

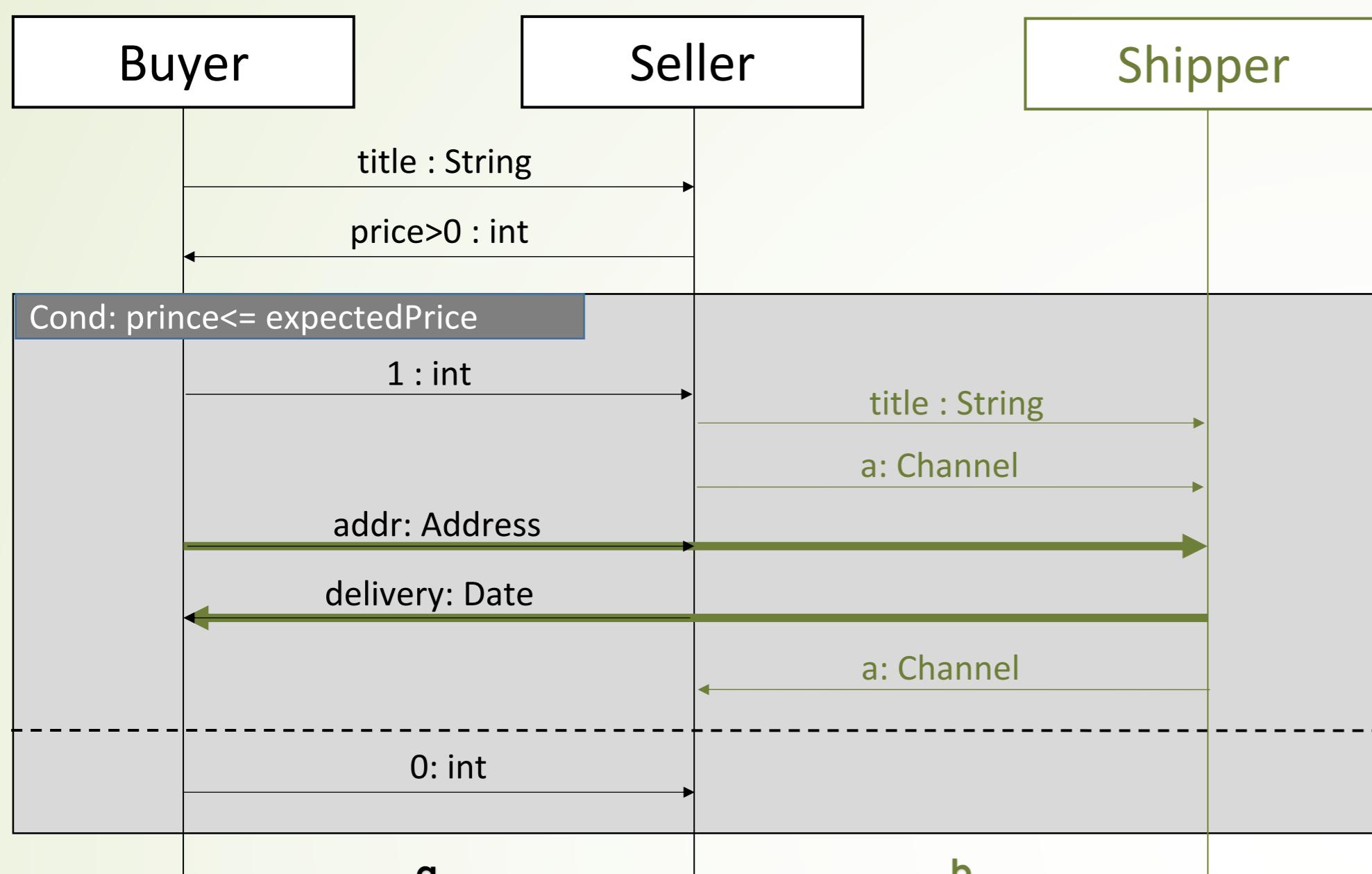
Towards a Session Logic for Multiparty Protocols

by Andreea Costea, Valentina Manea, Wei-Ngan Chin
School of Computing, National University of Singapore

Abstract

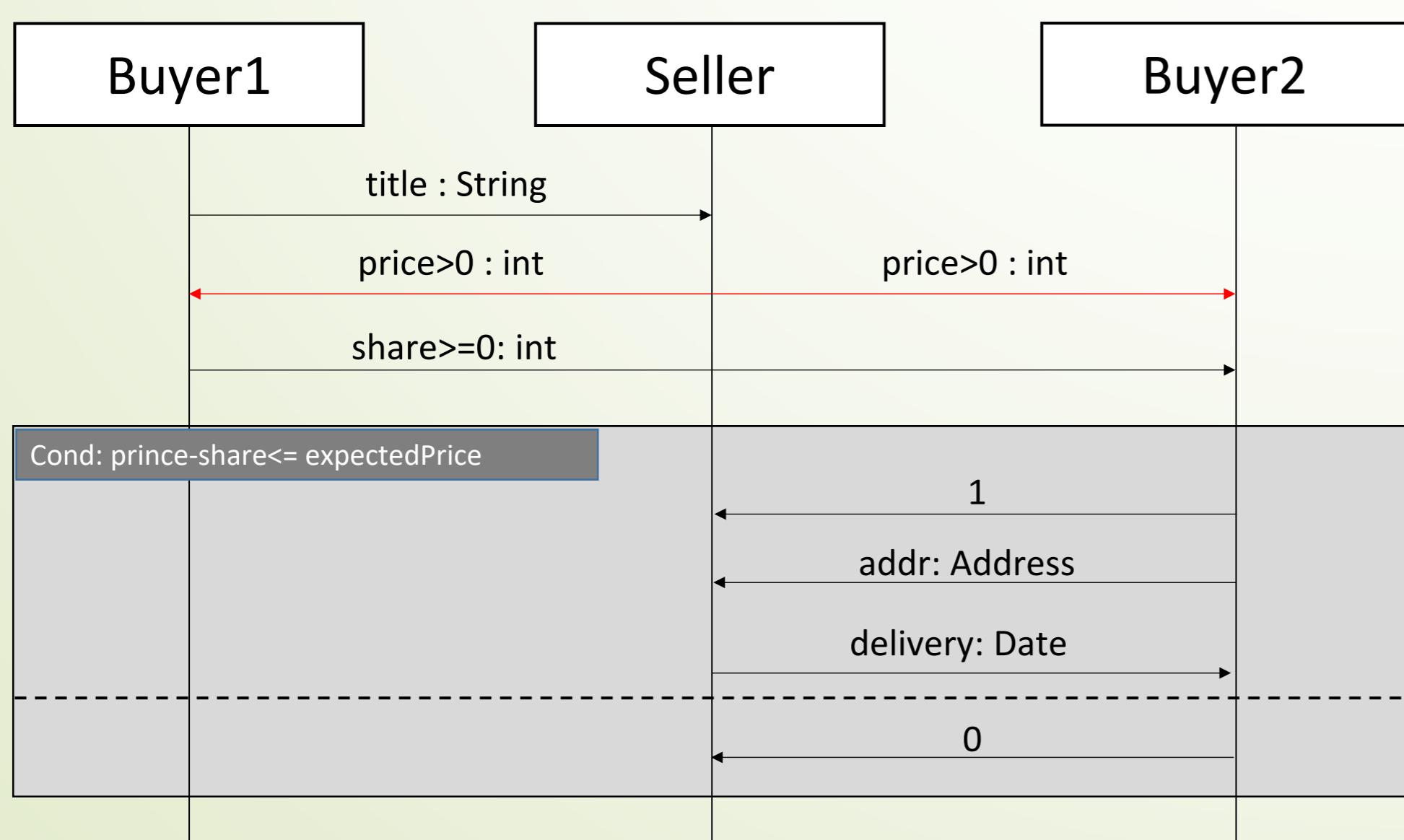
We present a multiparty session logic for reasoning about communication-centered applications. Our logic goes beyond the traditional message-type consistency check and deals with more complex properties of the exchanged messages. Similar to the session type approaches, we propose a specification logic which provides the means to formally describe the communication protocols from a global perspective. Unlike the type checking approaches, our specification logic provides the necessary abstractions to describe a wide range of properties about the exchanged message, such as numeric properties or resource handling.

Example 1: binary session



$$\begin{aligned} \text{buyer}_a &\triangleq !\text{String}; ?\text{int}; ((!1; !\text{Address}; ?\text{Date}) \vee !0) \\ \text{seller}_a &\triangleq ?\text{String}; !\text{int}; ((?1; ?\text{Address}; !\text{Date}) \vee ?0) \\ \text{seller}_b &\triangleq !\text{String}; !v \cdot \mathcal{C}(v, ?\text{Address}; !\text{Date}); ?v \cdot \mathcal{C}(v, \text{emp}) \\ \text{shipper}_b &\triangleq ?\text{String}; ?v \cdot \mathcal{C}(v, ?\text{Address}; !\text{Date}); !v \cdot \mathcal{C}(v, \text{emp}) \end{aligned}$$

Example 2: multiparty session



$$\begin{aligned} G_{BBS}(B_1, B_2, C) &\triangleq B_1 \rightarrow S : \text{String}; \\ &((S \rightarrow B_1 : v \cdot v > 0) \circledast (S \rightarrow B_2 : v \cdot v > 0)); \\ &B_2 \rightarrow B_1 : v \cdot v \geq 0; \\ &((B_2 \rightarrow S : 1; B_2 \rightarrow S : \text{Addr}; S \rightarrow B_2 : \text{Date}) \vee (B_2 \rightarrow S : 0)) \end{aligned}$$

(automatic sync algorithm)

$$\begin{aligned} G_{BBS}(B_1, B_2, C) &\triangleq B_1 \rightarrow S : \text{String}; \zeta_1; \\ &((S \rightarrow B_1 : v \cdot v > 0) \circledast (S \rightarrow B_2 : v \cdot v > 0)); \zeta_2; \\ &B_2 \rightarrow B_1 : v \cdot v \geq 0; \zeta_3; \\ &((B_2 \rightarrow S : 1; B_2 \rightarrow S : \text{Addr}; S \rightarrow B_2 : \text{Date}) \vee (B_2 \rightarrow S : 0)) \end{aligned}$$

Specification Language

$$\begin{aligned} G &::= A \rightarrow B : \Phi \mid A \xrightarrow{d} B : G \mid p(v^*) \mid \zeta_{id} \mid G \otimes G \mid G \vee G \mid G; G \\ P &::= \text{emp} \mid !v \cdot \Delta \mid ?v \cdot \Delta \mid p(v^*) \mid \zeta_{id} \mid V \mid P \vee P \mid P; P \end{aligned}$$

Projection Rules

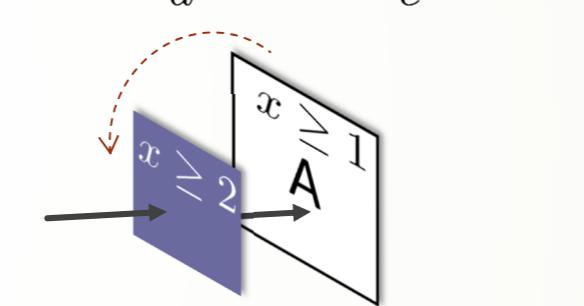
$$\begin{aligned} (A \rightarrow B : \Delta)|_A^B &:= !v \cdot \Delta \quad (A \rightarrow B : \Delta)|_B^A := ?v \cdot \Delta \\ (A \xrightarrow{d} B : G(A, X))|_A^B &:= !v \cdot \mathcal{C}(v, (G(A, X))|_A^X) \\ (A \xrightarrow{d} B : G(A, X))|_B^A &:= ?v \cdot \mathcal{C}(v, (G(A, X))|_A^X) \\ (G_1; G_2)|_R^{R'} &:= (G_1)|_R^{R'} ; (G_2)|_R^{R'} \\ (G_1 \vee G_2)|_R^{R'} &:= (G_1)|_R^{R'} \vee (G_2)|_R^{R'} \\ (G_1 \otimes G_2)|_R^{R'} &:= (G_1)|_R^{R'} \text{ iff } (G_2)|_R^{R'} = \text{emp} \\ &:= (G_2)|_R^{R'} \text{ iff } (G_1)|_R^{R'} = \text{emp} \\ &:= \perp \text{ otherwise} \end{aligned}$$

Entailment Rules

$$\frac{\square_a \vdash \square_c \rightsquigarrow S_1 \quad P_a \vdash P_c \rightsquigarrow S_2 \quad \text{where } \square := ?v \cdot \Delta \mid !v \cdot \Delta \mid \vee P \mid f}{\square_a; P_a \vdash \square_c; P_c \rightsquigarrow \{\text{emp} \wedge \pi_1 \wedge \pi_2 \mid \pi_1 \in S_1 \wedge \pi_2 \in S_2\}}$$

$$\frac{P_a \vdash P_c \rightsquigarrow S' \quad S = \{\pi_i^e \mid \pi_i^e \in S'\}}{\mathcal{C}(v, P_a) \vdash \mathcal{C}(v, P_c) \rightsquigarrow S}$$

$$\frac{\Delta_a \vdash \Delta_c \rightsquigarrow S' \quad S = \{\pi_i^e \mid \pi_i^e \in S'\}}{?v \cdot \Delta_a \vdash ?v \cdot \Delta_c \rightsquigarrow S} \quad \frac{\Delta_c \vdash \Delta_a \rightsquigarrow S' \quad S = \{\pi_i^e \mid \pi_i^e \in S'\}}{!v \cdot \Delta_a \vdash !v \cdot \Delta_c \rightsquigarrow S}$$



$$!x \cdot x \geq 1 \vdash !x \cdot x \geq 2$$

$$?x \cdot x \geq 1 \vdash ?x \cdot x \geq 0$$

Example:

$$A \rightarrow B : x \geq 1$$

Communication Primitives

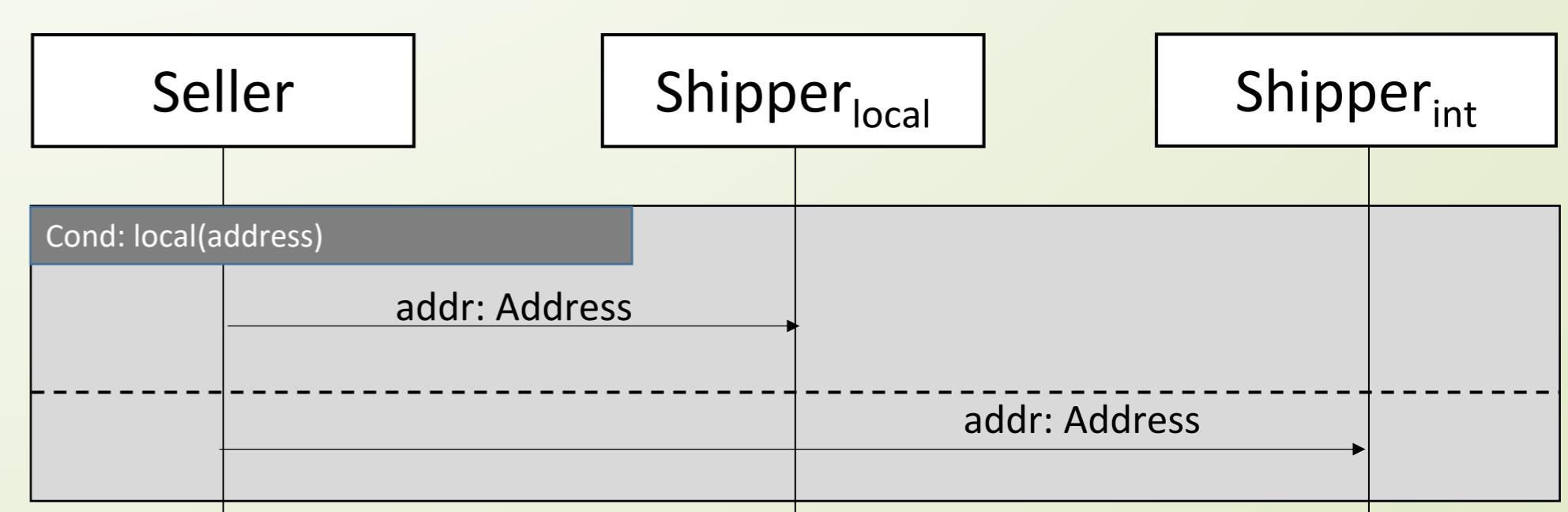
$$\frac{}{\vdash \{\text{emp}\} \text{ open}(c) \text{ with } P \{ \mathcal{C}(c, S_1) * \mathcal{C}(c, S_2) \}}$$

$$\frac{}{\vdash \{\mathcal{C}(c, \text{emp}) * \mathcal{C}(c, \text{emp})\} \text{ close}(c) \{ \text{emp} \}}$$

$$\frac{}{\vdash \{\mathcal{C}(c, !v \cdot L(v); P) * L(x)\} \text{ send}(c, x) \{ \mathcal{C}(c, P) \}}$$

$$\frac{}{\vdash \{\mathcal{C}(c, ?v \cdot L(v); P)\} x = \text{receive}(c) \{ L(x) * \mathcal{C}(c, P) \}}$$

Distributive Conditional



The Take-Away

Type safety → logic with flow awareness (precision)

Communication as resource: concurrency, sequence, nondeterminism

Higher-Order Predicates: expressivity, modularity, maintainability