

Macroeconomic Risks and Asset Prices

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Introduction: Traditional Macroeconomics and Asset Prices

Key Features of Standard Models:

- **Consumption-Based Pricing:** Asset prices reflect marginal utility of consumption (Lucas, Epstein-Zin).
- **Loglinear Euler Equation:**

$$x_t = f_x \mathbb{E}_t x_{t+1} + \rho_x x_{t-1} - \psi r_t$$

- **Fixed Preferences, Exogenous Shocks:** Time variation in risk premia requires exogenous volatility or recursive preferences.
- **Asset Return Co-movement:** Typically lacks microfoundations for changes in bond-stock correlation.

Innovations in Macroeconomic Asset Pricing:

- **Habit-Based Preferences:** Surplus consumption ratio $s_t = \frac{C_t - H_t}{C_t}$ drives time-varying risk aversion.
- **Exact Euler Equation:** Preferences consistent with standard macro loglinear structure.
- **Empirical Regime Shift:**
 - **Pre-2001:** Inflation-output gap correlation negative \Rightarrow bonds risky.
 - **Post-2001:** Correlation positive \Rightarrow bonds hedge assets.

Why Asset Risks Change:

- **Flight to Safety:** In recessions, increased risk aversion shifts demand to safe assets (bonds).
- **Risk Premia Amplification:** Time-varying premia strengthen bond-stock co-movement dynamics.
- **Quantitative Fit:** Model matches observed transition in bond-stock correlation (positive \rightarrow negative).
- **Policy Implication:** Structural macro changes (e.g., Fed reaction function) reshape asset risk profiles.

Two Streams in Macro-Finance:

- **Consumption-Based Asset Pricing (Lucas, 1978; Mehra-Prescott, 1985):**
 - Explains asset prices using marginal utility of consumption.
 - Cannot generate realistic equity premium or time-varying risk premia under smooth consumption.
- **Habit Formation (Campbell-Cochrane, 1999):**
 - Introduces surplus consumption ratio to induce endogenous risk aversion.
 - Powerful for equity volatility and predictability, but not naturally embedded in macro models.

Literature Review: New Keynesian Models and Macroeconomic Frictions

Key Ideas of the New Keynesian Approach:

- **Loglinear Euler Equation:**

$$x_t = f_x \mathbb{E}_t x_{t+1} + \rho_x x_{t-1} - \psi r_t$$

- **Nominal Rigidities:** Sticky prices and wages create real effects of monetary policy.
- **Monetary Rules:** Taylor rules guide central bank responses to inflation and output gaps.
- **Focus:** Business cycle dynamics, inflation targeting, but usually ignore asset prices.

Literature Review: How Macro Models Influence Asset Prices

Mechanisms Linking Macro to Markets:

- **Euler Equation as Pricing Kernel:** Determines real interest rate and discount factor.
- **Inflation and Output Risk:** Affect real payoffs of nominal assets (bonds).
- **Monetary Policy Regime:** Changes in policy reaction functions shift return dynamics.
- **Expectations Channel:** Bond prices reflect expectations of future inflation and policy.
- **Risk Premia Channel:** Surplus consumption dynamics feed back into required returns.

Framework of the Model

Goal: Integrate macroeconomic dynamics and asset pricing in a unified structure.

Three Building Blocks:

- **Preferences:** Habit formation à la CampbellCochrane, generating endogenous, time-varying risk aversion.
- **Macroeconomic Dynamics:** Loglinear, homoskedastic processes for the output gap, inflation, and the nominal interest rate.
- **Asset Pricing:** Bonds and stocks priced as claims on consumption; returns depend on macro state and surplus consumption.

Key Innovation: Preferences are designed to be consistent with an *exact* loglinear Euler equation a bridge between asset pricing and structural macro models.

Framework: Key Formulas of the Model

Preferences and Surplus Consumption:

$$U_t = \frac{(C_t - H_t)^{1-\gamma} - 1}{1-\gamma}, \quad S_t = \frac{C_t - H_t}{C_t}, \quad \text{RRA}_t = \frac{\gamma}{S_t}$$

Euler Equation (output gap version):

$$x_t = f_x \mathbb{E}_t x_{t+1} + \rho_x x_{t-1} - \psi r_t$$

Inflation and Interest Rate Laws of Motion:

$$\pi_t = b_{\pi x} x_{t-1} + b_{\pi \pi} \pi_{t-1} + b_{\pi i} i_{t-1} + \varepsilon_t^\pi$$

$$i_t = b_{ix} x_{t-1} + b_{i\pi} \pi_{t-1} + b_{ii} i_{t-1} + \varepsilon_t^i$$

Bond Pricing Recursion:

$$P_t^n = \mathbb{E}_t \left[M_{t+1} e^{-\pi_{t+1}} P_{t+1}^{n-1} \right],$$

Risk Premia Driven by Surplus Consumption:

- Time-varying risk premia arise from variation in the surplus consumption ratio S_t :

$$\text{RRA}_t = \frac{\gamma}{S_t}, \quad \text{so higher risk aversion when } S_t \downarrow$$

Stock Risk Premium:

$$\mathbb{E}_t[R_{t+1}^{\text{stock}} - r_t] + \frac{1}{2} \text{Var}_t(R_{t+1}^{\text{stock}}) = \gamma(1 + \lambda(S_t))\sigma_x^2$$

- Positively related to output gap volatility and surplus sensitivity.

Bond Risk Premium (e.g. 2-period nominal bond):

$$\mathbb{E}_t[R_{t+1}^b - r_t] + \frac{1}{2} \text{Var}_t(R_{t+1}^b) = \gamma(1 + \lambda(S_t)) \cdot \text{Cov}_t(x_{t+1}, -i_{t+1} - \pi_{t+1})$$

Framework: Calibration and Estimation Strategy

Objective: Match model-implied moments to empirical moments using Simulated Method of Moments (SMM).

Parameter Vector:

$$\theta = [b_{\pi x}, b_{\pi\pi}, b_{\pi i}, b_{ix}, b_{i\pi}, b_{ii}, \sigma_{\pi}, \sigma_i, \sigma^*, \rho_{\pi i}, \rho_{\pi^*}, \rho_{i^*}]$$

Objective Function:

$$W(\theta) = \left(\hat{\Psi} - \Psi(\theta) \right)^{\top} \hat{W} \left(\hat{\Psi} - \Psi(\theta) \right)$$

- $\hat{\Psi}$: vector of empirical moments
- $\Psi(\theta)$: vector of model-implied simulated moments
- \hat{W} : weighting matrix (diagonal, inverse variances)

Targeted Moments:

- Impulse responses (VAR) for x_t, π_t, i_t
- Correlation between 20-quarter average Fed Funds rate and output gap

Enhancing SMM Calibration with Machine Learning:

1. Neural Network Surrogate Model

- Approximates the mapping $\theta \mapsto \Psi(\theta)$ using a feedforward neural network trained on simulated data.
- Allows fast evaluation of moments without solving the full model each time.
- Facilitates gradient-based optimization in high-dimensional parameter space.

2. Bayesian Optimization

- Global optimization method using probabilistic surrogate (e.g., Gaussian process).
- Efficiently explores the parameter space with few evaluations.
- Balances exploration (new areas) and exploitation (known good fits).

Asset Pricing Successes:

- **Stocks:** Realistic Sharpe ratios and excess return volatility.
- **Bonds:** Positive bond-stock correlation in period 1, negative in period 2.
- **Risk Premia:** Endogenous and nonlinear; respond to surplus consumption dynamics.

Macroeconomic Dynamics:

- Captures switch in inflation-output gap correlation (negative positive).
- Smooth and hump-shaped impulse responses to interest rate shocks.
- Matches long-term Fed Funds output gap correlation across regimes.

Estimation Insights:

- Two subperiods: 1979Q3-2001Q1 and 2001Q2-2011Q4.
- Break in inflation-output gap cyclicalities validated by QLR tests.
- Lag parameters (especially b_{ix}) drive regime shift in bond risk.

Key Estimates:

- Period 1: Bonds *risky*, positively correlated with stocks.
- Period 2: Bonds *hedged*, negatively correlated with stocks.
- Time-varying stock and bond risk premia explain 70-80% of the shift in bond-stock correlation.

Conclusion: The SMM-calibrated model explains asset return regime shifts using only macro targets.

Post-Estimation: ML-Based Calibration Results

Goal: Evaluate whether ML methods improve or confirm SMM-based calibration.

Using Machine Learning Methods:

- **Neural Network Surrogate:** Improved the speed of moment evaluations significantly.
- **Bayesian Optimization:** Found better-fitting parameter regions under fewer simulations.

Results:

- Slightly better match to long-horizon Fed Funds output gap correlation.
- Improved fit to the bond return variance and bond-stock beta in period 2.
- Reduced numerical instability in asset pricing recursion for low surplus states.

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All data, code, and calibration tools used in this presentation are freely available at:

[github.com/andrealandini/
Empirical-Asset-Processing-Project2025](https://github.com/andrealandini/Empirical-Asset-Processing-Project2025)

Includes:

- Replication data (macro series, impulse responses, returns)
- Calibration code (SMM + machine learning)
- Presentation slides and LaTeX source

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Thanks for your attention.

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