

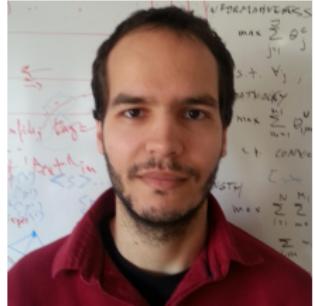
# AD<sup>3</sup>: A New Decoder for Structured Prediction

André Martins



Joint NAACL/ICML Symposium—Atlanta, 15/06/13

# Collaborators



■ Mário Figueiredo, Noah Smith, Pedro Aguiar, Eric Xing, Miguel Almeida.

# Structured Prediction and NLP

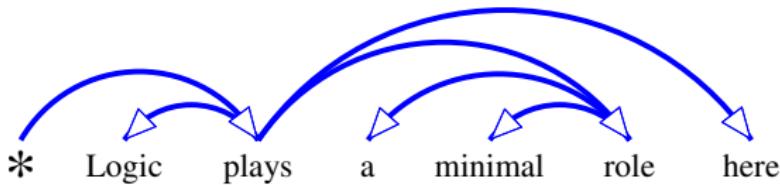
**Structured prediction:** a machine learning framework for predicting structured, constrained, and interdependent outputs

**NLP** deals with *structured* and *ambiguous* textual data:

- machine translation
- speech recognition
- syntactic parsing
- semantic parsing
- information extraction
- ...

# Dependency Parsing

Map **sentences** to their **syntactic structure**.



- A lexicalized syntactic formalism
- Grammar functions represented as lexical relationships (dependencies)

(Eisner, 1996; McDonald et al., 2005; Nivre et al., 2006; Koo et al., 2007)

# Multi-Document Summarization

Map a set of related **documents** to a brief **summary**.



Obama hopes for 'continued progress' in Myanmar

## STORY HIGHLIGHTS

- Obama meets with pro-democracy icon Aung San Suu Kyi and Myanmar's president
- He's the first sitting U.S. president to visit Myanmar, also known as Burma
- Obama encourages the country to continue a "remarkable journey"
- He also visits Cambodia to meet the prime minister and attend the East Asia Summit

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The first sitting U.S. president to visit Myanmar, Obama urged its leaders, who have embarked on a series of far-reaching political and economic reforms since 2011, not to extinguish the "flickers of progress that we have seen."

Obama said that his visit to the lakeside villa where the pro-democracy icon spent years under house arrest marked a new chapter between the two countries.

"Here, through so many difficult years, is where she has displayed such unbreakable courage and determination," Obama told reporters, standing next to his fellow Nobel peace laureate. "It is here where she showed that human freedom and human dignity cannot be denied."



Myanmar Obama visit

The country, which is also known as Burma, was ruled by military leaders until early 2011 and for decades was politically and economically cut off from the rest of the world.

Suu Kyi acknowledged that Myanmar's opening up would be difficult.

# The New York Times

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The visit was intended to show support for the reforms put in place by Thein Sein's government since the end of military rule in November 2010.

Activists have warned that the visit may be too hasty - political prisoners remain behind bars and ethnic conflicts in border areas are unresolved.



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- 1 Dependency parsing
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Could be a great fit to many other applications!!

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- 1 Structured Prediction and Factor Graphs
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- For each  $x \in \mathcal{X}$ : a **large** set of candidate outputs  $\mathcal{Y}(x)$
- **Decoding problem:**

$$\hat{y} = \arg \max_{y \in \mathcal{Y}(x)} F_w(x, y)$$

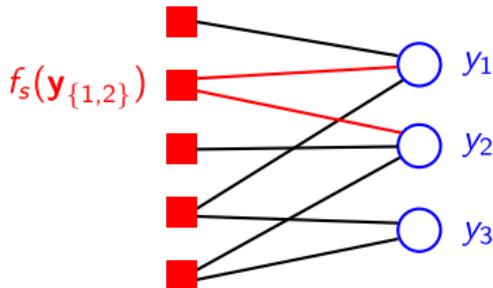
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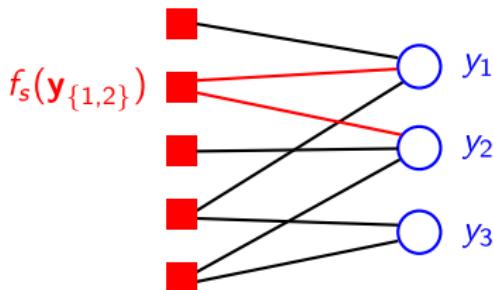
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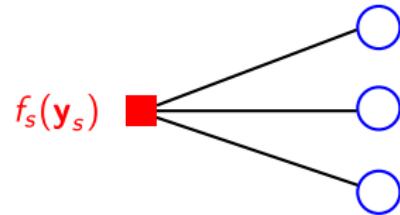
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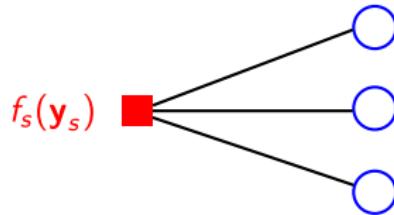


- **Examples:** HMMs, CRFs, PCFGs, general graphical models

# What's in a Factor?



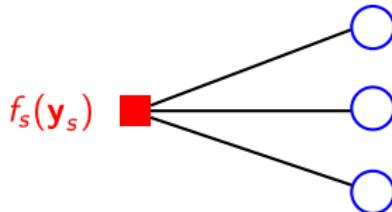
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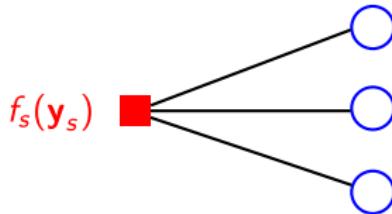


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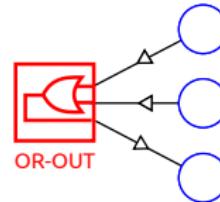
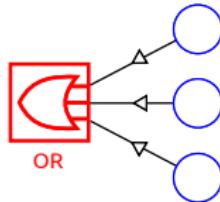
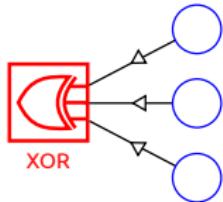
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- 3 Hard constraint factors:**

$$f_s(\mathbf{y}_s) := \begin{cases} 0, & \text{if } \mathbf{y}_s \in \mathcal{Y}_s \\ -\infty, & \text{otherwise.} \end{cases}$$

# Example: Hard Constraint Factors

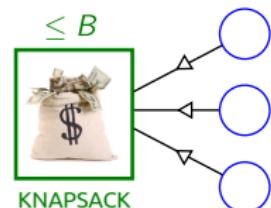


**Logic factors:** can express arbitrary FOL constraints

- Applications: Markov logic networks (Richardson and Domingos, 2006), constrained conditional models (Roth and Yih, 2004)

**Knapsack factor:** can express budget constraints

- Applications: summarization, diversity problems,...



(Martins et al., 2011b, 2012; Almeida and Martins, 2013)

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- combination of dynamic programs (**blow-up the number of states**)
- non-projective parsing with higher-order features (**NP-hard**)
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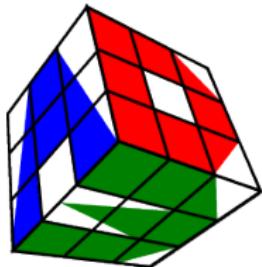
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We'll build (approximate) global decoders given only local decoders.

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# AD<sup>3</sup>: Alternating Directions Dual Decomposition



- A. Martins, M. Figueiredo, P. Aguiar, N. Smith, E. Xing.  
“An Augmented Lagrangian Approach to Constrained MAP Inference.”  
ICML, Bellevue, USA, 2011.

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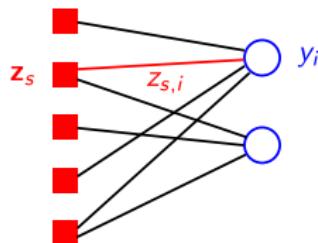
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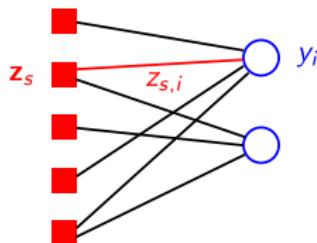


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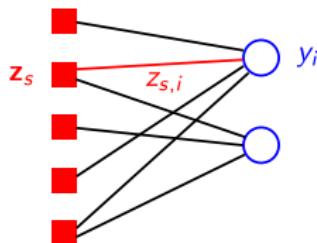
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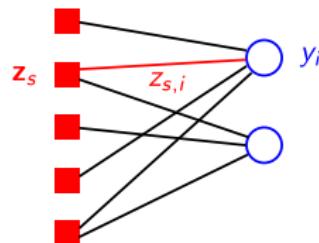
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- 2 Dualize out the equality constraints via **Lagrange multipliers**  $\lambda_{s,i}$

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- **problem:** convergence is slow when there are many factors

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## Alternating Direction Method of Multipliers (ADMM):

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$AD^3 = ADMM$  applied to graphical models (Martins et al., 2010a, 2011a)

# From Subgradient to AD<sup>3</sup> (Martins et al., 2011a)

initialize  $\lambda = \mathbf{0}$  and  $y$  uniformly

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- **better stopping conditions:** keeps track of primal and dual residuals

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initialize  $\lambda = \mathbf{0}$  and  $\mathbf{y}$  uniformly

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for each component  $s = 1, \dots, S$  do

**z-step:**

$$\mathbf{z}_s := \arg \max_{\mathbf{z}'_s \in \mathcal{Z}_s} f_s(\mathbf{z}_s) + \sum_{i \in N(s)} \lambda_{s,i} z_{s,i} - \underbrace{\frac{\eta}{2} \sum_{i \in N(s)} (z_{s,i} - y_i)^2}_{\text{penalty term}}$$

end for

**y-step:**  $y_i := |N(i)|^{-1} \sum_{s \in N(i)} z_{s,i}$

**λ-step:**  $\lambda_{s,i} := \lambda_{s,i} - \eta (z_{s,i} - y_i)$

until certificate found or **primal/dual residuals below threshold**

- **faster consensus:** regularize z-step towards average votes in  $\mathbf{y}$
- **better stopping conditions:** keeps track of primal and dual residuals

# Theoretical Guarantees of AD<sup>3</sup>

**Convergent** in primal and dual (Glowinski and Le Tallec, 1989)

**Iteration bound:**  $O(1/\epsilon)$  (cf.  $O(1/\epsilon^2)$  for projected subgradient)

**Inexact AD<sup>3</sup> subproblems:** still convergent if residuals are summable  
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May embed AD<sup>3</sup> in a branch-and-bound procedure for *exact* decoding:

- D. Das, A. Martins, N. Smith.  
“An Exact DD Algorithm for Shallow Semantic Parsing with Constraints.”  
\*SEM Workshop, 2012.

# AD<sup>3</sup> Subproblems

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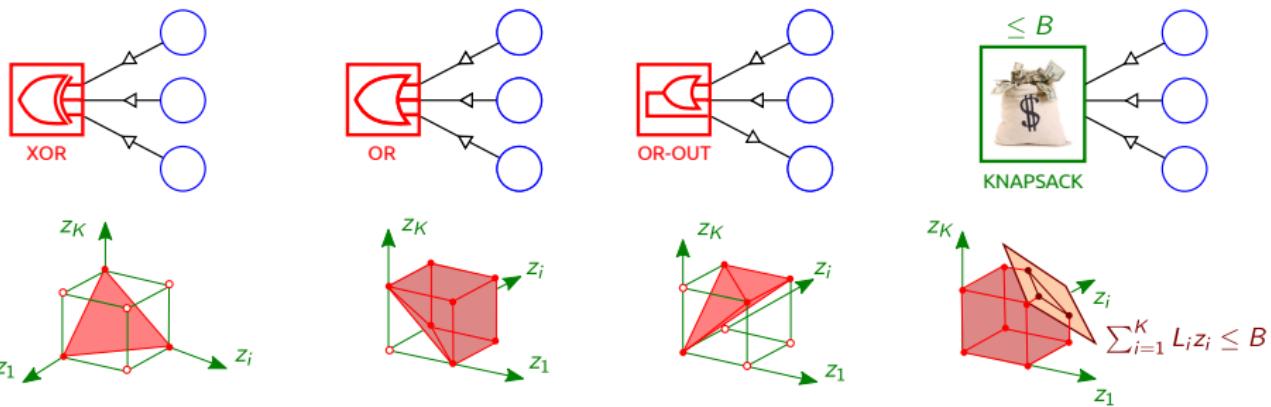
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- More involved than in projected subgradient
- Closed form solution for pairwise binary factors (Ising models)
- Hard constraint factors: projection onto the marginal polytope  $\mathcal{Z}_s$
- Very easy and efficient for logic and knapsack factors!

# Projecting onto Hard Constraint Polytopes



- Martins et al. (2012): logic factors can be solved in  $O(K)$  time
- **Almeida and Martins (2013): same for knapsack factors!**

# Structured Factors

What about structured factors?

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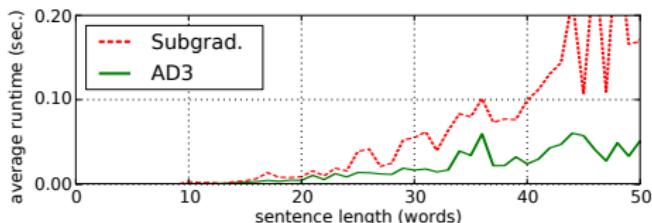
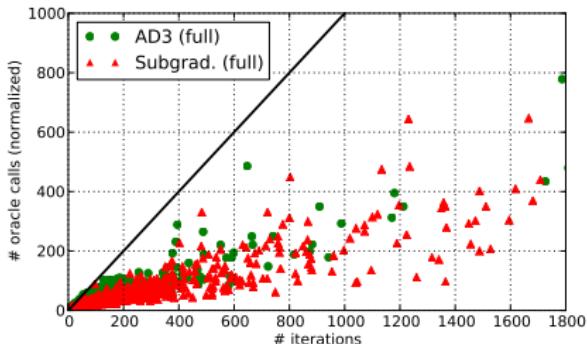
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More info: Martins et al. (2012)

# Runtime of AD<sup>3</sup> vs Subgradient (Parsing)

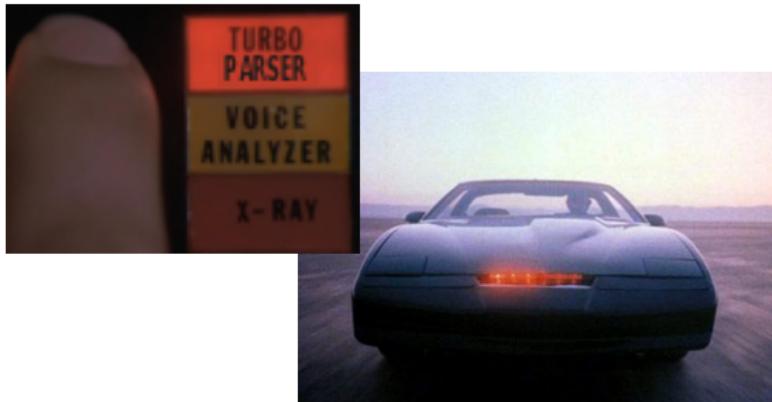


- **Caching** and **warm-starting** the subproblems reduces drastically the number of oracle calls—**huge speed-ups!!**
- **AD<sup>3</sup> faster to achieve consensus** (due to the quadratic penalty)

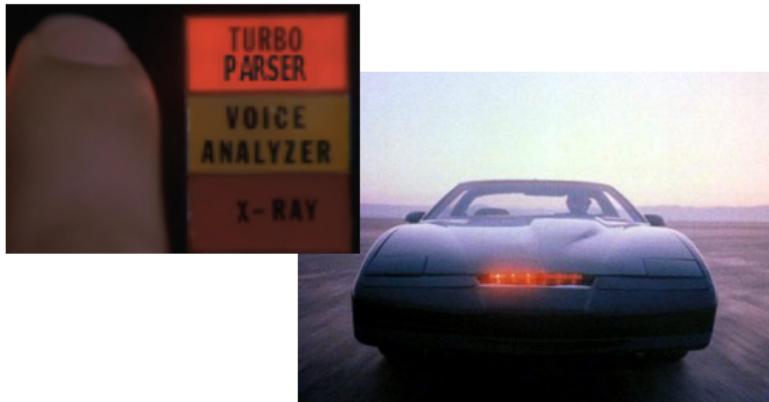
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# What is a Turbo Parser?

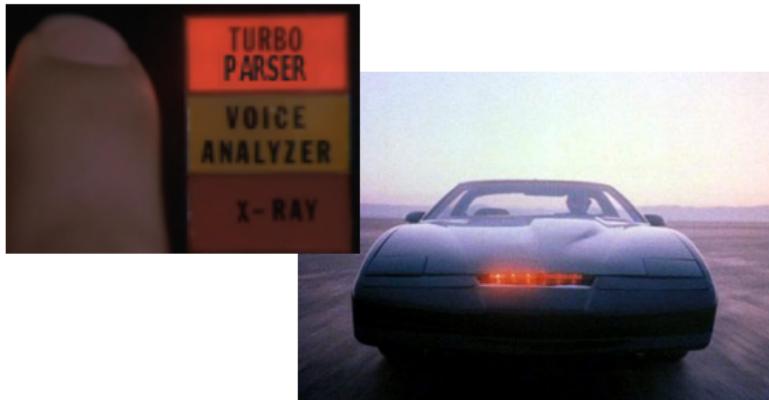


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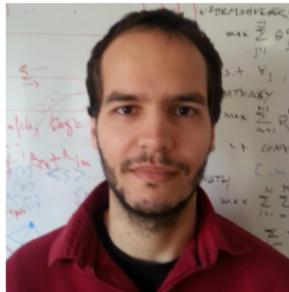
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# What is a Turbo Parser?



- A parser that runs inference in factor graphs, ignoring global effects caused by loops (Martins et al., 2010b)
- name inspired from *turbo* decoders (Berrou et al., 1993)
- **This talk:** we speed up turbo parsers via AD<sup>3</sup> w/ active set

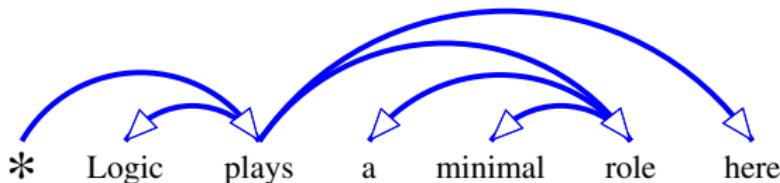
# Forthcoming Paper



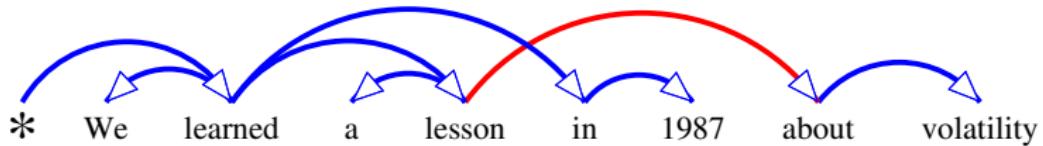
- André F. T. Martins, Miguel B. Almeida, Noah A. Smith.  
“Turning on the Turbo: Fast Third-Order Non-Projective Turbo Parsers.”  
To appear at ACL 2013.

# An Important Distinction

- A projective tree:

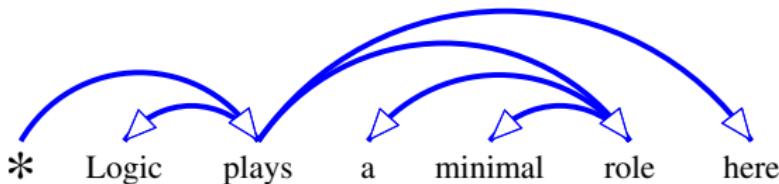


- A non-projective tree:

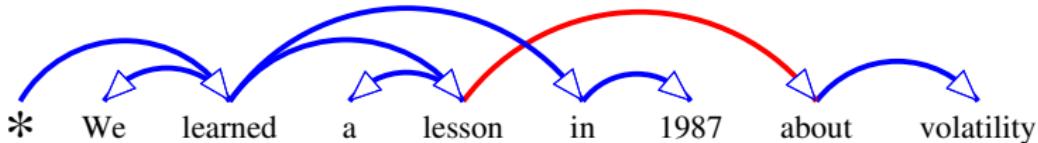


# An Important Distinction

- A projective tree:



- A non-projective tree:



This talk: we allow non-projective trees.

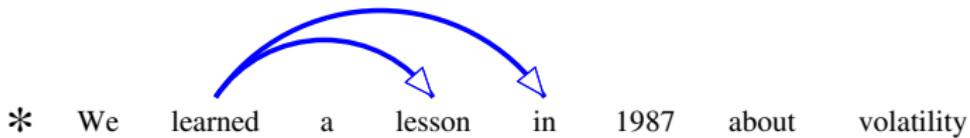
Suitable for languages with flexible word order (Dutch, German, Czech,...)

# First-Order Scores for Arcs

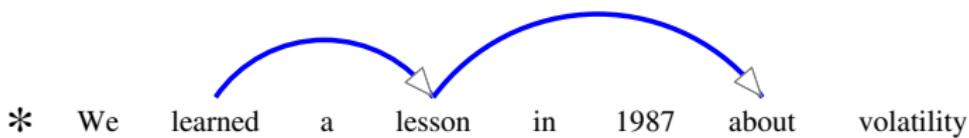
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# Second-Order Scores for Consecutive Siblings

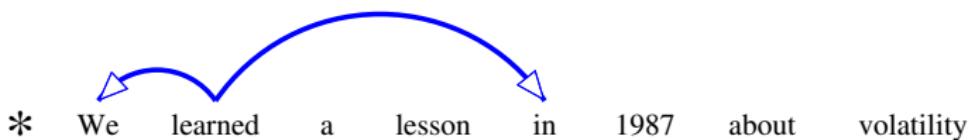


# Second-Order Scores for Grandparents



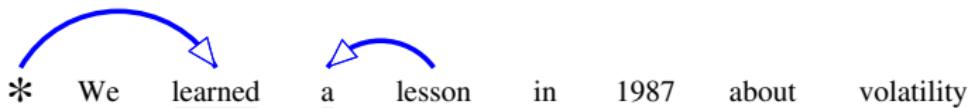
# Scores for Arbitrary Siblings

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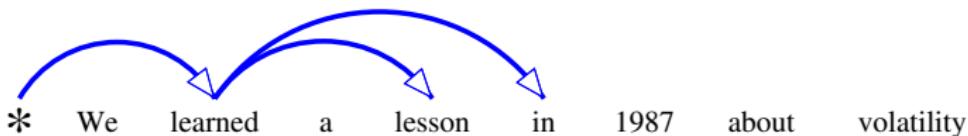


# Scores for Head Bigrams

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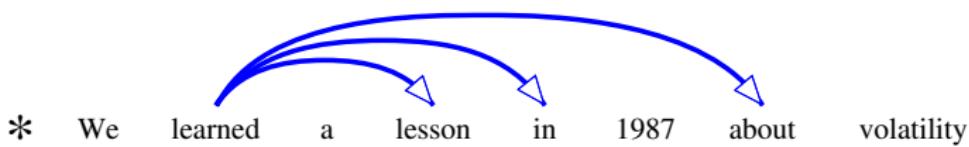


# Third-Order Scores for Grand-siblings



Used by Koo and Collins (2010) for *projective* parsing.

# Third-Order Scores for Tri-siblings



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# Decoding

How to deal with all these parts?

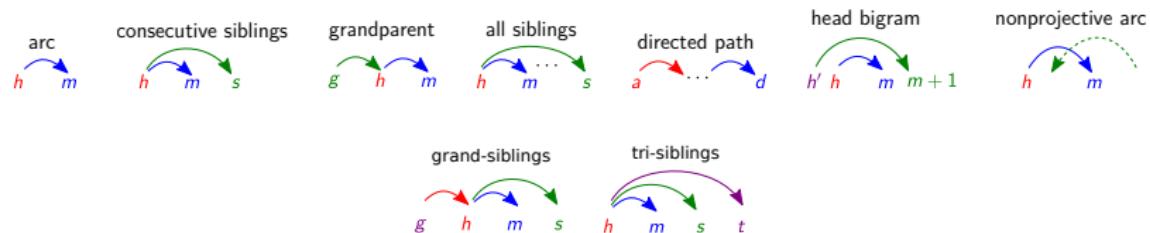
- Dynamic programming only available for the *projective* case...

# Decoding

How to deal with all these parts?

- Dynamic programming only available for the *projective* case...
- Beyond arc-factored models, non-projective parsing is **NP-hard** (McDonald and Satta, 2007)
- **Need to embrace approximations!**

# Approximate Dependency Parsers



	parser	AF	CS	G	AS	DP	HB	NPA	GS	TS
McDonald et al. (2006)	projective + greedy	✓	✓							
Smith et al. (2008)	loopy BP	✓	✓	✓	✓					
Martins et al. (2010)	LP solver	✓		✓	✓			✓		
Koo et al. (2010)	dual decomp.	✓	✓							
Martins et al. (2011)	AD <sup>3</sup>	✓	✓	✓	✓	✓	✓	✓		
This work	AD <sup>3</sup> & active set	✓	✓	✓	✓		✓		✓	✓

# Factor Graph Representation

- Variables nodes for **dependency arcs**, linked to a tree constraint
- Head automata for **consecutive siblings and grandparents** (as in Smith and Eisner (2008); Koo et al. (2010))
- Pairwise factors for **arbitrary siblings** (as Martins et al. (2011b))

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We solve an LP relaxation with AD<sup>3</sup>.

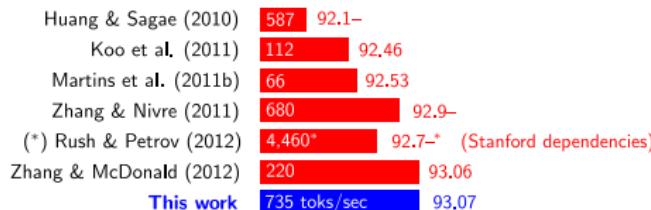
# Parsing Accuracies/Runtimes

## ■ Projective dataset (English PTB):

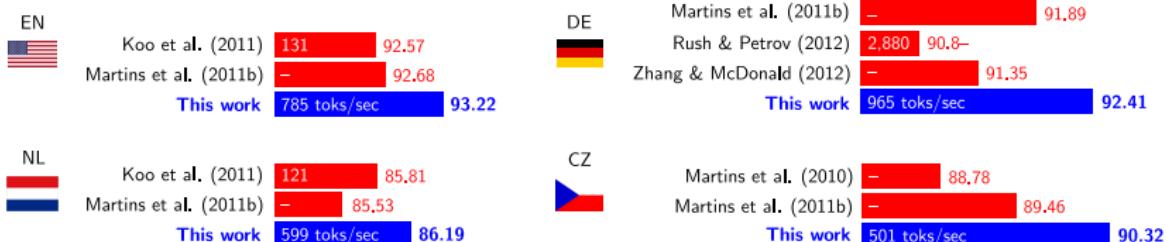


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## ■ Non-projective datasets (CoNLL-2006 and CoNLL-2008):

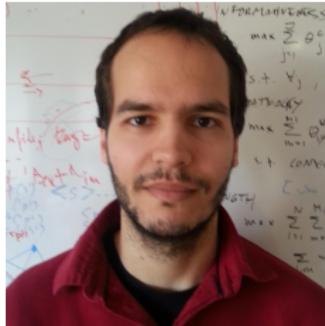


We get SOTA accuracies for the largest non-projective datasets!

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# Forthcoming Paper



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“Fast and Robust Compressive Summarization with Dual Decomposition and Multi-Task Learning.”  
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# Multi-Document Summarization

Map a set of related **documents** to a brief **summary**.



Obama hopes for 'continued progress' in Myanmar

## STORY HIGHLIGHTS

- Obama meets with pro-democracy icon Aung San Suu Kyi and Myanmar's president
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# Compressive Summarization as Global Optimization

- Indicator variables for every word of the  $n$ th sentence,  $\mathbf{z}_n := \langle z_{n,\ell} \rangle_{\ell=1}^{L_n}$
- Summary length must not exceed the **budget** ( $B$  words)
- Quality function rewards *global informativeness* (through  $g(\mathbf{z})$ )...
- ... but also *local grammaticality* (through  $h_n(\mathbf{z}_n)$ ):

$$\begin{aligned} & \text{maximize} \quad g(\mathbf{z}) + \sum_{n=1}^N h_n(\mathbf{z}_n) \\ \text{s.t.} \quad & \sum_{n=1}^N \sum_{\ell=1}^{L_n} z_{n,\ell} \leq B. \end{aligned}$$

# Grammaticality: Sentence Compression Model

Inspired by Knight and Marcu (2000)'s word deletion model

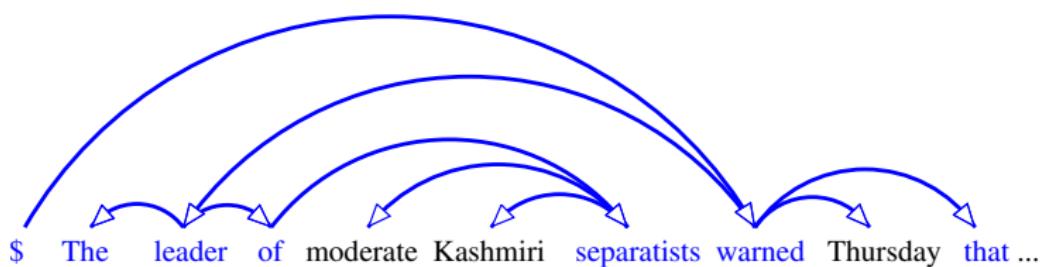
Other relevant work: McDonald (2006); Clarke and Lapata (2008);  
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Our model factors over dependency arcs:

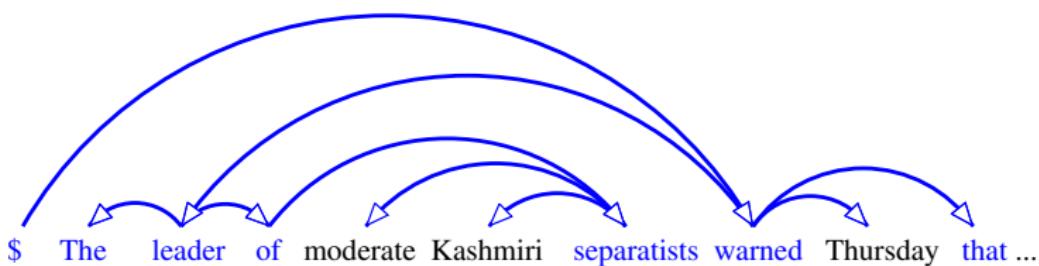


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A structured factor, locally decodable with dynamic programming.

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Inspired by *extractive* max-coverage models (Filatova and Hatzivassiloglou, 2004; Yih et al., 2007; Gillick et al., 2008; Lin and Bilmes, 2010)

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- Define  $g(\mathbf{z})$  as the global concept coverage:

$$g(\mathbf{z}) := \sum_{m=1}^M \sigma_m u_m, \quad \text{where } u_m := \bigvee_{\langle n, \ell_s, \ell_e \rangle \in \mathcal{T}_m} \left( \bigwedge_{\ell=\ell_s}^{\ell_e} z_{n,\ell} \right)$$

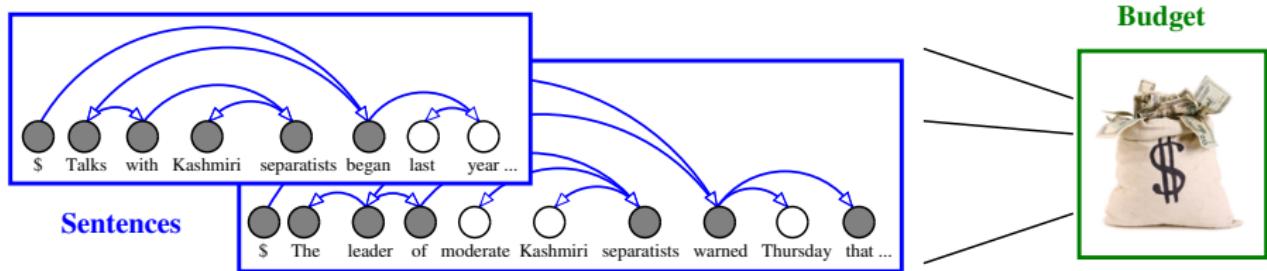
- Intuitively: a **concept type** occurs if some **concept token** occurs.

# Graphical Model for Our Compressive Summarizer

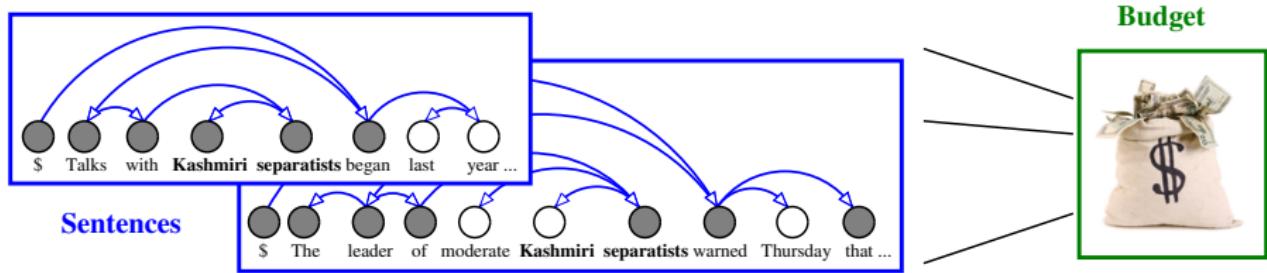
Budget



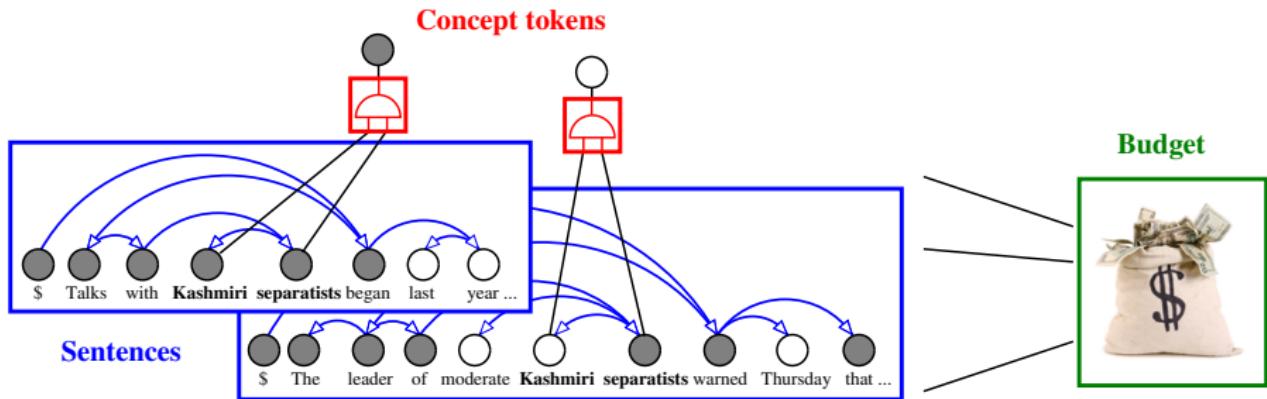
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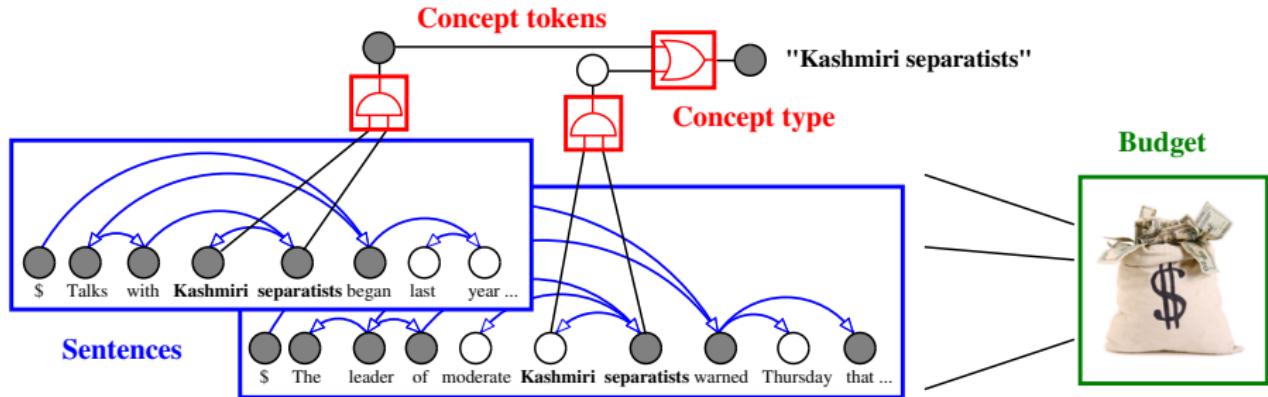
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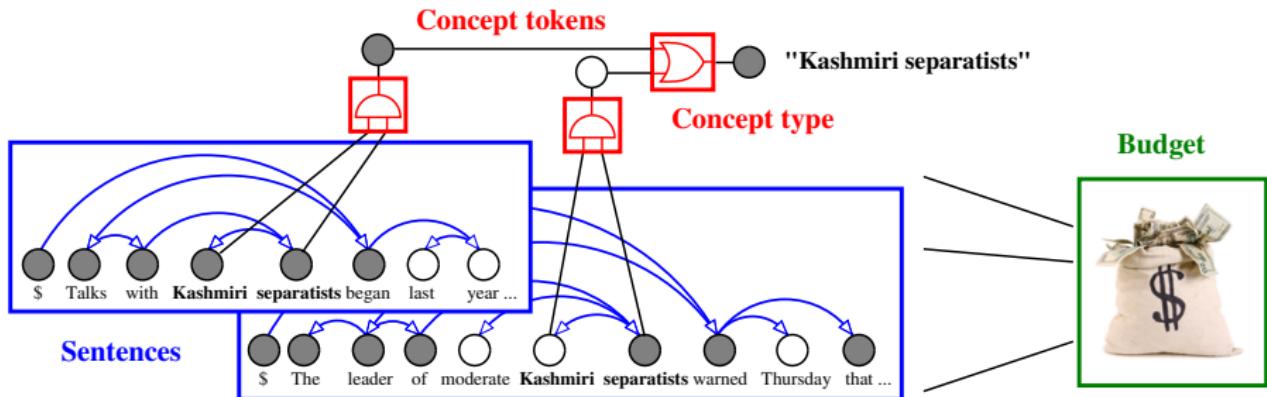
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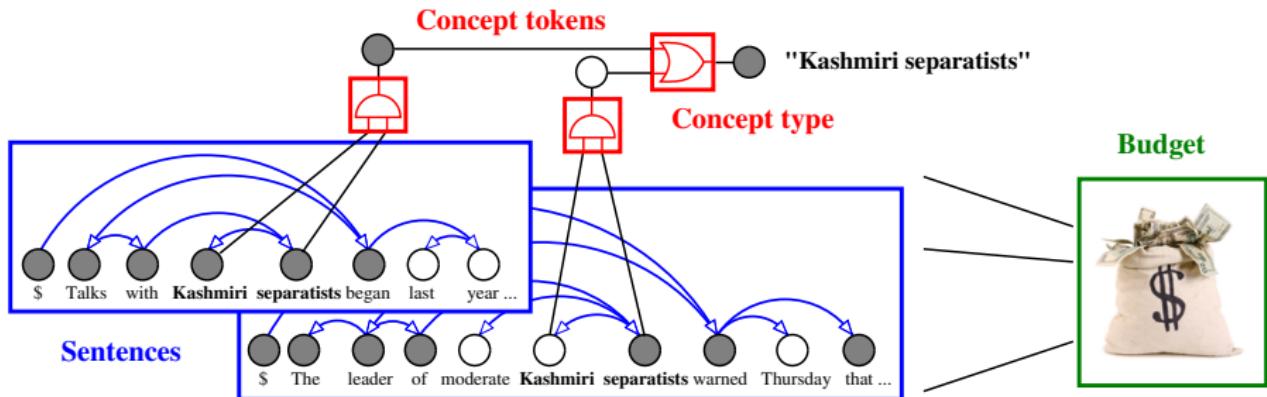


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**Multi-task learning:** user-generated data (Simple English Wikipedia) along with manual abstracts and compressive summaries

# Results on TAC-2008 Dataset

## ■ Quality scores:

	ROUGE-2	Pyramid	LQ (1–5)
ICSI-1 (Gillick et al., 2008)	11.03	–	–
Berg-Kirkpatrick et al. (2011)	11.71	–	–
Woodsend and Lapata (2012)	11.37	–	–
Extractive, ILP	11.16	36.0	<b>4.6</b>
Single-task, AD <sup>3</sup>	11.88	41.0	3.8
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## ■ Averaged runtimes per summarization problem (10 documents):

Solver	Runtime (sec.)	ROUGE-2
ILP Exact, GLPK	10.394	12.40
LP-Relax., GLPK	2.265	12.38
<b>AD<sup>3</sup> (1,000 its.)</b>	<b>0.406</b>	<b>12.30</b>
Extractive (ILP)	0.265	11.16

# Outline

- 1 Structured Prediction and Factor Graphs
- 2 AD<sup>3</sup>: Alternating Directions Dual Decomposition
- 3 Turbo Parsers
- 4 Compressive Summarization
- 5 Conclusions

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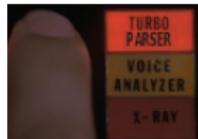
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# Conclusions

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- An **active set method** to tackle structured factors assuming only a local decoder
- Two applications with SOTA results: **turbo parsing** and **compressive summarization**
- **Could be a great fit to many other applications!!**

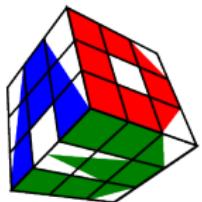
# Thank you!

The parser and AD<sup>3</sup> are freely available at:



*<http://www.ark.cs.cmu.edu/TurboParser>*

*<http://www.ark.cs.cmu.edu/AD3>*



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- Fundação para a Ciência e Tecnologia, grant PTDC/EEI-SII/2312/2012.
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