

# Monte Carlo introduction

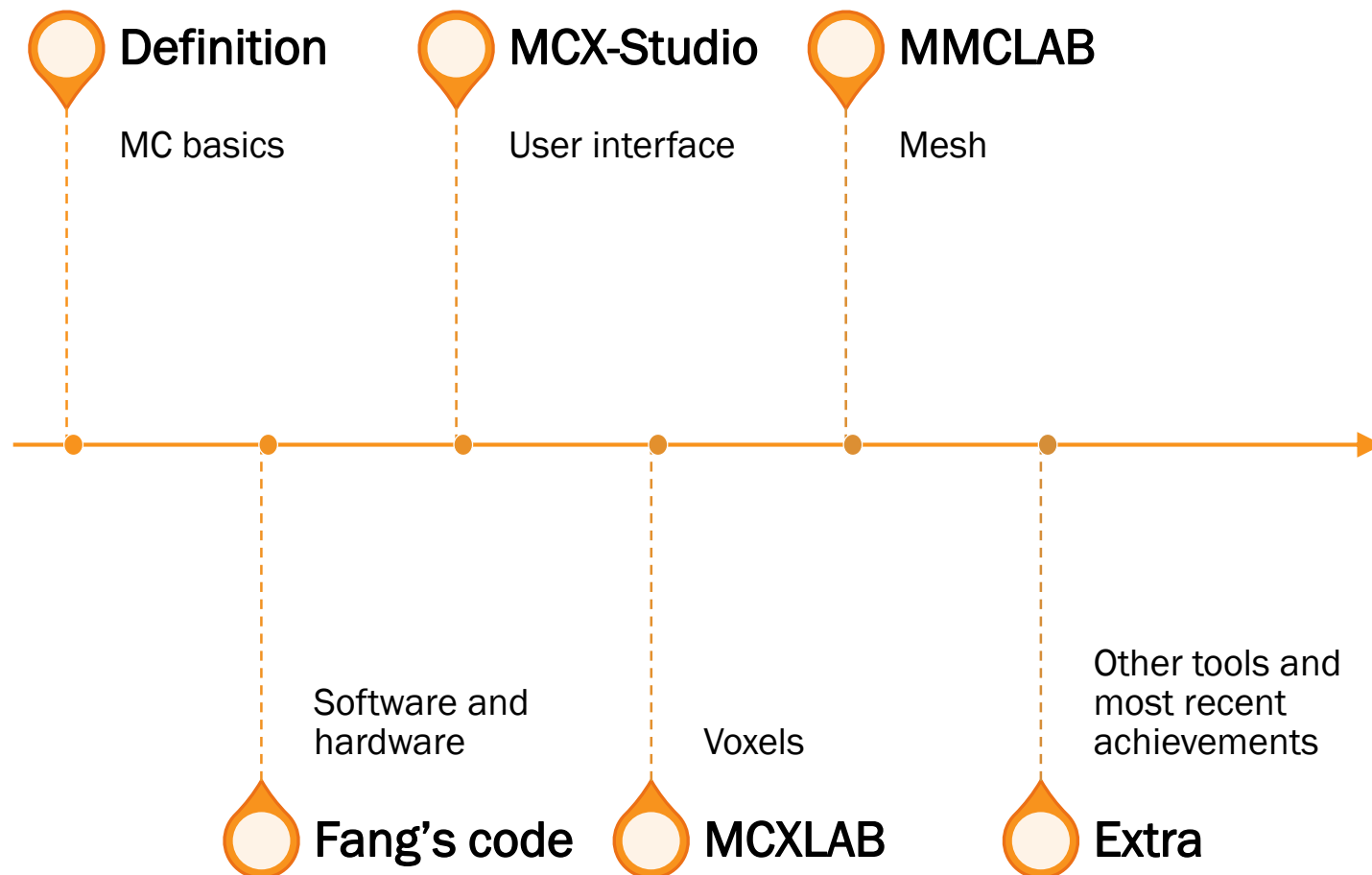
16<sup>th</sup> December 2021

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CATERINA AMENDOLA

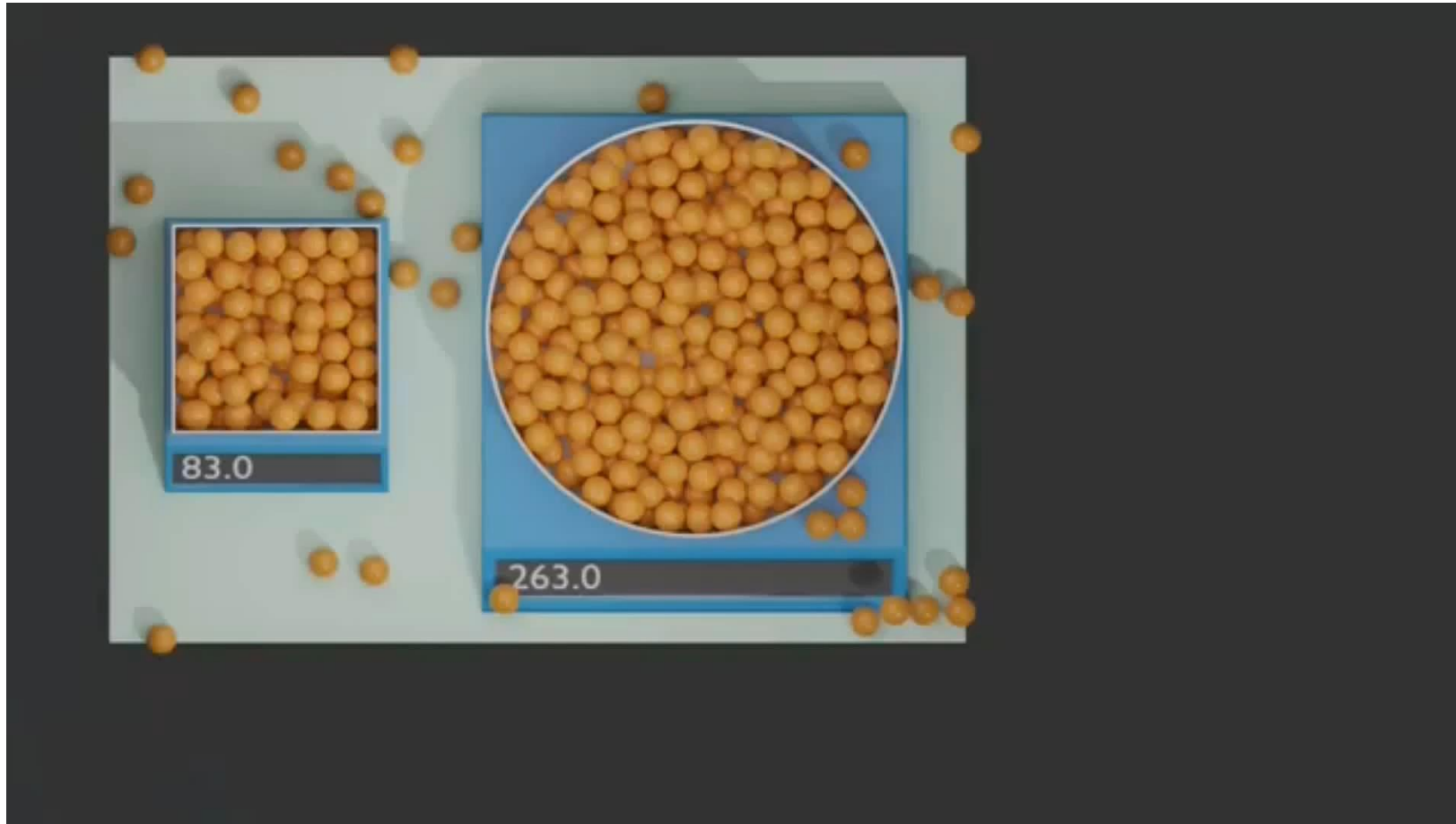
GIULIA MAFFEIS

# Outline



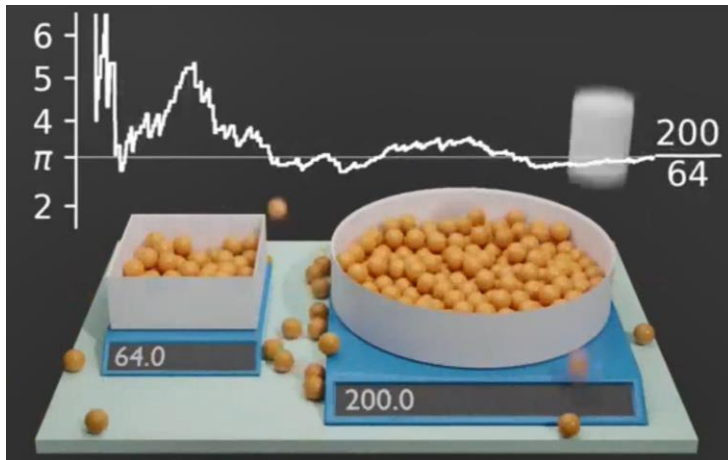
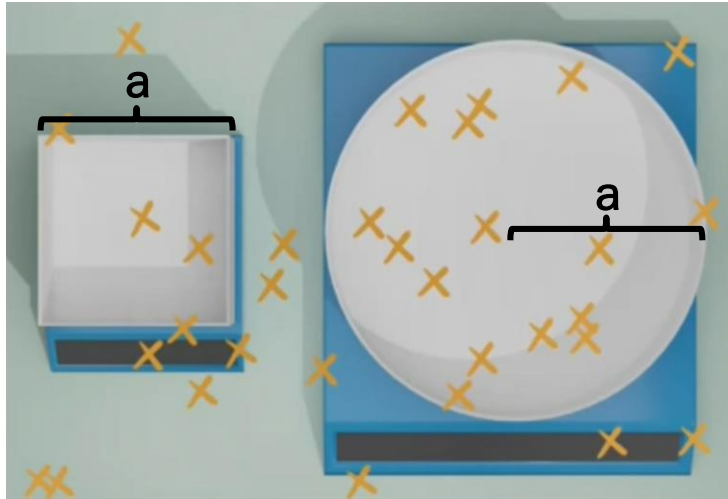
# Definition

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[https://www.youtube.com/watch?v=7ESK5SaP-bc&t=47s&ab\\_channel=MarbleScience](https://www.youtube.com/watch?v=7ESK5SaP-bc&t=47s&ab_channel=MarbleScience)

# Definition



Randomness

Sparsity

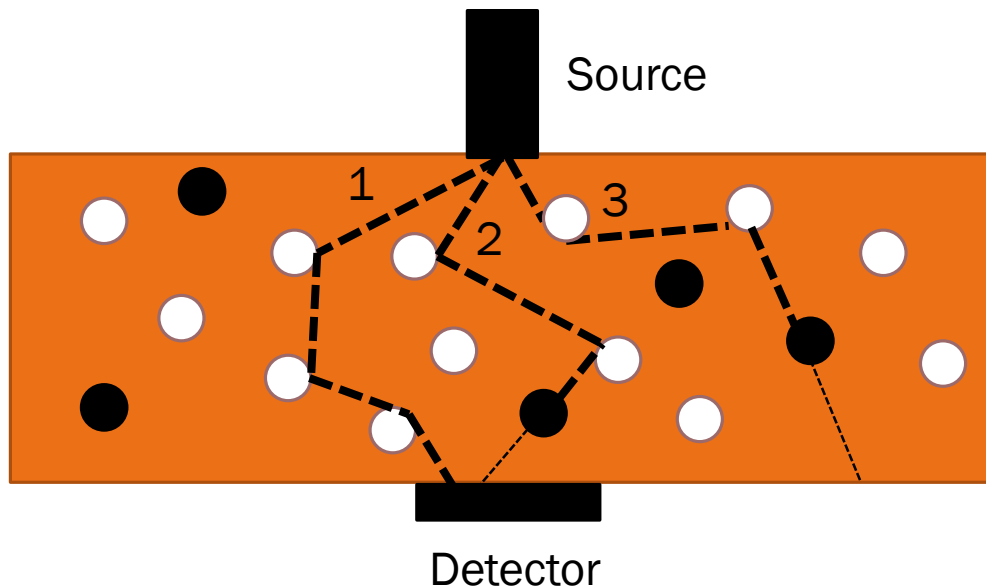
Finiteness



# Fang's code

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Open-source light transport simulator



- Scattering centre
- Absorption centre

## SEED

Initial number of the **pseudorandom number generator**. It returns a sequence of numbers that looks random, but **always generates the same sequence for a given value**.

## WEIGHT

Initial

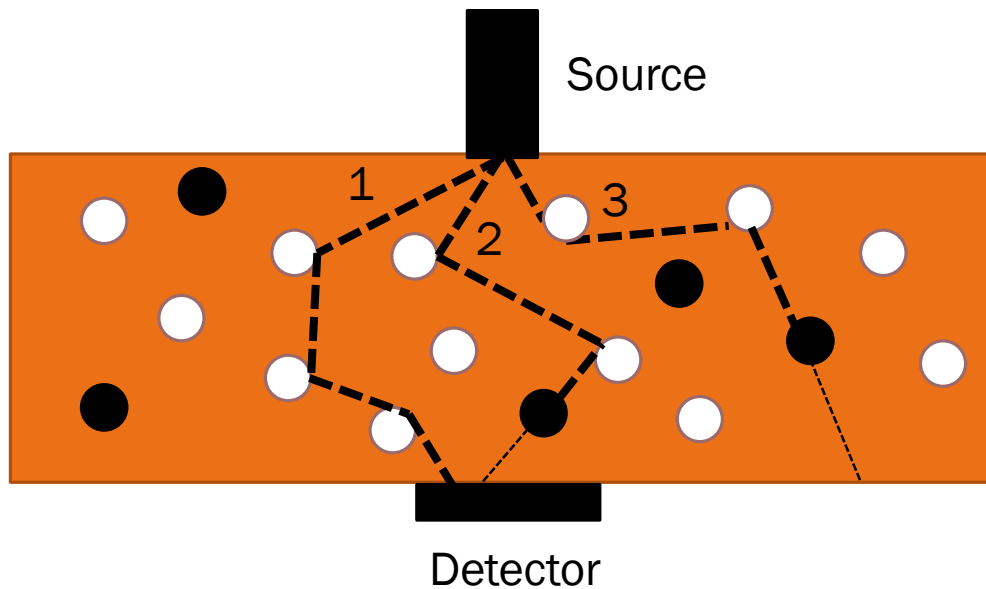
For each photon,  $W = 1$

Final

Affected by absorption

# Fang's code

Open-source light transport simulator



- Scattering centre
- Absorption centre

## PROPAGATION

Scattering Deviation in direction

Absorption Reduction in photon weight

ATTENTION! No annihilation!

## DETECTION

In Collected photon (1, 2)

Out Lost photon (3)

Final curve = Weight distribution!

# Fang's code

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## WHY DID WE CHOOSE IT?

- Above all, MCX is **open-source** and free for everyone!
- **Time-resolved** photon transport simulations
- Supporting arbitrarily complex 3-D volume using a **voxelated/meshed domains**
- Supporting various boundary conditions, source forms and media (also continuously varying)
- Recording rich set of detected photon information (fluence, energy, jacobian...)
- MATLAB/GNU Octave/JSON/ Python languages
- Supporting **GPU acceleration** using a single or multiple GPUs (
  - **NVIDIA GeForce RTX 3080 Ti on Eulero and Keplero!**
  - **ATTENTION! Always monitor GPU updates!**

# Fang's code

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## GENERAL INFORMATION

- Web page: <http://mcx.space/wiki/index.cgi?Home>
- Download the last version of MCX/MMC/MCXSTUDIO: <http://mcx.space/wiki/index.cgi?Get>
- Tutorials and installation guide: <http://mcx.space/wiki/index.cgi?Learn#mcxstudio>
- Iso2mesh: <http://iso2mesh.sourceforge.net/cgi-bin/index.cgi>
- Forum MCX USERS: <https://groups.google.com/g/mcx-users?pli=1>
- Speed information: <http://mcx.space/wiki/index.cgi?Speed>



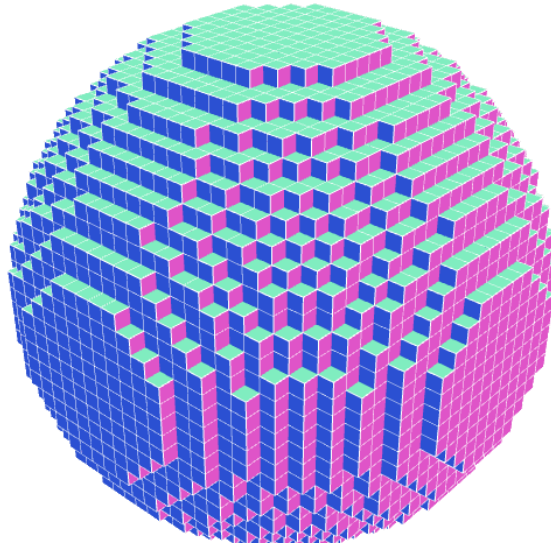
# Fang's code

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## Voxel – MCX

Monte Carlo eXtreme

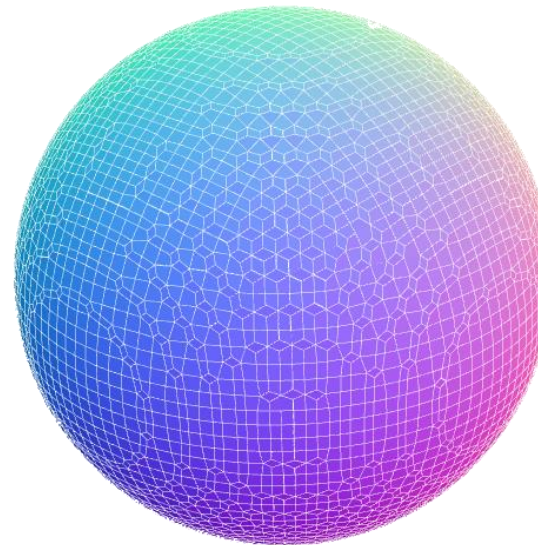
The volume is discretised  
in **cubes** of **same**  
**dimension and shape**



## Mesh - MMC

Mesh-based Monte Carlo

The volume is discretised  
in **tetrahedrons** of  
**different dimensions and**  
**shapes**



# Fang's code

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## Voxel – MCX

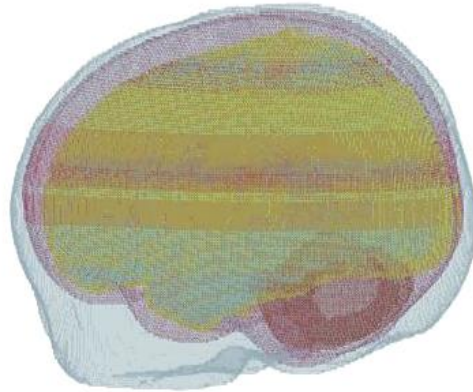
Monte Carlo eXtreme

### PRO

- Fast → GPU!
- Easy to implement

### CON

- Lack of smoothness



2 min

## Mesh - MMC

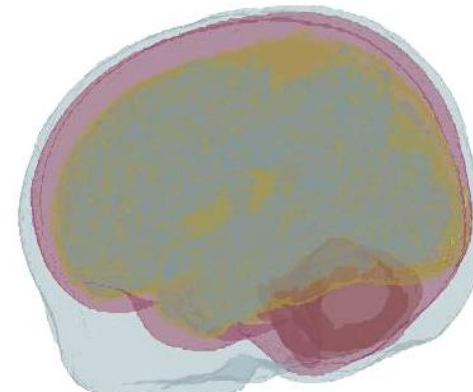
Mesh-based Monte Carlo

### PRO

- Accurate
- Smooth surfaces

### CON

- Long computational time → CPU!



31 min

# Fang's code

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CPU

Central Processing Unit



GPU

Graphics Processing Unit

Optimized for latency	Optimized for throughput
Mainly serial approach	Parallel approach
Versatile	Specific tasks
Smart	Repetitive tasks
Few units	Thousands of units
Es: PC “brain”	Es: machine learning, cryptocurrency mining, videogaming, scientific computation

# Fang's code

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## MMCCCL

MMC for OpenCL

### PRO

- Accurate
- Smooth surfaces
- Faster than MMC → **CPU + GPU!**

### CON

- Longer than MCX
- NVIDIA does not fully support OpenCL

## MCXCL

MCX for OpenCL

### PRO

- Unlike MCX (only NVIDIA GPUs), MCX-CL can be executed on up-to-date CPUs and GPUs

### CON

- Longer than MCX
- NVIDIA does not fully support OpenCL

**OpenCL** (Open Computing Language) is a framework for writing programs that execute across heterogeneous platforms, e.g. CPUs, GPUs, DSPs, FPGAs. It provides a standard interface for parallel computing using task- and data-based parallelism.

# Voxel: MCX Studio

Graphical **user interface** for MCX.

Example #1: Head layered structure

- Trhree-layer cylinder:  $D = 60$  mm,  $H_1 = 5$  mm,  $H_2 = 10$  mm,  $H_3 = 45$  mm

	Background (0)	Layer (1)	Layer (2)	Layer (3)
$\mu_a$ [mm <sup>-1</sup> ]	0	0.01	0.02	0.03
$\mu_s$ [mm <sup>-1</sup> ]	0	4.55	9.09	13.64
$g$	1	0.89	0.89	0.89
$n$	1	1.4	1.3	1.4

- Reflectance geometry: unit given by  $\text{unitinmm} = 1$

	x	y	z	R
Source	32.5	30	0	Pencil beam
Detector	27.5	30	0	2

→ Interfiber distance = 5 mm

- Nphoton:  $10^7$
- Tstart: 0
- Tstep: 25 ps
- Tend: 2 ns
- Seed: random
- Single detector,  $r=2$  mm
- Outputtype: fluence and photon path

# Voxel: MCX Studio



## DIY #1: Tumor in compressed breast

- Cube (6x6x4 cm<sup>3</sup>) with a central spherical inclusion ( $r = 1$  cm)

	Background (0)	Cube (1)	Sphere (2)
$\mu_a$ [mm <sup>-1</sup> ]	0	0.02	0.05
$\mu_s$ [mm <sup>-1</sup> ]	0	4.55	9.09
$g$	1	0.89	0.89
$n$	1	1.40	1.40

- Reflectance geometry: unit given by  $\text{unit in mm} = 1$

	x	y	z	R
Source	20	30	0	Pencil beam
Detector	40	30	0	2

- Nphoton:  $10^7$
- Tstart: 0
- Tstep: 25 ps
- Tend: 2 ns
- Seed: random
- Single detector,  $r=2$  mm
- Outputtype: fluence and photon path



# Voxel: MCX Studio

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## HOW TO ACCESS RESULTS IN MATLAB

- Add the path '`...\MCXStudio\MCXSuite\mcx\utils`'
- Use the function '`loadmch.m`' to load data about detected photons → Useful mainly for MCX Studio!

## USEFUL FUNCTIONS FOR DATA ELABORATION

- '`mcxdettime.m`': to determine the time of flight of collected photons
- '`mcxdetweight.m`': to determine the weight of collected photons
- '`mcxdettpsf.m`': to reconstruct the output Time Point Spread Function (TPSF)



**ATTENTION: BUG!**

```
detp.ppath=detp.ppath(detp.detid==detnum,:);
```

```
detp.detid=detp.detid(detp.detid==detnum);
```

```
detp.w0=detp.w0(detp.detid==detnum); → MISSING IN OLD SOFTWARE VERSIONS!
```

# Voxel: MCXLAB

MCXLAB is a **voxel-based** photon simulator based on Matlab.

## REQUIRED

- `cfg.nphoton`: the total number of photons to be simulated (integer)
  - `cfg.unitinmm`: defines the length unit for a grid edge length
  - `cfg.vol`: a 3D array specifying the media index in the domain.
- **ATTENTION! Each subdomain is identified with a tag!**
- `cfg.prop`: [`mua`, `mus`, `g`, `n`]
- **ATTENTION!  $\text{mm}^{-1}$ ! `mus`, NOT `musp`!**
- `cfg.tstart`, `cfg.tstep`, `cfg.tend`: time-resolved curve features

## SOURCE-DETECTOR PARAMETERS

- `cfg.detpos`: [x, y, z, radius]
- `cfg.srcpos`, `cfg.srkdir`, `cfg.srctype`: source position, direction and type

## MC SIMULATION SETTINGS

- `cfg.seed`: seed for the random number generator (integer)

## GPU SETTINGS

- `cfg.autopilot`: 1-automatically set threads and blocks

## OUTPUT

- `cfg.outputtype`: 'flux' - fluence-rate, (default value)
  - 'fluence' - fluence integrated over time,
  - 'energy' - energy deposit per voxel
  - 'jacobian' or 'wl' - mua Jacobian
  - 'nscat' or 'wp' - weighted scattering counts

# Voxel: MCXLAB

## TIPS & TRICKS

Computational time

Output signal level

- Launch **many simulations with a limited number of input photons**, rather than a single simulation with a large amount of photons
- Launch **“absorption-free” simulations** and add *mua* a *posteriori*
- Take advantage of domain **symmetry** to create many **detectors** and increase output signal level

Example #2: Again, trilayer cylinder (Example #1)

BUT

with central source and ring detector ( $r = 1\text{mm}$ )

→ Try same/different seed

→ Try with/without absorption

→ Plot TPSF

## FUNCTIONS

- `mcxpreview`: domain plot
- `mcxlab`: launch simulation

## MATRIX DIMENSIONS

- Output: # collected photons, included “absorbed” ones  
    → **ATTENTION!**  
    Max #collected photons by default =  $1e6!!!$

# Voxel: MCXLAB



## DIY #2: Tumour in compressed breast

- Cube (xyz 6x6x4 cm<sup>3</sup>) with a central spherical inclusion ( $r = 1$  cm)

	Background (0)	Cube (1)	Sphere (2)
mua [mm <sup>-1</sup> ]	0	0.01	0.02
musp [mm <sup>-1</sup> ]	0	1.0	1.5
g	1	0.89	0.89
n	1	1.4	1.4

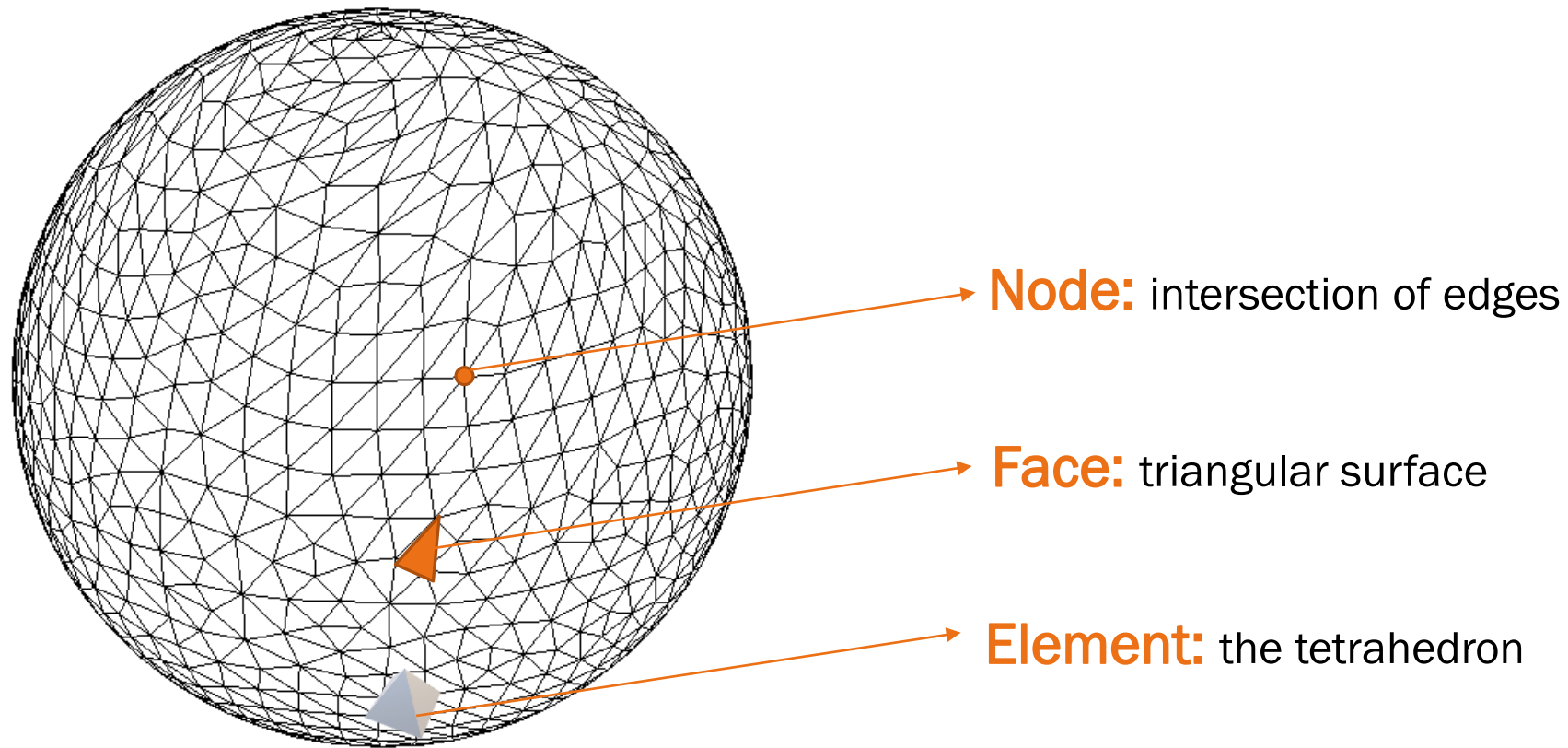
- Unit given in mm
- Transmittance geometry (source and detector aligned along z axis)
- Enable reflection at exterior boundary
- Enable reflection at interior boundary too
- Measure elapsed time (tic toc)
- Plot: fluence isolines (10 levels) at yz plane ( $x = X/2$ )

- Nphoton:  $10^8$
- Tstart: 0
- Tstep: 80 ps
- Tend: 14 ns
- Seed: random
- Detector area: 8 mm<sup>2</sup>
- GPU autopilot: 1
- Outputtype: fluence

# Mesh: MMCLAB

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MMCLAB utilizes a **tetrahedral mesh** to model complex anatomical structures.



# Mesh: MMCLAB - Iso2mesh

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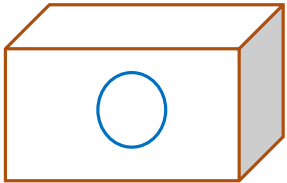
**iso2mesh** is a free Matlab/Octave-based mesh generation and processing toolbox.

It can create 3D tetrahedral finite element (FE) mesh from surfaces, 3D binary and gray-scale volumetric images such as segmented MRI/CT scans.



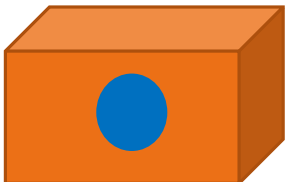
- `[node, face, elem]=meshabox (p0,p1,opt,nodesize)`

To create the surface and tetrahedral mesh of a box geometry



- `[newnode,newelem]=mergemesh (node,elem,varargin)`

To concatenate two or more tetrahedral meshes or triangular surfaces



- `[node,elem,face]=surf2mesh (v,f,p0,p1,keepratio,maxvol,regions,holes,forcebox)`

To create quality volumetric mesh from isosurface patches



# Mesh: MMCLAB

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## Example #3: Tumor in compressed breast

- Cube (xyz 6x6x4 cm<sup>3</sup>) with spherical inclusion ( $r = 1$  cm)

	Background (0)	Cube (1)	Sphere(2)
mua [mm <sup>-1</sup> ]	0	0.01	0.02
musp [mm <sup>-1</sup> ]	0	1.0	1.5
g	1	0.89	0.89
n	1	1.4	1.3

- Reflectance geometry: unit given by unitinmm

	x	y	z	R
Source	25	30	0	Pencil beam
Detector	35	30	2	2

- Nphoton:  $10^8$
- Tstart: 0
- Tstep: 25 ps
- Tend: 5 ns
- Detector:  $r = 4$  mm
- Seed: random
- Autopilot: 1
- Outputtype: TPSF, fluence

# Mesh: MMCLAB



## DIY #3: AT HOME

- Bilayer cylinder:  $R = 60$  mm,  $H_1 = 5$  mm,  $H_2 = 30$  mm

	Background (0)	Layer (1)	Layer (2)
$\mu_{\text{a}}$ [ $\text{mm}^{-1}$ ]	0	0.01	0.02
$\mu_{\text{s}}$ [ $\text{mm}^{-1}$ ]	0	1.0	1.5
$g$	1	0.89	0.89
$n$	1	1.4	1.4

- Reflectance geometry: unit given by unitinmm

	x	y	z	R
Source	35	30	0	Pencil beam
Detector	25	30	0	2

- $N_{\text{photon}}$ :  $10^8$
- $T_{\text{start}}$ : 0
- $T_{\text{step}}$ : 25 ps
- $T_{\text{end}}$ : 2 ns
- Detector:  $r = 2$  mm
- Seed: random
- Autopilot: 1
- Outputtype: fluence

# From mesh to voxel

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## USEFUL FUNCTIONS

- `[img, v2smap] = surf2vol(node, face, xi, yi, zi, varargin)`  
To convert a triangular surface to a shell of voxels in a 3D image
- `[mask weight] = mesh2vol(node, elem, xi, yi, zi)`  
To enable a fast rasterization of a 3D mesh to a volume with tetrahedron index labels
- How to load and plot existing `cfg`:  
`load cfg;`  
`mcxpreview(cfg);`

# Extra

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## OTHER TOOLS AVAILABLE

- **Photon replay:** It gives the possibility to retrace photon trajectories, obtaining photons' sensitivities (*i.e.* Jacobian) rather than weights.  
[Ruoyang Yao, Xavier Intes, Qianqian Fang\*, "A direct approach to compute Jacobians for diffuse optical tomography using perturbation Monte Carlo-based photon 'replay'," *Biomed. Optics Express* 9(10), 4588-4603, (2018)]
- **iMMC:** It incorporates both mesh- and shape-based tissue representations to create highly complex (e.g. dense vessel networks and porous tissues), yet memory-efficient light transport simulations.  
[Yaoshen Yuan, Shijie Yan, and Qianqian Fang\*, "Light transport modeling in highly complex tissues using the implicit mesh-based Monte Carlo algorithm," *Biomed. Optics Express*, 12(1), 147-161, (2021)]
- **SVMC:** Split Voxel MC is a hybrid algorithm combining meshes and voxels by means of the fast marching cubes method to greatly improve accuracy across curved boundaries while remaining highly flexible and efficient in parallel hardware.  
[Qianqian Fang\* and Shijie Yan, "Hybrid mesh and voxel based Monte Carlo algorithm for accurate and efficient photon transport modeling in complex bio-tissues" *J. of Biomedical Optics*, 11(11), 6262, 6270 (2020).]
- **DMMC:** Dual-grid mesh-based Monte Carlo to accelerate photon simulations using a coarsely tessellated tetrahedral mesh for ray-tracing computation and an independent voxelated grid for output data storage.  
[Shijie Yan, Anh Phong Tran, Qianqian Fang\*, "A dual-grid mesh-based Monte Carlo algorithm for efficient photon transport simulations in complex 3-D media," *J. of Biomedical Optics*, 24(2), 020503 (2019).]



# Thank you!

16<sup>th</sup> December 2021

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