

Machine Learning for Graphs and Sequential Data

Deep Generative Models - Summary

Lecturer: Prof. Dr. Stephan Günnemann
www.daml.in.tum.de

Summer Term 2020

Data Analytics and
Machine Learning 

Roadmap

- Chapter: Deep Generative Models
 1. Introduction
 2. Normalizing Flows
 3. Variational Inference
 4. Generative Adversarial Networks
 5. **Summary**

Generating New Samples

- Normalizing flows

1. Sample $\mathbf{z} \sim p(\mathbf{z})$
2. Compute $\mathbf{x} = f_{\theta}(\mathbf{z})$

$p(\mathbf{z})$ is the base distribution

f_{θ} is an invertible transformation

- Variational Autoencoder

1. Sample $\mathbf{z} \sim p(\mathbf{z})$
2. Compute $\boldsymbol{\theta} = f_{\psi}(\mathbf{z})$
3. Sample $\mathbf{x} \sim p_{\theta}(\mathbf{x}|\mathbf{z})$

$p(\mathbf{z})$ is the prior on \mathbf{z}

f_{ψ} is the decoder

$p_{\theta}(\mathbf{x}|\mathbf{z})$ is the predefined conditional likelihood

- Generative Adversarial Network

1. Sample $\mathbf{z} \sim p(\mathbf{z})$
2. Compute $\mathbf{x} = f_{\theta}(\mathbf{z})$

$p(\mathbf{z})$ is the noise distribution

f_{θ} is the generator network

Likelihood Computation

- Normalizing flows
 - Use the change of variables formula

$$p_{\theta}(x) = p\left(f_{\theta}^{-1}(x)\right) \left| \det \left(\frac{\partial f_{\theta}^{-1}(x)}{\partial x} \right) \right|$$

- Variational Autoencoder
 - Marginalize out the latent variable

$$p_{\theta}(x) = \int p_{\theta}(x|z)p(z)dz$$

- Generative Adversarial Network
 - Compute partial derivatives of the CDF of x

$$p_{\theta}(x) = \frac{\partial}{\partial x_1} \dots \frac{\partial}{\partial x_d} \int_{\{f_{\theta}(z) \leq x\}} p(z)dz = \frac{\partial}{\partial x_1} \dots \frac{\partial}{\partial x_d} \Pr(f_{\theta}(z) \leq x)$$

Optimization Objective

- Normalizing Flows (for density estimation)

- Maximum likelihood

$$\max_{\theta} \log p_{\theta}(x)$$

- Variational Autoencoder

- Evidence Lower BOund (ELBO)

$$\max_{\psi, \lambda} \mathbb{E}_{z \sim q_{\phi}(z)} [\log p_{\theta}(x|z) + \log p(z) - \log q_{\phi}(z)]$$

where $\phi = g_{\lambda}(x)$ and $\theta = f_{\psi}(z)$

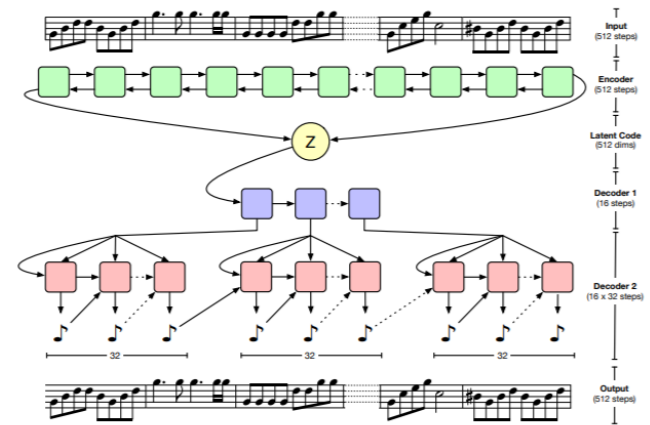
- Generative Adversarial Network

- Minimax optimization of ratio loss & generative loss

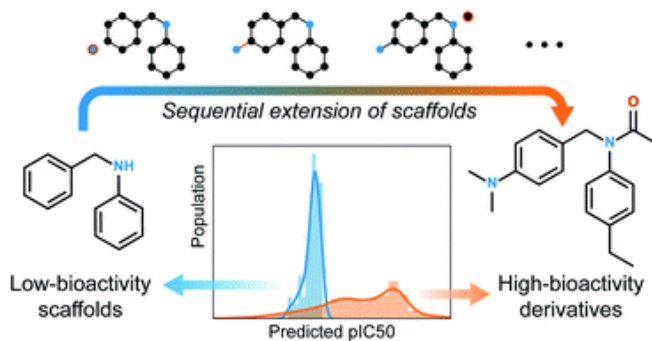
$$\min_{\theta} \max_{\phi} \pi \mathbb{E}_{p^*(x)} [\log D_{\phi}(x)] + (1 - \pi) \mathbb{E}_{p(z)} [\log [1 - D_{\phi}(f_{\theta}(z))]]$$

Outlook

- (Deep) Generative models are seen as a promising approach towards "understanding the world"
- Some applications require conditional generation, i.e. modeling $p_{\theta}(x|y)$
 - [Missing data imputation](#)
 - ["Translation" tasks \(e.g. text-to-speech\)](#)
 - [Controllable generation](#)
- Modeling non-standard data types
 - Graphs, sequences, [waveforms](#)



[Roberts+, 2019]



[Lim+, 2019]



[Karras+, 2018]

References for Figures

- Karras et al. 2019, <https://github.com/NVlabs/stylegan>
- Lim et al. 2019, Scaffold-based molecular design with a graph generative model
- Roberts et al. 2019, A Hierarchical Latent Vector Model for Learning Long-Term Structure in Music, <https://arxiv.org/pdf/1803.05428.pdf>