

Machine Learning for Modelling: *Supervised Learning*

Simone Bianco

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SIFT – Scale Invariant Feature Transform

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Object Recognition

Classes of objects

Class 1: cars



Class 2: animals



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Object Recognition

Object instances

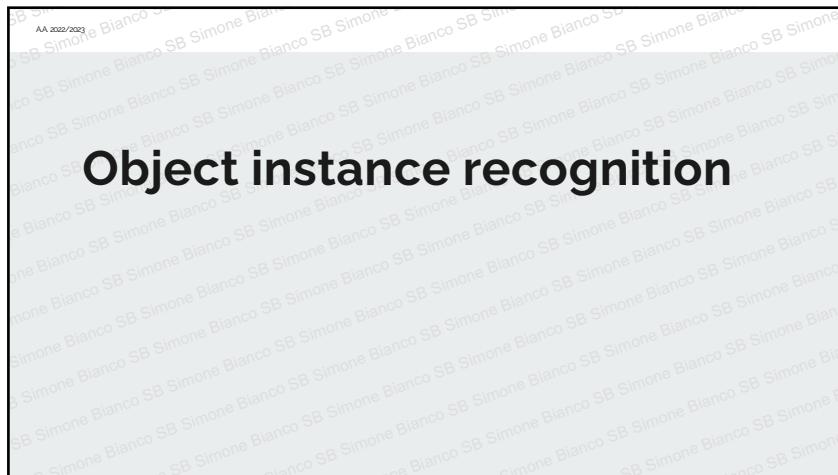
Instance 1: Tesla Model S



Instance 2: Book «The Martian» by Andy Weir



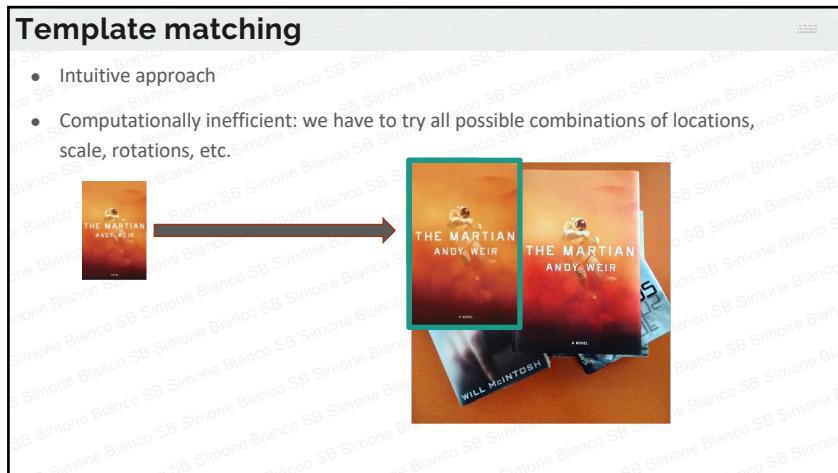
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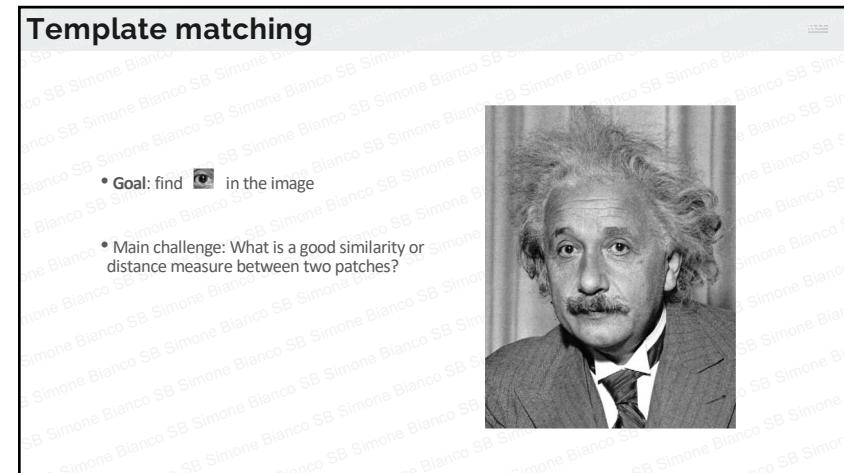
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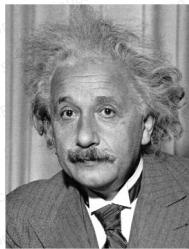
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Matching with filters

Goal: find  in image

Method: SSD (Sum of Squared Differences)

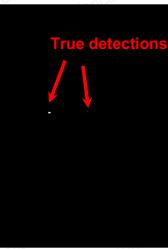
$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k, n+l])^2$$



Input



1- sqrt(SSD)



True detections

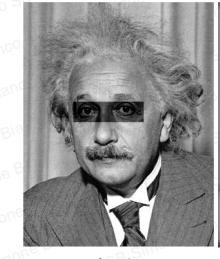
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Matching with filters

Goal: find  in image

Method: SSD (Sum of Squared Differences)

$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k, n+l])^2$$



Input



1- sqrt(SSD)

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Matching with filters

Goal: find  in image

Method : Normalized cross-correlation

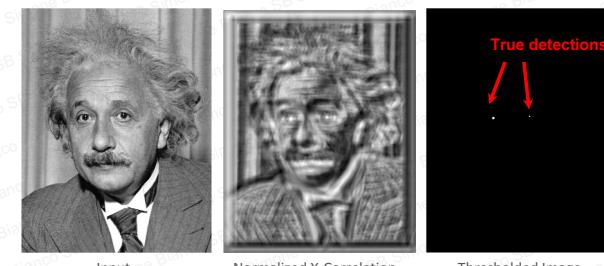
$$h[m,n] = \frac{\sum_{k,l} (g[k,l] - \bar{g}) f[m-k, n-l] - \bar{f}_{m,n})}{\left(\sum_{k,l} (g[k,l] - \bar{g})^2 \sum_{k,l} (f[m-k, n-l] - \bar{f}_{m,n})^2 \right)^{0.5}}$$

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Matching with filters

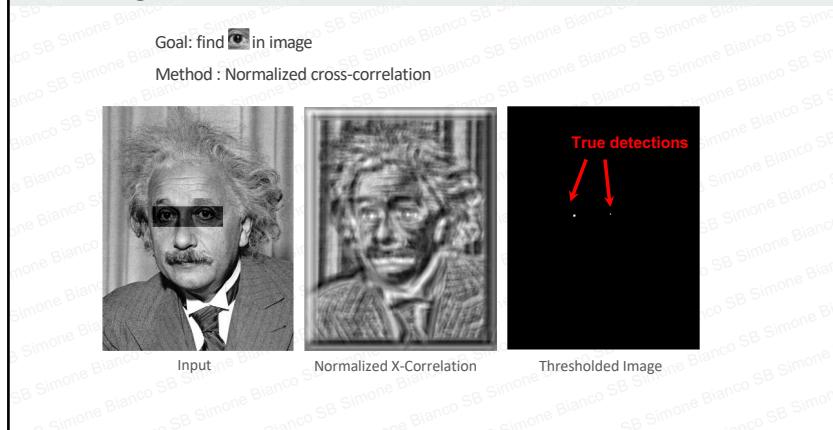
Goal: find  in image

Method : Normalized cross-correlation



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Matching with filters



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Matching with filters

Q: What is the best method to use?

SSD

- Faster
- Sensitive to overall intensity

Normalized cross-correlation

- Slower
- Invariant to local average intensity
- Invariant to local contrast

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Template matching – Sliding window

Example



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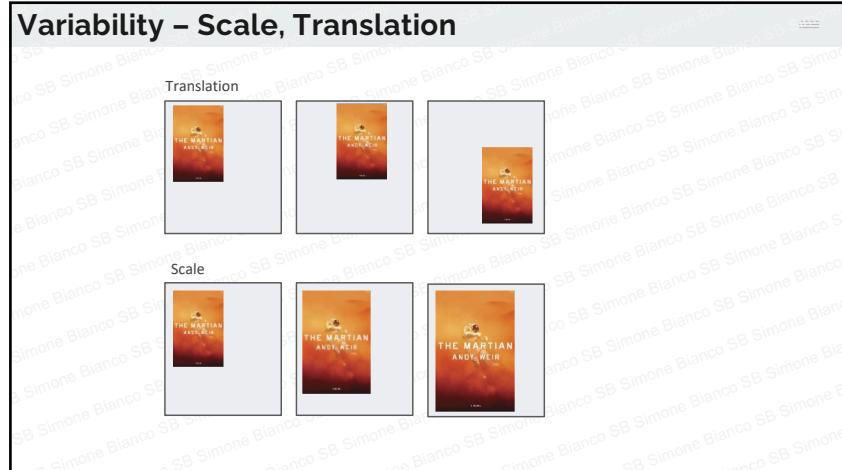
Template matching – Sliding window

Example



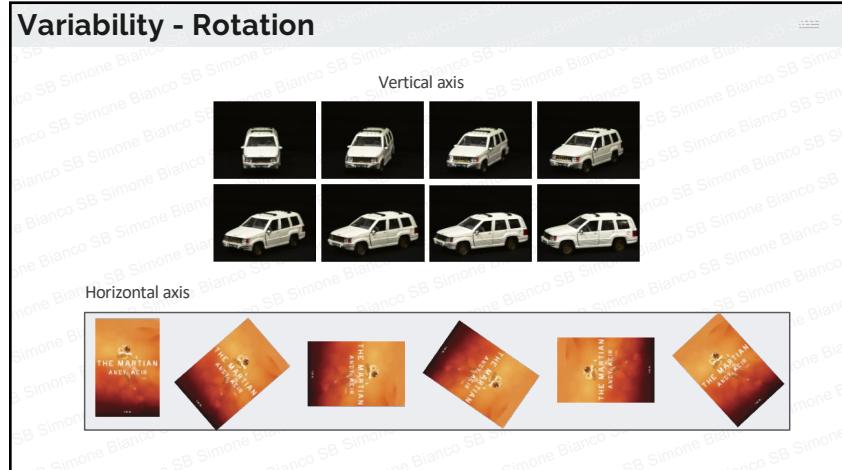
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Variability – Scale, Translation



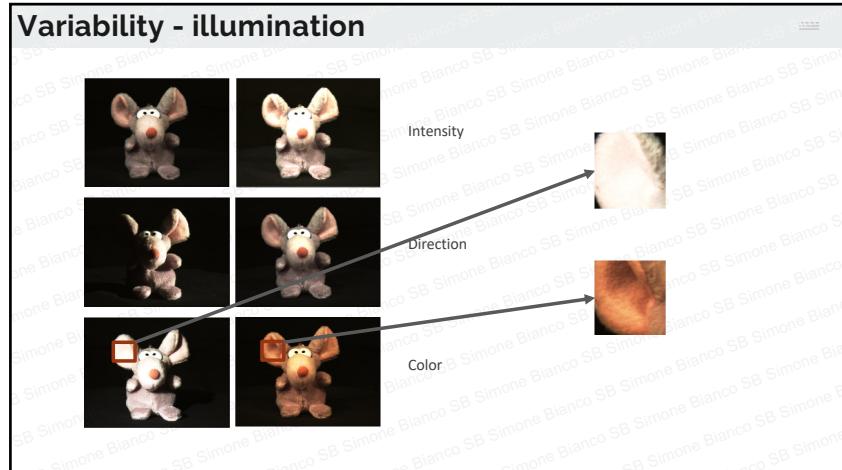
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Variability - Rotation



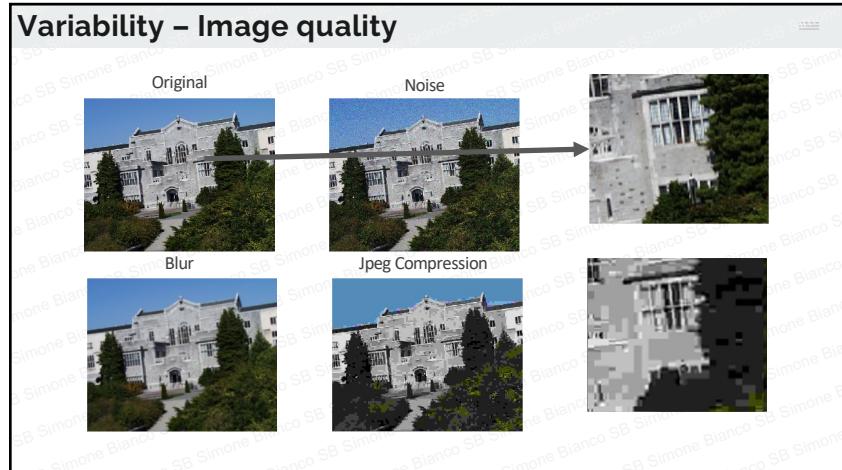
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Variability - illumination



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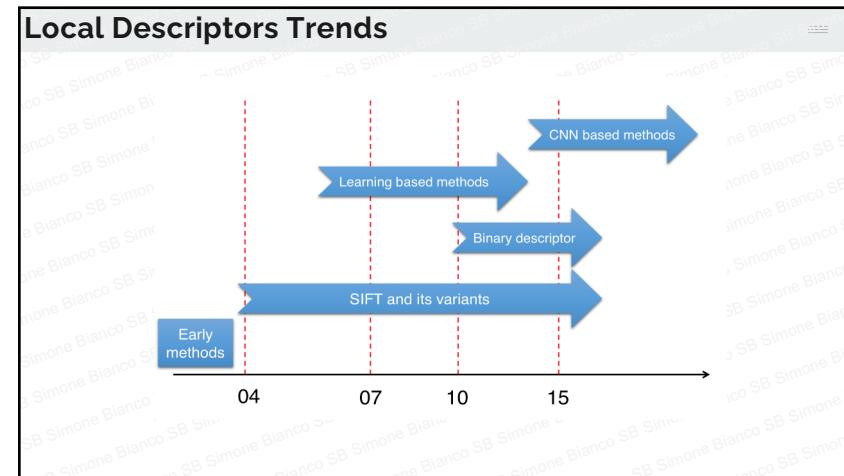
Variability – Image quality



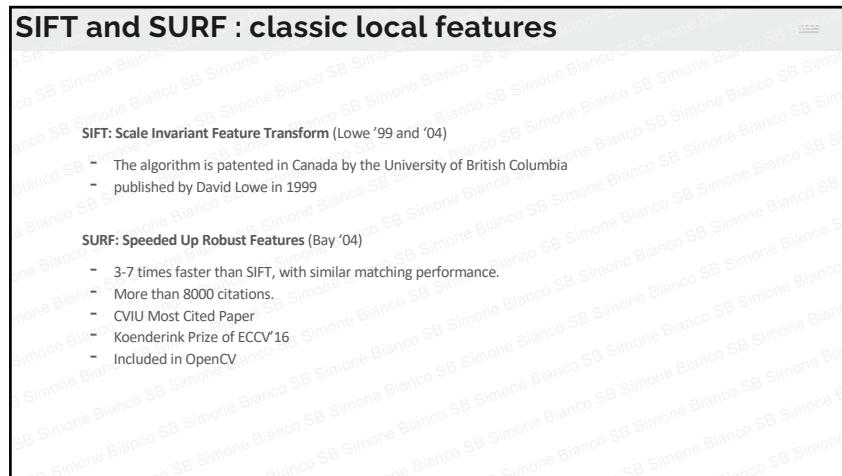
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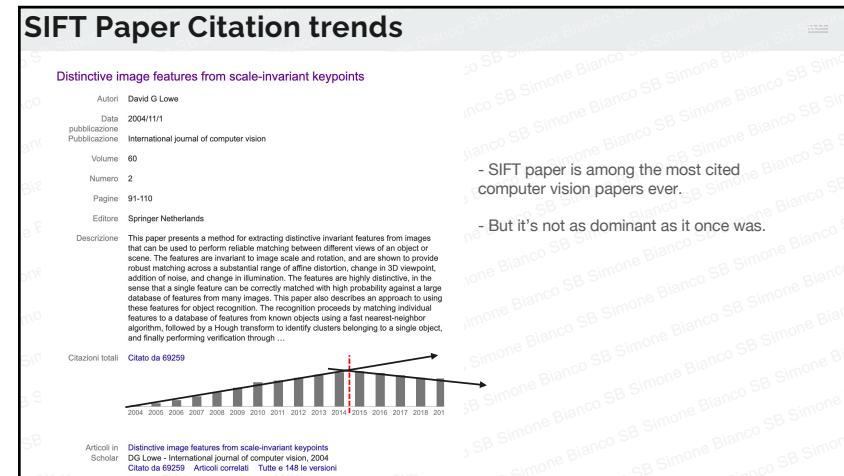
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Why Keypoints-based methods?

Keypoints Remain Relevant

- When accurate geometric recovery matters, they remain unequalled.
- They are efficient for real-time applications.
- They provide an effective way
 - to compress the information present in large images,
 - to recognize specific locations.
- The algorithms do not need to be retrained for each new application.

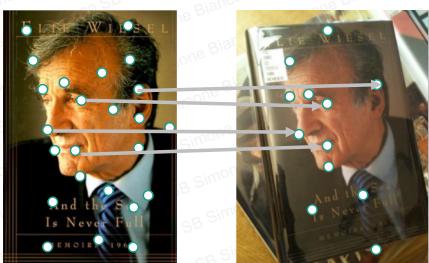
Future algorithms will combine Deep Learning and keypoint matching.

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Keypoints-Based Approaches

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Keypoints-based approaches



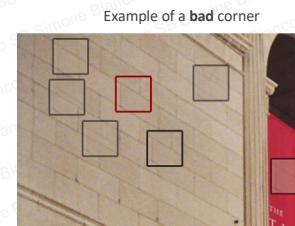
Steps

- Keypoint detection
- Keypoint description
- Matching of similar keypoints
- Similarity score based on matching points
- Use of Interest points (keypoints)
- Do not need to try all the combinations of transformations.

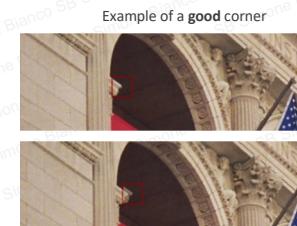
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Harris Corner Detector

- Corners are better than edges!
- How to define a corner?
- Harris et al. [1] → Patches that generate a large variation when moved around



Example of a **bad** corner



Example of a **good** corner

[1] Harris, Chris, and Mike Stephens. "A combined corner and edge detector." Alvey vision conference. Vol. 15. 1988.

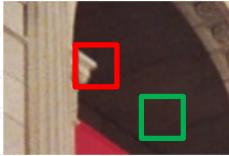
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Harris Corner Detector

Patches that generate a large variation when moved around

$$E(u, v) = \sum_{x,y} w(x, y)[I(x+u, y+v) - I(x, y)]^2$$

- E is the difference between the original and the moved window.
- u is the window's displacement in the x direction
- v is the window's displacement in the y direction
- w(x, y) is the window at position (x, y). This acts like a mask. Ensuring that only the desired window is used.
- I(x, y) is the intensity of the image at a position (x, y)
- I(x+u, y+v) is the intensity of the moved window
- I(x, y) is the intensity of the original window



[1] Harris, Chris, and Mike Stephens. "A combined corner and edge detector." Alvey vision conference. Vol. 15. 1988.

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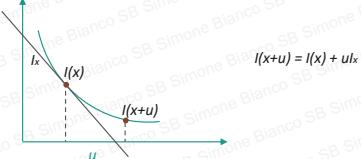
Harris Corner Detector

$$E(u, v) = \sum_{x,y} w(x, y)[I(x+u, y+v) - I(x, y)]^2 \quad \text{Patches that generate a large variation when moved around}$$

$$\sum_{x,y} [I(x+u, y+v) - I(x, y)]^2 \quad \text{Leave out the weights (for simplification)}$$

$$E(u, v) \approx \sum_{x,y} [I(x, y) + uI_x + vI_y - I(x, y)]^2 \quad \text{Can be approximated with the first Taylor expansion}$$

Math hints (derivative):



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Harris Corner Detector

$$E(u, v) = \sum_{x,y} w(x, y)[I(x+u, y+v) - I(x, y)]^2 \quad \text{Patches that generate a large variation when moved around}$$

$$\sum_{x,y} [I(x+u, y+v) - I(x, y)]^2 \quad \text{Leave out the weights (for simplification)}$$

$$E(u, v) \approx \sum_{x,y} [I(x, y) + uI_x + vI_y - I(x, y)]^2 \quad \text{Can be approximated with the first Taylor expansion}$$

$$E(u, v) \approx \sum_{x,y} u^2 I_x^2 + 2uv I_x I_y + v^2 I_y^2 \quad \text{Square expansion}$$

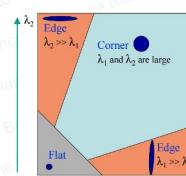
$$E(u, v) \approx [u \ v] \begin{pmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix} \quad \text{Conversion into a matrix}$$

$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \quad E(u, v) \approx [u \ v] M \begin{bmatrix} u \\ v \end{bmatrix} \quad \text{Another way to write it}$$

Harris Corner Detector

$$M = \sum_{x,y} w(x, y) \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \quad \text{M matrix (see slides before)}$$

Eigenvalues of the matrix can help determine the suitability of a window:



$$R = \det M - k(\text{trace } M)^2 \quad \text{All windows that have a score R greater than a certain value are corners.}$$

$$\det M = \lambda_1 \lambda_2 \quad \lambda_1, \lambda_2 \text{ are the eigenvalues}$$

[1] Images credits: <http://alshack.in/tutorials/harris-corner-detector/> very good website with lot of didactic material

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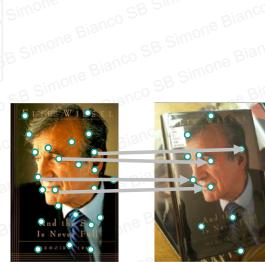
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SIFT

- SIFT [1] (Scale Invariant Features Transform)
- Author: David Lowe. University of British Columbia –Canada

Main difference with Harris detector:

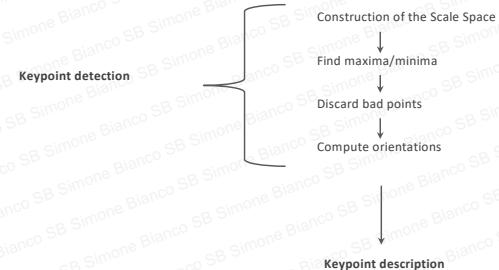
- Not only a Keypoint Detector but also a **Keypoint Descriptor**
- Robust to:
 - Scale
 - Rotation
 - Illumination
 - Viewpoint



[1] David G. Lowe, "Distinctive image features from scale-invariant keypoints," International Journal of Computer Vision, 60, 2 (2004), pp. 91-110.

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Keypoint detection – Processing steps



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Scale Space



◦ Needed to obtain **Scale Invariance**

- Higher scales = higher blur
- Higher blur = less details

Increasing blur
Increasing scale

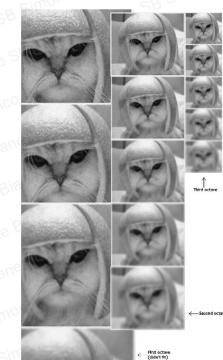
Blurred image Gaussian blur operator Original Image

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

scale parameter: higher value higher blur

$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2}$$

Scale Space - Octaves



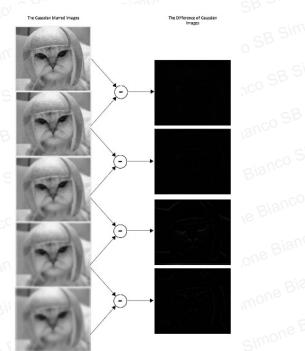
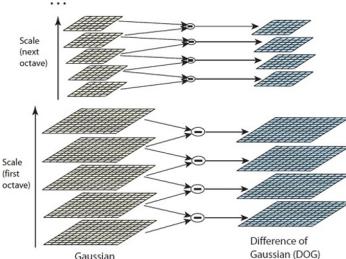
- **Scales and Octaves**
- Usually 4 octaves and 5 blur levels
- Reduces computations

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Difference Of Gaussians

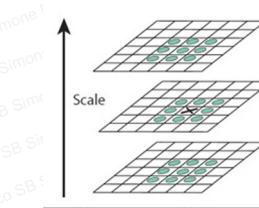
- Used to detect edges and corners
- Laplacian of Gaussian (LoG) approximation
- Very fast and efficient (only subtraction)



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Locate maxima/minima in DoG images

- X is the current pixel
- Green circles are the considered neighbours
- $26 (=9+8+8)$ checks.
- X is a **keypoint** if it is the greatest of all its neighbours
- Usually there is no need to check all the neighbours.
Discard happens after few checks.



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Refinements

- To be removed
 - Low Contrast Points
 - Check for the value of pixel in the DoG image
 - If value is under threshold the point is rejected
 - Edges
 - Compute gradients in the two directions.
 - Gradient in one direction is just a difference of pixel values

Flat region	Edge	Corner
Small ↔ Small	Big ↔ Small	Big ↔ Big
Abs difference $41 - 40 = 1$	$42 - 41 = 1$	

Searching for this!

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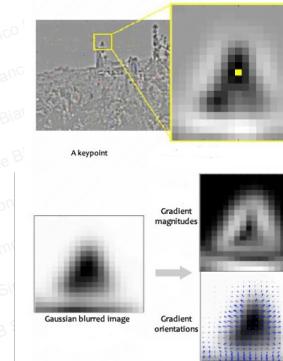
Keypoint Orientation

Goal: achieve rotation invariance

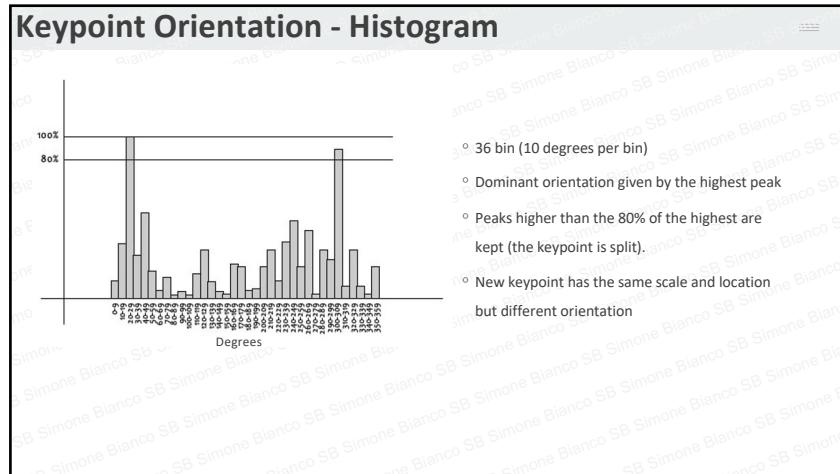
- Histogram of Orientations
- Weighted by Gradient magnitudes

Gradient magnitude: $m(x, y) = \sqrt{(L(x+1, y) - L(x-1, y))^2 + (L(x, y+1) - L(x, y-1))^2}$

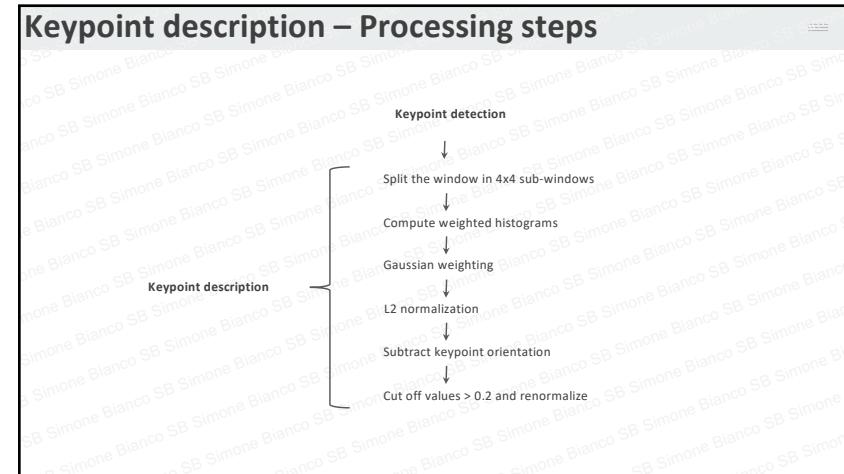
Gradient orientation: $\theta(x, y) = \tan^{-1}((L(x, y+1) - L(x, y-1)) / (L(x+1, y) - L(x-1, y)))$



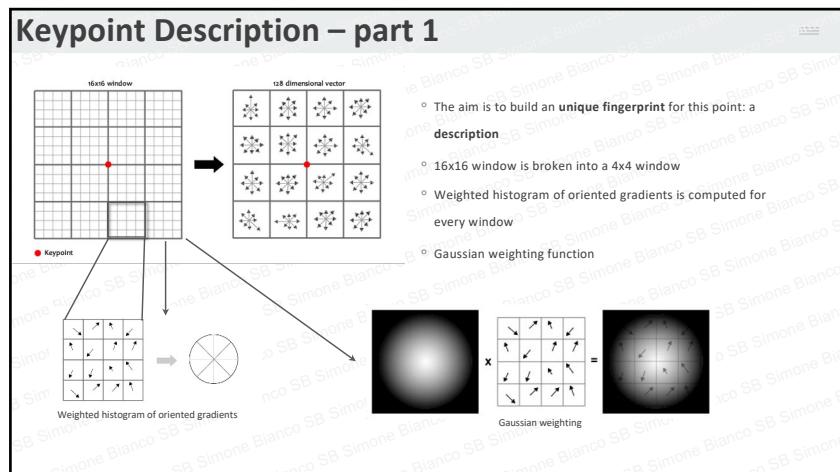
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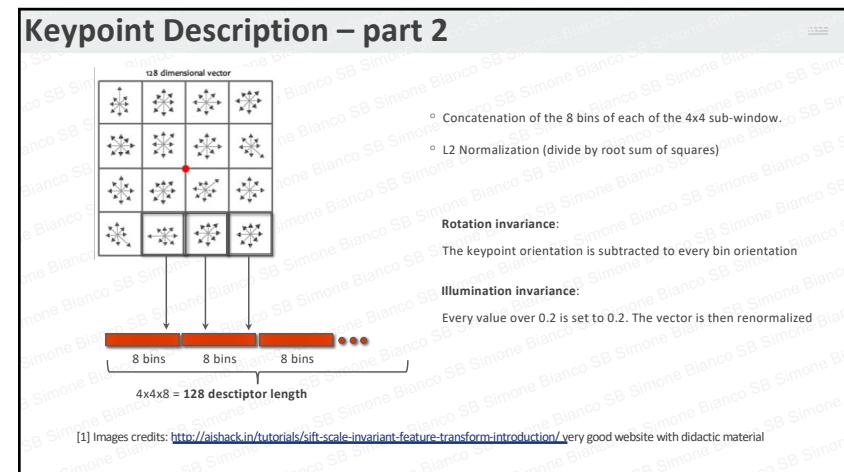
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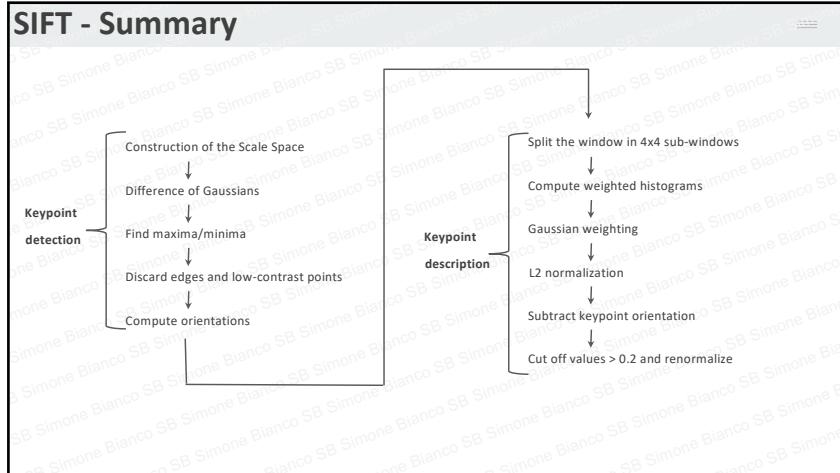


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SIFT - Summary



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List of keypoint detectors/descriptors

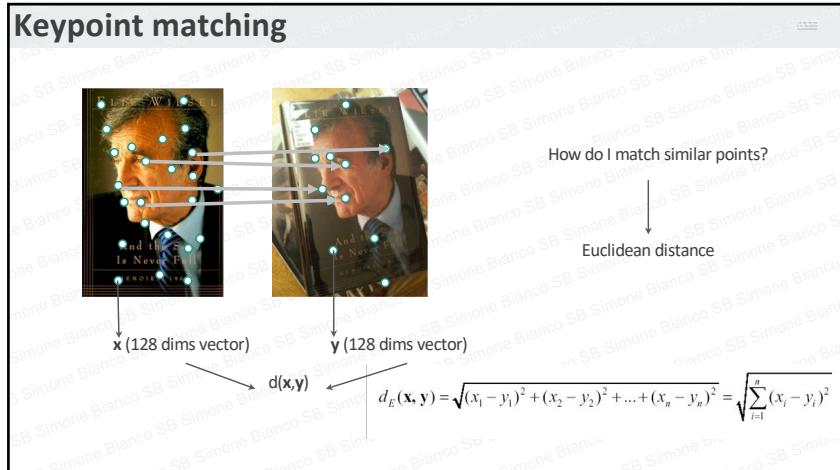
SIFT implementations		
Detector	Descriptor	Dimensionality
SIFT Lowe (SIFT 1999)	SIFT Lowe	128
SIFT OpenCV	SIFT OpenCV	128
SIFT VLFeat (Vedaldi 2010)	SIFT VLFeat	128

Affine Invariant Detectors		
Detector	Descriptor	Dimensionality
DoG	SIFT	128
Multiscale-Harris	SIFT	128
Harris-Laplace	SIFT	128
Hessian	SIFT	128
Multiscale-Hessian	SIFT	128
Hessian-Laplace	SIFT	128

Others		
Detector	Descriptor	Dimensionality
SURF	SURF (Bay 2006)	64
SURF	FREAK (Alahi 2012)	64
Kaze	Kaze (Alcantarilla 2012)	64

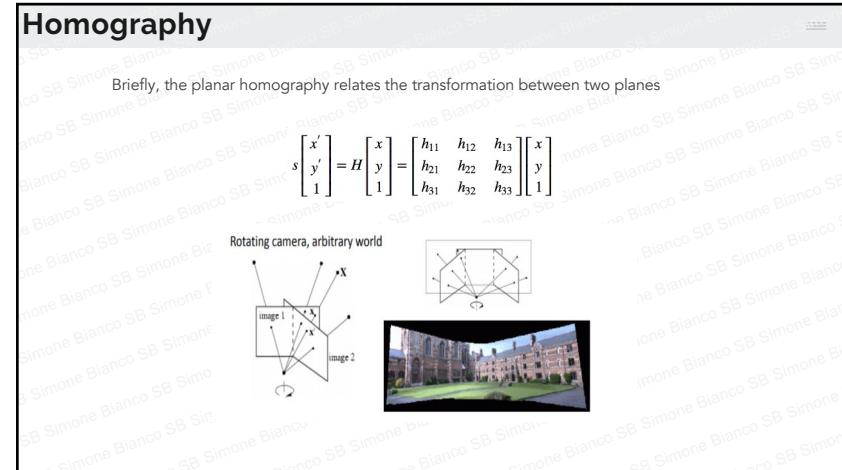
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Keypoint matching



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Homography



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RANSAC



RANSAC – RANDOM SAmple Consensus
Used to discard false matches

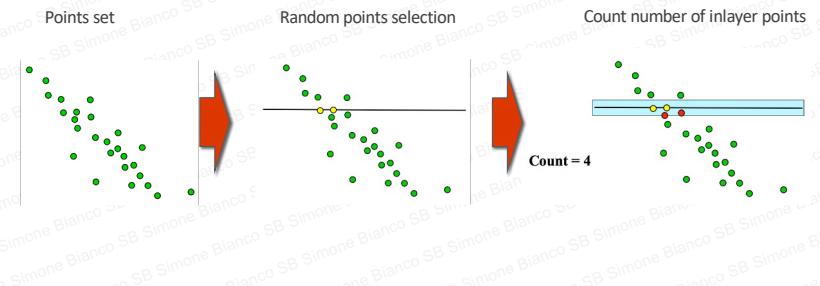
Algorithm outline:

1. Select at least four feature pairs (at random)
 2. Compute homography H (exact)
 3. Compute inliers where $SSD(p', Hp) < \epsilon$
 4. Keep largest set of inliers
 5. Re-compute least-squares H estimate on all of the inliers
- } Iterate multiple times

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RANSAC

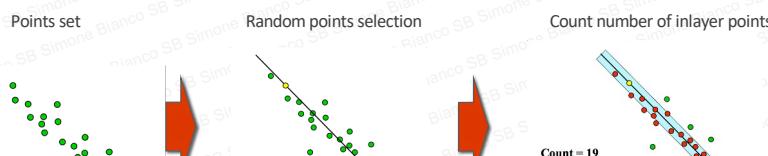
First iteration



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RANSAC

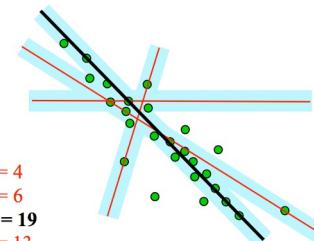
Second iteration



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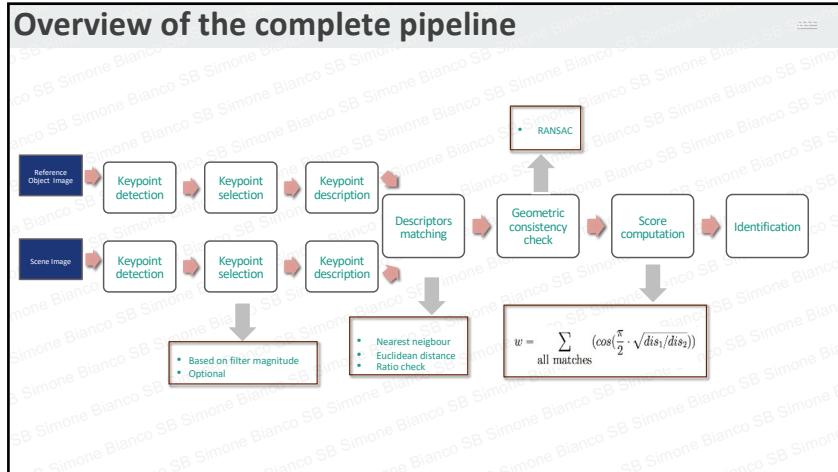
RANSAC

- Choose the model with the highest number of inliers.
- Simple example with lines.
- The same algorithm is used with more complex models (e.g. to handle affine transformations).
- Robust even if the majority of points are outliers



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Overview of the complete pipeline



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Identification

Example formula used to check the correspondence:

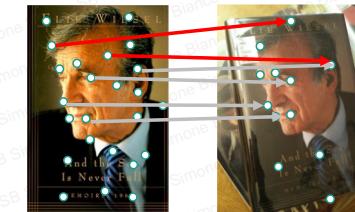
$$w = \sum_{all\ matches} (\cos(\frac{\pi}{2} \cdot \sqrt{dis_1/dis_2}))$$

All correct matches Distance from the nearest and second nearest.

To verify how strong the matching is.

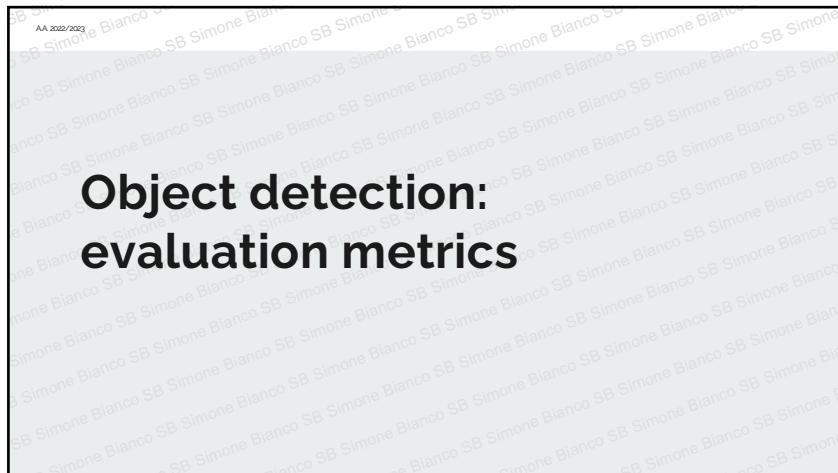
Final score

- To be thresholded
- If w is over the threshold the two images contain the same object



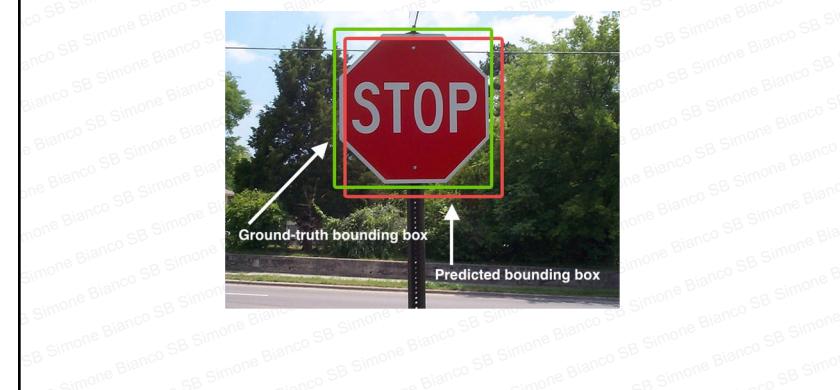
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Object detection: evaluation metrics



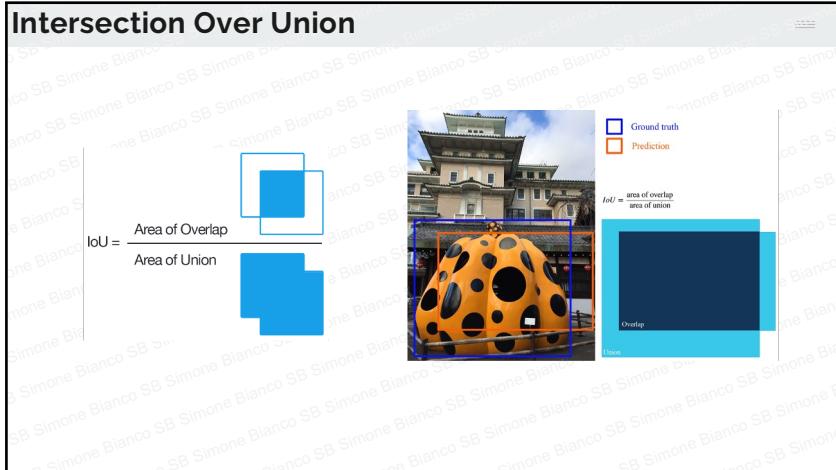
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Intersection Over Union



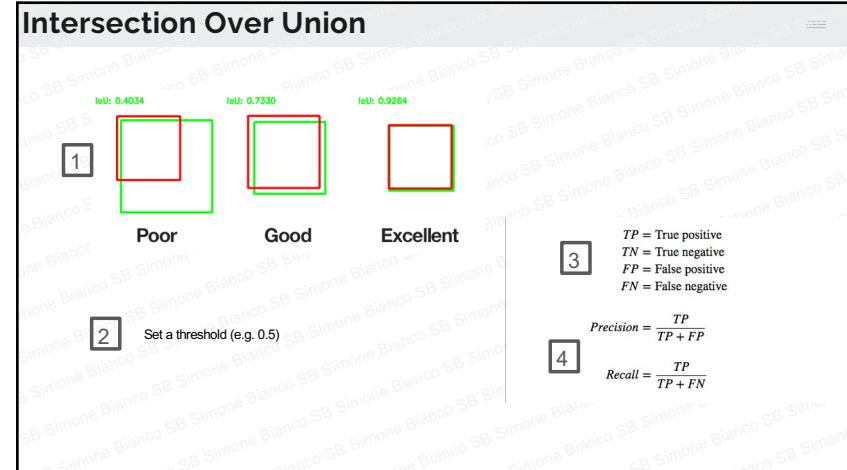
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Intersection Over Union



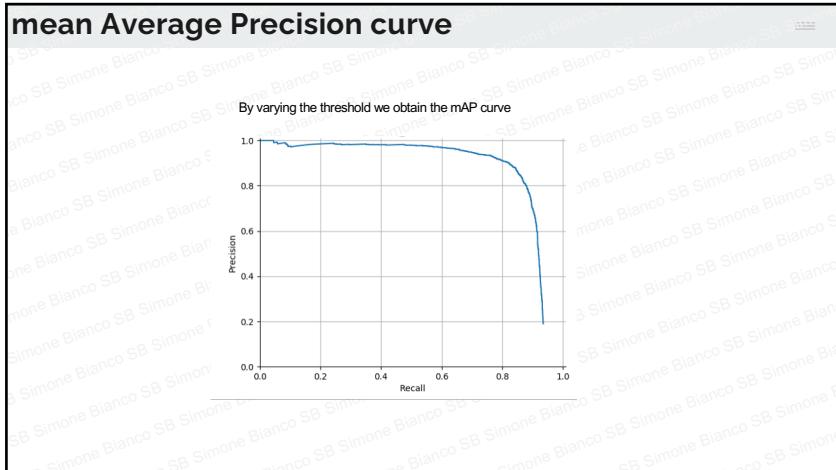
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Intersection Over Union



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mean Average Precision curve

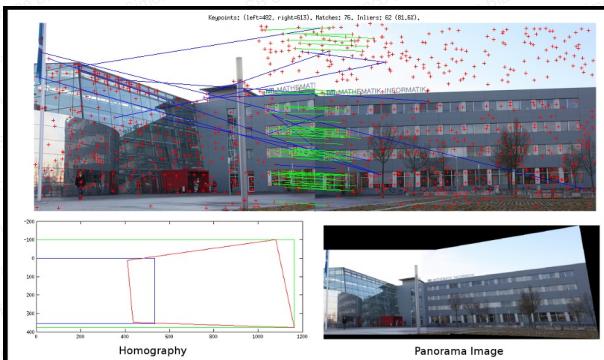


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Applications

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Applications – Panorama Stitching



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Applications – Panorama Stitching



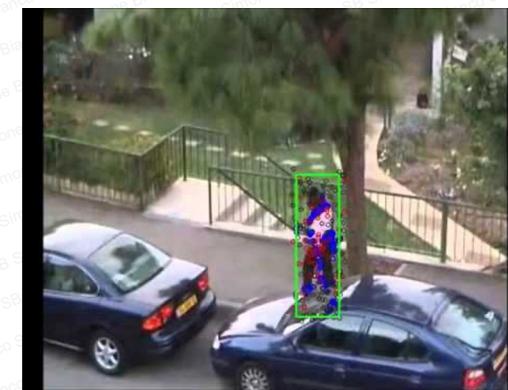
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Applications – Video Stabilization



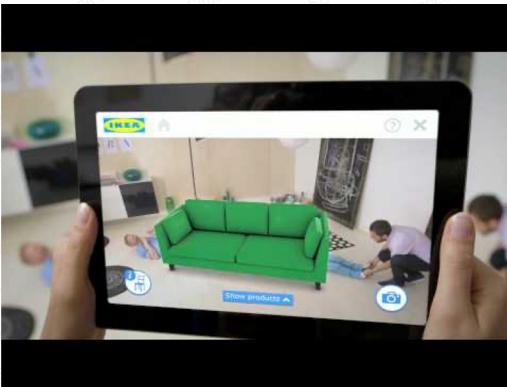
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Applications – Tracking



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Applications – Augmented reality - IKEA

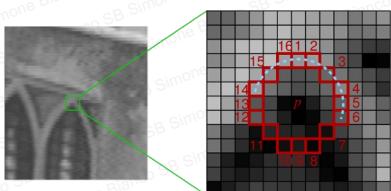


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Variation on the theme

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FAST – another keypoint detector



- FAST – Features from accelerated segment test
- For every pixel check the value of the neighbors
- If the value of at least N neighbors is less than the value of the center pixel, this is a corner

Tips for faster computation:

- First compare values of pixels 1,5,9,13
- At least 3 of these pixel values must be under the value of the central pixel
- If not the keypoint candidate is discarded
- Else everyone of the 16 neighbors is checked

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Dense SIFT

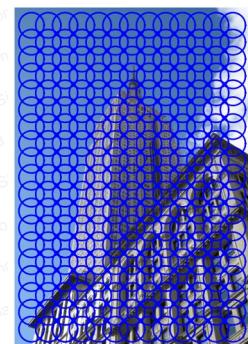
- Instead of computing keypoints use a fixed grid
- Every point in the fixed grid is described using the SIFT descriptor

PRO:

- Faster to compute (no keypoint detection)
- Can work with smooth surfaces (few corners)

CONS:

- Corners are usually more distinctive (reliable)
- Slower keypoint comparison (usually a lot more points to be compared)



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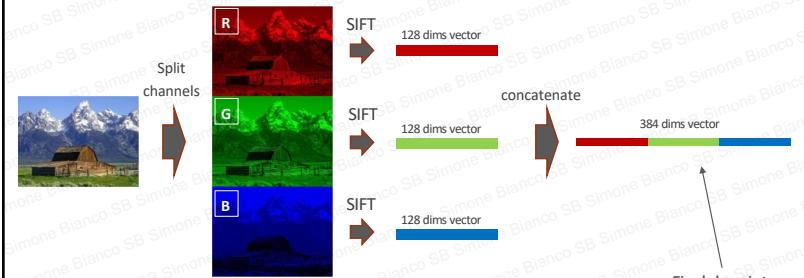
Color descriptors

- SIFT does not use color information
- It just works on grayscale images
- Some objects categories need color information to be distinguished
- Two ways of mixing the color and shape information:
 - Late Fusion approaches
 - Early Fusion approaches



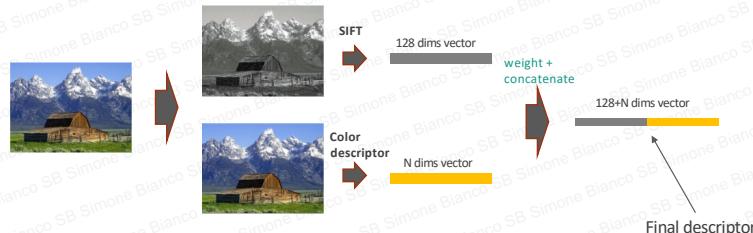
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Early Fusion approaches



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Late Fusion approaches



- N depends on the type of descriptor
- Example: simple histogram on color-space
- Before the concatenation of color and shape descriptor usually the two components are weighted
- Possibility to give more importance (higher weight) to color or shape information

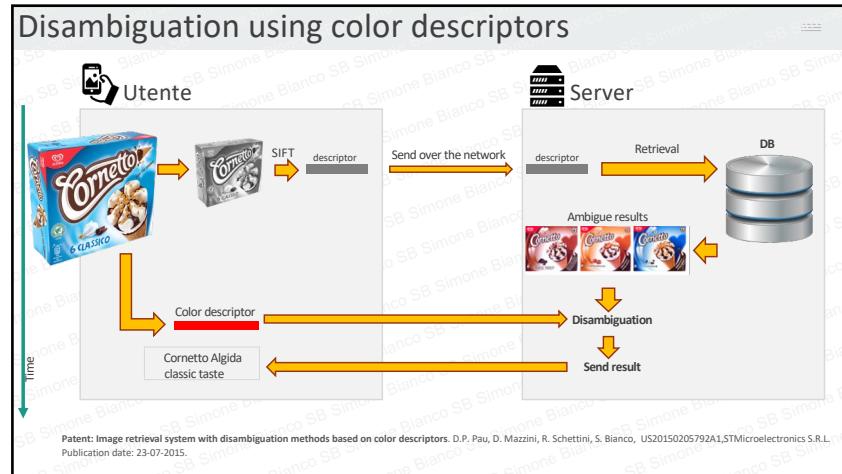
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Color Descriptors

Detector	Dimension	Fusion
RGB SIFT [1]	384	Early
Opponent SIFT [1]	384	Early
Transformed Color SIFT [1]	384	Early
HSV SIFT [1]	384	Early
C-SIFT [2]	384	Early
rSIFT [1]	256	Early
cRGB-SIFT [1]	384	Early
Hue SIFT [1]	164	Late
Color Name [3]	139	Late
Fuzzy Sets Color Names [3]	139	Late
Discriminative Color [3]	139, 153, 178	Late

[1] K.E. Van De Sande, T. Gevers, C.G. Snoek, Evaluating color descriptors for object and scene recognition, IEEE Trans. Pattern Anal. Mach. Intell. 32 (9) (2010) 1582–1596.
 [2] A.E. Abdel-Hakim, A.A. Farag, Csift: a sift descriptor with color invariant characteristics, in: 2006 IEEE Computer Society Conference on Computer Vision and Pattern Recognition, vol. 2, IEEE, 2006, pp. 1978–1983.
 [3] Van De Weijer, C. Schmid, Applying color names to image description, in: IEEE International Conference on Image Processing, 2007, ICIP 2007, vol. 3, IEEE, 2007, p. III-493.

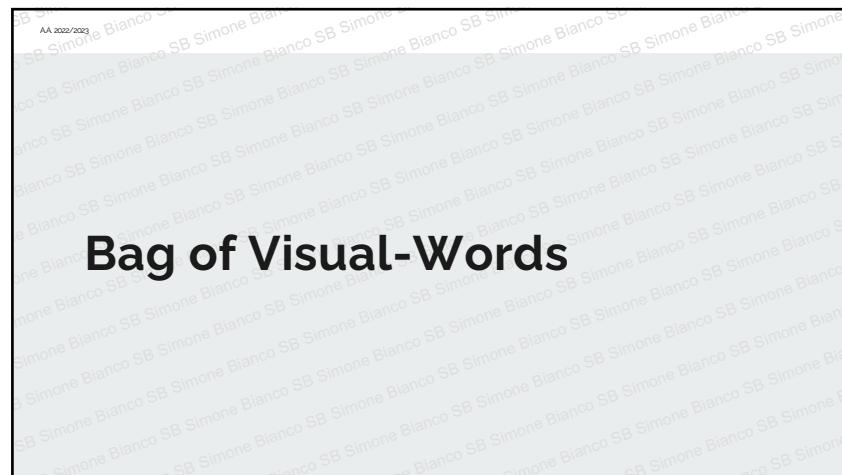
73



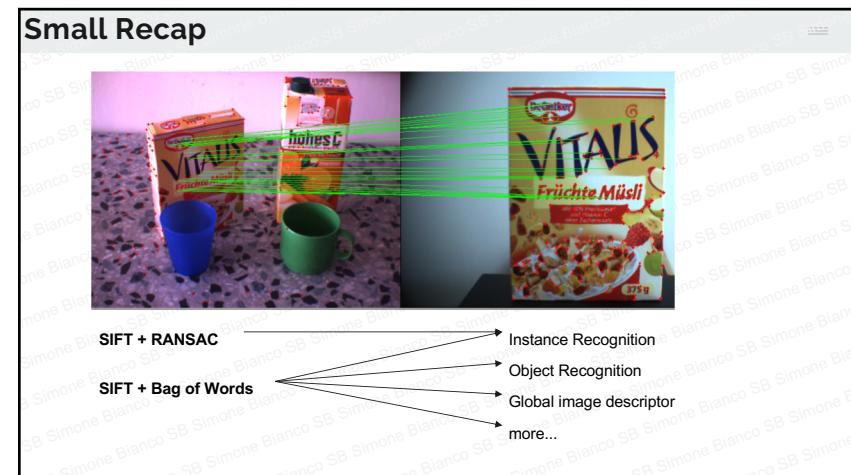
74



75



76



77

Bag-of-words: motivation

President George W. Bush Speech In 2001

ADDRESS TO THE JOINT SESSION OF THE 107TH CONGRESS
UNITED STATES CAPITOL
WASHINGTON, DC, SEPTEMBER 20, 2001

Mr. Speaker, Mr. Vice President, Temporary members of Congress, and fellow Americans, in a solemn course of events, Presidents come to this chamber to report on the state of the Union. Tonight, no such report is needed; it has already been delivered by the American people. We have seen in the course of passengers, who rushed terrorists to save others on the ground—passengers like the exceptional man Todd Beamer. And would you please stand? Let us give a standing ovation to Todd Beamer. We have seen the acts of valor in the performance of rescuers, workers, and neighbors. We have seen the unfolding of flags, the lighting of candles, the giving of life, the saving of lives, in English, Hebrew, and Arabic. We have seen the demands of a loving God giving people who have made the grief of America their own, the strength to go forward. We have seen the love that has been set in the state of our Union—on faraway days. Tonight we are a country awakened to danger and called to defend freedom. Our grief has turned to anger, and anger to resolution. Whether we bring our enemies to justice or seek justice for ourselves, justice will be done.

For many Americans, the attack on our country was a reminder that America was touched on the evening of the tragedy to see Republicans and Democrats joined together on the steps of this Capitol, singing "God Bless America." And you did more than sing; you acted, by delivering \$40 billion to rebuild our country, and meet the needs of our military. Speaker Hastert, Minority Leader Gephardt, Majority Leader Daschle and Senator Lott, I thank you for your friendship, for your leadership and for your service to our country... (to be continued)

- We want to represent the topic of the document in a compact way
 - **Orderless** document representation: frequencies of words from a dictionary
Salton & McGill (1983)

78

Bag-of-words: motivation



US Presidential Speeches Tag Cloud
<http://chir.ag/projects/preztags/>

79

Bag-of-words: motivation



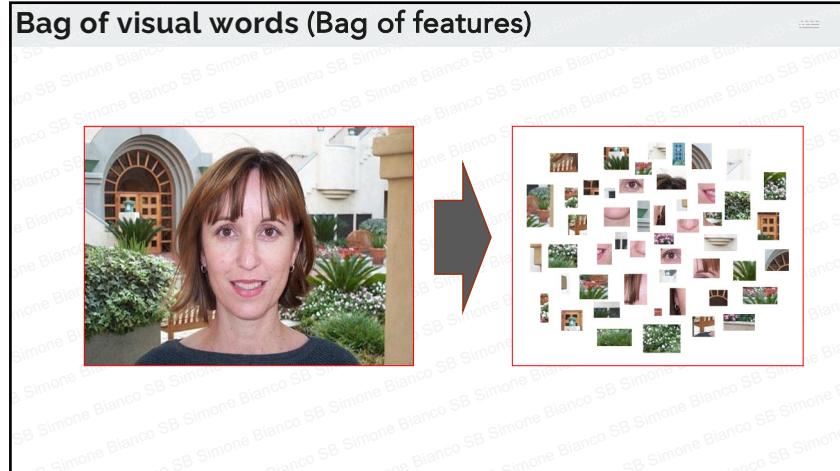
80

Bag-of-words: motivation



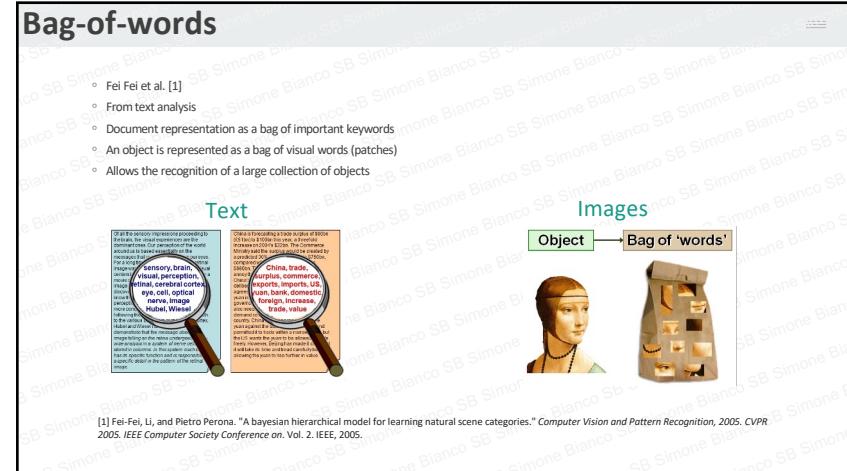
81

Bag of visual words (Bag of features)



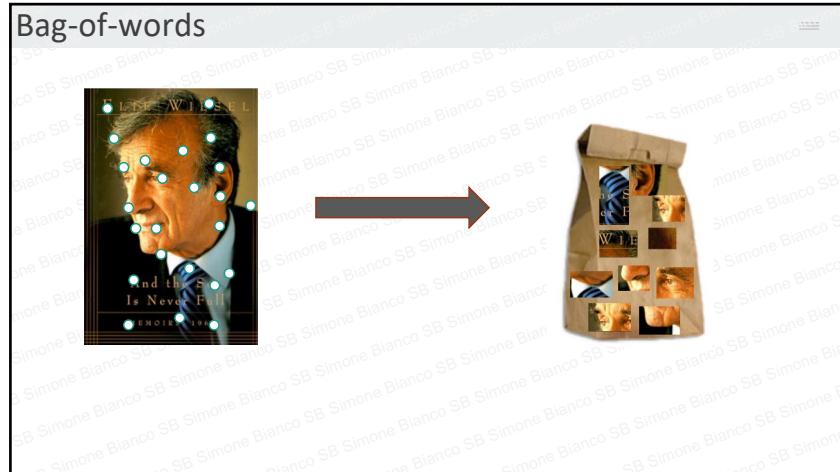
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Bag-of-words



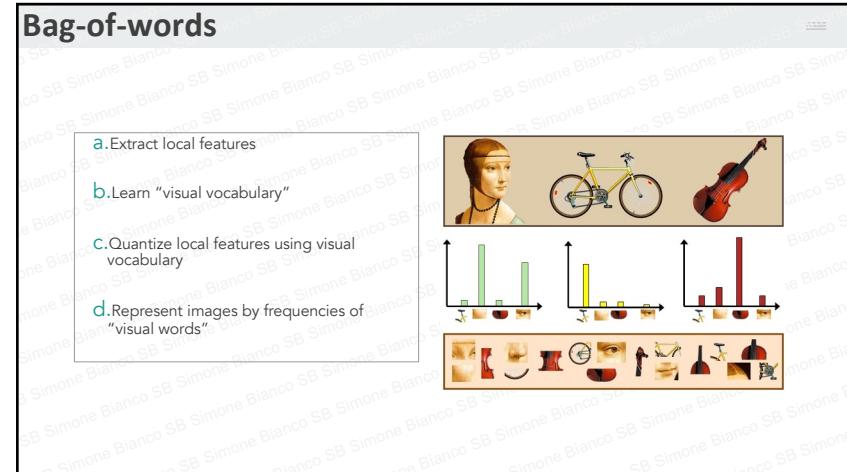
83

Bag-of-words



84

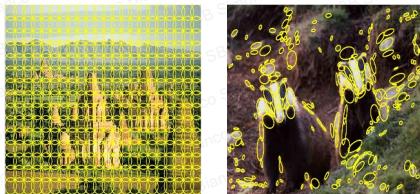
Bag-of-words



85

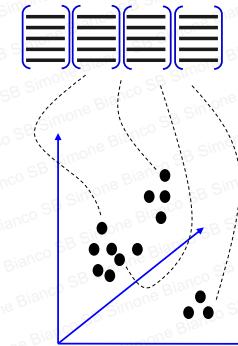
Local features extraction

Sample patches and extract descriptors



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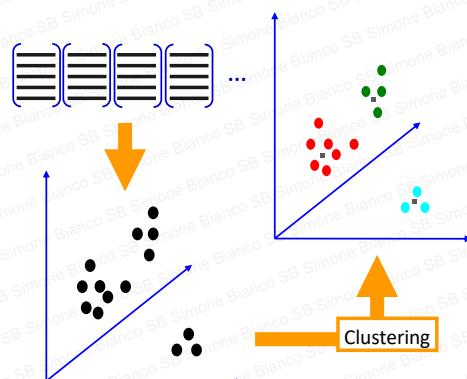
Learning the visual vocabulary (1/2)



Extracted descriptors from
the training set

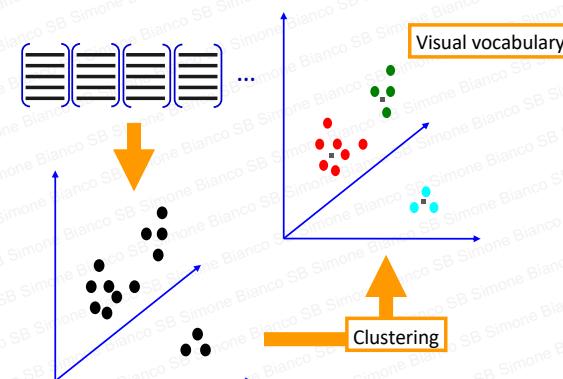
87

Learning the visual vocabulary (2/2)

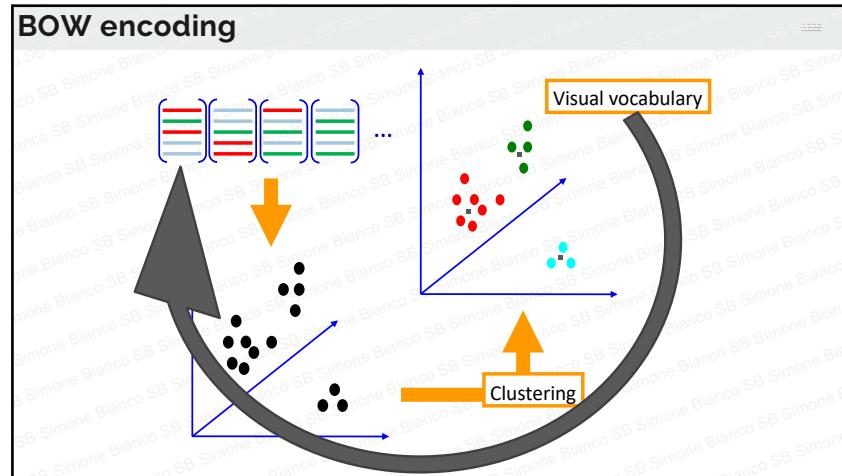


88

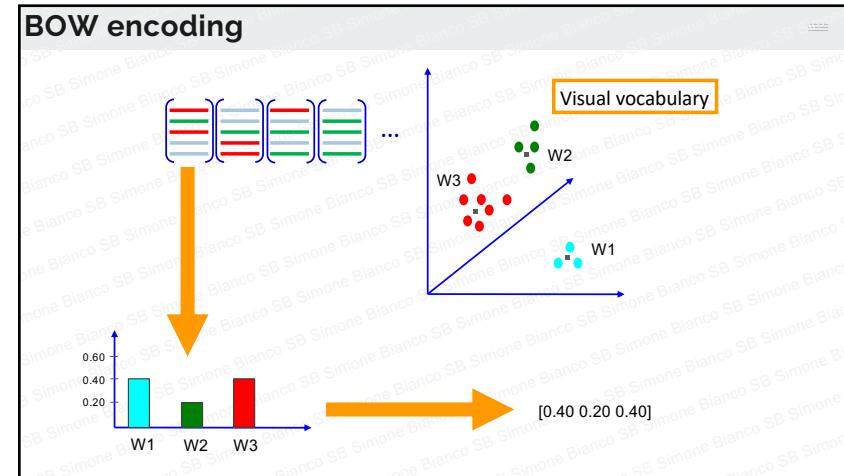
Learning the visual vocabulary (2/2)



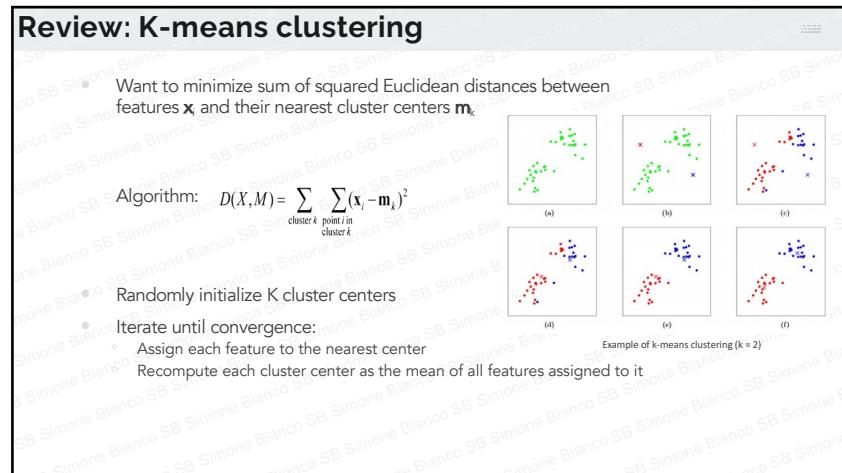
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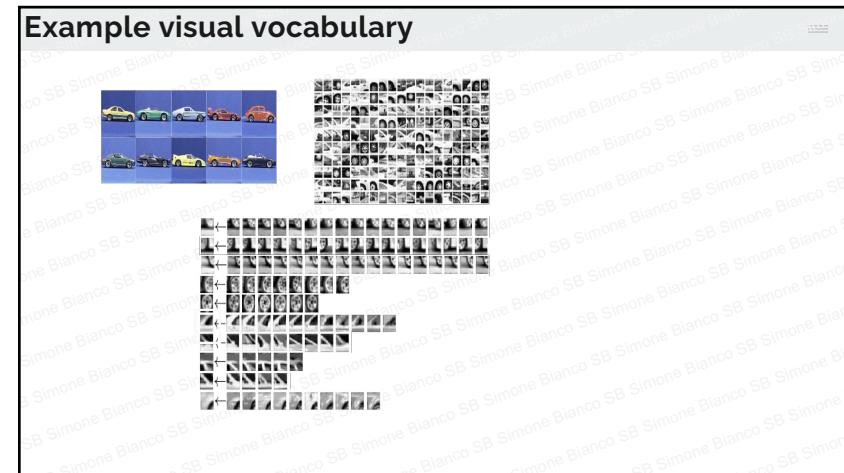
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91

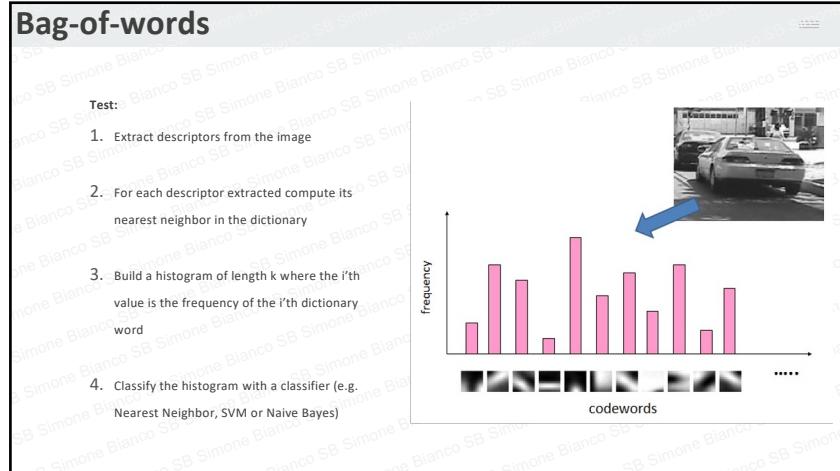


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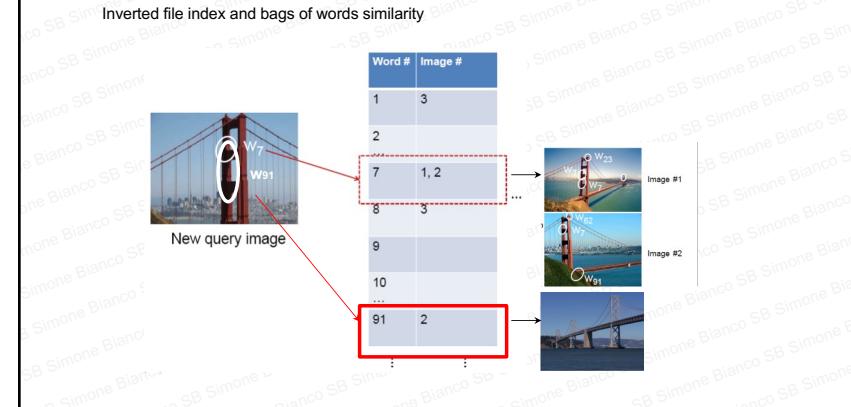
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Bag-of-words



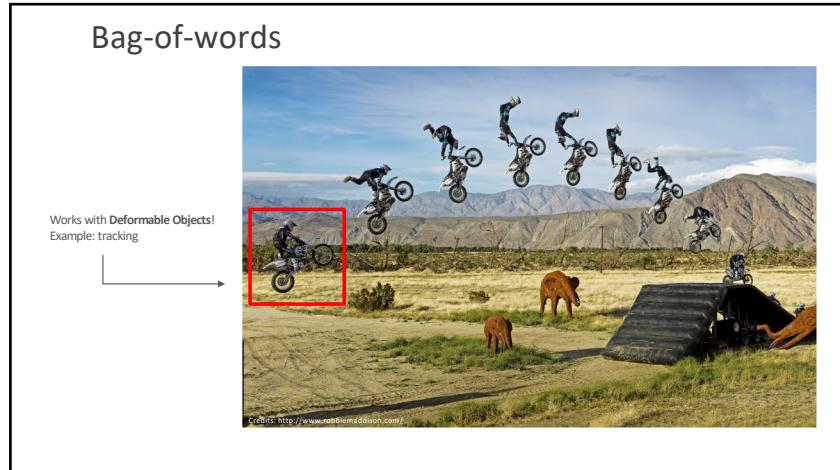
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Applications of Bag of words



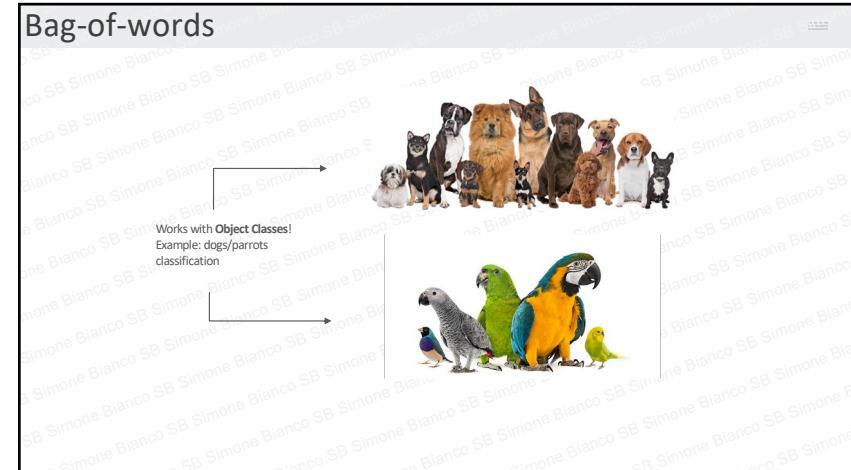
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Bag-of-words



96

Bag-of-words



97