

Chapter 1 A Tour of Computer Systems

Problem 1.1

A. We use the formula with $\alpha = \frac{3}{5}$ and $k = \frac{150}{100} = \frac{3}{2}$.

$$\begin{aligned} S &= \frac{1}{\left(1 - \frac{3}{5}\right) + \frac{3}{5} \cdot \frac{2}{3}} \\ &= \frac{1}{\frac{2}{5} + \frac{2}{5}} \\ &= \frac{5}{4} \\ &= 1.25 \times \end{aligned}$$

B. We use the formula and work our way back:

$$\begin{aligned} \frac{5}{3} &= \frac{1}{\left(1 - \frac{3}{5}\right) + \frac{3}{5k}} \\ \frac{3}{5} &= \frac{2}{5} + \frac{3}{5k} \\ \frac{1}{5} &= \frac{3}{5k} \\ 1 &= \frac{3}{k} \\ k &= 3 \end{aligned}$$

So the drive through Montana needs a speedup of $3 \times$ which is 300 km/hr.

Problem 1.2

Use the formula with $\alpha = \frac{4}{5}$ and $S = 2$ and solve for k .

$$\begin{aligned} 2 &= \frac{1}{\left(1 - \frac{4}{5}\right) + \frac{4}{5k}} \\ \frac{2}{5} + \frac{8}{5k} &= 1 \\ \frac{8}{5k} &= \frac{3}{5} \\ \frac{1}{k} &= \frac{3}{8} \\ k &= \frac{8}{3} \end{aligned}$$

Chapter 2 Representing and Manipulating Information

Problem 2.1

- A. `0x39A7F8` to binary: `0011 1001 1010 0111 1111 1000`
- B. `1100100101111011` to hexadecimal: `0xC97B`
- C. `0xD5E4C` to binary: `1101 0101 1110 0100 1100`
- D. `1001101110011110110101` to hexadecimal: `0x26E7B5`

Problem 2.2

n	2^n (decimal)	2^n (hexadecimal)
9	512	<code>0x200</code>
19	524288	<code>0x80000</code>
14	16384	<code>0x4000</code>
16	65536	<code>0x10000</code>
17	131072	<code>0x20000</code>
5	32	<code>0x20</code>
7	128	<code>0x80</code>

Problem 2.3

Decimal	Binary	Hexadecimal
0	<code>0000 0000</code>	<code>0x00</code>
167	<code>1010 0111</code>	<code>0xA7</code>
62	<code>0011 1110</code>	<code>0x3E</code>
188	<code>1011 1100</code>	<code>0xBC</code>
55	<code>0011 0111</code>	<code>0x37</code>
136	<code>1000 1000</code>	<code>0x88</code>
243	<code>1111 0011</code>	<code>0xF3</code>
82	<code>0101 0010</code>	<code>0x52</code>
172	<code>1010 1100</code>	<code>0xAC</code>

Decimal	Binary	Hexadecimal
231	1110 0111	0xE7

Problem 2.4

- A. $0x503c + 0x8 = 0x5044$
- B. $0x503c - 0x40 = 0x4ffc$
- C. $0x503c + 64 = 0x507c$
- D. $0x50ea - 0x503c = 0xae$

Problem 2.5

	Little endian	Big endian
A.	21	87
B.	21 43	87 65
C.	21 43 65	87 65 43

Problem 2.6

A.

$0x00359141$ in binary: 0000 0000 0011 0101 1001 0001 0100 0001

$0x4A564504$ in binary: 0100 1010 0101 0110 0100 0101 0000 0100

B.

```
00000000001101011001000101000001
01001010010101100100010100000100
*****
```

There are 21 matching bits.

C.

The whole integer occurs in the float representation, except for the most-significant bit which is a 1. Similarly, some of the most-significant bits of the float representation do not occur in the int representation.

Problem 2.7

It prints 61 62 63 64 65 66 (it does not print the terminating null character because the `strlen` function does not count it).

Problem 2.8

Operation	Result
a	[01101001]
b	[01010101]
~a	[10010110]
~b	[10101010]
a & b	[01000001]
a b	[01111101]
a ^ b	[00111100]

Problem 2.9

A. The following colors complement each other:

Black \leftrightarrow White

Blue \leftrightarrow Yellow

Green \leftrightarrow Magenta

Cyan \leftrightarrow Red

B.

Blue | Green = Cyan

Yellow & Cyan = Green

Red ^ Magenta = Blue

Problem 2.10

Step	*x	*y
Initially	a	b
Step 1	a	a ^ b
Step 2	a ^ (a ^ b) = b	a ^ b
Step 3	b	b ^ (a ^ b) = a

Problem 2.11

A. In the final iteration we have `first = k` and `last = k` (swap the middle element with itself).

B. In this case `*x` and `*y` point to the same address and the steps become:

Step	*x	*y
Initially	a	a
Step 1	$a \wedge a = 0$	$a \wedge a = 0$
Step 2	$0 \wedge 0 = 0$	$0 \wedge 0 = 0$
Step 3	$0 \wedge 0 = 0$	$0 \wedge 0 = 0$

C. We can fix it by changing the condition to `first < last` since the middle element does not need to be swapped anyway.

Problem 2.12

- A. `x & 0xFF` leaves the least significant byte and sets everything else to zero.
- B. `x ^ ~0xFF` inverts everything except the least significant byte.
- C. `x | 0xFF` sets the least significant byte to ones and leaves everything else.

Problem 2.13

`x | y` is equivalent to `bis(x, y)`.

`x ^ y` is equivalent to `bis(bic(x, y), bic(y, x))`.

Problem 2.14

We have `x = 0110 0110` and `y = 0011 1001`.

Expression	Value	Expression	Value
<code>x & y</code>	0010 0000	<code>x && y</code>	1
<code>x y</code>	0111 1111	<code>x y</code>	1
<code>~x ~y</code>	1111 1111 1111 1111 1111 1111 1101 1111 (assuming 32-bit int)	<code>!x !y</code>	0
<code>x & !y</code>	0	<code>x && ~y</code>	1

Problem 2.15

`!(x ^ y)` is equivalent to `x == y` because `x ^ y` will be 0 only if all the bits match.

Problem 2.16

x	x << 3	x >> 2 (logical)	x >> 2 (arithmetic)
0xC3 = 1100 0011	0001 1000 = 0x18	0011 0000 = 0x30	1111 0000 = 0xF0
0x75 = 0111 0101	1010 1000 = 0xA8	0001 1101 = 0x1D	0001 1101 = 0x1D
0x87 = 1000 0111	0011 1000 = 0x38	0010 0001 = 0x21	1110 0001 = 0xE1
0x66 = 0110 0110	0011 0000 = 0x30	0001 1001 = 0x19	0001 1001 = 0x19

Problem 2.17

Hexadecimal	Binary	$B2U_4(x)$	$B2T_4(x)$
0xE	[1110]	$2^3 + 2^2 + 2^1 = 14$	$-2^3 + 2^2 + 2^1 = -2$
0x0	[0000]	0	0
0x5	[0101]	$2^2 + 2^0 = 5$	$2^2 + 2^0 = 5$
0x8	[1000]	$2^3 = 8$	$-2^3 = -8$
0xD	[1101]	$2^3 + 2^2 + 2^0 = 13$	$-2^3 + 2^2 + 2^0 = -3$
0xF	[1111]	$2^3 + 2^2 + 2^1 + 2^0 = 15$	$-2^3 + 2^2 + 2^1 + 2^0 = -1$

Problem 2.18

- A. 0x2e0 = 736
- B. -0x58 = -88
- C. 0x28 = 40
- D. -0x30 = -48
- E. 0x78 = 120
- F. 0x88 = 136
- G. 0x1f8 = 504
- H. 0xc0 = 192
- I. -0x48 = -72

Problem 2.19

x	$T2U_4(x)$
-8	8
-3	$2^3 + 2^2 + 2^0 = 13$
-2	$2^3 + 2^2 + 2^1 = 14$
-1	$2^3 + 2^2 + 2^1 + 2^0 = 15$
0	0
5	5

Problem 2.20

Equation 2.5 can be used to solve the previous problem. Since $\omega = 4$, we need to add $2^4 = 16$ to all negative numbers in Two's Complement. For example, $-8 + 16 = 8$ and $-1 + 16 = 15$. Positive numbers (and zero) stay the same.

Problem 2.21

Expression	Type	Evaluation
$-2147483647 - 1 == 2147483648U$	Unsigned	1
$-2147483647 - 1 < 2147483647$	Signed	1
$-2147483647 - 1U < 2147483647$	Unsigned	0
$-2147483647 - 1 < -2147483647$	Signed	1
$-2147483647 - 1U < -2147483647$	Unsigned	1

Problem 2.22

- A. $[1011] = -2^3 + 2^1 + 2^0 = -5$
 B. $[11011] = -2^4 + 2^3 + 2^1 + 2^0 = -5$
 C. $[111011] = -2^5 + 2^4 + 2^3 + 2^1 + 2^0 = -5$

Problem 2.23

w	$\text{fun1}(w)$	$\text{fun2}(w)$
0x00000076	0x00000076	0x00000076
0x87654321	0x00000021	0x00000021
0x000000C9	0x000000C9	0xFFFFF9C9
0xEDCBA987	0x00000087	0xFFFFF087

`fun1` keeps only the least significant byte and sets the other three to all zeroes, resulting in a value between 0 and 255. `fun2` also extracts the least significant byte, but it performs sign extension instead of zero extension, which results in a value between -128 and 127.

Problem 2.24

Hex		Unsigned		Two's complement	
Original	Truncated	Original	Truncated	Original	Truncated
0	0	0	0	0	0
2	2	2	2	2	2
9	1	9	1	-7	1
B	3	11	3	-5	3
F	7	15	7	-1	-1

We can use the equations to verify these results. For example, in hex F truncates to 7, in unsigned $B2U_4(1111) \bmod 2^3 = 7$ and in two's complement $U2T_3(B2U_4(1111) \bmod 2^3) = -1$.

Problem 2.25

Because `length` is unsigned the expression $0 - 1$ evaluates to `UMax`. The comparison has an unsigned integer on one side, which means the other side will also be treated as unsigned. Of course every unsigned number is $\leq \text{UMax}$ and so we try to access invalid array elements.

We can fix it by changing the condition to `i < length` or changing `length` to a signed integer.

Problem 2.26

A. The function returns wrong results in case `t` is longer than `s`.

B. The problem is that `strlen` returns a `size_t` which is unsigned. When calculating `strlen(s) - strlen(t)` where `t` is longer than `s` unsigned arithmetic is used, resulting in a number close to `UMax` instead of a negative number. This is obviously greater than 0 so the function incorrectly says that `s` is longer.

C. We can fix it by changing the condition to `strlen(s) > strlen(t)`.

Problem 2.27

```
/* Determine whether arguments can be added without overflow */
int uadd_ok(unsigned x, unsigned y) {
    return x + y >= x;
}
```


Problem 2.28

x		$-\omega^u x$	
Hex	Decimal	Decimal	Hex
0	0	0	0
5	5	11	B
8	8	8	8
D	13	3	3
F	15	1	1

Problem 2.29

x	y	$x + y$	$x + \frac{t}{5} y$	Case
-12 [10100]	-15 [10001]	-27 [100101]	5 [00101]	1
-8 [11000]	-8 [11000]	-16 [110000]	-16 [10000]	2
-9 [10111]	8 [01000]	-1 [111111]	-1 [11111]	2
2 [00010]	5 [00101]	7 [000111]	7 [00111]	3
12 [01100]	4 [00100]	16 [010000]	-16 [10000]	4

Problem 2.30

```

/* Determine whether arguments can be added without overflow */
int tadd_ok(int x, int y) {
    int sum = x + y;

    if (x > 0 && y > 0) {
        return sum > 0;
    }

    if (x < 0 && y < 0) {
        return sum < 0;
    }

    return 1;
}

```

Problem 2.31

$\text{sum} - x$ can overflow again, since it's another two's complement addition. For example, if x and y are large positive numbers whose sum overflows to a negative number, then $\text{sum} - x$ will cause a negative overflow "wrapping back around" to y . So this check will not detect the overflow.

Problem 2.32

The function will be incorrect for $y = \text{TMin}_\omega$. This is because the two's complement representation is not symmetric. $-y = -\text{TMin}_\omega = \text{TMin}_\omega$ causes an overflow possibly resulting in an incorrect return value.