

Gauged 2HDM with Axion-Dirac Neutrino Interplay

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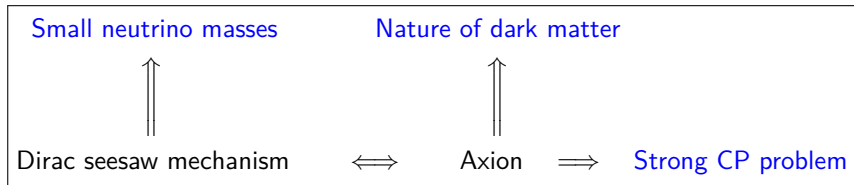
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Motivation

Problems to solve beyond the SM:



Framework: 2HDM with extra $U(1)_X$ and $U(1)_{PQ}$ symmetries.

Model building

	\mathcal{G}_{SM}	$U(1)_{global}$	$U(1)_{afree}$
L_{aL}	$(\mathbf{1}, \mathbf{2}, -1/2)$	$q'_{n_L} - q'_{\Phi_u} - 2q'_{\sigma} - q'_{\varphi}$	$-3l_{Q_L}$
e_{aR}	$(\mathbf{1}, \mathbf{1}, -1)$	$q'_{n_L} - 2q'_{\Phi_u} - 2q'_{\sigma} - q'_{\varphi}$	$-3l_{Q_L} - l_{\Phi_u}$
ν_{aR}	$(\mathbf{1}, \mathbf{1}, 0)$	$q'_{n_L} - q'_{\varphi}$	$-3l_{Q_L} + l_{\Phi_u}$
n_{aL}	$(\mathbf{1}, \mathbf{1}, 0)$	q'_{n_L}	$-3l_{Q_L} + l_{\Phi_u} + l_{\varphi}$
n_{aR}	$(\mathbf{1}, \mathbf{1}, 0)$	$q'_{n_L} - q'_{\sigma}$	$-3l_{Q_L} + l_{\Phi_u} + l_{\varphi}$
Q_{aL}	$(\mathbf{3}, \mathbf{2}, 1/6)$	q'_{Q_L}	l_{Q_L}
u_{aR}	$(\mathbf{3}, \mathbf{1}, 2/3)$	$q'_{Q_L} + q'_{\Phi_u}$	$l_{Q_L} + l_{\Phi_u}$
d_{aR}	$(\mathbf{3}, \mathbf{1}, -1/3)$	$q'_{Q_L} - q'_{\Phi_u} - q'_{\sigma} - q'_{\varphi}$	$l_{Q_L} - l_{\Phi_u} - l_{\varphi}$
k_{aL}	$(\mathbf{3}, \mathbf{1}, -1/3)$	$q'_{Q_L} - q'_{\Phi_u} - q'_{\sigma} - q'_{\varphi}$	$l_{Q_L} - l_{\Phi_u} - l_{\varphi}$
k_{aR}	$(\mathbf{3}, \mathbf{1}, -1/3)$	$q'_{Q_L} - q'_{\Phi_u} - q'_{\sigma}$	$l_{Q_L} - l_{\Phi_u}$
Φ_u	$(\mathbf{1}, \mathbf{2}, 1/2)$	q'_{Φ_u}	l_{Φ_u}
Φ_d	$(\mathbf{1}, \mathbf{2}, 1/2)$	$q'_{\Phi_u} + q'_{\sigma} + q'_{\varphi}$	$l_{\Phi_u} + l_{\varphi}$
φ	$(\mathbf{1}, \mathbf{1}, 0)$	q'_{φ}	l_{φ}
σ	$(\mathbf{1}, \mathbf{1}, 0)$	q'_{σ}	0

The scalar potential has only one **non-Hermitian term**:

$$V = V_{\text{Hermitian}} - \left[\lambda_4 (\Phi_d^\dagger \Phi_u) (\sigma \varphi) + \text{h.c.} \right] \quad (1)$$

Anomaly cancellation:

$$\begin{aligned} I : [SU(3)_C]^2 \times U(1)_{\text{global}} ; & \quad II : [SU(2)_L]^2 \times U(1)_{\text{global}} ; \\ III : [U(1)_Y]^2 \times U(1)_{\text{global}} ; & \quad IV : U(1)_Y \times [U(1)_{\text{global}}]^2 ; \\ V : [Grav]^2 \times U(1)_{\text{global}} ; & \quad VI : [U(1)_{\text{global}}]^3 \end{aligned} \quad (2)$$

Polar decomposition:

$$\Phi_{u,d} = \begin{pmatrix} \phi_{u,d}^+ \\ \phi_{u,d}^0 \end{pmatrix}, \quad \text{with} \quad \phi_{u,d}^0 = \frac{v_{u,d} + s_{u,d}}{\sqrt{2}} \exp\left(i \frac{a_{u,d}}{v_{u,d}}\right)$$

$$\varphi = \frac{v_\varphi + s_\varphi}{\sqrt{2}} \exp\left(i \frac{a_\varphi}{v_\varphi}\right) \quad \text{and} \quad \sigma = \frac{v_\sigma + s_\sigma}{\sqrt{2}} \exp\left(i \frac{a_\sigma}{v_\sigma}\right) \quad (3)$$

SSB pattern:

$$\begin{aligned} & \mathcal{G}_{SM} \otimes U(1)_X \otimes U(1)_{PQ} \otimes U(1)_B \otimes U(1)_L \\ & \quad \downarrow \quad v_\sigma \sim 10^{12} \text{ GeV} \\ & \mathcal{G}_{SM} \otimes U(1)_X \otimes U(1)_B \otimes U(1)_L \\ & \quad \downarrow \quad v_\varphi \sim 10^4 \text{ GeV} \\ & \mathcal{G}_{SM} \otimes U(1)_B \otimes U(1)_L \\ & \quad \downarrow \quad v \sim 246 \text{ GeV} \\ & SU(3)_C \otimes U(1)_{EM} \otimes U(1)_B \otimes U(1)_L \end{aligned} \quad (4)$$

CP-odd potential:

$$V(\mathbf{a}_i) = -\frac{\lambda_4}{2} v_u v_d v_\varphi v_\sigma \cos \left(\frac{\mathbf{a}_u}{v_u} - \frac{\mathbf{a}_d}{v_d} + \frac{\mathbf{a}_\varphi}{v_\varphi} + \frac{\mathbf{a}_\sigma}{v_\sigma} \right) \quad (5)$$

Massive field:

$$A = \frac{v_d v_\varphi v_\sigma \mathbf{a}_u - v_u v_\varphi v_\sigma \mathbf{a}_d + v_u v_d v_\sigma \mathbf{a}_\varphi + v_u v_d v_\varphi \mathbf{a}_\sigma}{\sqrt{v_\sigma^2 (v_\varphi^2 v^2 + v_u^2 v_d^2) + v_\varphi^2 v_u^2 v_d^2}}, \quad m_A^2 \approx \frac{\lambda_4 v_\sigma v_\varphi}{v_u v_d} v^2 \quad (6)$$

Massless fields:

$$G_c = \frac{1}{f_G} \sum_{\phi} c_\phi v_\phi \mathbf{a}_\phi, \quad c = X, Y, PQ \quad (7)$$

$$a = \frac{-\frac{v_d^2 v_\varphi^2 v_u}{v_u^2 v_d^2 + v_\varphi^2 v^2} \mathbf{a}_u + \frac{v_u^2 v_\varphi^2 v_d}{v_u^2 v_d^2 + v_\varphi^2 v^2} \mathbf{a}_d - \frac{v_u^2 v_d^2 v_\varphi}{v_u^2 v_d^2 + v_\varphi^2 v^2} \mathbf{a}_\varphi + v_\sigma \mathbf{a}_\sigma}{\sqrt{v_\sigma^2 + \frac{v_u^2 v_d^2 v_\varphi^2}{v_u^2 v_d^2 + v_\varphi^2 v^2}}}, \quad m_a = 0 \quad (8)$$

Gauge sector: Unmixed $U(1)_X$ gauge boson

In the basis $(W_3^\mu, B_Y^\mu, B_X^\mu)$:

$$M_{NGB}^2 = \frac{1}{4} \begin{pmatrix} g_L^2 v^2 & -g_L g_Y v^2 & 0 \\ -g_L g_Y v^2 & g_Y^2 v^2 & 0 \\ 0 & 0 & 4g_X^2 \left(v_\varphi^2 + \frac{v_u^2 v_d^2}{v^2} \right) \end{pmatrix} \quad (9)$$

Neutral gauge boson masses:

$$\begin{aligned} m_\gamma &= 0, \\ m_Z &= v (g_L^2 + g_Y^2)^{1/2}, \\ m_{Z'} &= g_X \left(v_\varphi^2 + \frac{v_u^2 v_d^2}{v^2} \right)^{1/2} \end{aligned} \quad (10)$$

Fermion sector

Flipped (Type-Y) 2HDM Yukawa Lagrangian:

$$\begin{aligned} -\mathcal{L}_y = & y_{ab}^u \overline{Q_{aL}} \widetilde{\Phi}_u u_{bR} + y_{ab}^d \overline{Q_{aL}} \Phi_d d_{bR} + y_{ab}^e \overline{L_{aL}} \Phi_u e_{bR} + y_{ab}^n \overline{L_{aL}} \widetilde{\Phi}_d n_{bR} \\ & + y_{ab}^\alpha \varphi \overline{n_{aL}} \nu_{bR} + y_{ab}^\beta \sigma \overline{n_{aL}} n_{bR} + y_{ab}^k \varphi^* \overline{k_{aL}} k_{bR} + \frac{y_{ab}^\mu \mu}{\sqrt{2}} \overline{k_{aL}} d_{bR} + \text{h.c.} \end{aligned} \quad (11)$$

Charged lepton and up-type quark mass matrices:

$$M^F = \frac{y^F v_u}{\sqrt{2}}, \quad F = e, u \quad (12)$$

Down-type quark mass matrix in the basis $D = (d, k)$:

$$M^D = \frac{1}{\sqrt{2}} \begin{pmatrix} y^d v_d & 0 \\ y^\mu \mu & y^k v_\varphi \end{pmatrix} \quad (13)$$

Diagonalisation of M^D :

$$(U_L^D)^\dagger M^D U_R^D = \text{diag}(m_d, m_s, m_b, M_1, M_2, M_3) \quad (14)$$

Neutral lepton mass matrix in the basis $N = (\nu, n)$:

$$M^N = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & y^n v_d \\ y^\alpha v_\varphi & y^\beta v_\sigma \end{pmatrix} \quad (15)$$

Dirac seesaw mechanism:

$$m_\nu \simeq \frac{y^n (y^\beta)^{-1} (y^\alpha)^T}{\sqrt{2}} \frac{v_d v_\varphi}{v_\sigma} = \frac{Y_{eff}^\nu}{\sqrt{2}} \frac{v_d v_\varphi}{v_\sigma} \quad (16)$$

$Y_{eff}^\nu \sim 10^{-4}$ implies $v_\varphi/v_\sigma \ll 1$. Intermediate scale physics?

FCNC mediated by Z :

$$\mathcal{L}_{FCNC}^Z \simeq \frac{g_L}{2 \cos \theta_W} Z^\mu \overline{d'_{iL}} \gamma_\mu \left(V_L^{d\dagger} B_L^D B_L^{D\dagger} V_L^d \right)_{ij} d'_{jL} \quad (17)$$

$B_L^D \sim 10^{-3}$ suppresses the FCNC below experimental limit.

Axion-photon and axion-gluon anomaly coefficients:

$$\begin{aligned} C_{a\gamma} &\equiv 2 \sum_{f=\text{fermions}} (PQ_{f_L} - PQ_{f_R})(Q_f)^2 = 2PQ_\sigma, \\ C_{ag} &\equiv \sum_{q=\text{quarks}} (PQ_{q_L} - PQ_{q_R}) = 3PQ_\sigma \end{aligned} \tag{18}$$

Axion-photon coupling:

$$g_{a\gamma} \approx \frac{\alpha}{2\pi f_a} \left(\frac{C_{a\gamma}}{C_{ag}} - 1.95 \right) \tag{19}$$

Axion mass from nonperturbative QCD effects [[Weinberg, 1978](#)]:

$$m_a \simeq 5.7 \left(\frac{10^{12} \text{ GeV}}{f_a} \right) \mu\text{eV} \tag{20}$$

$f_a \simeq \frac{v_\sigma}{3} \sim 10^{12} \text{ GeV}$, implies $m_a \simeq 17 \mu\text{eV}$.

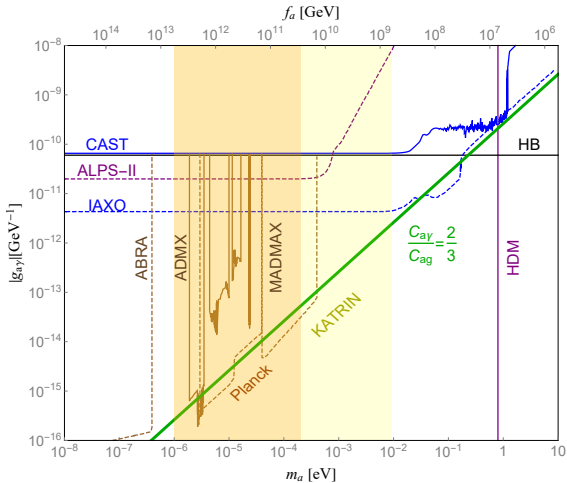


Figure 1: The green line shows our model prediction for $|g_{a\gamma}|$ vs m_a . Constraints from experiments, cosmology and astrophysics are also displayed.

Flavour-violating process [[Adler et al., 2008](#), [Björkeröth et al., 2018](#)]:

$$\text{Br}(K^+ \rightarrow \pi^+ a) = 9.77 \times 10^{11} \frac{1}{f_a^2} \left(\frac{\mu \sin \theta}{v_\varphi} \right)^4 \text{GeV}^2 \lesssim 7.3 \times 10^{-11} \quad (21)$$


$\frac{\mu \sin \theta}{v_\varphi} \simeq 9.1 \times 10^{-4}$ implies that $f_a \gtrsim 10^5 \text{ GeV}$. [[Ema et al., 2017](#)]: $f_a \gtrsim 10^{10} \text{ GeV}$


Conclusions


Solution to the neutrino masses, nature of dark matter and strong CP problem may arise from the axion-neutrino interplay;


Imposition of orthogonality of the Goldstone bosons fixes the physical charges of $U(1)_{PQ}$ and $U(1)_X$ charges;

The preferred region for neutrino masses and axion dark matter may be tested by forthcoming axion experiments looking for axion-photon interactions

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 Ema, Y., Hamaguchi, K., Moroi, T., and Nakayama, K. (2017).
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