Discrete and exact boundary flow

