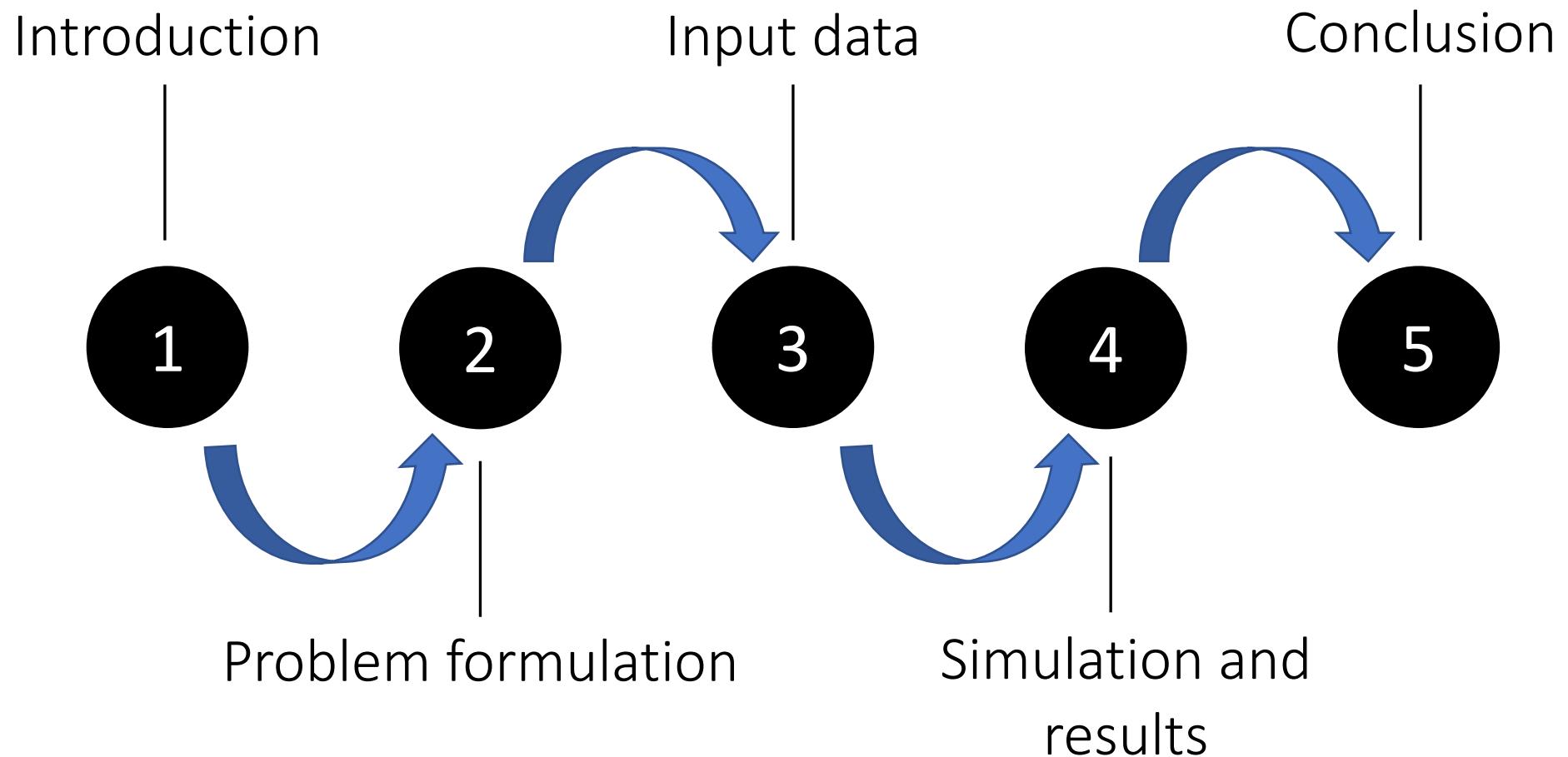


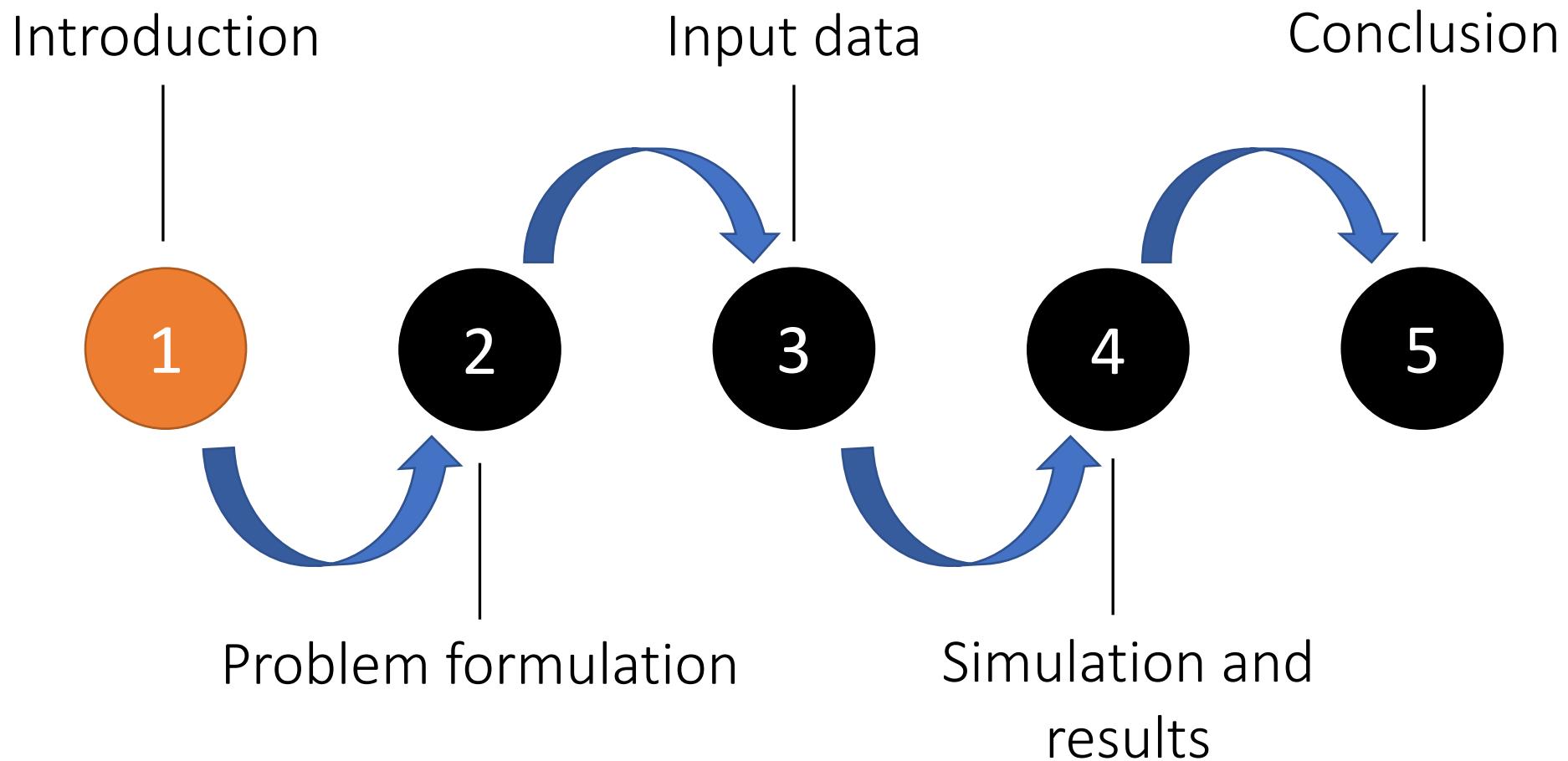
Optimal Scheduling of Vehicle-to-Grid Energy and Ancillary Services



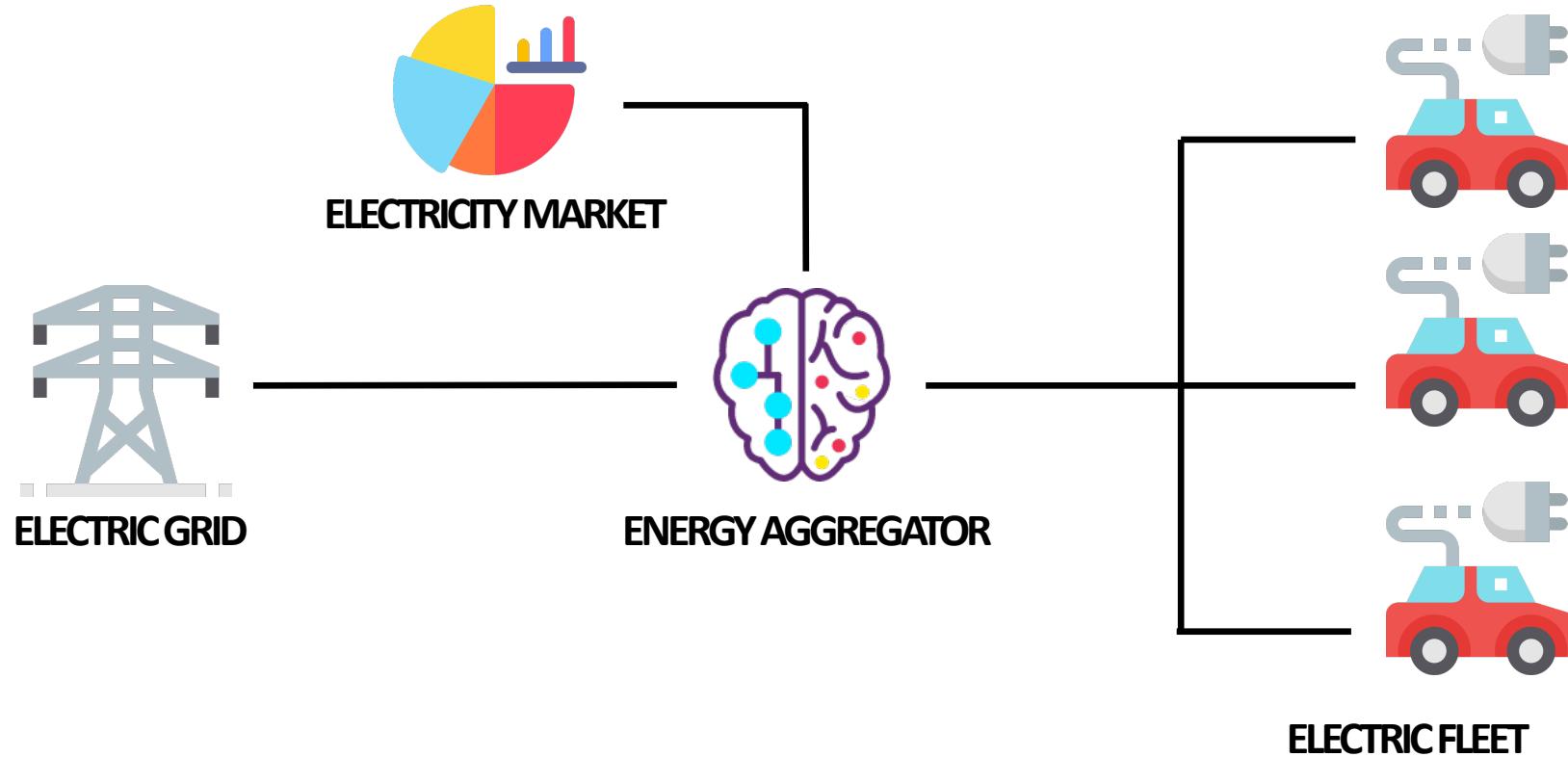
Agenda



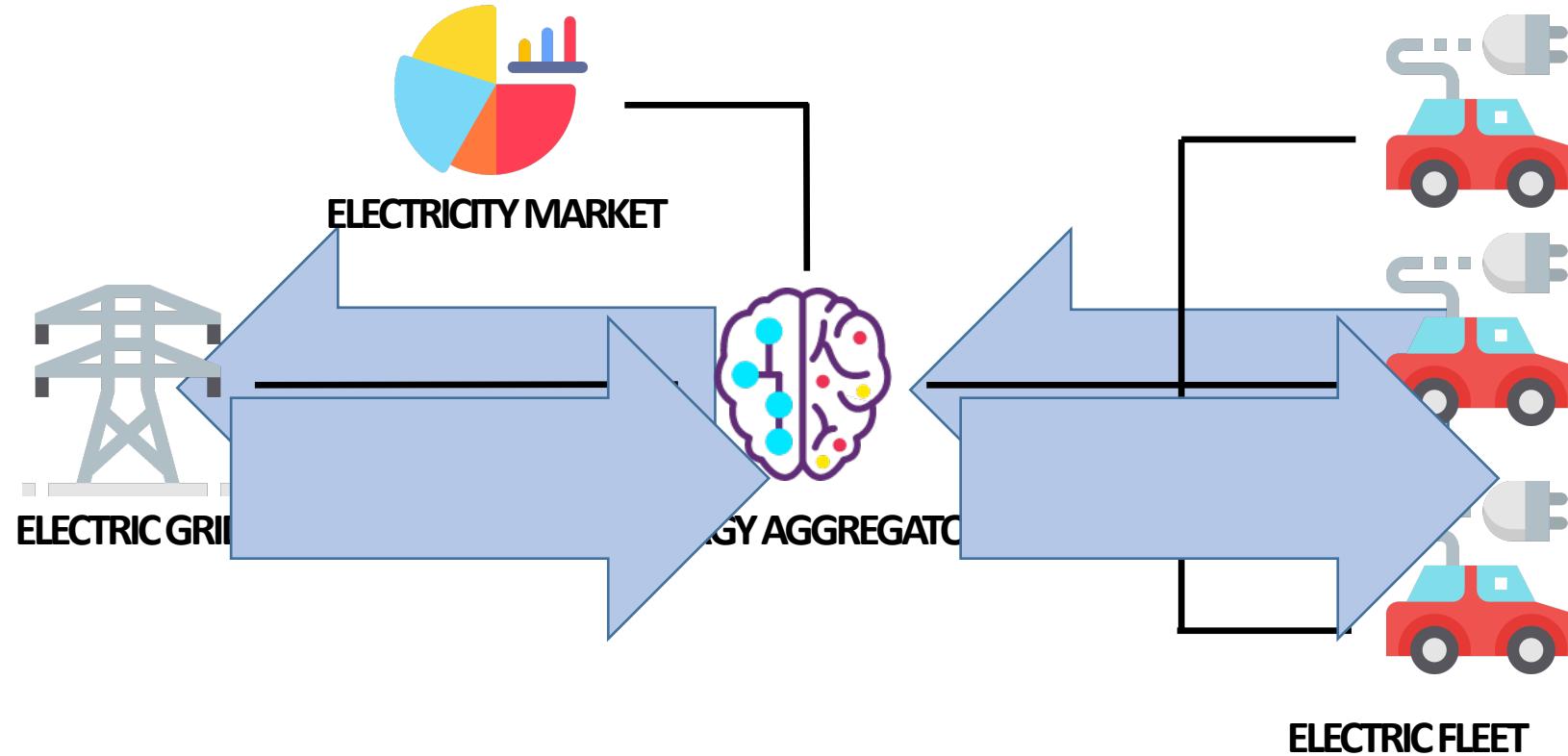
Agenda



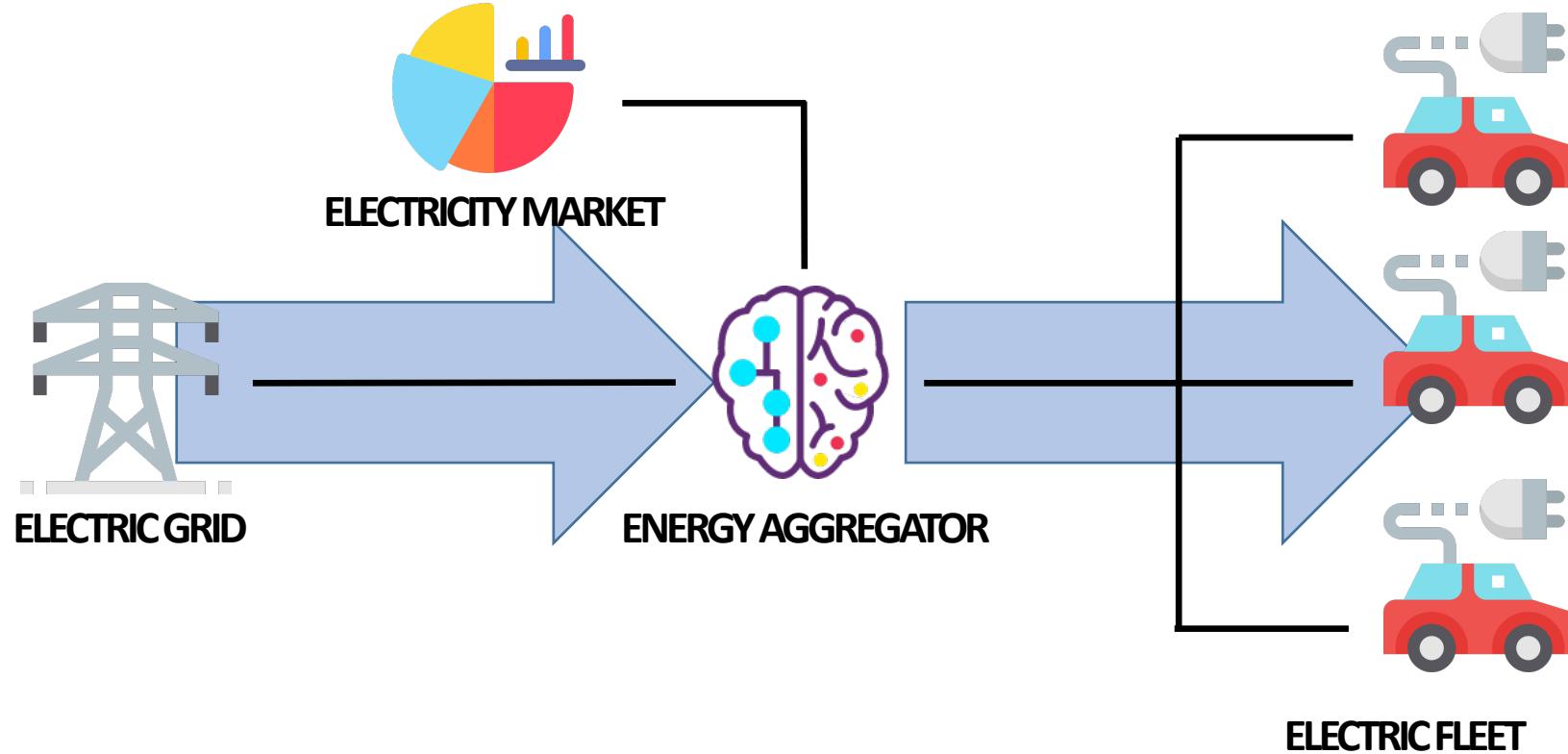
Introduction



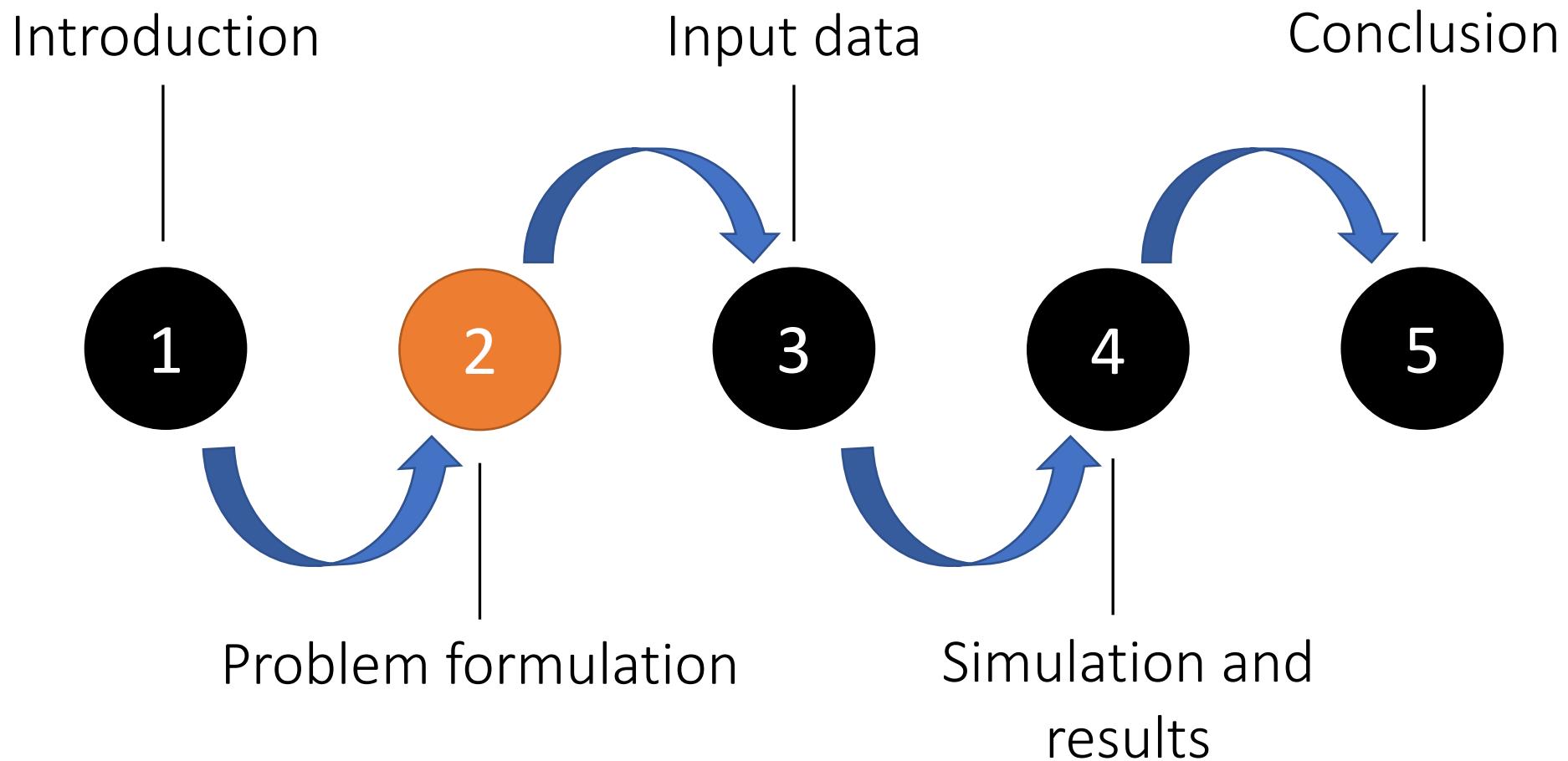
Introduction - V2G



Introduction - Smart Charging



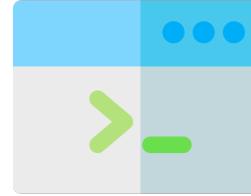
Agenda



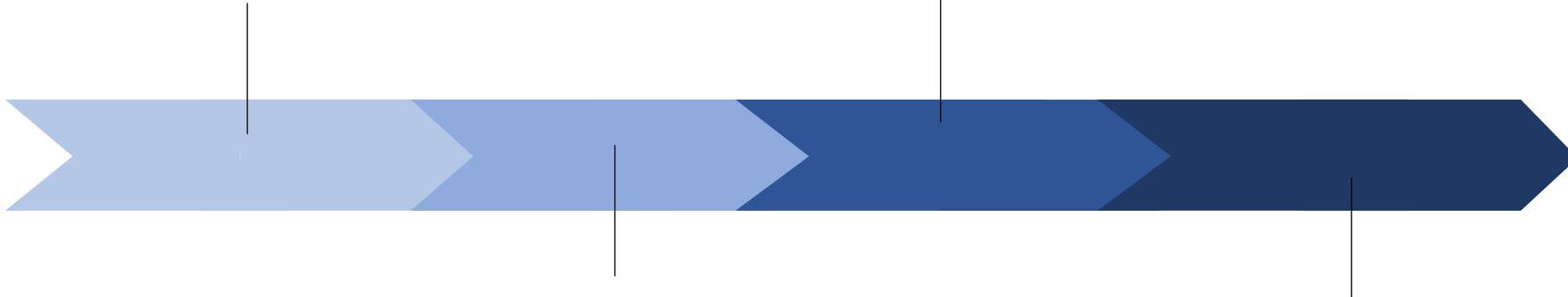
Software package & work-flow



Python programming language and **Pyomo** library



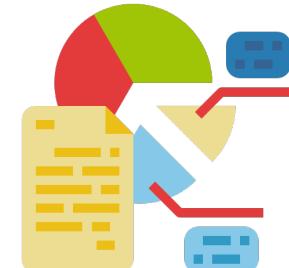
Run the script and **solve** the problem (GLPK)



Energy and ancillary services prices collected in **excel spreadsheets**



Converted all input data of the model in a **DAT file**



Analysis of the **results** from the optimization

Creation of the model and definition of the parameters

Parameter	Description
Arrival	Daily arrival time of every EV
T_Trip	Daily departure time of every EV
EVPer	Expected percentage of the EVs remaining to perform V2G
Dep	Probability of unexpected departure of the EV
Comp	Compensation factor to account for unplanned departures
SOC	Initial state of charge of the EV
Ef	Efficiency of the EV's battery charger
Mc	Maximum charge capacity of the EV
DC	Degradation cost of the battery for discharging
MP	Maximum possible power draw of the EV (if not plugged, this value is 0)
Price_RD	Price of regulation down
Price_RU	Price of regulation up
P	Electricity price

DRIVING
PROFILES

EVs and
CHARGERS

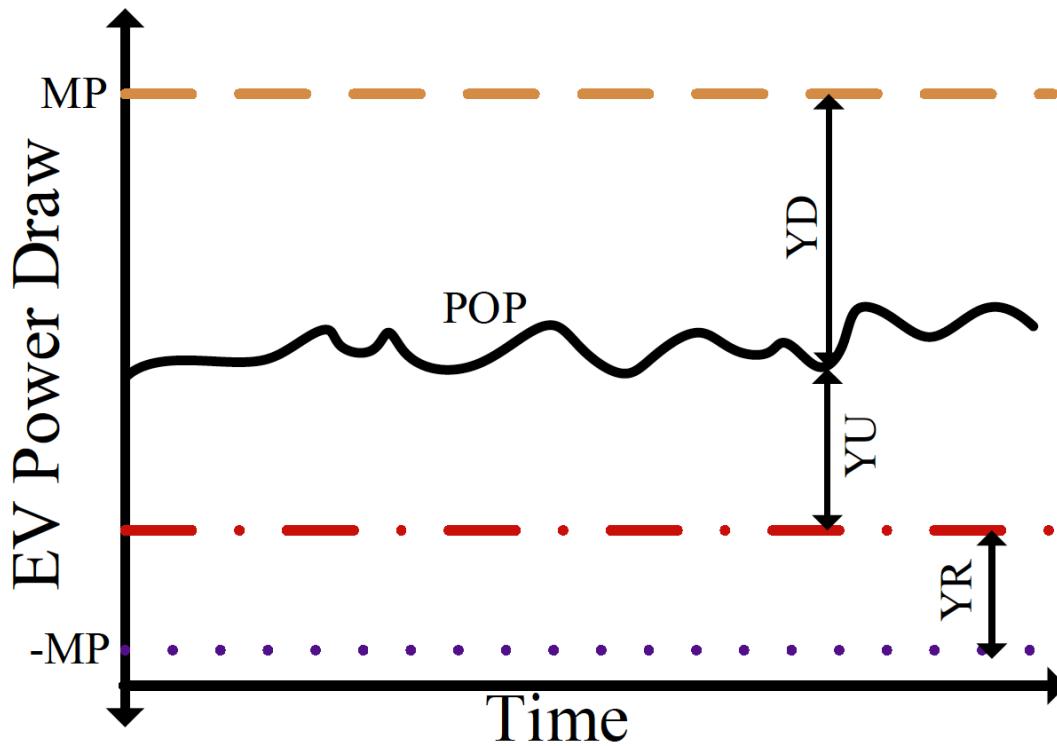
PRICE
SIGNALS

```

20 #CREATE MODEL
21 model = AbstractModel()
22
23
24 #DEFINE PARAMETERS
25 model.time = Param(within=NonNegativeIntegers)
26 model.cars = Param(within=NonNegativeIntegers)
27 model.days = Param(within=NonNegativeIntegers)
28
29 model.Arrival = Param(model.I, model.J, within=NonNegativeIntegers)
30 model.T_Trip = Param(model.I, model.J, within=NonNegativeIntegers)
31
32 model.EVPer = Param(model.J, model.T, within = NonNegativeReals)
33 model.Dep = Param(model.I, model.J, model.T, within = NonNegativeReals)
34 model.Comp = Param(model.I, model.J, model.T, within = NonNegativeReals)
35
36 model.SOC = Param(model.I, model.J, within = NonNegativeReals)
37
38
39 #Technical specifications of cars and chargers
40 model.Ef = Param(model.I, within = NonNegativeReals)
41 model.Mc = Param(model.I, within = NonNegativeReals)
42
43 model.DC = Param(model.I, within = NonNegativeReals)
44
45 model.MP = Param(model.I, model.J, model.T)
46
47
48 #Prices (electricity + ancillary services)
49 model.Price_RD = Param(model.J, model.T, within = NonNegativeReals)
50 model.Price_RU = Param(model.J, model.T, within = NonNegativeReals)
51 model.P = Param(model.J, model.T, within = NonNegativeReals)
52
53 #DEFINE ITERATORS
54 model.T = RangeSet(1, model.time)
55 model.I = RangeSet(1, model.cars)
56 model.J = RangeSet(1, model.days)

```

Decision variables



```
36 #DATA STRUCTURES – DECISION VARIABLES
37 POP_dict = {}
38 for i in range(1, number_EVs+1):
39     for j in range(1, num_days+1):
40         for t in range(1, final_time+1):
41             POP_dict[i, j, t] = 0
42             #print(i, j, t, POP_dict[i,j,t])
43
44 MxAP_dict = {}
45 for i in range(1, number_EVs+1):
46     for j in range(1, num_days+1):
47         for t in range(1, final_time+1):
48             MxAP_dict[i, j, t] = 0
49             #print(i, j, t, MxAP_dict[i,j,t])
50
51 MnAP_dict = {}
52 for i in range(1, number_EVs+1):
53     for j in range(1, num_days+1):
54         for t in range(1, final_time+1):
55             MnAP_dict[i, j, t] = 0
56             #print(i, j, t, MnAP_dict[i,j,t])
57
58 Deg_dict = {}
59 for i in range(1, number_EVs+1):
60     for j in range(1, num_days+1):
61         for t in range(1, final_time+1):
62             Deg_dict[i, j, t] = 0
63             #print(i, j, t, Deg_dict[i,j,t])
64
65
66 #DEFINE DECISION VARIABLES
67 model.POP = Var(model.I, model.J, model.T, domain=Reals, initialize = POP_dict)
68 model.MxAP = Var(model.I, model.J, model.T, domain=NonNegativeReals, initialize
69 model.MnAP = Var(model.I, model.J, model.T, domain=NonNegativeReals, initialize
70 model.Deg = Var(model.I, model.J, model.T, domain=NonNegativeReals, initialize
```

Objective function

Objective function's equations term	Definition
$\sum_t (P_{RU}(t) \cdot R_U(t) + P_{RD}(t) \cdot R_D(t) + P_{RR}(t) \cdot R_R(t))$	Revenues from selling regulation and responsive services
$+ M_k \sum_i \sum_t (E[FP_i(t)])$	Fixed rate on the energy delivered to the EV
$+ \sum_i \sum_t (E[FP_i(t)] \cdot P(t))$ if $E[FP_i(t)] \leq 0$	Revenues from selling energy to the grid

INCOME

$\sum_i \sum_t (E[FP_i(t)] \cdot P(t))$	Wholesale cost of energy delivered to the EVs
$+ \sum_i \sum_t \left(\frac{DC_i \cdot E[FP_i^-(t)]}{E f_i} \right)$	Battery degradation associated from discharging

COSTS

```

99 #OBJECTIVE FUNCTION
100 def income(model):
101     return sum(sum((model.Price_RD[j,t] * sum(model.MxAP[i,j,t] for i in model.I) + model.Price_RU[j,t]
102                   * sum(model.MnAP[i,j,t] for i in model.I)) * model.EVPer[j,t] for t in model.T) for j in model.J)
103     + M_k * sum(sum((model.MxAP[i,j,t] * ExD + model.POP[i,j,t] - model.MnAP[i,j,t] * ExU)
104                   * model.EVPer[j,t] for t in model.T) for j in model.J) for i in model.I)
105
106 def costs(model):
107     return sum(sum((model.MxAP[i,j,t] * ExD + model.POP[i,j,t] - model.MnAP[i,j,t] * ExU)
108                   * model.EVPer[j,t] * model.PI[j,t] for t in model.T) for j in model.J) for i in model.I)
109     + sum(sum(model.Deg[i,j,t] for t in model.T) for j in model.J) for i in model.I)
110
111 #Final equation
112 def profit(model):
113     return income(model) - costs(model)
114 model.obj = Objective(rule = profit, sense = maximize)

```

Operational constraints

```

117 #OPERATIONAL CONSTRAINTS
118 def fifteen_rule(model, i):
119     for j in range(1, num_days+1):
120         for k in range(model.Arrival[i,j], model.T_Trip[i,j]):
121             return sum((model.MxAP[i,j,t] * ExD + model.POP[i,j,t] - model.MnAP[i,j,t] * ExU) * model.Comp[i,j,t]
122                         + (model.Deg[i,j,t]/model.DC[i])*(1-model.Ef[i]*model.Ef[i])/model.Ef[i]
123                         for t in range(model.Arrival[i,j], model.T_Trip[i,j]):[k-model.Arrival[i,j]+1]) * model.Ef[i]
124             + model.SOC[i,j] <= model.Mc[i]
125 model.fifteen = Constraint(model.I, rule=fifteen_rule)
126
127 def sixteen_rule(model, i):
128     for j in range(1, num_days+1):
129         for k in range(model.Arrival[i,j], model.T_Trip[i,j]):
130             return sum((model.MxAP[i,j,t] * ExD + model.POP[i,j,t] - model.MnAP[i,j,t] * ExU) * model.Comp[i,j,t]
131                         + (model.Deg[i,j,t]/model.DC[i])*(1-model.Ef[i]*model.Ef[i])/model.Ef[i]
132                         for t in range(model.Arrival[i,j], model.T_Trip[i,j]):[k-model.Arrival[i,j]+1]) * model.Ef[i]
133                         + model.SOC[i,j] >= 0
134 model.sixteen = Constraint(model.I, rule=sixteen_rule)
135
136 def seventeen_rule(model, i):
137     for j in range(1, num_days+1):
138         return sum((model.MxAP[i,j,t] * ExD + model.POP[i,j,t] - model.MnAP[i,j,t] * ExU) * model.Comp[i,j,t]
139                         + (model.Deg[i,j,t]/model.DC[i])*(1-model.Ef[i]*model.Ef[i])/model.Ef[i]
140                         for t in range(model.Arrival[i,j], model.T_Trip[i,j])) + model.SOC[i,j] >= 0.99 * model.Mc[i]
141 model.seventeen = Constraint(model.I, rule=seventeen_rule)
142
143 def eighteen_rule(model, i):
144     for j in range(1, num_days+1):
145         return (model.MxAP[i,j,model.Arrival[i,j]] + model.POP[i,j,model.Arrival[i,j]])
146         * model.Comp[i,j,model.Arrival[i,j]] * model.Ef[i] + model.SOC[i,j] <= model.Mc[i]
147 model.eighteen = Constraint(model.I, rule=eighteen_rule)
148
149 def nineteen_rule(model, i):
150     for j in range(1, num_days+1):
151         return (model.POP[i,j,model.Arrival[i,j]] - model.MnAP[i,j,model.Arrival[i,j]])
152         + (model.Deg[i,j,model.Arrival[i,j]]/model.DC[i])*(1-model.Ef[i]*model.Ef[i])/model.Ef[i] *
153         model.Comp[i,j,model.Arrival[i,j]] * model.Ef[i] + model.SOC[i,j] >= 0
154 model.nineteen = Constraint(model.I, rule=nineteen_rule)
155
156
157
158

```

Operational constraint	Description
$\left(\sum_{t=1}^{time} (E[FP_i(t)] \cdot Comp_i(t) + \rho_i(t)) \cdot Ef_i \right) \leq M_{Ci}$ $+ SOC_{I,i} - Trip_i(time)$	The energy level of the battery is bounded between 0 and its maximum capacity at every moment of the daily scheduling and it is set to be at least 99% of its maximum capacity at the end of the daily scheduling
$\left(\sum_{t=1}^{time} (E[FP_i(t)] \cdot Comp_i(t) + \rho_i(t)) \cdot Ef_i \right) \geq 0$ $+ SOC_{I,i} - Trip_i(time)$ $\forall i, time$	
$\left(\sum_{t=1}^T (E[FP_i(t)] \cdot Comp_i(t) + \rho_i(t)) \cdot Ef_i \right) \geq 0.99M_{Ci}$ $+ SOC_{I,i} - Trip_i(T)$	
$(MxAP_i(1) + POP_i(1)) \cdot Comp_i(1) \cdot Ef_i + SOC_{I,i} \leq M_{Ci}$	Conditions on the arrival times of the electric vehicles
$\left((POP_i(1) - MnAP_i(1) - RSRP_i(1) + \rho_i(1)) \cdot Comp_i(1) \cdot Ef_i + SOC_{I,i} \right) \geq 0$	
$(MxAP_i(t) + POP_i(t)) \cdot Comp_i(t) \leq MP_i(t) \quad \forall i$ $MnAP_i(t) \leq POP_i(t) + MP_i(t) \quad \forall i$	Ancillary services capacities cannot exceed the admissible limits of the maximum possible power draw of the charger
$MxAP_i(t) \geq 0 \quad \forall i$ $MnAP_i(t) \geq 0 \quad \forall i$ $POP_i(t) \geq -MP_i(t) \quad \forall i$ $Deg_i(t) \geq 0 \quad \forall i$	Bounds of the decision variables
$Deg_i(t) \geq DC_i \cdot E[FP_i^-(t)] \cdot \frac{Comp_i(t)}{Ef_i} \quad \forall i$	Condition on the degradation of the battery

Operational constraints

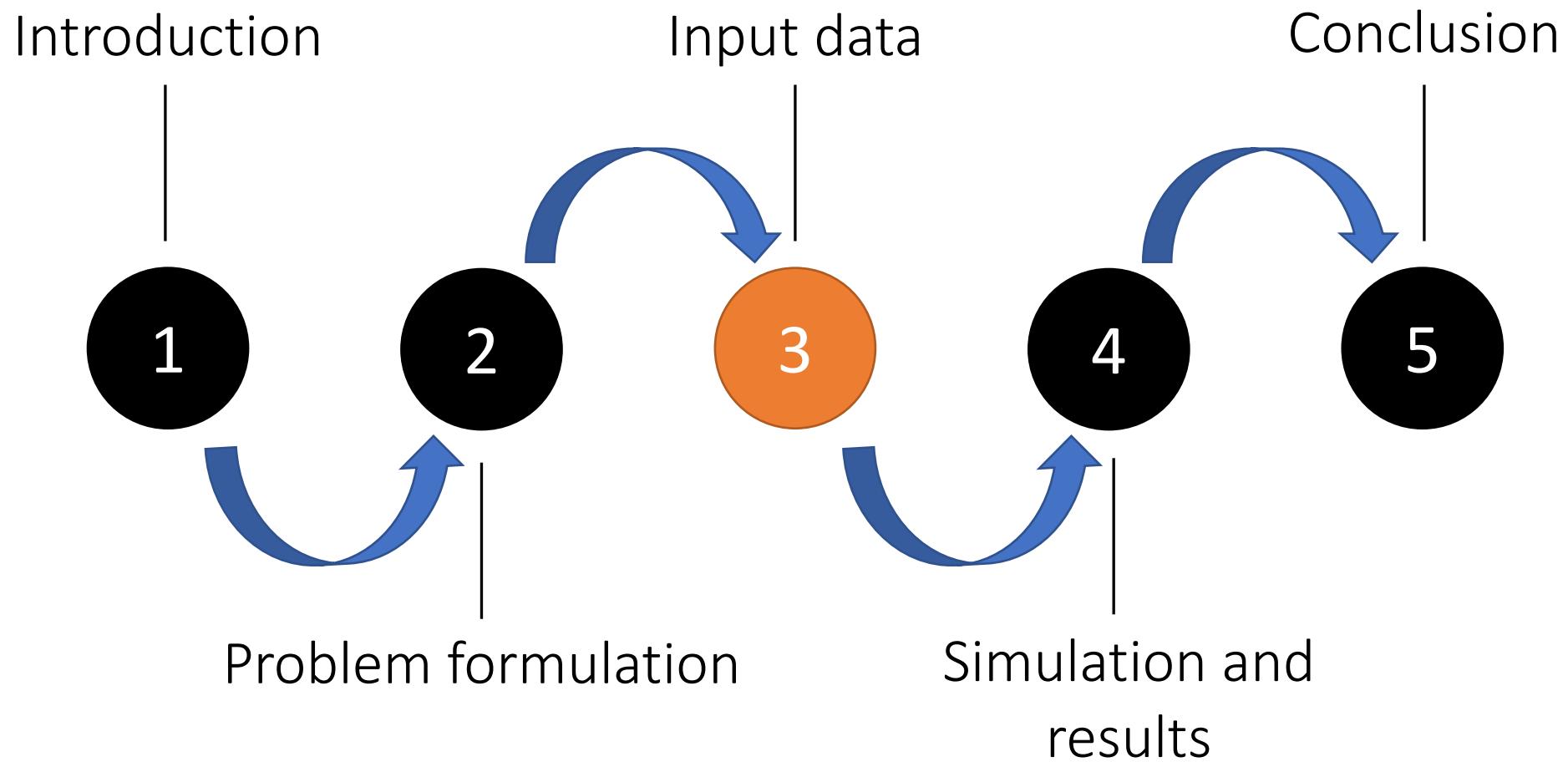
```

161 def twenty_one_rule(model, i, j, t):
162     return (model.MxAP[i,j,t] + model.POP[i,j,t]) * model.Comp[i,j,t] <= model.MP[i,j,t]
163 model.twenty_one = Constraint(model.I, model.J, model.T, rule=twenty_one_rule)
164
165 def twenty_two_rule(model, i, j, t):
166     return model.MnAP[i,j,t] <= model.POP[i,j,t] + model.MP[i,j,t]
167 model.twenty_two = Constraint(model.I, model.J, model.T, rule=twenty_two_rule)
168
169
170 def twenty_four_rule(model, i, j, t):
171     return model.MxAP[i,j,t] >= 0
172 model.twenty_four = Constraint(model.I, model.J, model.T, rule=twenty_four_rule)
173
174
175
176 def twenty_five_rule(model, i, j, t):
177     return model.MnAP[i,j,t] >= 0
178 model.twenty_five = Constraint(model.I, model.J, model.T, rule=twenty_five_rule)
179
180
181
182 def twenty_seven_rule(model, i, j, t):
183     return model.POP[i,j,t] >= -model.MP[i,j,t]
184 model.twenty_seven = Constraint(model.I, model.J, model.T, rule=twenty_seven_rule)
185
186
187
188 def twenty_eight_rule(model, i, j, t):
189     return model.Deg[i,j,t] >= 0
190 model.twenty_eight = Constraint(model.I, model.J, model.T, rule=twenty_eight_rule)
191
192
193 def twenty_nine_rule(model, i, j, t):
194     return model.Deg[i,j,t] >= model.DC[i] * (model.POP[i,j,t] - model.MnAP[i,j,t] * ExU
195                                         * model.Comp[i,j,t]/model.Ef[i])
196 model.twenty_nine = Constraint(model.I, model.J, model.T, rule=twenty_nine_rule)

```

Operational constraint	Description
$\left(\sum_{t=1}^{time} (E[FP_i(t)] \cdot Comp_i(t) + \rho_i(t)) \cdot Ef_i \right) \leq M_{Ci}$ $+ SOC_{I,i} - Trip_i(time)$ $\left(\sum_{t=1}^{time} (E[FP_i(t)] \cdot Comp_i(t) + \rho_i(t)) \cdot Ef_i \right) \geq 0$ $+ SOC_{I,i} - Trip_i(time)$ $\forall i, time$ $\left(\sum_{t=1}^T (E[FP_i(t)] \cdot Comp_i(t) + \rho_i(t)) \cdot Ef_i \right) \geq 0.99M_{Ci}$ $+ SOC_{I,i} - Trip_i(T)$	The energy level of the battery is bounded between 0 and its maximum capacity at every moment of the daily scheduling and it is set to be at least 99% of its maximum capacity at the end of the daily scheduling
$(MxAP_i(1) + POP_i(1)) \cdot Comp_i(1) \cdot Ef_i + SOC_{I,i} \leq M_{Ci}$ $\left((POP_i(1) - MnAP_i(1) - RSRP_i(1) + \rho_i(1)) \cdot Comp_i(1) \cdot Ef_i + SOC_{I,i} \right) \geq 0$	Conditions on the arrival times of the electric vehicles
$(MxAP_i(t) + POP_i(t)) \cdot Comp_i(t) \leq MP_i(t) \forall i$ $MnAP_i(t) \leq POP_i(t) + MP_i(t) \forall i$	Ancillary services capacities cannot exceed the admissible limits of the maximum possible power draw of the charger
$MxAP_i(t) \geq 0 \forall i$ $MnAP_i(t) \geq 0 \forall i$ $POP_i(t) \geq -MP_i(t) \forall i$ $Deg_i(t) \geq 0 \forall i$	Bounds of the decision variables
$Deg_i(t) \geq DC_i \cdot E[FP_i^-(t)] \cdot \frac{Comp_i(t)}{Ef_i} \forall i$	Condition on the degradation of the battery

Agenda



Driving profiles



Hypothetical group of **100** EVs



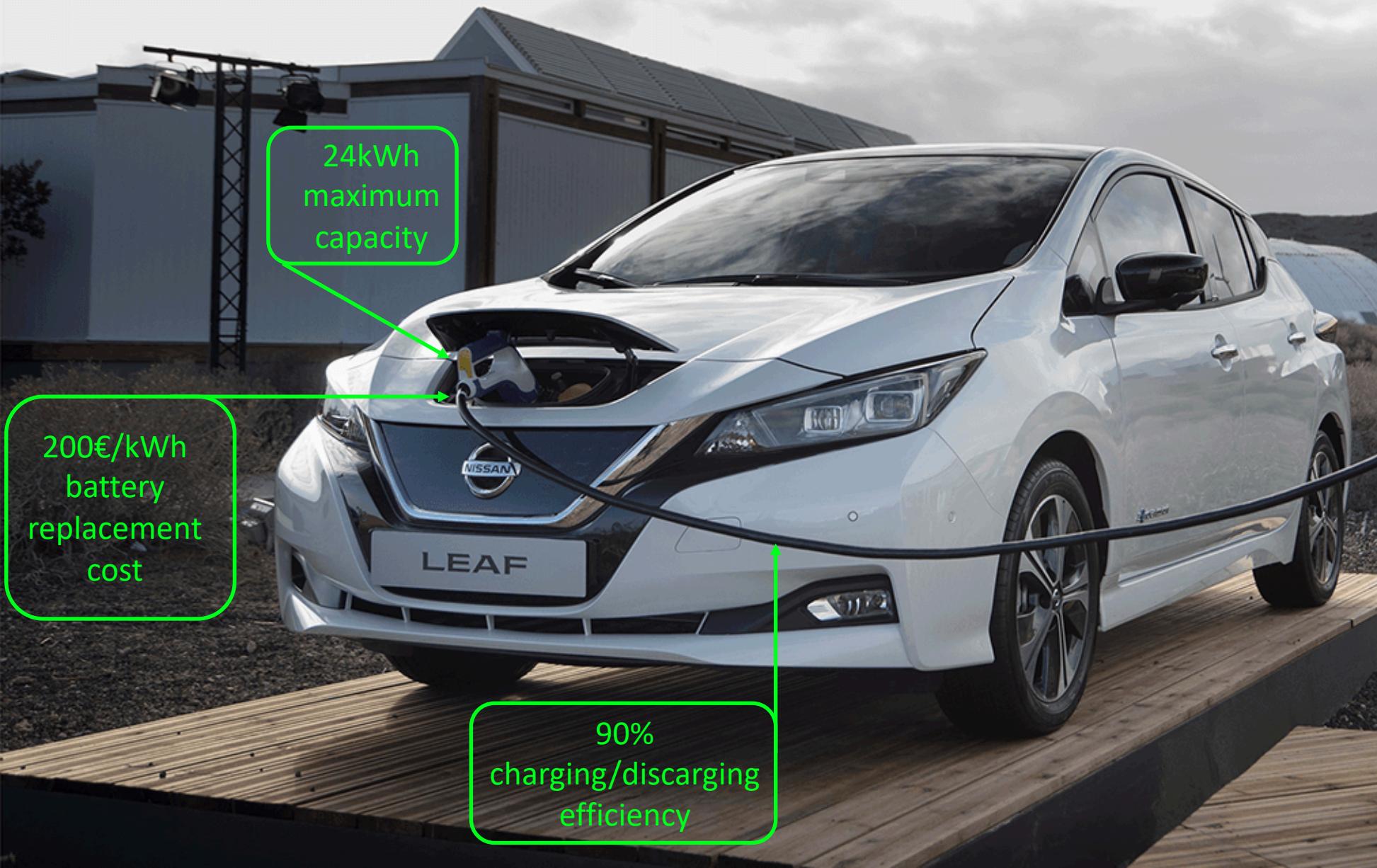
People arrive at work every morning between **6AM** and **9AM** and come back home every evening between **4PM** and **7PM**



Battery's SOC in the morning is **randomly generated**

	6AM	7AM	8AM	9AM	10AM	11AM	12AM	1PM	2PM	3PM	4PM	5PM	6PM	7PM
EV 1														
EV 2														
EV 3														
⋮														
EV 100														

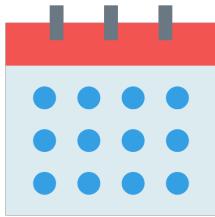
EV's and chargers' technical specifications



Price signals



Ancillary services and
electricity prices found in
Terna public archives and
GME repository



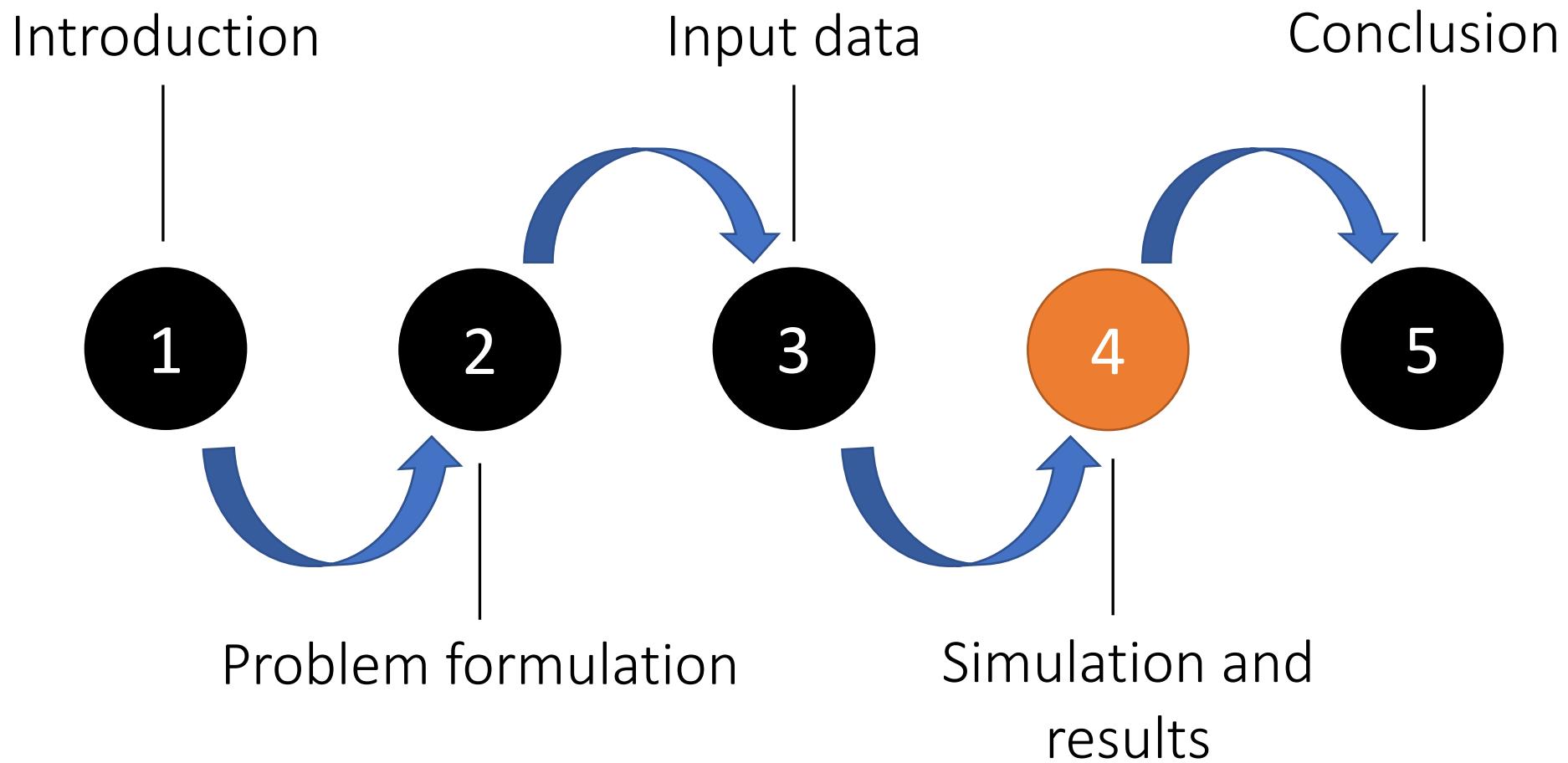
Simulation period of **three months**, from
August 2019 to October 2019



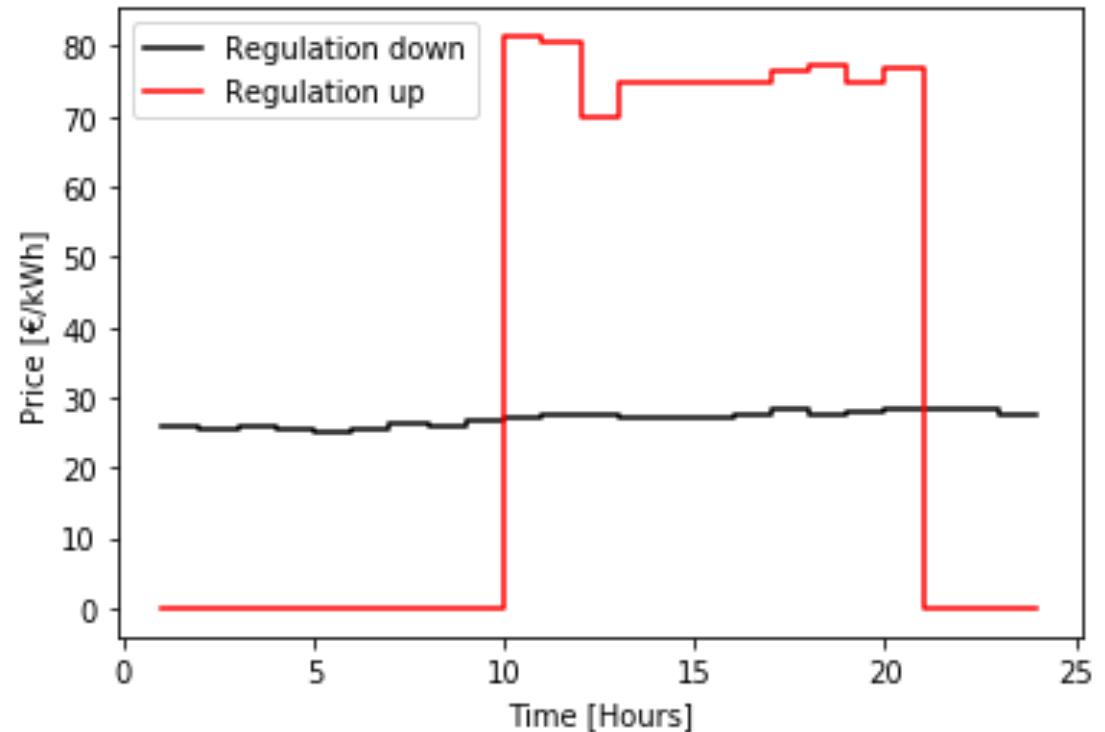
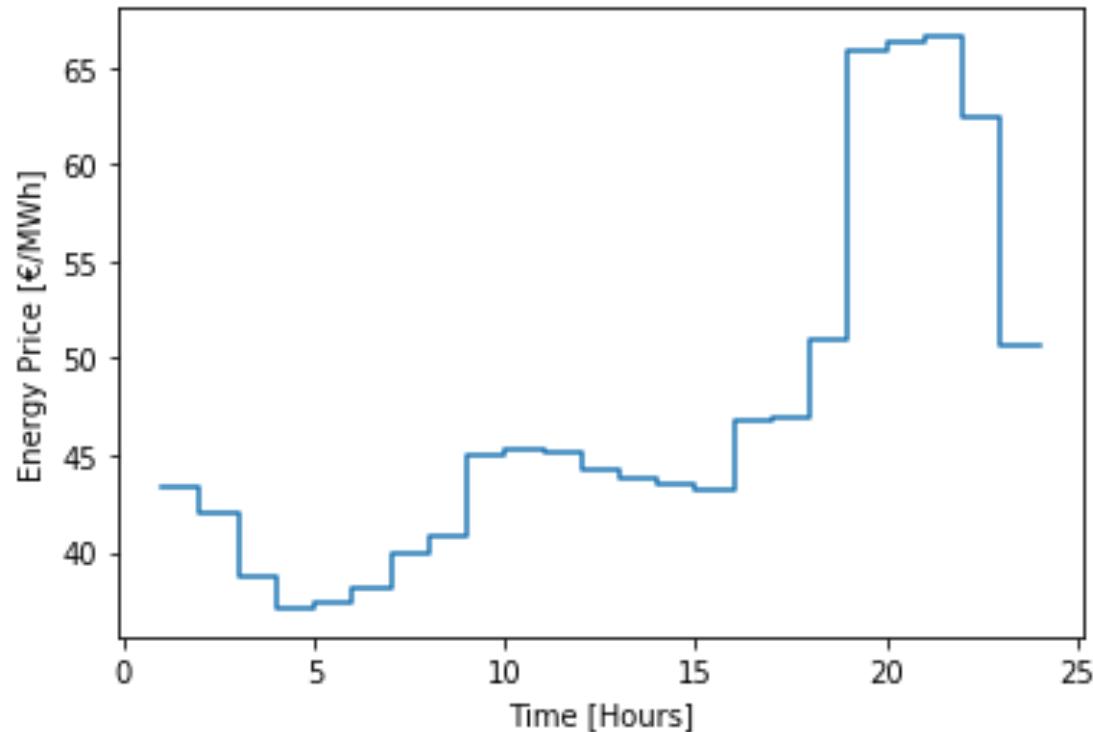
Aggregator rate of energy
charged to the consumer has
fixed at **€0.01/kWh**



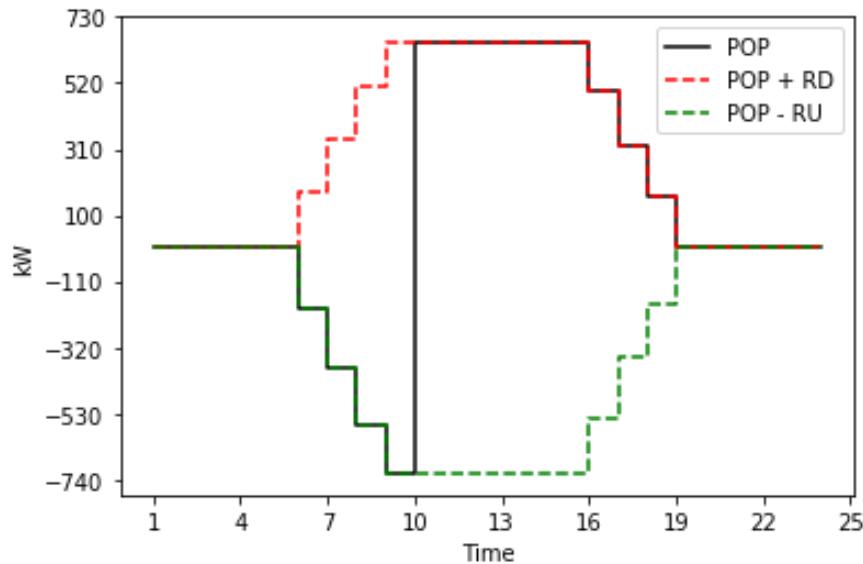
Agenda



Energy and Ancillary Services Prices

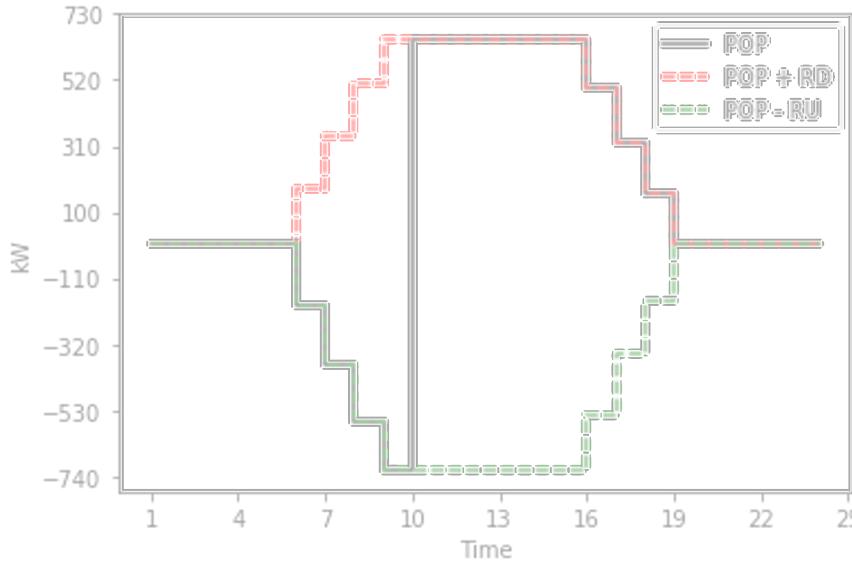


V2G and Smart Charging algorithms



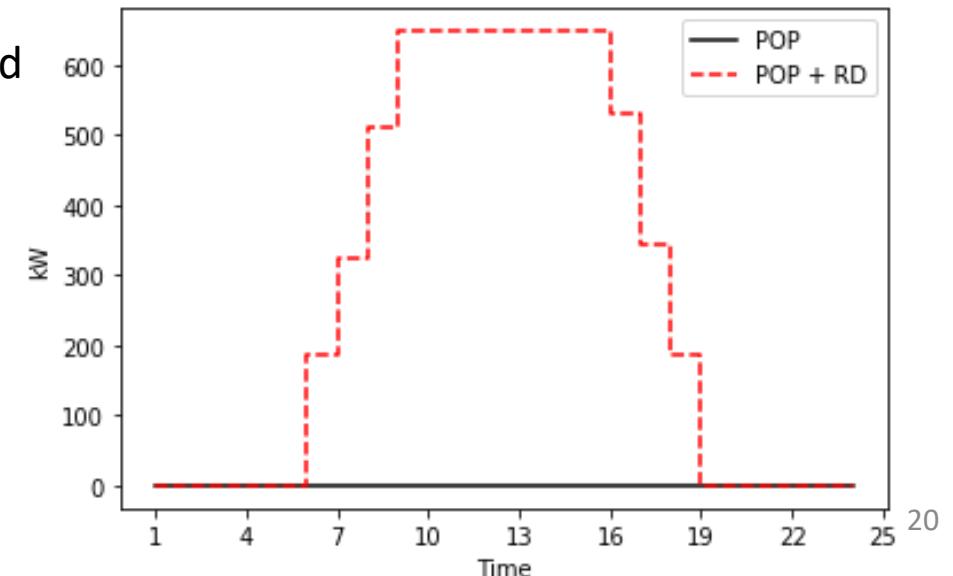
- Vehicle discharge until **10AM** and charge during the second part of the day
- Charging process always happens at the **maximum** of his capability
- The variables stay at zero **before the arrival** of the EVs and **after their departure**

V2G and Smart Charging algorithms

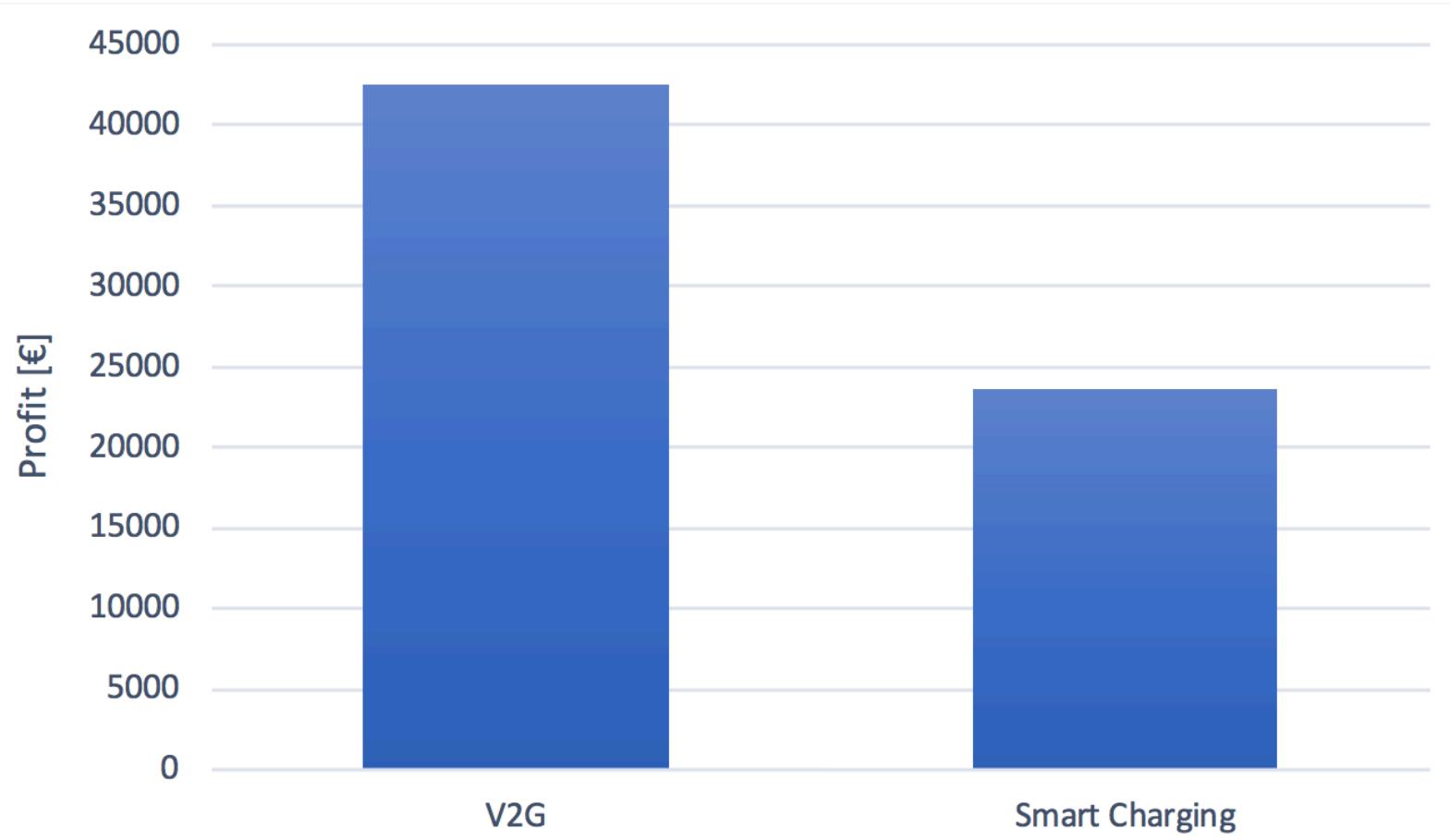


- Vehicle discharge until **10AM** and charge during the second part of the day
- Charging process always happens at the **maximum of his capability**
- The variables stay at zero **before the arrival of the EVs and after their departure**

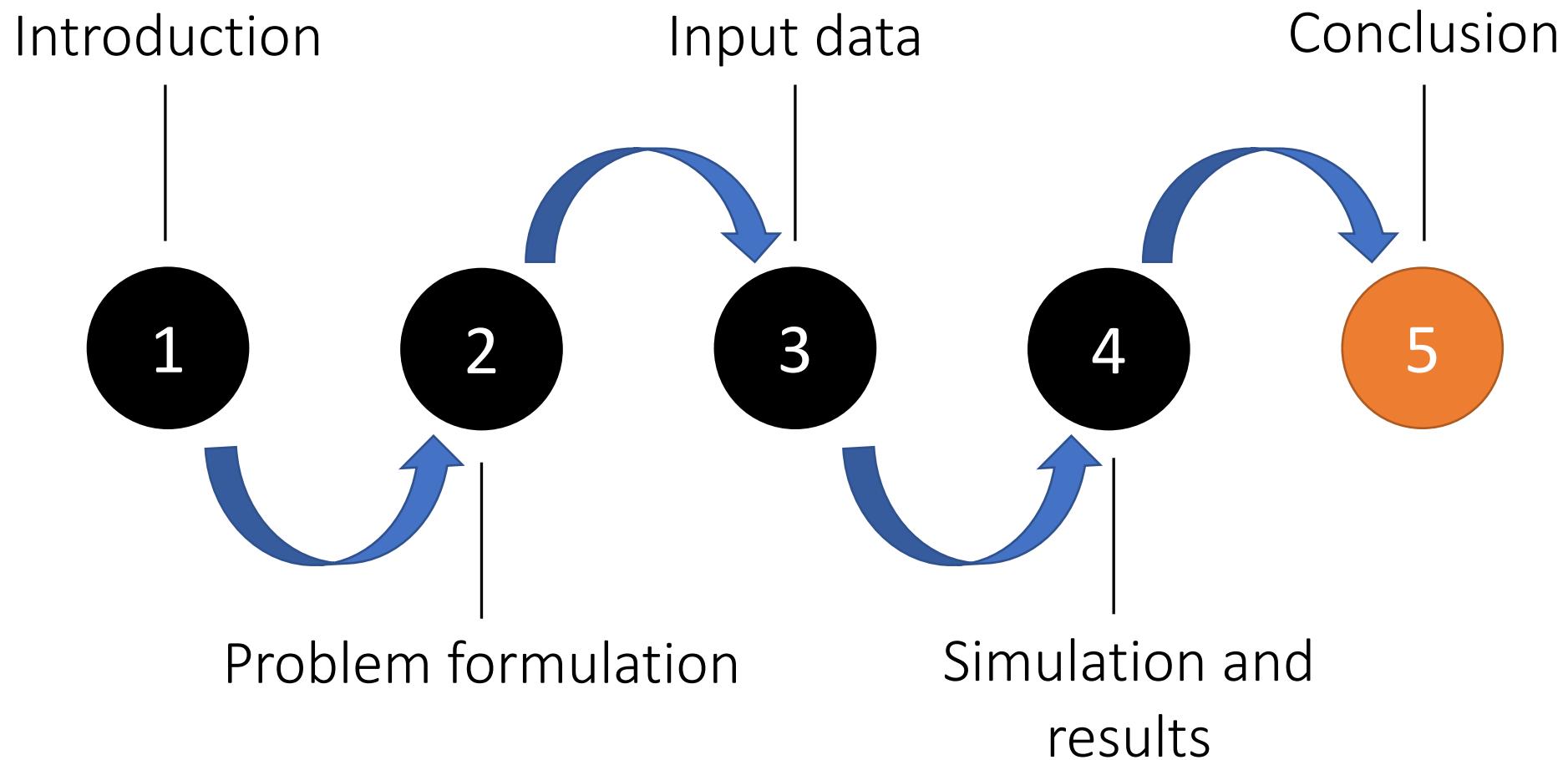
- Decision variables related to **regulation up** (and its prices) and **degradation of the battery** are not taken into account
- Charging of the fleet **doesn't need to be altered** during that day
- Capacity of regulation down **increases** as people arrive to connect their vehicles.



Profits comparison



Agenda

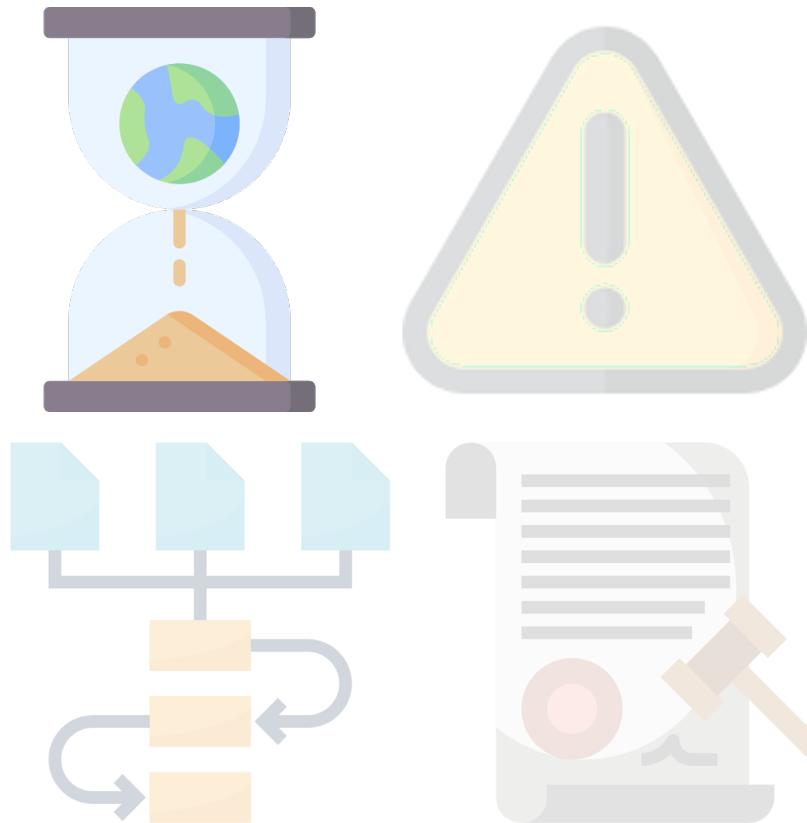


Conclusion



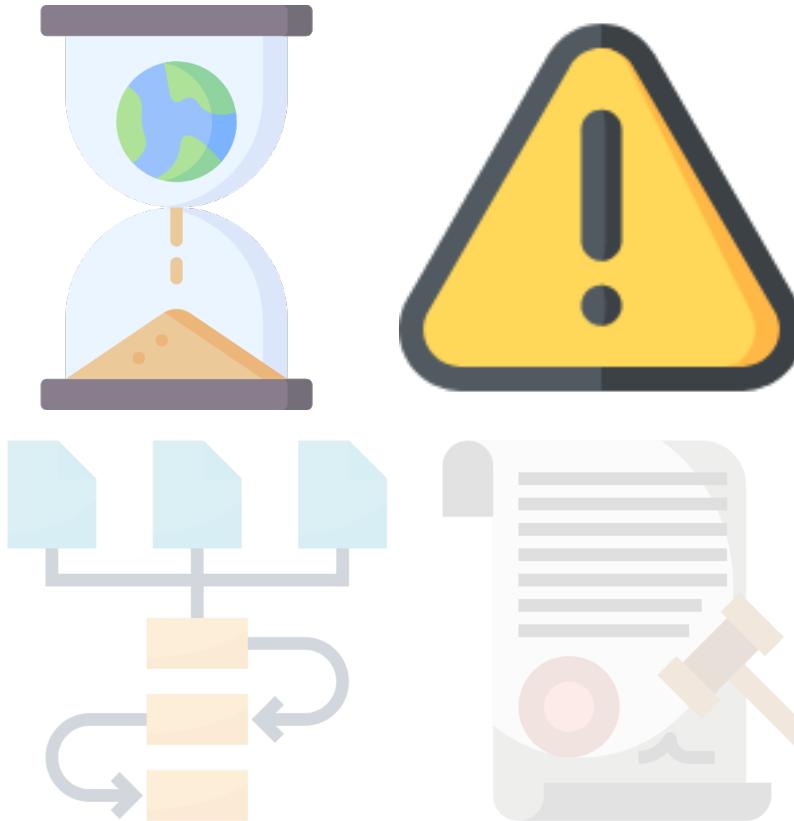
Conclusion

**EXPONENTIAL
EXECUTION TIME**



Conclusion

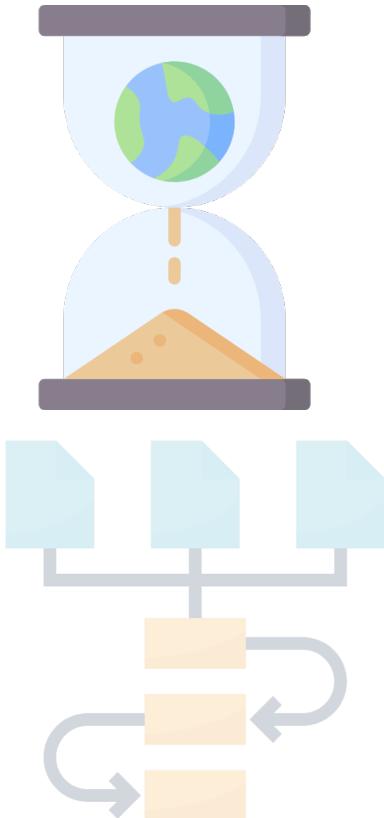
**EXPONENTIAL
EXECUTION TIME**



**PROBLEMS WITH THE
SMART CHARGING
OPTIMIZATION**

Conclusion

**EXPONENTIAL
EXECUTION TIME**



**PROBLEMS WITH THE
SMART CHARGING
OPTIMIZATION**

**ELECTRICITY MARKET
NEEDS TO BE MODELED
PROPERLY**

Conclusion



THANK YOU!

Q&A



References

- Eric Sortomme and Mohamed A. El-Sharkawi, *Optimal Scheduling of Vehicle-to-Grid Energy and Ancillary Services*, IEEE Transactions on smart grid, VOL. 3, NO. 1, (2012)