# **CPSC 322: Introduction to Artificial Intelligence (Section 2)**

# Solving CSPs using arc consistency and domain splitting

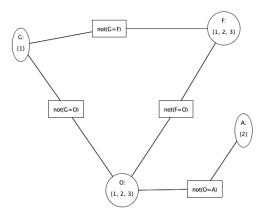
Do this exercise in pairs. If there's an odd number, do it in a group of 3.

# Submit the sheet before leaving.

Name of Student (last, first)	Student Number

# **Question1: Arc consistency**

Consider the following subset of the constraint network we worked on last week. Trace the arc consistency algorithm on the network. Show at least 4 to 6 iterations. For each iteration, show TDA and domain values.



Variables:

Google (G), Facebook (F), OpenAI (O), Apple (A)

## Start

TDA =

$$\{ \langle F, G \neq F \rangle, \langle F, F \neq O \rangle, \langle O, G \neq O \rangle, \langle O, F \neq O \rangle, \langle O, O \neq A \rangle, \langle A, O \neq A \rangle, \langle G, G \neq F \rangle, \langle G, G \neq O \rangle \}$$
  
Domains: G = {1}; F = {1,2,3}; O = {1,2,3}; A = {2}

## **Iteration 1**

Select arc  $\langle F, \text{not}(G = F) \rangle$ 

TDA =

$$\{ \langle F, F \neq O \rangle, \langle O, G \neq O \rangle, \langle O, F \neq O \rangle, \langle O, O \neq A \rangle, \langle A, O \neq A \rangle, \langle G, G \neq F \rangle, \langle G, G \neq O \rangle \}$$

Check  $\langle F, \text{not}(G = F) \rangle$  for consistency.

1 removed from the domain of F to make arc  $\langle F, \text{not}(G=F) \rangle$  consistent.

New domains:  $G = \{1\}$ ;  $F = \{2,3\}$ ;  $O = \{1,2,3\}$ ;  $A = \{2\}$ 

Affected arcs due to domain pruning: <0, not(F=0)>

Not adding the affected arcs in TDA because they are already there.

#### **Iteration 2**

Select arc  $\langle F, \text{not}(F = O) \rangle$ 

TDA =

$$\{ < O, G \neq O >, < O, F \neq O >, < O, O \neq A >, < A, O \neq A >, < G, G \neq F >, < G, G \neq O > \}$$

Check  $\langle F, \text{not}(F = O) \rangle$  for consistency.

The arc is consistent and the domains do not change.

Domains:  $G = \{1\}$ ;  $F = \{2,3\}$ ;  $O = \{1,2,3\}$ ;  $A = \{2\}$ 

## **Iteration 3**

Select arc <O, not(G=O)>

$$TDA = \{ < O, F \neq O > , < O, O \neq A > , < A, O \neq A > , < G, G \neq F > , < G, G \neq O > \}$$

Check <O, not(G = O)> for consistency.

1 removed from the domain of O to make arc <0, not(G=O)> consistent.

New domains:  $G = \{1\}$ ;  $F = \{2,3\}$ ;  $O = \{2,3\}$ ;  $A = \{2\}$ 

Affected arcs due to domain pruning: <F, not(F=O) >, <A, not(O=A)>

TDA=

$$\{ \langle O, F \neq O \rangle, \langle O, O \neq A \rangle, \langle A, O \neq A \rangle, \langle G, G \neq F \rangle, \langle G, G \neq O \rangle, \langle F, F \neq O \rangle \}$$

## **Iteration 4**

Select <O, not(F=O)>

TDA = { 
$$< O, O \ne A >$$
,  $< A, O \ne A >$ ,  $< G, G \ne F >$ ,  $< G, G \ne O >$ ,  $< F, F \ne O >$  } Check  $<$ O, not(F=O)> for consistency.

The arc is consistent and the domains do not change.

Domains:  $G = \{1\}$ ;  $F = \{2,3\}$ ;  $O = \{2,3\}$ ;  $A = \{2\}$ 

## **Iteration 5**

Select <O, not(O=A)>

$$TDA = \{ \langle A, O \neq A \rangle, \langle G, G \neq F \rangle, \langle G, G \neq O \rangle, \langle F, F \neq O \rangle \}$$

Check <O, not(O=A)> for consistency.

2 removed from the domain of O to make arc <0, not(O=A)> consistent.

New domains:  $G = \{1\}$ ;  $F = \{2,3\}$ ;  $O = \{3\}$ ;  $A = \{2\}$ 

Affected arcs due to domain pruning: <F, not(F=O)>, <G, not(G=O)>

Arcs are already on TDA so not adding them.

.... continue till you get an arc-consistent network

# **Question 2: Domain splitting**

Variables: A, B, C; Domains:  $\{1,2,3,4\}$ ; Constraints: A = B, B = C, A = CSolve this CSP using arc consistency and domain splitting. How many solutions are there?

