

Supersonic electroweak baryogenesis


Gláuber Carvalho Dorsch



arXiv:2106.06547

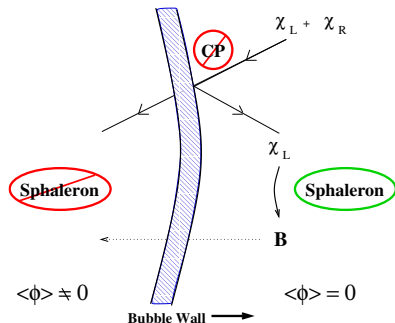
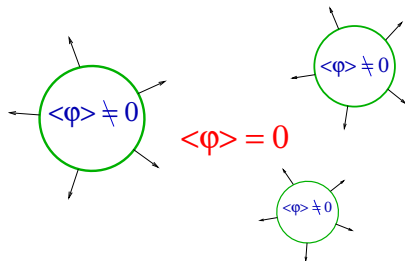
in collaboration with
T. Konstandin and S. Huber

PhenoBR

Natal () Zoom), 24 de Junho de 2021

Electroweak baryogenesis mechanism

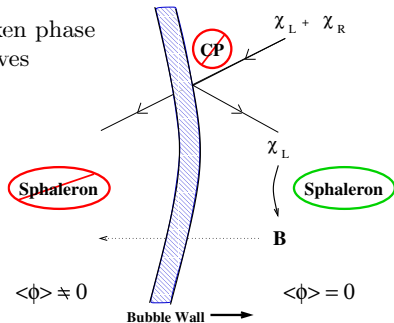
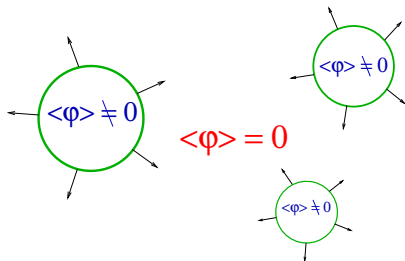
- Bubbles nucleate during the EWPT
- Plasma + bubble interaction \rightarrow $\begin{matrix} \text{chiral excess} \\ \text{diffuses in front} \\ \text{of the wall} \end{matrix}$



*Morrissey and Ramsey-Musolf,
New J. Phys. 14 (2012) 125003*

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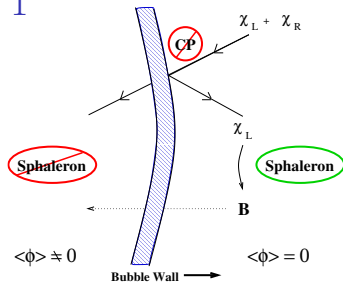
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- Plasma + bubble interaction \rightarrow $\begin{matrix} \text{chiral excess} \\ \text{diffuses in front} \\ \text{of the wall} \end{matrix}$
- $B + L$ chiral anomaly active in unbroken phase
Sphalerons: chiral excess $\rightarrow B$ excess
- Bubble expansion sweeps excess inside broken phase
 Sphalerons inactive $\rightarrow B$ asymmetry survives



Morrissey and Ramsey-Musolf,
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Supersonic baryogenesis – Round 1

Can fluctuations in the plasma propagate with speed $> c_s$ and produce a chiral asymmetry in front of a supersonic wall?



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Cline & Kainulainen,
PRD **101** 063525 (2020)

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It turns out...

For BAU one is interested in microscopic transport. Different than collective macroscopic oscillations (sound)

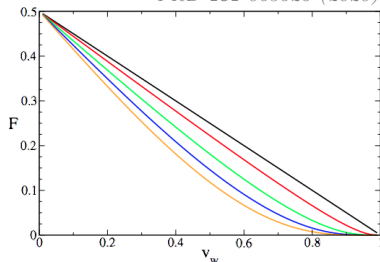


FIG. 1: Fraction of plasma particles that can stay ahead of a bubble wall moving at speed v_w . Different curves are for fermions with $m/T = 0, 1, 2, 3, 4$ (top to bottom).

$$f_i(x, p) = \frac{1}{e^{p^\mu u_\mu / T} \pm 1} + \delta f_i(x, p)$$

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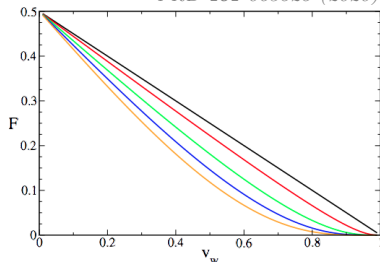


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$$f_i(x, p) = \frac{1}{e^{p^\mu u_\mu / T} \pm 1} + \delta f_i(x, p)$$

Fluid approximation

$$\delta f \simeq -(\mu/T + p^\mu \delta u_\mu / T - p^\mu u_\mu \delta T / T^2) \times f'_{eq}(p^\mu u_\mu / T)$$

$$f_i(x, p) = \frac{1}{e^{\beta(p^\mu u_\mu + \delta)} \pm 1}$$

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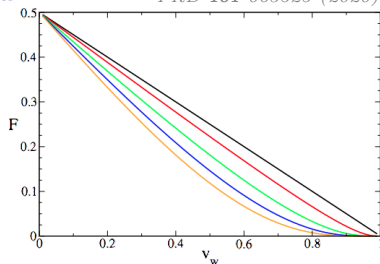
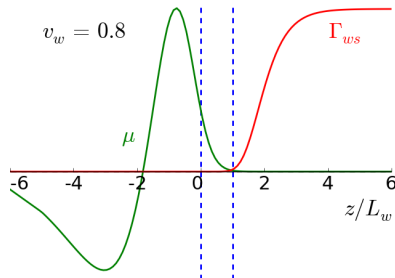


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But how reliable is this Ansatz?
Are three perturbations enough?

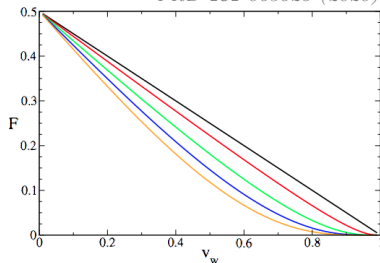
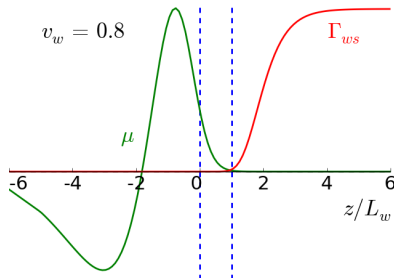


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Outline

- Modelling charge transport:
The Boltzmann equation and the need for an Ansatz
- Generalized fluid Ansatz

$$f(x, p) \simeq f_{\text{eq}}(p) + \left(\underbrace{w^{(0)}}_{-\mu} + p^\mu \underbrace{w_\mu^{(1)}}_{\delta T/T, -\delta v} + p^\mu p^\nu w_{\mu\nu}^{(2)} + \dots \right) f'_{\text{eq}}(p)$$

- Wall velocity dependence of the BAU:
continuity and convergence
- Conclusions and outlook

Modelling transport: Boltzmann equation

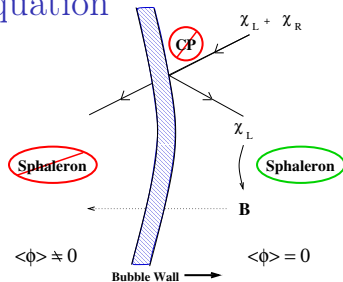
How can we model this complicated process?

FROM FIRST PRINCIPLES...

Wightman functions (propagators)

$$\Delta^{>,<} \sim \delta(p^2 - m^2) f_i(x, p)$$

satisfy Kadanoff-Baym equations



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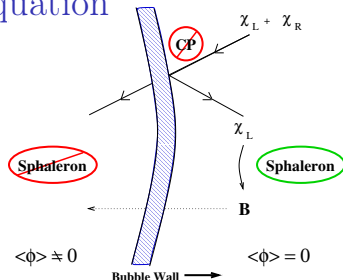
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GRADIENT EXPANSION $\left(L_w \gtrsim 1/T \iff \begin{array}{l} \text{SEMICLASSICAL,} \\ \text{PLASMA IS ON-SHELL} \end{array} \right)$

$$p^\mu \partial_\mu f_i(x^\mu, p^\mu) + m F^\mu \partial_{p^\mu} f_i(x^\mu, p^\mu) = \mathcal{C}[f_j]$$

$$f_i = f_i^{\text{eq}} + \delta f_i$$



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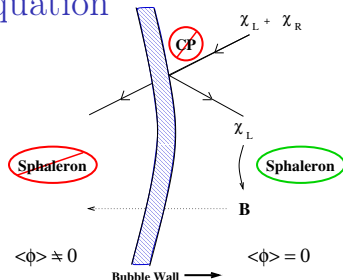
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$$p^\mu \partial_\mu \delta f_i(x^\mu, p^\mu) = \mathcal{S}[f_j] + \mathcal{C}[f_j]$$

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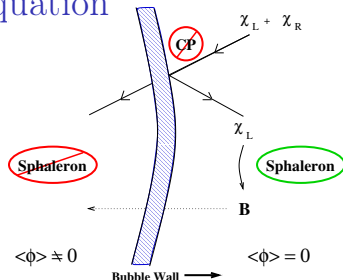
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$$\mathcal{C}[f] = \sum_{\text{processes}} \frac{1}{2} \int_k \int_{p'} \int_{k'} |\mathcal{M}|^2 (2\pi)^4 \delta^4(p + k - p' - k') \mathcal{P}[f]$$

$$\mathcal{P}[f] \equiv \left[f_p f_k (1 \pm f_{p'}) (1 \pm f_{k'}) - f_{p'} f_{k'} (1 \pm f_p) (1 \pm f_k) \right]$$



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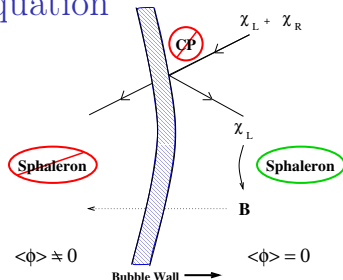
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We need
an Ansatz!



The fluid Ansatz

$$f_i(x, p) = \frac{1}{e^{\beta(p^\mu u_\mu + \delta)} \pm 1}$$

$$\delta = -(\mu - p^\mu u_\mu \delta T/T + p^\mu \delta u_\mu + \dots)$$

Steady planar wall

3 fluctuations

$$q = (\mu, -\delta T/T, \delta v)^T$$

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Get rid of p^μ dependence \implies take moments!

$$\partial_\mu J^\mu = \int \frac{d^3 p}{E_p} p^\mu \partial_\mu f = \int \frac{d^3 p}{E_p} p^\mu \mathcal{C} + \text{source}$$

$$\partial_\mu T^{\mu\nu} = \int \frac{d^3 p}{E_p} p^\mu p^\nu \partial_\mu f = \int \frac{d^3 p}{E_p} p^\mu p^\nu \mathcal{C} + \text{source}$$

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LINEARIZING IN PERTURBATIONS, COLLISION TERMS BECOME
TRACTABLE
(even analytically at leading-log)

$$\begin{aligned} \int_p p^\mu \dots p^\nu \mathcal{C}[f] &= \int_p \int_k \int_{p'} \int_{k'} |\mathcal{M}|^2 (2\pi)^4 \delta^4(p + k - p' - k') f_p^{\text{eq}} f_k^{\text{eq}} (1 \pm f_{p'}^{\text{eq}}) (1 \pm f_{k'}^{\text{eq}}) \times \\ &\quad \times p^\mu \dots p^\nu (\delta_p + \delta_k - \delta_{p'} - \delta_{k'}) \end{aligned}$$

The linearized system

$$\boxed{A \cdot q' + \Gamma \cdot q = S} \quad A = \begin{pmatrix} v_w c_2 & v_w c_3 & c_3/3 \\ v_w c_3 & v_w c_4 & c_4/3 \\ c_3/3 & c_4/3 & v_w c_4/3 \end{pmatrix} \quad \begin{array}{l} \Gamma \text{ calculated since the 90s} \\ \textit{Moore \& Prokopec,} \\ \textit{PRD 52, n. 12 (1995) 7182} \end{array}$$

$$q(z) = \int_z^\infty dz' \sum_{\lambda_i > 0} (\chi_i^{-1} \cdot A^{-1} \cdot S)(z') \chi_i \exp[-\lambda_i(z' - z)] \\ - \int_{-\infty}^z dz' \sum_{\lambda_i < 0} (\chi_i^{-1} \cdot A^{-1} \cdot S)(z') \chi_i \exp[-\lambda_i(z' - z)]$$

The linearized system

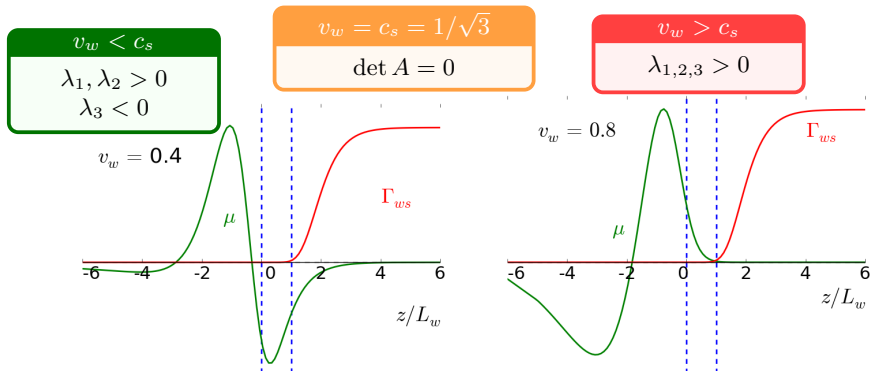
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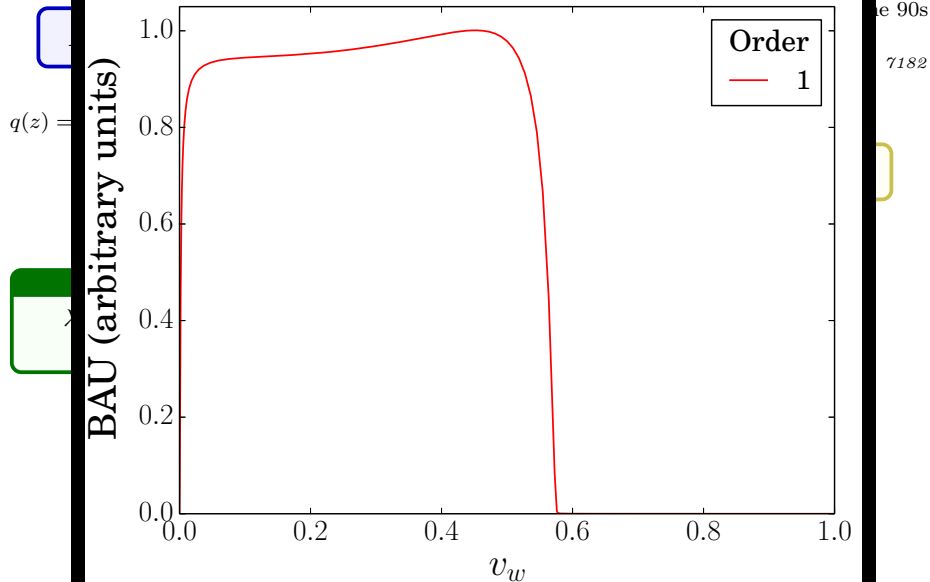
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$$\lambda_i = \text{eig}(A^{-1} \cdot \Gamma)$$



The linearized system



The need for higher orders

The eigenvalue sign flip is associated to the mode $v_w \delta v = -\delta T/T$

$$\begin{aligned}\delta f &= (p_z \delta v - E_p \delta T/T) f'(E_p/T)/T \\ &\simeq (p_z + v_w E_p) \delta v f'(E_p/T)/T\end{aligned}$$

$$\xi \equiv z + v_w t$$

$$p^\mu \partial_\mu = (v_w E_p - p_z) \partial_\xi$$

$$p^\mu \partial_\mu \delta f = \left(v_w^2 E_p^2 - p_z^2 \right) (\partial_\xi \delta v) \frac{f'(E_p/T)}{T}$$

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But

$$\langle E_p^n p_z^2 f' \rangle = \frac{\langle E_p^{n+2} f' \rangle}{3}$$

At $c_s = 1/\sqrt{3}$

$$p_\mu \partial_\mu \delta f \simeq 0$$

unless terms p_z^4 (or higher) appear!

Extended fluid Ansatz

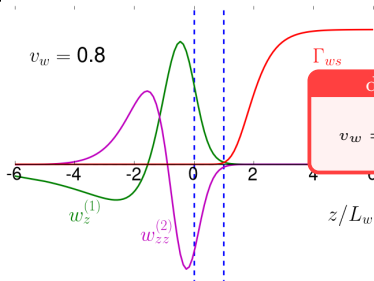
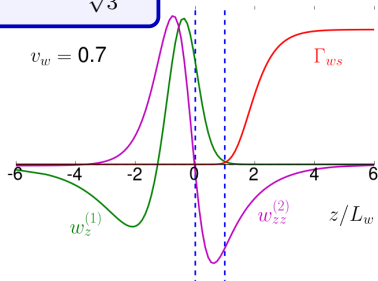
$$\delta f = \left(w^{(0)} + p^\mu w_\mu^{(1)} + p^\mu p^\nu w_{\mu\nu}^{(2)} + \dots \right) f'_{\text{eq}}(p^\mu u_\mu / T)$$

To 2nd order

$$A = \begin{pmatrix} v_w c_2 & v_w c_3 & c_3/3 & v_w c_4 & c_4/3 & v_w c_4/3 \\ v_w c_3 & v_w c_4 & c_4/3 & v_w c_5 & c_5/3 & v_w c_5/3 \\ c_3/3 & c_4/3 & v_w c_4/3 & c_5/3 & v_w c_5/3 & c_5/5 \\ v_w c_4 & v_w c_5 & c_5/3 & v_w c_6 & c_6/3 & v_w c_6/3 \\ c_4/3 & c_5/3 & v_w c_5/3 & c_6/3 & v_w c_6/3 & c_6/5 \\ v_w c_4/3 & v_w c_5/3 & c_5/5 & v_w c_6/3 & c_6/5 & v_w c_6/5 \end{pmatrix}$$

$$\det A = 0$$

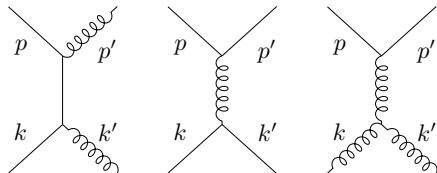
$$v_w = \frac{1}{\sqrt{3}}$$



$$\det A = 0$$

$$v_w = \sqrt{\frac{3}{5}} \approx 0.77$$

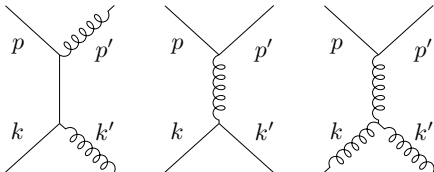
Collision terms



Singular behaviour \leftarrow kinetic term
but
collisions important for convergence

We consider a “network” of tops only
Other particles treated as background

Collision terms



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$$\text{coll.} \sim \delta_p + \delta_k - \delta_{p'} - \delta_{k'}$$

Annihilations

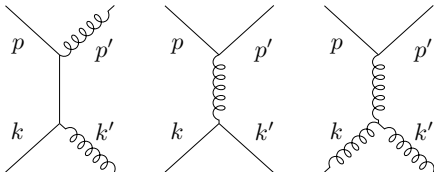
$$|\mathcal{M}|^2 \sim -g_s^4 \frac{st}{(t - m_q^2)^2}$$

$$t = -2p \cdot p' = -2|\mathbf{p}||\mathbf{p}'| \cos \theta_{pp'}$$

$$\int_p p^\mu \dots p^\nu C[f] \simeq \int_p \int_k \int_{p'} \int_{k'} \frac{st}{(t - m_q^2)^2} \delta^4(\dots) p^\mu \dots p^\nu f_p f_k (1 \pm f_{p'}) (1 \pm f_{k'}) \times$$

$$\times \left[\dots + w_{\rho\sigma}^{(2)} (p^\rho p^\sigma + k^\rho k^\sigma) + \dots \right]$$

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$$\text{coll.} \sim \delta_p + \delta_k - \delta_{p'} - \delta_{k'}$$

Scatterings

$$|\mathcal{M}|^2 \sim -g_s^4 \frac{s^2}{(t - m_q^2)^2}$$

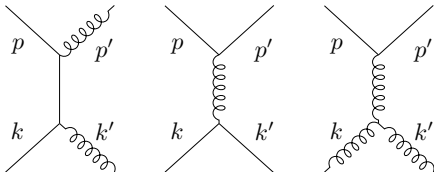
Much more complicated

Can be done analytically to leading-log!

$$\int_p p^\mu \dots p^\nu C[f] \simeq \int_p \int_k \int_{p'} \int_{k'} \frac{s^2}{(t - m_q^2)^2} \delta^4(\dots) p^\mu \dots p^\nu f_p f_k (1 \pm f_{p'}) (1 \pm f_{k'}) \times$$

$$\times \left[\dots + w_{\rho\sigma}^{(2)} (p^\rho p^\sigma - p'^\rho p'^\sigma) + \dots \right]$$

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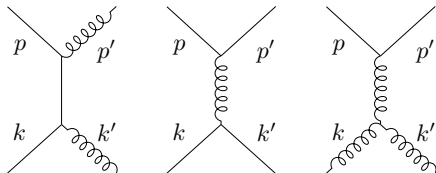
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QCD processes

$\Gamma \sim \alpha_s^2 \log \alpha_s$
Transport regulated by α_s

Calculated analytically to leading-log!

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QCD processes

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Transport regulated by α_s

Calculated analytically to leading-log!

Source

CPV obviously important for BAU

But...

v_w dependence dominated by kinetic term
Collisions set the convergence behaviour
Details of the source not so important

CP-even source!

$$mF_\mu \equiv \frac{\partial_\mu m^2}{2}$$

Ignore strong sphalerons,
chirality flips
These affect BAU magnitude
but not v_w dependence

Weak sphalerons

Sphaleron rate is known

$$\Gamma_{ws} \simeq 10^{-6} T \exp(-a\phi(z)/T)$$

But how does it couple to the
fluid fluctuations?

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Typically

$$\partial_z n_B \sim \Gamma_{ws} \frac{\mu}{T}$$

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$$\partial_z n_B \sim \Gamma_{ws} \left(\frac{\mu}{T} \right)$$


But how does it couple to the fluid fluctuations?

Merely zeroth-order term of a long expansion!

Strongly dependent on basis choice for fluctuations

This Ansatz seems inadequate here!

Weak sphalerons

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Merely zeroth-order term of a long expansion!

Strongly dependent on basis choice for fluctuations

This Ansatz seems inadequate here!

Our Ansatz

Couple sphaleron to particle number current density

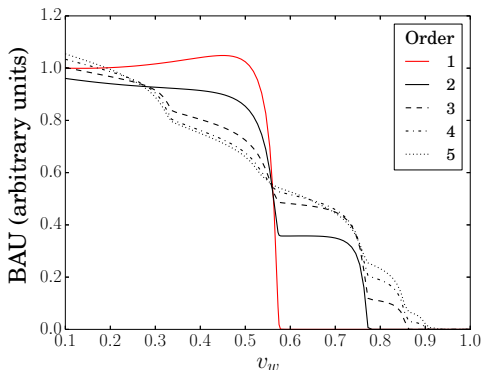
$$J^\mu = \int_p p^\mu f$$

At 0-th order, $J^\mu \sim \mu$

$$\partial_z n_B = \frac{3}{2v_w} \Gamma_{ws} \left(\kappa u_\mu J^\mu - \frac{15}{2} n_B \right)$$

Full computation requires solving the full collision integral for sphaleron multi-fermionic operator!

Results: Supersonic baryogenesis – Round 2

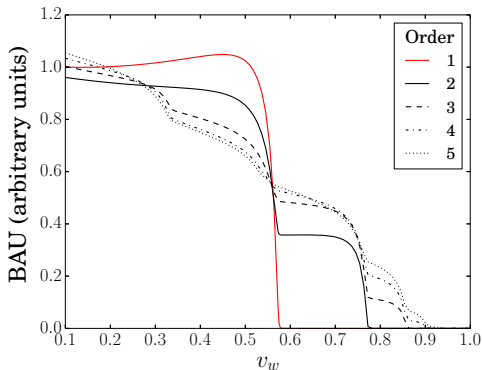


$$\alpha_s = 0.01$$

BAU suppressed for $v_w > c_s$, but
not prohibitively small!
(except for $v_w \rightarrow 1$)

Continuous along v_w
similar to found recently in
Cline & Kainulainen
PRD 101 (2020) no. 6, 063525

Results: Supersonic baryogenesis – Round 2



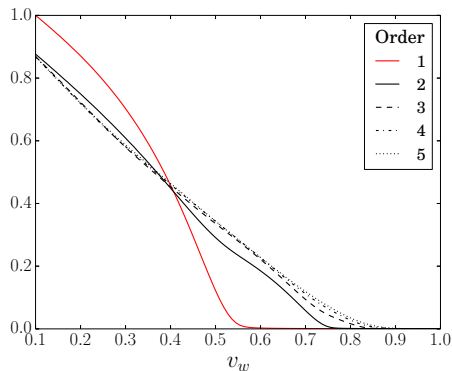
$\alpha_s = 0.01$

Continuous along v_w
similar to found recently in
Cline & Kainulainen
PRD 101 (2020) no. 6, 063525

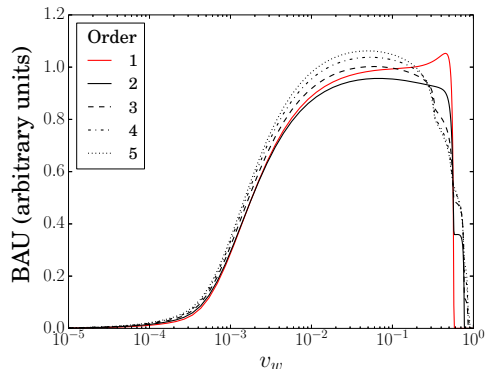
BAU suppressed for $v_w > c_s$, but
not prohibitively small!
(except for $v_w \rightarrow 1$)

convergence
parameter $\sim \frac{T}{\Gamma} \sim DT$

$\alpha_s = 0.06$



Results: small v_w



$\alpha_s = 0.01$

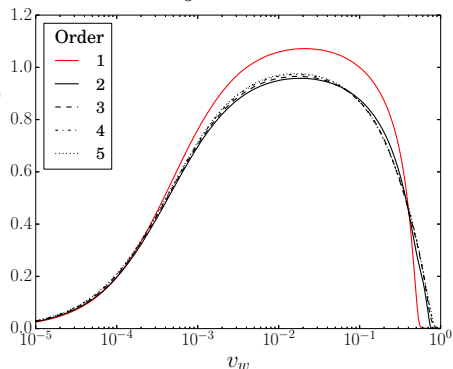
Either way the discrepancy is
 $\sim \mathcal{O}(20\%)$ for subsonic walls



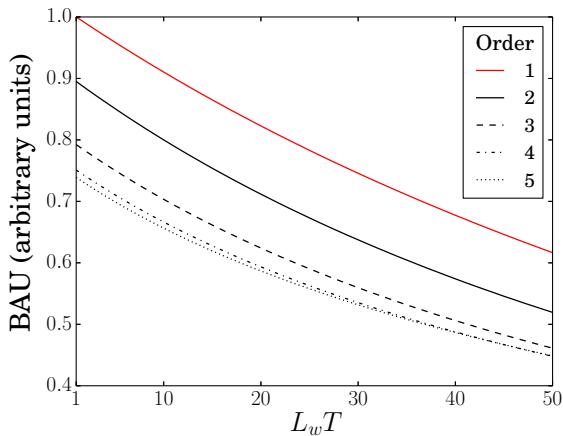
3-fluid reasonably reliable
in this regime

BAU can be either
enhanced or suppressed
relative to 1st order

$\alpha_s = 0.06$



Results: L_w dependence



$$\alpha_s = 0.01$$

$$v_w = 0.4$$

Convergence apparent
Dependence on L_w unaffected

Conclusions

- Supersonic baryogenesis is **not necessarily** impossible (though suppressed)
- We need an Ansatz to solve transport problem
Fluid-like Ansatz adequate, but
extension beyond 3 fluctuations may be (very) relevant

Outlook

- Full evaluation of coupling sphaleron–fluctuations still missing
- Systematics of series convergence
When to truncate the momentum expansion?
- Supersonic walls enhance GW production
Baryogenesis \longleftrightarrow Gravitational Waves interplay

THANK YOU!