

Answer to Beal's Conjecture

Abstract

This paper, tends to solve the Beal's Conjecture, using all possible combinations, on the three variables (A,B,C). Since A^x , B^y and C^z in terms of getting the common prime are treated like A (without the exponent), B and C. Since A^x can be treated as $A*A*A$, the same prime factors of A that apply to $A*A*A$, are the same. Having concluded that, we can use A instead of A^x . Then its just a matter of testing all hipotesys, to all A,B,C test if each is prime or nonprime. For example for $A=2$, then $A^3 = 2*2*2$, which has a prime factor of 2. There aren't different factors of the numbers, because its the same number that is elevated to exponent

Beal's conjecture

If $A^x + B^y = C^z$, where A, B, C, x, y and z are positive integers and x, y and z are all greater than 2, then A, B and C must have a common prime factor.

Solution

Since A^x will have the same primes factor as A, we only consider A

If A, B and C are equal its impossible, because $A+B = C$ cant be equal to C

If there is a prime on the equation then

$$a) \text{PrimeA} + \text{NonPrimeB} = C$$

The only possible common prime factor in a) is PrimeA (since it only has one factor)

So C doesnt have PrimeA as possible common prime factor

$$b) \text{PrimeA} + \text{PrimeB} = C$$

two different primes, C cant be equal to either PrimeA or PrimeB (since its a sum), and hence can't share a prime common factor

c) $\text{Prime A} + \text{NonPrimeB} = \text{PrimeC}$

two different primes (because is $\text{PrimeA} + \text{something}$, so they are different)

d) $\text{NonPrimeA} + \text{NonePrimeB} = \text{PrimeC}$

PrimeC can't be decomposed in sum of two non primes

So, A,B,C must be NonPrimes (to have a common prime factor)

Hipothese

$$\text{NonPrime1} + \text{NonPrime2} = \text{NonPrime3}$$

1) If NonPrime1 e NonPrime2 have common prime factors then NonPrime3 also has common prime factors

If we did have a common factor, in this case 3, then that could be put in evidence as in:

$$2*3 + 3*7 = 27$$

$$3(2+7) = 27$$

and its assured that 3 divides 27,so 3 is a prime common number

2) If they don't have common prime factors, then they don't share a common prime

Therefore $A^x + B^y = C^z$, doesnt hold, for example if A is prime.

Keywords

Beal's conjecture,divisors,primes,multiple

Palavras Chave:

conjeture de beals,primos,divisores,multiple

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