

© If  $y_t$  is ordered first, then our matrix  $b$  will be:

$$B = \begin{bmatrix} 1 & 0 \\ -0,2 & 1 \end{bmatrix} \text{ and the inverse } \rightarrow B^{-1} = \begin{bmatrix} 1 & 0 \\ 0,2 & 1 \end{bmatrix}$$

Let's recalculate the reduced form parameters:

$$B^{-1} \Gamma_0 = A_0 \text{ and } B^{-1} \Gamma_1 = A_1$$

$$\Gamma_1 = \begin{bmatrix} 0,3 & 0,3 \\ 0,1 & 0,4 \end{bmatrix} \quad \Gamma_0 = \begin{bmatrix} 0,1 \\ -0,2 \end{bmatrix}$$

$$A_0 = \begin{bmatrix} 1 & 0 \\ 0,2 & 1 \end{bmatrix} \begin{bmatrix} 0,1 \\ -0,2 \end{bmatrix} = \begin{bmatrix} 0,1 \\ -0,18 \end{bmatrix}$$

$$A_1 = \begin{bmatrix} 1 & 0 \\ 0,2 & 1 \end{bmatrix} \begin{bmatrix} 0,3 & 0,3 \\ 0,1 & 0,4 \end{bmatrix} = \begin{bmatrix} 0,3 & 0,3 \\ 0,16 & 0,46 \end{bmatrix}$$

Now, let's calculate the responses of  $y_t$  and  $y_{t+1}$  to a shock in  $z_t$ :

let's <sup>note</sup> ~~see~~ that:

$$\begin{bmatrix} 1 & 0 \\ 0,2 & 1 \end{bmatrix} \begin{bmatrix} \varepsilon_{y_t} \\ \varepsilon_{z_t} \end{bmatrix} = \begin{bmatrix} e_{1t} \\ e_{2t} \end{bmatrix} \Leftrightarrow \begin{bmatrix} \varepsilon_{y_t} \\ 0,2\varepsilon_{y_t} + \varepsilon_{z_t} \end{bmatrix} = \begin{bmatrix} e_{1t} \\ e_{2t} \end{bmatrix}$$

Now we can interpret  $e_{1t}$  directly.  
we also know that with cholesky decomposition,  $\boxed{L = B^{-1}}$

MA representation of the model:

$$x_t = \mu + L \varepsilon_t + A_1 L \varepsilon_{t-1} + A_1^2 L \varepsilon_{t-2} + \dots$$

$$\frac{\partial x_t}{\partial \varepsilon_t} = \begin{bmatrix} \frac{\partial y_t}{\partial \varepsilon_t} & \frac{\partial y_t}{\partial \varepsilon_{zt}} \\ \frac{\partial z_t}{\partial \varepsilon_t} & \frac{\partial z_t}{\partial \varepsilon_{zt}} \end{bmatrix} = L = \begin{bmatrix} 1 & 0 \\ 0,2 & 1 \end{bmatrix}$$

(at impact)

Hence,  $\frac{\partial y_t}{\partial \varepsilon_{zt}} = 0$

we were already expecting this result as this comes from the restriction we have imposed.

At impact, a shock in  $y_t$  doesn't affect  $y_t$ .

For the first step:

$$\frac{\partial x_{t+1}}{\partial \varepsilon_t} = \begin{bmatrix} \frac{\partial y_{t+1}}{\partial \varepsilon_t} & \frac{\partial y_{t+1}}{\partial \varepsilon_{zt}} \\ \frac{\partial z_{t+1}}{\partial \varepsilon_t} & \frac{\partial z_{t+1}}{\partial \varepsilon_{zt}} \end{bmatrix} = A_1 L$$

$$\begin{bmatrix} 0,3 & 0,3 \\ 0,16 & 0,46 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0,2 & 1 \end{bmatrix} = \begin{bmatrix} 0,36 & 0,3 \\ 0,252 & 0,46 \end{bmatrix}$$

$\frac{\partial y_{t+1}}{\partial \varepsilon_{zt}} = 0,3$  A one standard deviation ~~in~~ shock in  $z_t$  will lead to ~~an increase of 0,3 units in  $y_{t+1}$~~  an increase of 0,3 units in  $y_{t+1}$ .

This makes sense since that, although  $z_t$ , contemporaneously doesn't affect  $y_t$ , the past values of the variable do impact.