

# 9 Matlab Tricks that You Probably Want to Know

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Gatsby Tea Talk

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## 1. Matrix storage is column-major order

- Physical memory is linear.
- To store a multi-dimensional array, need to arrange it linearly.

Matlab:

- $A = \begin{pmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{pmatrix} \in \mathbb{R}^{r \times c}$  is internally stored as  $(1, 2, 3, 4, 5, 6)^\top$  (column-major).

Tricks/Facts:

- $A(1, 2) == 3$ . Can also use **linear index**.  $A(3) == 3$
- To flatten  $A$ , do  $A(:) == (1, 2, 3, 4, 5, 6)^\top$ . Get a column vector.
- Internally, Matlab does  $A((j-1)r + i)$  for  $A(i, j)$ .
- C/C++, Python use row-major order.

## 2. Set diagonal elements

### Task:

■  $A = \begin{pmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{pmatrix} \in \mathbb{R}^{r \times r}$ . Want to set the diagonal to 0.

■ Don't want to use (slow)

```
for i=1:r
    A(i, i) = 0;
end
```

### Tricks:

- Use linear indexing.  $A(1 : (r + 1) : \text{end}) = 0$ .
- "end" == 9.
- $1 : (r + 1) : \text{end} == 1 : 4 : 9 == [1, 5, 9] ==$  indices of the diagonal elements.

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### 3. reshape

`reshape(..)` is used to change the shape of an array.

- Read elements in linear order (column-wise).

- $A = \begin{pmatrix} 1 & 3 & 5 \\ 2 & 4 & 6 \end{pmatrix}$

- `reshape(A, 1, 6) == (1, 2, 3, 4, 5, 6)`. Row vector.

- `reshape(A, 3, 2) ==`  $\begin{pmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{pmatrix}$ .

- `reshape(A, 3, 3)`. Get an error.

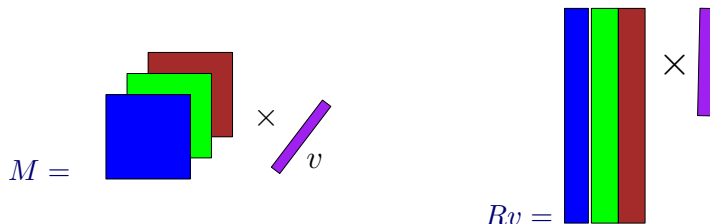
- `reshape(A, 3, 2) == reshape(A(:), 3, 2)`

- `reshape(..)` is computationally very cheap.

## 4. Weighted average on a 3D array

### Task:

- $T \in \mathbb{R}^{r \times c \times d}$ , a 3d array e.g.,  $d$  images of size  $r \times c$ .
- $v \in \mathbb{R}^d$ , a weight vector.
- Want to multiply to get  $M = \sum_{i=1}^d T(:, :, i) * v(i) \in \mathbb{R}^{r \times c}$ .



- Do not want to use a loop.

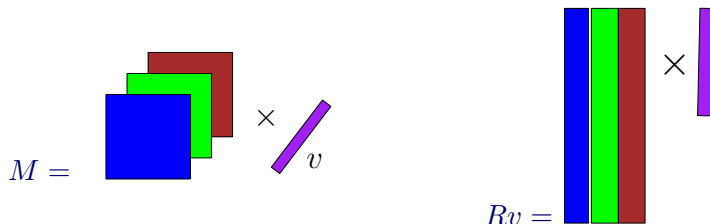
### Tricks

- Use reshape
- $R = \text{reshape}(T, r * c, d)$
- $M = \text{reshape}(R * v, r, c)$

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### Tricks

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## 5. Minimum element of a multi-dimensional array

### Task:

- $E \in \mathbb{R}^{r \times c \times d}$  e.g., validation errors of param.1  $\times$  param.2  $\times$  param.3
- Find the minimum error, and the corresponding three parameters.

### Problem:

- Matlab's **min** operates along one dimension.
- Tedious to find min three times.

### Tricks:

```
[minerr, ind] = min(E(:));  
[p1_ind, p2_ind, p3_ind] = ind2sub(size(E), ind);
```

- Flatten the array  $E(:)$ . Find min and its linear index (ind).
- Convert the linear index back to the subscript index.



## 6. $\text{tr}(A^\top B)$

### Task:

- $A, B \in \mathbb{R}^{m \times n}$ . Want  $\text{tr}(A^\top B)$ .
- Inefficient to compute  $A^\top B$  and take the trace.

### Tricks:

- Let  $A := (\mathbf{a}_1 | \cdots | \mathbf{a}_n)$  and  $B := (\mathbf{b}_1 | \cdots | \mathbf{b}_n)$ .

$$\begin{aligned}\text{tr}(A^\top B) &= \text{sum}(\text{diag}(A^\top B)) \\ &= \sum_{j=1}^n \mathbf{a}_j^\top \mathbf{b}_j = \sum_{j=1}^n \sum_{i=1}^m a_{ij} b_{ij} \\ &= \text{sum}(\text{sum}(A .* B)) \\ &= A(:)' * B(:) \text{ in Matlab}\end{aligned}$$

- $\text{trace}(A' * B)$  costs  $O(mn^2)$ .
  - Compute  $A' * B$ . Then, throw away off-diagonal entries.
- $A(:)' * B(:) = \text{sum}(\text{sum}(A .* B))$  costs  $O(mn)$ .

## 7. log-sum-exp trick (not specific to Matlab)

- Want  $r^{(k)} = \frac{\prod_{d=1}^D p_d^{(k)}}{\sum_{k'=1}^K \prod_{d=1}^D p_d^{(k')}} \text{ where } p_d^{(k)} \in (0, 1) \text{ and } D \text{ is big.}$
- Example: Posterior probability of the  $k^{th}$ -component of a mixture of Bernoulli.

### Problem:

- $\prod_{d=1}^D p_d^{(k)}$  leads to numerical underflow. Try `prod(rand(1, 1000))`.

### Tricks:

- 1 Store log prob.  $\log r^{(k)} = \sum_d \log p_d^{(k)} - \log \sum_{k'} \prod_d p_d^{(k')}$
- 2 Introduce  $c$

$$\begin{aligned} \log \sum_{k'} \prod_d p_d^{(k')} &= \log \exp(c) + \log \exp(-c) + \log \sum_{k'} \exp \left( \log \prod_d p_d^{(k')} \right) \\ &= c + \log \sum_{k'} \exp \left( \sum_d \log p_d^{(k')} - c \right), \end{aligned}$$

choose  $c$  so that  $\exp \left( \sum_d \log p_d^{(k')} - c \right) > 0$ .

- 3 One way is  $c := \max_{k'} \sum_d \log p_d^{(k')} < 0$ .

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## 8. bsxfun and repmat

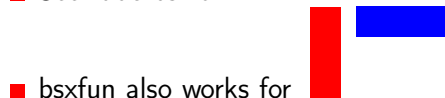
### Task:

- $A \in \mathbb{R}^{m \times n}, v \in \mathbb{R}^m$ .
- Want  $B = f(A, v)$  ( $f$ : element-wise) such that  $B_{ij} = f(A_{ij}, v_i)$ .
- Example: Subtract mean from each column.

### Tricks:



- Trick 1:  $f(A, \text{repmat}(v, [1, n]))$
- Trick 2:  $\text{bsxfun}(@f, A, v)$ 
  - Same effect as Trick 1 without replicating  $v$ . Memory efficient.
- $\text{bsxfun}$  can only take in simple  $f$ 
  - $f \in \{ @plus, @minus, @times, @max, @eq, \dots \}$ , not any arbitrary  $f$
- See “doc bsxfun”.



- $\text{bsxfun}$  also works for .

## 9. Embarrassingly parallel for-loop

- Want to run an embarrassingly parallel for-loop on multiple machines.
- Example: `validation_error( $\theta_i$ )` for  $i$  in a long list.

### Tricks:

- Download Multicore package (open source).

<http://uk.mathworks.com/matlabcentral/fileexchange/13775-multicore-parallel-processing-on-multiple-cores>

- Master/slave machines need to share **temp\_dir** for passing information.
- On slave Matlab's, run

```
startmulticoreslave(temp_dir);
```

- On the master,

```
v_error_func = .. (some func. of theta) ..  
thetas = {t1, t2, ...}  
resultCell = startmulticoremaster(v_error_func, thetas, setting);
```

- `resultCell{i}` == validation error of  $\theta_i$ .
- Master/slave machines can be on the same or different machines. Need to share the same file system. Work at Gatsby.
- Should launch slave Matlab's through the job queue (slurm).

## References I