Chapter 1 A Tour of Computer Systems

Problem 1.1

A. We use the formula with $\alpha = \frac{3}{5}$ and $k = \frac{150}{100} = \frac{3}{2}$.

$$S = \frac{1}{\left(1 - \frac{3}{5}\right) + \frac{3}{5} \cdot \frac{2}{3}}$$
$$= \frac{1}{\frac{2}{5} + \frac{2}{5}}$$
$$= \frac{5}{4}$$
$$= 1.25 \times$$

B. We use the formula and work our way back:

$$\frac{5}{3} = \frac{1}{(1 - \frac{3}{5}) + \frac{3}{5k}}$$

$$\frac{3}{5} = \frac{2}{5} + \frac{3}{5k}$$

$$\frac{1}{5} = \frac{3}{5k}$$

$$1 = \frac{3}{k}$$

$$k = 3$$

So the drive through Montana needs a speedup of $3 \times$ which is 300 km/hr.

Problem 1.2

Use the formula with $\alpha = \frac{4}{5}$ and S = 2 and solve for k.

$$2 = \frac{1}{\left(1 - \frac{4}{5}\right) + \frac{4}{5k}}$$
$$\frac{2}{5} + \frac{8}{5k} = 1$$
$$\frac{8}{5k} = \frac{3}{5}$$
$$\frac{1}{k} = \frac{3}{8}$$
$$k = \frac{8}{3}$$

Chapter 2 Representing and Manipulating Information

Problem 2.1

A. 0x39A7F8 to binary: 0011 1001 1010 0111 1111 1000

B. 1100100101111011 to hexadecimal: 0xC97B

C. 0xD5E4C to binary: 1101 0101 1110 0100 1100

D. 1001101110011110110101 to hexadecimal: 0x26E7B5

Problem 2.2

n	2^n (decimal)	2^n (hexadecimal)
9	512	0×200
19	524288	0×80000
14	16384	0×4000
16	65536	0×10000
17	131072	0×20000
5	32	0×20
7	128	0×80

Decimal	Binary	Hexadecimal
0	0000 0000	0×00
167	1010 0111	0xA7
62	0011 1110	0x3E
188	1011 1100	0×BC
55	0011 0111	0x37
136	1000 1000	0x88
243	1111 0011	0xF3
82	0101 0010	0x52
172	1010 1100	0×AC

Decimal	Binary	Hexadecimal	
231	1110 0111	0xE7	

```
A. 0x503c + 0x8 = 0x5044
```

B.
$$0x503c - 0x40 = 0x4ffc$$

C.
$$0x503c + 64 = 0x507c$$

D.
$$0x50ea - 0x503c = 0xae$$

Problem 2.5

	Little endian	Big endian
A.	21	87
В.	21 43	87 65
C.	21 43 65	87 65 43

Problem 2.6

A.

```
0x00359141 in binary: 0000 0000 0011 0101 1001 0001 0100 0001
0x4A564504 in binary: 0100 1010 0101 0110 0100 0101 0000 0100
```

В.

There are 21 matching bits.

C.

The whole integer occurs in the float representation, except for the most-significant bit which is a 1. Similarly, some of the most-significant bits of the float representation do not occur in the int representation.

Problem 2.7

It prints 61 62 63 64 65 66 (it does not print the terminating null character because the strlen function does not count it).

Operation	Result	
а	[01101001]	
b	[01010101]	
~a	[10010110]	
~b	[10101010]	
a & b	[01000001]	
a b	[01111101]	
a ^ b	[00111100]	

Problem 2.9

A. The following colors completent each other:

 $Black \leftrightarrow White$ $Blue \leftrightarrow Yellow$ $Green \leftrightarrow Magenta$ $Cyan \leftrightarrow Red$

B.

Blue | Green = Cyan Yellow & Cyan = Green Red ^ Magenta = Blue

Problem 2.10

Step	*X	*y	
Initially	а	b	
Step 1	а	a ^ b	
Step 2	$a ^ (a ^ b) = b$	a ^ b	
Step 3	b	b ^ (a ^ b) = a	

Problem 2.11

A. In the final iteration we have first = k and last = k (swap the middle element with itself).

B. In this case *x and *y point to the same address and the steps become:

Step	* X	*y	
Initially	а	а	
Step 1	a ^ a = 0	a ^ a = 0	
Step 2	0 ^ 0 = 0	0 ^ 0 = 0	
Step 3	0 ^ 0 = 0	0 ^ 0 = 0	

C. We can fix it by changing the condition to first < last since the middle element does not need to be swapped anyway.

Problem 2.12

A. x & 0xFF leaves the least significant byte and sets everything else to zero.

B. $\times ^ \sim 0 \times FF$ inverts everything except the least significant byte.

C. $x \mid 0xFF$ sets the least significant byte to ones and leaves everything else.

Problem 2.13

 $x \mid y$ is equivalent to bis(x, y).

 $x ^ y$ is equivalent to bis(bic(x, y), bic(y, x)).

Problem 2.14

We have $x = 0110 \ 0110$ and $y = 0011 \ 1001$.

Expression	Value	Expression	Value
x & y	0010 0000	x && y	1
x y	0111 1111	x y	1
~x ~y	1111 1111 1111 1111 1111 1111 1101 1111	!x !y	0
	(assuming 32-bit int)		
x & !y	0	x && ~y	1

Problem 2.15

 $!(x ^ y)$ is equivalent to x == y because $x ^ y$ will be 0 only if all the bits match.

x	x << 3	x >> 2 (logical)	x >> 2 (arithmetic)
$0 \times C3 = 1100 \ 0011$	$0001\ 1000 = 0 \times 18$	$0011 \ 0000 = 0 \times 30$	1111 0000 = $0 \times F0$
$0 \times 75 = 0111 \ 0101$	1010 1000 = 0xA8	$0001 \ 1101 = 0 \times 1D$	$0001 \ 1101 = 0 \times 1D$
$0 \times 87 = 1000 \ 0111$	$0011\ 1000 = 0 \times 38$	$0010\ 0001 = 0 \times 21$	1110 0001 = 0×E1
$0 \times 66 = 0110 \ 0110$	$0011 \ 0000 = 0 \times 30$	$0001\ 1001 = 0 \times 19$	$0001\ 1001 = 0 \times 19$

Problem 2.17

Hexadecimal	Binary	$B2U_4(x)$	$B2T_4(x)$
0xE	[1110]	$2^3 + 2^2 + 2^1 = 14$	$-2^3 + 2^2 + 2^1 = -2$
0×0	[0000]	0	0
0x5	[0101]	$2^2 + 2^0 = 5$	$2^2 + 2^0 = 5$
0x8	[1000]	$2^3 = 8$	$-2^3 = -8$
0xD	[1101]	$2^3 + 2^2 + 2^0 = 13$	$-2^3 + 2^2 + 2^0 = -3$
0xF	[1111]	$2^3 + 2^2 + 2^1 + 2^0 = 15$	$-2^3 + 2^2 + 2^1 + 2^0 = -1$

- **A.** 0x2e0 = 736
- **B.** -0x58 = -88
- $C. 0 \times 28 = 40$
- **D.** -0x30 = -48
- **E.** $0 \times 78 = 120$
- F. 0x88 = 136
- **G.** 0x1f8 = 504
- **H.** $0 \times c0 = 192$
- I. $-0 \times 48 = -72$

$oldsymbol{x}$	$T2U_4(x)$
-8	8
-3	$2^3 + 2^2 + 2^0 = 13$
-2	$2^3 + 2^2 + 2^1 = 14$
-1	$2^3 + 2^2 + 2^1 + 2^0 = 15$
0	0
5	5

Problem 2.20

Equation 2.5 can be used to solve the previous problem. Since $\omega=4$, we need to add $2^4=16$ to all negative numbers in Two's Complement. For example, -8+16=8 and -1+16=15. Positive numbers (and zero) stay the same.

Problem 2.21

Expression	Type	Evaluation
-2147483647 - 1 == 2147483648U	Unsigned	1
-2147483647 - 1 < 2147483647	Signed	1
$-2147483647 - 1\mathrm{U} < 2147483647$	Unsigned	0
-2147483647 - 1 < -2147483647	Signed	1
$-2147483647 - 1\mathrm{U} < -2147483647$	Unsigned	1

Problem 2.22

A.
$$[1011] = -2^3 + 2^1 + 2^0 = -5$$

B.
$$[11011] = -2^4 + 2^3 + 2^1 + 2^0 = -5$$

C.
$$[111011] = -2^5 + 2^4 + 2^3 + 2^1 + 2^0 = -5$$

W	fun1(w)	fun2(w)
0×00000076	0×00000076	0×00000076
0x87654321	0×00000021	0×00000021
0×000000C9	0×000000C9	0xFFFFFFC9
0xEDCBA987	0×00000087	0xFFFFFF87

fun1 keeps only the least significant byte and sets the other three to all zeroes, resulting in a value between 0 and 255. fun2 also extracts the least significant byte, but it performs sign extension instead of zero extension, which results in a value between -128 and 127.

Problem 2.24

I	łex	Uns	igned	Two's co	mplement
Original	Truncated	Original	Truncated	Original	Truncated
0	0	0	0	0	0
2	2	2	2	2	2
9	1	9	1	-7	1
В	3	11	3	-5	3
F	7	15	7	-1	-1

We can use the equations to verify these results. For example, in hex F truncates to 7, in unsigned $B2U_4(1111) \mod 2^3 = 7$ and in two's complement $U2T_3(B2U_4(1111) \mod 2^3) = -1$.

Problem 2.25

Because length is unsigned the expression 0-1 evaluates to UMax. The comparison has an unsigned integer on one side, which means the other side will also be treated as unsigned. Of course every unsigned number is \leq UMax and so we try to access invalid array elements.

We can fix it by changing the condition to i < length or changing length to a signed integer.

Problem 2.26

A. The function returns wrong results in case t is longer than s.

B. The problem is that strlen returns a size_t which is unsigned. When calculating strlen(s) - strlen(t) where t is longer than s unsigned arithmetic is used, resulting in a number close to UMax instead of a negative number. This is obviously greater than 0 so the function incorrectly says that s is longer.

C. We can fix it by changing the condition to strlen(s) > strlen(t).

```
/* Determine whether arguments can be added without overflow */
int uadd_ok(unsigned x, unsigned y) {
  return x + y >= x;
}
```

	\boldsymbol{x}	$-^{u}_{\omega}x$;
Hex	Decimal	Decimal	Hex
0	0	0	0
5	5	11	В
8	8	8	8
D	13	3	3
F	15	1	1

Problem 2.29

x	y	x + y	$x +_5^t y$	Case
-12	-15	-27	5	1
[10100]	[10001]	[100101]	[00101]	
-8	-8	-16	-16	2
[11000]	[11000]	[110000]	[10000]	
-9	8	-1	-1	2
[10111]	[01000]	[111111]	[11111]	
2	5	7	7	3
[00010]	[00101]	[000111]	[00111]	
12	4	16	-16	4
[01100]	[00100]	[010000]	[10000]	

```
/* Determine whether arguments can be added without overflow */
int tadd_ok(int x, int y) {
   int sum = x + y;

   if (x > 0 && y > 0) {
      return sum > 0;
   }

   if (x < 0 && y < 0) {
      return sum < 0;
   }

   return 1;
}</pre>
```

sum -x can overflow again, since it's another two's complement addition. For example, if x and y are large positive numbers whose sum overflows to a negative number, then sum -x will cause a negative overflow "wrapping back around" to y. So this check will not detect the overflow.

Problem 2.32

The function will be incorrect for $y=\mathrm{TMin}_{\omega}$. This is because the two's complement representation is not symmetric. $-y=-\mathrm{TMin}_{\omega}=\mathrm{TMin}_{\omega}$ causes an overflow possibly resulting in an incorrect return value.

Problem 2.33

	x	$-\frac{t}{4}x$	
Hex	Decimal	Decimal	Hex
0	0	0	0
5	5	-5	В
8	-8	-8	8
D	-3	3	3
F	-1	1	1

The bit patterns for two's complement and unsigned negation are the same.

Problem 2.34

Mode	x	y	$x \cdot y$	Truncated $x \cdot y$
Unsigned	4 = [100]	5 = [101]	20 = [010100]	4 = [100]
Two's complement	-4 = [100]	-3 = [101]	12 = [001100]	-4 = [100]
Unsigned	2 = [010]	7 = [111]	14 = [001110]	6 = [110]
Two's complement	2 = [010]	-1 = [111]	-2 = [111110]	-2 = [110]
Unsigned	6 = [110]	6 = [110]	36 = [100100]	4 = [100]
Two's complement	-2 = [110]	-2 = [110]	4 = [000100]	-4 = [100]

Problem 2.35

- **1.** Let $t=u+p_{\omega-1}$ where u is the two's complement number represented by the ω upper bits of the 2ω -bit representation of $x\cdot y$. Since $p_{\omega-1}$ is either 0 or 1, there are two possibilities for t to equal 0.
- 1. If $p_{\omega-1}=0$ then it must be that u=0 (upper ω bits are all 0s).
- 2. If $p_{\omega-1}=1$ then it must be that u=-1 (upper ω bits are all 1s).

So t=0 if the upper $\omega+1$ bits are all 0s or all 1s. These are exactly the cases where the multiplication does not overflow. All other cases do overflow.

This means we can write $x \cdot y = p + t2^{\omega}$ which overflows iff $t \neq 0$.

- **2.** To show that p can be written in the form $p = x \cdot q + r$, where |r| < |q| we consider integer division. Dividing p by nonzero x gives a quotiont q and remainder r, such that |r| < |q|.
- **3.** By plugging in we get $x \cdot y = x \cdot q + r + t2^{\omega}$. If $r + t2^{\omega} = 0$ then q = y. Since $|r| < |q| < 2^{\omega}$ this can only hold if r = t = 0.

Problem 2.36

```
/* Determine whether arguments can be multiplied without overflow */
int tmult_ok(int x, int y) {
  int64_t prod = ((int64_t)x) * y;
  int64_t upper = prod >> 31;
  // if the upper 33 bits are all 1s or 0s the number fits into 32 bits
  return upper == 0 || upper == -1;
}
```

Problem 2.37

A. The new code does not improve the situation since the 64-bit number will be truncated to 32 bits when passed to malloc. This truncation is the same that also happens when the multiplication overflows.

B. Check the multiplication for overflow (by one of the previous methods) and if it overflows immediately abort and don't allocate any memory.

Problem 2.38

A single LEA instruction can compute the following multiples:

k	b	$(a \ll k) + b$
0	0	$(2^0 + 0)a = 1a$
0	a	$(2^0+1)a = 2a$
1	0	$(2^1+0)a = 2a$
1	a	$(2^1+1)a = 3a$
2	0	$(2^2+0)a = 4a$
2	a	$(2^2+1)a = 5a$
3	0	$(2^3 + 0)a = 8a$
3	a	$(2^3+1)a = 9a$

Problem 2.39

In this case the expression simplifies to $-(x \ll m)$. This is because shifting by $n+1=\omega$ to the left results in 0 so we can ignore the first term.

K	Shifts	Add/Subs	Expression
6	2	1	$(x \ll 2) + (x \ll 1)$
31	1	1	$(x \ll 5) - x$
-6	2	1	$(x\ll 1)-(x\ll 3)$
55	2	2	$(x\ll 6)-(x\ll 3)-x$

Problem 2.41

Consider two cases:

- m>0: In this case form A requires n-m+1 shifts and n-m additions while form B requires 2 shifts and 1 subtraction. So if n=m, form A is favorable since it requires only 1 shift and 0 additions which is less than the constant numbers required for form B. If n=m+1, form A takes 2 shifts and 1 addition, so either form is equally efficient in this case. If n>m+1 form A takes n-m+1>2 shifts and n-m>1 additions so form B is favorable in this case.
- m=0: In this case the last bit does not cause a shift so form A requires n shifts and n additions, while form B takes 1 shift and 1 subtraction. The same three cases apply in the same way here, so the above analysis extends to this case as well.

Problem 2.42

```
int div16(int x) {
  int bias = (x >> 31) & 15;
  return (x + bias) >> 4;
}
```

Problem 2.43

x is shifted to the left by 5 which is equivalent to multiplying by $2^5=32$. Then, one x is subtracted from it, so we end up with 31x and M=31.

If y is negative, a bias of 7 = 8 - 1 is added. Then y is shifted right arithmetically by 3 which is equivalent to dividing by $2^3 = 8$. This means that N = 8.

Problem 2.44

A. false for $x=-2^{31}$ which is <code>INT32_MIN</code> . x is obviously not greater than 0, and x-1 overflows to <code>INT32_MAX</code> which is not lower than 0.

B. Always true . The expressions are connected by OR so both parts would need to evaluate to 0. Let x_2 be x's third bit from the right. For the first part to evaluate to 0 we need $x_2=1$. For the second part, x_2 will become the sign so it needs to be 0 to represent a positive number. This is obviously not possible at the same time so at least one part always evaluates to 1.

C. false for $x = 2^{16} - 1$.

D. Always true . For all negative numbers the first part of the expression evaluates to 1. For 0 the second part evaluates to 1. Every positive number can be negated and still fits into a 32-bit integer so in this case also the second parts evaluates to 1.

E. false for $x=-2^{31}$ which is INT32_MIN . It's not greater than 0 and negating it causes an overflow (-INT32 MIN = INT32 MIN) which is still lower than 0.

F. Always true . Addition works the same on the bit level for both unsigned and two's complement numbers. Since the right side is unsigned, C will interpret both sides as unsigned numbers for the comparison.

G. Always true . ~y is equal to -y-1. Also, on the bit level uy * ux is the same as x * y . Plugging in we get x(-y-1)+xy=-xy-x+xy=-x.

Problem 2.45

Fractional value	Binary representation	Decimal representation
$\frac{1}{8}$	0.001	0.125
$\frac{3}{4}$	0.11	0.75
$\frac{25}{16}$	1.1001	1.5625
$\frac{43}{16}$	10.1011	2.6875
$\frac{9}{8}$	1.001	1.125
$\frac{47}{8}$	101.111	5.875
$\frac{51}{16}$	11.0011	3.1875

Problem 2.46

A. Binary representation of 0.1 - x is: 0.0000000000000000000000011001100...

B. The above is the binary representation of 0.1 with the binary point shifted to the left by 20, so it is equal to $0.1 \times 2^{-20} \approx 9.54 \times 10^{-8}$.

C. After 100 hours the clock is behind by $9.54 \times 10^{-8} \cdot 100 \cdot 60 \cdot 60 \cdot 10 \approx 0.343$ seconds.

D. $2000 \text{m/s} \cdot 0.343 \text{s} \approx 686 \text{m}$

Bits	e	E	2^E	f	M	$2^E \times M$	V	Decimal
0 00 00	0	0	1	$\frac{0}{4}$	$\frac{0}{4}$	$\frac{0}{4}$	0	0.0
0 00 01	0	0	1	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	0.25
0 00 10	0	0	1	$\frac{2}{4}$	$\frac{2}{4}$	$\frac{2}{4}$	$\frac{1}{2}$	0.5

Bits	e	E	2^E	f	M	$2^E \times M$	V	Decimal
0 00 11	0	0	1	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{4}$	0.75
0 01 00	1	0	1	$\frac{0}{4}$	$\frac{4}{4}$	$\frac{4}{4}$	1	1.0
0 01 01	1	0	1	$\frac{1}{4}$	$\frac{4}{4}$ $\frac{5}{4}$	$\frac{4}{4}$ $\frac{5}{4}$	$\frac{5}{4}$	1.25
0 01 10	1	0	1	$\frac{2}{4}$		$\frac{6}{4}$	$\frac{\frac{5}{4}}{\frac{3}{2}}$ $\frac{7}{4}$	1.5
0 01 11	1	0	1	$\frac{2}{4}$ $\frac{3}{4}$	$\frac{6}{4}$ $\frac{7}{4}$	$\frac{7}{4}$	$\frac{7}{4}$	1.75
0 10 00	2	1	2	$\frac{0}{4}$		$\frac{8}{4}$	2	2.0
0 10 01	2	1	2	$\frac{1}{4}$	$\frac{4}{4}$ $\frac{5}{4}$ $\frac{6}{4}$ $\frac{7}{4}$	$\frac{10}{4}$	$\frac{5}{2}$	2.5
0 10 10	2	1	2	$\frac{2}{4}$	$\frac{6}{4}$	$\frac{12}{4}$	3	3.0
0 10 11	2	1	2	$\frac{3}{4}$	$\frac{7}{4}$	$\frac{14}{4}$	$\frac{7}{2}$	3.5
0 11 00	-	-	-	-	-	-	∞	-
0 11 01	-	-	-	-	-	-	NaN	-
0 11 10	-	-	-	-	-	-	NaN	-
0 11 11	-	-	-	-	-	-	NaN	-

3'510'593 in binary is 11 0101 1001 0001 0100 0001 which equals $1.101011001000101000001 \times 2^{21}$. So the biased exponent is $21 + 2^7 - 1 = 148$.

The complete single-precision floating-point representation is:

0 10010100 10101100100010100000100 or 0x4A564504

Comparing the two we see that part of it overlaps:

Problem 2.49

A.
$$2^{n+1} + 1$$

B.
$$2^{24} + 1 = 16'777'217$$

Ex	act	Rounded		
Binary	Decimal	Binary	Decimal	
10.010_{2}	$2\frac{1}{4}$	10.0_{2}	2	
10.011_2	$2\frac{3}{8}$	10.1_2	$2\frac{1}{2}$	
10.110_2	$2\frac{3}{4}$	11.0_2	3	
11.001_2	$3\frac{1}{8}$	11.0_{2}	3	

A. 0.00011001100110011001101

В.

This is equal to $\frac{1}{10} \times 2^{-22} \approx 2.38 \times 10^{-8}$.

C. After 100 hours the clock is ahead by $2.38 \times 10^{-8} \cdot 100 \cdot 60 \cdot 60 \cdot 10 \approx 0.086$ seconds.

D. $2000 \text{m/s} \cdot 0.086 \text{s} \approx 172 \text{m}$

Problem 2.52

Format A		Format B	
Bits	Value	Bits	Value
011 0000	1	0111 000	1
101 1110	$\frac{15}{2}$	1001 111	$\frac{15}{2}$
010 1001	$\frac{25}{32}$	0110 100	$\frac{3}{4}$
110 1111	$\frac{31}{2}$	1011 000	16
000 0001	$\frac{1}{64}$	0001 000	$\frac{1}{64}$

Problem 2.53

```
#define POS_INFIFINTY 1e400 // overflows
#define NEG_INFINITY (-POS_INFINITY)
#define NEG_ZERO (1.0/NEG_INFINITY)
```

Problem 2.54

A. Always true . double has enough range to represent all int values and it does not need to round. This also means no rounding when casting back.

B. false for $2^{24} + 1$. It is not true for all numbers with 24 or more significant bits, since the uses 23 bits for representing the fraction, which means these values get rounded and lose precision.

C. false for $2^{24} + 1$. The same reasoning as above applies here.

D. Always true . double has enough range and precision to exactly represent any float .

- **E.** Always true . Negating the float only flips the sign bit and loses no information. So flipping it back results in the original value.
- F. Always true . The integers get converted to float first.
- **G.** Always true . If the multiplication overflows it results in $\infty > 0$.
- H. false for $f=10^{20}$ and d=1.0. All values are promoted to double but even then the precision is not enough to represent $10^{20}+1.0$. This is because $\log_2 10^{20}>66$ and double has only 52 bits for representing the fraction. So when we set the least significant bit to 1 we would need about 66 bits to store the precise number. This means that adding 1.0 will have no effect on the very large number.

```
int is_little_endian() {
   // set only least significant byte to 0x01
   uint16_t x = 1;
   // char pointer reads only first byte, so it will be:
   // 0x00 on big endian systems
   // 0x01 on little endian systems
   return *(char *)&x;
}
```

Problem 2.59

```
int main() {
  int x = 0x89ABCDEF;
  int y = 0x76543210;
  int mask = 0xFF;
  printf("%d\n", ((x & mask) | (y & ~mask)) == 0x765432EF);
}
```

```
unsigned replace_byte(unsigned x, int i, unsigned char b) {
  unsigned mask = ~(0xFF << (i << 3));
  return (x & mask) | (b << (i << 3));
}

int main() {
  printf("%d\n", replace_byte(0x12345678, 2, 0xAB) == 0x12AB5678);
  printf("%d\n", replace_byte(0x12345678, 0, 0xAB) == 0x123456AB);
}</pre>
```

```
int A = !!x;
int B = !!~x;
int C = !!(x & 0xFF);
int D = !!~(x >> ((sizeof(int) - 1) << 3));</pre>
```

Problem 2.62

```
int int_shifts_are_arithmetic() {
  return (-1 >> 1) == -1;
}
```

Problem 2.63

```
unsigned srl(unsigned x, int k) {
   /* Perform shift arithmetically */
   unsigned xsra = (int)x >> k;

   int w = sizeof(int) << 3;
   int mask = ~(-1 << (w - k));
   return xsra & mask;
}

int sra(int x, int k) {
   /* Perform shift logically */
   int xsrl = (unsigned) x >> k;

   int w = sizeof(int) << 3;
   int mask = -1 << (w - k);
   int sign = -(x & (1 << (w - 1)));
   return xsrl | (mask & sign);
}</pre>
```

```
int any_odd_one(unsigned x) {
  int mask = 0b10101010101010101010101010101010;
  return !!(x & mask);
}
```

```
int odd_ones(unsigned x) {
    x ^= x >> 16;
    x ^= x >> 8;
    x ^= x >> 4;
    x ^= x >> 2;
    x ^= x >> 1;
    return x & 1;
}
```

Problem 2.66

```
int leftmost_one(unsigned x) {
   // Spread leftmost 1 to the right
   x |= x >> 1;
   x |= x >> 2;
   x |= x >> 4;
   x |= x >> 8;
   x |= x >> 16;
   return x ^ (x >> 1);
}
```

Problem 2.67

Shifting by an amount \geq the width of the type is undefined for signed integers.

```
int int_size_is(unsigned w) {
  unsigned set_msb = 1U << (w - 1);
  unsigned beyond_msb = set_msb << 1;
  return set_msb && !beyond_msb;
}</pre>
```

```
int lower_one_mask(int n) {
  int w = sizeof(int) << 3;
  return ~0U >> (w - n);
}
```

```
unsigned rotate_left(unsigned x, int n) {
  unsigned w = sizeof(unsigned) << 3;
  unsigned rotated_bits = x >> (w - n - 1) >> 1;
  return (x << n) | rotated_bits;
}</pre>
```