



Compliance to the code of conduct

I hereby assure that I solve and submit this exam myself under my own name by only using the allowed tools listed below.

Signature or full name if no pen input available

Distributed Systems

Exam: IN2259 / DS Final

Date: Thursday 25th February, 2021

Examiner: Prof. Dr. Hans-Arno Jacobsen

Time: 16:30 – 17:45

Working instructions

- This exam consists of **14 pages** with a total of **8 problems**.
Please make sure now that you received a complete copy of the exam.
- The total amount of achievable credits in this exam is 100 credits.
- Detaching pages from the exam is prohibited.
- Allowed resources:
 - The exam is an open book, and course materials are allowed to be used.
 - **Any collaboration is cheating and will be reported to administrations!**
- Unless stated differently, please use the algorithms that have been introduced in the lecture or the tutorial.
Self-defined algorithms may reduce the awarded credits.
- **Do not write with red or green colors.**

Left room from _____ to _____ / Early submission at _____



☐ Exam empty





Problem 1 Logical Clocks (19.5 credits)

Consider a distributed system consisting of five processes. These processes broadcast messages among themselves and make use of logical clocks of $\{V_A, V_B, V_C, V_D, C_E\}$ for timestamping the messages.

a) For each process, determine the value of the logical clock at the **end** of the time/event diagram according to the **Vector Clock** algorithm. Only write the final value of clocks in the table below. All clocks **must** be initialised with zero.

0

1

2

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4

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6

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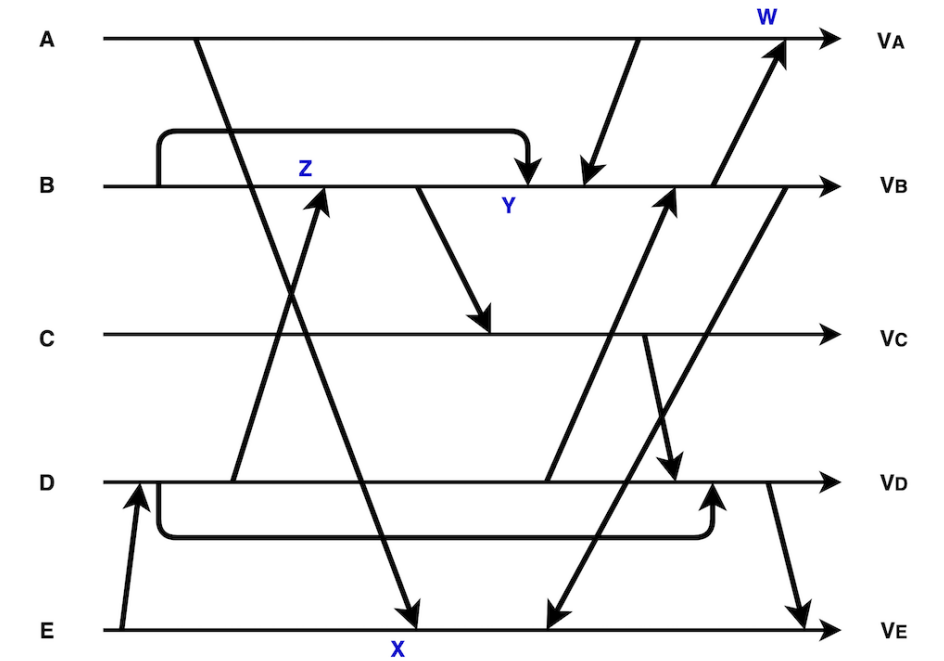
8

9

10

11

12



	1st Element	2nd Element	3rd Element	4th Element	5th Element
V_A					
V_B					
V_C					
V_D					
V_E					

b) Using the results of the previous task, **show and prove** whether the happened-before relationship (\rightarrow) between the following event pairs holds or events are concurrent (||). The events are marked on the time/event diagram.

1. (X, Y)

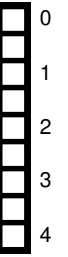
2. (Y, Z)

3. (X, W)





c) Consider the following distributed algorithm to implement causal-ordered (CO) broadcast. L_i denotes the Lamport clock value at process P_i . *B-Broadcast* and *B-Deliver* denote the corresponding two basic primitives. Read the algorithm and answer the questions below.



CO-Broadcast at Process P_i :

On Initialisation:

$L_i := 0$

To CO-Broadcast message M :

$L_i := L_i + 1$

B-Broadcast($\langle L_i, M \rangle$)

On B-Deliver($\langle L_j, M \rangle$) *from* P_j ($j \neq i$):

Place $\langle L_j, M \rangle$ in hold-back queue

Wait until $L_j = L_i + 1$

Remove message from queue and *CO-Deliver* M

$L_i := L_i + 1$

1. This algorithm cannot satisfy the requirements of the causal-ordered broadcast. What is the reason for that?

2. Give a hint for fixing this algorithm so that the requirements of the causal-ordered broadcast are addressed.





Problem 2 Leader Election / Time Adjustment (12 credits)

Consider a distributed system consisting of eight processes of $\{P_1, P_2, P_3, P_4, P_5, P_6, P_7, P_8\}$. Answer the following questions.

0 ☐

1 ☐

2 ☐

3 ☐

4 ☐

a) Process P_1 and P_3 suspect the demise of network's leader. Both processes simultaneously initialize a leader election based on **Bully Algorithm**. Explain the procedure for electing the leader and determine which process will be elected to be the network's new leader.

0 ☐

1 ☐

2 ☐

3 ☐

4 ☐

b) The newly elected leader performs a clock synchronization round using the **Berkeley Algorithm**. The threshold value for acceptable deviation is $\delta = \pm 2000ms$. Show what times are selected for calculating T_{ref} and what reference time T_{ref} does the leader calculate for synchronization?

Process	Local Time (hh:mm:ss:fff)
P_1	11:10:41:000
P_2	11:10:48:000
P_3	11:10:40:000
P_4	11:10:39:000
P_5	11:10:47:000
P_6	11:10:37:000
P_7	11:10:34:000
P_8	11:10:40:000





c) Based on the calculated T_{ref} time, what values does the leader calculate and send to other processes? Fill in the table below.

0

1

2

3

4

Process	Value
P_1	
P_2	
P_3	
P_4	
P_5	
P_6	
P_7	
P_8	





Problem 3 MapReduce (8 credits)

Formulate the below algorithm for MapReduce. Explain how the input is mapped into **(key, value)** pairs, i.e., specify what is the key and what is the associated value in each pair, and, if needed, how the key(s) and value(s) are computed. Then, explain how the **(key, value)** pairs produced by the map stage are processed by the reduce stage to get the final result.

0 ☐ Consider a set of documents (each with a documentID and a documentContent), where the content consists of a
1 ☐ list of words. Provide a MapReduce program that generates a list of locations (word position in the documentID) for
2 ☐ each word occurrence:

3 **File Content:**

4 Document1 : {Word1 Word2 Word1 Word3}
5 Document2 : {Word4 Word2 Word4 Word2 Word1}
6 documentId documentContent

7 **Final Output:**

8 Word1: {Document1 : [1, 3], Document2 : [5]}
Word2: {Document1 : [2], Document2 : [2, 4]}
Word3: {Document1 : [4]}
Word4: {Document2 : [1, 3]}

1. **Map:** What does the map function do?

2. **Map Input:** Define the Map input in the **(key, value)** format.

3. **Map Output:** Define the Map output in the **(key, value)** format.

4. **Reduce:** What does the reduce function do?

5. **Reduce Input:** Define the Reduce input in the **(key, value)** format.

6. **Reduce Output:** Define the Reduce output in the **(key, value)** format.





Problem 4 Consistency Models (18 credits)

a) Consider the execution depicted in Figure 4.1. Is it **linearizable** (Yes/No)? Is it **sequentially consistent** (Yes/No)? For both questions, if yes, valid execution sequences **must** be written. If no, explain. (Hint: a Yes without providing the sequence or a No without explanation, is zero point for every part.)

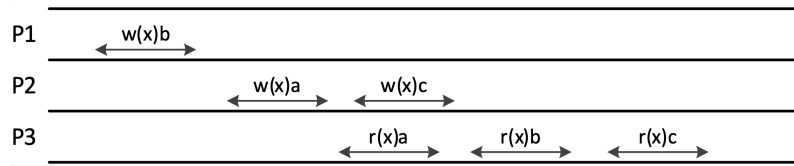


Figure 4.1: Execution.

b) Consider the execution depicted in Figure 4.2. Is it **linearizable** (Yes/No)? Assuming each operation is performed at the start of its time interval, is it **strictly consistent** (Yes/No)? For both questions, if yes, valid execution sequences **must** be written. If no, explain.

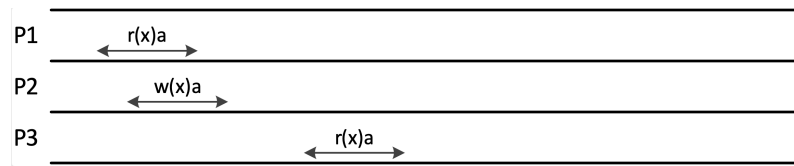


Figure 4.2: Execution.

c) Consider the execution depicted in Figure 4.3. Is the execution **sequentially consistent** (Yes/No)? Is it **causally consistent** (Yes/No)? For both questions, if yes, valid execution sequences **must** be written. If no, explain.

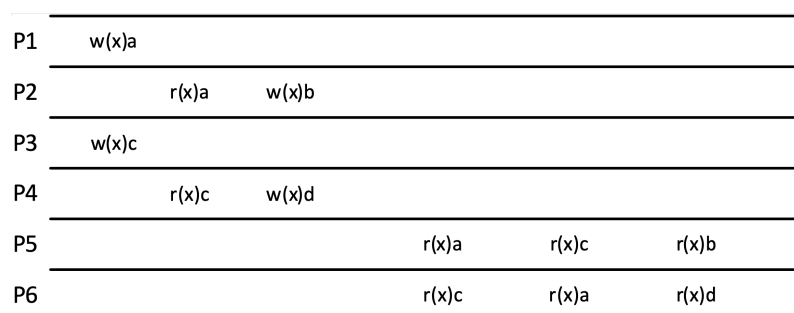


Figure 4.3: Execution.





0

1

2

3

d) Is the execution depicted in Figure 4.4 **sequentially consistent** (Yes/No)? Is it **causally consistent** (Yes/No)? For both questions, if yes, valid execution sequences **must** be written. If no, explain.

P1	w(x)a	r(x)b
P2	w(x)b	r(x)a

Figure 4.4: Execution.

0

1

2

e) Is the execution depicted in Figure 4.5 **FIFO consistent** (Yes/No)? Is it **causally consistent** (Yes/No)? For both questions, if yes, valid execution sequences **must** be written. If no, explain.

P1	w(x)a	w(x)b	
P2	w(x)c	r(x)b	r(x)a
P3		r(x)a	

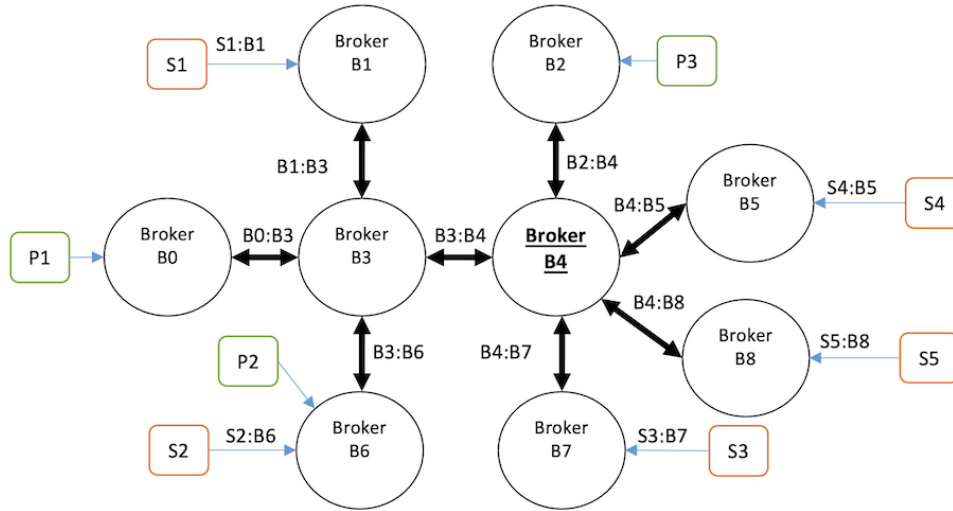
Figure 4.5: Execution.





Problem 5 Publish/Subscribe (10.5 credits)

Consider an overlay broker network based on a **rendezvous-based routing model** containing nine brokers, as demonstrated in the figure below. Consider all subscribers are already subscribers and stored in the **Rendezvous Broker B4** which uses Bloom filters. Also, each link has a unique ID. Answer the following questions.



a) Publisher **P3** creates a publication that matches the subscriptions of **S1** and **S3**. Specify which links are added to the bloom filter.

b) The rendezvous broker creates a bloom filter of size 16 for routing the matching publications. The table below contains the hashed value of each link using four hash functions. The bloom filter uses all four hash functions in the order when inserting and looking up values.

Publisher **P3** creates a publication that matches the subscription of **S1**. The rendezvous broker adds the links required for delivering the publication to the bloom filter below. Show the effect of adding the links to the bloom filter by filling in the vector below.

Edge	H_1	H_2	H_3	H_4
B0:B3	14	15	1	10
B1:B3	9	1	7	12
B2:B4	10	2	11	16
B3:B4	8	14	16	7
B3:B6	6	15	9	10
B4:B5	2	15	3	14
B4:B7	4	13	2	12
B4:B8	2	7	15	5
S1:B1	16	11	8	2
S2:B6	9	7	13	15
S3:B7	10	4	9	2
S4:B5	4	7	6	15
S5:B8	15	7	14	2

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16

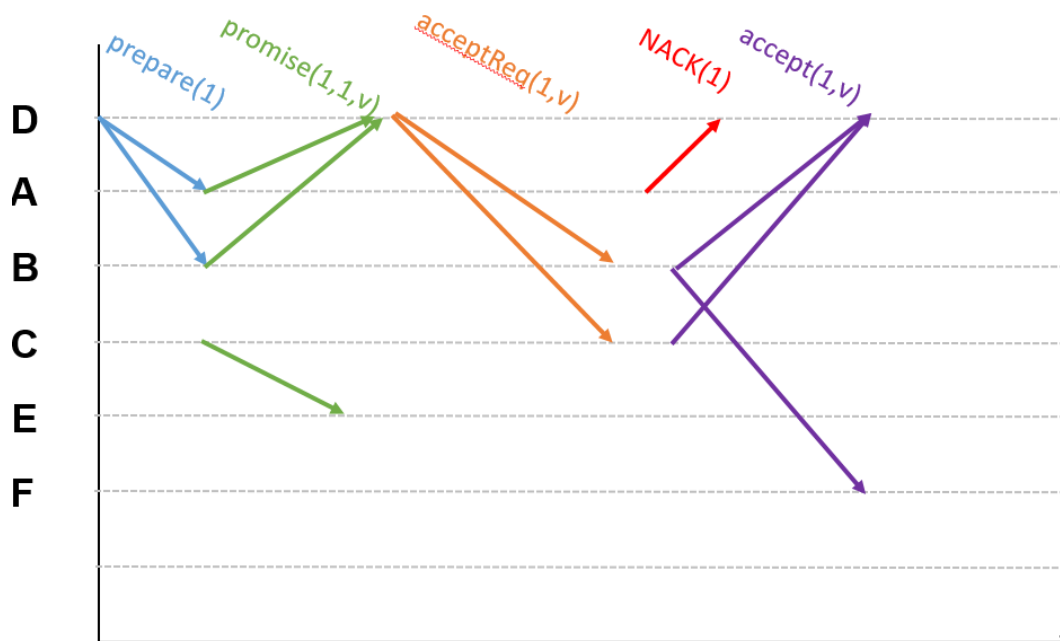




Problem 6 Paxos (6 credits)

0 ☐
1 ☐
2 ☐
3 ☐
4 ☐
5 ☐
6 ☐

The figure below shows the execution of Basic Paxos with two proposers (D, E), three acceptors (A, B, C), and one learner (F). This diagram contains precisely four mistakes that are not allowed in Basic Paxos. Identify them and write them below.





Problem 7 Peer-To-Peer Systems (16 credits)

a) Consider the Pastry network, where every node ID $\in \{0, 1, 2, 3, 4\}^5$ and is represented by a 4-digit string. The network contains the following nodes:

{ 0014, 0100, 0103, 0202, 0213, 0231, 0322, 0431, 1041, 1111, 1243, 1341, 1432, 2030, 2230, 2323, 2402, 2413, 3010, 3113, 3133, 3240, 3302, 3343, 3424, 4004, 4030, 4133, 4201, 4331, 4341, 4414 }

Complete the routing table of node **2323** and **3010** in the table below:

Table 7.1: Routing Table **2323**

RT	0	1	2	3	4
0					
1					
2					
3					

Table 7.2: Routing Table **3010**

RT	0	1	2	3	4
0					
1					
2					
3					





0

1

2

3

b) Let C be the Chord ring given in the figure below. The network contains several peers, each of which was mapped to a node $N_i \in C$ by a uniform hash function with bit-string length $m = 7$. Consider the standard Chord implementation where peer nodes store a finger table. Fill in the finger table of the peer at node **N115**:

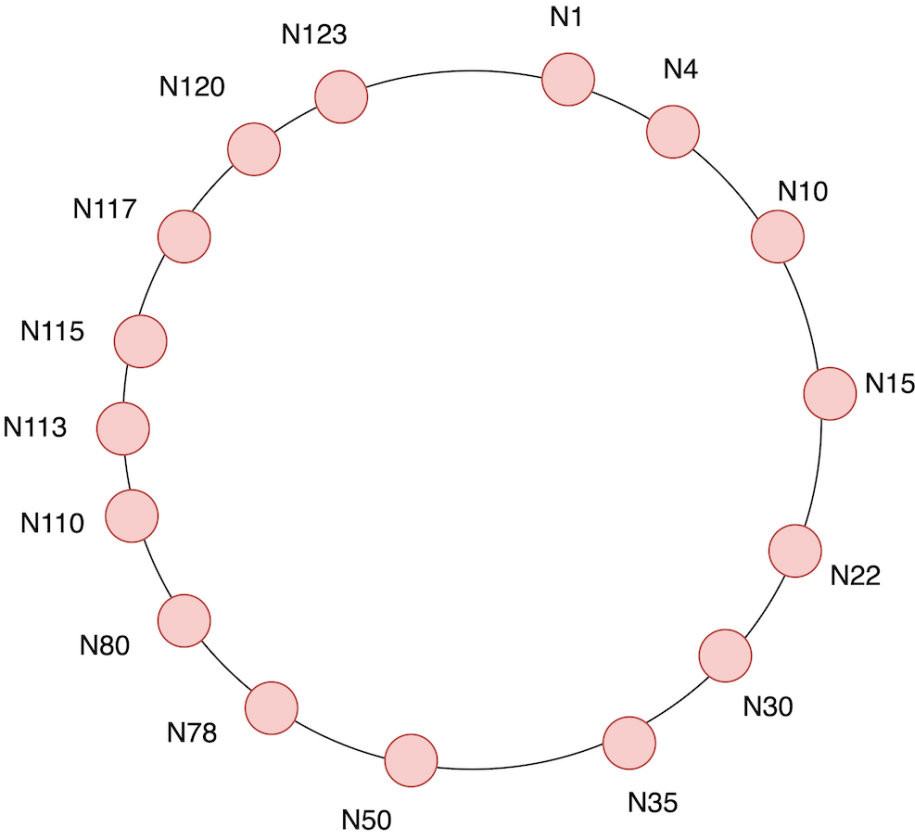


Table 7.3: Finger Table **N115**

Peer ID	Successor





Problem 8 Short Answers (10 credits)

a) Consider a distributed system that uses gossiping for lazy replication. According to the CAP theorem, what is this system called?

0
1
2

b) Consider a Byzantine general's problem with five faulty processes. What is the minimum number of processes to reach the consensus based on Lamport's original solution?

0
1

c) Given 10 data pieces and 10 parity pieces, how many failures does a Reed-Solomon encoding tolerate?

0
1

d) Conflict-Free Replicated Data Sets are used to provide what type of consistency?

0
1
2

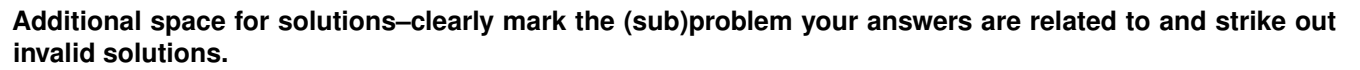
e) Which theoretical property does Paxos NOT guarantee?

0
1
2

f) Consider a cryptocurrency that operates like Bitcoin, and the reward for mining a block is 50 coins, and each block contains 200 transactions with an average fee of 0.5 coins for each transaction. What is the total gain for mining a block?

0
1
2



This image shows a full page of blank graph paper. The grid consists of small, equal-sized squares formed by thin, light gray lines. The grid covers the entire area of the page, leaving no margins or other markings. There are 20 columns and 20 rows of squares, creating a total of 400 square units.