



UNIVERSITY OF REGINA

DEEP
CONVOLUTIONAL
SUM-PRODUCT
NETWORKS

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OUTLINE



GENERATIVE MODELS

IN DEEP LEARNING



SUM-PRODUCT NETWORKS (SPNs)



CONVOLUTIONAL NEURAL NETWORKS AS SPNs



CONVOLUTIONAL SPNs (CSPNs)

OUTLINE



DEEP CONVOLUTIONAL SPNs
(DCSPNs)



STATE-OF-THE-ART
RESULTS



AND A FEW
NICE SURPRISES



CONCLUSIONS



GENERATIVE MODELS IN DEEP LEARNING

GENERATIVE MODELS ARE OF CURRENT INTEREST



NADE

*Larochelle
and Murray*

2011



VARIATIONAL AUTOENCODERS

*Kingma
and Welling*

2014



GANs

*Goodfellow
et al.*

2014



PIXEL RNN

*Oord, Kalchbrenner,
and Kavukcuoglu*

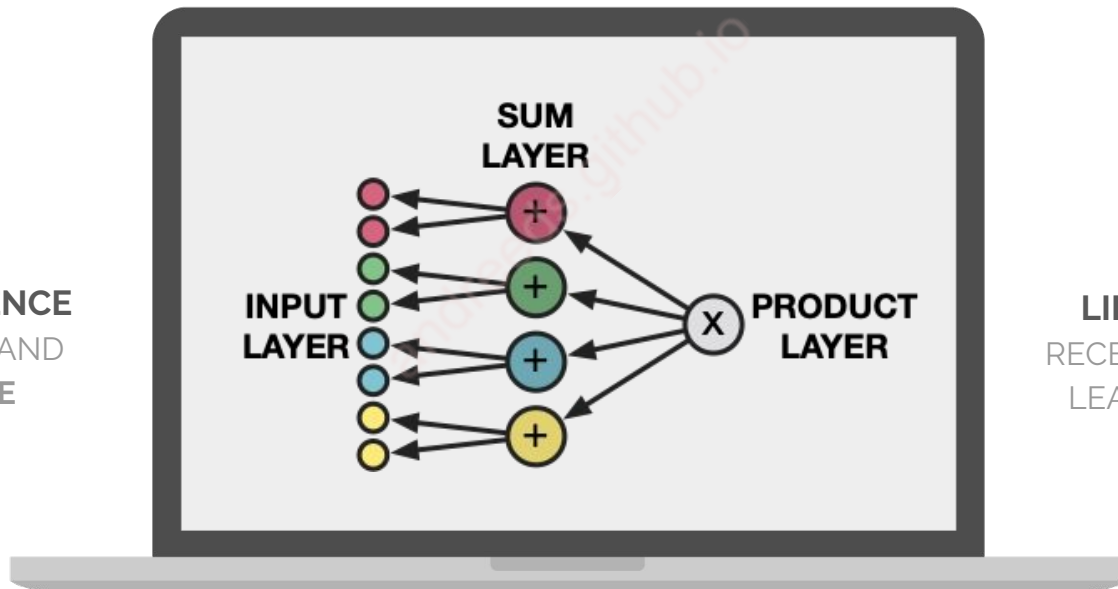
2016

SUM-PRODUCT NETWORKS

GENERATIVE DEEP LEARNING MODEL



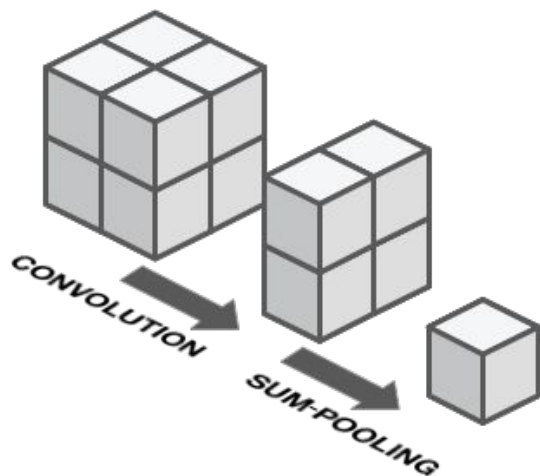
EFFICIENT INFERENCE
WHEN **COMPLETE** AND
DECOMPOSABLE



LIMITED ATTENTION
RECEIVED FROM THE DEEP
LEARNING COMMUNITY

Peharz et al.
2018

CONVOLUTIONAL NEURAL NETWORKS



CONVOLUTIONAL LAYERS

NETWORK PARAMETERS ARE FILTERS

POOLING LAYERS

USES SLIDING WINDOWS

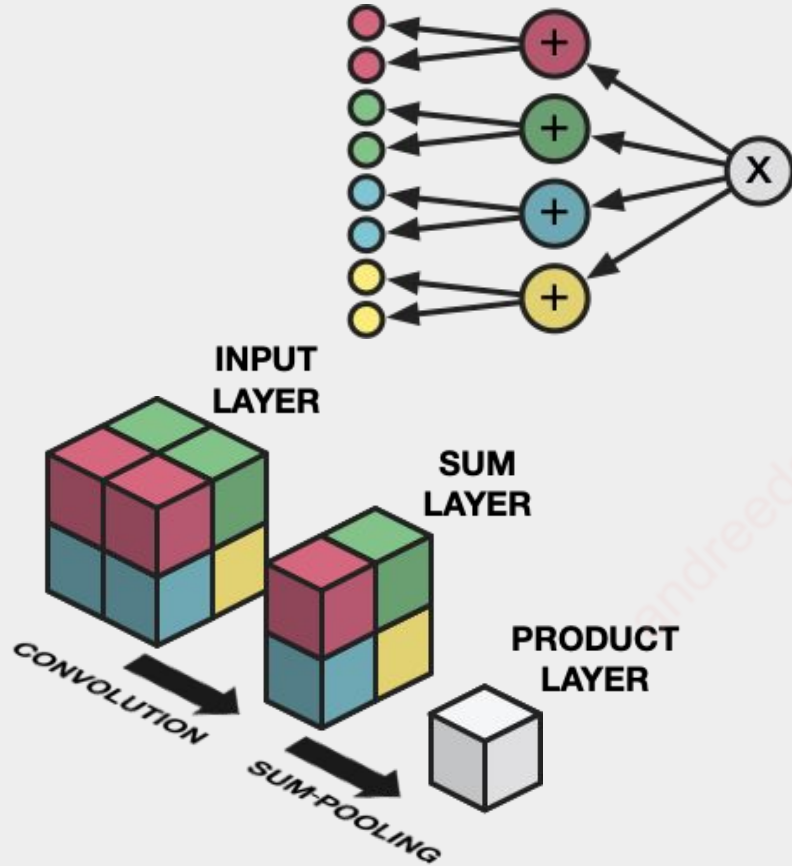
CNNs AS SPNs

CONVOLUTIONAL LAYERS

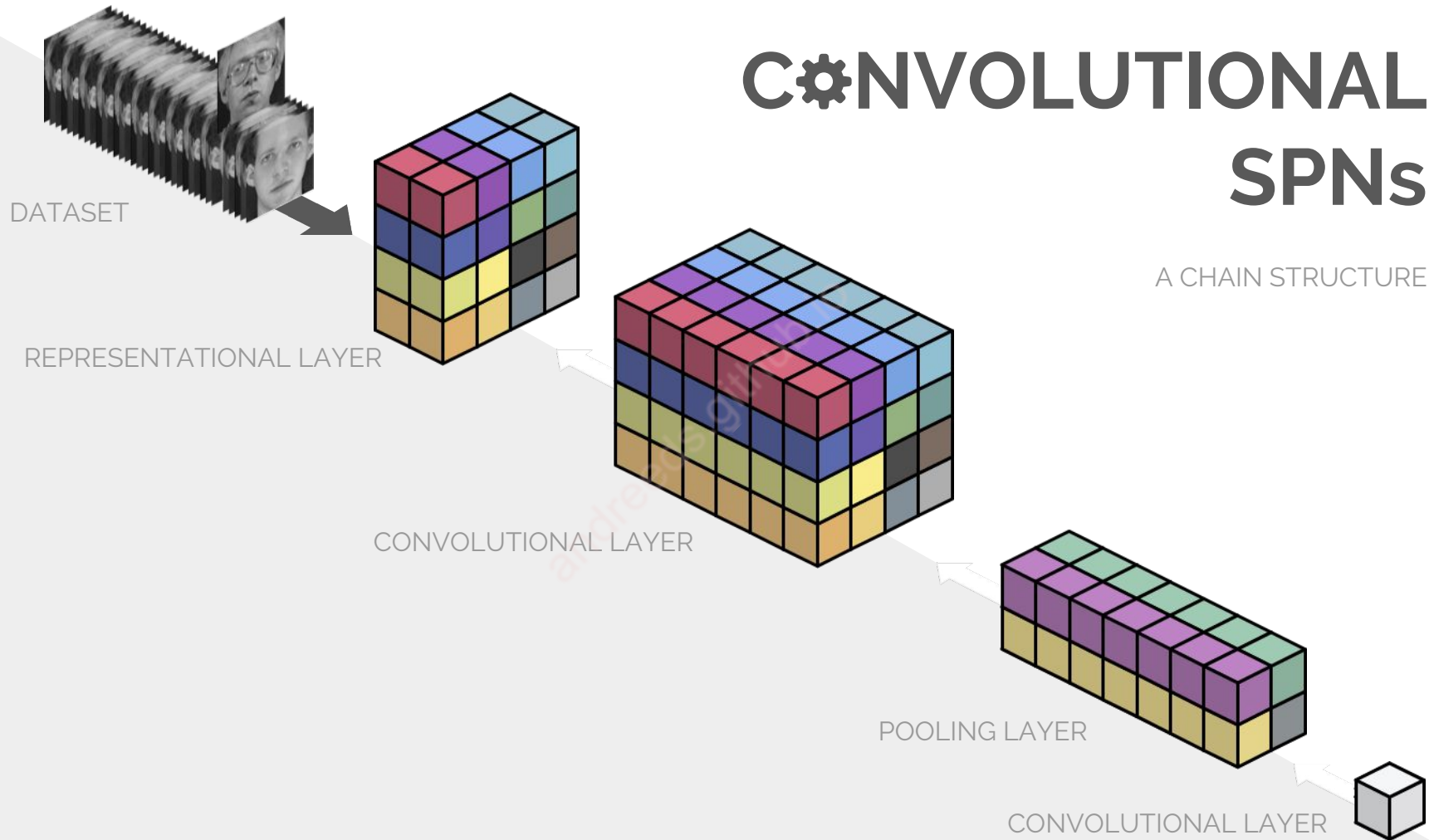
- FILTERS OF CERTAIN SIZES
- MAINTAINS **COMPLETENESS**

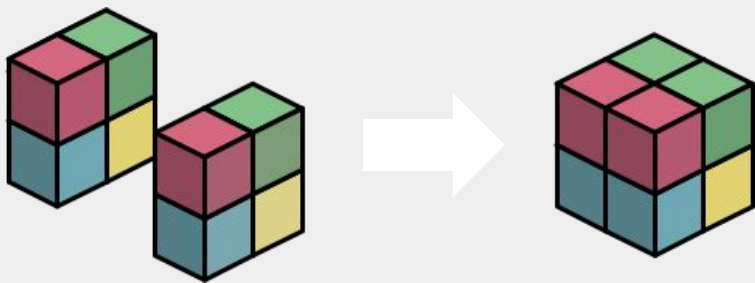
POOLING LAYERS

- NON-OVERLAPPING WINDOWS
- MAINTAINS **DECOMPOSABILITY**



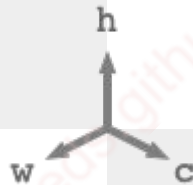
C[⚙]ONVOLUTIONAL SPNs



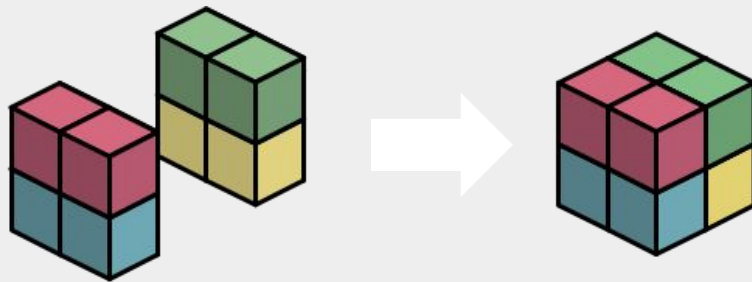


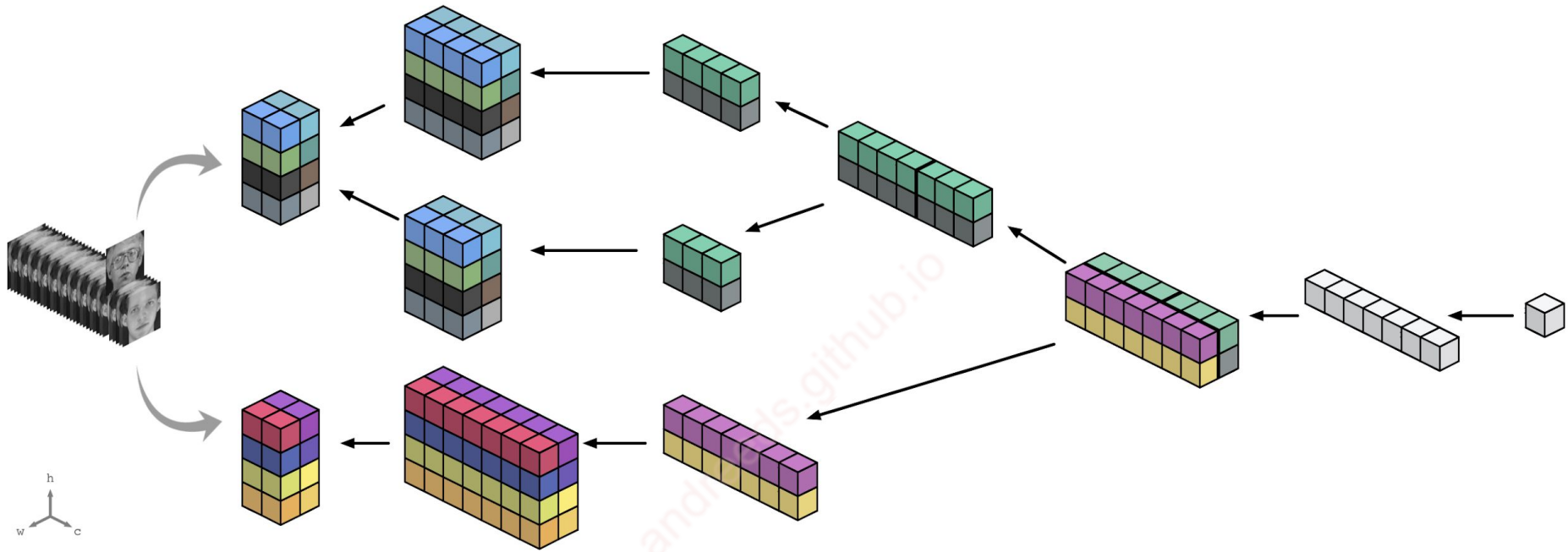
**LAYERS (TENSORS)
CAN BE AUGMENTED**

WHILE MAINTAINING
COMPLETENESS AND DECOMPOSABILITY



**CREATING DEEPER
STRUCTURES**

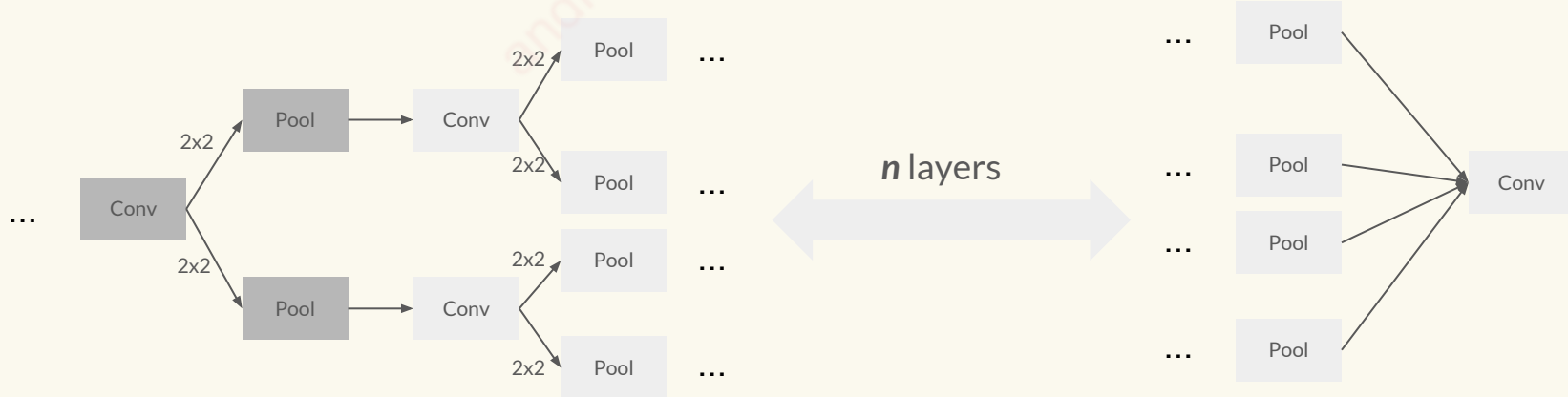
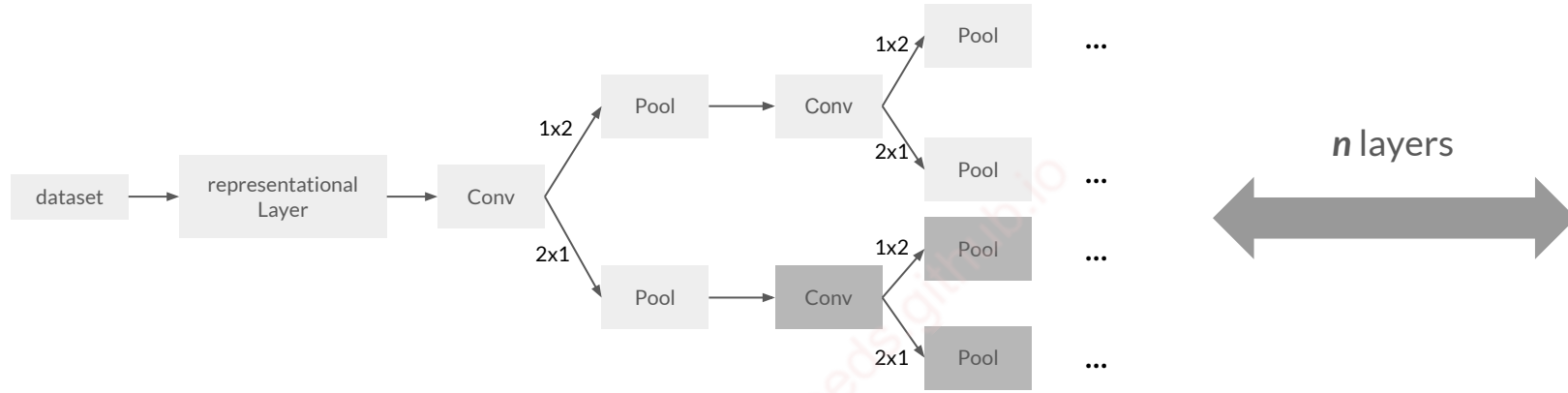




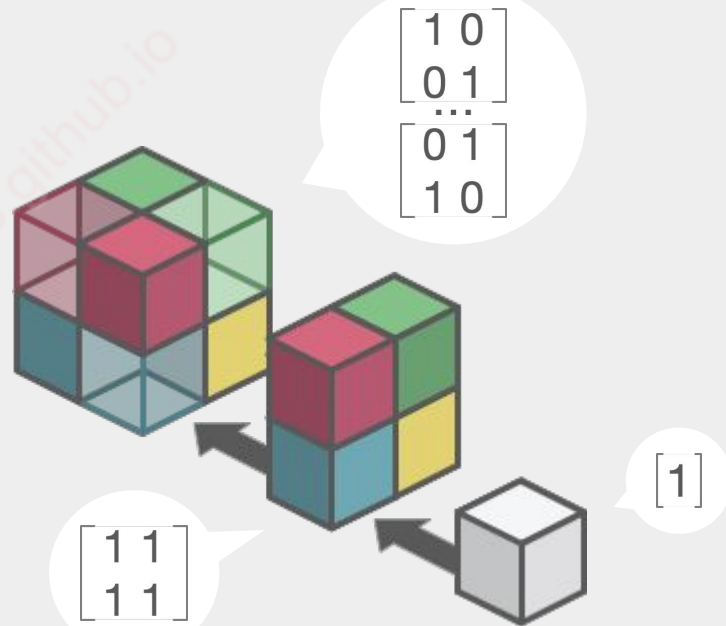
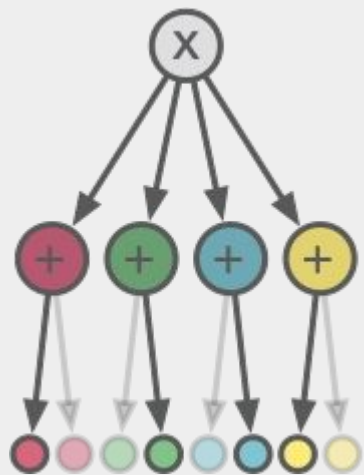
DEEP CONVOLUTIONAL SPNs

A RICH DAG OF CONVOLUTIONAL AND SUM-POOLING LAYERS

A WINNING STRUCTURE



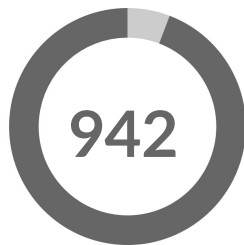
VECTORIZED MPE



STATE-OF-THE-ART RESULTS IN OLIVETTI FACE

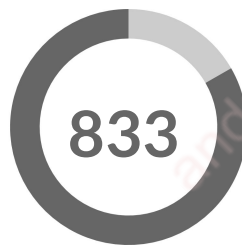
P&D

*Poon and
Domingos
2011*



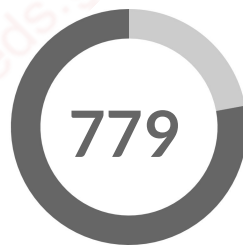
ICNN

*Amos, Xu,
and Kolter
2017*



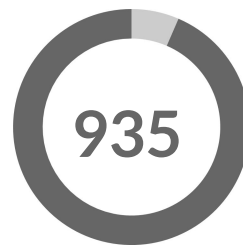
D&V

*Dennis and
Ventura
2012*



DCGAN

*Yeh
et al.
2017*



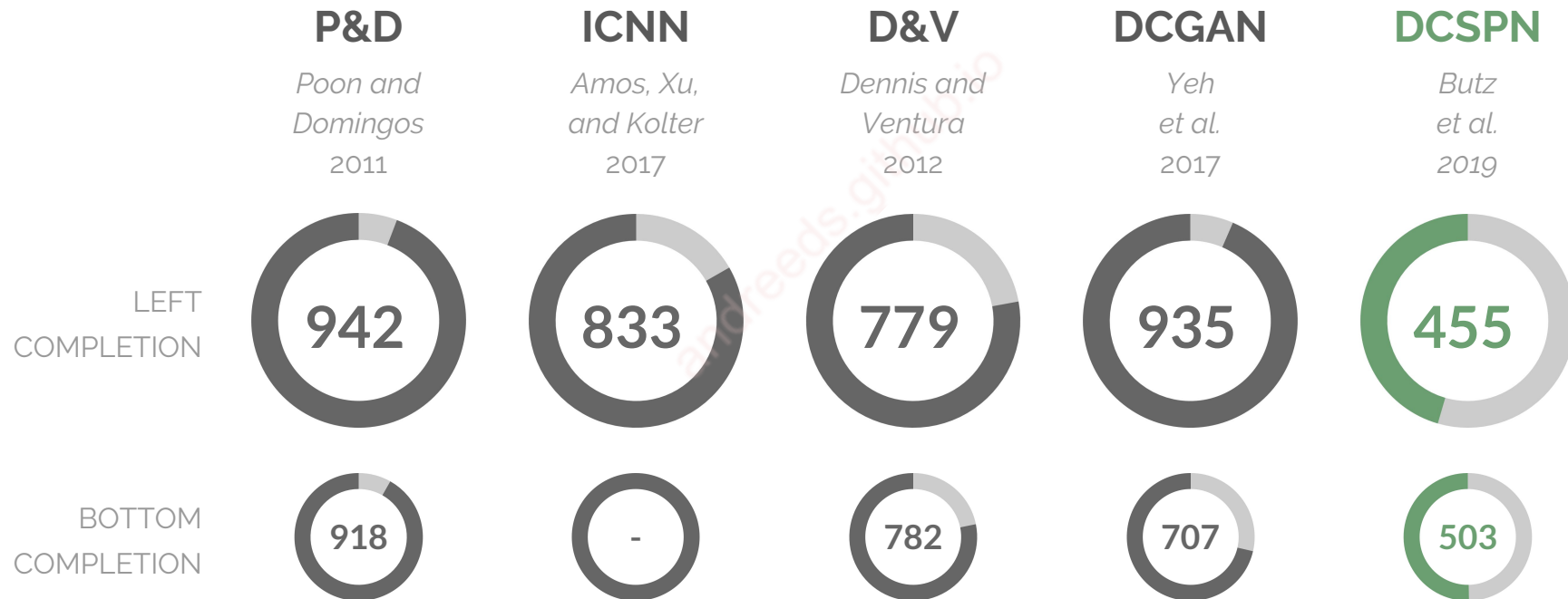
DCSPN

*Butz
et al.
2019*



LEFT
COMPLETION

STATE-OF-THE-ART RESULTS IN OLIVETTI FACE



STATE-OF-THE-ART RESULTS IN CALTECH

LEFT COMPLETION	FACE	1815	1657	1334	1178
	DOLPHIN	3096	-	4096	2002
	HELICOPTER	2749	-	3925	1702
BOTTOM COMPLETION	FACE	1924	1517	1046	1149
	DOLPHIN	2767	-	4016	2102
	HELICOPTER	3064	-	3811	2103

P&D

*Poon and
Domingos
2011*

D&V

*Dennis and
Ventura
2012*

DCGAN

*Yeh
et al.
2017*

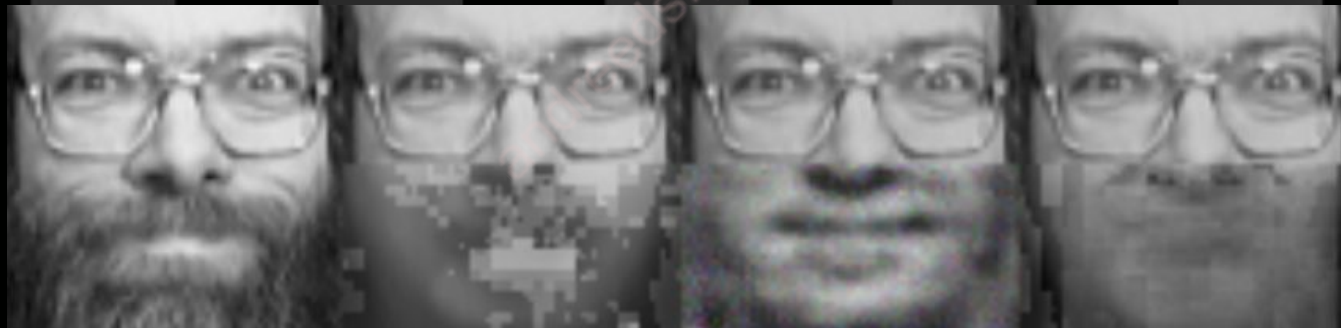
DCSPN

*Butz
et al.
2019*

LEFT
COMPLETION



BOTTOM
COMPLETION



ORIGINAL

DCSPN

P&D

GAN

OLIVETTI

LEFT
COMPLETION



BOTTOM
COMPLETION



ORIGINAL

DCSPN

P&D

GAN

CALTECH



AND A FEW NICE SURPRISES TOO

01

Learning
DCSPNs with
differentiable
MPE

02

Relationship
with GANs

03

Image sampling
with variability

04

Good
performance on
a dataset with
65 images

01

02

03

04

LEARNING DCSPN WITH DIFFERENTIABLE MPE

MOTIVATED BY FUTURE WORK SUGGESTED IN

(Vergari et al., AAAI 2018)

LEARN DCSPNs USING DIFFERENTIABLE MPE

$$\min_G \max_D \mathbb{E}[\log D(\mathbf{x})] + \mathbb{E}[\log(1 - D(G(\mathbf{z})))]$$



DCSPNs yields an
MSE score of **651**



**More promising
than simply a low
MSE score**

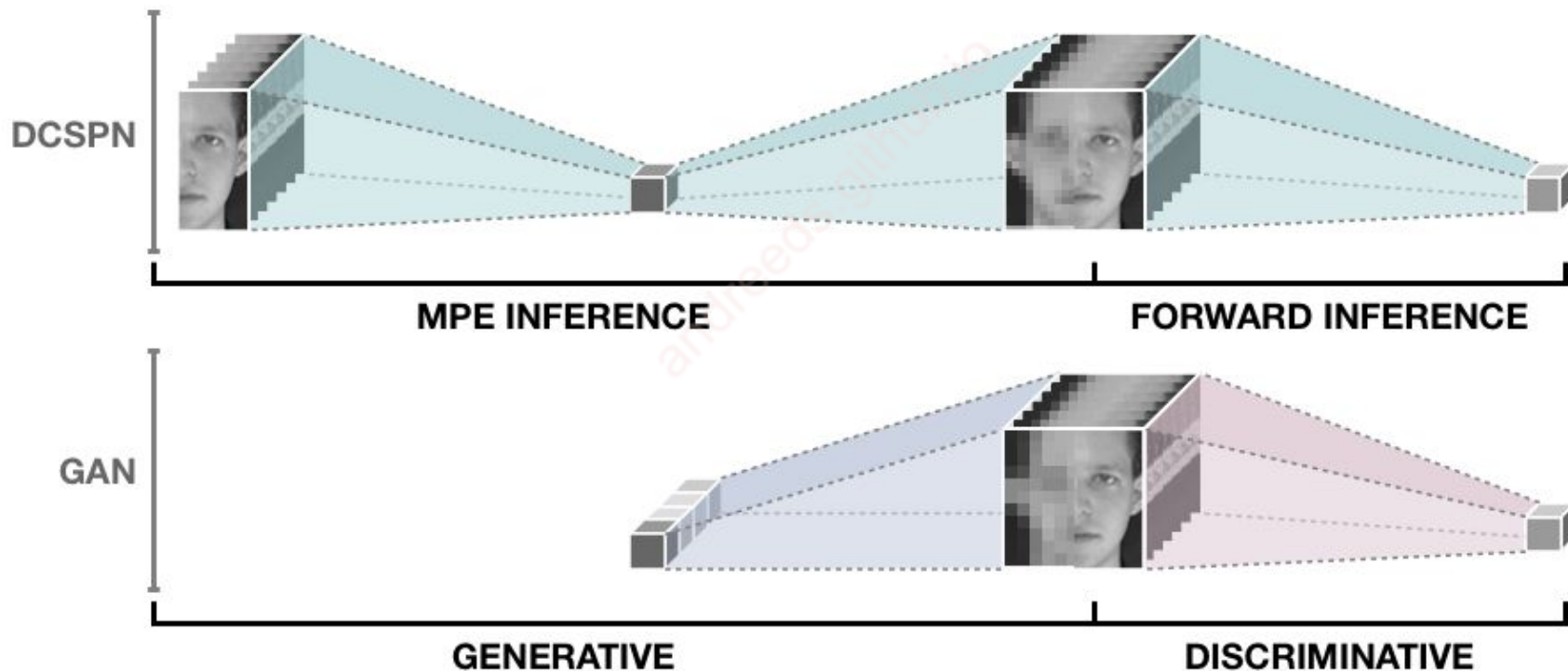
01

02

03

04

RELATIONSHIP WITH GANs



01

02

03

04

IMAGE SAMPLING



Simple modification in
MPE Algorithm



DCSPN sampled images
exhibit variability



01

02

03

04

GOOD PERFORMANCE ON A SMALL DATASET



ORIGINAL

DCSPN

P&D

GAN



DCSPNs left-complete
well on a small dataset



Caltech Dolphin
contain 65 images

ANALYSIS



SMALL HORIZONTAL AND VERTICAL SUM-POOLING WINDOW SIZES CAN

- yield **deeper** structures
- leverage **local structure** in the image data



ALTERNATING SUM-POOLING WINDOW SIZES CAN

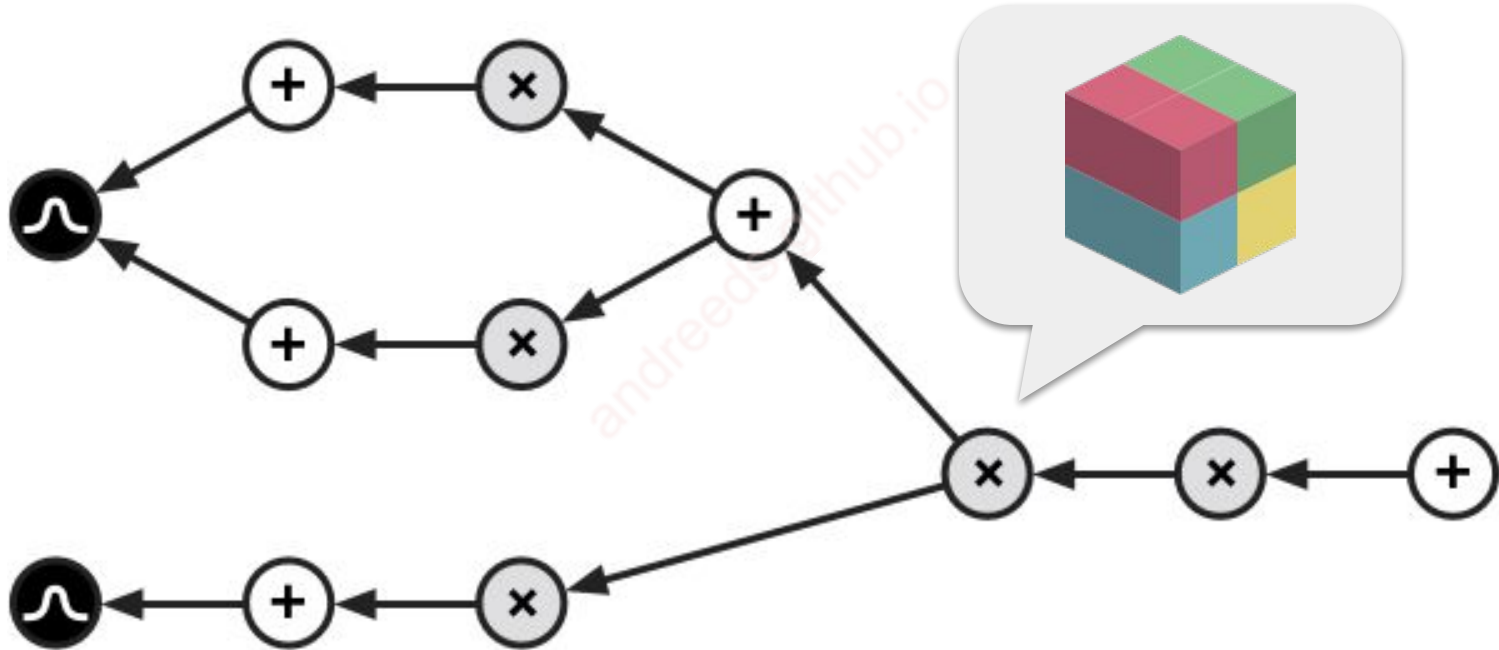
- serve as a **regularization** technique
- alleviate **vanishing gradient**



TWO FILTER SIZE OPTIONS ALLOWS FOR

controlling trade-off between
quality and size

FUTURE WORK



CONCLUSION

WE ESTABLISH WHEN
SUBCLASSES OF CNNs
DEFINE SPNs



DCSPNs ARE CNNs WHICH ALSO
CAN TAKE ADVANTAGE OF KNOWN
TECHNIQUES IN PROBABILISTIC
GRAPHICAL MODELS



SEVERAL STATE-OF-THE-ART MSE
SCORES IN IMAGE COMPLETION



AND NICE SURPRISES INCLUDING
VARIABILITY IN IMAGE SAMPLING
AND AN INTRIGUING
RELATIONSHIP WITH GAN





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