. Mg^{2+} concentration was increasing with time above the sample while coupled, on the other hand, it was decreasing after 10 minutes while not coupled (Fig. 4.6A). Based on the method of Scott and White [117], using the Mg^{2+} concentration profiles, Mg^{2+} flow rate from the Mg piece was possible to estimate:

$$\Omega = 4DC_s a \quad (4.3)$$

where Ω is the amount of Mg^{2+} released from the disc shaped Mg/Al surface, D is the diffusion coefficient of Mg^{2+} , C_s is the surface concentration of Mg^{2+} (at the height $z = 0$ μm), a is the radius of the Mg/Al sample. As the only unknown variable in the equation above, Ω could be calculated. Substituting the value of $D = 7.06 \times 10^{-8} \text{ dm}^2 \cdot \text{s}^{-1}$ [118], $C_s = 3.29 \times 10^{-2} \text{ M}$, $a = 0.0038 \text{ dm}$, the result is $\Omega = 3.53 \times 10^{-11} \text{ mol} \cdot \text{s}^{-1}$.

Corrosion current between the Mg/Al sample and four Fe samples with different

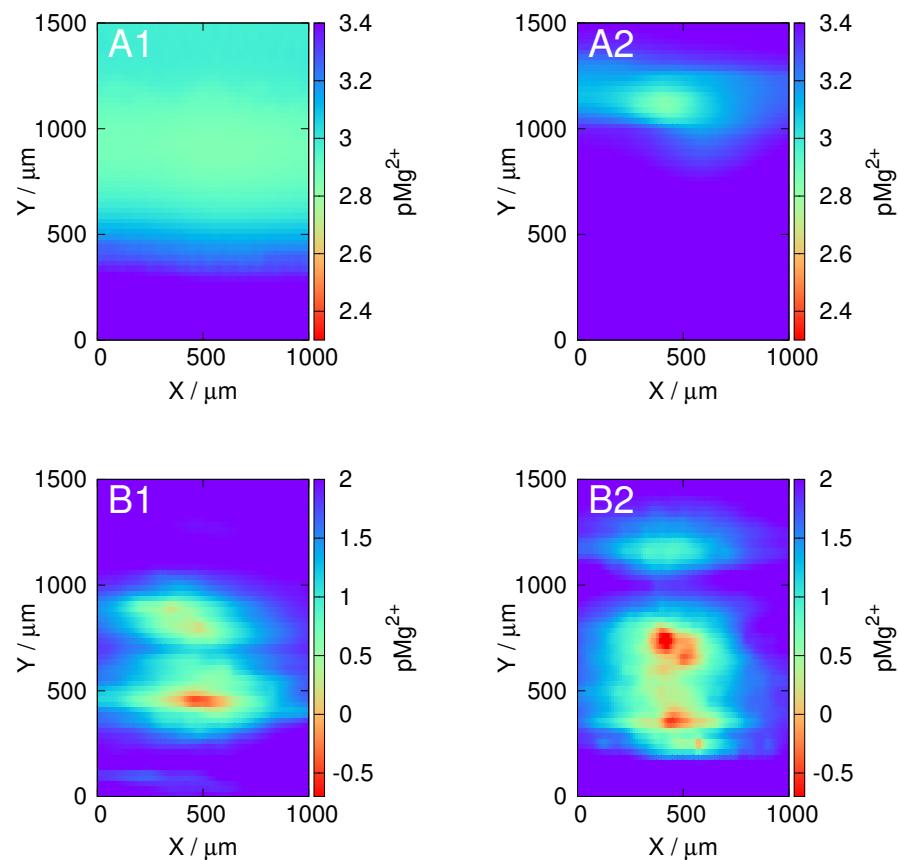


Figure 4.5: SECM scans above the magnesium sample (A) uncoupled, and (B) galvanically coupled to the iron sample, while the cell was equipped with the conventional (1) liquid contact, and the new, (2) solid contact micropipette. Scans were performed with the Sensolytics SECM, with impedance matching provided by the TL082 based voltage follower. Reference electrode was Ag/AgCl/3M KCl. Height of scan was 100 μm , scanrate was 12.5 $\mu\text{m}/\text{s}$.

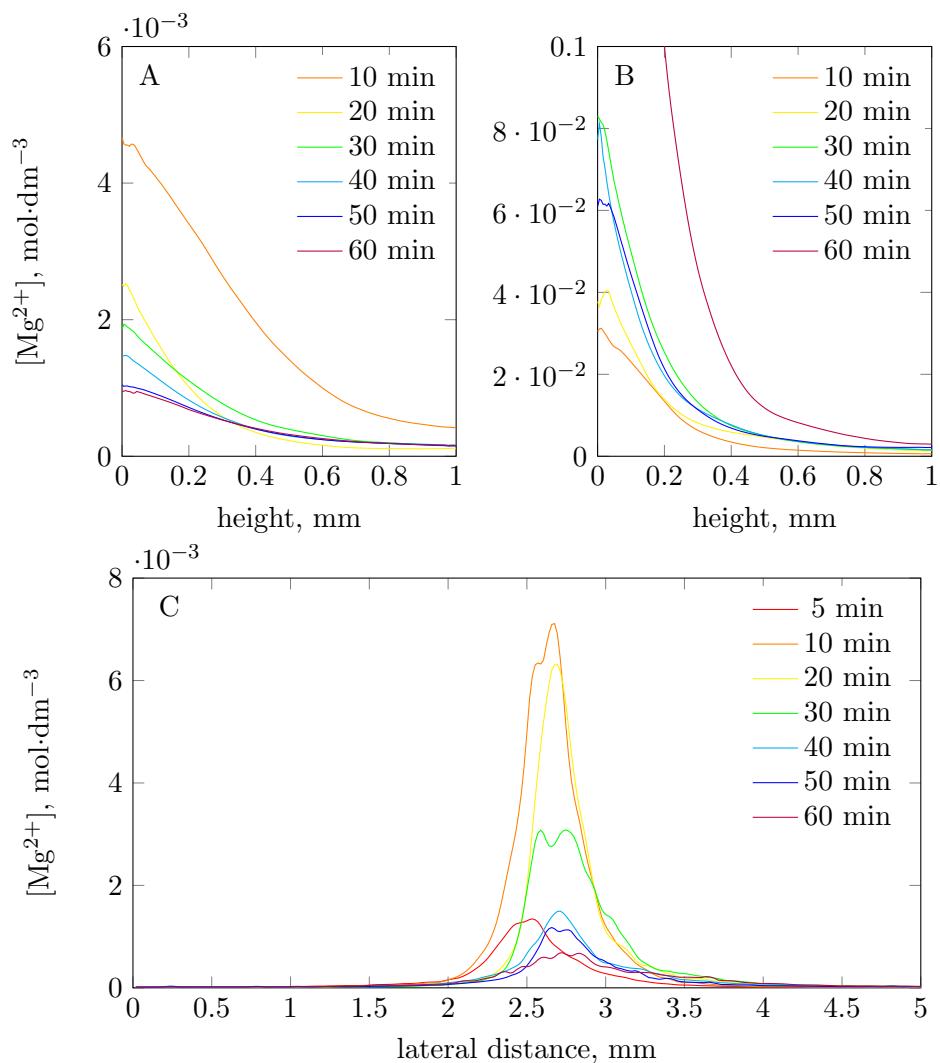


Figure 4.6: Retracting and lateral SECM linescans above the AZ63 magnesium-aluminium-zinc alloy sample initiated at different instances in time. Scan rate: 10 $\mu\text{m}/\text{s}$.

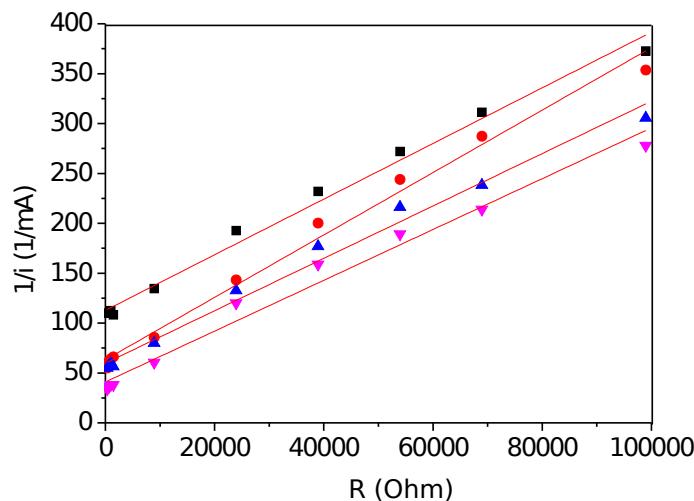


Figure 4.7: $1/i$ plots used for the determination of corrosion current between the AZ63 magnesium-aluminium-zinc alloy and various iron samples of different diameters. Diameter of the iron cathodes; black rectangle: $d = 0.59$ mm, red circle: $d = 0.76$ mm, blue triangle $d = 1.2$ mm, purple upside-down triangle: $d = 2.3$ mm.

diameters was also measured directly. As expected, current gets higher with increasing diameter. Corrosion current was $8.87 \mu\text{A}$, $15.83 \mu\text{A}$, $16.72 \mu\text{A}$, $24.4 \mu\text{A}$ with Fe sample diameters of 0.59 mm, 0.76 mm, 1.2 mm, 2.3 mm, respectively (Fig. 4.7). Using Faraday's law of electrolysis, this means, that $8.20 \cdot 10^{-11} \text{ mol Mg}^{2+}$ is being dissolved in every second from the Mg/Al sample ($\Omega_{0.76 \text{ mm}} = 8.20 \cdot 10^{-11} \text{ mol/s}$). This result is in fairly good agreement with the SECM measurement ($\Omega = 3.53 \cdot 10^{-11} \text{ mol/s}$). Ion flow rates from Mg/Al samples coupled with Fe samples of different diameters are proportional with the surface area of the sample; $\Omega_{0.59 \text{ mm}} = 4.60 \cdot 10^{-11} \text{ mol/s}$, $\Omega_{1.2 \text{ mm}} = 4.66 \cdot 10^{-11} \text{ mol/s}$, $\Omega_{2.3 \text{ mm}} = 1.26 \cdot 10^{-10} \text{ mol/s}$.

4.2 Optimization of scanning algorithms

4.2.1 SECM simulations

First, SECM scanning simulations were performed and the resulting images were compared (Figure 4.8). It was expected that the new, polar coordinate-based scanning algorithms would yield less distorted images than the traditional, raster-based algorithms. Not only the two new algorithms finish faster, but result images with lower distortion (Table 4.2). Mean squared error is $9.63 \cdot 10^{-3}$ and $2.95 \cdot 10^{-3}$ for the images scanned with the web and the arc algorithms, respectively. In comparison, mean squared error for the images scanned with traditional meander, fast-comb, and comb algorithms are $2.75 \cdot 10^{-2}$, $2.07 \cdot 10^{-2}$, and $2.75 \cdot 10^{-2}$, respectively.

4.2.2 Experimental SECM images

Next, the experimental SECM scans were performed, with the same scanning algorithms as the simulations were. The results (Figure 4.9) confirmed our presumption, that using the two new algorithms, images have less distortion, with higher similarity to the expected image.

Considering scanning time also, which are 440, 520, and 881 seconds for the meander, fast-comb, and comb algorithms, and 109, and 340 seconds for the web, and arc patterns respectively, it can be said, that the new scanning algorithms proposed in this paper shorten scanning time, and significantly improve imaging quality of circularly symmetric systems. There are two additional advantageous properties of the new algorithms. First, data is gathered in order of decreasing relevance, from closest to the target, to farthest from the target, without the corners of the rectangular raster patterns, which are of less importance, because of the larger distance from the target. Second, with the new algorithms, there is only positive imaging distortion (Figure 3.14I, J). The observed potential, for a perfect hemispherical concentration distribution, in theory, cannot be lower above the center than the maximum value. It also cannot be higher, since the probe starts scanning in the center, where $E_{cell}(t) \approx E_{cell}(\infty)$ (Equation 4.2). But positive distortion can occur as the probe leaves the close vicinity of the target, advancing towards coordinates with lower concentration. This has an importance when accurate quantitative information is required about the concentration distribution above the target, such as in estimating fluxes by fitting simulation to measured images [46, 119].

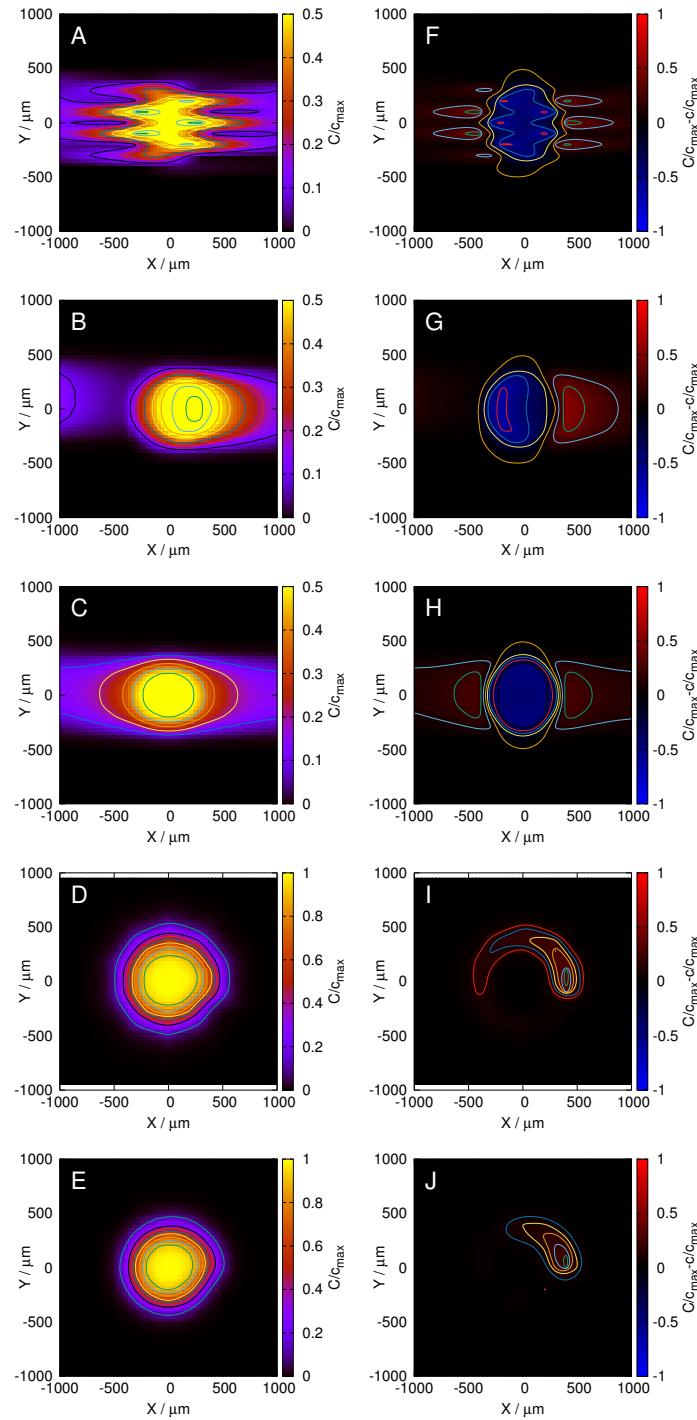
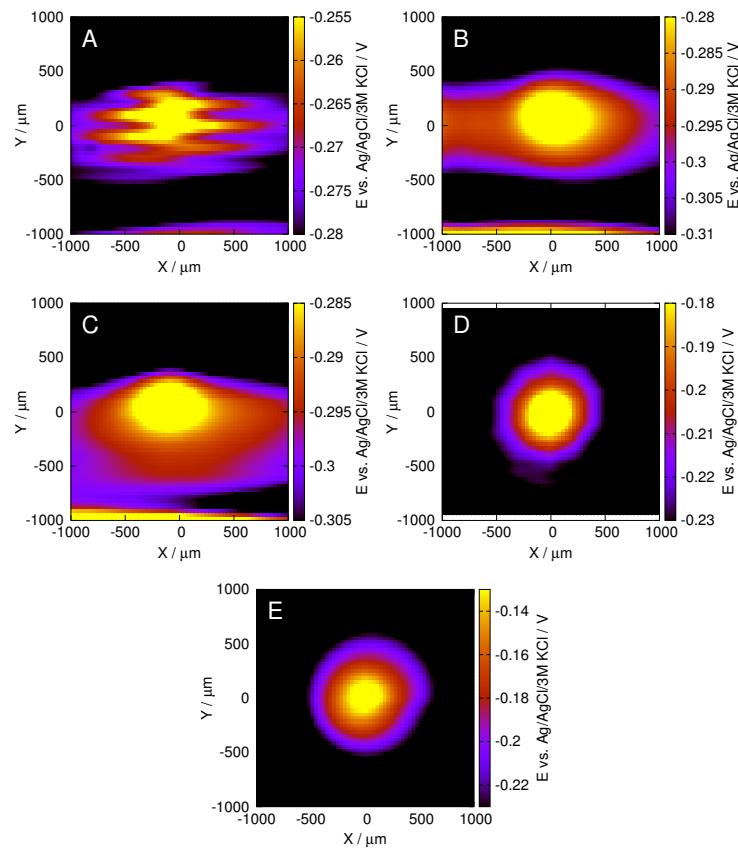


Figure 4.8: (A-E) Simulated SECM scans 100 μm above the disc source with the meander, fast comb, comb, web, and the arc scanning algorithms, respectively. All images were normalized to the maximum concentration of the expected image (c_{max}). (F-J) Deviation from the expected concentration image using the meander, fast comb, comb, web, and the arc scanning algorithms, respectively. „ C “ is the input (expected concentration profile), „ c “ is the output (observed concentration profile) matrix for the scan simulation.

Table 4.2: Comparison of the scanning algorithms.

Algorithm	Number of sampling points	Total scan time (s)	Mean squared error
Meander	441	440	$2.75 \cdot 10^{-2}$
Fast comb	441	520	$2.07 \cdot 10^{-2}$
Comb	441	881	$2.75 \cdot 10^{-2}$
Web	110	109	$9.63 \cdot 10^{-3}$
Arc	341	340	$2.95 \cdot 10^{-3}$

**Figure 4.9:** Experimental SECM scans 100 μm above the disc source with the (A) meander, (B) fast comb, (C) comb, (D) web, and (E) the arc scanning algorithms. Measuring electrode was a pH-sensitive antimony micro-electrode. Potential was measured against an Ag/AgCl/3M KCl reference electrode.

4.3 Signal processing in potentiometric SECM

4.3.1 Deconvolution of measurements performed with metal/metal-oxide microelectrodes

Deconvolution of measurements obtained with the metal/metal-oxide electrodes (antimony/antimony-oxide, and tungsten/tungsten-oxide) are attempted. First, a simple step response, then 1D linescans, and finally 2D raster images were deconvoluted, using four different electrodes; pH sensing microelectrodes made from antimony and tungsten, and ion selective microelectrodes for magnesium and potassium ions. This method has been already proposed in 1981 to determine the response time of potentiometric cells, based on the initial portion of the response curve, since it holds the same information. However, the authors of the paper about that method didn't go any further with their proposition. As Lindner and his coauthors write in [120]:

„This new definition [of response time] has several advantages in contrast to the earlier propositions and accepted definitions: it does not require the knowledge of the equilibrium potential value (E_∞); it holds the same sort of information as the time constant of a theoretical equation; it can be used in the case of response time curves consisting of different sections, e.g., even for rapid kinetic studies when $t \approx 0$ (6), and in practice it helps the analysts in determining when potential readings are to be taken. Accordingly to eliminate subjective errors in readings, one can regard the potential value corresponding to a limiting slope (dE/dt) as the steady-state or equilibrium value. This idea is realized in some pH meters produced by Radelkis (Hungary) in which a so-called slope controller is built in (16).

1 „

4.3.1.1 Minimal working example: deconvolution of a step response

The „minimal working example” method, originally used in programming, is a way of tracking down problems, and finding the cause of certain behaviour. The most important feature of a minimal working example is that it is as simple as possible, such that it is just sufficient to demonstrate the problem, but without any additional complexity which would make resolution harder. In this case, the minimal working example is a simple step function: the activity of the primary ion is changed

¹(6) refers to [121] and (16) refers to [122]

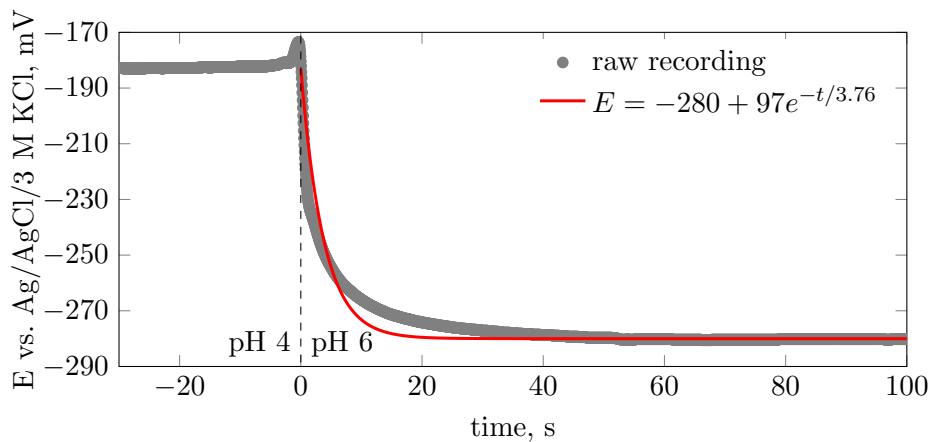


Figure 4.10: Transient response of the antimony microelectrode to analyte activity step. The measuring and reference electrodes were dipped into buffer solutions with pH = 4 before the measurements started, and pH = 6 at $t = 0$ s, respectively. Eq. 4.2 was fitted (red line) on the measurement (gray marks) from the pH step to the end of the curve when potential reaches equilibrium in the pH = 6 buffer.

suddenly, while the response of the potentiometric cell is recorded. The input of the system is a step function, the output is the recorded signal, an exponential decay function. If there is no additional distortion, and the transfer function is simply Eq. 3.3, the square step should be restored.

To measure the time-constant of the potentiometric cell employing the antimony microelectrode, the transient response curve was recorded while the pH = 4 buffer solution was changed to pH = 6. Then, Eq. 4.2 was fitted on the curve (Fig. 4.10). Based on the fit, time constant of the cell is $\tau = 3.76$ s, and $e^{-0.5 \text{ s}/3.76 \text{ s}} = 0.8755$, which means, only 12% of the total change occurs in 0.5 s ($1 - 0.8755 = 0.1245$).

The deconvolution of the very same recording was performed with several different time-constants, including that obtained from the response curve. Fig. 4.11 shows the results of those deconvolutions. As expected, the recording becomes most similar to the step function when the measured RC time-constant is used. When a higher value was substituted into Eq. 3.3, the recorded potential was underestimated, and the deconvolution recovered more than necessary. If a lower value was used, the cell was assumed to be faster than it actually was, and the deconvoluted potential values did not reach the equilibrium values. To see the effect of using a time constant other than the one that was obtained from the fit, statistics was performed on the deconvoluted data. Mean squared error was calculated by first taking the difference between the input function and the deconvoluted function at every time instance. Then the square of those differences was averaged. The input function was defined as

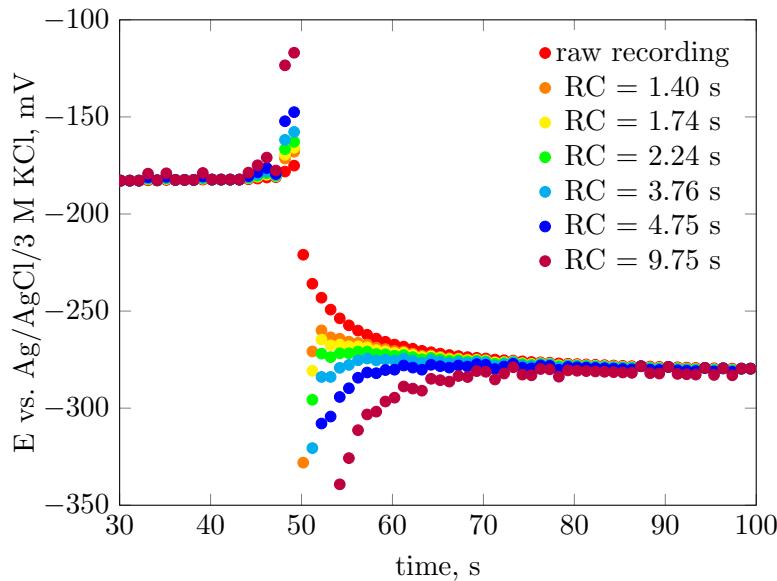


Figure 4.11: Transient response of the antimony microelectrode to analyte activity step (red), and decovolutions performed with different assumed RC time-constants (orange-purple). The measured time-constant was $\tau = 3.76$ s (cyan). The measuring and reference electrodes were dipped into buffer solutions with pH = 4 and pH = 6 respectively.

$$E_{cell}(t) = \begin{cases} -183.18 \text{ mV}, & \text{if } t < 50 \text{ s} \\ -280.20 \text{ mV}, & \text{if } t \geq 50 \text{ s} \end{cases} \quad (4.4)$$

The values for initial ($E_{cell}(0) = -183.18$ mV) and equilibrium ($E_{cell}(\infty) = -280.20$ mV) potentials were obtained by averaging certain portions of the recorded signal: the average from 0 to 49 s is -183.18 mV, and the average from 60 to 80 s is -280.20 mV. 4.4 should be obtained experimentally if the potentiometric cell was infinitely fast, and RC would be 0.

Table 4.3 shows the results of the statistical evaluation. Mean squared error rapidly increases when instead of the measured time constant, smaller or larger

Table 4.3: Comparison of the deconvoluted time-potential recordings with different assumed time-constants, including the measured value (highlighted in bold).

$e^{-0.5/RC}$	$RC(s)$	Mean squared error
raw recording (0)	raw recording (0)	53.43
0.7	1.4	22.03
0.75	1.74	15.88
0.8	2.24	9.01
0.8755	3.76	3.83
0.9	4.75	16.99
0.95	9.75	781.94

values were used in the deconvolution.

4.3.1.2 Investigation of possible surface processes

There are two interesting properties of the fit in Fig. 4.10. to be noted. First, the fitted curve is slightly different than the recorded response. The initial part of the measurement seems to be changing faster than it is expected from an RC circuit with a time-constant of 3.76 s, while the second part (from around 7 s) has a lower rate of change compared to the model. This means, that the transfer function is more complicated than Eq. 3.3, and the process cannot be properly described by simple potentiometric step response function. The effect of this behaviour can be observed in the first few data points of the deconvoluted measurement: there is a small overshoot compared to the equilibrium potential, even in the one that was deconvoluted with the measured RC . It was observed in all of the measurements, and the error was certainly carried through to all of the deconvoluted images, when the original measurement was performed with the antimony microelectrode.

The second discrepancy is that the RC determined in the previous section implies a very high resistance ($G\Omega$ range). It is possible to estimate the resistance of the antimony microelectrode from the specific resistance and the geometry of the antimony wire. Diameter, as mentioned in the chapter „*Materials and Methods*”, was 30 μm , length of the antimony wire was around 5 cm. Specific resistance of antimony is 417 $\text{n}\Omega\text{m}$ (at 20 °C) [118]. Then, resistance could be calculated as $R = 417 \text{ n}\Omega\text{m} \times 0.05 \text{ m} / ((15 \mu\text{m})^2 \times \pi) = 29.50 \Omega$. It must be noted however, that the measured resistance is a property of the whole cell, not just the microelectrode. Resistance of the reference electrode and the solution are included. Nevertheless, the difference between the estimated and the measured values is still too high. The very significant deviation from the expected value just calculated can be explained by a discontinuity defect in the antimony electrode, although it is unlikely, since all of the antimony electrodes appeared to have such a high resistance.

To verify that there was no discontinuity in the antimony microelectrodes, their resistance was measured directly by attaching one probe of a high precision multimeter to the microelectrode, while submersing the other probe and the tip of the microelectrode into a beaker containing mercury. Several electrodes has been tested this way, and their resistance never exceeded 20 Ω . The typical value was around 12 Ω , comparable to what was calculated from the electrode geometry and specific resistance of antimony.

Then, resistance of the whole cell was measured with the voltage divider method. Open circuit potential was -219.9 mV , while potential difference while the terminals were shorted through a 200 $\text{k}\Omega$ precision resistor was -105.0 mV . Resistance based

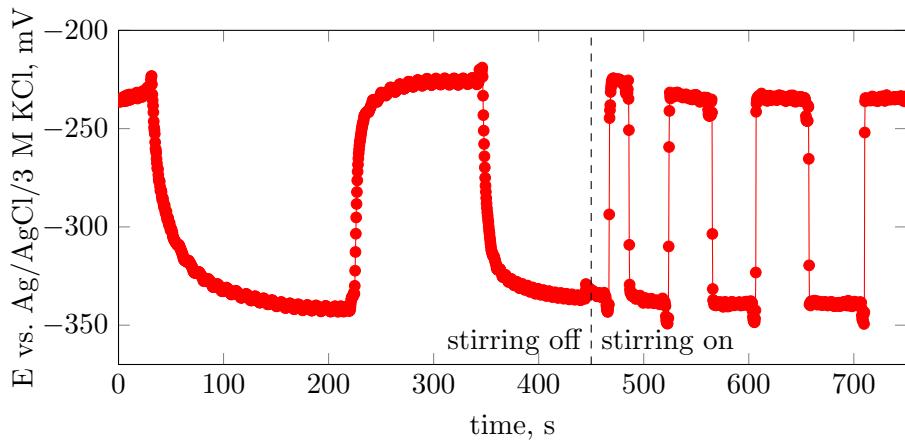


Figure 4.12: The effect of stirring on the antimony microelectrode. The buffer solution that was in contact with the electrodes was alternated between pH = 4 ($E \approx -240$ mV) and pH = 7 ($E \approx -340$ mV). Stirring was turned on at $t = 450$ s. To realize a quick change of the buffer solution without interrupting the potentiometric circuit, the „*hanging drop method*“ was used. For this experiment, the Arduino-based home-made DAQ was used.

on this result is $218.86\text{ k}\Omega$, which is the sum of the resistances of the microelectrode, the reference electrode, and the solution. This resistance is still not large enough to explain an RC time constant of 3.76 s , since then the capacitance should be $17.2\text{ }\mu\text{F}$, but it was in fact 11.15 nF (see section 4.3.2.1.).

Another way it could be explained is that there is a strongly adhered laminar layer (Prandtl-layer) on the surface of the electrode, and the exchange of this layer in a new solution is the slowest process as it is discussed by Lindner et al. in [123]. To test this hypothesis, step response measurements were carried out in unstirred and stirred buffers. The measuring electrode in this case was a large ($d = 1\text{ mm}$) antimony disc electrode, with a silver/silver-chloride quasi-reference electrode separated by 1 mm of epoxy resin. Because the antimony surface is much larger than in the case of a microelectrode, a more delayed response can be expected in the unstirred case, if there is indeed an adhered layer on the surface. By stirring the buffers when they are exchanged, the time constant should be the much lower RC time constant, with $R = 218.86\text{ }\Omega$.

Indeed, the response is much more delayed than in the case of a microelectrode, which can be observed in the response curves. The cell employing the microelectrode had an almost 100% response in about 1 minute (Fig. 4.10), while with the macro-electrode \sim 100% response was reached in about 200 s (first part of the curve in Fig. 4.12.). After stirring was turned on, the cell responded almost instantaneously (Fig. 4.12) to analyte activity step (that is depicted by the second part of the curve, after 450 s). Unfortunately, the magnetic stirrer introduced so much noise, that the time

constant couldn't be determined from this measurement. In another experiment, a filter was applied to decrease noise, but, as an RC filter, it added a time constant of its own to the measurement, and thus it could not be evaluated.

Despite this discrepancy, with deconvolution, a sharp step function could be obtained from the potential-time measurement, which was very similar to the step function caused by the sudden change in activity of the hydrogen ions. This means, that whatever the cause of the difference between the calculated and estimated resistance is, it distorts the measurement in a very similar way to the *RC* distortion. Based on the stirring experiments, this is most likely a surface process. Perhaps the antimony-oxide on the surface of the antimony microelectrode is porous, and it hinders diffusion. Since the recorded step response includes every parameter affecting the delay, the fitted function already accounts for this behaviour. The deconvolution function is certainly not complete and far from perfect. However, all deconvolution in this thesis was performed in a stepwise manner; by only using one $x - y$ pair from Eq. 3.3. X coordinate was most often 0.5 s, the time that elapses between two consecutive measurements. That part of the deconvolution function seems to describe the system very well.

4.3.1.3 Linescans with the antimony microelectrode

Going further, deconvolution of the simplest SECM experiment, the deconvolution of linescans was attempted. The potentiometric cell included the same measuring and reference electrodes as in the previous sections. A model system was built to perform the linescan on. In the system, a hemispherical pH gradient was created. The measured time constant ($\tau = 3.76$ s), implies a significant amount of imaging distortion if the equilibration period is only $t_e = 0.5$ s. As mentioned in the previous section, during 0.5 s, only about 12% of the total change occurs, and the measured difference between the recorded signal at two consecutive data acquisition points is significantly less than the difference between the equilibrium potentials. Since a single linescan can be completed very quickly, for reference a linescan was performed with $t_e = 5$ s. With this equilibration interval, the recorded potential at each point can be regarded equilibrium potential, and the linescan can be used as reference for the deconvoluted linescans performed with shorter t_e . Fig. 4.13A shows the raw linescans 100 μm above the graphite anode. Indeed, with $t_e = 0.5$ s, a significant amount of distortion can be observed. When t_e was increased to 1 s, the distortion decreased. After deconvolution however, all of the linescans became similar to the equilibrium linescans, regarding both their peak value, and shape (Fig. 4.13B).

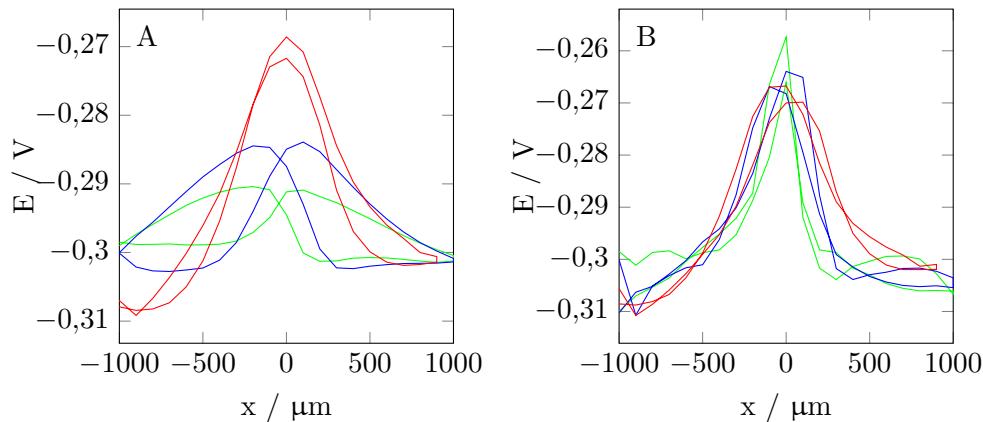


Figure 4.13: (A) Raw, and, (B) deconvoluted SECM linescans above the center of the target, at $h = 100$ mm height, using three different equilibration periods: 0.5 s, (green), 1 s, (blue), and 5 s, (red).

4.3.1.4 2D scans with the antimony microelectrode

Next, four 2D SECM scans were performed identically (Fig. 4.14A-D), with the meander scanning algorithm. The potentiometric cell and the studied system was the same as in the previous section. Again, line blur distortion in the raw images is visible along the alternating scanlines used by the meander scanning algorithm. By deconvoluting the images, the expected potential maps can be obtained (Fig. 4.14E-H).

Not only the circular shape of the target in the images is restored, but the peak value above the center of the target as well. Maximum value in the raw scans was around -300 mV, whereas in the deconvoluted image, it was about -260 mV, with a significant difference between the two.

4.3.1.5 2D scans with the tungsten microelectrodes

Additionally, 2D SECM scans were also performed with two different tungsten microelectrodes: one prepared from commercial tungsten microwire, and another from the filament of a 100 W Tungsram incandescent lighbulb. RC were determined with the same method, and were 4.62 s and 4.40 s, respectively. The studied target in this case was the zinc-copper galvanic pair. The scans were performed 100 μm above the copper target, while it was galvanically coupled to the zinc wire. Line blur distortion is also visible here in the raw images. After deconvolution the expected potential maps can be obtained (Fig. 4.15C-D). Electrode potential above the center of the target increased by about 70 mV in both cases, and the circular symmetry of the copper sample was restored in the image. Considering the sensitivity of the tungsten/tungsten-oxide electrode, the difference between the pH of the solution

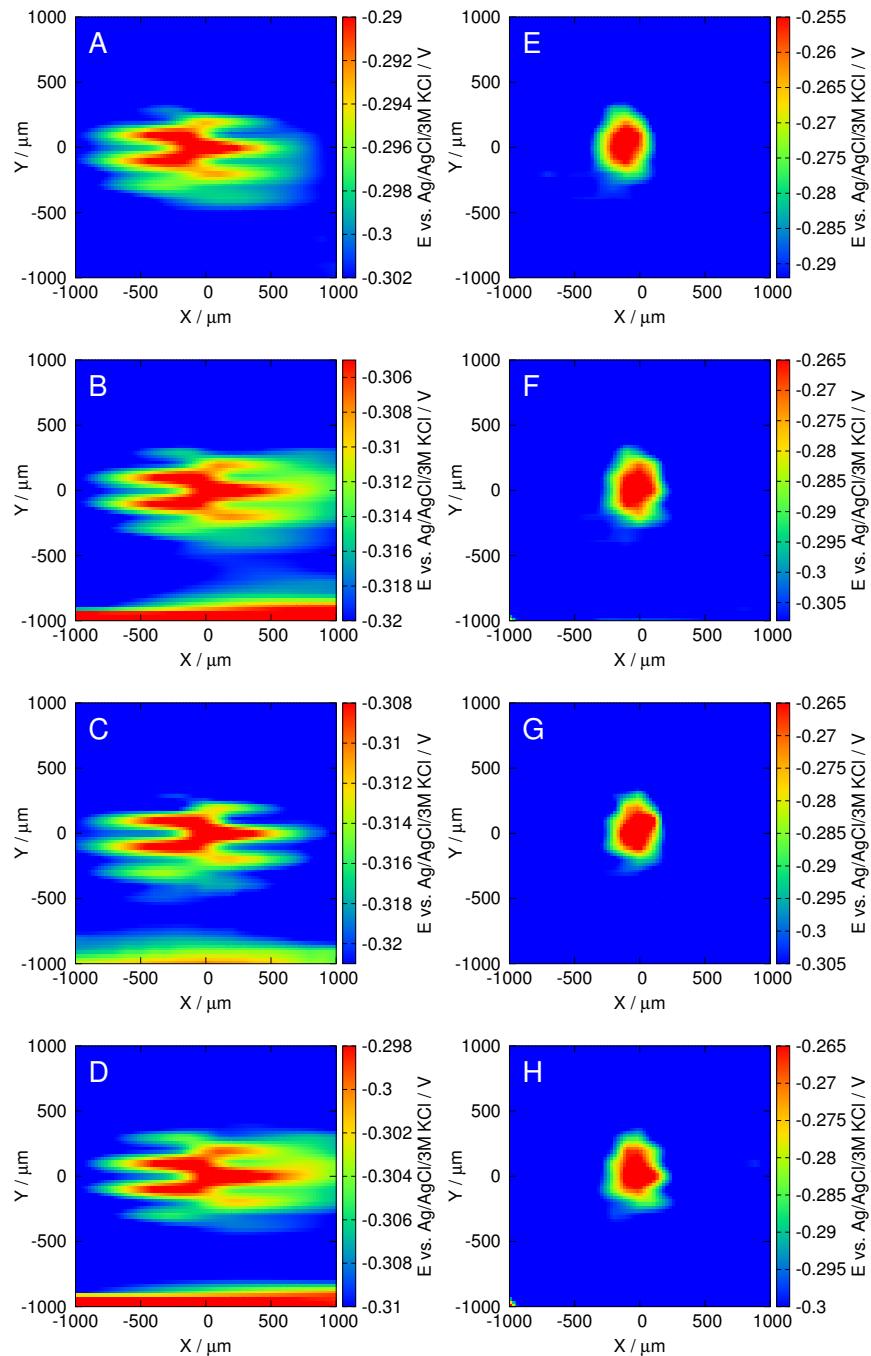


Figure 4.14: Parallel SECM images before (A-D) and after (E-H) deconvolution. Scans conducted with the antimony microelectrode. Note the different potential scales. Deconvolution restores not only the shape of the concentration profile, but the magnitude of the peak as well. The raster scan pattern was used with the meander algorithm starting in the bottom left corner of the image.

adjacent to the center of the target and the bulk pH would have been underestimated by about 1.5 pH units.

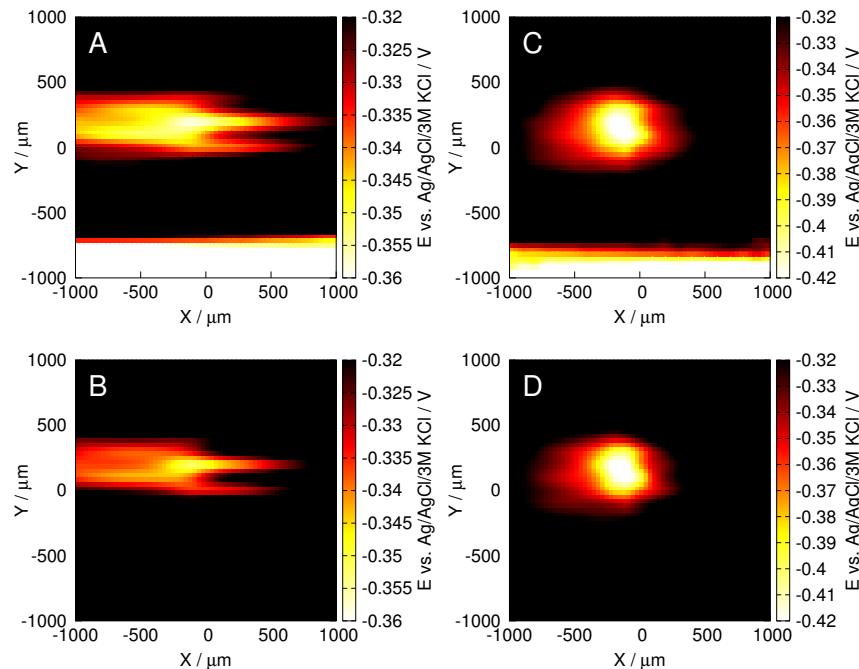


Figure 4.15: SECM image before (A-B) and after (C-D) deconvolution with microelectrodes prepared from commercial $d = 30 \mu\text{m}$ tungsten microwire (A) and tungsten filaments with the same diameter, taken from a 100 W Tungsram incandescent lightbulb (B). The raster scan pattern was used with the meander algorithm starting in the bottom left corner of the image.

4.3.2 Experiments with ion-selective micropipettes

Deconvolution was also applied to SECM scans performed with magnesium and potassium ion-selective micropipettes. In these cases however, RC was determined with another method. R and C were measured individually.

4.3.2.1 Linescans with a magnesium ion-selective micropipette

Measuring R and C . First, the Mg^{2+} ISME and the amplifier were characterized. Using the voltage divider method, electrode resistance of the micropipette was measured to be $197.31 \text{ M}\Omega$. Time constant of the cell with a $50 \text{ M}\Omega$ load inserted was 0.5577 s , therefore amplifier input capacitance (together with the capacitance of a 25 cm long coaxial cable between the electrodes and the amplifier) was 11.15 nF ($0.5577 \text{ s} / 50 \text{ M}\Omega$). Time constant of the potentiometric cell with the Mg^{2+} ion selective electrode could be obtained by multiplying R and C : $\tau = R \cdot C = 2.2 \text{ s}$.

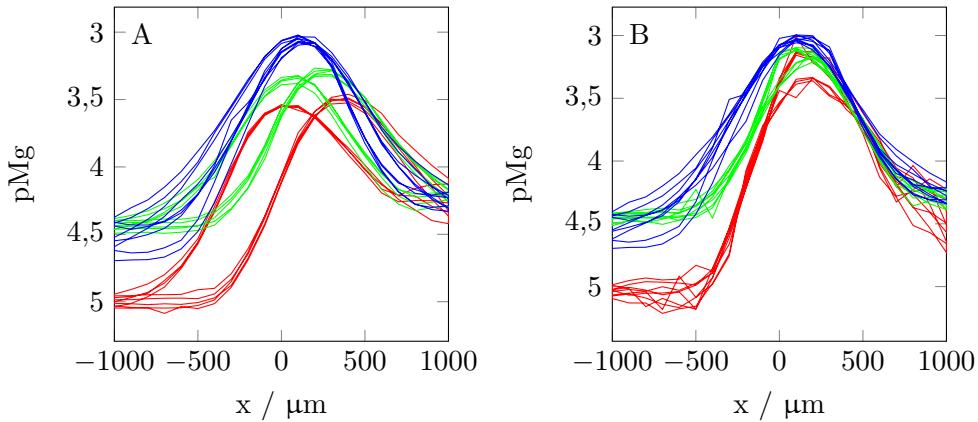


Figure 4.16: (A) Raw scan lines recorded $h = 100 \mu m$ over the center of the pipette orifice, which served as a Mg^{2+} ion diffusion source. (B) Scan lines obtained after deconvolution. t_e equilibration intervals were 4.9 s (blue), 1.9 s (green), and 0.4 s (red). Probe movement speed was 1000 $\mu m/s$, and probe movement interval was 0.1 s. 8 scan lines were recorded in each case, 4 forward, 4 reverse scans.

Sensitivity towards the primary ion was very close to nernstian, with 29.7 mV / decade.

Linescans. Next, line scans above the center of the target were performed using three different equilibration interval lengths. As expected, the shorter the time available for the cell for equilibration was, the more distorted the resulting scan became (Fig. 4.16A). Directional line blur distortion is visible along the raw scan lines recorded with shorter equilibration intervals (1.9 s, and 0.4 s). By setting t_e to 4.9 s, distortion became less visible. Based on the determined RC time constant, in 4.9 seconds, 89.22% of the total change occurs ($1 - e^{-4.9s/2.2s} = 0.8922$), and therefore the recorded signal is almost in equilibrium, and can be regarded as a reference for comparison with the concentration profiles obtained using smaller t_e parameters. With 1.9 s, and 0.4 s, only 57.87%, and 16.62% of the total change occurs respectively, causing a significant amount of distortion.

Using Eq. 3.4 and the measured RC , the scan lines could be deconvoluted, and the E_∞ values could be obtained (Fig. 4.16B). After deconvolution, almost no change can be observed in the scan line recorded with $t_e = 4.9$ s, which indicates that the recorded values in that scan were already in equilibrium. By deconvoluting the other scan lines with smaller t_e parameters, they became very similar to the equilibrium scan lines ($t_e = 4.9$ s). This indicates that the deconvolution restored the equilibrium scan line. With $t_e = 0.4$ s, a similar, low distortion image can be obtained as with $t_e = 4.9$ s, but in a fraction of the time that is required for the latter.

4.3.2.2 2D scans with the magnesium ion-selective micropipette

Going further, 2D raster scans were performed with the meander (Fig. 4.17A-D) and the fast comb (Fig. 4.18A-D) algorithms. Similarly as before, line blur distortion in the raw images is visible along the scanlines of the 2D raster. The shorter the equilibration period was, the more visible the distortion became. After deconvoluting the raw images, not only the circular shape of the target in the image is restored, but - based on the results of the linescan deconvolution - the maximum $p\text{Mg}^{2+}$ value above the center of the target as well, using the meander (Fig. 4.17E-H), and the fast comb scanning algorithms (Fig. 4.18E-H). For instance, maximum $p\text{Mg}^{2+}$ in the $t_e=0.4$ s meander raw scan is about 4.2, whereas in the deconvoluted image, it is about 3.6, with a significant difference between the two. This is important where accurate quantitative information is required about the target, such as in fitting simulated scans to measured ones to calculate mass transport rate [119].

4.3.2.3 2D scans with the potassium ion-selective micropipette

2D scans employing the most widely used potassium ion-selective micropipette were also carried out. The same cell was used as before, only the magnesium ion-selective micropipette was replaced with a potassium ion-selective micropipette. Resistance of the potassium ion-selective micropipette was measured with the same voltage divider method, and not surprisingly, the result was very similar; $R = 213.42 \text{ M}\Omega$. The time constant was $\tau = 2.38$ s. The target was the same micropipette source, except the filling gel was replaced with a 0.2 M KCl containing 4% agar-agar gel. The characteristic RC distortion is also visible in these images (Fig. 4.19A-B). After deconvolution, once again, the images resemble the radial geometry of the target.

4.3.3 Application: investigation of the corrosion of carbon steel

Corroding carbon steel was imaged as part of a collaboration with colleagues from the *University of Ibn Zohr*, Agadir. They were curious about the pH changes above the corroding sample while it was polarized anodically with different current densities applied. Since corrosion is highly localized, a single linescan above the center wasn't enough, as it might not have covered all of the local anodes, ie. the surface cannot be regarded homogeneous without proof. For this reason, the whole surface was scanned. The total surface area was about 0.2 cm^2 , and a relatively large image had to be taken for the whole sample to be included. A $6000 \mu\text{m} \times 6000 \mu\text{m}$ image was scanned with a step size of $100 \mu\text{m}$ in both directions. To make the scan as short as possible despite the large number of data acquisition

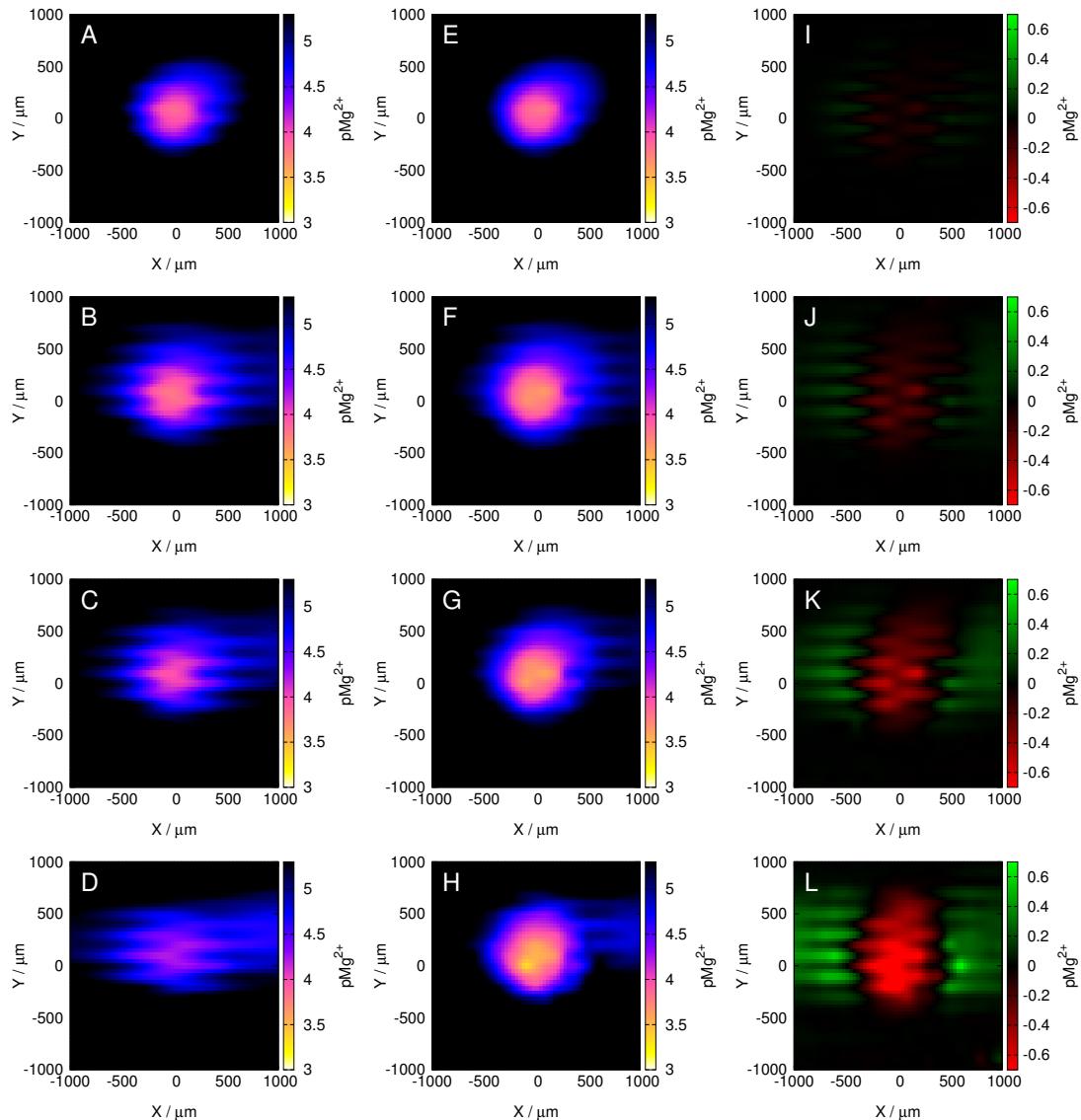


Figure 4.17: SECM images scanned with the meander algorithm, before (A-D) and after (E-H) deconvolution. Equilibration intervals from top to bottom row: $t_e = 4.9 \text{ s}, 1.9 \text{ s}, 0.9 \text{ s}, 0.4 \text{ s}$. Scanning started in the bottom left corner, scanlines were recorded horizontally from left to right. The difference between the raw and the deconvoluted images (I-L). Green: after deconvolution, pMg^{2+} increased, red: pMg^{2+} decreased in the images. That is, based on the original images, $[\text{Mg}^{2+}]$ concentration would have been over-, and underestimated at those specific coordinates, respectively. The raster scan pattern was used with the meander algorithm starting in the bottom left corner of the image.

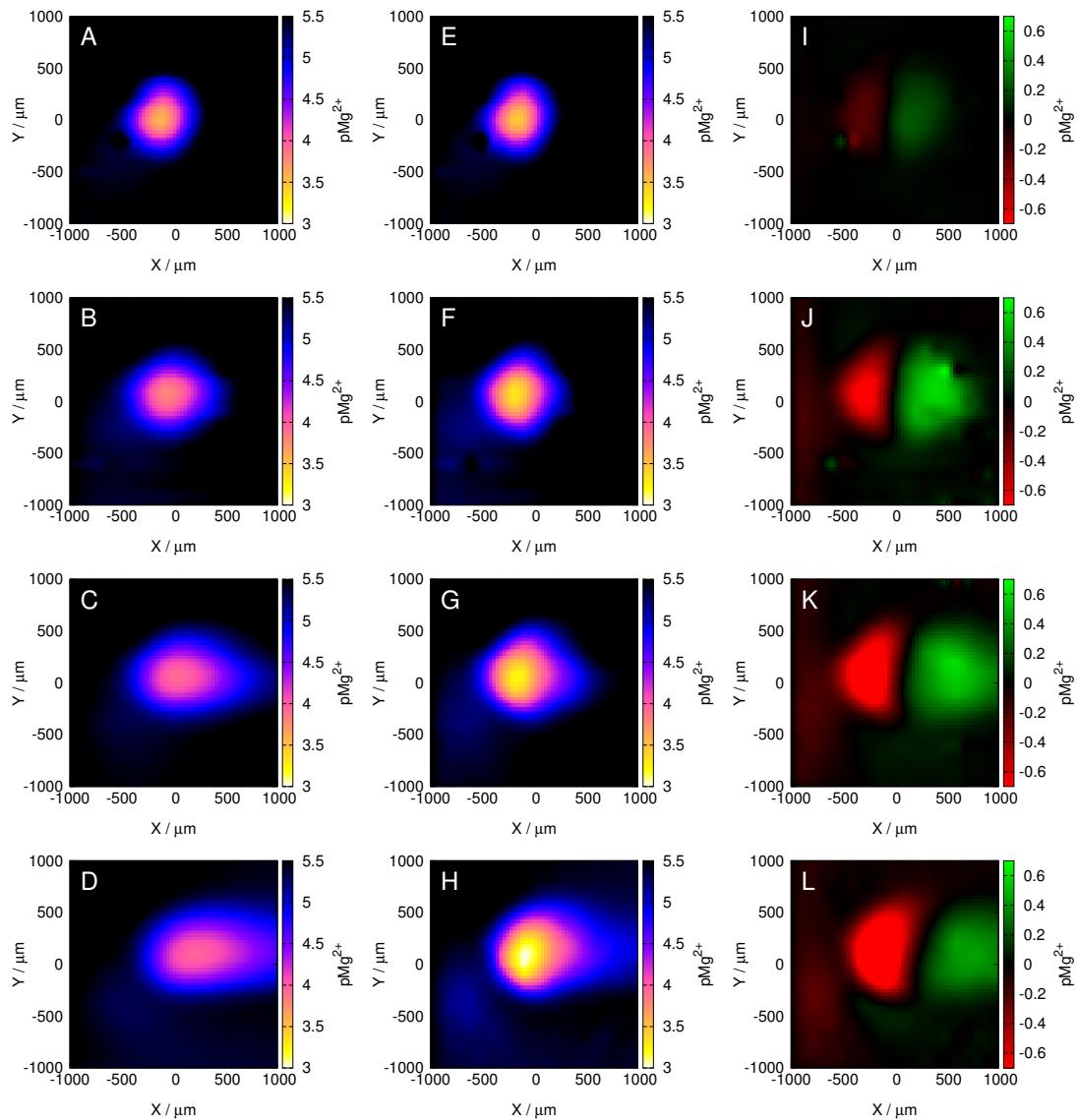


Figure 4.18: SECM images scanned with the fast comb algorithm, before (A-D) and after (E-H) deconvolution. Equilibration intervals from top to bottom row: $t_e = 4.9$ s, 1.9 s, 0.9 s, 0.4 s. Scanning started in the bottom left corner, scanlines were recorded horizontally from left to right. The difference between the raw and the deconvoluted images (I-L). Green: after deconvolution, pMg^{2+} increased, red: pMg^{2+} decreased in the images. That is, based on the original images, $[\text{Mg}^{2+}]$ concentration would have been over-, and underestimated at those specific coordinates, respectively. The raster scan pattern was used with the fast comb algorithm starting in the bottom left corner of the image.

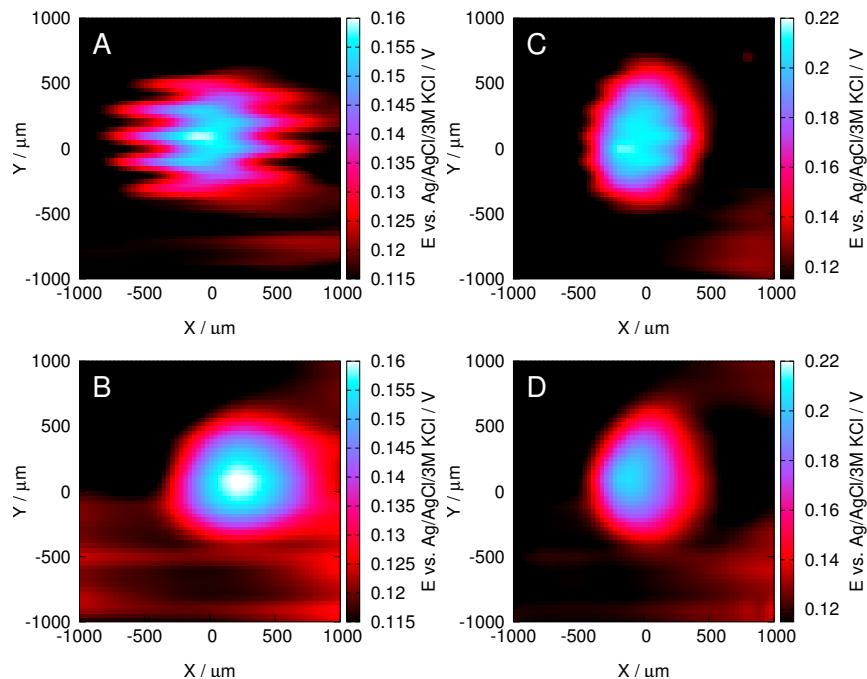


Figure 4.19: SECM image before (A-B) and after (C-D) deconvolution. Scans conducted with solid contact K^+ ion-selective micropipette. The raster scan pattern was used with the meander algorithm starting in the bottom left corner of the image.

points, a scanrate of $1000 \mu\text{m}/\text{s}$ was used. As expected, the image was distorted, and without any processing evaluation proved to be difficult. After deconvolution, conclusions about that particular experiment could be drawn. The irregular shape of the target (Fig. 4.20C) is recognisable after (Fig. 4.20B), but not before (Fig. 4.20A) the deconvolution. The difference between the original and the processed image is quite large. Potential difference between points of the bulk of the electrolyte and the electrolyte above the target was 140 mV and 200 mV before, and after the deconvolution, which is quite similar to values obtained in the previous experiments. Without any processing, pH would have been misestimated by about 1 pH unit. A different conclusion can be drawn based on the raw, and the deconvoluted image.

4.3.4 Possibility of „blind deconvolution”

„*Blind deconvolution*” is the technique of deconvoluting measured data without the complete knowledge of the transfer function that describes the convolution [124]. In the section titled „Minimal working example” I deconvoluted a simple step response with several different assumed RC time-constants, including the measured one. Even with just visual inspection of the deconvoluted data, one would choose the dataset that was obtained when the correct, measured RC was used in the de-

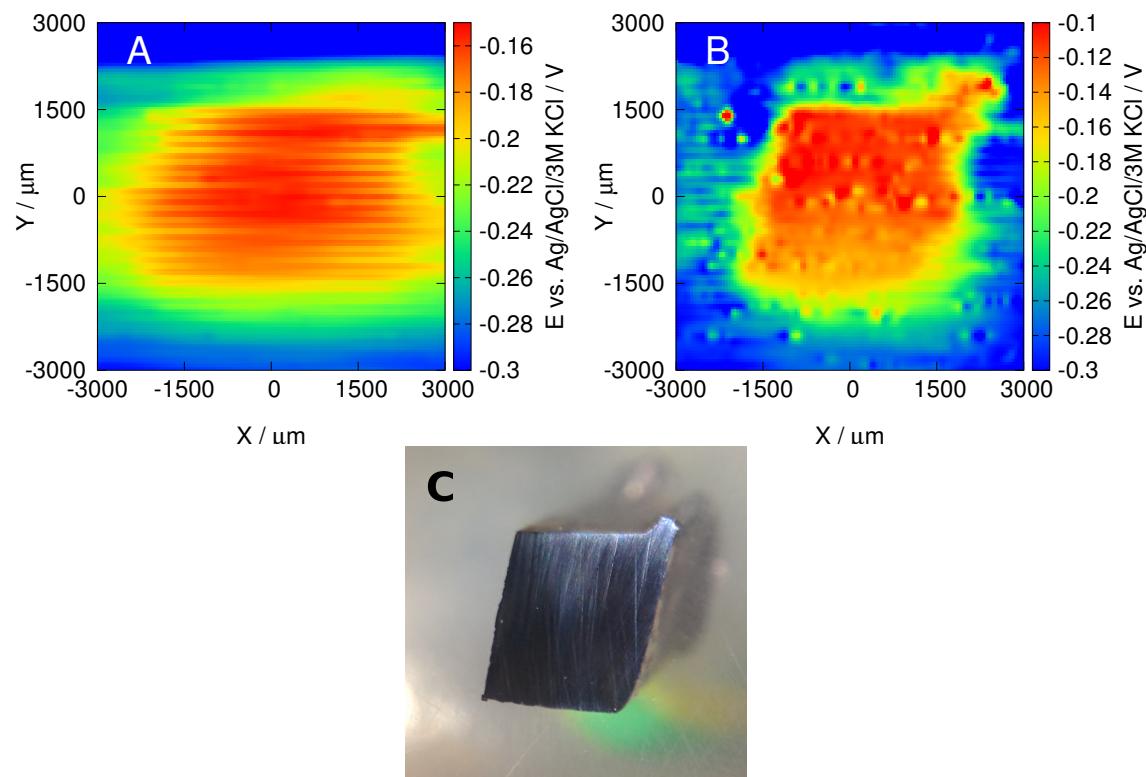


Figure 4.20: Raw (A), and deconvoluted (B) SECM image and microphoto (C) of a corroding carbon-steel sample polarized anodically with a current density of 10 mA/cm^2 . Measuring electrode was an antimony pH microelectrode. Potential was measured against an Ag/AgCl/3M KCl. Recorded $h = 100 \mu\text{m}$ above the surface with probe movement speed of $1000 \mu\text{m/s}$, equilibration interval 0.4 s .

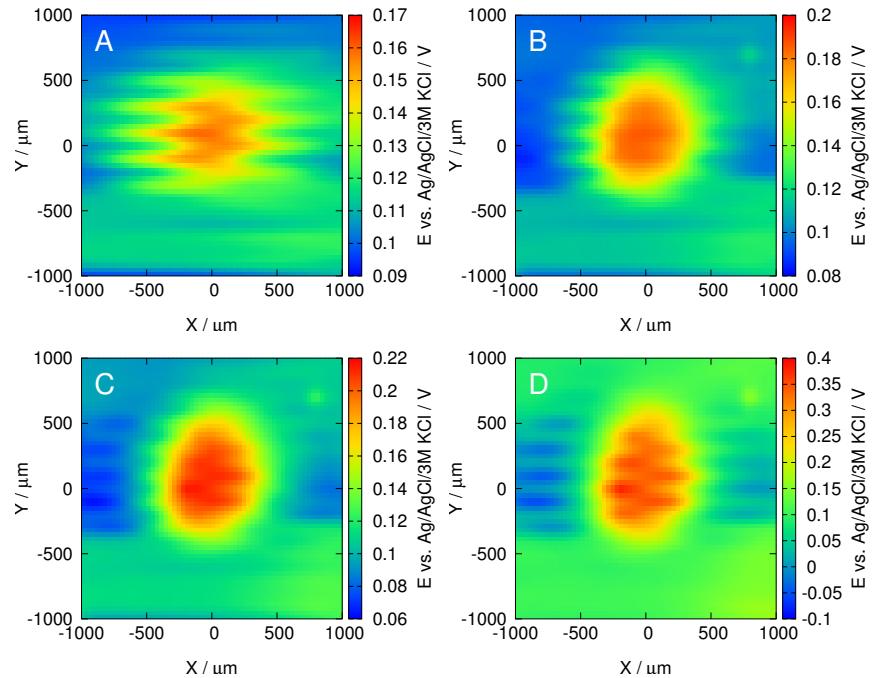


Figure 4.21: Deconvolutions of the image in Fig. 4.19A with different assumed RC time-constants, including the measured one. The measurement was done with a potassium ion-selective electrode. The measured time constant was $\tau = 2.38 \text{ s}$. Figure shows the raw image (A), and deconvolutions with assumed time-constants $\tau = 1.39 \text{ s}$ (B), $\tau = 2.38 \text{ s}$ (C), $\tau = 7.80 \text{ s}$ (D).

convolution. Based on this observation, blind deconvolution of 2D images might be possible. To explore this possibility, similarly to the step response deconvolution, I deconvoluted a pH image using the deconvolution function with several different time-constant substitutions, including the measured one.

A primitive version of applying this method involves the deconvolution with different RC values (Fig. 4.21), and choosing the images with the least amount of visible RC distortion. „Evaluating” distortion is relatively easy if the scanning algorithm is known. RC distortion is especially visible in images scanned with the meander algorithm. With this algorithm, subsequent scan lines in the images are shifted by twice the amount with respect to each other than with respect to a fixed point in the image, since the scan directions of subsequent lines are opposite.

Observing the images, (B) is still distorted, the individual lines are „shifted” in the same direction as in the raw image. In (D) however, they are shifted in the opposite direction, because the assumed time-constant is too high, and there is excess deconvolution in the image. (C) seems to be the best, but the lines are a bit shifted to the opposite direction. The best result based on visual inspection would be between (B) and (C), although much closer to (C). (C) is the image which was

obtained as a result of deconvolution with the measured time-constant.

A more advanced method would be a statistical approach, where one would try to detect any correlation between the scanning algorithm – taking into account the scan direction – and the image, and choose the deconvoluted image with the least correlation.

4.4 The effect of electric field on potentiometric SECM images

During galvanic corrosion, ions are being released from the anode. The measured potential of an ion selective microelectrode is thought to depend only on the activity of the primary ion. However, an electric field is also formed as a result of the potential difference between the surfaces of the galvanic pair, which has a direct influence on the potential of the measuring microelectrode, as it is depicted in Fig. 4.22. The measured potential is the sum of these two contributions:

$$\Delta E = E_M - E_R + (\phi_M - \phi_R) \quad (4.5)$$

where ΔE is the measured potential difference, E_M and E_R is the potential of the measuring and the reference electrode, and ϕ_M and ϕ_R are the local potentials in the electric field at the measuring and reference electrodes, respectively.

The potential difference caused by the electric field can be substantially large, even exceeding that of the potential difference associated with the activity of the primary ion. For instance, in [125] local alkalinization above the cathode of the studied galvanic pair could be observed as far as 2 mm from the surface, while oxygen reduction current had already reached the bulk level at only 900 μm from the target. This contradiction was explained by a contribution from the electric field of the galvanic pair. Similar discrepancy was found in [111, 126, 127], where the Mg^{2+} detected by the ion selective microelectrode exceeded the upper limit of detection. On the other hand, in [128] electrode potential of the employed magnesium ion selective electrode reached below potentials corresponding to the lower limit of detection of the electrode. These contradictory results can be explained by a contribution of the electric field that is formed during these experiments.

In this section, I present experimental evidence of this phenomenon, and investigate the extent to which it influences the final potentiometric SECM image. For this purpose, I use the Fe-AZ63 galvanic pair studied in the previous sections. The SECM probe was a solid contact magnesium ion selective microelectrode.

First, a series of consecutive Z-approach curves were recorded above the corroding AZ63 sample (as shown in fig. 4.23A). The first 6 measurements were conducted while the AZ63 sample was electrically isolated from the iron sample (red lines, a-b). As expected, Mg^{2+} activity slowly increased with time as a result of spontaneous corrosion. The overall change was about 10 mV in 5 minutes. Next, the two metals were connected at the rear of the mould. As result of establishing the galvanic connection, there was an immediate rise of about 40 mV in the measured potential of the microelectrode (transition from b to c, depicted by ΔE_1 in fig. 4.23A). Since

the galvanic coupling was established while the scanning tip was located 1000 μm from the AZ63 sample, the reported change cannot possibly be attributed solely to an abrupt increase in Mg^{2+} activity. Indeed, such a 40 mV change would correspond to an increase of ~ 1.5 orders of magnitude in Mg^{2+} activity occurring in less than one second. Immediately after, six additional Z-approach curves were recorded during the galvanic coupling. The resulting accelerated dissolution of Mg^{2+} can be distinguished from the blue curves (c-d) in fig. 4.23A. Intense gas evolution could be observed on the surface of the AZ63 sample, which explains the noticeably more noisy curves recorded in this case. During this period of galvanic coupling, the potential sensed at the ISME, when situated at $h = 1000 \mu\text{m}$, increased by ~ 40 mV. This rise (ΔE_2) can be totally attributed to the increase in activity of the dissolving metal, i.e.: $\Delta E = 29.5 \text{ mV} \cdot \Delta \lg[\text{Mg}^{2+}]$. Finally, when the galvanic connection was stopped, 2 additional Z-approach curves were measured (green curves in fig. 4.23A). A sudden jump in potential (ΔE_3 , transition from d to e) can be observed, of the same magnitude as before, though in the opposite direction, as a result of electric field vanishing. The shape of the latest Z-approach curves is very similar to the initial approaching curves recorded before galvanic connection was established, though they are shifted by about 40 mV in the positive direction. This is the result of the enhanced corrosion during the second phase of the experiment; Mg^{2+} activity changed by about the same factor along the length of the scan-line. The shape of the Z-approach curves recorded during the galvanic coupling is notoriously different from those recorded during the spontaneous corrosion of the metal. This is because the contribution of the electric field, just like the contribution from Mg^{2+} , is not uniform at different distances on the scanned line. The strength of the electric field is inversely proportional to the square of the distance. The shape of the function $1/z^2$ is recognizable from these plots.

An attempt was made to distinguish the effect of the electric field from that of the Nernstian response of the ISME by subtracting curve *b* from the subsequent curve *c*. *B* is the result of the Nernstian response, while *c* features the contribution from the electric field as well. Since *c* was recorded just after *b* in a short period of time, it can be assumed that there was no significant increase of Mg^{2+} concentration during these two scans, therefore *c* is just $b + \Delta\phi$. The result of the subtraction is curve *f* in fig. 4.23A, which can be regarded as the effect of the electric field formed between the galvanic pair.

In another series of experiments, the ISME was maintained at a constant height from the metal surface, and its potential was recorded as a function of time, while the galvanic connection was established between the two metals (fig. 4.23B). Thus, the tip was first positioned 100 μm above the center of the AZ63 wire (red curve in

fig. 4.23B), and for about 300 s the spontaneous corrosion of the alloy sample was recorded. Then, the galvanic connection was established, and a sharp increase in potential of about 70 mV could be observed. This change would correspond to a two orders of magnitude increase of Mg^{2+} activity in a very short period of time. When the galvanic connection was removed, a potential change of the same magnitude, though opposite direction could be observed. In order to discard the possibility that this rise could be still explained by an abrupt release of Mg^{2+} from the surface, the experiment was repeated while the tip was positioned 1000 μm above the target (blue curve in fig. 4.23B). A very similar sequence of potential changes could be observed, despite the big separation between the probe and the corroding sample. The only plausible explanation is that the abrupt change in the recorded potential is due to the electric field developed between the two metals.

Finally, in order to demonstrate the influence of the electric field on SECM imaging, measurements were made after 30 minutes of galvanic coupling by using a constant 100 μm tip-sample distance. Then the galvanic connection was ceased, and immediately another 2D scan was recorded above the Mg disk. The sequence of the two images can be seen in fig. 4.24. Apparently, in the case of galvanic coupling, a 0.1 M Mg^{2+} activity is monitored even in the bulk of the solution, whereas above the center of the disk the activity reaches the implausible 10^4 M value by using the calibration curve for calculation. In fig. 4.24B the measured values are in the linear range of the ISME, and the overall potential change is several orders of magnitude smaller than in fig. 4.24A.

The effect of the electric field in certain potentiometric SECM experiments has been demonstrated experimentally, as suspected by certain researchers in corrosion science for some time. A strong electric field is formed around galvanic coupling of dissimilar metals, that causes significant over- or underestimations of the real primary ion activity. The reason for this feature is that the electric field has a direct influence on the measured potential at the ISME.

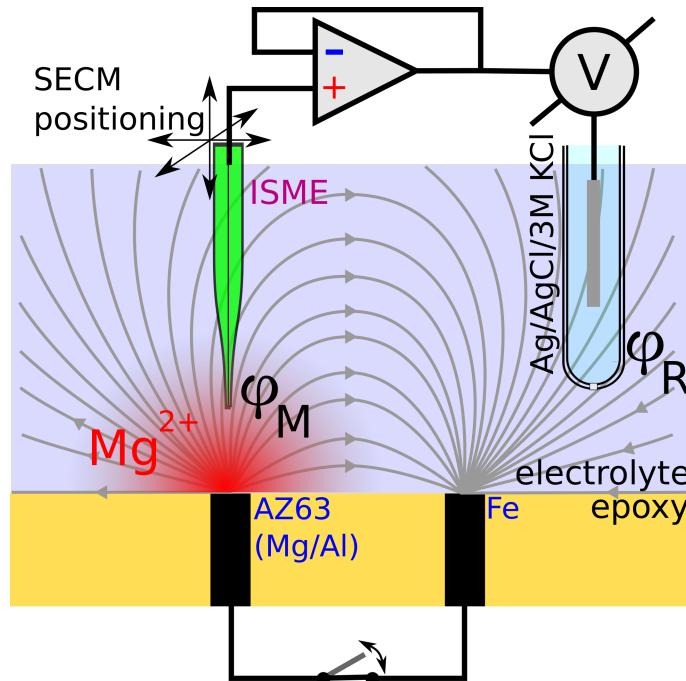


Figure 4.22: An electric field is formed between the surfaces of the galvanic couple. The potential difference between the measuring (ϕ_M) and reference (ϕ_R) electrodes is added to the Nernstian potential associated with the activity of the primary ion.

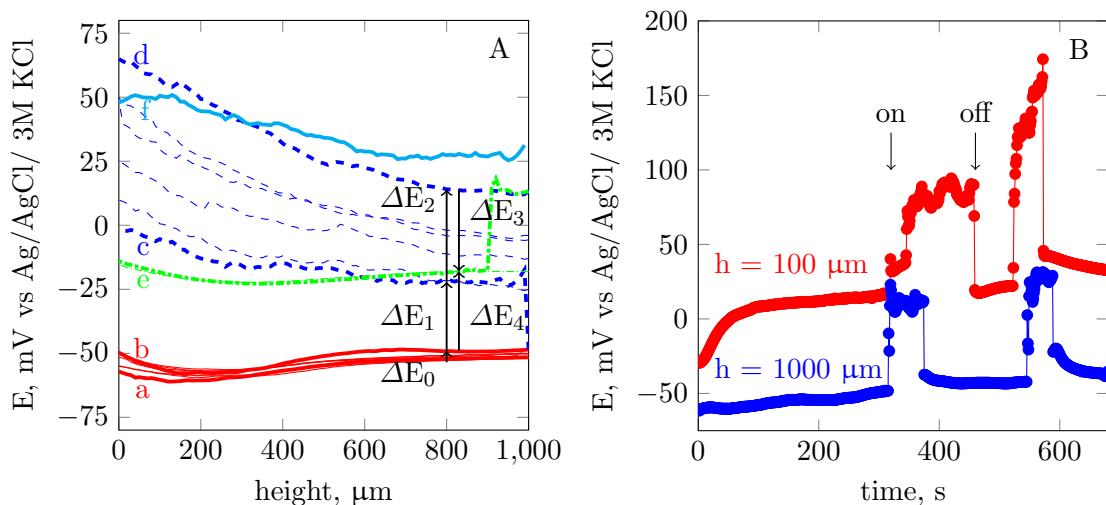


Figure 4.23: (A) Sequence of consecutive Z-approach curves recorded above the center of the AZ63 wire with a Mg^{2+} ISME. Step size: 10 μm . 500 ms settling time was allowed for the potentiometric cell at each points before measurements. Lines in chronological order: solid red = spontaneous corrosion, dashed blue = galvanic corrosion, dash dotted green = spontaneous corrosion. (B) Stationary recordings above the center of the AZ63 target with the ISME placed at: red = 100 μm , blue = 1000 μm distance from the metal. On/off denote the moment when galvanic coupling was either established or ceased. Temporal resolution was 1 Hz.

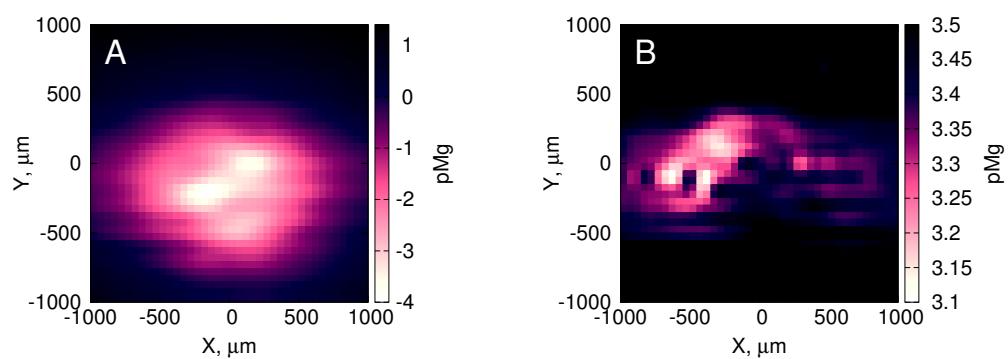


Figure 4.24: 2D Mg^{2+} ion distributions above the AZ63 wire while: (A) galvanically connected to Fe and (B) immediately after ceasing electrical connection between the two metallic materials. Tip-sample distance: 100 μm .

Chapter 5

Conclusions

The present work has been devoted to improve potentiometric Scanning Electrochemical Microscopy. Scanning is relatively slow due to the long response time of the potentiometric measuring cell. Shortened scanning time is useful when the studied system is changing. When scanned too fast however, distortion is added to the image. I've successfully sped up the technique without compromising image quality. In another effort, I've managed to separate the effect of electric field from the Nernstian potential response of the ion selective microelectrode.

The main results are summarized in the thesis points:

1. I've successfully shortened response time of the potentiometric cell by using low resistance, solid-contact microelectrodes. I've compared them to conventional, liquid contact microelectrodes by basic characterization and model system study to prove the improved performance.
2. Taking advantage of the new solid-contact electrodes, I've studied the galvanic corrosion of magnesium and the AZ63 magnesium alloy by mapping the concentration of dissolving ions. I used the new solid contact ion selective microelectrodes as SECM probes. This allowed faster scan rates.
3. I've estimated the corrosion current based on the SECM measurements, and compared the result with that obtained with another, established method; the indirect measurement of corrosion current. After applying Faraday's Law of Electrolysis, the two results could be compared. They were very similar, suggesting the applicability of SECM in obtaining quantitative results.
4. I've designed new scanning patterns and algorithms, optimized to radially symmetric targets. I've proven that with these new patterns and algorithms, image distortion is lower compared to the conventional ones, by numerical simulations and experimental SECM scans.

5. I've shown that by using deconvolution, RC distortion can be significantly lowered in the potentiometric SECM images. To prove the validity of the technique, I've compared deconvoluted images to equilibrium images scanned at a rate which allowed to record equilibrium potentials.
6. I've used deconvolution to restore potentiometric SECM images about a corroding carbon steel sample. Evaluation of this data was possible, because scanning time *and* distortion was reduced at the same time.
7. I've shown the applicability of blind deconvolution. This method can be used on measurements where the convolution function cannot be determined.
8. I've proven that the electric field present in many studied systems – galvanically corroding ones in particular – affects the measured potential. The electric field has a direct influence on the measured potential, which is then a sum of this contribution and the Nernstian response associated with ion activity. This effect can cause serious errors in interpretations in the measurements. In this case, the error was almost four orders of magnitude. By taking this effect into account, a more accurate conclusion can be drawn.

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List of Abbreviations

SECM	Scanning Electrochemical Microscopy
SPM	Scanning Probe Microscopy
AFM	Atomic Force Microscopy
STM	Scanning Tunnelling Microscopy
d_i	internal diameter
d_o	external diameter
THF	tetrahydrofuran
PVC	poly(vinyl chloride)
PTCB	potassium tetrakis(4-chlorophenyl)-borate
oNPOE	2-nitrophenyl octyl ether
ISME	ion-selective microelectrode
EDOT	ethylenedioxothiophene
PEDOT	poly(3,4-ethylenedioxothiophene)
$\text{BMIM}^+\text{PF}_6^-$	1-butyl-3-methylimidazolium hexafluorophosphate
r	scanrate ($\mu\text{m}/\text{s}$)
s	step size (μm)
t_e	equilibration interval length (s)
$E_{\text{cell}}(\infty)$	equilibrium cell potential difference (mV)
$E_{\text{cell}}(0)$	cell potential difference prior to change (mV)
$E_{\text{cell}}(t)$	cell potential difference at time t (s)
τ	time constant (s)
RC	time constant of a series RC circuit (s)
D	diffusion coefficient
R_{ISME}	resistance of the ion-selective microelectrode (Ω)
E_{OCP}	open circuit potential of the measuring electrode (mV)
Ω	ion flux
c_s	surface concentration ($\text{mol}\cdot\text{dm}^{-3}$)
z, h	height of scan (μm)
R_o	output resistance (Ω)
R_i	input resistance (Ω)

C_i	input capacitance (F)
R_0	electrode resistance (Ω)
C_s	cable capacitance (F)
$vcc+$	positive voltage rail of the power supply
$vcc-$	negative voltage rail of the power supply
RPM	revolution per minute
emf	electromotive force
LIX (membrane)	liquid ion exchanger (membrane)
CWE	coated wire electrode
PBM	Phase Boundary Model
NPP	Nernst-Planck-Poisson (Model)
DAQ	Data Acquisition

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Appendix

5.1 Diffusion and SECM scan simulation

```
program diffusion

implicit none

integer :: x_size, y_size, z_size
integer :: res, height
integer :: time_res

real :: const=0.017575
!for resolution of 20umx20um and 0.1s

integer :: h,i,j,k,x,y,m,switch,cells
real, dimension(0:101,0:101,0:101) :: a, b
real, dimension(1:100,1:100,1:100) :: flux
integer, dimension(1:100,1:100,1:100) :: mask
real :: pi=3.1415926535897932384626433832795
real maximum
real e0, x_real, y_real
real, dimension(0:100,0:100) :: sim
integer direction, divisions
real alpha, circumference, r_real
integer r, n
direction=-1
maximum=0.0000000000000000
height=50

a=0.
```

```

b=0.
mask=1

do i=1, 100
  do j=1, 100
    if ( ((i-50)**2+(j-50)**2) < 20**2 ) then
      !20 radius of source is 400 um
      flux(i,j,1)=0.1
    endif
  end do
end do

open(1,file='flux_at_1um.txt')
do i=0, 100
  do j=0, 100
    write(1, *) i*20, j*20, flux(i,j,1)
  end do
end do
close(1)

open(1,file='flux_at_1um_final_res.txt')
do i=0, 100, 5
  do j=0, 100, 5
    write(1, *) i*20, j*20, flux(i,j,1)
  end do
end do
close(1)

do k=1, 100
  do i=1, 100
    mask(i, 1, k)=0
    mask(i, 100, k)=0
  end do
end do
do k=1, 100
  do j=1, 100
    mask(1, j, k)=0
    mask(100, j, k)=0
  end do
end do

```

```

    end do
end do
do j=1, 100
  do i=1, 100
    do i=1, 100
      mask(i , j , 100)=0
    end do
  end do
end do

b=a
switch=0
! x=i , y=j , z=k , h=time
do h=1, 500 ! M A I N L O O P
  ! All real cells computed.
  ! Not cycled: borders , which are all zeros .
  do k=1, 100
    do j=1, 100
      do i=1, 100
        if (mask(i , j , k)==1) then
          cells=6
          if ((k==1) .or. (k==100)) then
            cells=cells -1
          endif
          if ((j==1) .or. (j==100)) then
            cells=cells -1
          endif
          if ((i==1) .or. (i==100)) then
            cells=cells -1
          endif
          b(i , j , k)=a(i , j , k)+const *(a(i , j +1,k)&
          +a(i -1,j , k)+a(i +1,j , k)+a(i , j -1,k)&
          +a(i , j , k-1)+a(i , j , k+1)- cells *a(i , j , k))
        endif
      end do
    end do
  end do

do j=1, 100

```

```

do i=1, 100
    b(i,j,1)=b(i,j,1)+flux(i,j,1)
end do
end do

a=b
print *,h

end do

do i=0, 100
    do j=0, 100
        if (a(i,j,height)>maximum) then
            maximum=a(i,j,height)
        endif
    end do
end do
print *,maximum
do i=0, 100
    do j=0, 100
        a(i,j,height)=a(i,j,height)/maximum
    end do
end do

! OUT PUT
open(1,file='real_100um_fullres.txt')
do i=0, 100
    do j=0, 100
        write(1, *) i*20, j*20, a(i,j,height)
    end do
end do
close(1)

open(1,file='real_100um_finalres.txt')
do i=0, 100, 5
    do j=0, 100, 5
        write(1, *) i*20, j*20, a(i,j,height)
    end do
end do

```

```

end do
close(1)

! SECM scanning simulation
! FAST COMB
sim=0
e0=a(0,0,height)
open(1, file='fast_comb.txt')
do y=0, 100, 5
  do x=0, 100, 5
    sim(x,y) = a(x,y,height)&
    +(e0-a(x,y,height))*0.8
    e0=sim(x,y)
    write(1, *) x*20, y*20, sim(x,y)
  end do
  do x=100, 0, 5
    e0 = a(x,y,height)&
    +(e0-a(x,y,height))*0.9
  end do
end do
close(1)

! MEANDER
sim=0
e0=a(0,0,height)
open(1, file='meander.txt')
do y=0, 100, 5
  direction=direction*(-1)
  if (direction==1) then
    do x=0, 100, 5
      sim(x,y) = a(x,y,height)&
      +(e0-a(x,y,height))*0.8
      e0=sim(x,y)
      write(1, *) x*20, y*20, sim(x,y)
    end do
  else
    do x=100, 0, -5
      sim(x,y) = a(x,y,height)&

```

```

        +(e0-a(x,y,height))*0.8
        e0=sim(x,y)
        write(1,*)
        x*20, y*20, sim(x,y)
    end do
endif
end do
close(1)

! COMB
sim=0
e0=a(0,0,height)
open(1,file='comb.txt')
open(2,file='comb-pattern.txt')
do y=0, 100, 5
    do x=0, 100, 5
        sim(x,y) = a(x,y,height)&
        +(e0-a(x,y,height))*0.8
        e0=sim(x,y)
        ! write(1,*)
        ! x*20, y*20, sim(x,y)
        write(2,*)
        x*20, y*20, sim(x,y)
    end do
    do x=100, 0, -5
        sim(x,y) = (sim(x,y) + a(x,y,height))&
        +(e0-a(x,y,height))*0.8)/2
        e0=a(x,y,height) + (e0-a(x,y,height))*0.8
        write(1,*)
        x*20, y*20, sim(x,y)
        write(2,*)
        x*20, y*20, sim(x,y)
    end do
end do
close(1)
close(2)

! WEB
x_real=0
y_real=0
e0=a(50,50,height)
open(1,file='web.txt')
do r=0, 10

```

```

do alpha=0, 2*pi-pi/10, 2*pi/10
  x_real=100*r*cos(alpha)
  y_real=100*r*sin(alpha)
  x=nint((x_real+1000)/20)
  y=nint((y_real+1000)/20)
  e0=a(x,y,height)+(e0-a(x,y,height))*0.8
  write(1, *) nint(x_real), nint(y_real), e0
  print *, x_real, y_real
end do
end do
close(1)

! ARC
x_real=0
y_real=0
e0=a(50,50,height)
open(1,file='arc.txt')
write(1, *) 0, 0, e0
do r=0, 10
  circumference=2*r*100*pi
  divisions=circumference/100
  do alpha=0, 2*pi-2*pi/divisions, 2*pi/divisions
    x_real=100*r*cos(alpha)
    y_real=100*r*sin(alpha)
    x=nint((x_real+1000)/20)
    y=nint((y_real+1000)/20)
    e0=a(x,y,height)+(e0-a(x,y,height))*0.8
    write(1, *) nint(x_real), nint(y_real), e0
    print *, x_real, y_real
  end do
end do
close(1)

end program diffusion

```

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