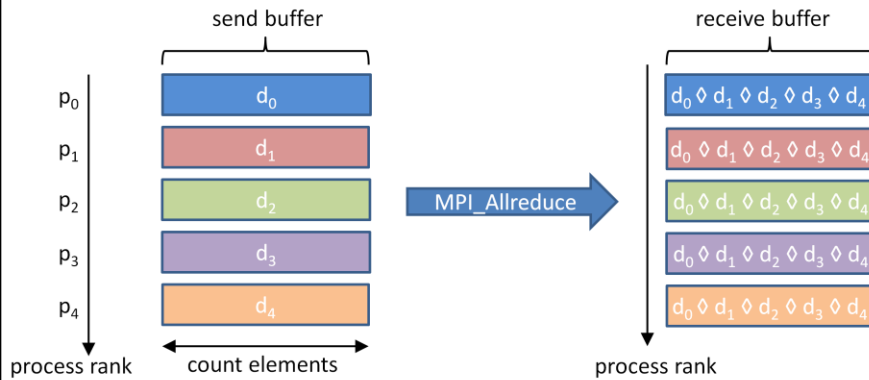


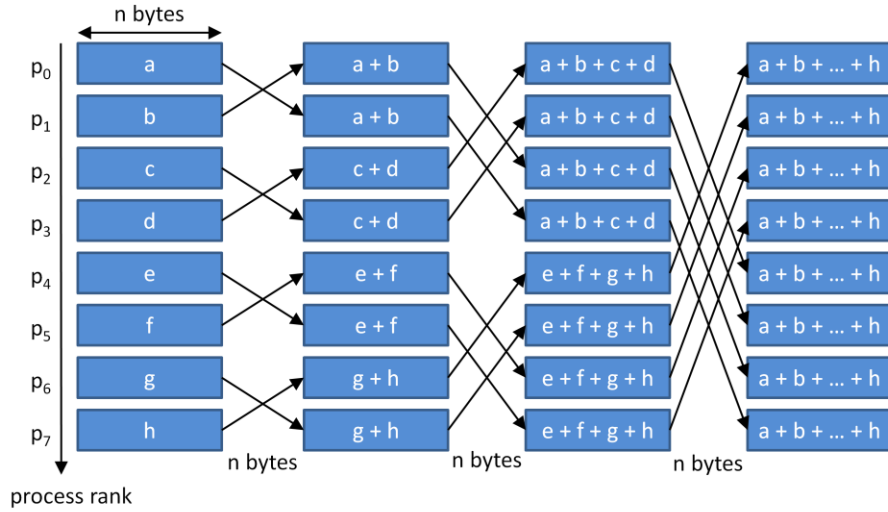
Allreduce algorithm

```
MPI_Allreduce(void *sendbuf, void *recvbuf, int count,  
               MPI_Datatype dataType, MPI_Op op, MPI_Comm comm)
```



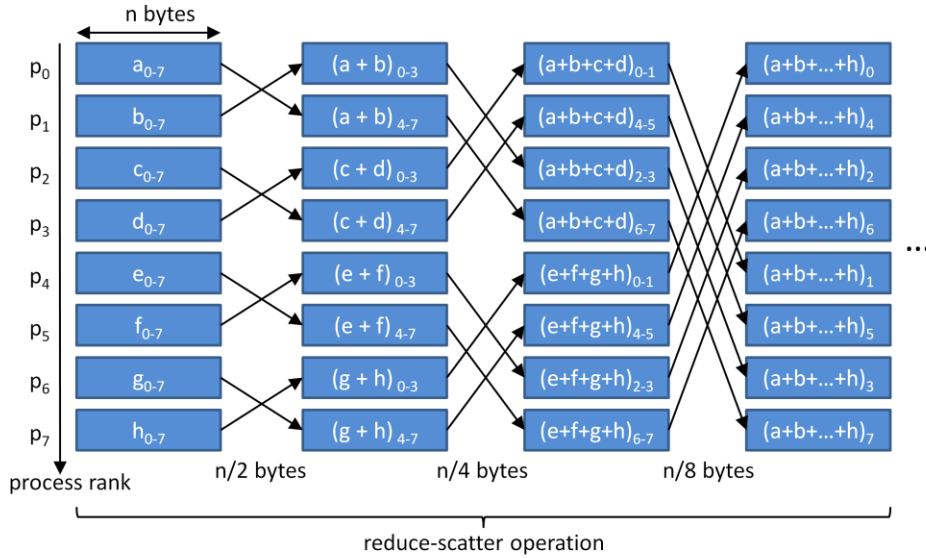
Q: Develop an algorithm for the allreduce routine. Derive the time complexity for that algorithm. Assume a fully non-blocking (duplex) network.

Solution 1: butterfly communication scheme



$$T_{\text{sol1}} = (\alpha + \beta n + \gamma n) \log_2 P \quad (\text{assume } P = 2^i)$$

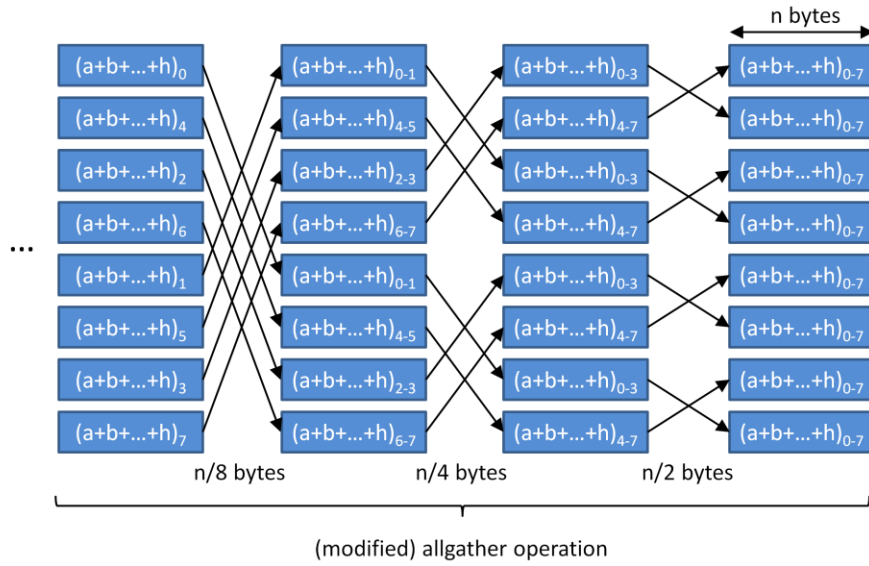
Solution 2: reduce-scatter + allgather



$$T_{\text{sol2}} = \alpha \log_2 P + (\beta n + \gamma n)(1 - 1/P) + \dots$$

Warning: box sizes are not drawn to scale.

Solution 2: reduce-scatter + allgather (cont'd)



$$T_{\text{sol2}} = 2\alpha \log_2 P + (2\beta n + \gamma n)(1 - 1/P) \quad (\text{assume } P = 2^i)$$