# Chapter 1 A Tour of Computer Systems

# Problem 1.1

**A.** We use the formula with  $\alpha = \frac{3}{5}$  and  $k = \frac{150}{100} = \frac{3}{2}$ .

$$S = \frac{1}{\left(1 - \frac{3}{5}\right) + \frac{3}{5} \cdot \frac{2}{3}}$$
$$= \frac{1}{\frac{2}{5} + \frac{2}{5}}$$
$$= \frac{5}{4}$$
$$= 1.25 \times$$

**B.** We use the formula and work our way back:

$$\frac{5}{3} = \frac{1}{(1 - \frac{3}{5}) + \frac{3}{5k}}$$

$$\frac{3}{5} = \frac{2}{5} + \frac{3}{5k}$$

$$\frac{1}{5} = \frac{3}{5k}$$

$$1 = \frac{3}{k}$$

$$k = 3$$

So the drive through Montana needs a speedup of  $3 \times$  which is 300 km/hr.

# Problem 1.2

Use the formula with  $\alpha = \frac{4}{5}$  and S = 2 and solve for k.

$$2 = \frac{1}{\left(1 - \frac{4}{5}\right) + \frac{4}{5k}}$$
$$\frac{2}{5} + \frac{8}{5k} = 1$$
$$\frac{8}{5k} = \frac{3}{5}$$
$$\frac{1}{k} = \frac{3}{8}$$
$$k = \frac{8}{3}$$

# **Chapter 2** Representing and Manipulating Information

# Problem 2.1

**A.** 0x39A7F8 to binary: 0011 1001 1010 0111 1111 1000

**B.** 1100100101111011 to hexadecimal: 0xC97B

C. 0xD5E4C to binary: 1101 0101 1110 0100 1100

**D.** 1001101110011110110101 to hexadecimal: 0x26E7B5

# Problem 2.2

n	$2^n$ (decimal)	$2^n$ (hexadecimal)
9	512	0×200
19	524288	0×80000
14	16384	0×4000
16	65536	0×10000
17	131072	0×20000
5	32	0×20
7	128	0×80

Decimal	Binary	Hexadecimal
0	0000 0000	0×00
167	1010 0111	0xA7
62	0011 1110	0x3E
188	1011 1100	0×BC
55	0011 0111	0x37
136	1000 1000	0x88
243	1111 0011	0xF3
82	0101 0010	0x52
172	1010 1100	0×AC

Decimal	Binary	Hexadecimal	
231	1110 0111	0xE7	

```
A. 0x503c + 0x8 = 0x5044
```

**B.** 
$$0x503c - 0x40 = 0x4ffc$$

C. 
$$0x503c + 64 = 0x507c$$

**D.** 
$$0x50ea - 0x503c = 0xae$$

## Problem 2.5

	Little endian	Big endian
A.	21	87
В.	21 43	87 65
C.	21 43 65	87 65 43

# Problem 2.6

#### A.

```
0x00359141 in binary: 0000 0000 0011 0101 1001 0001 0100 0001
0x4A564504 in binary: 0100 1010 0101 0110 0100 0101 0000 0100
```

#### В.

There are 21 matching bits.

#### C.

The whole integer occurs in the float representation, except for the most-significant bit which is a 1. Similarly, some of the most-significant bits of the float representation do not occur in the int representation.

## Problem 2.7

It prints 61 62 63 64 65 66 (it does not print the terminating null character because the strlen function does not count it).

Operation	Result	
а	[01101001]	
b	[01010101]	
~a	[10010110]	
~b	[10101010]	
a & b	[01000001]	
a   b	[01111101]	
a ^ b	[00111100]	

# Problem 2.9

**A.** The following colors completent each other:

 $Black \leftrightarrow White$   $Blue \leftrightarrow Yellow$   $Green \leftrightarrow Magenta$   $Cyan \leftrightarrow Red$ 

#### B.

Blue | Green = Cyan Yellow & Cyan = Green Red ^ Magenta = Blue

# Problem 2.10

Step	*X	*y	
Initially	а	b	
Step 1	а	a ^ b	
Step 2	$a ^ (a ^ b) = b$	a ^ b	
Step 3	b	b ^ (a ^ b) = a	

# Problem 2.11

**A.** In the final iteration we have first = k and last = k (swap the middle element with itself).

**B.** In this case \*x and \*y point to the same address and the steps become:

Step	* <b>X</b>	*y	
Initially	а	а	
Step 1	a ^ a = 0	a ^ a = 0	
Step 2	0 ^ 0 = 0	0 ^ 0 = 0	
Step 3	0 ^ 0 = 0	0 ^ 0 = 0	

**C.** We can fix it by changing the condition to first < last since the middle element does not need to be swapped anyway.

## Problem 2.12

**A.** x & 0xFF leaves the least significant byte and sets everything else to zero.

**B.**  $\times ^ \sim 0 \times FF$  inverts everything except the least significant byte.

C.  $x \mid 0xFF$  sets the least significant byte to ones and leaves everything else.

## Problem 2.13

 $x \mid y$  is equivalent to bis(x, y).

 $x ^ y$  is equivalent to bis(bic(x, y), bic(y, x)).

## Problem 2.14

We have  $x = 0110 \ 0110$  and  $y = 0011 \ 1001$ .

Expression	Value	Expression	Value
x & y	0010 0000	x && y	1
x   y	0111 1111	x    y	1
~x   ~y	1111 1111 1111 1111 1111 1111 1101 1111	!x    !y	0
	(assuming 32-bit int)		
x & !y	0	x && ~y	1

# Problem 2.15

 $!(x ^ y)$  is equivalent to x == y because  $x ^ y$  will be 0 only if all the bits match.

x	x << 3	x >> 2 (logical)	x >> 2 (arithmetic)
$0 \times C3 = 1100 \ 0011$	$0001\ 1000 = 0 \times 18$	$0011 \ 0000 = 0 \times 30$	1111 0000 = $0 \times F0$
$0 \times 75 = 0111 \ 0101$	1010 1000 = 0xA8	$0001 \ 1101 = 0 \times 1D$	$0001 \ 1101 = 0 \times 1D$
$0 \times 87 = 1000 \ 0111$	$0011\ 1000 = 0 \times 38$	$0010\ 0001 = 0 \times 21$	1110 0001 = 0×E1
$0 \times 66 = 0110 \ 0110$	$0011 \ 0000 = 0 \times 30$	$0001\ 1001 = 0 \times 19$	$0001\ 1001 = 0 \times 19$

# Problem 2.17

Hexadecimal	Binary	$B2U_4(x)$	$B2T_4(x)$
0xE	[1110]	$2^3 + 2^2 + 2^1 = 14$	$-2^3 + 2^2 + 2^1 = -2$
0×0	[0000]	0	0
0x5	[0101]	$2^2 + 2^0 = 5$	$2^2 + 2^0 = 5$
0x8	[1000]	$2^3 = 8$	$-2^3 = -8$
0xD	[1101]	$2^3 + 2^2 + 2^0 = 13$	$-2^3 + 2^2 + 2^0 = -3$
0xF	[1111]	$2^3 + 2^2 + 2^1 + 2^0 = 15$	$-2^3 + 2^2 + 2^1 + 2^0 = -1$

- **A.** 0x2e0 = 736
- **B.** -0x58 = -88
- $C. 0 \times 28 = 40$
- **D.** -0x30 = -48
- **E.**  $0 \times 78 = 120$
- F. 0x88 = 136
- **G.** 0x1f8 = 504
- **H.**  $0 \times c0 = 192$
- I.  $-0 \times 48 = -72$

$oldsymbol{x}$	$T2U_4(x)$
-8	8
-3	$2^3 + 2^2 + 2^0 = 13$
-2	$2^3 + 2^2 + 2^1 = 14$
-1	$2^3 + 2^2 + 2^1 + 2^0 = 15$
0	0
5	5

# Problem 2.20

Equation 2.5 can be used to solve the previous problem. Since  $\omega=4$ , we need to add  $2^4=16$  to all negative numbers in Two's Complement. For example, -8+16=8 and -1+16=15. Positive numbers (and zero) stay the same.

## Problem 2.21

Expression	Type	Evaluation
-2147483647 - 1 == 2147483648U	Unsigned	1
-2147483647 - 1 < 2147483647	Signed	1
$-2147483647 - 1\mathrm{U} < 2147483647$	Unsigned	0
-2147483647 - 1 < -2147483647	Signed	1
$-2147483647 - 1\mathrm{U} < -2147483647$	Unsigned	1

# Problem 2.22

**A.** 
$$[1011] = -2^3 + 2^1 + 2^0 = -5$$

**B.** 
$$[11011] = -2^4 + 2^3 + 2^1 + 2^0 = -5$$

C. 
$$[111011] = -2^5 + 2^4 + 2^3 + 2^1 + 2^0 = -5$$

W	fun1(w)	fun2(w)
0×00000076	0×00000076	0×00000076
0x87654321	0×00000021	0×00000021
0×000000C9	0×000000C9	0xFFFFFFC9
0xEDCBA987	0×00000087	0xFFFFFF87

fun1 keeps only the least significant byte and sets the other three to all zeroes, resulting in a value between 0 and 255. fun2 also extracts the least significant byte, but it performs sign extension instead of zero extension, which results in a value between -128 and 127.

#### Problem 2.24

I	łex	Uns	igned	Two's co	mplement
Original	Truncated	Original	Truncated	Original	Truncated
0	0	0	0	0	0
2	2	2	2	2	2
9	1	9	1	-7	1
В	3	11	3	-5	3
F	7	15	7	-1	-1

We can use the equations to verify these results. For example, in hex F truncates to 7, in unsigned  $B2U_4(1111) \mod 2^3 = 7$  and in two's complement  $U2T_3(B2U_4(1111) \mod 2^3) = -1$ .

## Problem 2.25

Because length is unsigned the expression 0-1 evaluates to UMax. The comparison has an unsigned integer on one side, which means the other side will also be treated as unsigned. Of course every unsigned number is  $\leq$  UMax and so we try to access invalid array elements.

We can fix it by changing the condition to i < length or changing length to a signed integer.

## Problem 2.26

**A.** The function returns wrong results in case t is longer than s.

B. The problem is that strlen returns a size\_t which is unsigned. When calculating strlen(s) - strlen(t) where t is longer than s unsigned arithmetic is used, resulting in a number close to UMax instead of a negative number. This is obviously greater than 0 so the function incorrectly says that s is longer.

C. We can fix it by changing the condition to strlen(s) > strlen(t).

```
/* Determine whether arguments can be added without overflow */
int uadd_ok(unsigned x, unsigned y) {
  return x + y >= x;
}
```

	$\boldsymbol{x}$	$-^{u}_{\omega}x$	;
Hex	Decimal	Decimal	Hex
0	0	0	0
5	5	11	В
8	8	8	8
D	13	3	3
F	15	1	1

# Problem 2.29

x	y	x + y	$x +_5^t y$	Case
-12	-15	-27	5	1
[10100]	[10001]	[100101]	[00101]	
-8	-8	-16	-16	2
[11000]	[11000]	[110000]	[10000]	
-9	8	-1	-1	2
[10111]	[01000]	[111111]	[11111]	
2	5	7	7	3
[00010]	[00101]	[000111]	[00111]	
12	4	16	-16	4
[01100]	[00100]	[010000]	[10000]	

```
/* Determine whether arguments can be added without overflow */
int tadd_ok(int x, int y) {
   int sum = x + y;

   if (x > 0 && y > 0) {
      return sum > 0;
   }

   if (x < 0 && y < 0) {
      return sum < 0;
   }

   return 1;
}</pre>
```

sum -x can overflow again, since it's another two's complement addition. For example, if x and y are large positive numbers whose sum overflows to a negative number, then sum -x will cause a negative overflow "wrapping back around" to y. So this check will not detect the overflow.

## Problem 2.32

The function will be incorrect for  $y=\mathrm{TMin}_{\omega}$ . This is because the two's complement representation is not symmetric.  $-y=-\mathrm{TMin}_{\omega}=\mathrm{TMin}_{\omega}$  causes an overflow possibly resulting in an incorrect return value.

## Problem 2.33

	x	$-\frac{t}{4}x$	
Hex	Decimal	Decimal	Hex
0	0	0	0
5	5	-5	В
8	-8	-8	8
D	-3	3	3
F	-1	1	1

The bit patterns for two's complement and unsigned negation are the same.

#### Problem 2.34

Mode	x	y	$x \cdot y$	Truncated $x \cdot y$
Unsigned	4 = [100]	5 = [101]	20 = [010100]	4 = [100]
Two's complement	-4 = [100]	-3 = [101]	12 = [001100]	-4 = [100]
Unsigned	2 = [010]	7 = [111]	14 = [001110]	6 = [110]
Two's complement	2 = [010]	-1 = [111]	-2 = [111110]	-2 = [110]
Unsigned	6 = [110]	6 = [110]	36 = [100100]	4 = [100]
Two's complement	-2 = [110]	-2 = [110]	4 = [000100]	-4 = [100]

#### Problem 2.35

- **1.** Let  $t=u+p_{\omega-1}$  where u is the two's complement number represented by the  $\omega$  upper bits of the  $2\omega$ -bit representation of  $x\cdot y$ . Since  $p_{\omega-1}$  is either 0 or 1, there are two possibilities for t to equal 0.
- 1. If  $p_{\omega-1}=0$  then it must be that u=0 (upper  $\omega$  bits are all 0s).
- 2. If  $p_{\omega-1}=1$  then it must be that u=-1 (upper  $\omega$  bits are all 1s).

So t=0 if the upper  $\omega+1$  bits are all 0s or all 1s. These are exactly the cases where the multiplication does not overflow. All other cases do overflow.

This means we can write  $x \cdot y = p + t2^{\omega}$  which overflows iff  $t \neq 0$ .

- **2.** To show that p can be written in the form  $p = x \cdot q + r$ , where |r| < |q| we consider integer division. Dividing p by nonzero x gives a quotiont q and remainder r, such that |r| < |q|.
- **3.** By plugging in we get  $x \cdot y = x \cdot q + r + t2^{\omega}$ . If  $r + t2^{\omega} = 0$  then q = y. Since  $|r| < |q| < 2^{\omega}$  this can only hold if r = t = 0.

## Problem 2.36

```
/* Determine whether arguments can be multiplied without overflow */
int tmult_ok(int x, int y) {
  int64_t prod = ((int64_t)x) * y;
  int64_t upper = prod >> 31;
  // if the upper 33 bits are all 1s or 0s the number fits into 32 bits
  return upper == 0 || upper == -1;
}
```

#### Problem 2.37

**A.** The new code does not improve the situation since the 64-bit number will be truncated to 32 bits when passed to malloc. This truncation is the same that also happens when the multiplication overflows.

**B.** Check the multiplication for overflow (by one of the previous methods) and if it overflows immediately abort and don't allocate any memory.

#### Problem 2.38

A single LEA instruction can compute the following multiples:

k	b	$(a \ll k) + b$
0	0	$(2^0 + 0)a = 1a$
0	a	$(2^0+1)a = 2a$
1	0	$(2^1+0)a = 2a$
1	a	$(2^1+1)a = 3a$
2	0	$(2^2+0)a = 4a$
2	a	$(2^2+1)a = 5a$
3	0	$(2^3 + 0)a = 8a$
3	a	$(2^3+1)a = 9a$

## Problem 2.39

In this case the expression simplifies to  $-(x \ll m)$ . This is because shifting by  $n+1=\omega$  to the left results in 0 so we can ignore the first term.

K	Shifts	Add/Subs	Expression
6	2	1	$(x \ll 2) + (x \ll 1)$
31	1	1	$(x \ll 5) - x$
-6	2	1	$(x\ll 1)-(x\ll 3)$
55	2	2	$(x\ll 6)-(x\ll 3)-x$

#### Problem 2.41

Consider two cases:

- m>0: In this case form A requires n-m+1 shifts and n-m additions while form B requires 2 shifts and 1 subtraction. So if n=m, form A is favorable since it requires only 1 shift and 0 additions which is less than the constant numbers required for form B. If n=m+1, form A takes 2 shifts and 1 addition, so either form is equally efficient in this case. If n>m+1 form A takes n-m+1>2 shifts and n-m>1 additions so form B is favorable in this case.
- m=0: In this case the last bit does not cause a shift so form A requires n shifts and n additions, while form B takes 1 shift and 1 subtraction. The same three cases apply in the same way here, so the above analysis extends to this case as well.

#### Problem 2.42

```
int div16(int x) {
  int bias = (x >> 31) & 15;
  return (x + bias) >> 4;
}
```

## Problem 2.43

x is shifted to the left by 5 which is equivalent to multiplying by  $2^5=32$ . Then, one x is subtracted from it, so we end up with 31x and M=31.

If y is negative, a bias of 7 = 8 - 1 is added. Then y is shifted right arithmetically by 3 which is equivalent to dividing by  $2^3 = 8$ . This means that N = 8.

#### Problem 2.44

A. false for  $x=-2^{31}$  which is <code>INT32\_MIN</code> . x is obviously not greater than 0, and x-1 overflows to <code>INT32\_MAX</code> which is not lower than 0.

**B.** Always true . The expressions are connected by OR so both parts would need to evaluate to 0. Let  $x_2$  be x's third bit from the right. For the first part to evaluate to 0 we need  $x_2=1$ . For the second part,  $x_2$  will become the sign so it needs to be 0 to represent a positive number. This is obviously not possible at the same time so at least one part always evaluates to 1.

C. false for  $x = 2^{16} - 1$ .

**D.** Always true . For all negative numbers the first part of the expression evaluates to 1. For 0 the second part evaluates to 1. Every positive number can be negated and still fits into a 32-bit integer so in this case also the second parts evaluates to 1.

**E.** false for  $x=-2^{31}$  which is INT32\_MIN . It's not greater than 0 and negating it causes an overflow ( -INT32 MIN = INT32 MIN ) which is still lower than 0.

**F.** Always true . Addition works the same on the bit level for both unsigned and two's complement numbers. Since the right side is unsigned, C will interpret both sides as unsigned numbers for the comparison.

**G.** Always true . ~y is equal to -y-1. Also, on the bit level uy \* ux is the same as x \* y . Plugging in we get x(-y-1)+xy=-xy-x+xy=-x.

## Problem 2.45

Fractional value	Binary representation	Decimal representation
$\frac{1}{8}$	0.001	0.125
$\frac{3}{4}$	0.11	0.75
$\frac{25}{16}$	1.1001	1.5625
$\frac{43}{16}$	10.1011	2.6875
$\frac{9}{8}$	1.001	1.125
$\frac{47}{8}$	101.111	5.875
$\frac{51}{16}$	11.0011	3.1875

## Problem 2.46

**A.** Binary representation of 0.1 - x is: 0.0000000000000000000000011001100...

**B.** The above is the binary representation of 0.1 with the binary point shifted to the left by 20, so it is equal to  $0.1 \times 2^{-20} \approx 9.54 \times 10^{-8}$ .

**C.** After 100 hours the clock is behind by  $9.54 \times 10^{-8} \cdot 100 \cdot 60 \cdot 60 \cdot 10 \approx 0.343$  seconds.

**D.**  $2000 \text{m/s} \cdot 0.343 \text{s} \approx 686 \text{m}$ 

Bits	e	E	$2^E$	f	M	$2^E \times M$	V	Decimal
0 00 00	0	0	1	$\frac{0}{4}$	$\frac{0}{4}$	$\frac{0}{4}$	0	0.0
0 00 01	0	0	1	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	0.25
0 00 10	0	0	1	$\frac{2}{4}$	$\frac{2}{4}$	$\frac{2}{4}$	$\frac{1}{2}$	0.5

Bits	e	E	$2^E$	f	M	$2^E \times M$	V	Decimal
0 00 11	0	0	1	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{4}$	$\frac{3}{4}$	0.75
0 01 00	1	0	1	$\frac{0}{4}$	$\frac{4}{4}$	$\frac{4}{4}$	1	1.0
0 01 01	1	0	1	$\frac{1}{4}$	$\frac{4}{4}$ $\frac{5}{4}$	$\frac{4}{4}$ $\frac{5}{4}$	$\frac{5}{4}$	1.25
0 01 10	1	0	1	$\frac{2}{4}$		$\frac{6}{4}$	$\frac{\frac{5}{4}}{\frac{3}{2}}$ $\frac{7}{4}$	1.5
0 01 11	1	0	1	$\frac{2}{4}$ $\frac{3}{4}$	$\frac{6}{4}$ $\frac{7}{4}$	$\frac{7}{4}$	$\frac{7}{4}$	1.75
0 10 00	2	1	2	$\frac{0}{4}$		$\frac{8}{4}$	2	2.0
0 10 01	2	1	2	$\frac{1}{4}$	$\frac{4}{4}$ $\frac{5}{4}$ $\frac{6}{4}$ $\frac{7}{4}$	$\frac{10}{4}$	$\frac{5}{2}$	2.5
0 10 10	2	1	2	$\frac{2}{4}$	$\frac{6}{4}$	$\frac{12}{4}$	3	3.0
0 10 11	2	1	2	$\frac{3}{4}$	$\frac{7}{4}$	$\frac{14}{4}$	$\frac{7}{2}$	3.5
0 11 00	-	-	-	-	-	-	$\infty$	-
0 11 01	-	-	-	-	-	-	NaN	-
0 11 10	-	-	-	-	-	-	NaN	-
0 11 11	-	-	-	-	-	-	NaN	-

3'510'593 in binary is 11 0101 1001 0001 0100 0001 which equals  $1.101011001000101000001 \times 2^{21}$ . So the biased exponent is  $21 + 2^7 - 1 = 148$ .

The complete single-precision floating-point representation is:

0 10010100 10101100100010100000100 or 0x4A564504

Comparing the two we see that part of it overlaps:

# Problem 2.49

**A.** 
$$2^{n+1} + 1$$

**B.** 
$$2^{24} + 1 = 16'777'217$$

Ex	act	Rounded		
Binary	Decimal	Binary	Decimal	
$10.010_{2}$	$2\frac{1}{4}$	$10.0_{2}$	2	
$10.011_2$	$2\frac{3}{8}$	$10.1_2$	$2\frac{1}{2}$	
$10.110_2$	$2\frac{3}{4}$	$11.0_2$	3	
$11.001_2$	$3\frac{1}{8}$	$11.0_{2}$	3	

**A.** 0.00011001100110011001101

В.

This is equal to  $\frac{1}{10} \times 2^{-22} \approx 2.38 \times 10^{-8}$ .

**C.** After 100 hours the clock is ahead by  $2.38 \times 10^{-8} \cdot 100 \cdot 60 \cdot 60 \cdot 10 \approx 0.086$  seconds.

**D.**  $2000 \text{m/s} \cdot 0.086 \text{s} \approx 172 \text{m}$ 

## Problem 2.52

Format A		Format B	
Bits	Value	Bits	Value
011 0000	1	0111 000	1
101 1110	$\frac{15}{2}$	1001 111	$\frac{15}{2}$
010 1001	$\frac{25}{32}$	0110 100	$\frac{3}{4}$
110 1111	$\frac{31}{2}$	1011 000	16
000 0001	$\frac{1}{64}$	0001 000	$\frac{1}{64}$

## Problem 2.53

```
#define POS_INFIFINTY 1e400 // overflows
#define NEG_INFINITY (-POS_INFINITY)
#define NEG_ZERO (1.0/NEG_INFINITY)
```

## Problem 2.54

**A.** Always true . double has enough range to represent all int values and it does not need to round. This also means no rounding when casting back.

**B.** false for  $2^{24} + 1$ . It is not true for all numbers with 24 or more significant bits, since the uses 23 bits for representing the fraction, which means these values get rounded and lose precision.

**C.** false for  $2^{24} + 1$ . The same reasoning as above applies here.

D. Always true . double has enough range and precision to exactly represent any float .

- **E.** Always true . Negating the float only flips the sign bit and loses no information. So flipping it back results in the original value.
- F. Always true . The integers get converted to float first.
- **G.** Always true . If the multiplication overflows it results in  $\infty > 0$ .
- H. false for  $f=10^{20}$  and d=1.0. All values are promoted to double but even then the precision is not enough to represent  $10^{20}+1.0$ . This is because  $\log_2 10^{20}>66$  and double has only 52 bits for representing the fraction. So when we set the least significant bit to 1 we would need about 66 bits to store the precise number. This means that adding 1.0 will have no effect on the very large number.

```
int is_little_endian() {
   // set only least significant byte to 0x01
   uint16_t x = 1;
   // char pointer reads only first byte, so it will be:
   // 0x00 on big endian systems
   // 0x01 on little endian systems
   return *(char *)&x;
}
```

## Problem 2.59

```
int main() {
  int x = 0x89ABCDEF;
  int y = 0x76543210;
  int mask = 0xFF;
  printf("%d\n", ((x & mask) | (y & ~mask)) == 0x765432EF);
}
```

```
unsigned replace_byte(unsigned x, int i, unsigned char b) {
  unsigned mask = ~(0xFF << (i << 3));
  return (x & mask) | (b << (i << 3));
}

int main() {
  printf("%d\n", replace_byte(0x12345678, 2, 0xAB) == 0x12AB5678);
  printf("%d\n", replace_byte(0x12345678, 0, 0xAB) == 0x123456AB);
}</pre>
```

```
int A = !!x;
int B = !!~x;
int C = !!(x & 0xFF);
int D = !!~(x >> ((sizeof(int) - 1) << 3));</pre>
```

## Problem 2.62

```
int int_shifts_are_arithmetic() {
  return (-1 >> 1) == -1;
}
```

## Problem 2.63

```
unsigned srl(unsigned x, int k) {
   /* Perform shift arithmetically */
   unsigned xsra = (int)x >> k;

   int w = sizeof(int) << 3;
   int mask = ~(-1 << (w - k));
   return xsra & mask;
}

int sra(int x, int k) {
   /* Perform shift logically */
   int xsrl = (unsigned) x >> k;

   int w = sizeof(int) << 3;
   int mask = -1 << (w - k);
   int sign = -(x & (1 << (w - 1)));
   return xsrl | (mask & sign);
}</pre>
```

```
int any_odd_one(unsigned x) {
   // Assume word size is 32 bits
   int mask = 0b10101010101010101010101010101010;
   return !!(x & mask);
}
```