

$$\begin{aligned}a_1 &= b_0Q + a_0Q + a_0P \\b_1 &= b_0P + a_0Q\end{aligned}$$

$$\begin{aligned}a_2 &= b_1Q + a_1Q + a_1P \\b_2 &= b_1P + a_1Q\end{aligned}$$

$$\begin{aligned}a_2 &= [b_0P + a_0Q]Q + [b_0Q + a_0Q + a_0P]Q + [b_0Q + a_0Q + a_0P]P \\b_2 &= [b_0P + a_0Q]P + [b_0Q + a_0Q + a_0P]Q\end{aligned}$$

$$\begin{aligned}a_2 &= b_0PQ + a_0QQ + b_0QQ + a_0QQ + a_0PQ + b_0QP + a_0QP + a_0PP \\b_2 &= b_0PP + a_0QP + b_0QQ + a_0QQ + a_0PQ\end{aligned}$$

$$\begin{aligned}a_2 &= b_0[PQ + QQ + QP] + a_0[QQ + PQ + PQ] + a_0[QQ + PP] \\b_2 &= b_0[PP + QQ] + a_0[QQ + PQ + PQ]\end{aligned}$$

We can then infer that:

$$\begin{aligned}a_2 &= b_0Q' + a_0Q' + a_0P' \\b_2 &= b_0P' + a_0Q'\end{aligned}$$

With $Q' = [QQ + 2QP]$ and $P' = [QQ + PP]$