

The Message Passing Interface (MPI): Parallelism on Distributed CPUs

<http://mpi-forum.org>
<https://www.open-mpi.org/>



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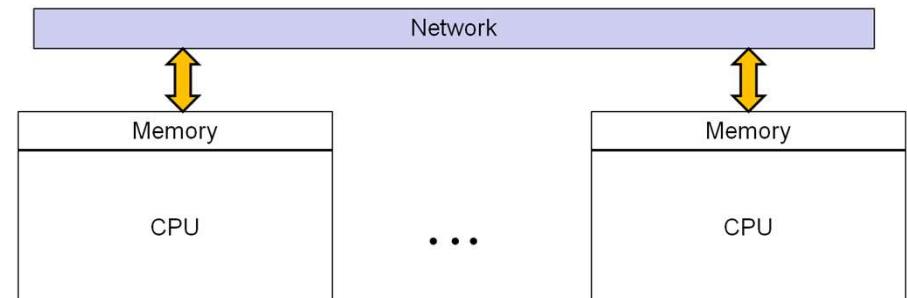
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Oregon State
University
 Computer Graphics



mpi.pptx

mjb – June 2, 2021

Why Two URLs?



<http://mpi-forum.org>

This is the definitive reference for the MPI standard. Go here if you want to read the official specification, which, BTW, continues to evolve.

<https://www.open-mpi.org/>

This consortium formed later. This is the open source version of MPI. If you want to start using MPI, I recommend you look here. This is the MPI that the COE systems use

<https://www.open-mpi.org/doc/v4.0/>

This URL is also really good – it is a link to all of the MPI man pages



The Open MPI Consortium

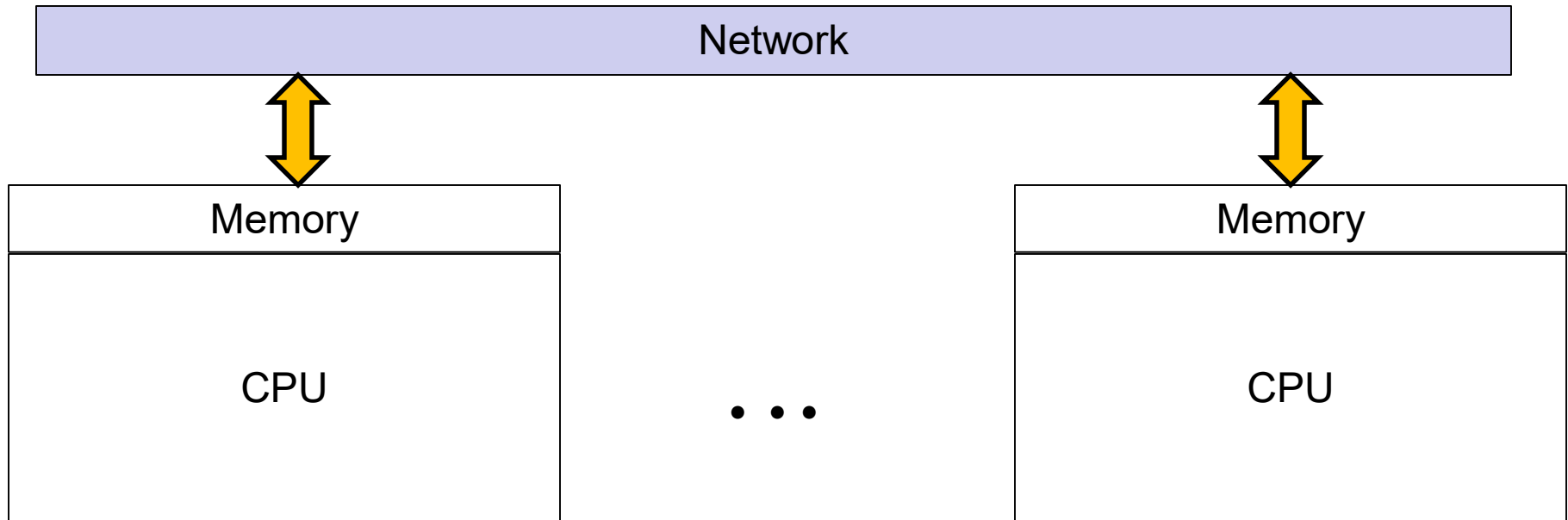


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MPI: The Basic Idea

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Programs on different CPUs coordinate computations by passing messages between each other

Note: Each CPU in the MPI “cluster” must be prepared ahead of time by having the MPI server code installed on it. Each MPI CPU must also have an integer ID assigned to it (called its *rank*).

This paradigm is how modern supercomputers work!

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How to SSH to the COE MPI Cluster

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ssh over to an MPI submission machine --
submit-a and **submit-b** will also work

flip3 151% ssh **submit-c.hpc.engr.oregonstate.edu**

submit-c 142% module load slurm
submit-c 143% module load openmpi/3.1

Type these two lines right away
to set your paths correctly

BTW, you can find out more about the COE cluster here:

<https://it.engineering.oregonstate.edu/hpc>

“The College of Engineering HPC cluster is a heterogeneous mix of 202 servers providing over 3600 CPU cores, over 130 GPUs, and over 31 TB total RAM. The systems are connected via gigabit ethernet, and most of the latest servers also utilize a Mellanox EDR InfiniBand network connection. The cluster also has access to 100TB global scratch from the College of Engineering's Dell/EMC Isilon enterprise storage.”

Compiling and Running from the Command Line

```
% mpicc -o program program.c . . .
```

← C

or

```
% mpic++ -o program program.cpp . . .
```

← C++

```
% mpiexec -mca btl self,tcp -np 4 program
```

All distributed processors execute the *same* program at the same time

of processors to use

Warning – use *mpic++* and *mpiexec* !

Don't use *g++* and don't run by just typing the name of the executable!

Running with a *bash* Batch Script

submit.bash:

```
#!/bin/bash
#SBATCH -J Heat
#SBATCH -A cs475-575
#SBATCH -p class
#SBATCH -N 8    # number of nodes
#SBATCH -n 8    # number of tasks
#SBATCH -o heat.out
#SBATCH -e heat.err
#SBATCH --mail-type=END,FAIL
#SBATCH --mail-user=joeparallel@cs.oregonstate.edu
module load openmpi/3.1
mpic++ heat.cpp -o heat -lm
mpiexec -mca btl self,tcp -np 4 heat
```

```
submit-c 143% sbatch submit.bash
Submitted batch job 258759
```



#SBATCH --mail-user=joeparallel@oregonstate.edu

You don't have to ask for email notification, but if you do, *please, please, please be sure you get your email address right!*

The IT people are getting *real* tired of fielding the bounced emails when people spell their own email address wrong.

Use slurm's *scancel* if your Job Needs to Be Killed

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submit-c 143% sbatch submit.bash
Submitted batch job 258759

submit-c 144% scancel 258759

Setting Up and Finishing

```
#include <mpi.h>

int
main( int argc, char *argv[ ] )
{
    . . .

        MPI_Init( &argc, &argv );

    . . .

        MPI_Finalize( );
    return 0;
}
```

You don't need to process command line arguments if you don't need to.
You can also call it as:

```
MPI_Init( NULL, NULL );
```



MPI Follows a Single-Program-Multiple-Data (SPMD) Model

A **communicator** is a collection of CPUs that are capable of sending messages to each other

Oh, look, a
communicator
of deer!



Oh, look, a
communicator
of turkeys!



This requires MPI server code getting installed on all those CPUs. Only an administrator can do this.

Getting information about our place in the **communicator**:

```
int numCPUs;    // total # of cpus involved
int me;         // which one I am

MPI_Comm_size( MPI_COMM_WORLD, &numCPUs );
MPI_Comm_rank( MPI_COMM_WORLD, &me );
```

Size, i.e., how many altogether?

Rank, i.e., which one am I?

It is then each CPU's job to figure out what piece of the overall problem it is responsible for and then go do it.

A First Test of MPI

```
#include <stdio.h>
#include <math.h>
#include <mpi.h>

#define BOSS 0

int
main( int argc, char *argv[ ] )
{
    MPI_Init( &argc, &argv );

    int numCPUs;      // total # of cpus involved
    int me;           // which one I am

    MPI_Comm_size( MPI_COMM_WORLD, &numCPUs );
    MPI_Comm_rank( MPI_COMM_WORLD, &me );

    if( me == BOSS )
        fprintf( stderr, "Rank %d says that we have a Communicator of size %d\n", BOSS, numCPUs );
    else
        fprintf( stderr, "Welcome from Rank %d\n", me );

    MPI_Finalize( );
    return 0;
}
```


submit-c 165% mpiexec -np 16 ./first

Welcome from Rank 13
 Welcome from Rank 15
 Welcome from Rank 3
 Welcome from Rank 7
 Welcome from Rank 5
 Welcome from Rank 8
 Welcome from Rank 9
 Welcome from Rank 11
 Rank 0 says that we have a Communicator of size 16
 Welcome from Rank 1
 Welcome from Rank 12
 Welcome from Rank 14
 Welcome from Rank 6
 Welcome from Rank 2
 Welcome from Rank 10
 Welcome from Rank 4

submit-c 166% mpiexec -np 16 ./first

Welcome from Rank 1
 Welcome from Rank 5
 Welcome from Rank 7
 Welcome from Rank 9
 Welcome from Rank 11
 Welcome from Rank 13
 Welcome from Rank 15
 Rank 0 says that we have a Communicator of size 16
 Welcome from Rank 2
 Welcome from Rank 3
 Welcome from Rank 4
 Welcome from Rank 6
 Welcome from Rank 8
 Welcome from Rank 12
 Welcome from Rank 14
 Welcome from Rank 10

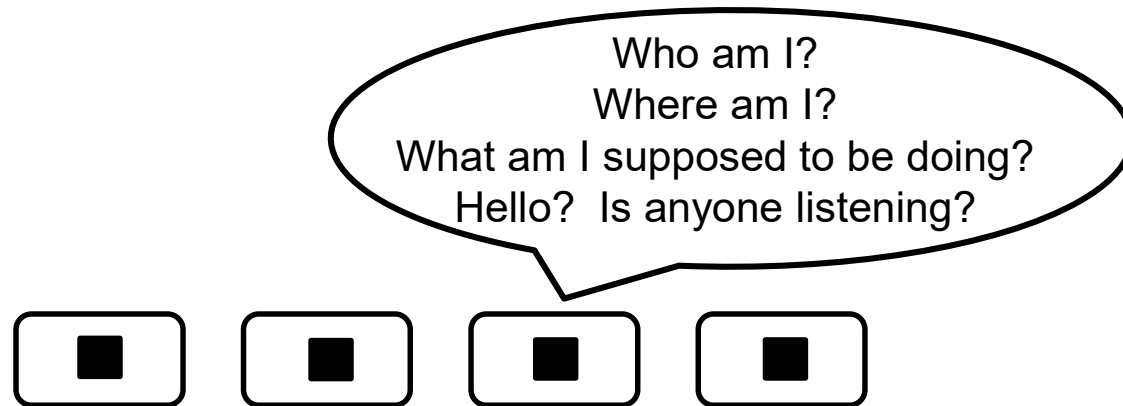
submit-c 167% mpiexec -np 16 ./first

Welcome from Rank 9
 Welcome from Rank 11
 Welcome from Rank 13
 Welcome from Rank 7
 Welcome from Rank 1
 Welcome from Rank 3
 Welcome from Rank 10
 Welcome from Rank 15
 Welcome from Rank 4
 Welcome from Rank 5
 Rank 0 says that we have a Communicator of size 16
 Welcome from Rank 2
 Welcome from Rank 6
 Welcome from Rank 8
 Welcome from Rank 14
 Welcome from Rank 12

submit-c 168% mpiexec -np 16 ./first

Welcome from Rank 13
 Welcome from Rank 15
 Welcome from Rank 7
 Welcome from Rank 3
 Welcome from Rank 5
 Welcome from Rank 9
 Welcome from Rank 11
 Welcome from Rank 1
 Welcome from Rank 12
 Welcome from Rank 14
 Welcome from Rank 4
 Welcome from Rank 2
 Rank 0 says that we have a Communicator of size 16
 Welcome from Rank 8
 Welcome from Rank 10
 Welcome from Rank 6

So, we have a group (a “communicator”) of distributed processors.
How do they communicate about what work they are supposed to do?



Example: You could coordinate the units of our DGX system using MPI



A Good Place to Start: MPI Broadcasting

```
MPI_Bcast( array, count, type, src, MPI_COMM_WORLD );
```

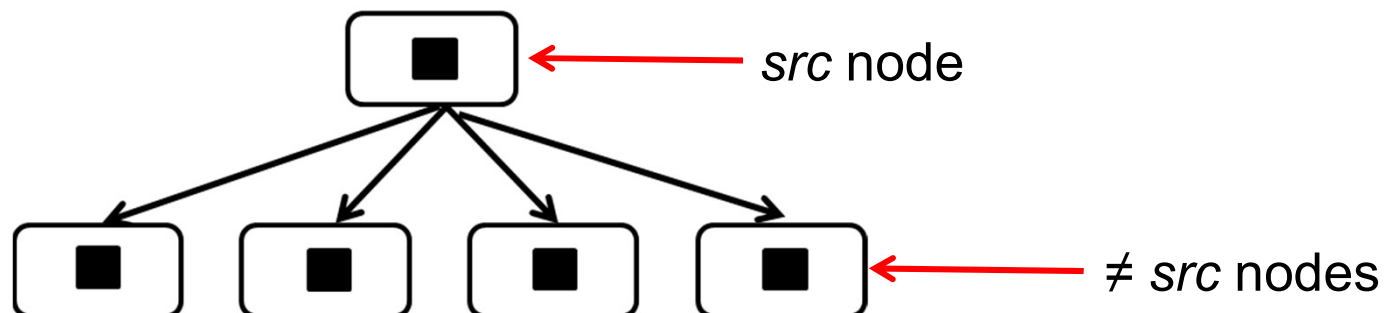
Address of data to
send from if you
are the *src* node;
Address of the
data to receive
into if you are not

elements

MPI_CHAR
MPI_INT
MPI_LONG
MPI_FLOAT
MPI_DOUBLE
...

rank of the CPU
doing the sending

Broadcast



Both the sender and receivers need to execute **MPI_Bcast** –
there is no separate receive function

MPI Broadcast Example

This is our heat transfer equation from before. Clearly, every CPU will need to know this value.

$$\Delta T_i = \left(\frac{k}{\rho C} \right) \left(\frac{T_{i-1} - 2T_i + T_{i+1}}{(\Delta x)^2} \right) \Delta t$$

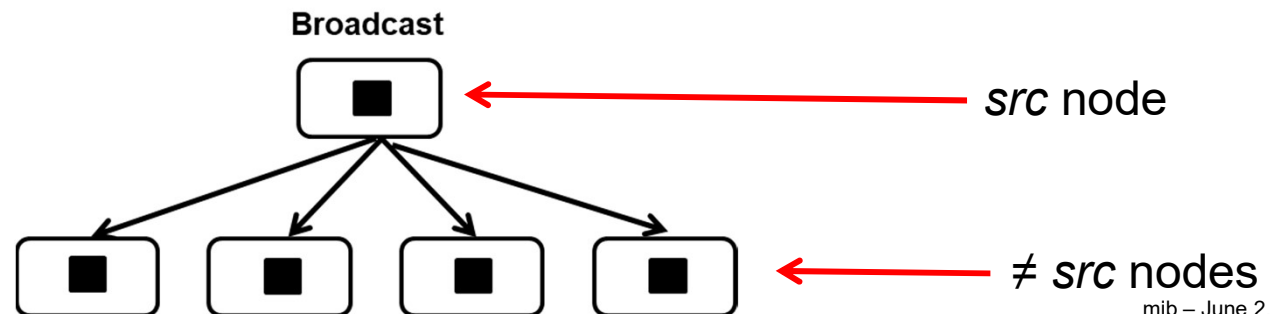
```
int  numCPUs;
int  me;
float k_over_rho_c;           // the BOSS node will know this value, the others won't (yet)

#define BOSS 0

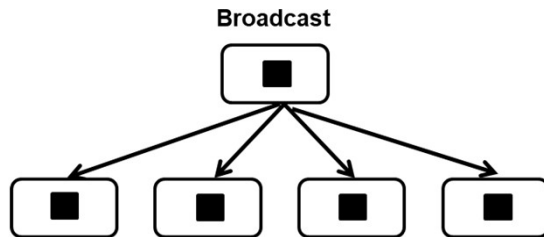
MPI_Comm_size( MPI_COMM_WORLD, &numCPUs );
MPI_Comm_rank( MPI_COMM_WORLD, &me );
...
if( me == BOSS )
{
    << read k_over_rho_c from the data file >>
}

MPI_Bcast( &k_over_rho_c, 1, MPI_FLOAT, BOSS, MPI_COMM_WORLD ); // send if BOSS, and receive if not
```

I am the BOSS: this identifies this call as a send



Confused? Look at this Diagram



Both the sender and receivers need to execute **MPI_Bcast** – there is no separate receive function

Executable code	k_over_rho_c (set)	
-----------------	--------------------	--

Node #BOSS:

```
MPI_Bcast(&k_over_rho_c, 1, MPI_FLOAT, BOSS, MPI_COMM_WORLD); // send if BOSS, and receive if not
```

All Nodes that are *not* #BOSS:

Executable code	k_over_rho_c (being set)	
Executable code	k_over_rho_c (being set)	
Executable code	k_over_rho_c (being set)	
Executable code	k_over_rho_c (being set)	



How Does this Work? Think Star Trek Wormholes!



Sending Data from One Source CPU to One Destination CPU

```
MPI_Send( array, numToSend, type, dst, tag, MPI_COMM_WORLD );
```

address of data to send from

elements

(note: this is the number of *elements*, not the number of *bytes*!)

MPI_CHAR
MPI_INT
MPI_LONG
MPI_FLOAT
MPI_DOUBLE
...

rank of the CPU
to send to

An integer to differentiate
this transmission from any
other transmission (be sure
this is unique!)

Rules:

- One message from a specific *src* to a specific *dst* cannot overtake a previous message from the same *src* to the same *dst*.
- MPI_Send() blocks until the transfer is far enough along that *array* can be destroyed or re-used.
- There are no guarantees on order from different *src*'s .



Receiving Data in a Destination CPU from a Source CPU

```
MPI_Recv( array, maxCanReceive, type, src, tag, MPI_COMM_WORLD, &status );
```

address of data to receive into

elements we can receive, at most

MPI_CHAR
MPI_INT
MPI_LONG
MPI_FLOAT
MPI_DOUBLE
...

Rank of the CPU we are expecting to get a transmission from

An integer to differentiate what transmission we are looking for with this call (be sure this matches what the sender is sending!). I like to use chars.

Type = MPI_Status

Rules:

- The receiver blocks waiting for data that matches what it declares to be looking for
- One message from a specific *src* to a specific *dst* cannot overtake a previous message from the same *src* to the same *dst*
- There are no guarantees on the order from different *src*'s
- The order from different *src*'s could be implied in the *tag*
- **status** is type MPI_Status – the “&status” can be replaced with MPI_STATUS_IGNORE



src node



dst node

Example

Remember, this *identical* code runs on all CPUs:

```
int numCPUs;
int me;
#define MYDATA_SIZE 128
char mydata[ MYDATA_SIZE ];
#define BOSS 0

MPI_Comm_size( MPI_COMM_WORLD, &numCPUs );
MPI_Comm_rank( MPI_COMM_WORLD, &me );

if( me == BOSS )      // the primary
{
    for( int dst = 0; dst < numCPUs; dst++ )
    {
        if( dst != BOSS )
        {
            char *InputData = "Hello, Beavers!";
            MPI_Send( InputData, strlen(InputData)+1, MPI_CHAR, dst, 'B', MPI_COMM_WORLD );
        }
    }
}
else                  // a secondary
{
    MPI_Recv( myData, MYDATA_SIZE, MPI_CHAR, BOSS, 'B', MPI_COMM_WORLD, MPI_STATUS_IGNORE );
    printf( " '%s' from rank # %d\n", in, me );
}
```




Be sure the receiving tag matches the sending tag

The tag to send

The tag to expect

Or
Com You are highly discouraged from sending to yourself. Because both the send and receive are capable of blocking, the result could be deadlock.

Look at this Diagram

src node    dst node

Executable code	Input Data	
-----------------	------------	--

```

if( dst != BOSS )
{
    char *InputData = "Hello, Beavers!";
    MPI_Send( InputData, strlen(InputData)+1, MPI_CHAR, dst, 0, MPI_COMM_WORLD );
}

```

Destinations

Source

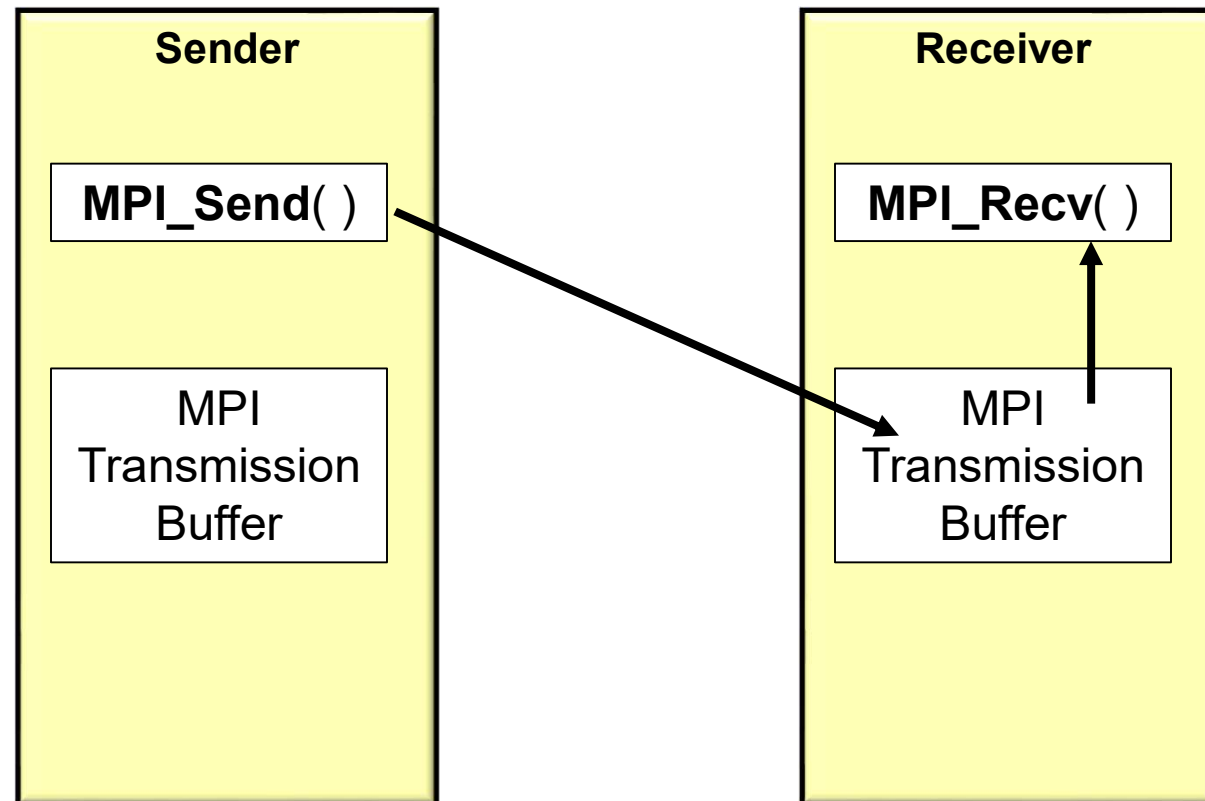
```

else // a secondary
{
    MPI_Recv( myData, MYDATA_SIZE, MPI_CHAR, BOSS, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE );
    printf( " '%s' from rank %d\n", in, me );
}

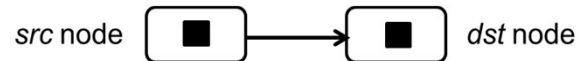
```

Executable code		MyData
Executable code		MyData
Executable code		MyData
Executable code		MyData

How does MPI let the Sender perform an `MPI_Send()` even if the Receivers are not ready to `MPI_Recv()`?



`MPI_Send()` blocks until the transfer is far enough along that the *array* can be destroyed or re-used.



Another Example


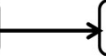

You typically don't send the entire workload to each dst – you just send part of it, like this:

```
#define NUMELEMENTS  ?????
int  numCPUs;
int  me;
#define BOSS      0

MPI_Comm_size( MPI_COMM_WORLD, &numCPUs );
MPI_Comm_rank( MPI_COMM_WORLD, &me );

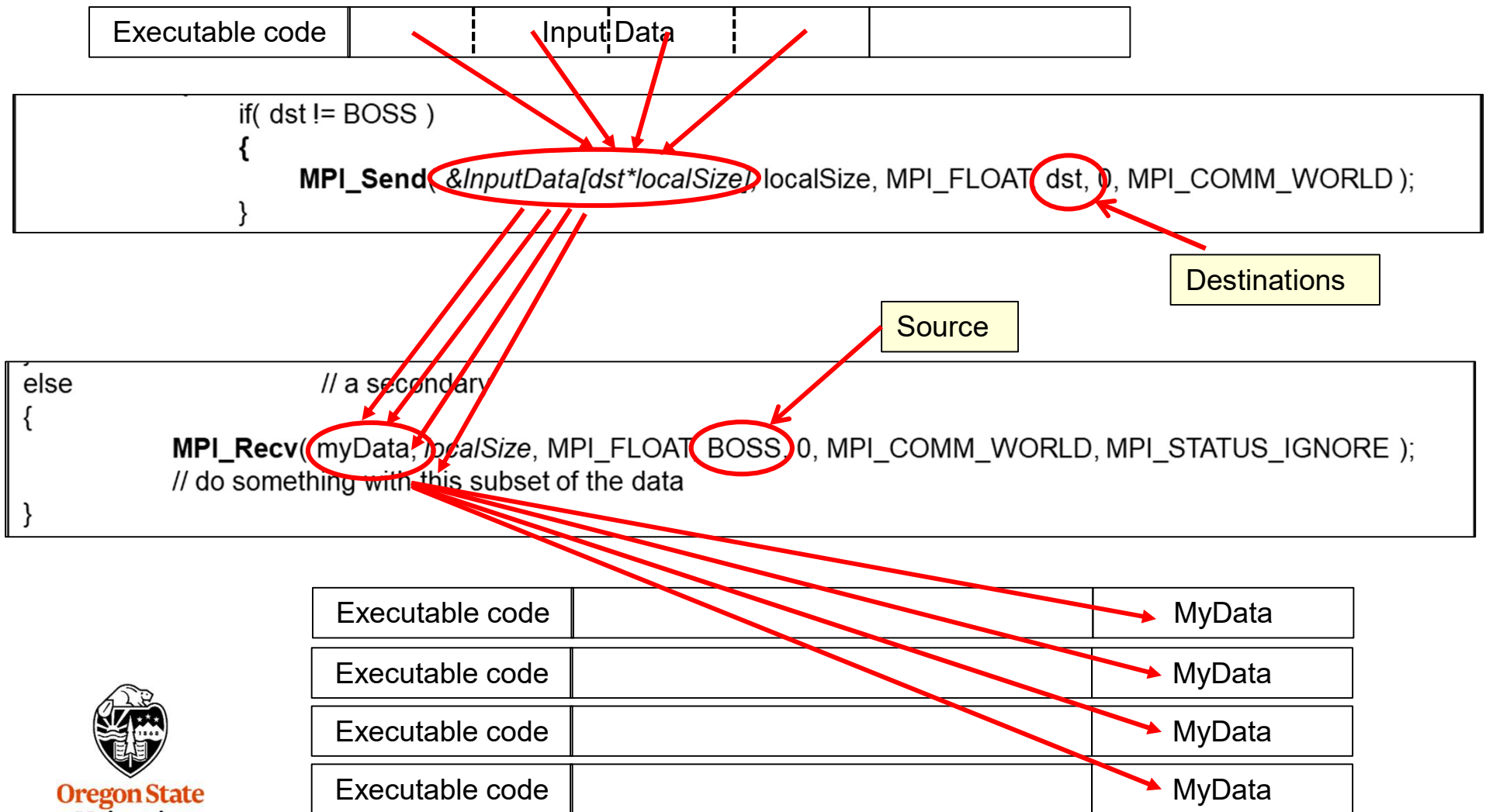
int localSize = NUMELEMENTS / numCPUs;      // assuming it comes out evenly
float *myData = new float [ localSize ];

if( me == BOSS )      // the sender
{
    float *InputData = new float [ NUMELEMENTS ];
    << read the full input data into InputData from disk >>
    for( int dst = 0; dst < numCPUs; dst++ )
    {
        if( dst != BOSS )
        {
            MPI_Send( &InputData[dst*localSize], localSize, MPI_FLOAT, dst, 0, MPI_COMM_WORLD );
        }
    }
}
else      // a receiver
{
    MPI_Recv( myData, localSize, MPI_FLOAT, BOSS, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE );
    // do something with this subset of the data
}
```

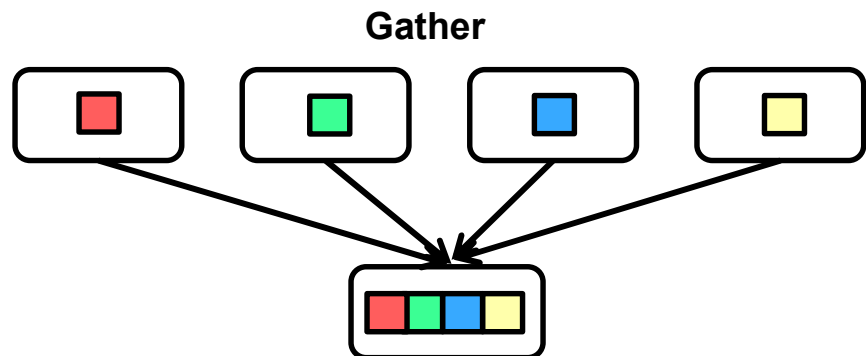
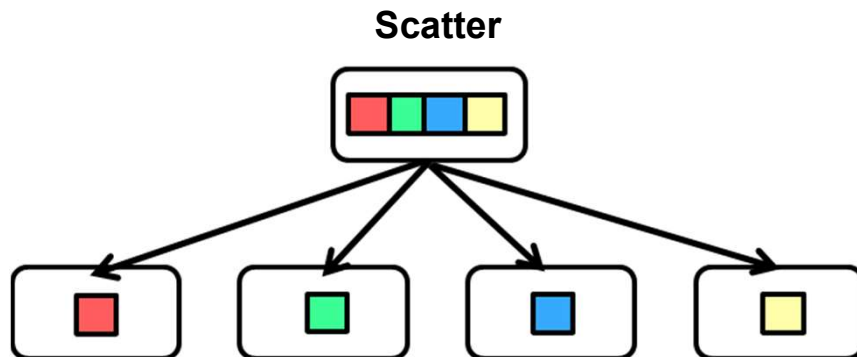
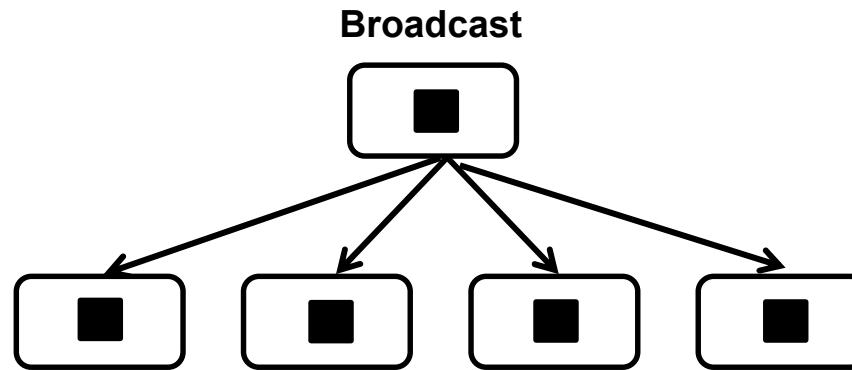
src node    dst node

Another Example

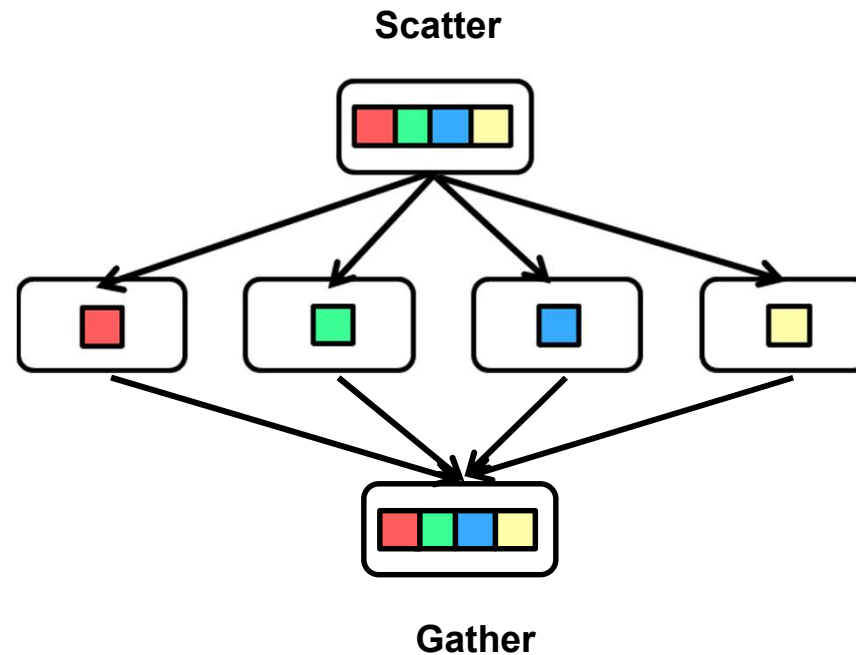
You typically don't send the entire workload to each dst – you just send part of it, like this:



In Distributed Computing, You Often Hear About These Design Patterns²⁷



Scatter and Gather Usually Go Together



Note surprisingly, this is referred to as *Scatter/Gather*

MPI Scatter

Take a data array, break it into ~equal portions, and send it to each CPU

```
MPI_Scatter( snd_array, snd_count, snd_type, rcv_array, rcv_count, rcv_type, src, MPI_COMM_WORLD );
```

The total large array
to split up

elements to send
per-processor

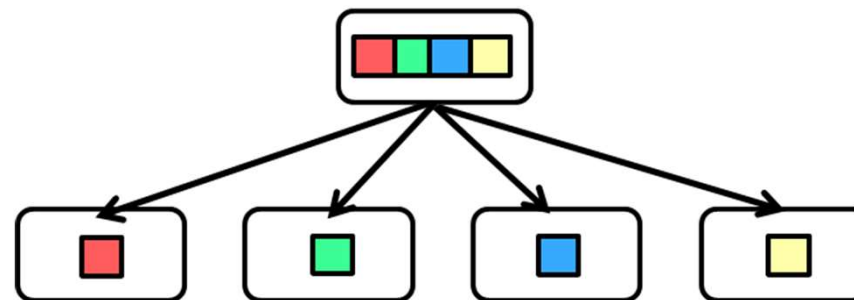
MPI_CHAR
MPI_INT
MPI_LONG
MPI_FLOAT
MPI_DOUBLE
...

Local array to store
this processor's
piece in

elements to receive
per-processor

MPI_CHAR
MPI_INT
MPI_LONG
MPI_FLOAT
MPI_DOUBLE
...

This is who is doing
the sending –
everyone *else* is
receiving

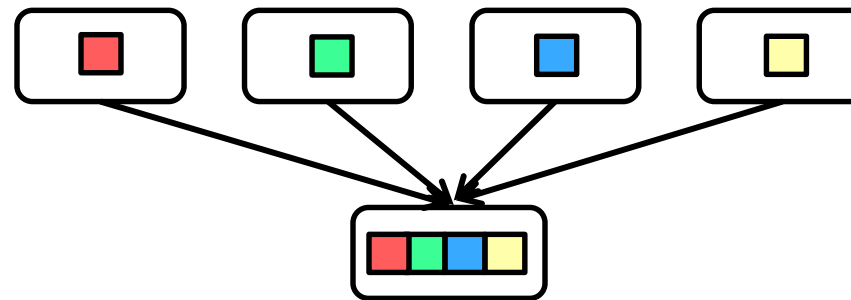
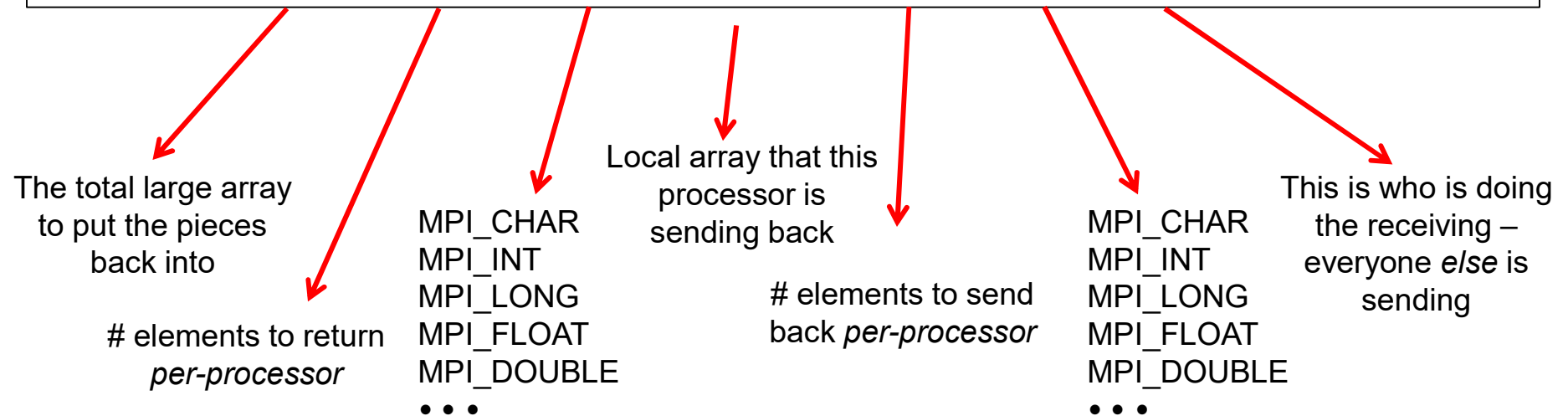


Scatter

Both the sender and receivers need to execute **MPI_Scatter**.
There is no separate receive function

MPI Gather

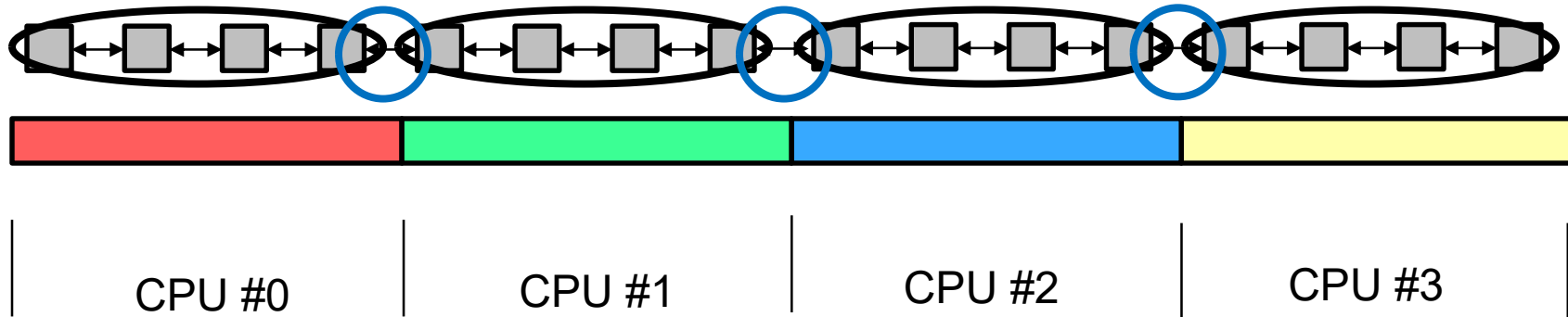
```
MPI_Gather( snd_array, snd_count, snd_type, rcv_array, rcv_count, rcv_type, dst, MPI_COMM_WORLD );
```



Gather

Both the sender and receivers need to execute **MPI_Gather**.
 There is no separate receive function

Remember This? It's Baaaaaack as a complete Scatter/Gather Example



The **Compute : Communicate Ratio** still applies, except that it is even more important now because there is much more overhead in the Communicate portion.

This pattern of breaking a big problem up into pieces, sending them to different CPUs, computing on the pieces, and getting the results back is *very* common. That's why MPI has its own scatter and gather functions.



```
#include <stdio.h>
#include <math.h>
#include <mpi.h>

const float RHO = 8050.;
const float C   = 0.466;
const float K   = 20.;
float k_over_rho_c = K / (RHO*C); // units of m^2/sec  NOTE: this cannot be a const!
// K / (RHO*C) = 5.33x10^-6 m^2/sec

const float DX   = 1.0;
const float DT   = 1.0;

#define BOSS 0

#define NUMELEMENTS      (8*1024*1024)
#define NUM_TIME_STEPS  4
#define DEBUG             false

float *    NextTemps;           // per-processor array to hold computer next-values
int        NumCpus;             // total # of cpus involved
int        PPSize;              // per-processor local array size
float *    PPTemps;             // per-processor local array temperature data
float *    TempData;            // the overall NUMELEMENTS-big temperature data

void        DoOneTimeStep( int );
```

```
int
main( int argc, char *argv[ ] )
{
    MPI_Init( &argc, &argv );

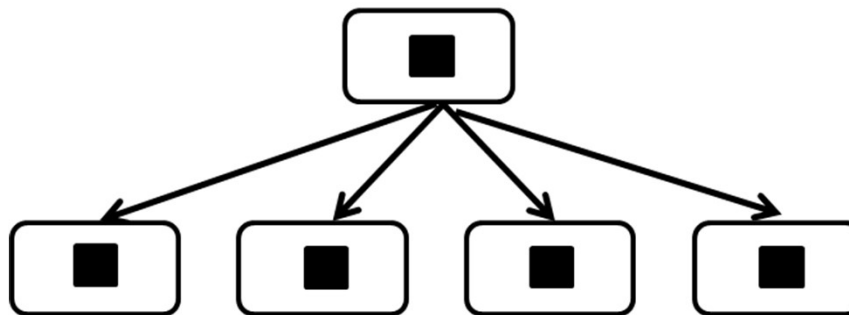
    int me;                // which one I am

    MPI_Comm_size( MPI_COMM_WORLD, &NumCpus );
    MPI_Comm_rank( MPI_COMM_WORLD, &me );

    // decide how much data to send to each processor:
    PPSize = NUMELEMENTS / NumCpus;                // assuming it comes out evenly
    PPTemps = new float [PPSize]; // all processors now have this uninitialized Local array
    NextTemps = new float [PPSize]; // all processors now have this uninitialized local array too

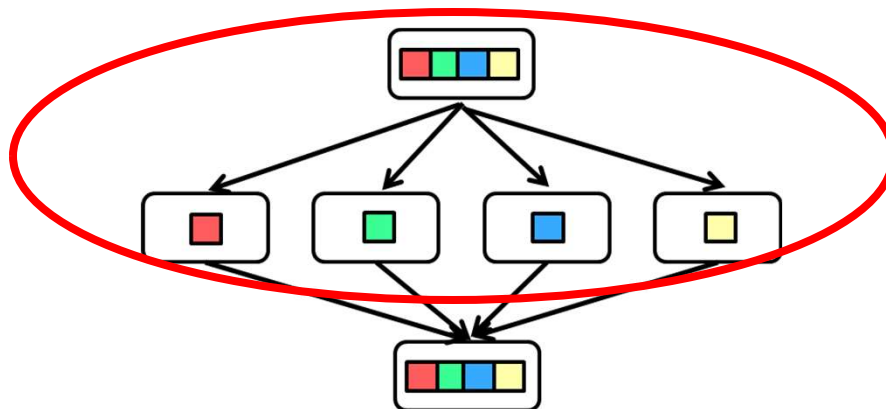
    // broadcast the constant:
    MPI_Bcast( (void *)&k_over_rho_c, 1, MPI_FLOAT, BOSS, MPI_COMM_WORLD );
}
```

Broadcast



```
if( me == BOSS )    // this is the data-creator
{
    TempData = new float [NUMELEMENTS];
    for( int i = 0; i < NUMELEMENTS; i++ )
        TempData[ i ] = 0.;
    TempData[NUMELEMENTS/2] = 100.;
}

MPI_Scatter( TempData, PPSize, MPI_FLOAT, PPTemps, PPSize, MPI_FLOAT,
            BOSS, MPI_COMM_WORLD );
```



```

// all the PPTemps arrays have now been filled
// do the time steps:

double time0 = MPI_Wtime( );

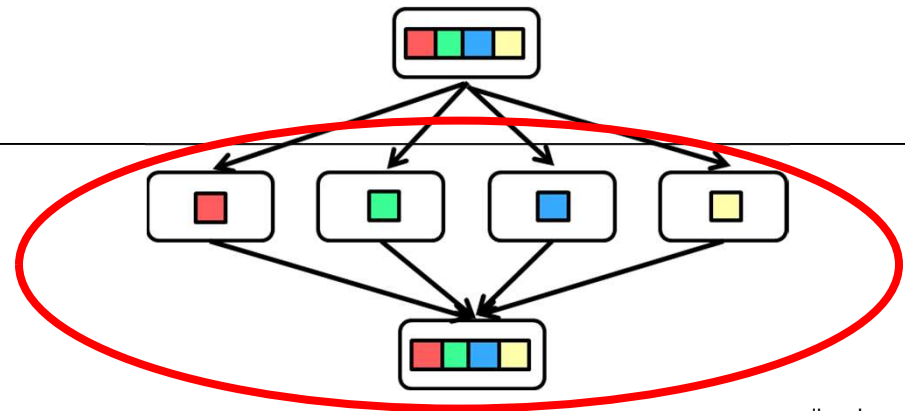
for( int steps = 0; steps < NUM_TIME_STEPS; steps++ )
{
    // do the computation for one time step:
    DoOneTimeStep( me );

    // ask for all the data:
#ifdef WANT_EACH_TIME_STEPS_DATA
        MPI_Gather( PPTemps, PPSize, MPI_FLOAT, TempData, PPSize, MPI_FLOAT,
                    BOSS, MPI_COMM_WORLD );
#elseif
}

#ifdef WANT_EACH_TIME_STEPS_DATA
    MPI_Gather( PPTemps, PPSize, MPI_FLOAT, TempData, PPSize, MPI_FLOAT,
                BOSS, MPI_COMM_WORLD );
#elseif

double time1 = MPI_Wtime( );

```




```
if( me == BOSS )
{
    double seconds = time1 - time0;
    double performance =
        (double)NUM_TIME_STEPS * (double)NUMELEMENTS / seconds / 1000000.;
        // mega-elements computed per second
    fprintf( stderr, "%3d, %10d, %8.2lf\n", NumCpus, NUMELEMENTS, performance );
}

MPI_Finalize( );
return 0;
}
```



```
// read from PerProcessorData[ ], write into NextTemps[ ]
```

```
void
```

```
DoOneTimeStep( int me )
```

```
{
```

```
    MPI_Status status;
```

```
    // send out the left and right end values:
```

```
    // (the tag is from the point of view of the sender)
```

```
    if( me != 0 )                // i.e., if i'm not the first group on the left
```

```
    {
```

```
        // send my PPTemps[0] to me-1 using tag 'L'
```

```
        MPI_Send( &PPTemps[0], 1, MPI_FLOAT, me-1, 'L', MPI_COMM_WORLD );
```

```
        if( DEBUG ) fprintf( stderr, "%3d sent 'L' to %3d\n", me, me-1 );
```

```
    }
```

```
    if( me != NumCpus-1 )        // i.e., not the last group on the right
```

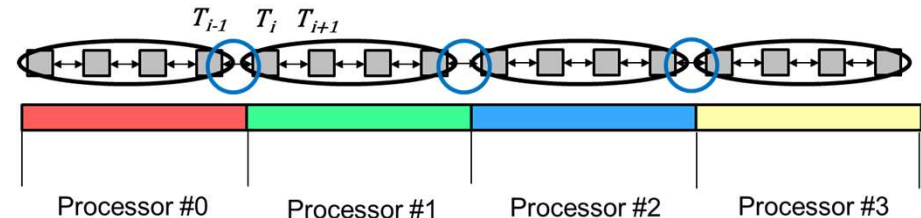
```
    {
```

```
        // send my PPTemps[PPSize-1] to me+1 using tag 'R'
```

```
        MPI_Send( &PPTemps[PPSize-1], 1, MPI_FLOAT, me+1, 'R', MPI_COMM_WORLD );
```

```
        if( DEBUG ) fprintf( stderr, "%3d sent 'R' to %3d\n", me, me+1 );
```

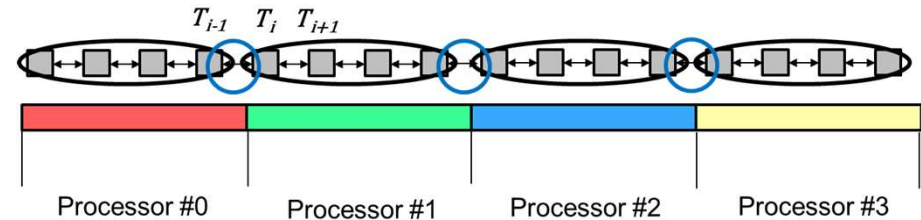
```
    }
```



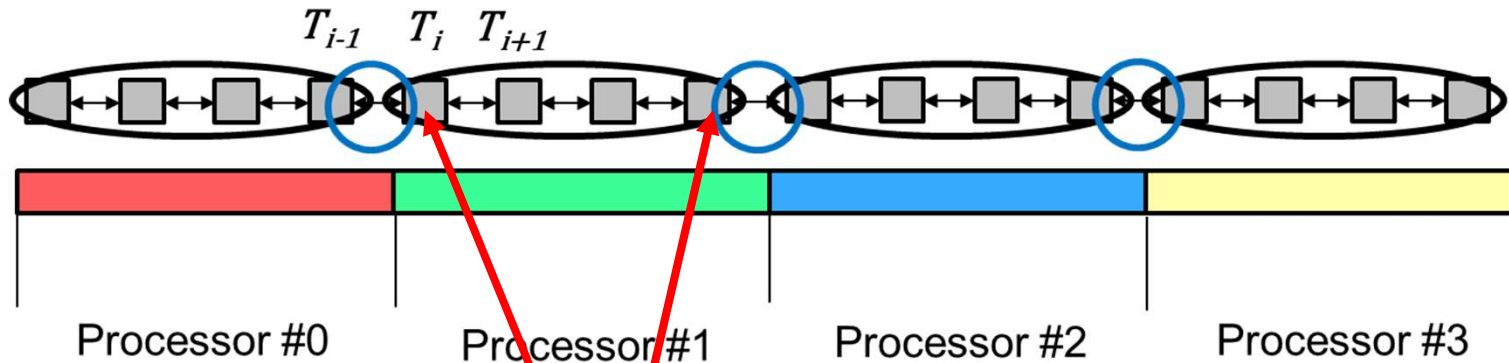
```
float left = 0.;
float right = 0.;
```

```
if( me != 0 )                // i.e., if i'm not the first group on the left
{
    // receive my "left" from me-1 using tag 'R'
    MPI_Recv( &left, 1, MPI_FLOAT, me-1, 'R', MPI_COMM_WORLD, &status );
    if( DEBUG ) fprintf( stderr, "%3d received 'R' from %3d\n", me, me-1 );
}

if( me != NumCpus-1 )       // i.e., not the last group on the right
{
    // receive my "right" from me+1 using tag 'L'
    MPI_Recv( &right, 1, MPI_FLOAT, me+1, 'L', MPI_COMM_WORLD, &status );
    if( DEBUG ) fprintf( stderr, "%3d received 'L' from %3d\n", me, me+1 );
}
```



Sharing Values Across the Boundaries

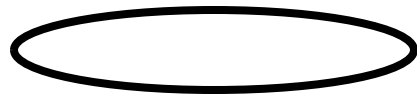
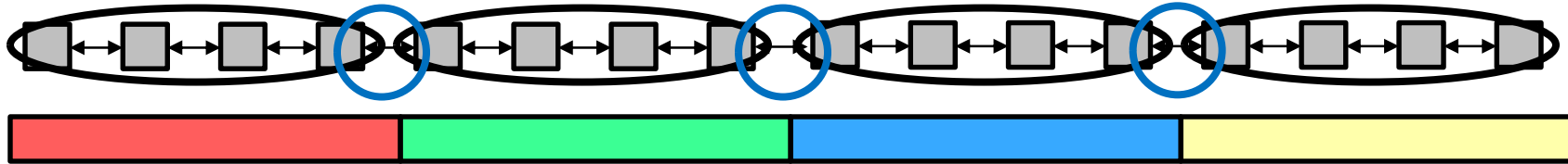


1 sent 'L' to 0
 1 sent 'R' to 2
 2 sent 'L' to 1
 2 sent 'R' to 3
 2 received 'R' from 1
 0 sent 'R' to 1
 0 received 'L' from 1
 1 received 'R' from 0
 1 received 'L' from 2
 3 sent 'L' to 2
 3 received 'R' from 2
 2 received 'L' from 3



1D Compute-to-Communicate Ratio

40



Intraprocessor computing



Interprocessor communication

Compute : Communicate ratio = $N : 2$

where N is the number of compute cells per processor

In the above drawing, Compute : Communicate is 4 : 2

DoOneTimeStep, III

41

```
// first element on the left (0):
{
    float dtemp = ( k_over_rho_c *
                    ( left - 2.*PPTemps[0] + PPTemps[1] ) / ( DX*DX ) ) * DT;
    NextTemps[0] = PPTemps[0] + dtemp;
}

// all the nodes in the middle:
for( int i = 1; i < PPSize-1; i++ )
{
    float dtemp = ( k_over_rho_c *
                    ( PPTemps[i-1] - 2.*PPTemps[ i ] + PPTemps[i+1] ) / ( DX*DX ) ) * DT;
    NextTemps[i] = PPTemps[i] + dtemp;
}

// last element on the right (PPSize-1):
{
    float dtemp = ( k_over_rho_c *
                    ( PPTemps[PPSize-2] - 2.*PPTemps[PPSize-1] + right ) / ( DX*DX ) ) * DT;
    NextTemps[PPSize-1] = PPTemps[PPSize-1] + dtemp;
}
```

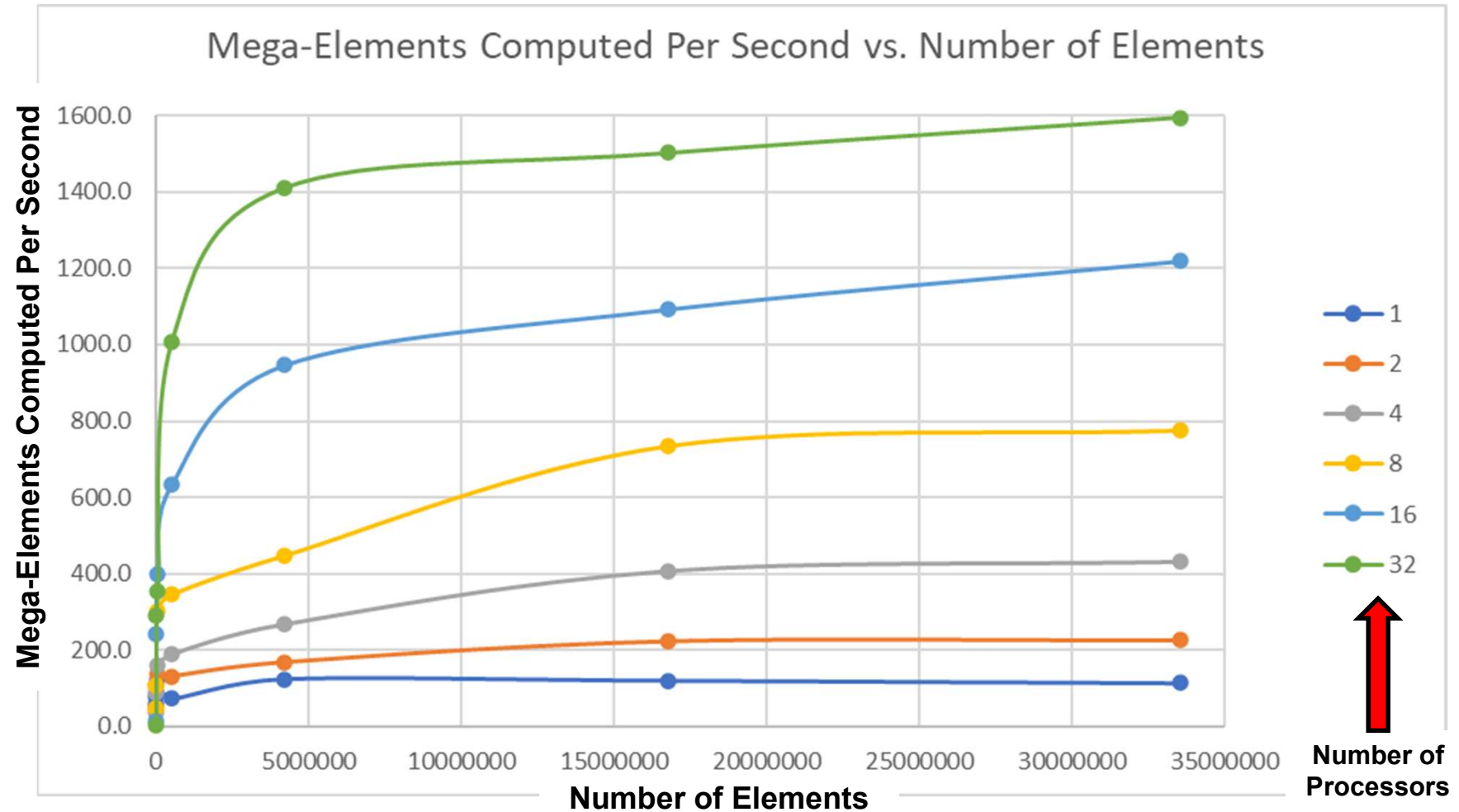


DoOneTimeStep, IV

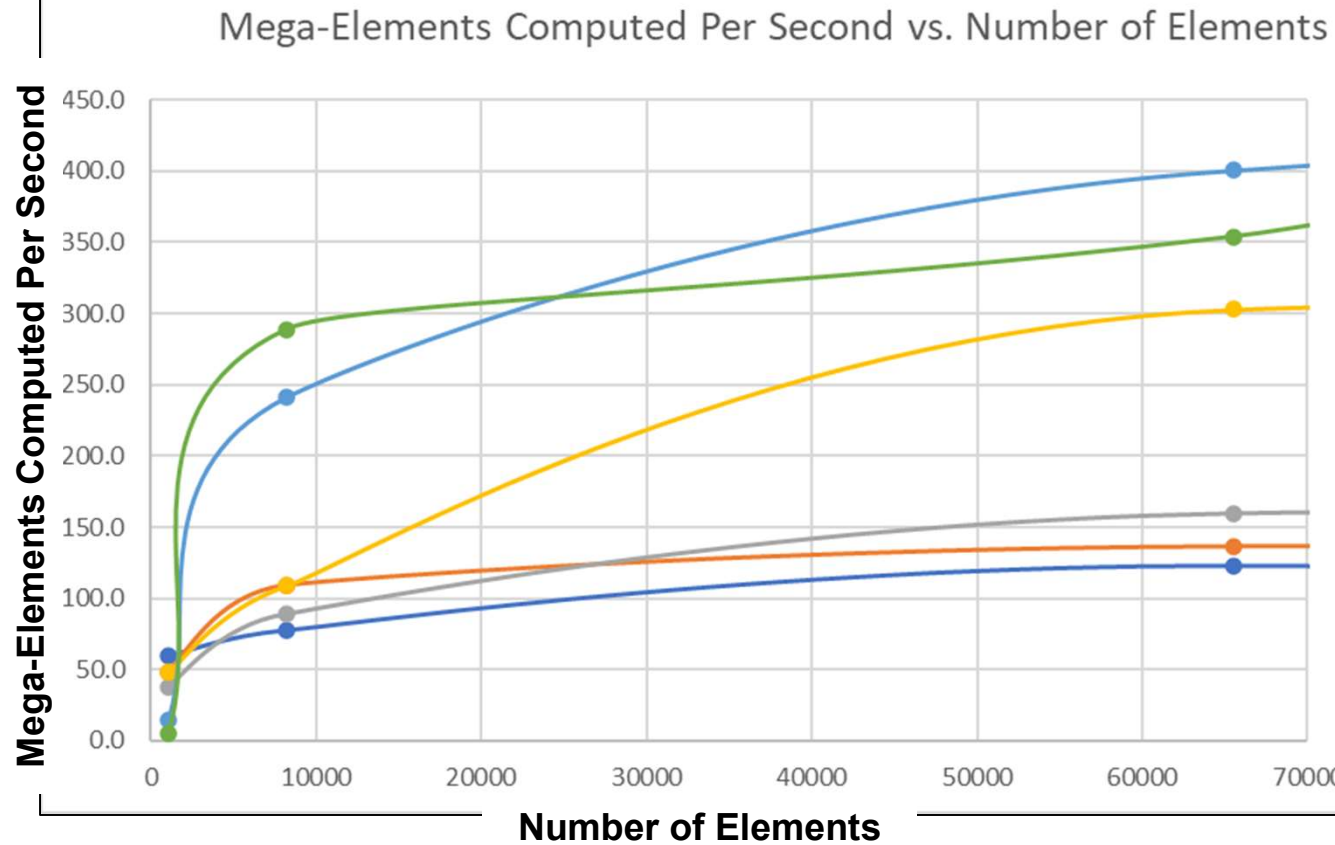
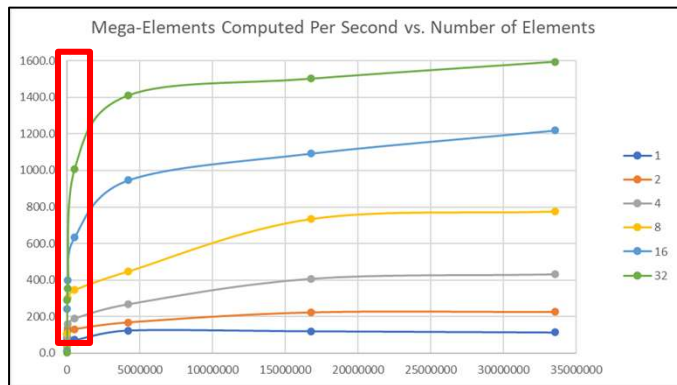
42

```
// update the local dataset:  
  
for( int i = 0; i < PPSize; i++ )  
{  
    PPTemps[ i ] = NextTemps[ i ];  
}  
}
```



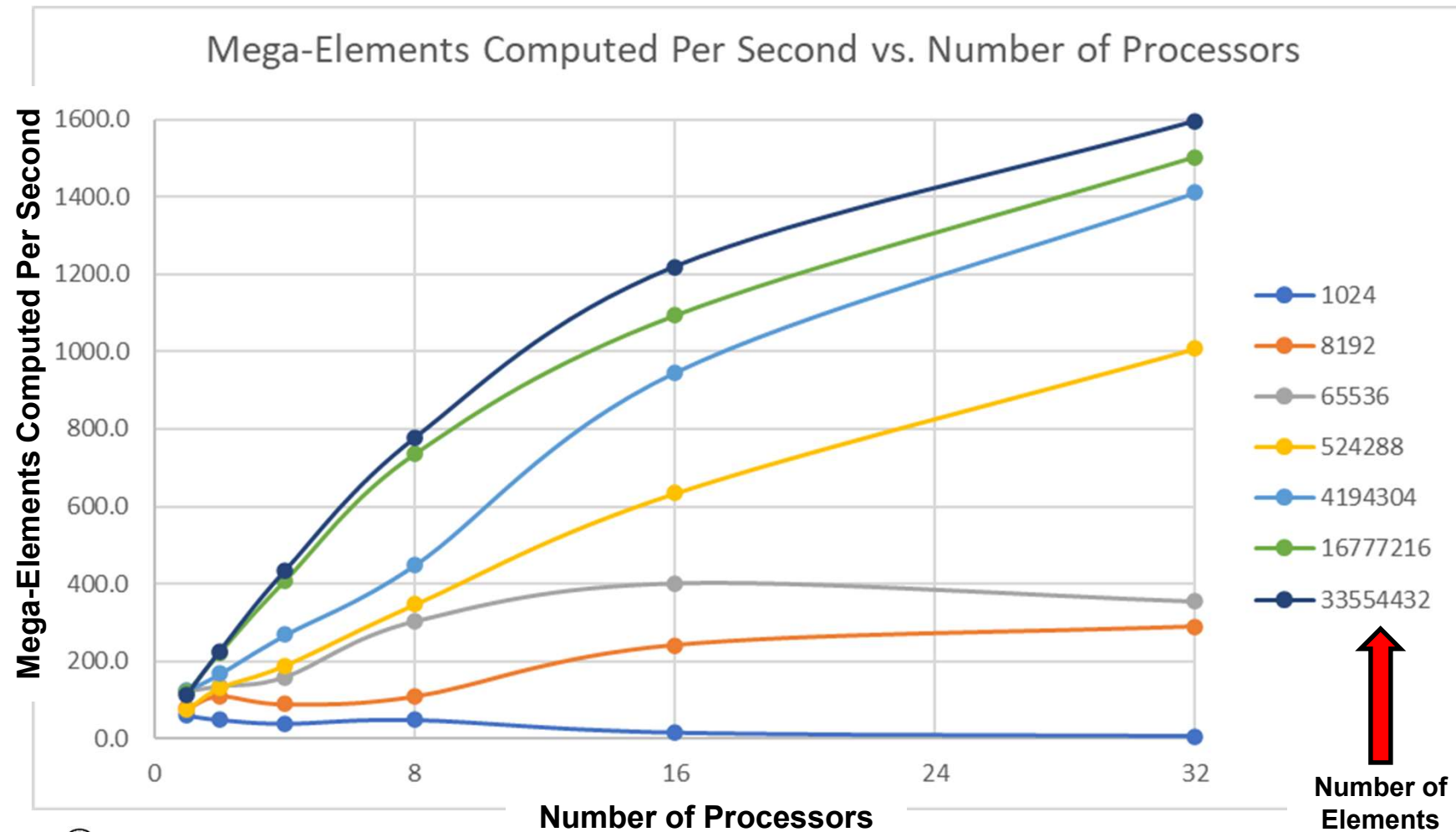


Low Dataset-Size MPI Performance



Number of
Processors

mjb – June 2, 2021



MPI Reduction

```
MPI_Reduce( partialResult, globalResult, count, type, operator, dst, MPI_COMM_WORLD );
```

Where the partial result is stored on each CPU

Place to store the full result on the dst CPU

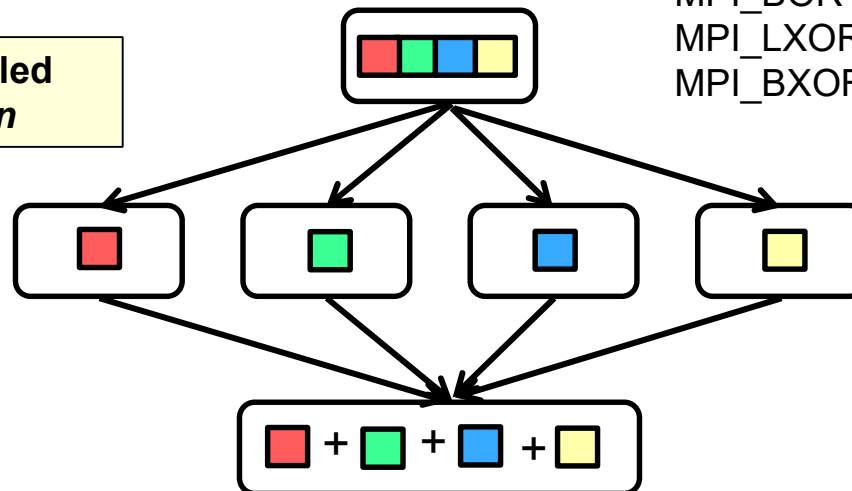
Number of elements in the partial result

MPI_CHAR
MPI_INT
MPI_LONG
MPI_FLOAT
MPI_DOUBLE
...

MPI_MIN
MPI_MAX
MPI_SUM
MPI_PROD
MPI_MINLOC
MPI_MAXLOC
MPI_LAND
MPI_BAND
MPI_LOR
MPI BOR
MPI_LXOR
MPI_BXOR

Who is given the final answer

This really should be called
Scatter/Gather/Reduction



Reduction

Both the sender and receivers need to execute **MPI_Reduce**.
There is no separate receive function

MPI Reduction Example

// gratuitous use of a reduce -- average all the temperatures:

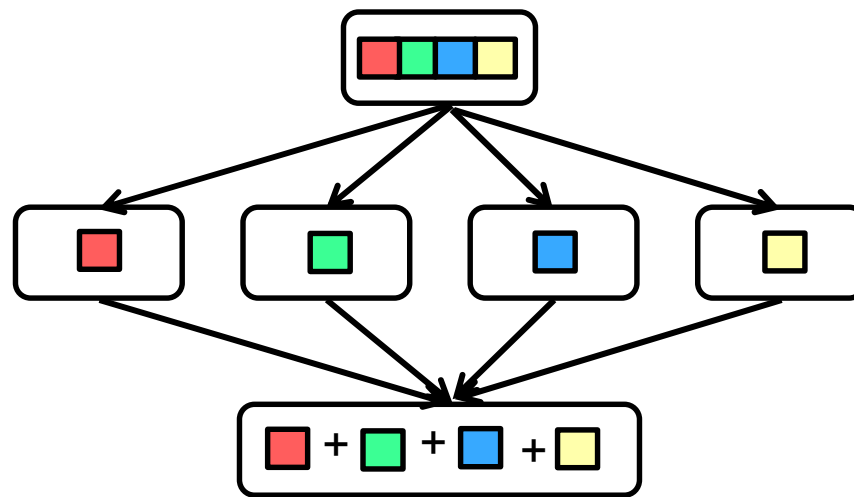
```
float partialSum = 0.;  
for( int i = 0; i < PPSize; i++ )  
    partialSum += PPTemps[ i ];
```

```
float globalSum = 0.;
```

```
MPI_Reduce( &partialSum, &globalSum, 1, MPI_FLOAT, MPI_SUM, BOSS, MPI_COMM_WORLD );
```

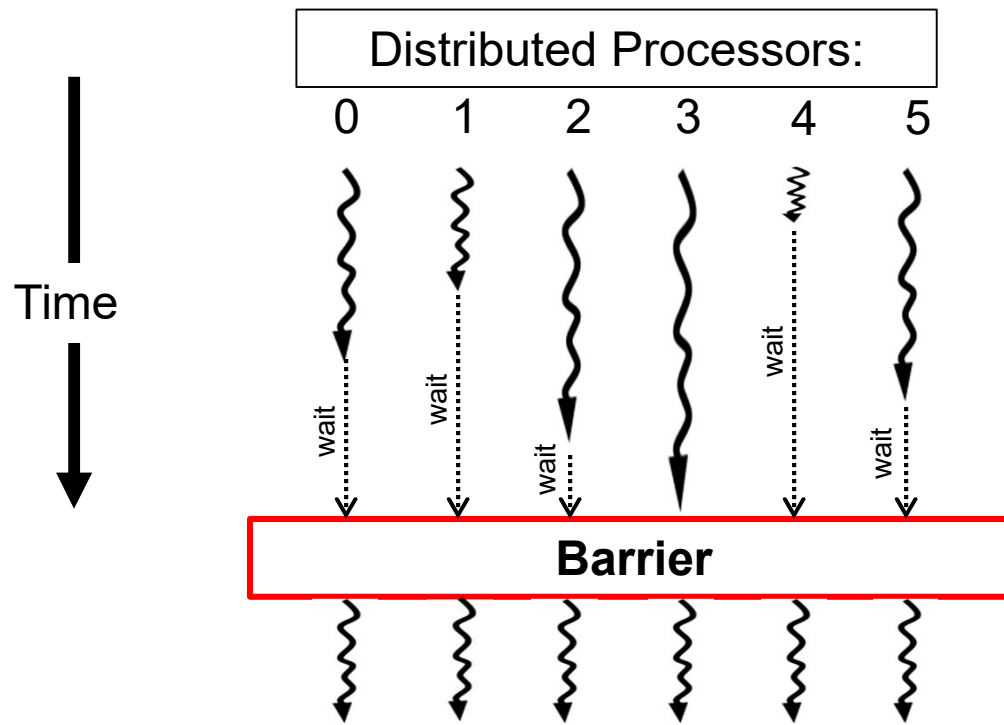
```
if( me == BOSS )
```

```
    fprintf( stderr, "Average temperature = %f\n", globalSum/(float)NUMELEMENTS );
```



MPI Barriers

```
MPI_Barrier( MPI_COMM_WORLD );
```



All CPUs must execute the call to `MPI_Barrier()` before any of the CPUs can move past it. That is, each CPU's `MPI_Barrier()` blocks until all CPUs execute a call to `MPI_Barrier()`.

MPI Derived Types

Idea: In addition to types MPI_INT, MPI_FLOAT, etc., allow the creation of new MPI types so that you can transmit an “array of structures”.

Reason: There is significant overhead with each transmission. Better to send one entire array of structures instead of sending several arrays separately.

```
MPI_Type_create_struct( count, blocklengths, displacements, types, datatype );
```

```
struct point
{
    int    pointSize;
    float x, y, z;
};
```

```
MPI_Datatype MPI_POINT;
int blocklengths[ ] = { 1, 1, 1, 1 };
int displacements[ ] = { 0, 4, 8, 12 };
MPI_type types[ ] = { MPI_INT, MPI_FLOAT, MPI_FLOAT, MPI_FLOAT };

MPI_Type_create_struct( 4, blocklengths, displacements, types, &MPI_POINT );
```



You can now use **MPI_POINT** everywhere you could have used **MPI_INT**, **MPI_FLOAT**, etc.

MPI Timing

```
double MPI_Wtick( );
```

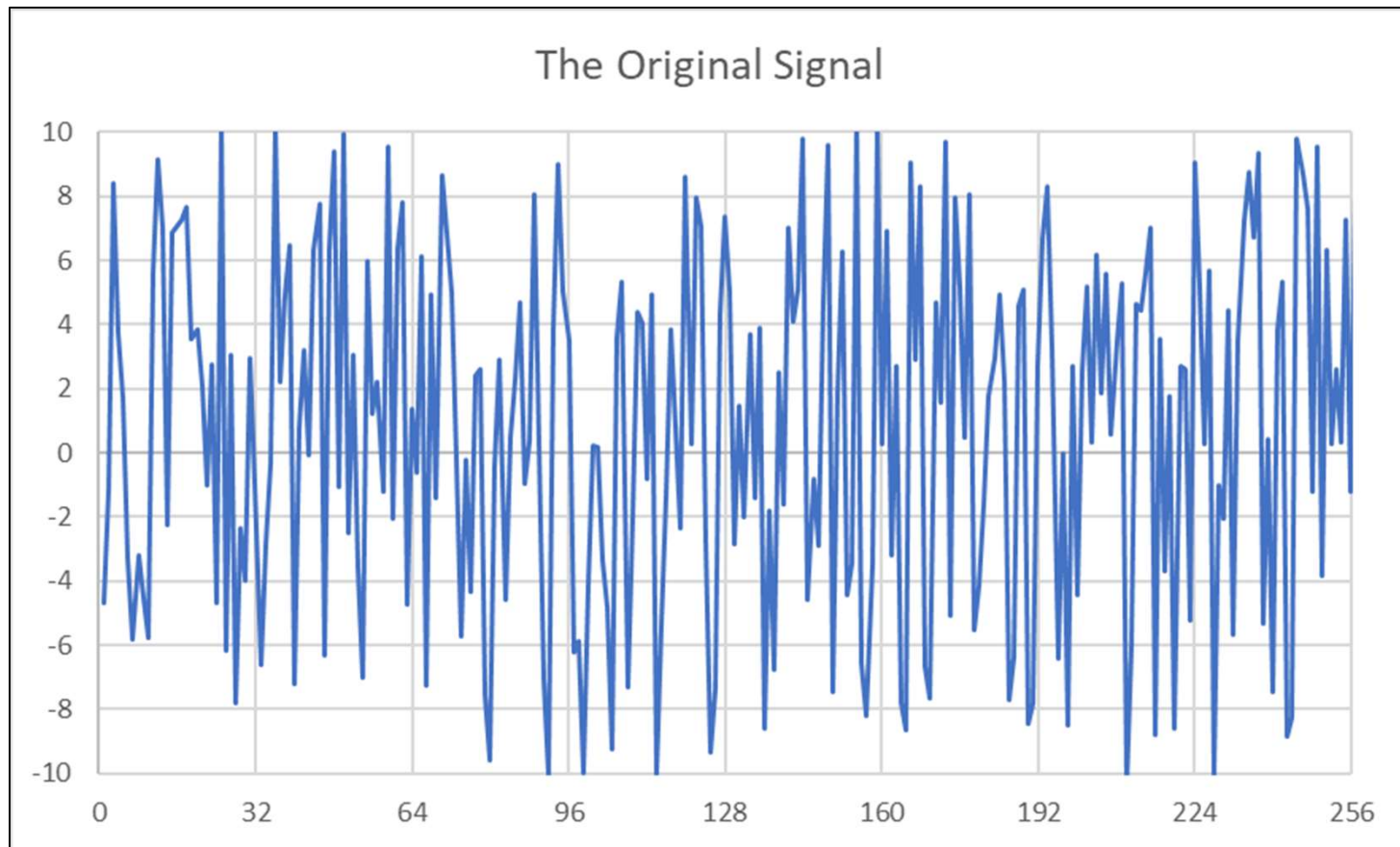
Returns the resolution of the clock, in seconds.

```
double MPI_Wtime( );
```

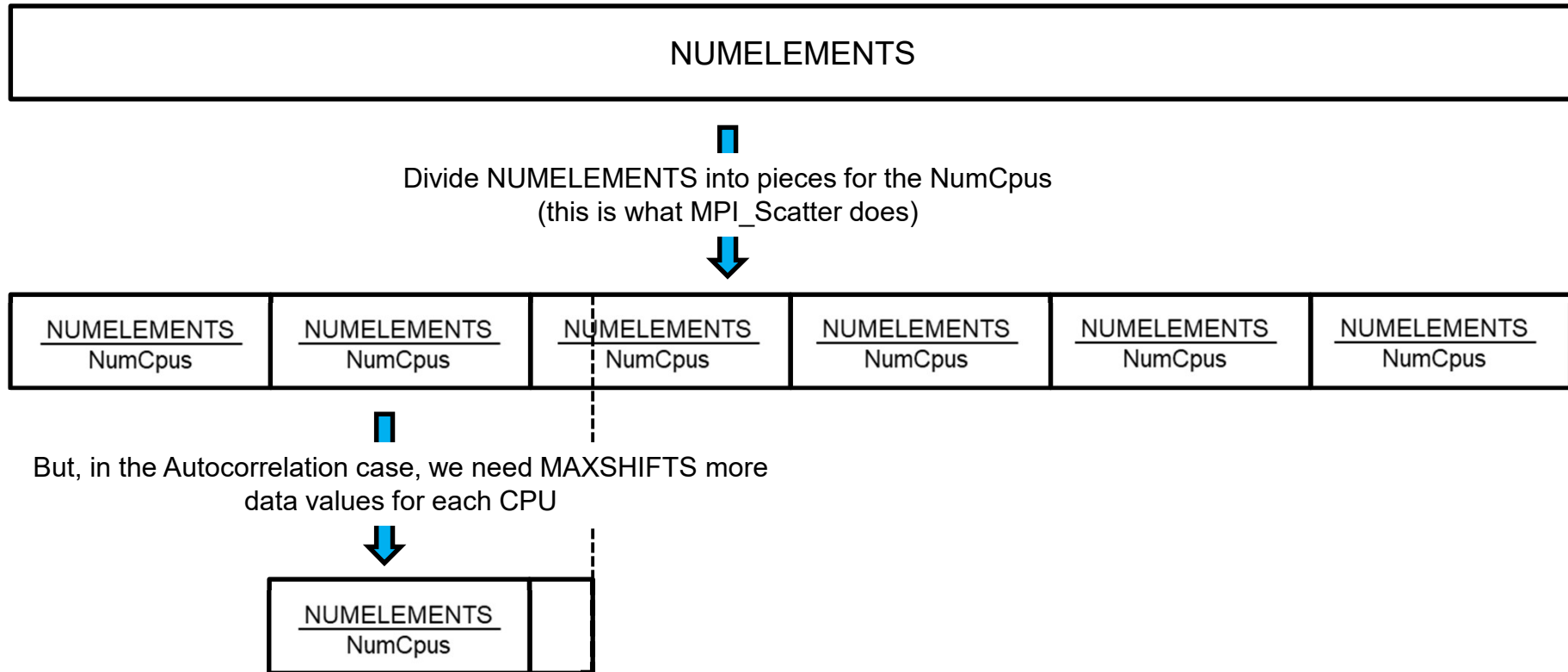
Returns the time, in seconds, since “some time in the past”.

Warning: the clocks on the different CPUs are not guaranteed to be synchronized!

Autocorrelation – a Piece of the Original Signal



Autocorrelation – More than Just a Scatter



Autocorrelation – How the Shifting Works

