



Millimeter-Wave Networks for Vehicular Communication: Modeling and Performance Insights

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Belfast, 8th July 2016



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- Why Should I Put Comms Onto Self-Driving Vehicles?
- ... and Why Should I go for mmWave Systems?
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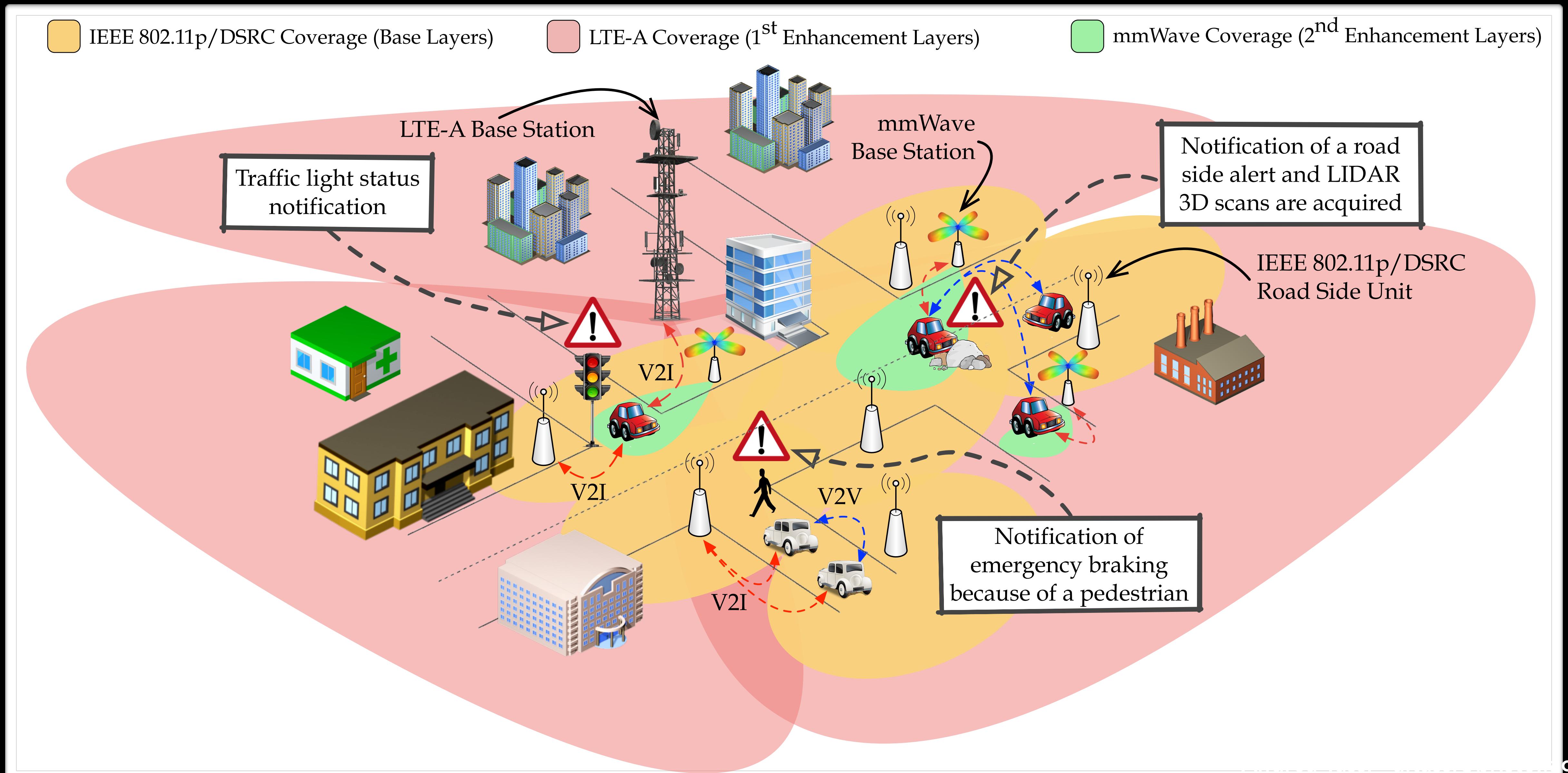


mmWave Comms for Next Generation ITSs

- The IEEE 802.11p/DSRC can achieve at most ~27 Mbps, in practice it is hard to observe that.
- However, DSRC standards are suitable for low-rate data services (for e.g., positioning beacon, emergency stop messages, etc.).
- On the other hand, future CAVs will require solutions ensuring gigabit-per-second communication links to achieve proper 'look-ahead' services (involving cameras, LIDARS, etc.), etc.
- It is reasonable to design hybrid networks integrating both mmWave and DSRC technologies



mmWave Comms for Next Generation ITSs





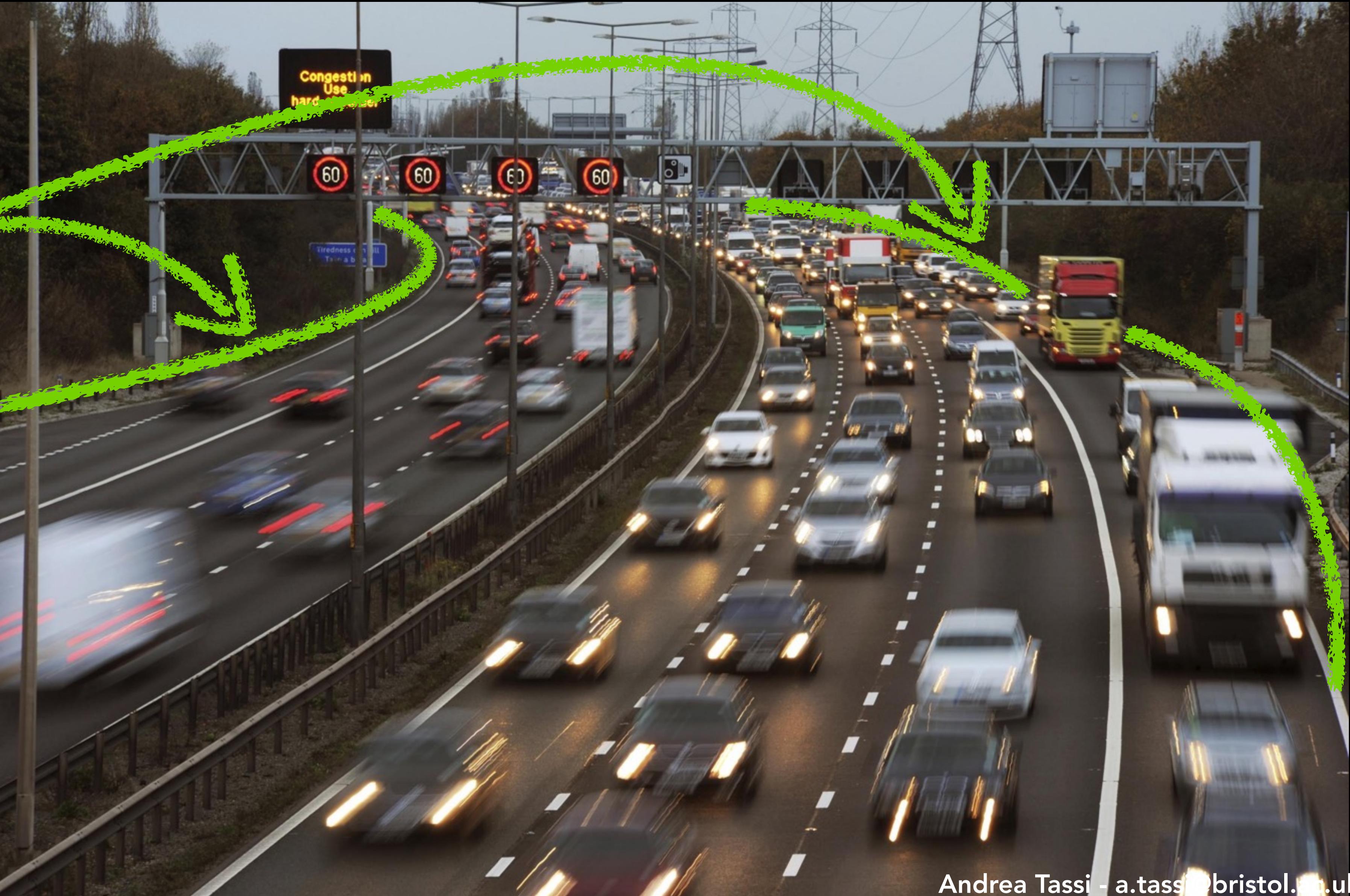
System Model





Practical Highway Scenario

mmWave BSSs
placed at
the side of
the road

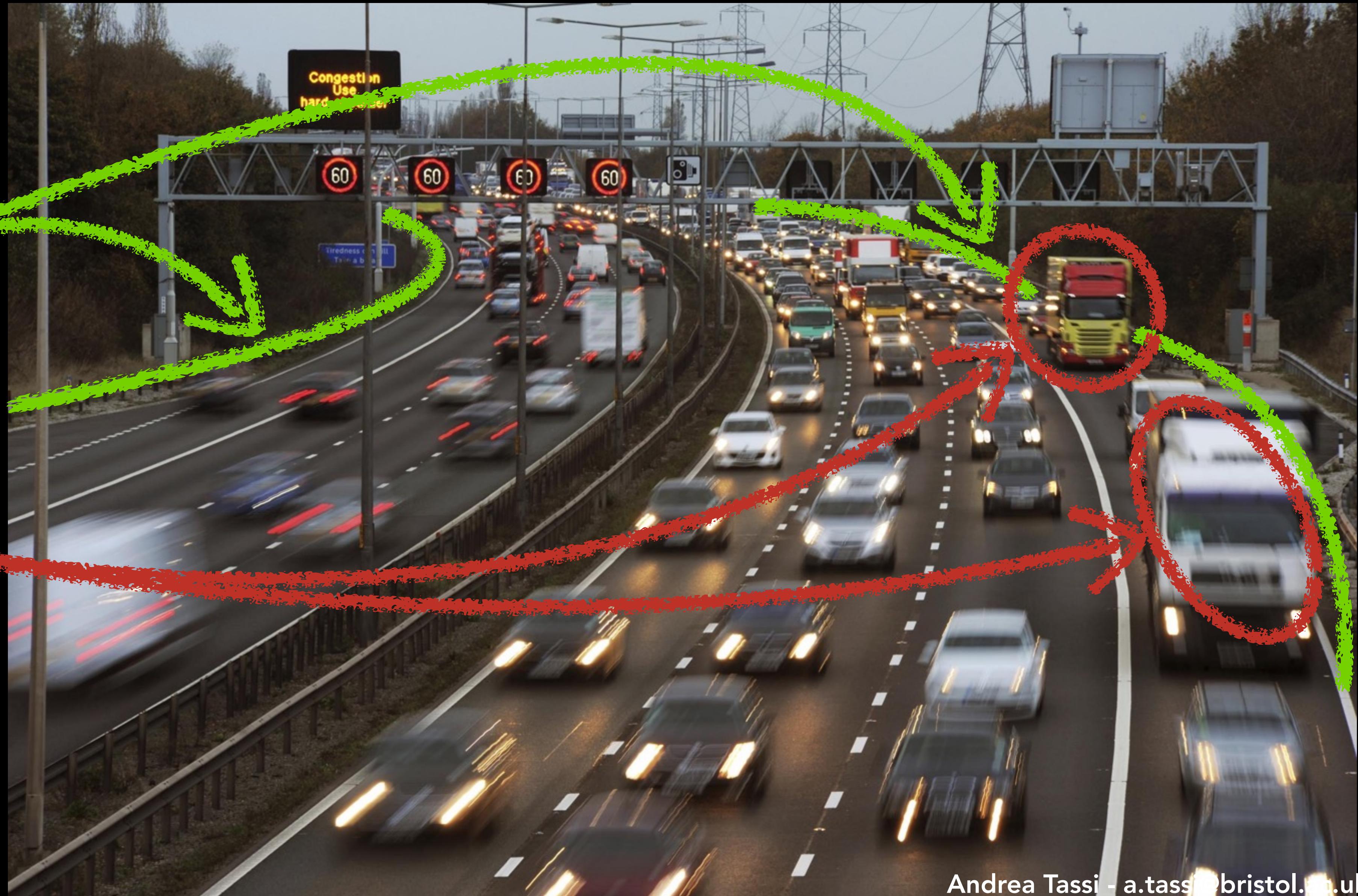




Practical Highway Scenario

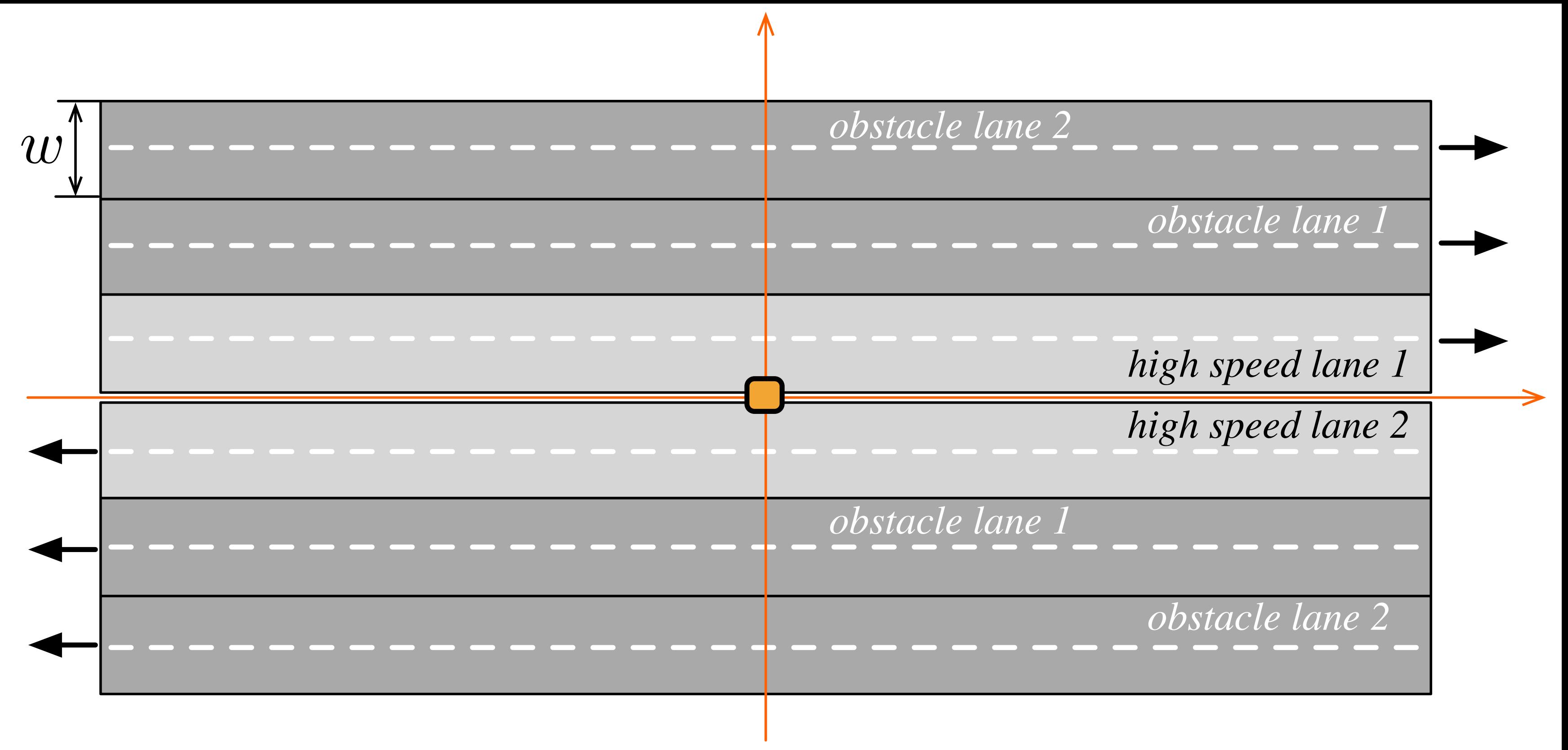
mmWave BSSs
placed at
the side of
the road

Obstacles





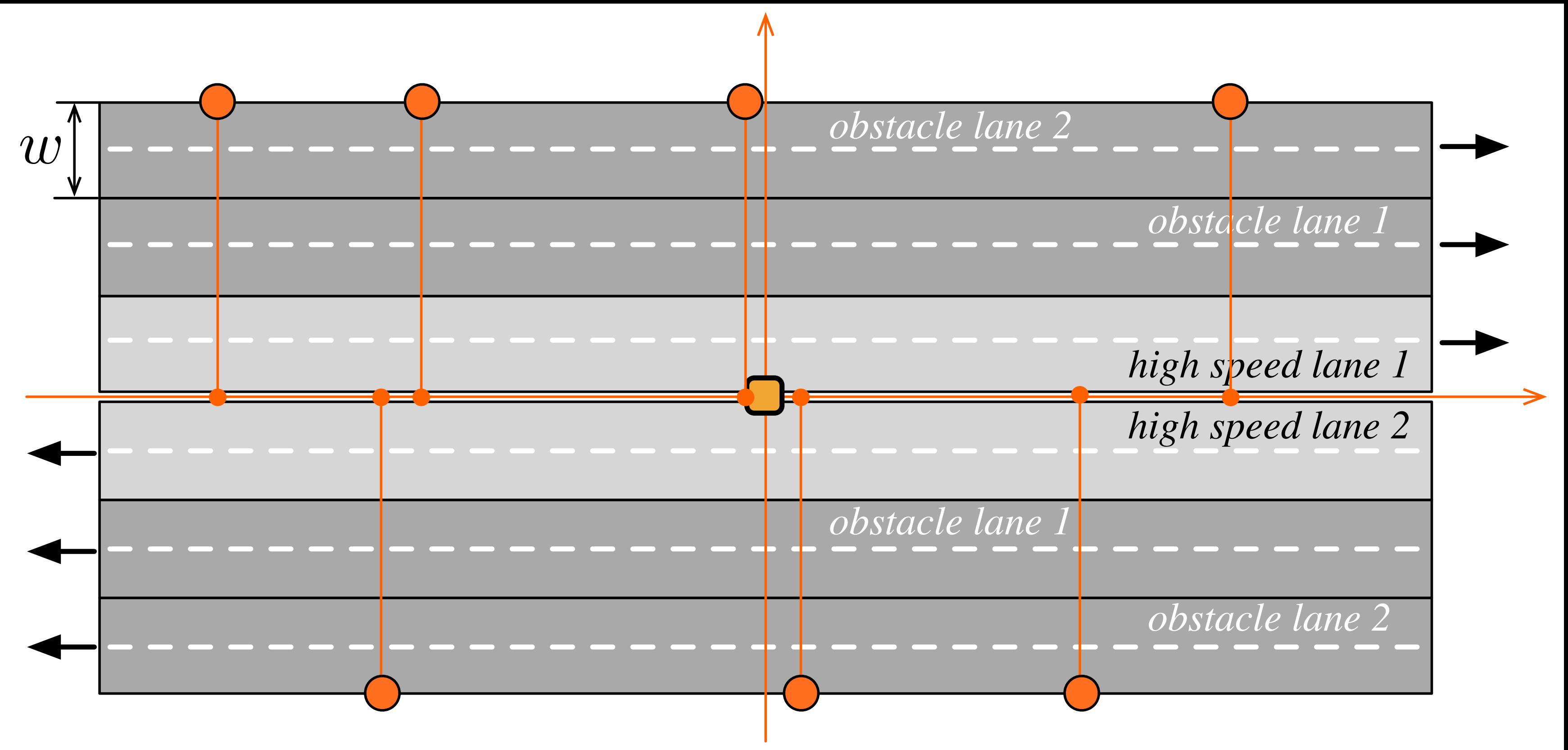
System Model (Road Layout)



- Straight and **homogeneous** road section
- Vehicles are required to drive on the **left hand side** of the road
- We characterize the performance of a **standard user** placed at the **origin of the axis**.



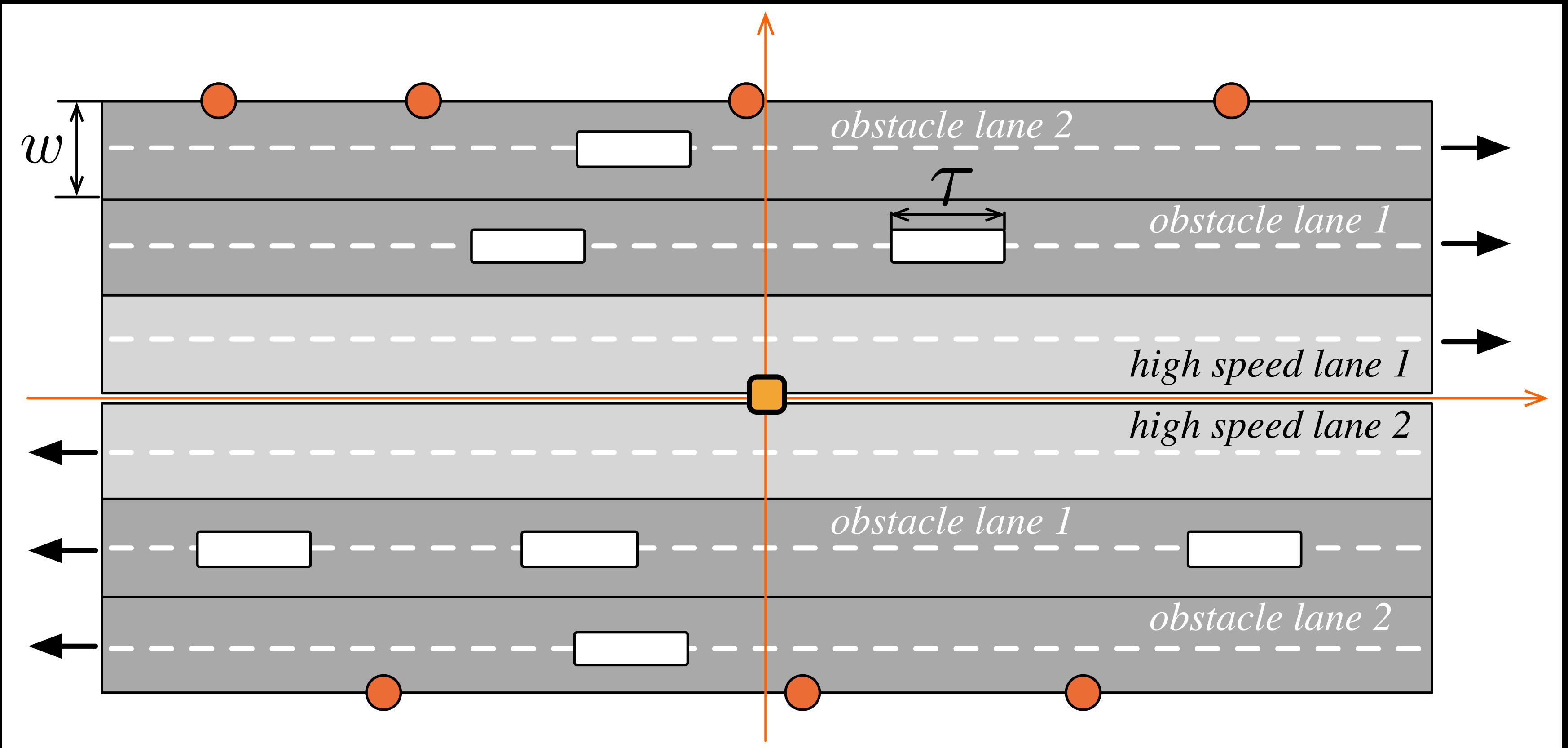
System Model (BS Distribution)



- x -comp. of BS positions follow a 1D PPP of density λ_{BS}
- A BS is placed on a side of the road (upper/bottom side) with probability $q = 0.5$. Hence, BSs on a side of the road define a 1D PPP of density $q\lambda_{\text{BS}}$



System Model (Blockage Distribution)

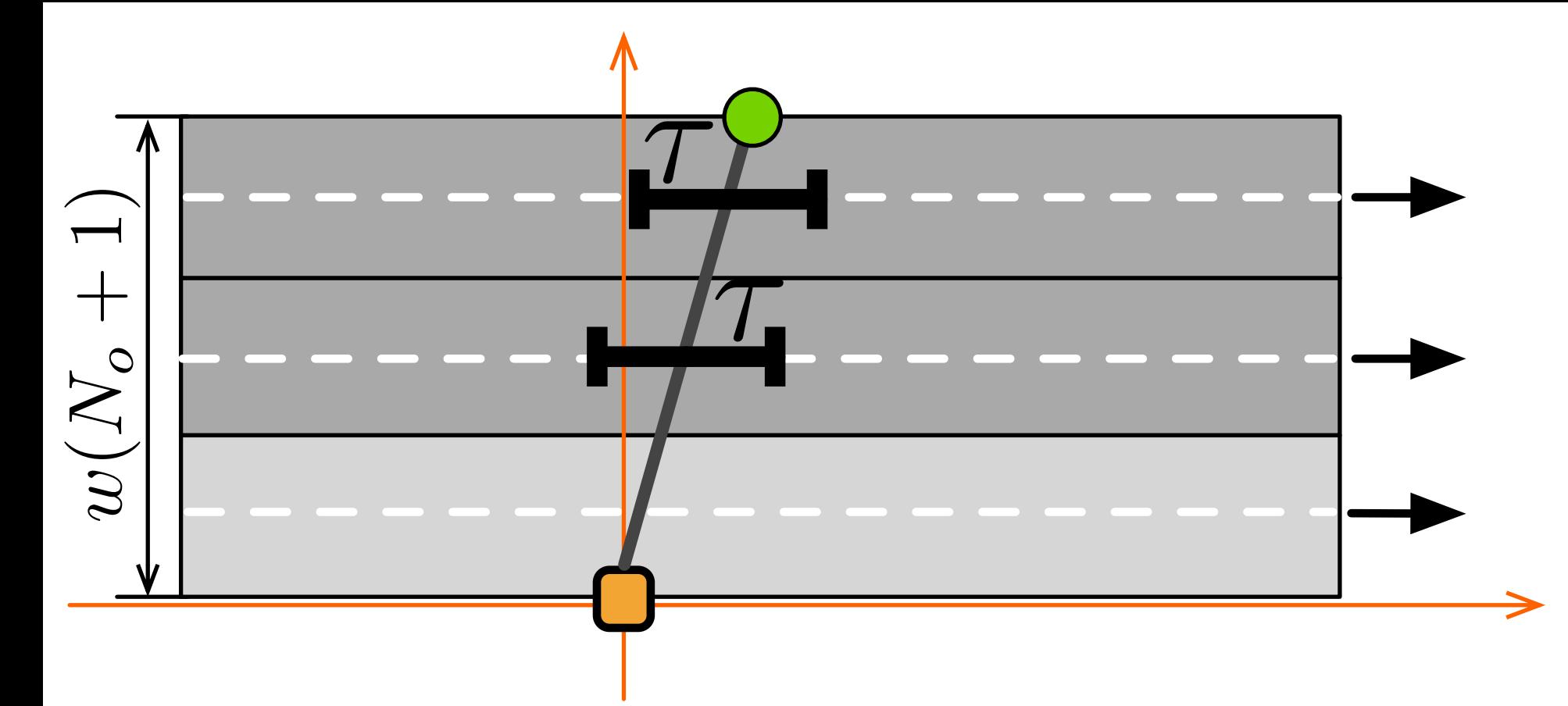
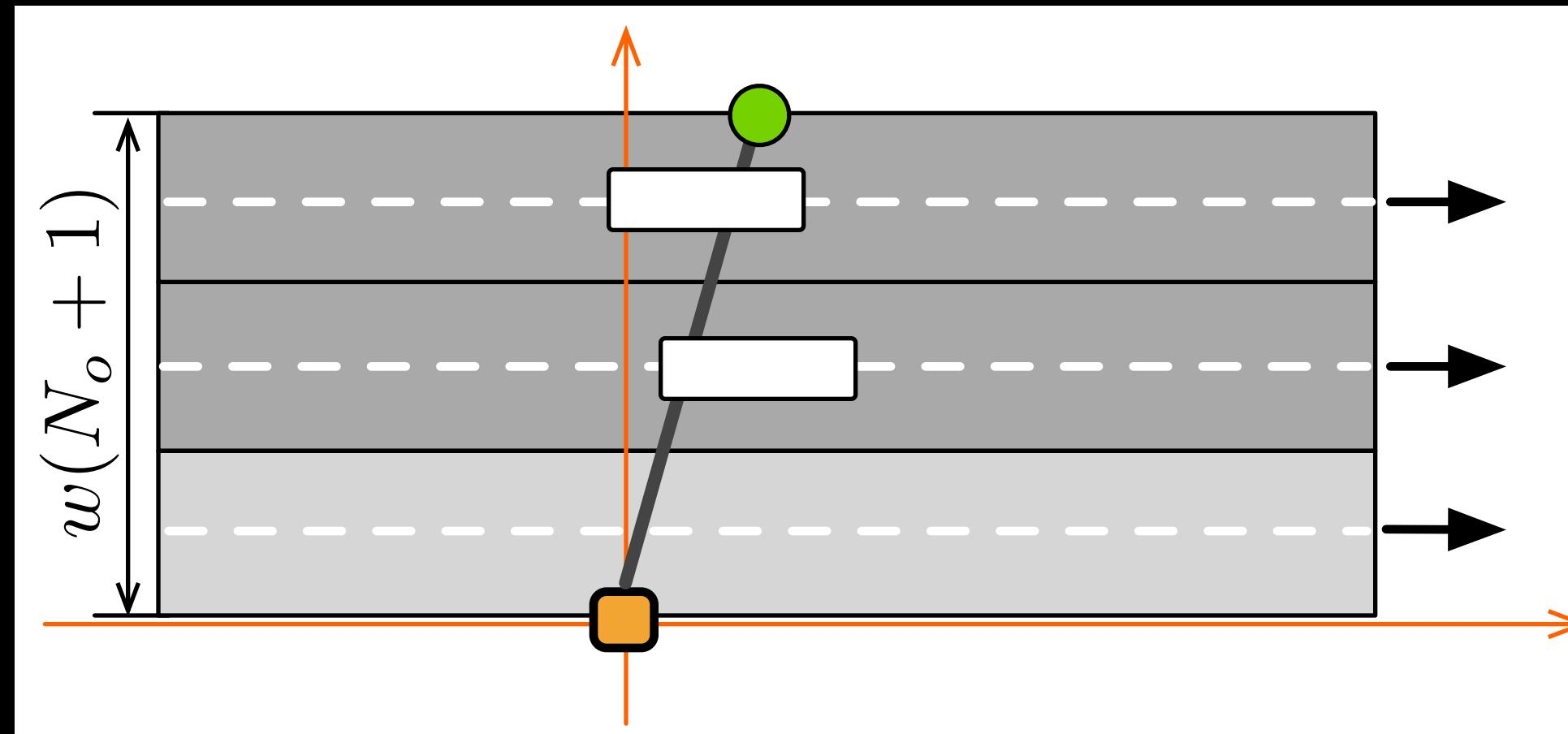


- Obstacles on each obstacle lane follow a 1D PPP of density $\lambda_{o,\ell}$
- **Obstacle processes are independent** but the blockage density of lane ℓ on each traffic direction is the same
- Each blockage is associated with a **footprint** of length τ



PL Model and User Association

- We approximate p_L with the probability that no blockages are present within a distance of $\tau/2$ on either side of the ray connecting the user to a BS. Hence, our **approximation is independent on the distance** of BS i to O



- The PL function associated with BS i is
$$\ell(r_i) = \mathbf{1}_{i,L} C_L r_i^{-\alpha_L} + (1 - \mathbf{1}_{i,L}) C_N r_i^{-\alpha_N}$$
- The standard user always connects to the BS with the **minimum PL component**



PL Model and User Association

- We approximate p_L with the probability that no blockages are present within a distance of $\tau/2$ on either side of the ray connecting the user to a BS. Hence, our **approximation is independent on the distance** of BS i to O

#Obs. Lane
per driving
direction

$$p_L \approx \prod_{\ell=1}^{N_o} e^{-\lambda_{o,\ell}\tau}$$

1D PPP void
probability

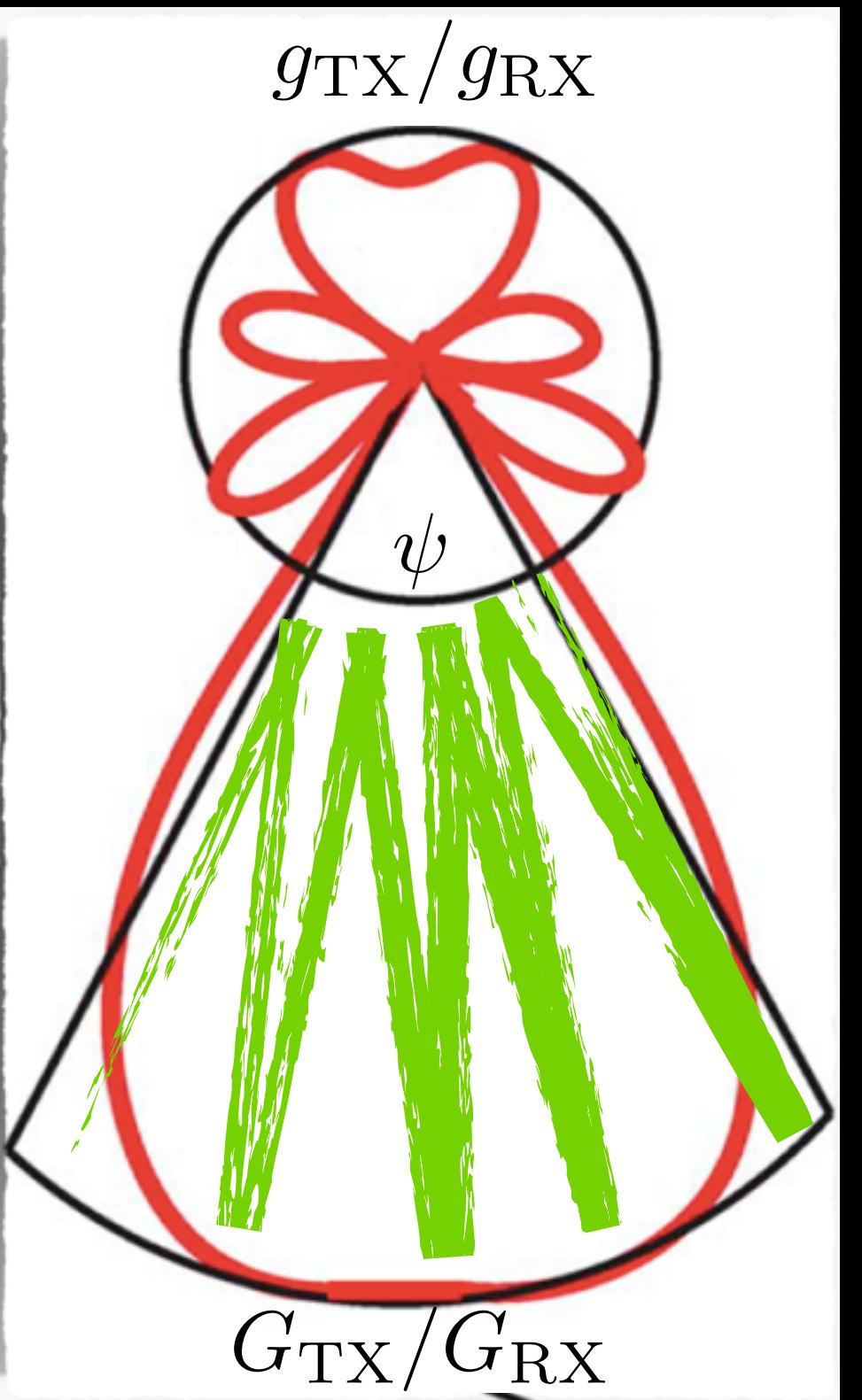
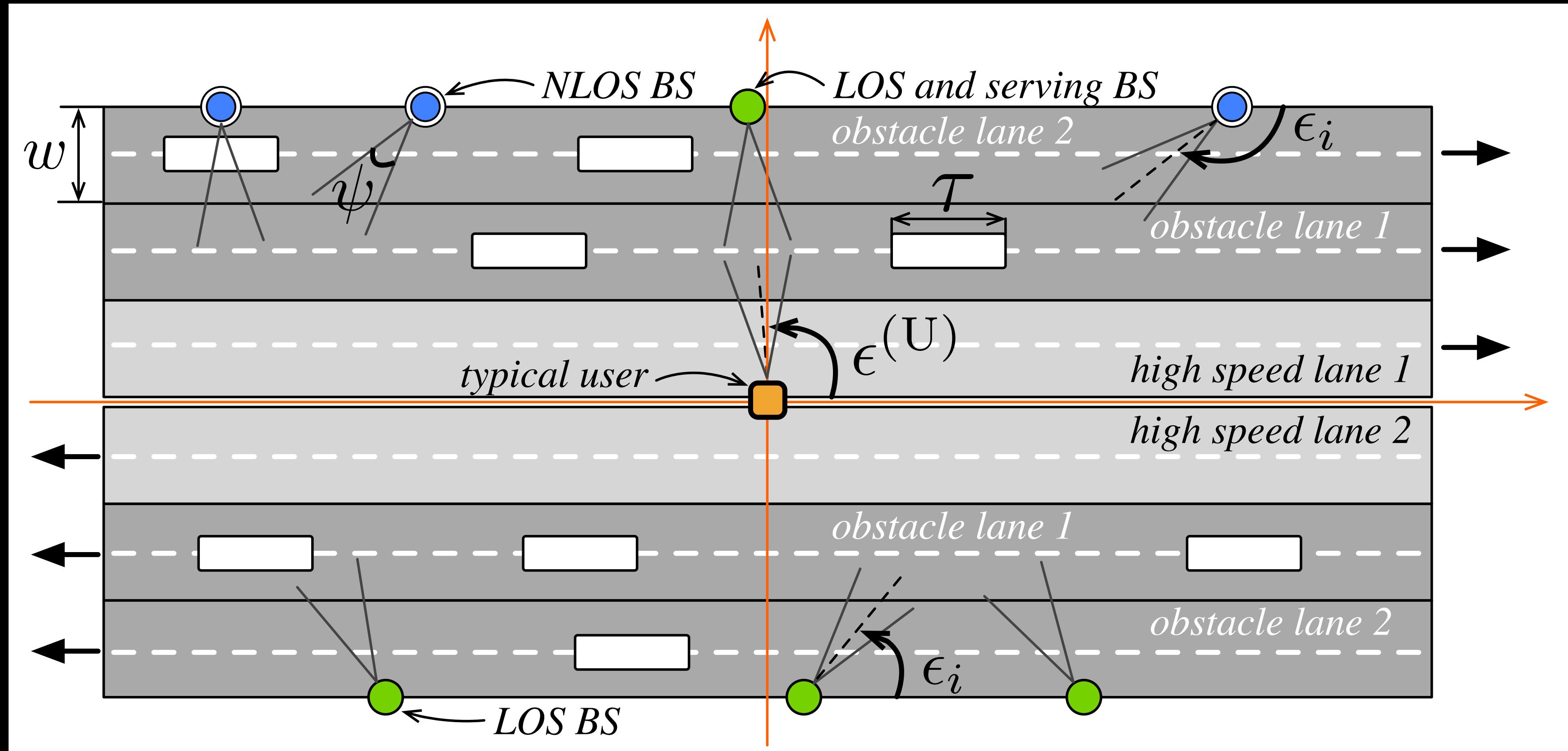
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- The standard user always connects to the BS with the **minimum PL component**



System Model (Beam Steering)



- The **main lobe** of each BS is always entirely directed towards the road
- The **user/BS beam alignment** is assumed error-free
- The beam on an interfering BS is steered uniformly within 0° and 180°



SINR Outage and Rate Coverage





The Probability Framework

- Assume the user connects to BS 1, we define the SINR as

$$\text{SINR}_O = \frac{h_1 \Delta_1 \ell(r_1)}{\sigma + \sum_{j=2}^b h_j \Delta_j \ell(r_j)}$$

normalized thermal noise power

antenna gains $h_j \sim \text{EXP}(1)$

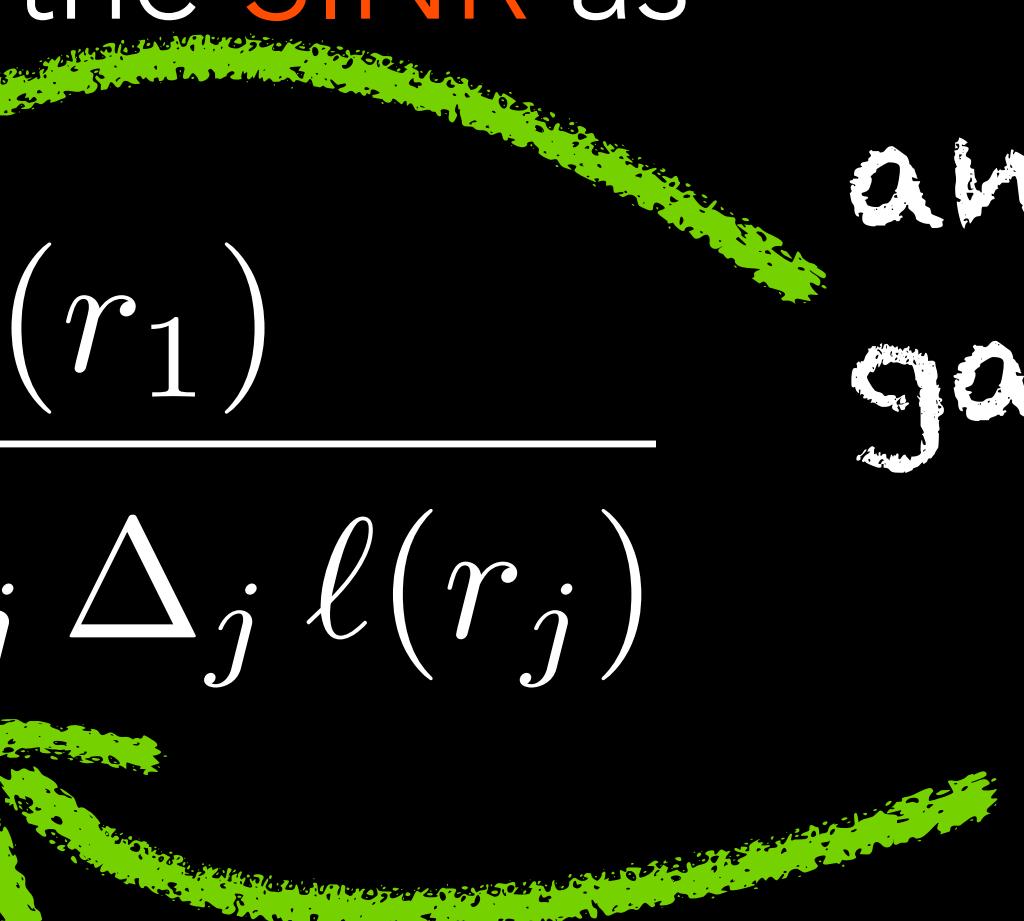


The Probability Framework

- Assume the user connects to BS 1, we define the **SINR** as

$$\text{SINR}_O = \frac{h_1 \Delta_1 \ell(r_1)}{\sigma + \sum_{j=2}^b h_j \Delta_j \ell(r_j)}$$

normalized thermal noise power 

 antenna gains  $h_j \sim \text{EXP}(1)$

- We characterize the following **SINR outage**

$$\overbrace{\mathbb{P}[\text{SINR}_O < \theta]}^{P_T(\theta)} = P_L - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in LOS}]}_{P_{CL}(\theta)} + P_N - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in NLOS}]}_{P_{CN}(\theta)}$$



Probability of Being Served in LOS/NLOS

- The standard user connects to a **NLOS BS** with probability

$$P_N = \int_{w(N_o+1)}^{\infty} f_N(r) e^{-2\lambda_L \sqrt{A_L^2(r) - w^2(N_o+1)^2}} dr$$

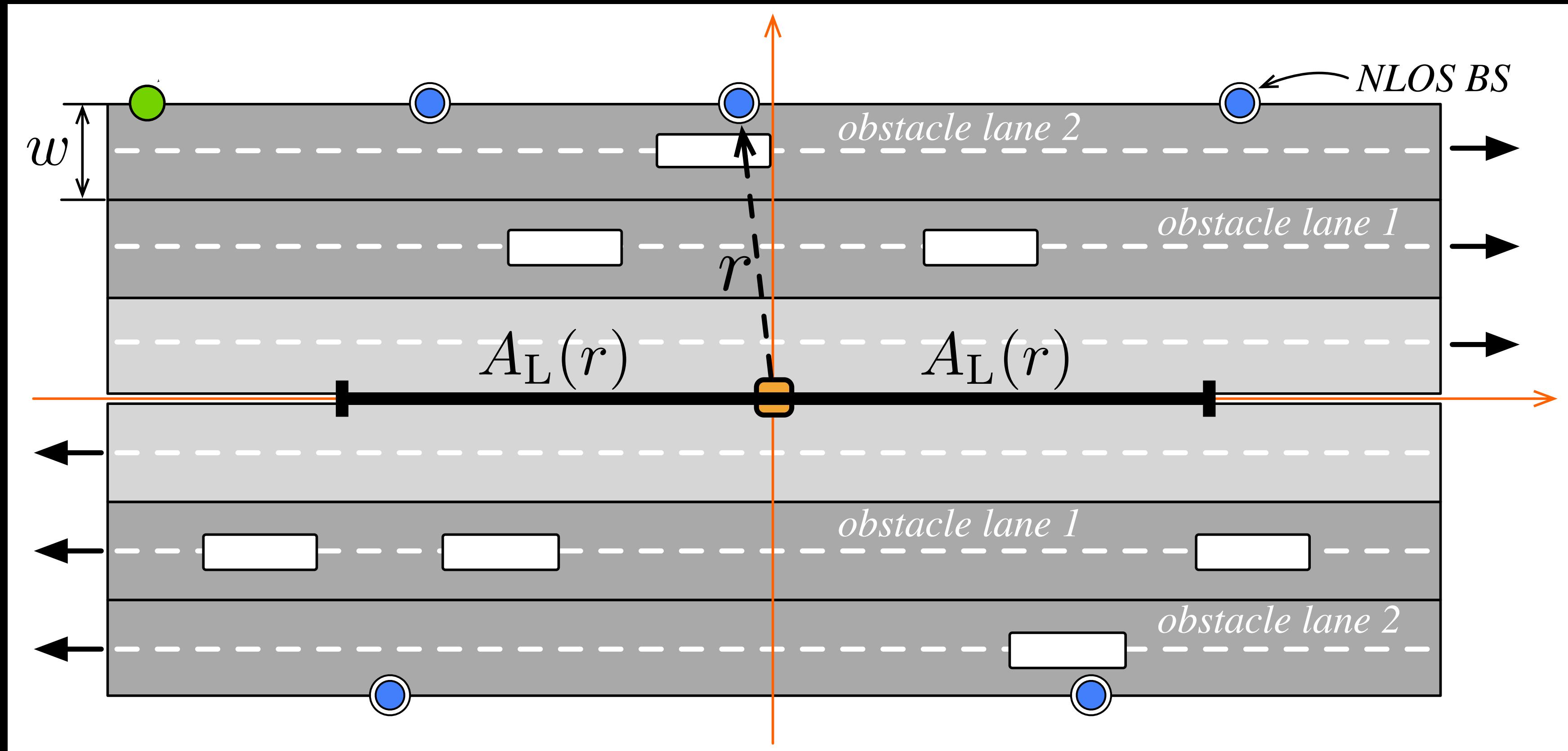
PDF of the closest
NLOS BS

PPP LOS void probability in
the segment $[0, A_L(r)]$

Probability of Being Served in LOS/NLOS

- The standard user connects to a **NLOS BS** with probability

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$$P_N = \int_{w(N_o+1)}^{\infty} f_N(r) e^{-2\lambda_L \sqrt{A_L^2(r) - w^2(N_o+1)^2}} dr$$

where

$$A_L(r) = \max \left\{ w(N_o + 1), \left[\frac{C_N}{C_L} r^{-\alpha_N} \right]^{-\frac{1}{\alpha_L}} \right\}$$

from
 $C_N r^{-\alpha_N} = C_L A_L^{-\alpha_L}$

- While, $P_L = 1 - P_N$



Coverage Probability Terms

$$\underbrace{\mathbb{P}[\text{SINR}_O < \theta]}_{P_T(\theta)} = P_L - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in LOS}]}_{P_{CL}(\theta)} + P_N - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in NLOS}]}_{P_{CN}(\theta)}$$



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Coverage Probability Terms

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Coverage Probability Terms

as $h_1 \sim \text{EXP}(1)$

$$P_{CL}(\theta) = \mathbb{P}\left[\frac{h_1 \Delta_1 \ell(r_1)}{\sigma + I} > \theta \text{ and std. user is served in LOS}\right]$$

$$\stackrel{(i)}{=} \mathbb{E}_I \int_{w(N_o+1)}^{+\infty} e^{-\frac{(\sigma+I)\theta}{\Delta_1 C_L} r_1^{\alpha_L}} f_L(r_1) F_N(A_N(r_1)) dr_1$$

$$\stackrel{(ii)}{=} \int_{w(N_o+1)}^{+\infty} e^{-\frac{\sigma\theta}{\Delta_1 C_L} r_1^{\alpha_L}} \mathcal{L}_{I,L}\left(\frac{\theta r_1^{\alpha_L}}{\Delta_1 C_L}\right) f_L(r_1) F_N(A_N(r_1)) dr_1$$

Expectation Prob. of not being
w.r.t I served in NLOS



Coverage Probability Terms

$$\overbrace{\mathbb{P}[\text{SINR}_O < \theta]}^{P_T(\theta)} = P_L - \underbrace{\mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in LOS}] + P_N - \mathbb{P}[\text{SINR}_O > \theta \text{ and std. user served in NLOS}]}_{P_{CN}(\theta)}$$

- As α_N increases, in order to be convenient, a NLOS BS has to be quite close to O . Up to a point where P_L is (almost) 1. If so,

$$P_T(\theta) \cong 1 - \int_{w(N_o+1)}^{+\infty} e^{-\frac{\theta\sigma}{\Delta_1 C_L} r_1^{\alpha_L}} \mathcal{L}_{I,L}\left(\frac{\theta r_1^{\alpha_L}}{\Delta_1 C_L}\right) f_L(r_1) dr_1$$



Coverage Probability Terms

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- The rate coverage follows from the Fubini's theorem (for a bandwidth W)

$$R_C(\kappa) = 1 - P_T(2^{\kappa/W} - 1)$$



$\mathcal{L}_I(s)$

at a glance...





A Fundamental Result

- We proved that the Laplace transform of the interference component generated by the BSs on the upper/bottom side of the road ($S = U, S = B$) that are in LOS/NLOS with the user ($E = L, E = N$) can be approximated as

$$\mathcal{L}_{I_{S,E},E_1}(s) \cong \prod_{\substack{S_1 \in \{U,B\}, \\ (a,b,\Delta) \in \mathcal{C}_{|\mathbf{x}_1|,S_1,E_1,S,E}}} \sqrt{\mathcal{L}_{I_{S,E},E_1}(s; a, b, \Delta)}$$

Conditioned of being served in LOS/NLOS ($E_1 = L, E_1 = N$).

- Where the fundamental Laplace transform term is...



A Fundamental Result

$$\mathcal{L}_{I_{S,E}, \mathbb{E}_1}(s; a, b, \Delta) \cong \exp\left(-\left(\mathbb{E}_h[\Theta(h, \Delta)] + \mathbb{E}_h[\Lambda(h, \Delta)]\right)\right)$$

$$\mathbb{E}_h[\Theta(h, \Delta)] = 2q\lambda_E \left[x^{-\alpha_E^{-1}} \left(1 - \frac{1}{s\Delta x + 1} \right) \right]_{x=a^{-\alpha_E}}^{b^{-\alpha_E}}$$

$$\begin{aligned} \mathbb{E}_h[\Lambda(h, \Delta)] &= -2q\lambda_E (s\Delta)^{\frac{1}{\alpha_E}} \left[t(-t^{-1})^{-\frac{1}{\alpha_E}} \Gamma\left(\frac{1}{\alpha_E} + 1\right) \right. \\ &\quad \left. \cdot {}_2F_1\left(\frac{1}{\alpha_E}, \frac{1}{\alpha_E} + 1; \frac{1}{\alpha_E} + 2; -t\right) \right]_{t=-(s\Delta a^{-\alpha_E} + 1)^{-1}}^{-(s\Delta b^{-\alpha_E} + 1)^{-1}} \end{aligned}$$



A Fundamental Result

$$\mathcal{L}_{I_{S,E}, \mathbb{E}_1}(s; a, b, \Delta) \simeq \exp\left(-\left(\mathbb{E}_h[\Theta(h, \Delta)] + \mathbb{E}_h[\Lambda(h, \Delta)]\right)\right)$$

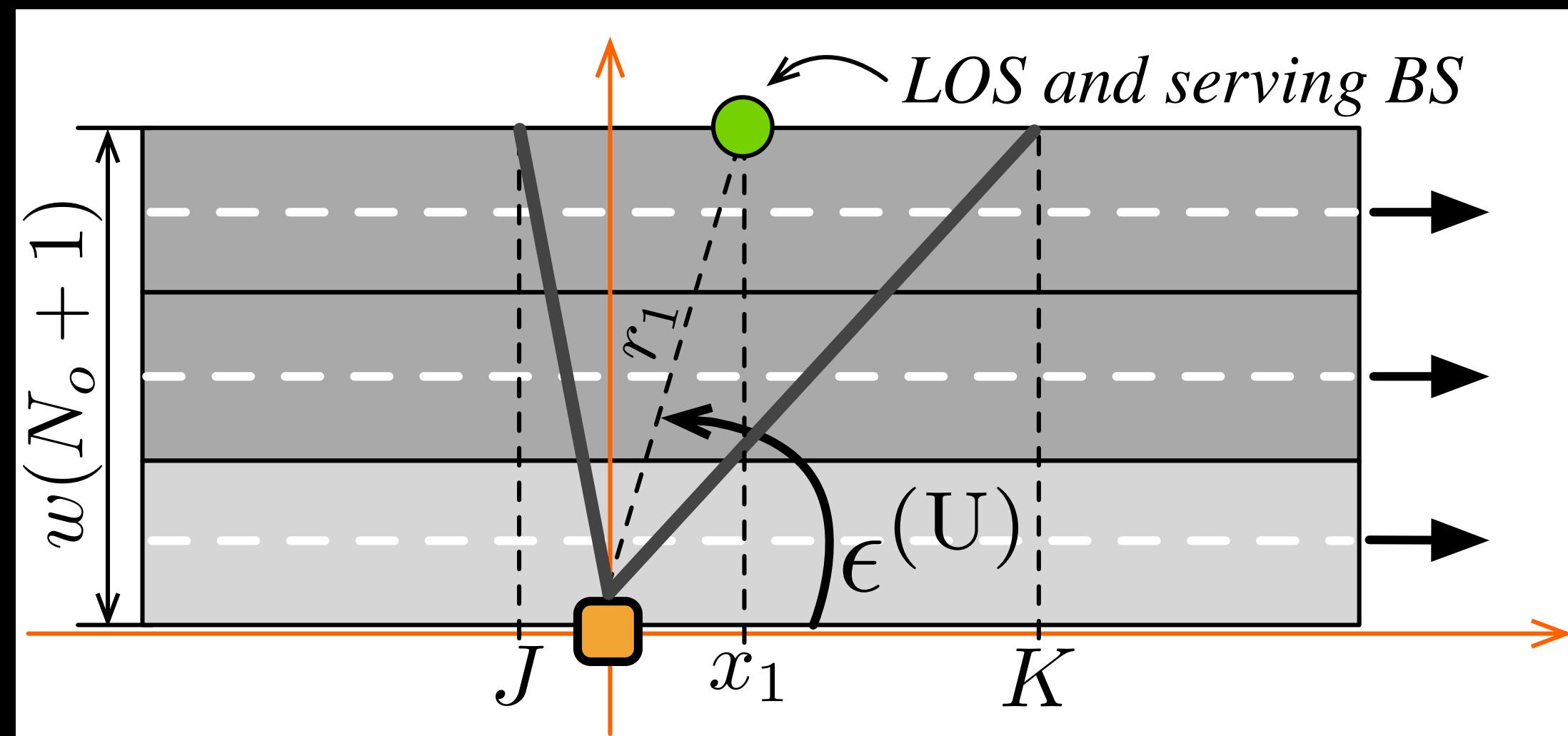
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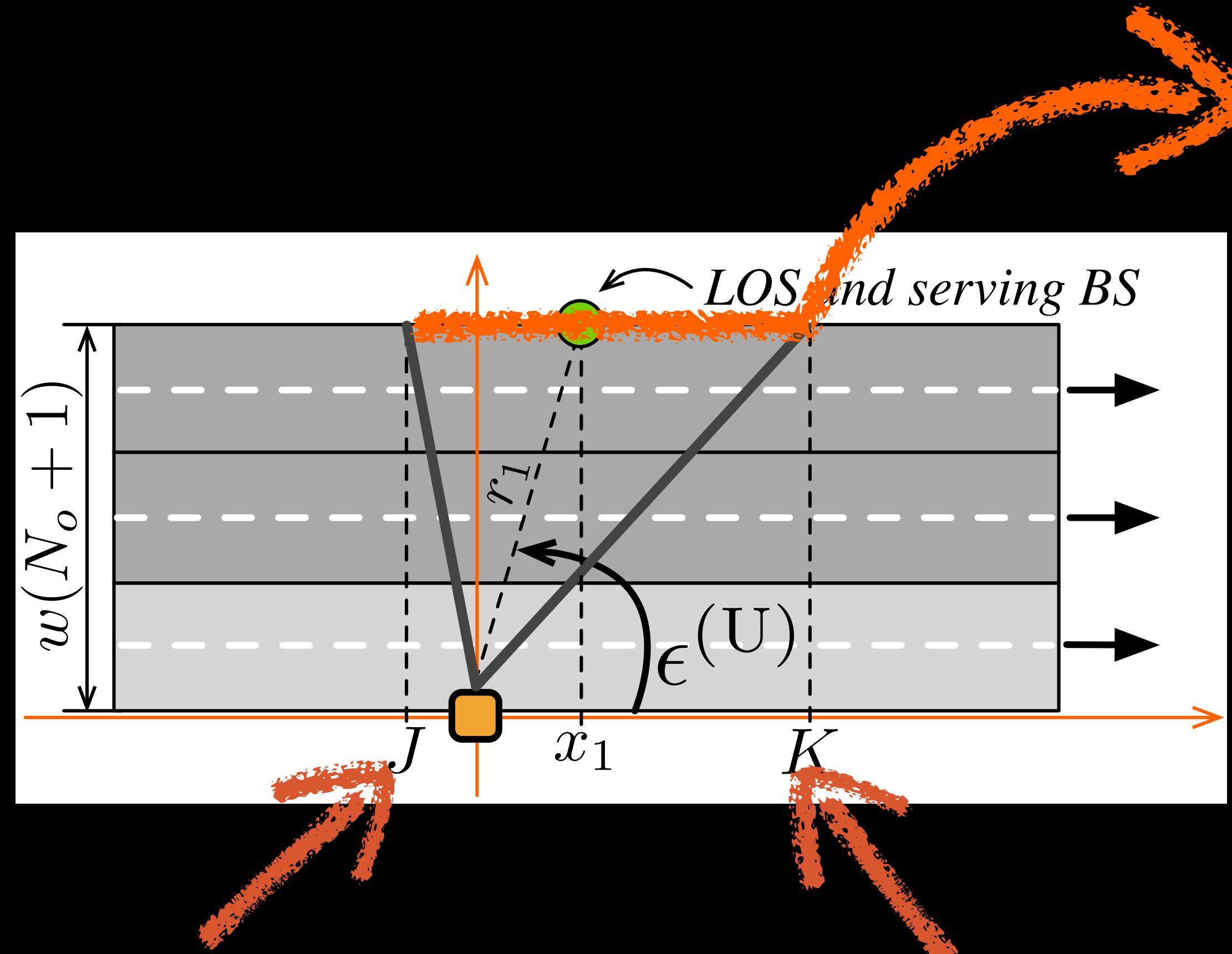
Parametrization of $\mathcal{L}_{\text{I}_{\text{S},\text{E}},\text{E}_1}$

- For simplicity, we assume that the TX antenna gain is always equal to the minimum value.
- However, we characterize the RX antenna gain.



Parametrization of $\mathcal{L}_{\text{IS}, \text{E}, \mathbb{E}_1}$

- For simplicity, we assume that the TX antenna gain is always equal to the minimum value.
- However, we characterize the RX antenna gain.

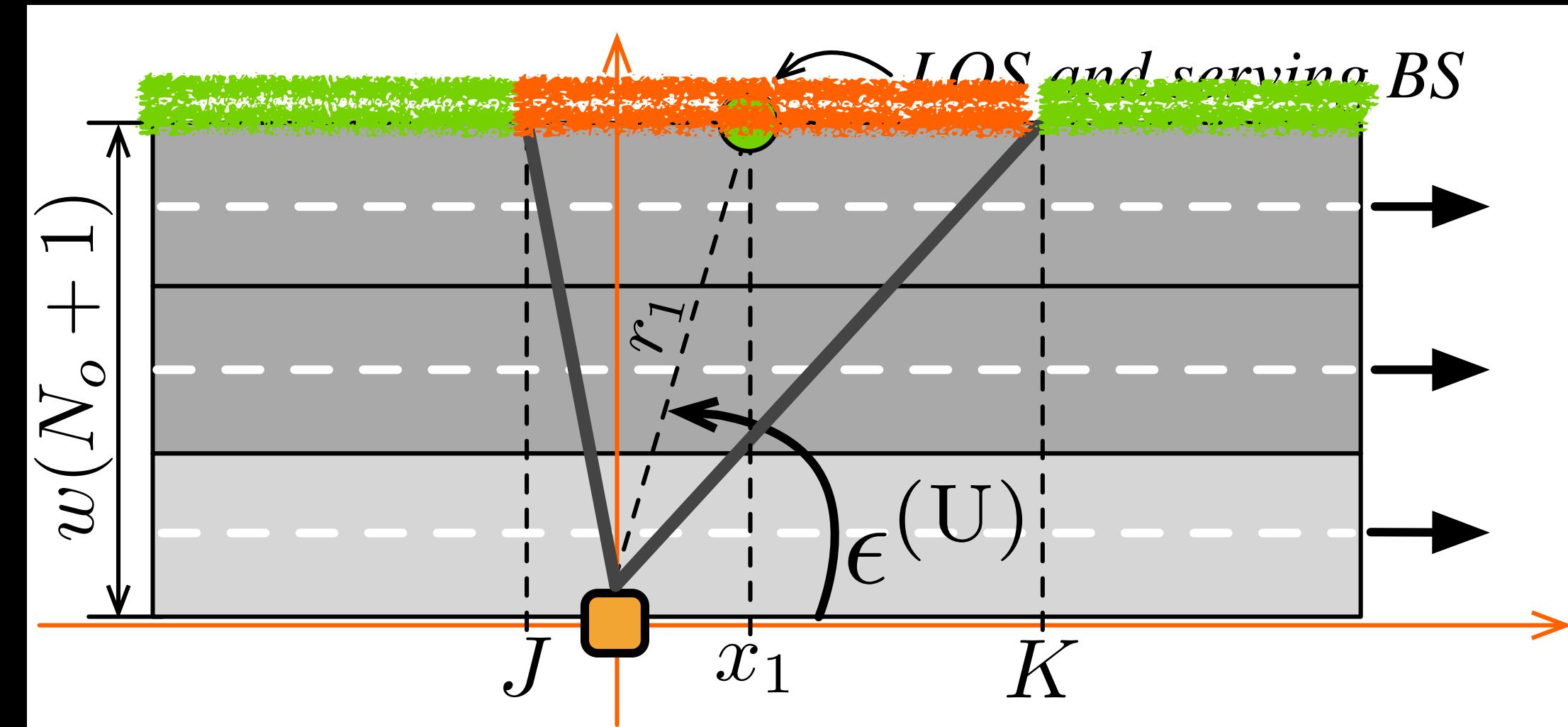




Parametrization of $\mathcal{L}_{\text{IS}, \text{E}, \mathbb{E}_1}$

- For simplicity, we assume that the TX antenna gain is always equal to the minimum value.
- However, we characterize the RX antenna gain.

Min RX gain
Max RX gain





Parametrization of $\mathcal{L}_{I_{S,E},\mathbb{E}_1}$

$< \mathbb{S}_1, \mathbb{E}_1, S, E >$	Conditions on $ x_1 $	$(a, b, \Delta) \in \mathcal{C}_{ x_1 , \mathbb{S}_1, \mathbb{E}_1, S, E}$
$< U, L, U, L >$	For any $ x_1 $ such that $J > 0$	$(x_1 , K, g_{TX}G_{RX}),$ $(K, +\infty, g_{TX}g_{RX}),$ $(x_1 , +\infty, g_{TX}g_{RX})$
	For any $ x_1 $ such that $J \leq 0$	$(x_1 , K, g_{TX}G_{RX}),$ $(K, +\infty, g_{TX}g_{RX}),$ $(x_1 , J , g_{TX}G_{RX}),$ $(J , +\infty, g_{TX}g_{RX})$
$< U, L, U, N >$	For any $ x_1 $ such that $J > 0$	$(x_N(r_1), J, g_{TX}g_{RX}),$ $(x_N(r_1), +\infty, g_{TX}g_{RX}),$ $(J, K, g_{TX}G_{RX}),$ $(K, +\infty, g_{TX}g_{RX})$
	For any $ x_1 $ such that $J \leq 0$	Refer to the case $< U, L, U, L >$ ($J \leq 0$) and replace $ x_1 $ with $x_N(r_1)$
$< U, L, B, L >$	For any $ x_1 $	$(x_1 , +\infty, g_{TX}g_{RX}),$ $(x_1 , +\infty, g_{TX}g_{RX}),$
$< U, L, B, N >$	Refer to the case $< U, L, B, L >$ and replace $ x_1 $ with $x_N(r_1)$	
$< U, N, U, L >$	For any $ x_1 $ such that $x_L(r_1) > K$	Refer to the case $< U, L, B, L >$ and replace $ x_1 $ with $x_L(r_1)$
	For any $ x_1 $ such that $x_L(r_1) \leq K$	Refer to the case $< U, L, U, L >$ and replace $ x_1 $ with $x_L(r_1)$
$< U, N, U, N >$	Refer to the case $< U, L, U, L >$	
$< U, N, B, L >$	Refer to the case $< U, L, B, L >$ and replace x_1 with $x_L(r_1)$	
$< U, N, B, N >$	Refer to the case $< U, L, B, L >$	
Cases where $\mathbb{S}_1 = B, S = B$	Refer to the correspondent cases where $\mathbb{S}_1 = U$ and $S = U$	
Cases where $\mathbb{S}_1 = B, S = U$	Refer to the correspondent cases where $\mathbb{S}_1 = U$ and $S = B$	

- Finally, we can say

$$\mathcal{L}_{I,\mathbb{E}_1}(s) \cong \prod_{S \in \{U,B\}, E \in \{L,N\}} \mathcal{L}_{I_{S,E},\mathbb{E}_1}(s)$$

- For e.g., if $\mathbb{E}_1 = L$ and $J > 0$, it follows

$$\begin{aligned} \mathcal{L}_{I,\mathbb{E}_1}(s) &\cong \mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; |x_1|, K, g_{TX}G_{RX}) \\ &\cdot \mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; x_N(r_1), J, g_{TX}g_{RX}) \\ &\cdot \mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; J, K, g_{TX}G_{RX}) \\ &\cdot (\mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; K, +\infty, g_{TX}g_{RX}))^2 \\ &\cdot (\mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; |x_1|, +\infty, g_{TX}g_{RX}))^3 \\ &\cdot (\mathcal{L}_{I_{S,E},\mathbb{E}_1}(s; x_N(r_1), +\infty, g_{TX}g_{RX}))^3 \end{aligned}$$

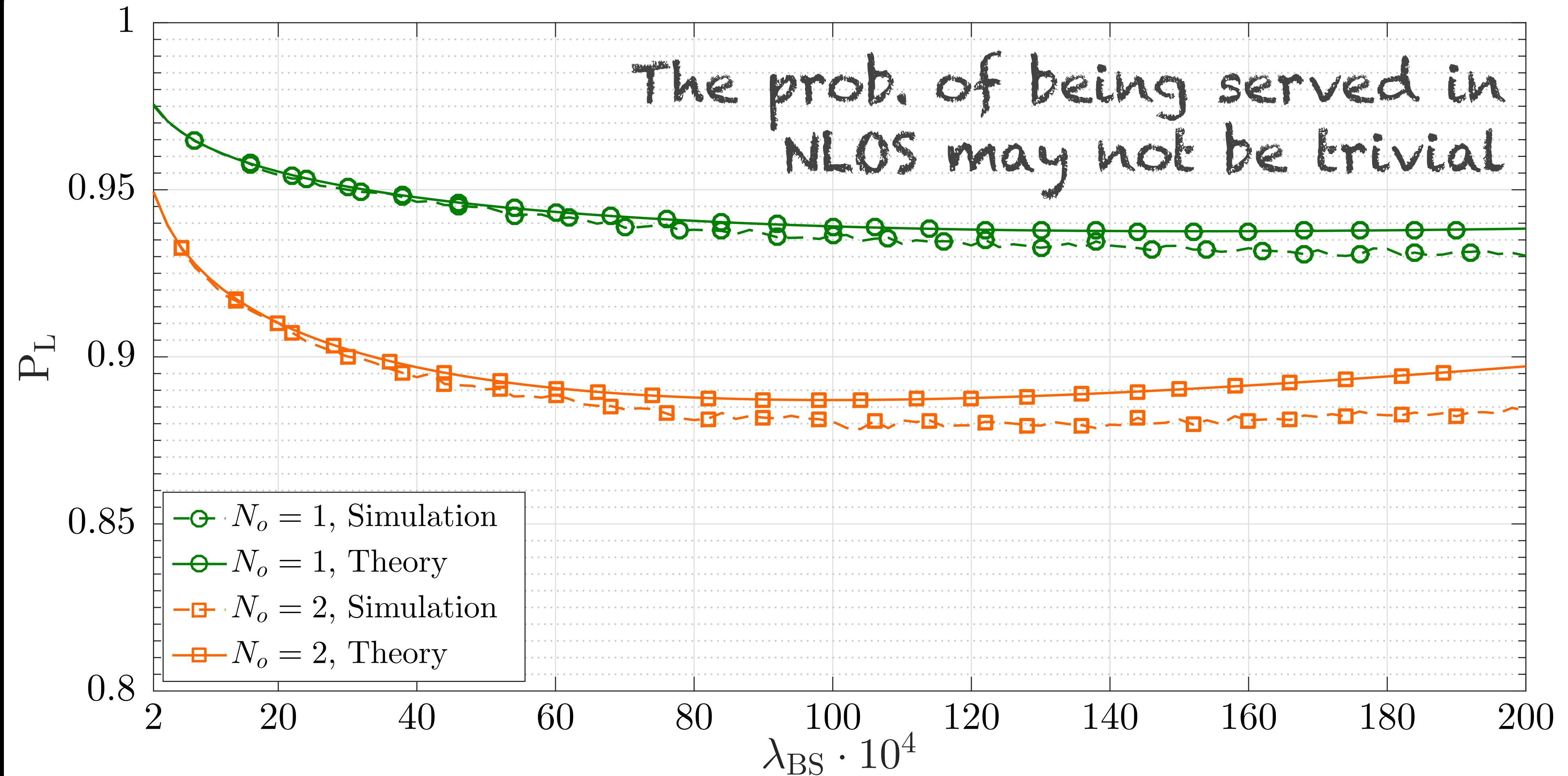


Numerical Results



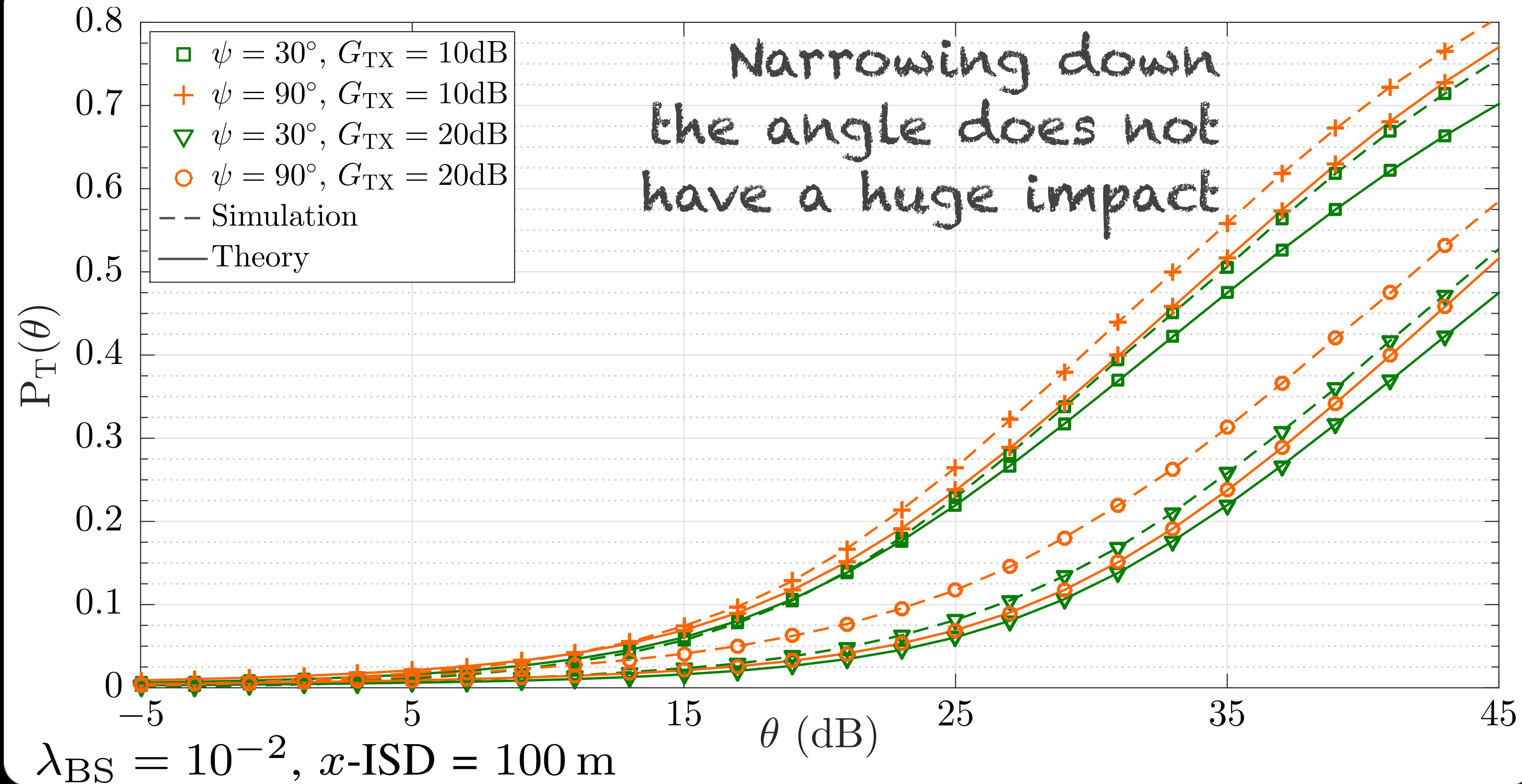


LOS vs. NLOS



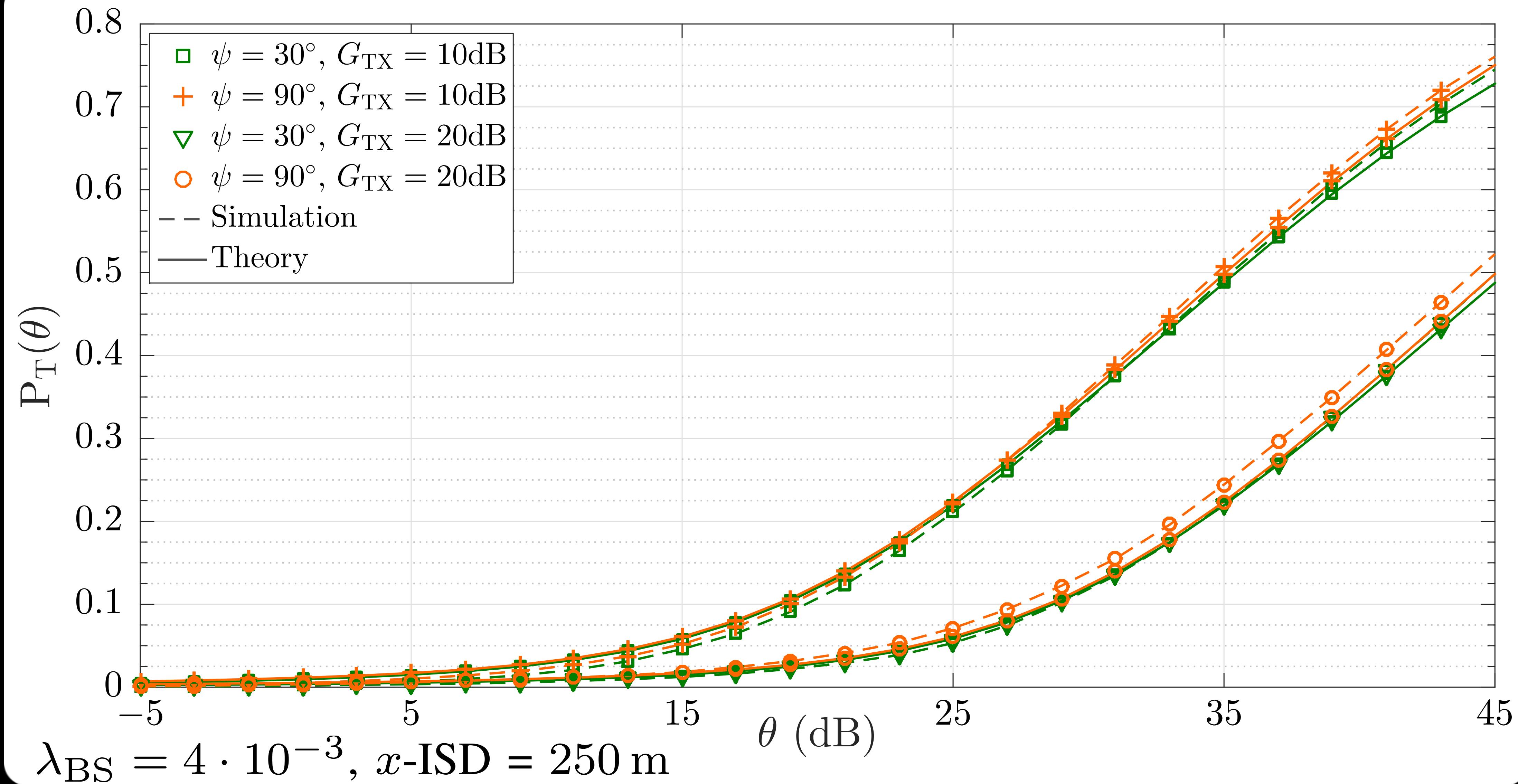


SINR Outage



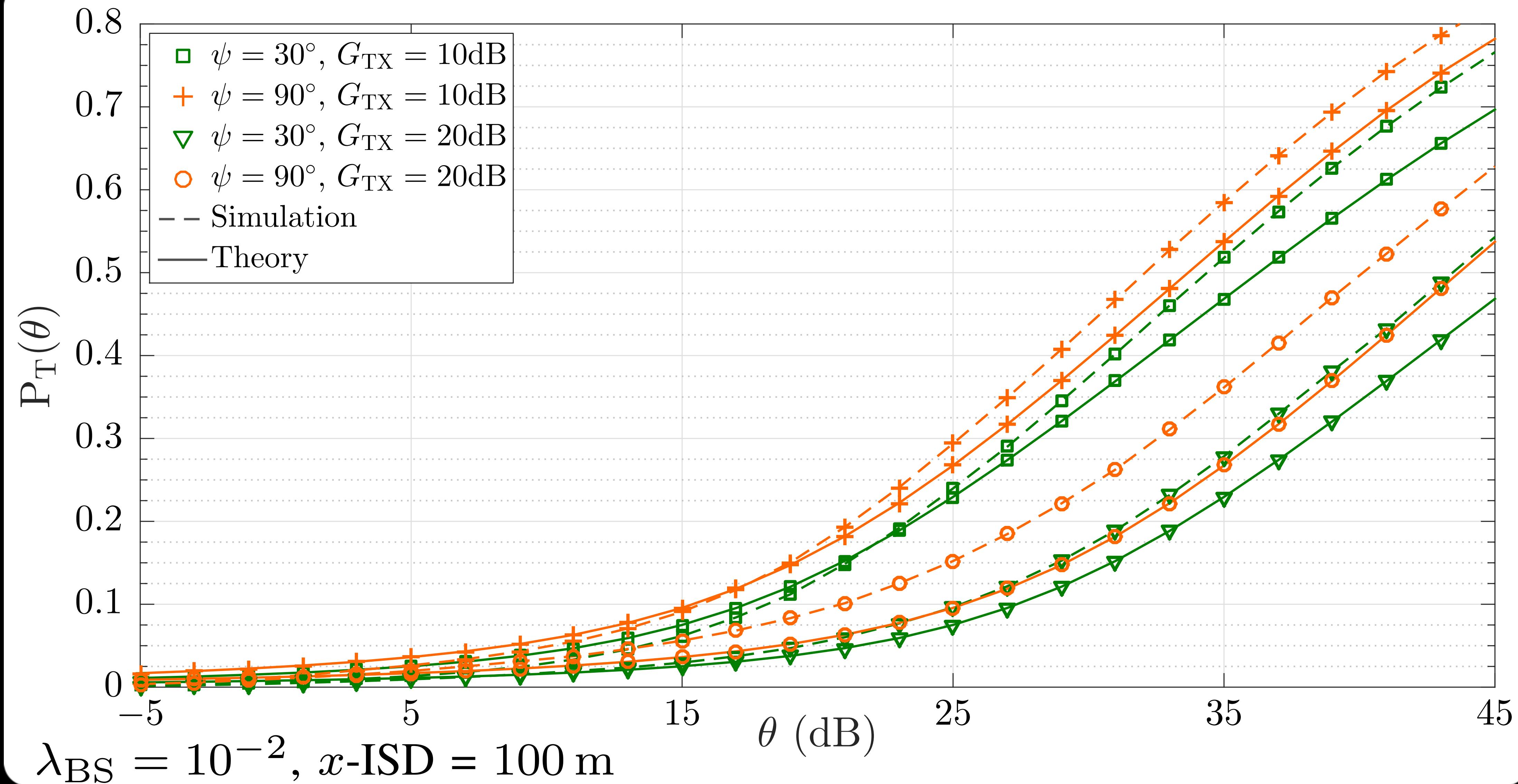


SINR Outage



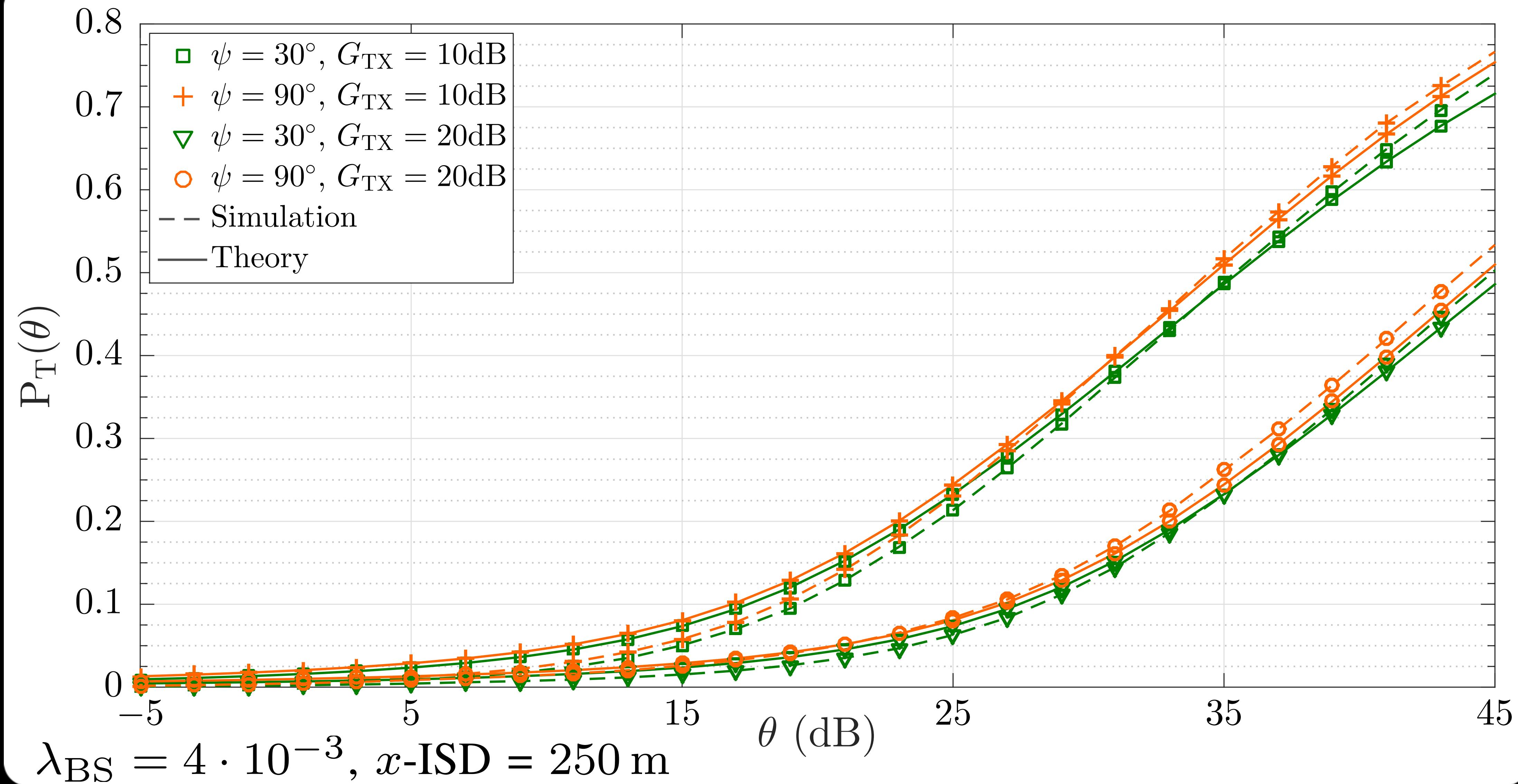


SINR Outage



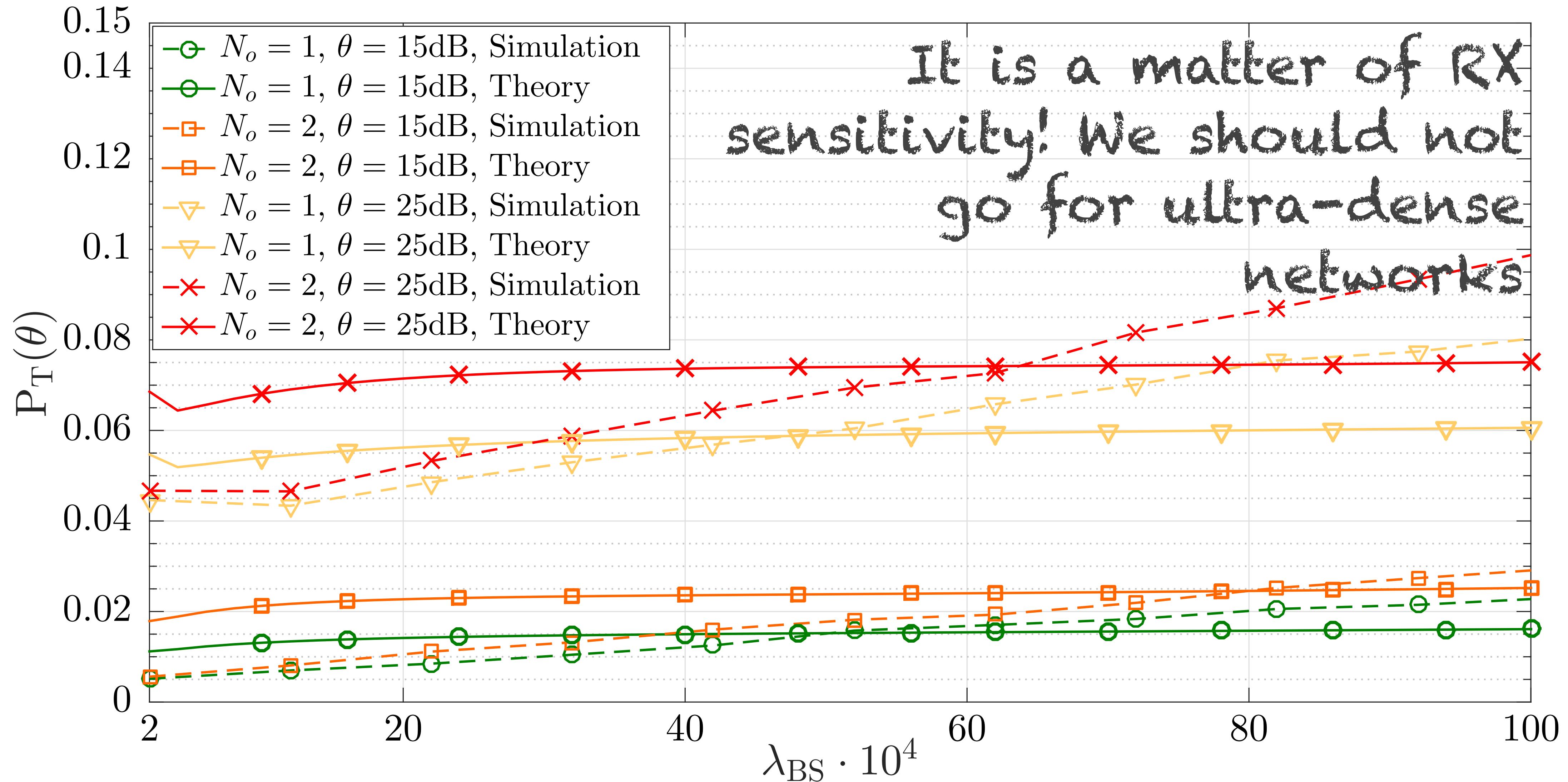


SINR Outage



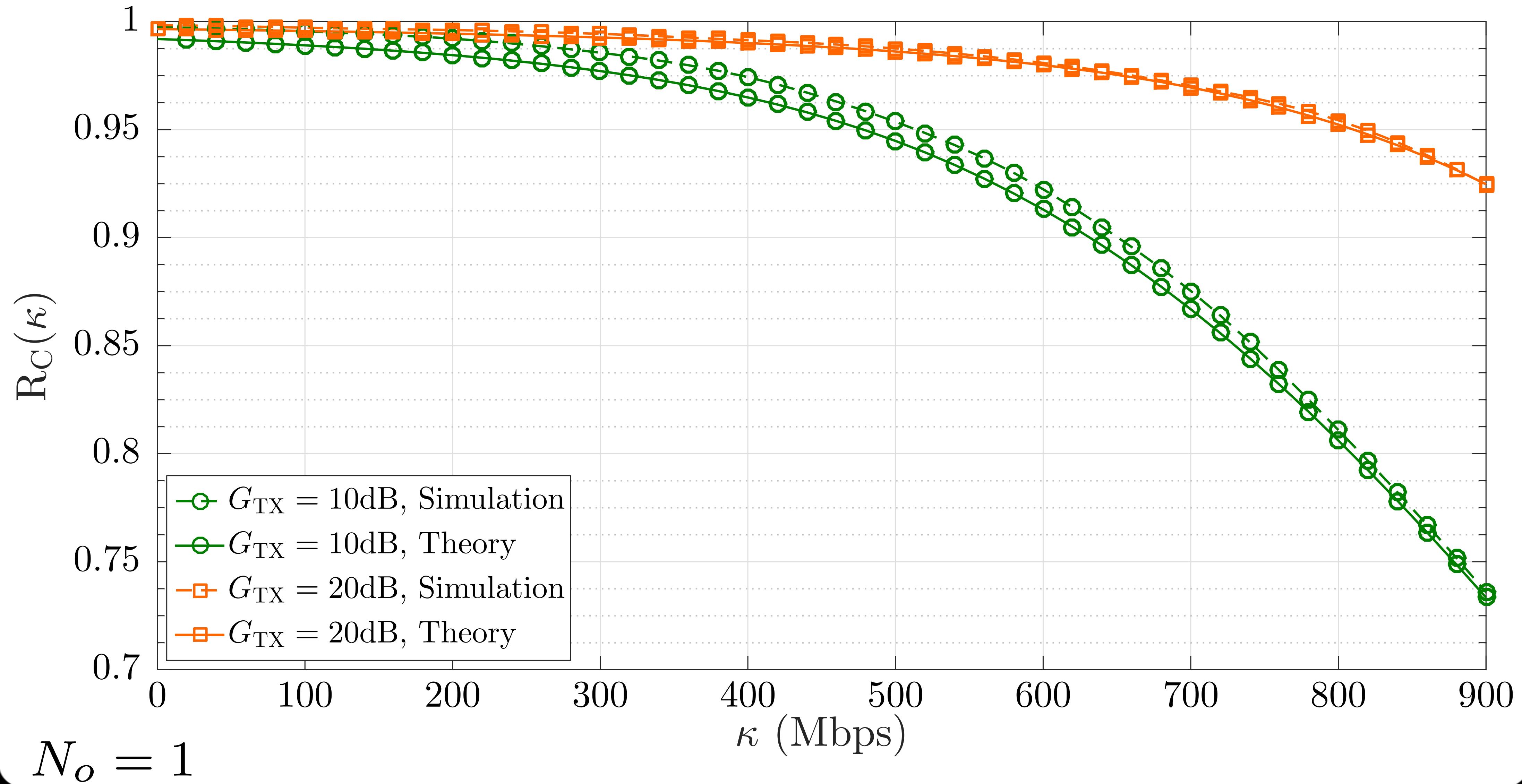


SINR Outage



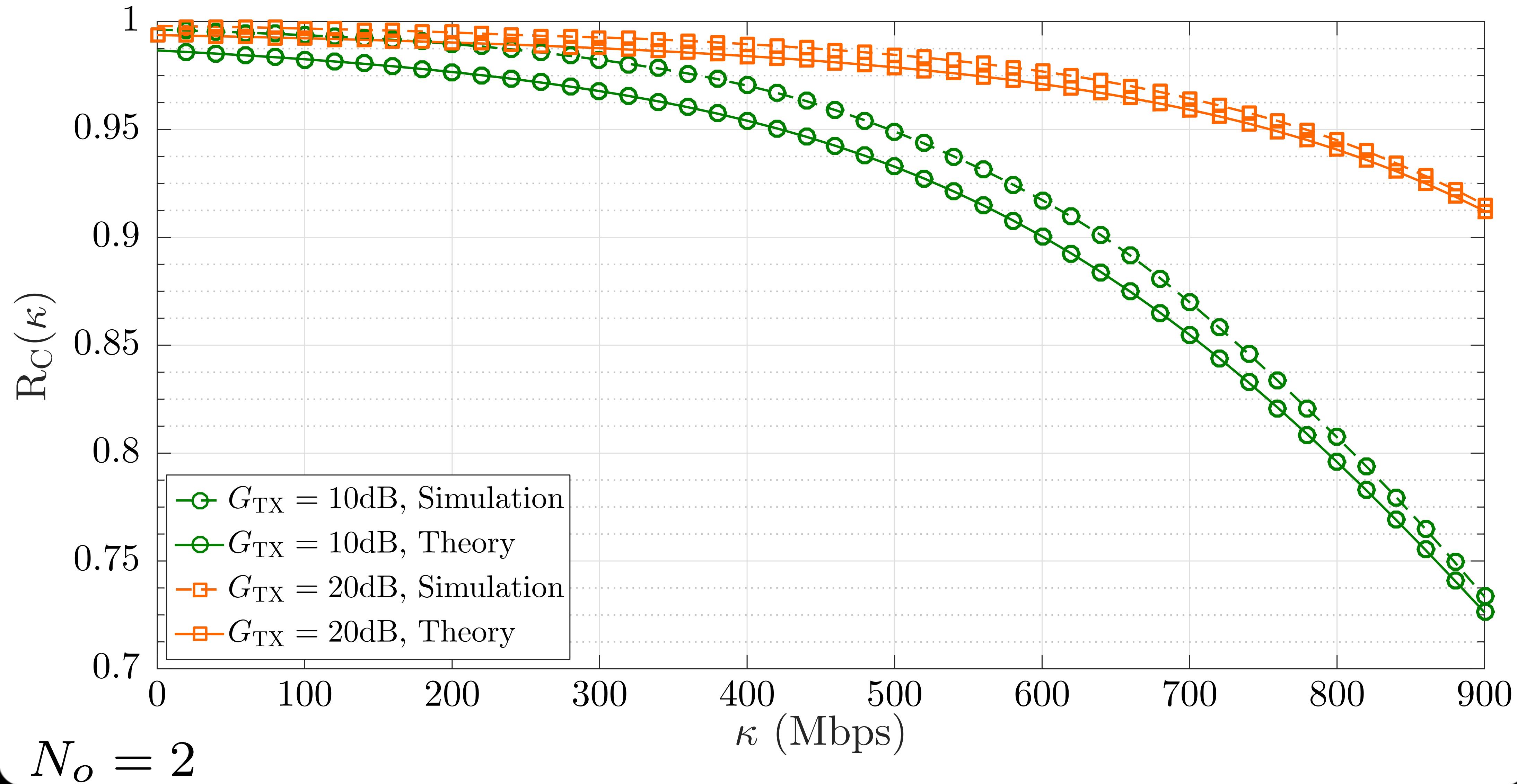


Rate Coverage





Rate Coverage





Conclusions





What Have we seen?

- The probability of being served by a NLOS BS **cannot** be considered negligible.
- By reducing the antenna beamwidth from 30° to 90° does not necessarily have a disruptive impact on the SINR outage probability, and hence, on the rate coverage probability.
- Differently to what happens in bi-dimensional mmWave cellular networks, the BSs density does not largely affect the network performance.
- Overall, for a fixed SINR threshold, the SINR outage probability tends to be minimized by density values associated to sparse network deployments.



Thanks for your attention!

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Belfast, 8th July 2016