



**POLITECNICO**  
MILANO 1863



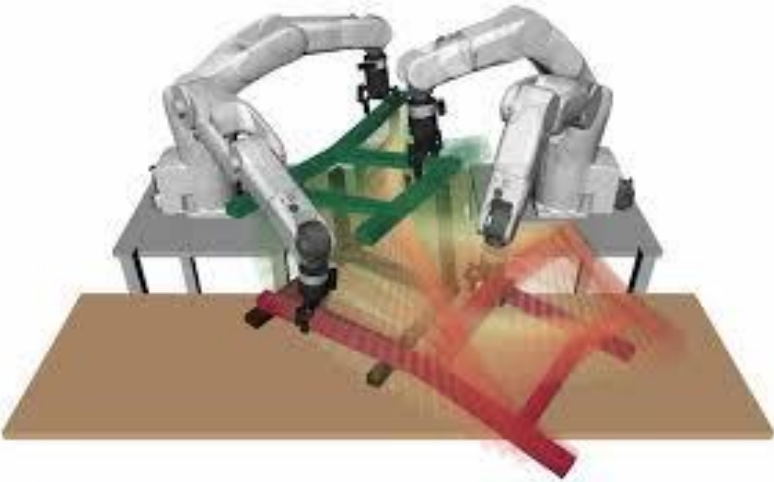
# MT-RRT: a general purpose multithreading library for path planning

Andrea Casalino, Andrea Maria Zanchettin and Paolo Rocco

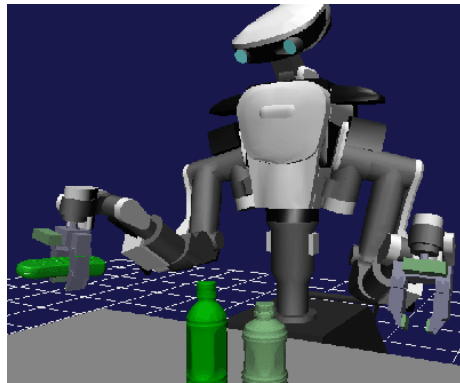
# Motivations

Possible planning problems:

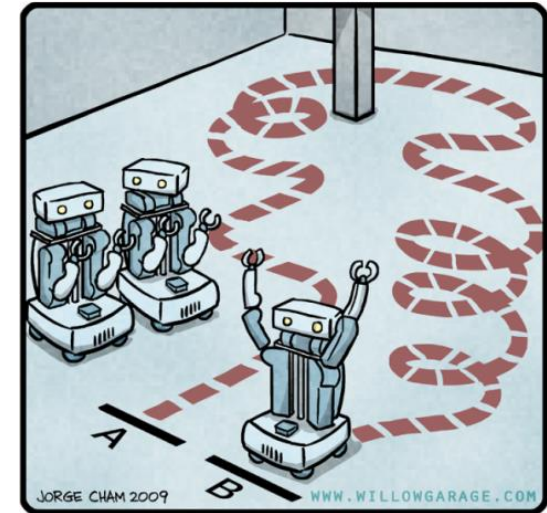
Pick and place



Plan grasping motions






Mobile robots navigation



# Possible approaches

Possible approaches to solve a planning problem:

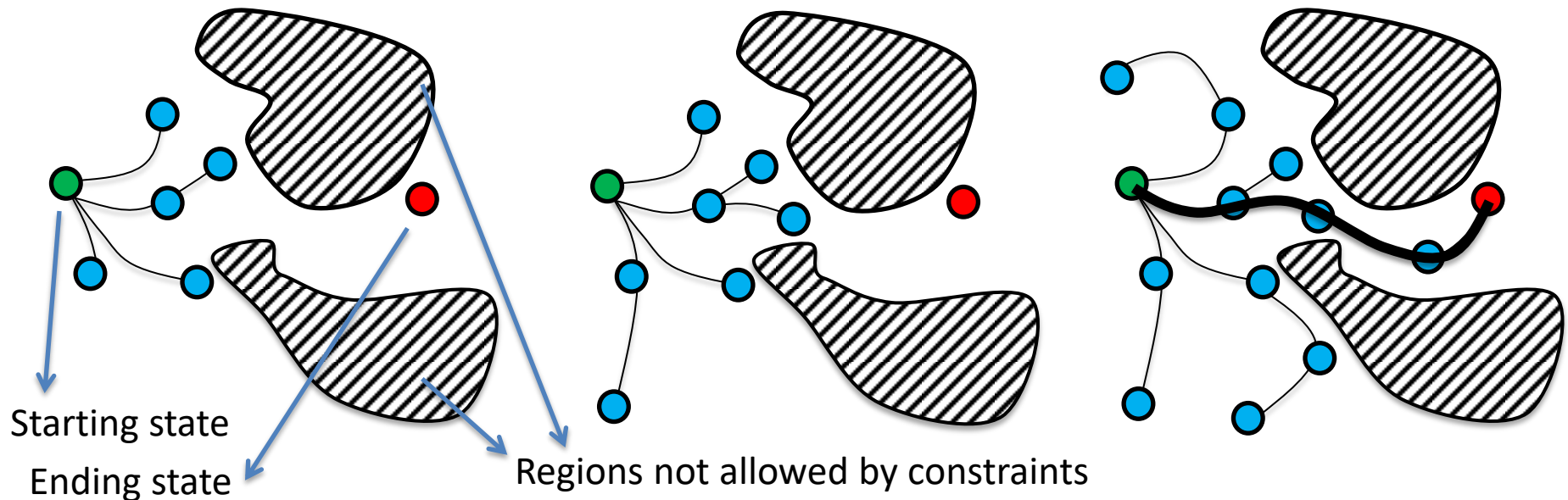
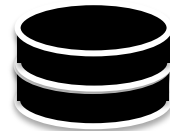
- ❑ closed loop control schemes
  - ❑ Repulsive/attractive fields  Local minimum problems
  - ❑ MPC approaches  May fail to find a feasible solution for complex workspace
  
- ❑ Rapidly random exploring tree strategies  Flexible and capable of always finding a solution, in the case a solution exists...  
  
... but computationally intense: thousands of iterations are required also to get at a sub-optimal solution.

# RRT mechanism

The algorithm consists essentially in exploring the configurational space admitted by a series of constraints, with the aim of building a search tree. Once the starting and the ending states are connected at least a solution is found.

Iterations

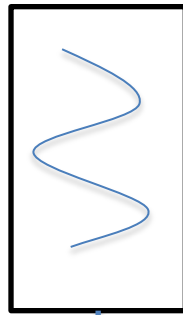
Database of  
connections



# Accelerating RRT algorithms

Why don't explore the configurational space in different threads in order to grow faster the search tree?

Standard single thread

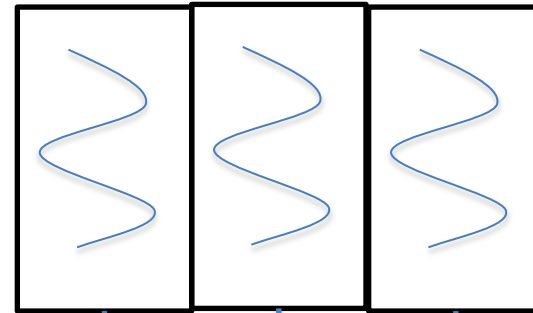


After N iterations

Database of connections



Ideal multi-threaded approach



After N iterations



=

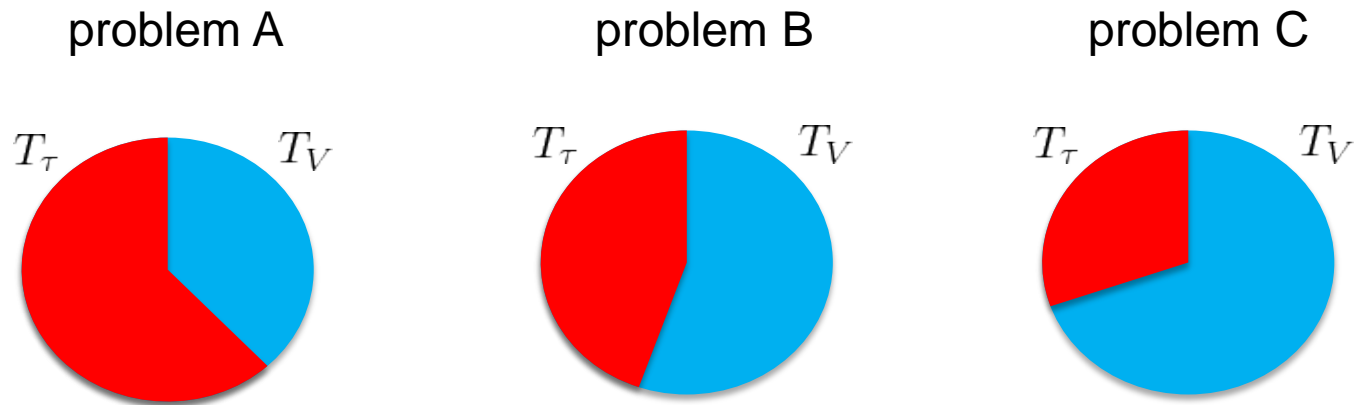


How to achieve a good parallelism when applying RRTs?

# RRT profiling

The computational times are shared by the following main operations:

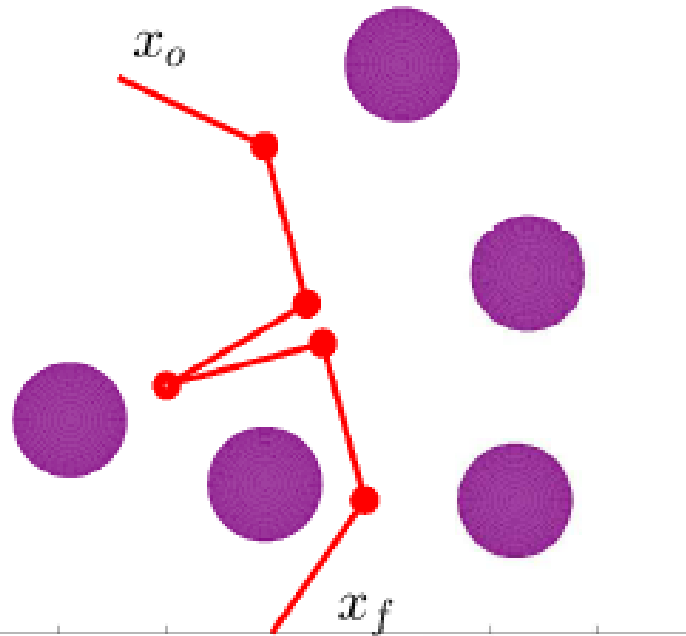
- $T_\tau$  — Optimal trajectory computation (includes Nearest Neighbour searches)
- $T_V$  — Check the feasibility of sampled states



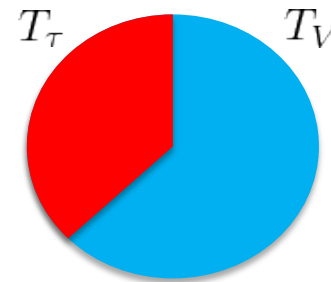
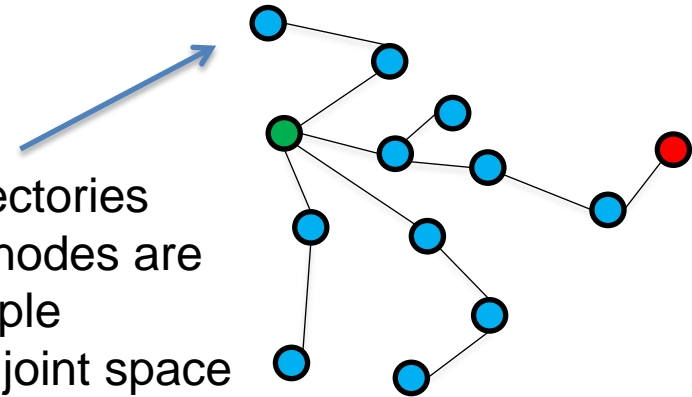
The ripartition of times can significantly vary from one application to another.

# Benchmark A

Path planning of a planar 3 d.o.f. robot:



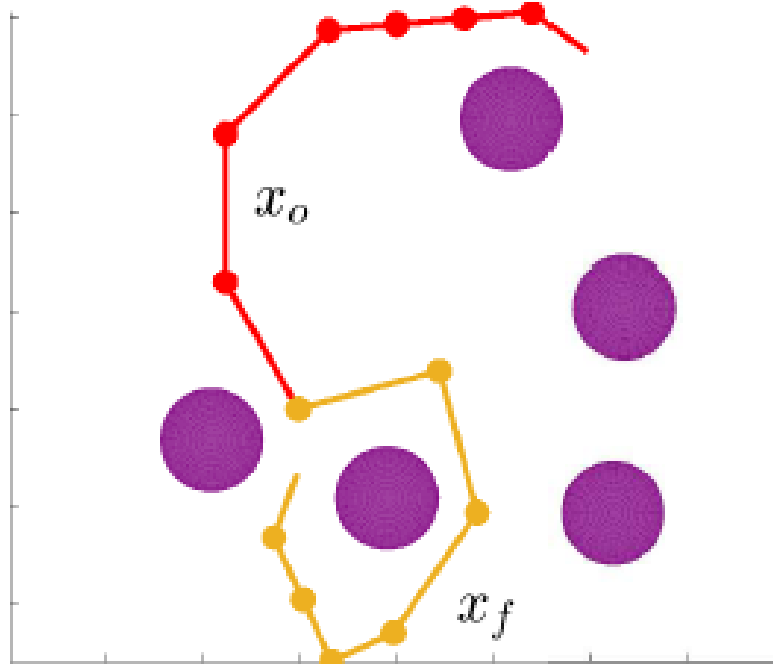
The optimal trajectories connecting the nodes are assumed as simple segments in the joint space



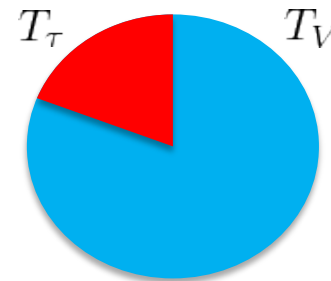
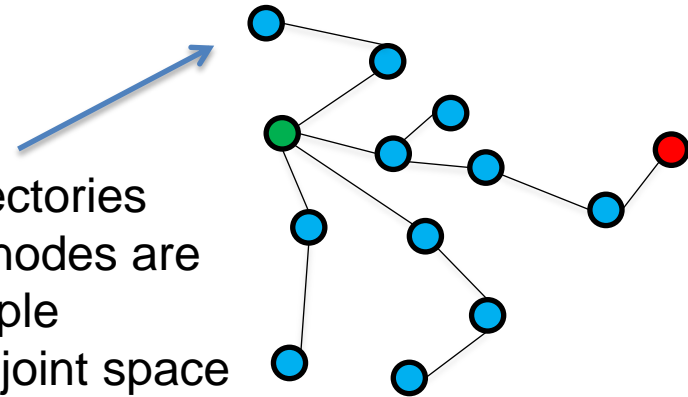
- $T_\tau$  — Optimal trajectory computation (includes Nearest Neighbour searches)
- $T_V$  — Check the feasibility of sampled states

# Benchmark B

Path planning of a planar 7 d.o.f. robot:



The optimal trajectories connecting the nodes are assumed as simple segments in the joint space

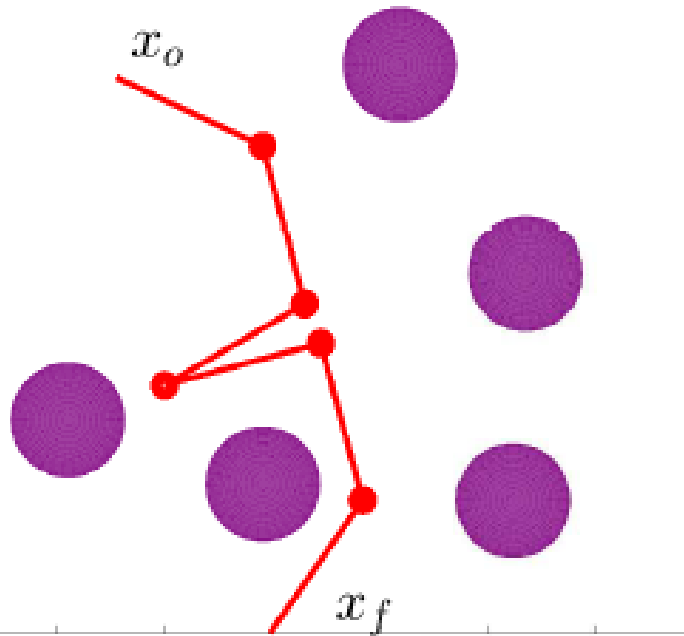


- $T_\tau$  — Optimal trajectory computation (includes Nearest Neighbour searches)
- $T_V$  — Check the feasibility of sampled states

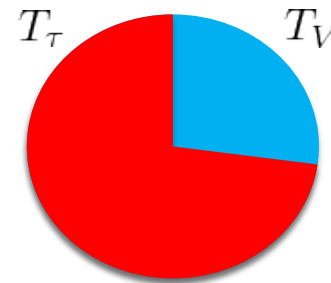
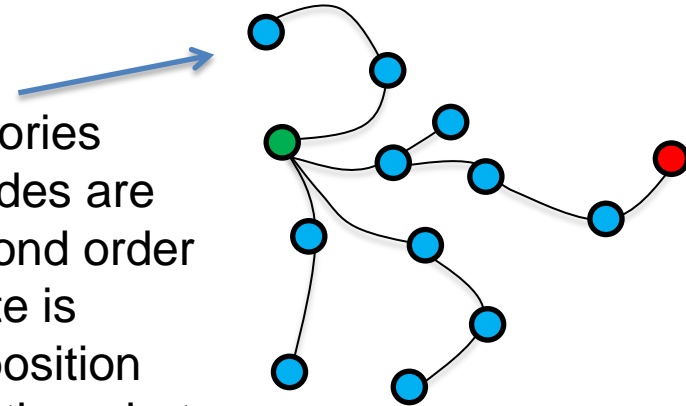


# Benchmark C

Trajectory planning of a planar 3 d.o.f. robot:



The optimal trajectories connecting the nodes are minimum time second order time laws. The state is made of both the position and the velocity of the robot



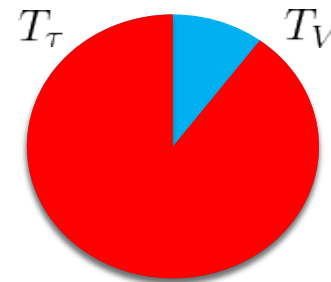
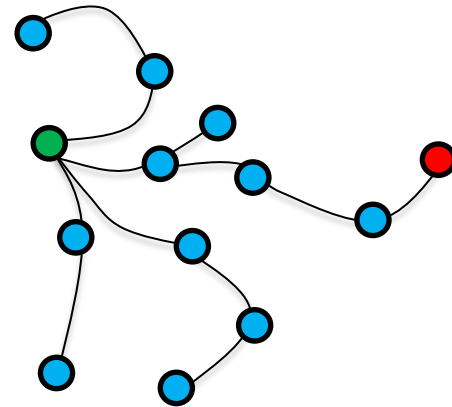
- $T_\tau$  — Optimal trajectory computation (includes Nearest Neighbour searches)
- $T_V$  — Check the feasibility of sampled states

# Benchmark D

Kinodynamic planning:

$$\begin{cases} \dot{x} = f(x) + u \\ u = u_o + \frac{\partial f}{\partial x} \Big|_{x_o} (x - x_o) + K(x_f - x) \\ s.t. \quad x \in \mathcal{X}, u \in \mathcal{U} \end{cases}$$

The optimal trajectories connecting the nodes are computed by considering a LQR controller applied on a linearization of the system.

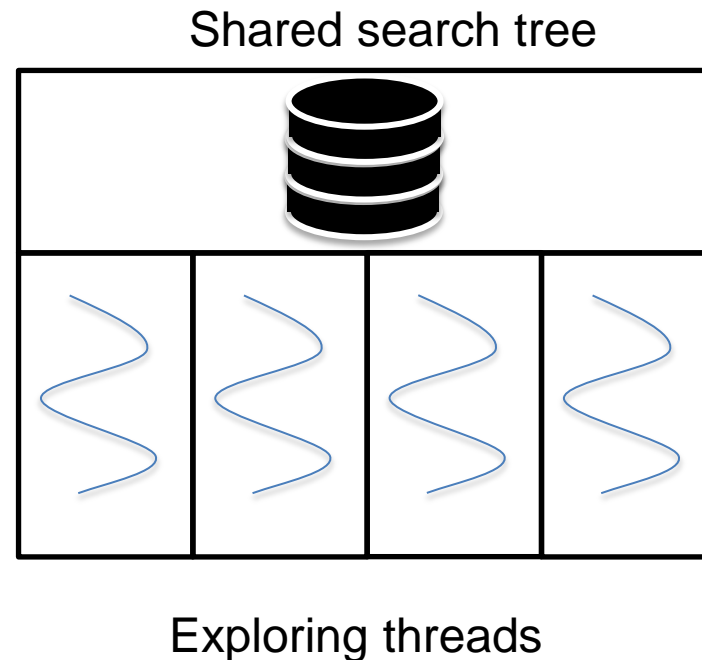


$T_\tau$  — Optimal trajectory computation (includes Nearest Neighbour searches)

$T_V$  — Check the feasibility of sampled states

# Shared tree exploration

The whole exploration process is parallelized. Threads share the same tree and have to synchronize each other for modifying it.



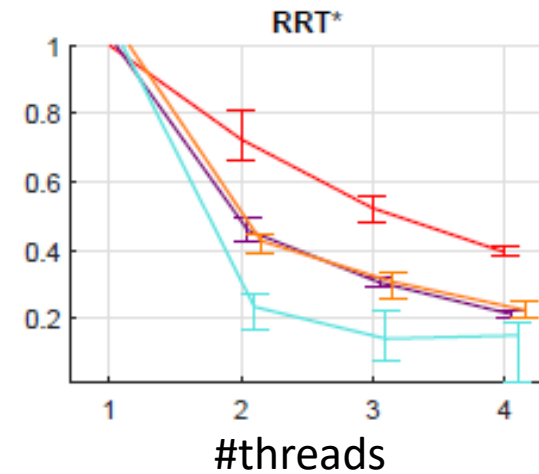
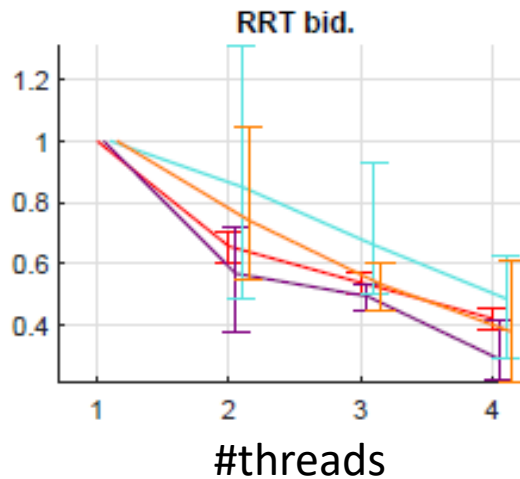
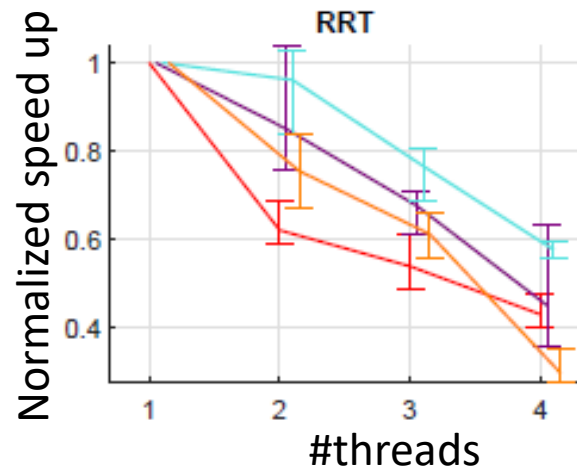
# Shared tree exploration: results

3 dof path planning

7 dof path planning

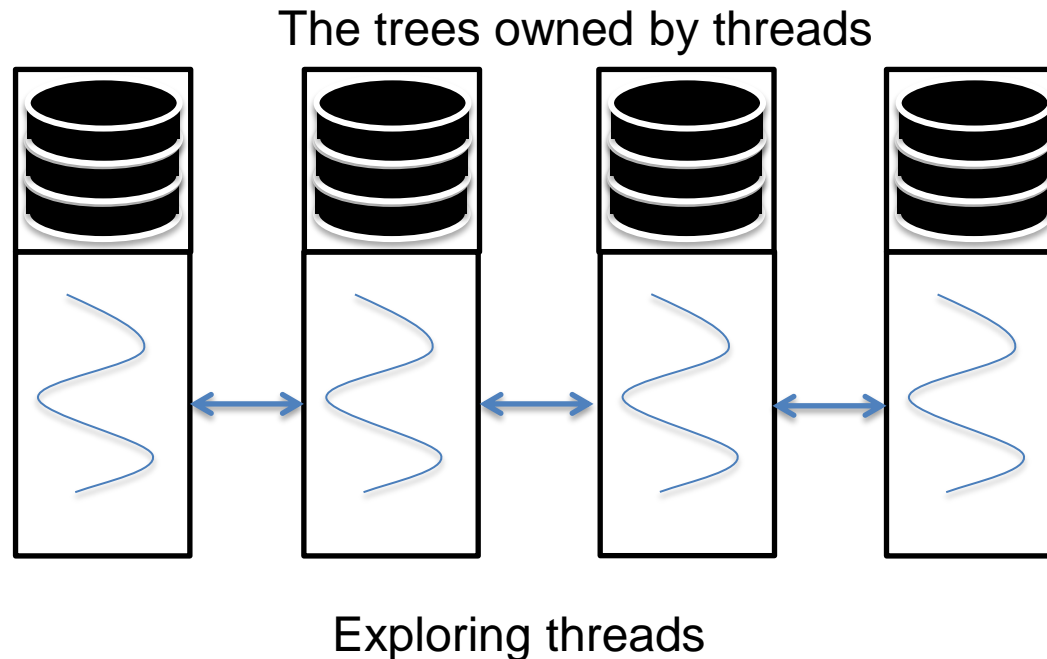
3 dof traj. planning

Kinodynamic planning



# Local tree copies

The whole exploration process is parallelized. Each thread has its proper tree to expand. In this case, threads don't need to synchronize at each iteration. With a certain frequency, data are exchanged among threads.



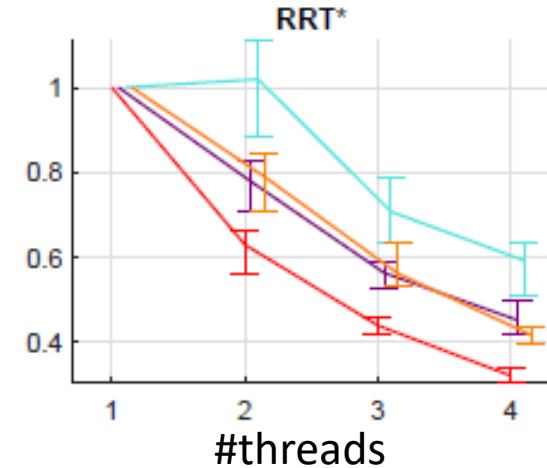
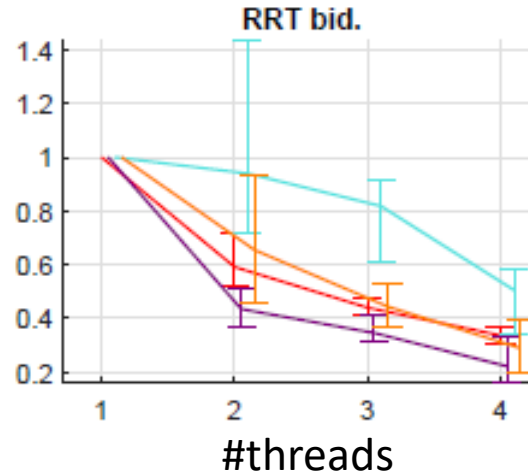
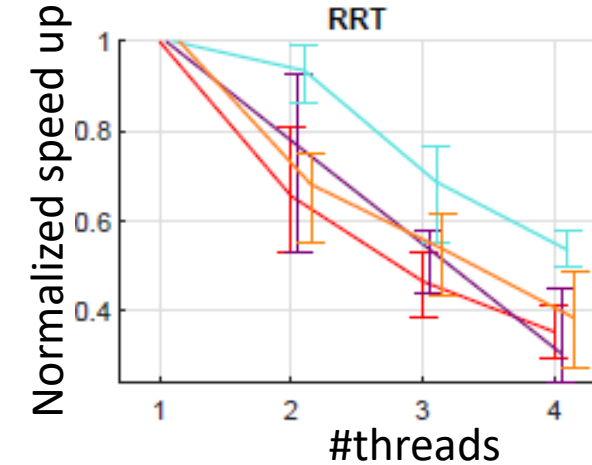
# Local tree copies: results

3 dof path planning

7 dof path planning

3 dof traj. planning

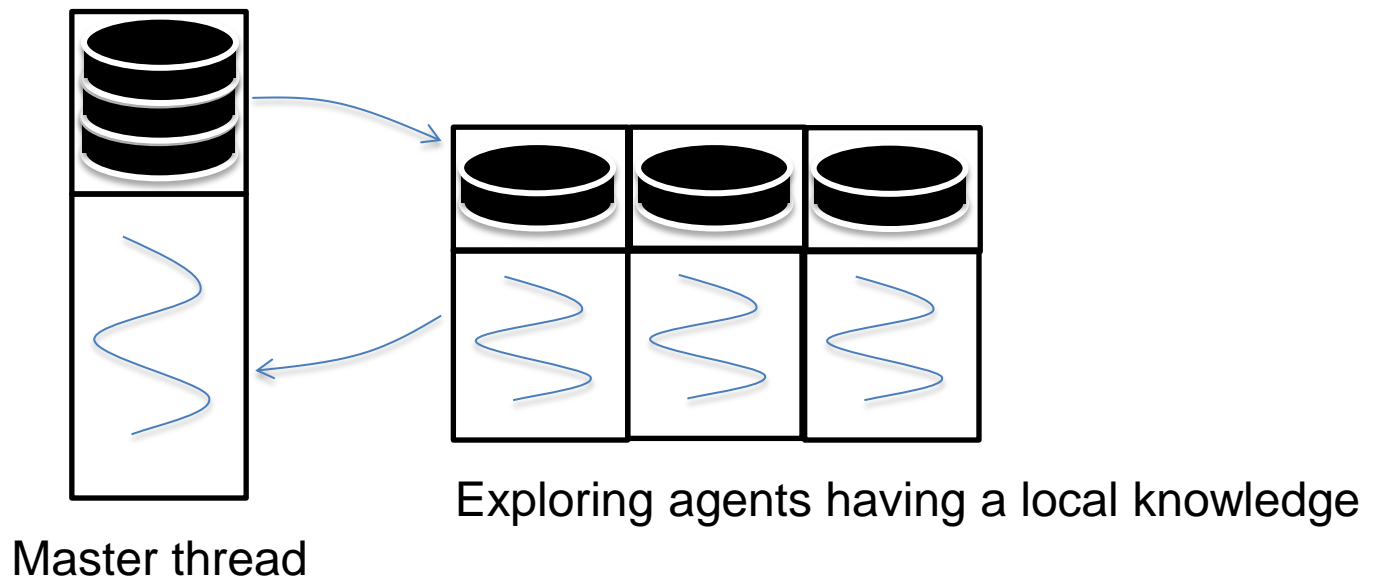
Kinodynamic planning



# Multi agents approach

Blinded multi agents exploration: a pool of threads locally explore the configurational space, starting every time from a new root and obtaining a new tree. The explorations are notified to a master, which integrates the knowledge acquired by the slaves into a single tree and dispatch new roots to explore.

Rewirds are locally done on the local tree in case of the RRT\*.



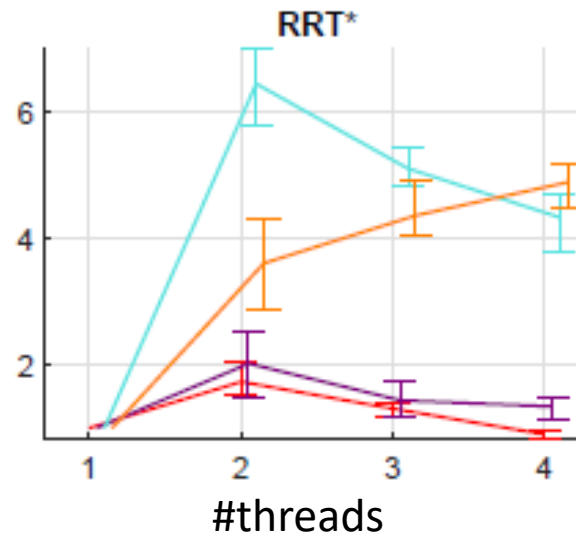
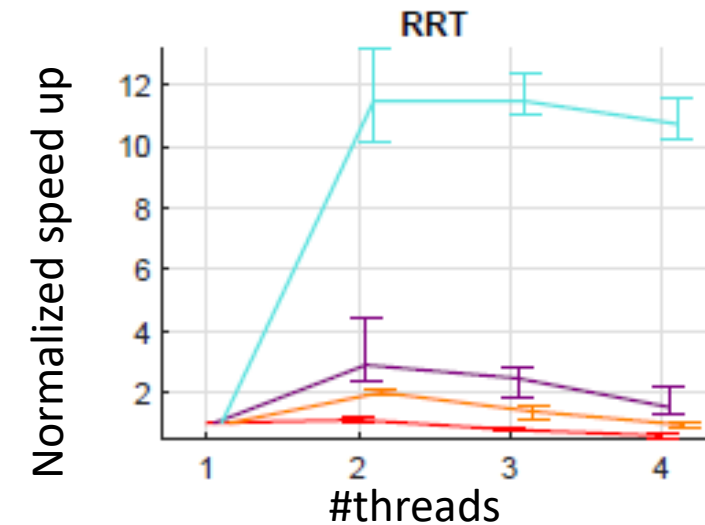
# Multi agents approach: results

3 dof path planning

7 dof path planning

3 dof traj. planning

Kinodynamic planning



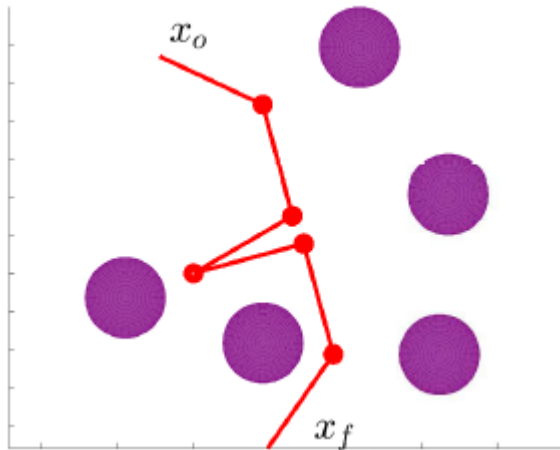
Speed up increased dramatically



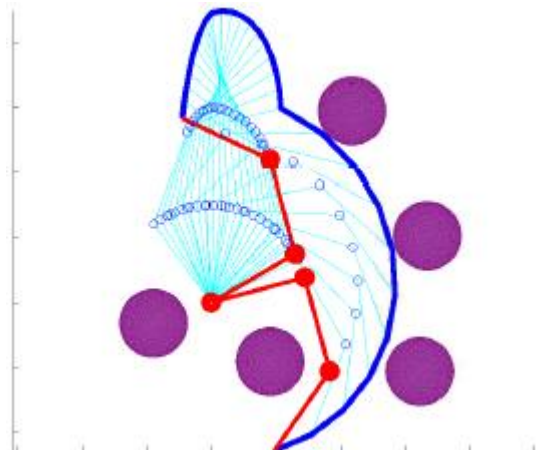
# Multi agents approach

The optimality property of the RRT\* seems to be preserved also in this multi agents strategy:

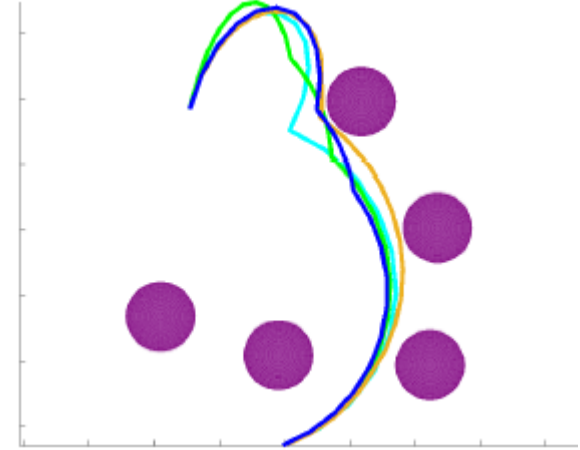
3 d.o.f. path  
planning problem



Minimum distance  
path (in joint space)



Solutions obtained by the RRT\*  
parallelized with the  
multi agents strategy



# MT-RRT C++ library

All the proposed strategies are contained in an open source library C++. It was made so as to easily customize a new planning problem and use the proposed solvers.

Check out the the Github profile:

[https://github.com/andreacasalino/MT\\_RRT](https://github.com/andreacasalino/MT_RRT)

