

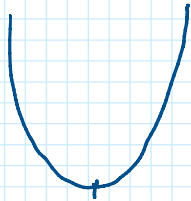
$$\vec{y} = A \vec{x} = \sum_j A_{ij} x_j$$

$$y_i = (A \vec{x})_i = \sum_j A_{ij} x_j$$

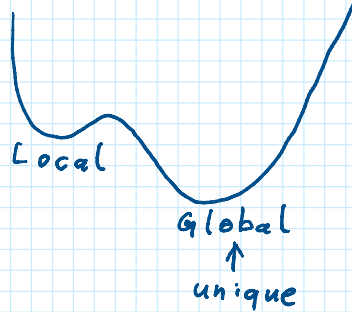
$$C = AB \Leftrightarrow C_{ik} = \sum_j A_{ij} B_{jk}$$

$\begin{matrix} \text{H} \\ B A \end{matrix}$
 $\begin{matrix} \text{H} \\ \sum_j B_{jk} A_{ij} \end{matrix}$

i) Convex

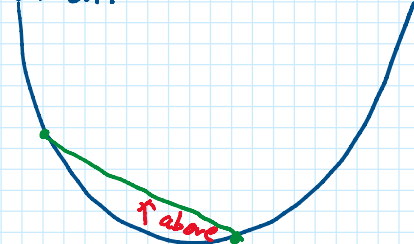


Non-convex

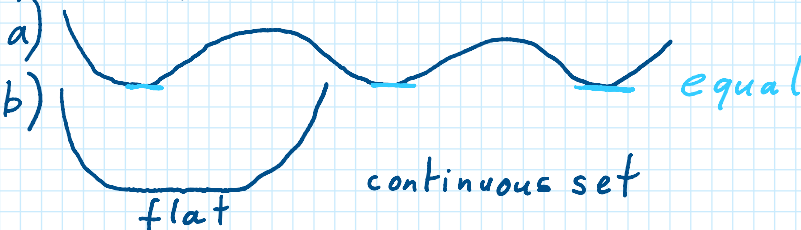


Convexity

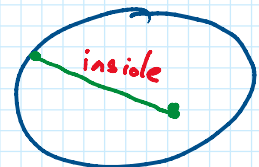
Function:



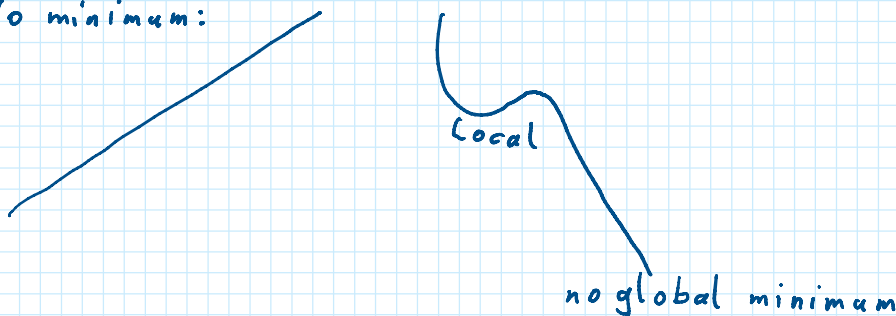
ii) Non-unique optima:



Set:



iii) No minimum:



Random variables A, B, C

$$p(a|b,c) = p(A=a|B=b, C=c)$$

$$p(a) = p_A(a)$$

$$p(a) = p(A=a)$$

Sum rule

$$p(a) = \sum_b p(a,b)$$

$$p(\text{sick}) = p(\text{sick}|\text{pan})p(\text{pandemic}) + p(\text{sick}|\neg\text{pandemic})p(\neg\text{pandemic})$$

Product rule

$$p(a,b) = p(a|b)p(b), \text{ if } a \& b \text{ independent: } p(a,b) = p(a)p(b)$$

Product rule

$p(a, b) = p(a|b)p(b)$, if a & b independent: $p(a, b) = p(a)p(b)$
 $\Rightarrow p(a|b) = p(a)$

$$p(a|b, c) = p(a|b \cap c) = p(\underbrace{A=a}_{\text{event}} | \underbrace{B=b \cap C=c}_{\text{random variable (discrete or continuous)}})$$

value
↓
↑
random variable (discrete or continuous)

What if $p(b, c) = 0$?

$$p(a, b, c) = p(a|b, c)p(b, c)$$

↓ ↓ ↓
0 ill defined 0