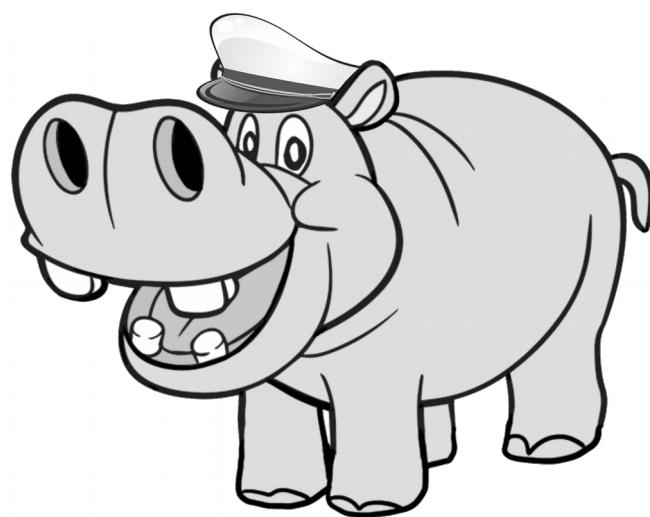


Behavioral Data Science



Expecting to be HIP:
Hawkes Intensity Processes for
modeling online popularity and virality

Marian-Andrei Rizoiu

Popularity over time



My philosophy for a happy life | Sam Berns |
TEDxMidAtlantic

TEDx Talks

TEDx 2,346,801

8,190,511

+ Add to Share More 75,912 1,287

Video statistics Through May 12, 2015

IEWS	TIME WATCHED	SUBSCRIPTIONS DRIVEN	SHARES
8,190,550	85 years	18,065	28,720



J.S.Bach - Brandenburg Concerto No.5 in D BWV1050 -
Croatian Baroque Ensemble

Croatian Baroque Ensemble

3,860

1,225,253

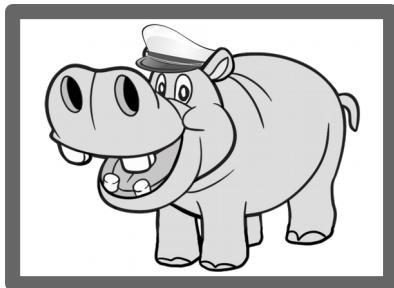
+ Add to Share More 5,275 128

Video statistics Through May 12, 2015

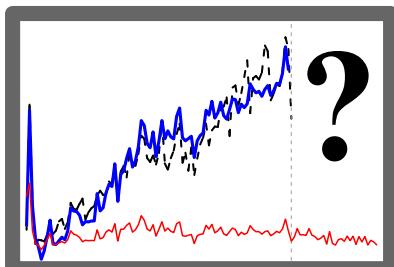
IEWS	SHARES
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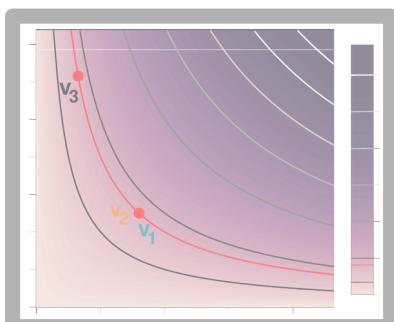
Presentation outline



Modeling popularity with HIP



Forecasting popularity under promotion

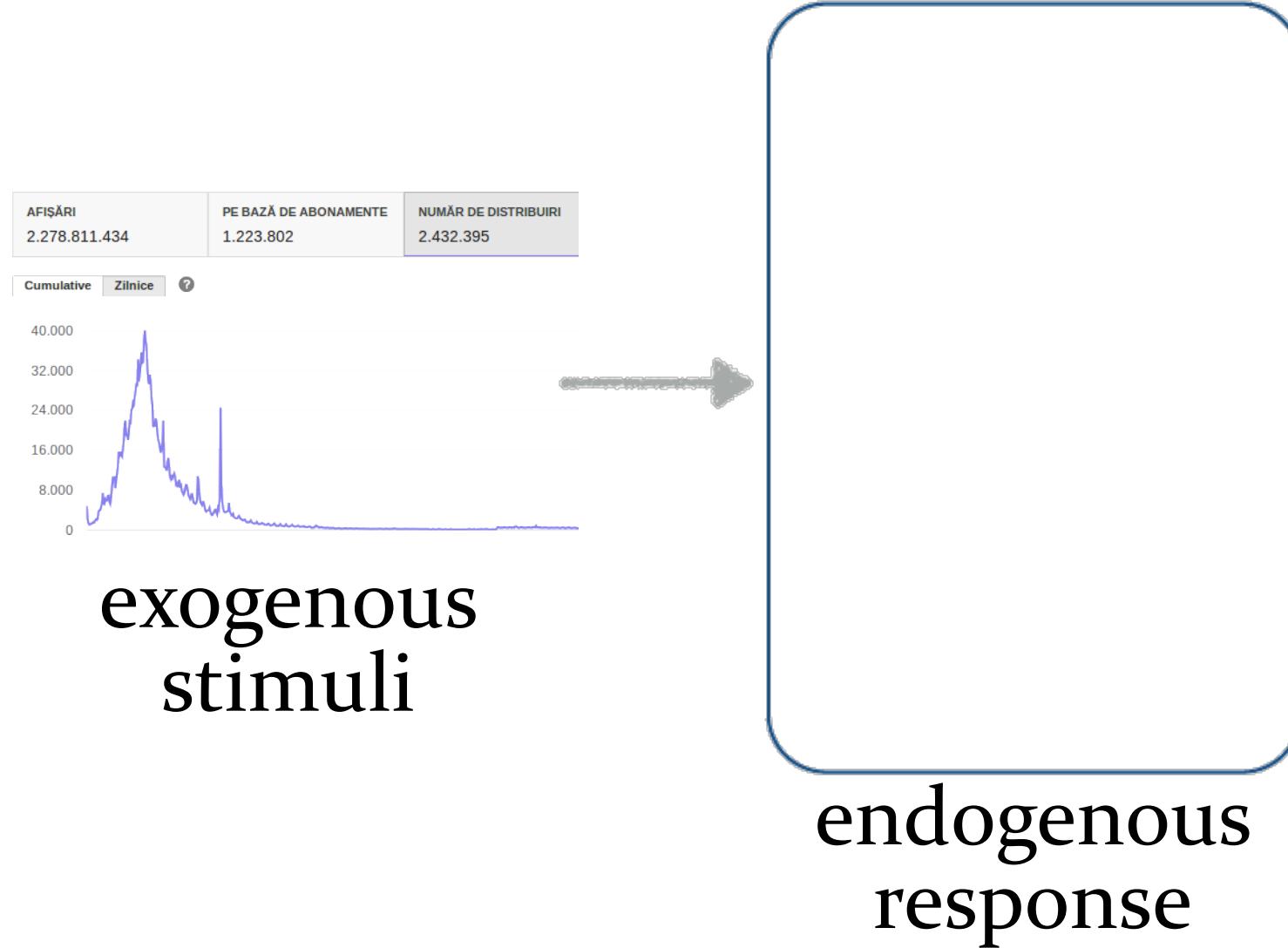


Content virality and maturity time



Promotions schedules and memory lengthening through promotion

Linking exo-endo popularity



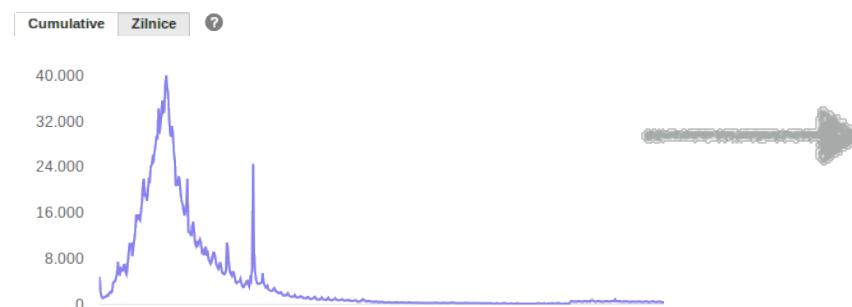
PSY - GANGNAM STYLE (강남스타일) M/V



Subscribe 7,938,545

2,321,368,075

AFIŞARI	PE BAZĂ DE ABONAMENTE	NUMĂR DE DISTRIBUIRI
2.278.811.434	1.223.802	2.432.395



exogenous
stimuli

VIEWS	SUBSCRIPTIONS DRIVEN	SHARES
2,278,812,248	1,223,802	2,432,395

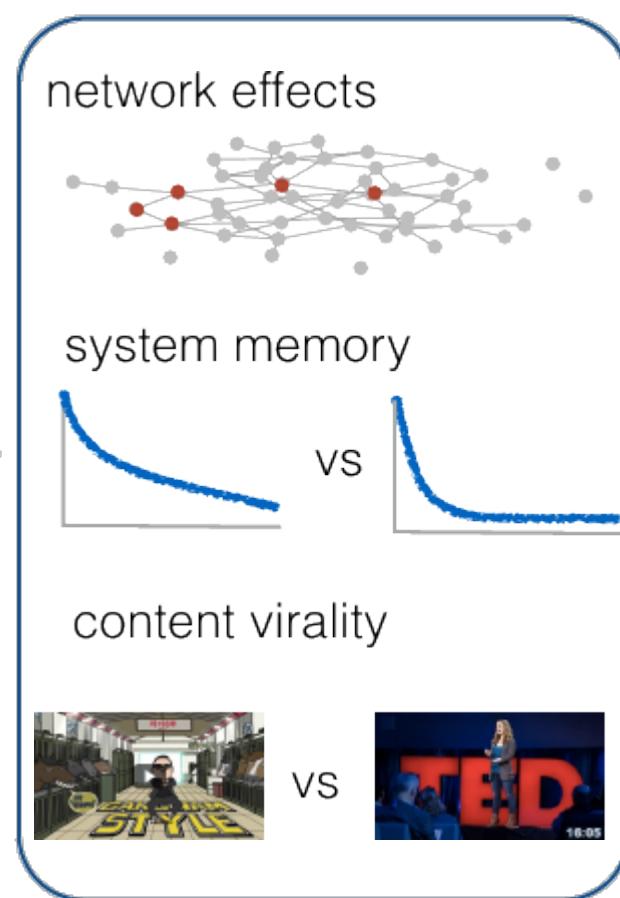


observed
popularity

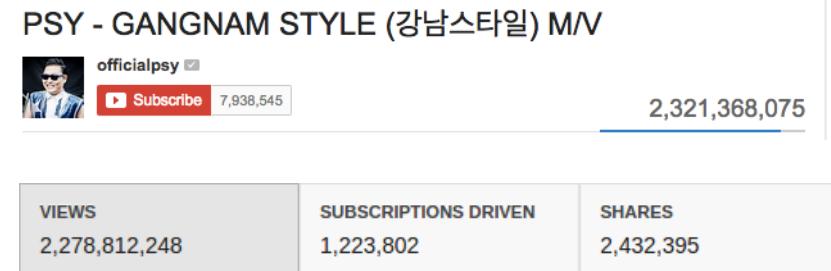
Linking exo-endo popularity



exoogenous
stimuli



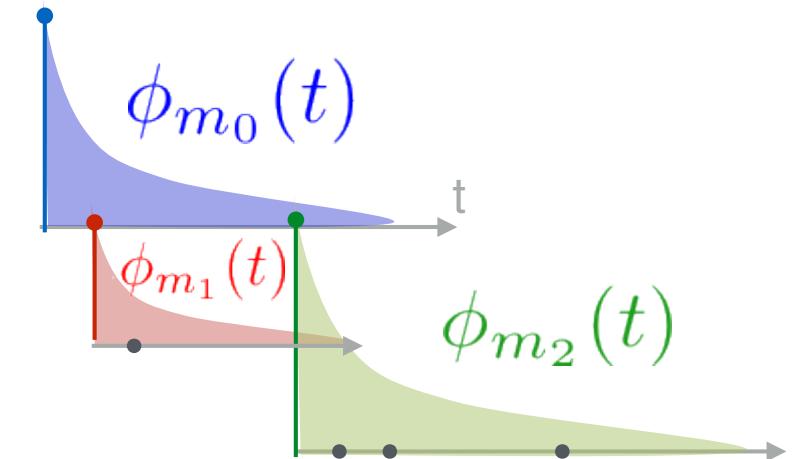
endogenous
response



observed
popularity

Hawkes Process [Hawkes '71]

$$\lambda(t) = \mu(t) + \sum_{t_i < t} \phi_{m_i}(t - t_i)$$



Most state-of-the-art popularity prediction systems require observing individual events.

[Zhao et al KDD'15] [Shen et al AAAI'14]

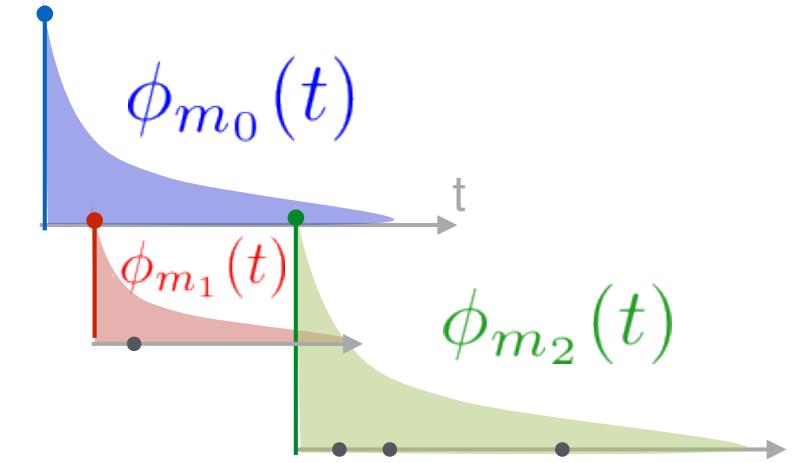
[Farajtabar et al NIPS'15]

Hawkes Process [Hawkes '71]

$$\lambda(t) = \mu(t) + \sum_{t_i < t} \phi_{m_i}(t - t_i)$$

the rate of
'daughter' events content virality user influence memory

$$\phi_m(\tau) = \kappa m^\beta \hat{\tau}^{-(1+\theta)}$$



[Mishra et al CIKM'16]

Most state-of-the-art popularity prediction systems require observing individual events.

[Zhao et al KDD'15] [Shen et al AAAI'14]

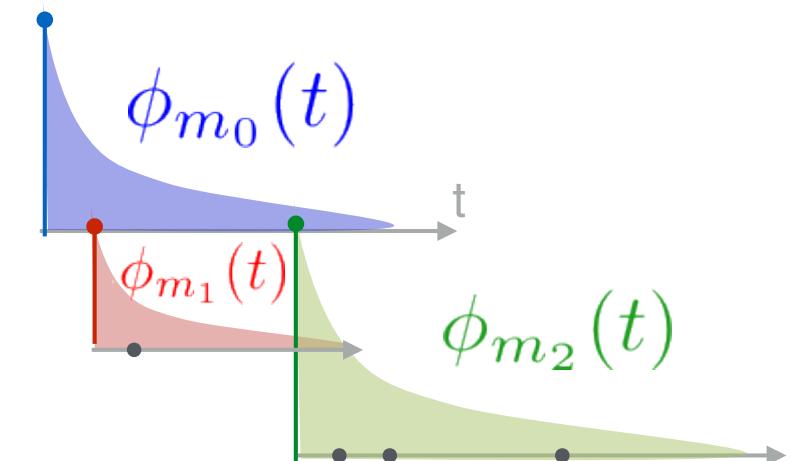
[Farajtabar et al NIPS'15]

Hawkes Intensity Process (HIP)

[Rizoiu et al, WWW'17]

$$\lambda(t) = \mu(t) + \sum_{t_i < t} \phi_{m_i}(t - t_i)$$

the rate of content user memory
‘daughter’ events virality influence



$$\phi_m(\tau) = \kappa m^\beta \hat{\tau}^{-(1+\theta)}$$

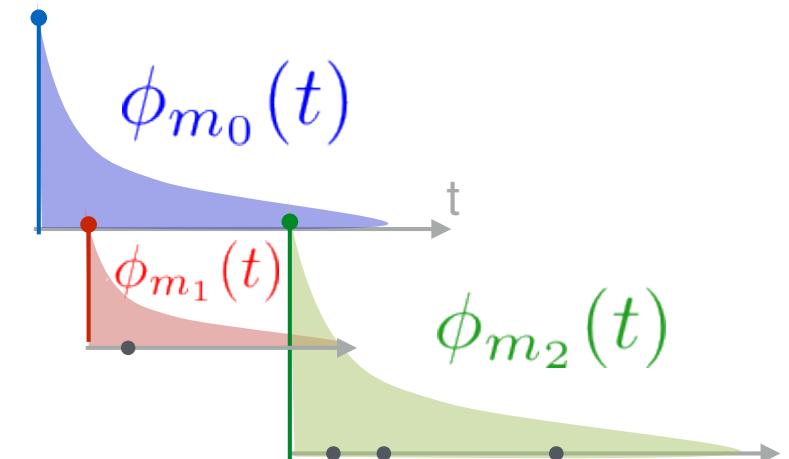
expected number of events

Hawkes Intensity Process (HIP)

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$$\lambda(t) = \mu(t) + \sum_{t_i < t} \phi_{m_i}(t - t_i)$$

the rate of
'daughter' events content virality user influence memory



$$\phi_m(\tau) = \kappa m^\beta \hat{\tau}^{-(1+\theta)}$$

expected number of events

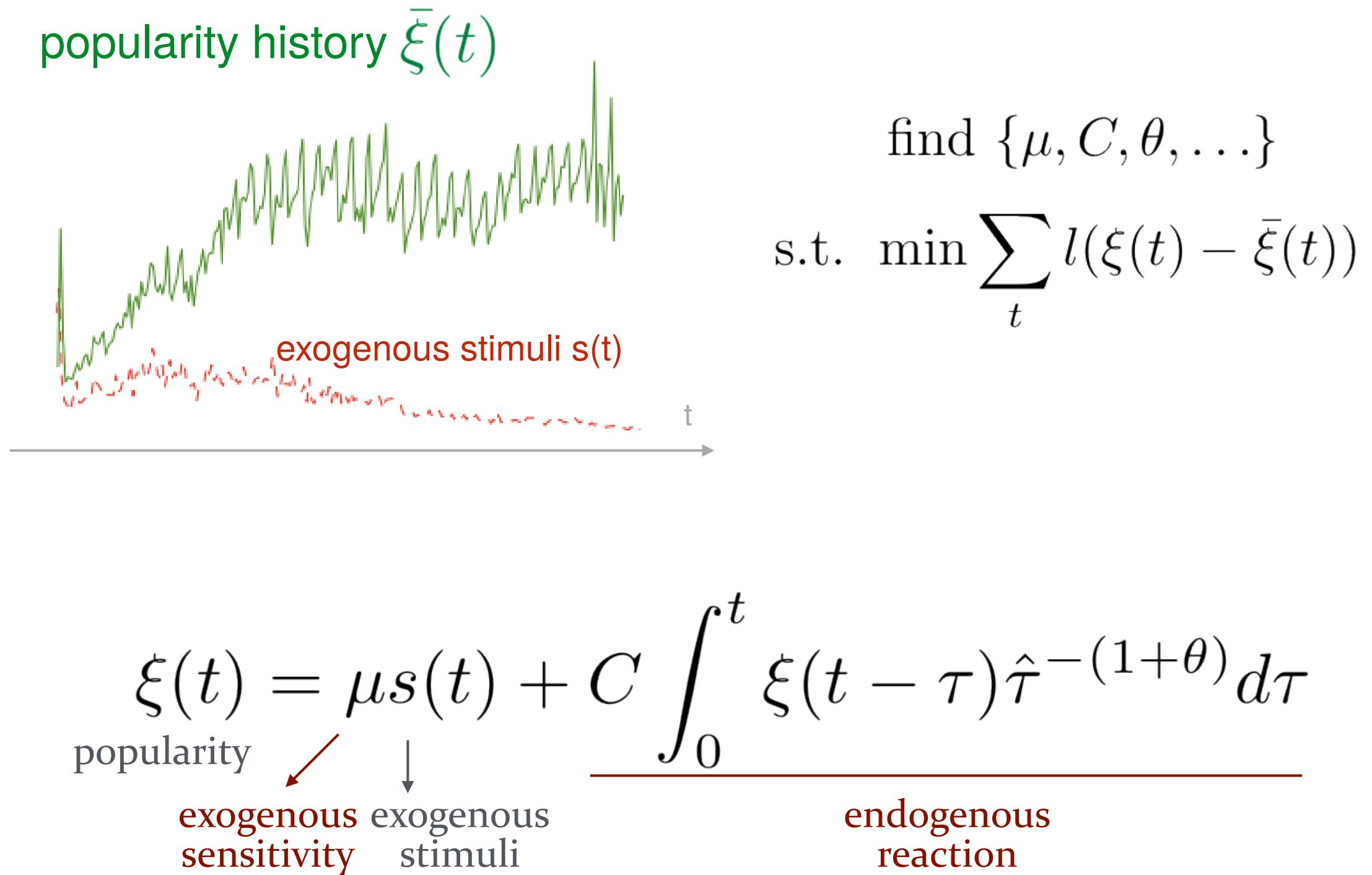
$$\xi(t) = \mu s(t) + C \int_0^t \xi(t - \tau) \hat{\tau}^{-(1+\theta)} d\tau$$

popularity

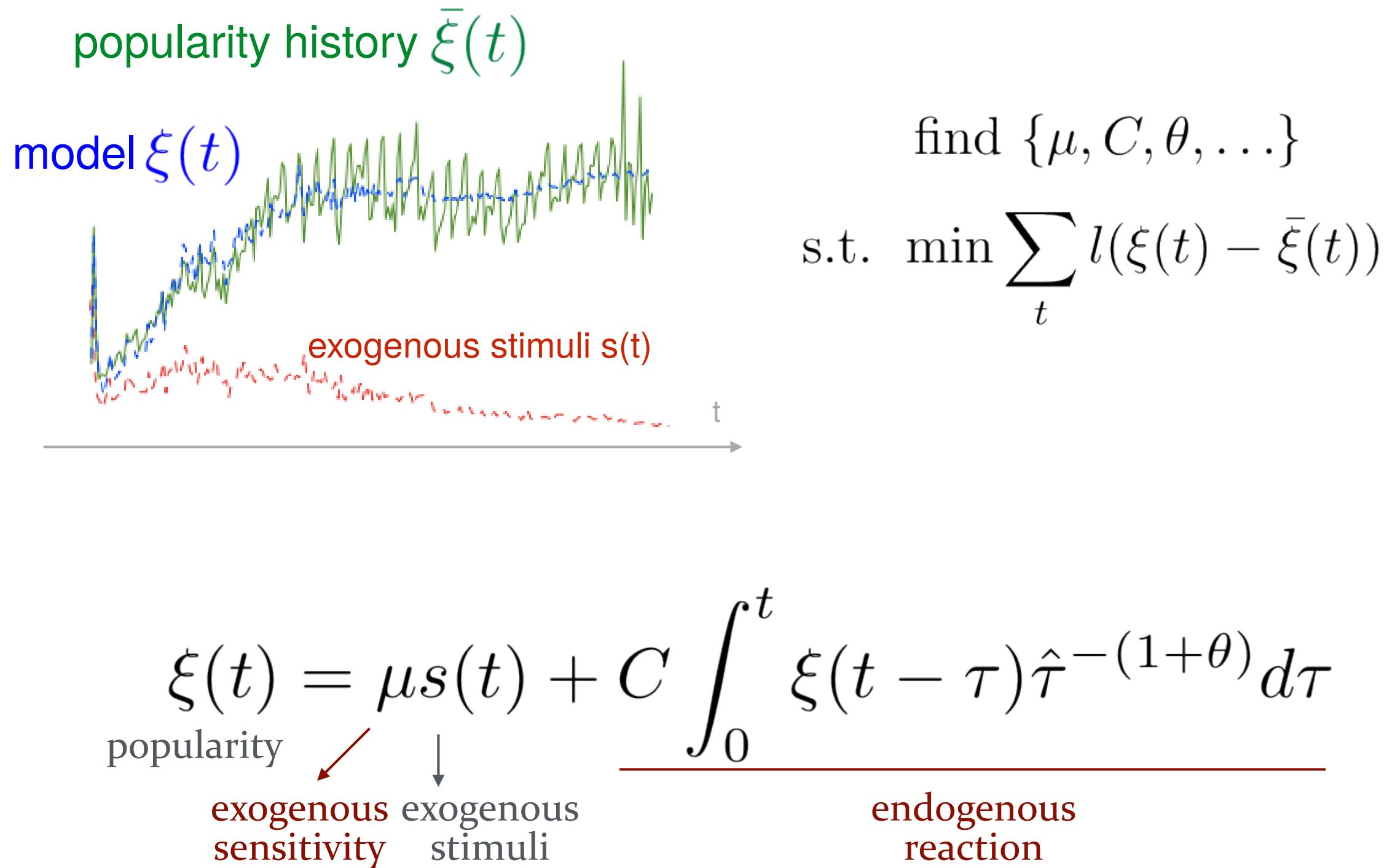
exogenous sensitivity exogenous stimuli

endogenous reaction

Estimating the HIP model

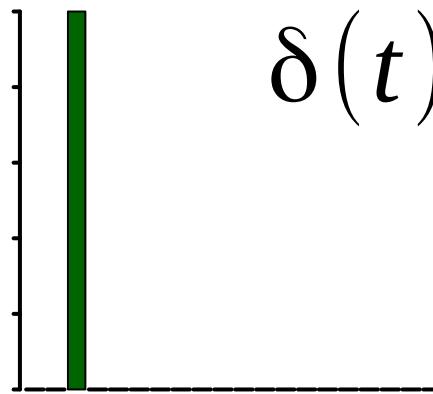


Estimating the HIP model

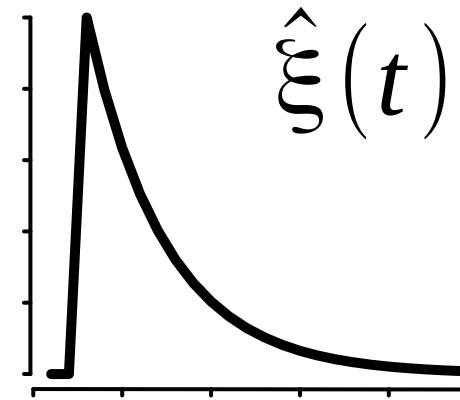


HIP as a Linear Time-Invariant system

promotion



response



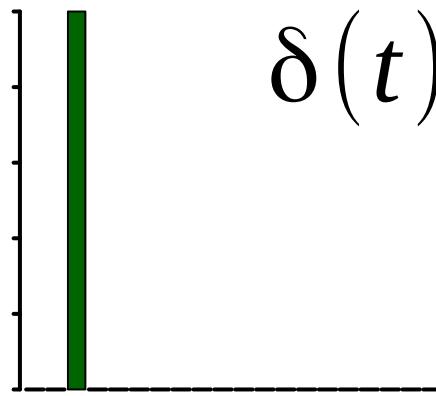
$$\xi(t) = \mu s(t) + C \int_0^t \xi(t - \tau) \hat{\tau}^{-(1+\theta)} d\tau$$

popularity ↓
exogenous sensitivity exogenous stimuli endogenous reaction

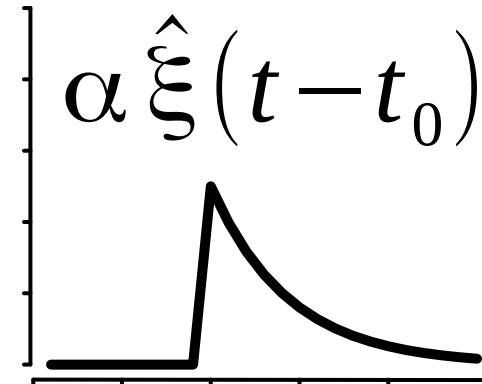
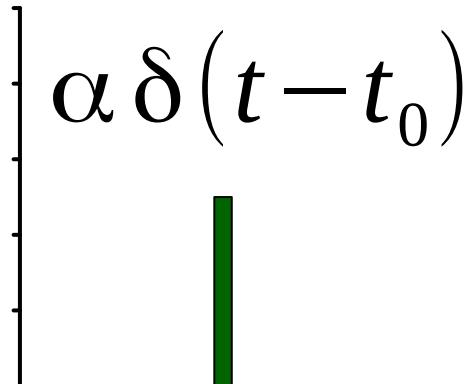
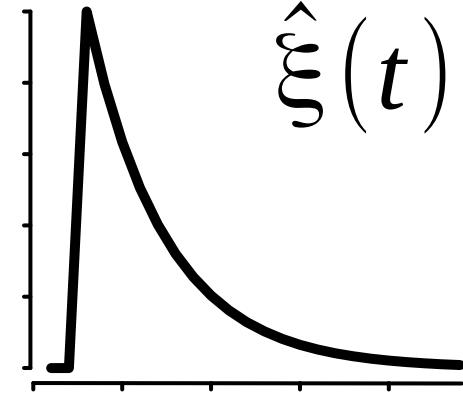
The equation shows the state $\xi(t)$ as a sum of an exogenous stimulus $\mu s(t)$ and an endogenous reaction $C \int_0^t \xi(t - \tau) \hat{\tau}^{-(1+\theta)} d\tau$. Red arrows point from the words "popularity" and "exogenous sensitivity" to the terms $\mu s(t)$ and $\int_0^t \xi(t - \tau) \hat{\tau}^{-(1+\theta)} d\tau$ respectively.

HIP as a Linear Time-Invariant system

promotion



response

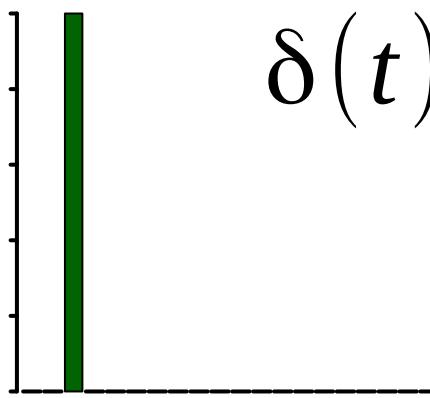


$$\xi(t) = \mu s(t) + C \int_0^t \xi(t - \tau) \hat{\tau}^{-(1+\theta)} d\tau$$

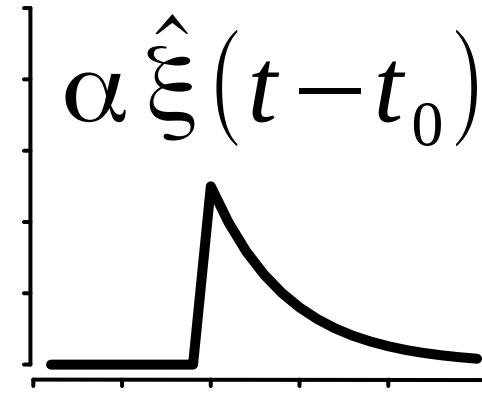
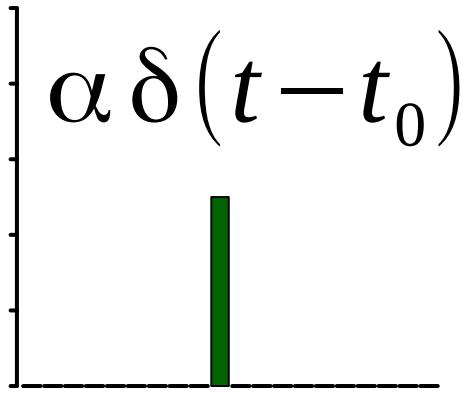
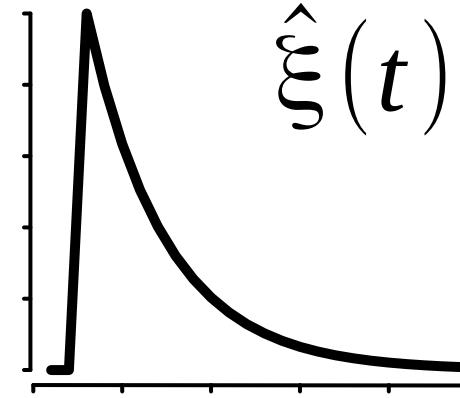
popularity ↓
exogenous sensitivity exogenous stimuli endogenous reaction

HIP as a Linear Time-Invariant system

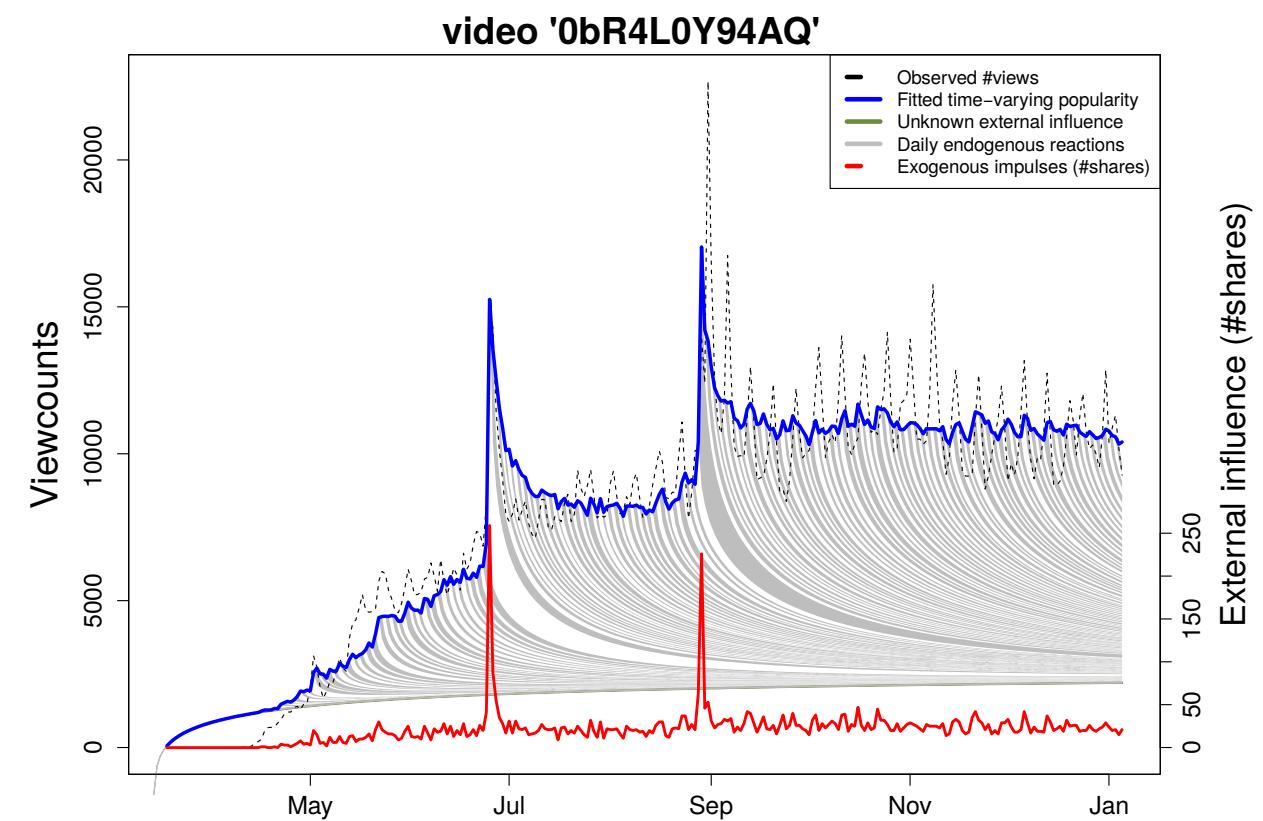
promotion



response

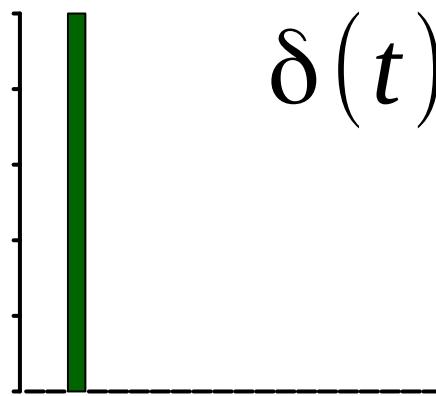


scale,
shift, add

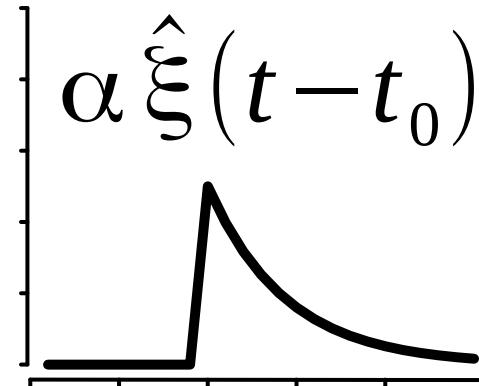
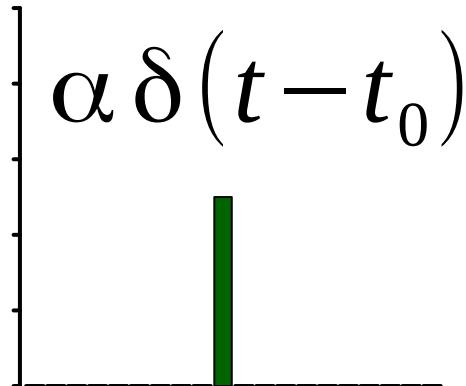
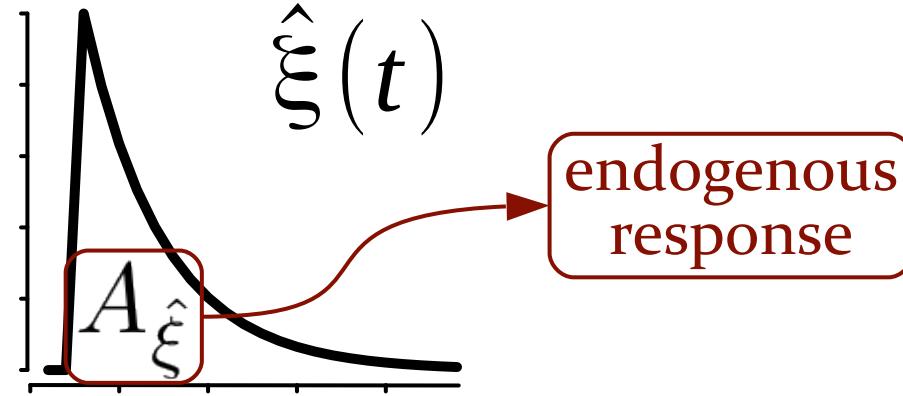


HIP as a Linear Time-Invariant system

promotion



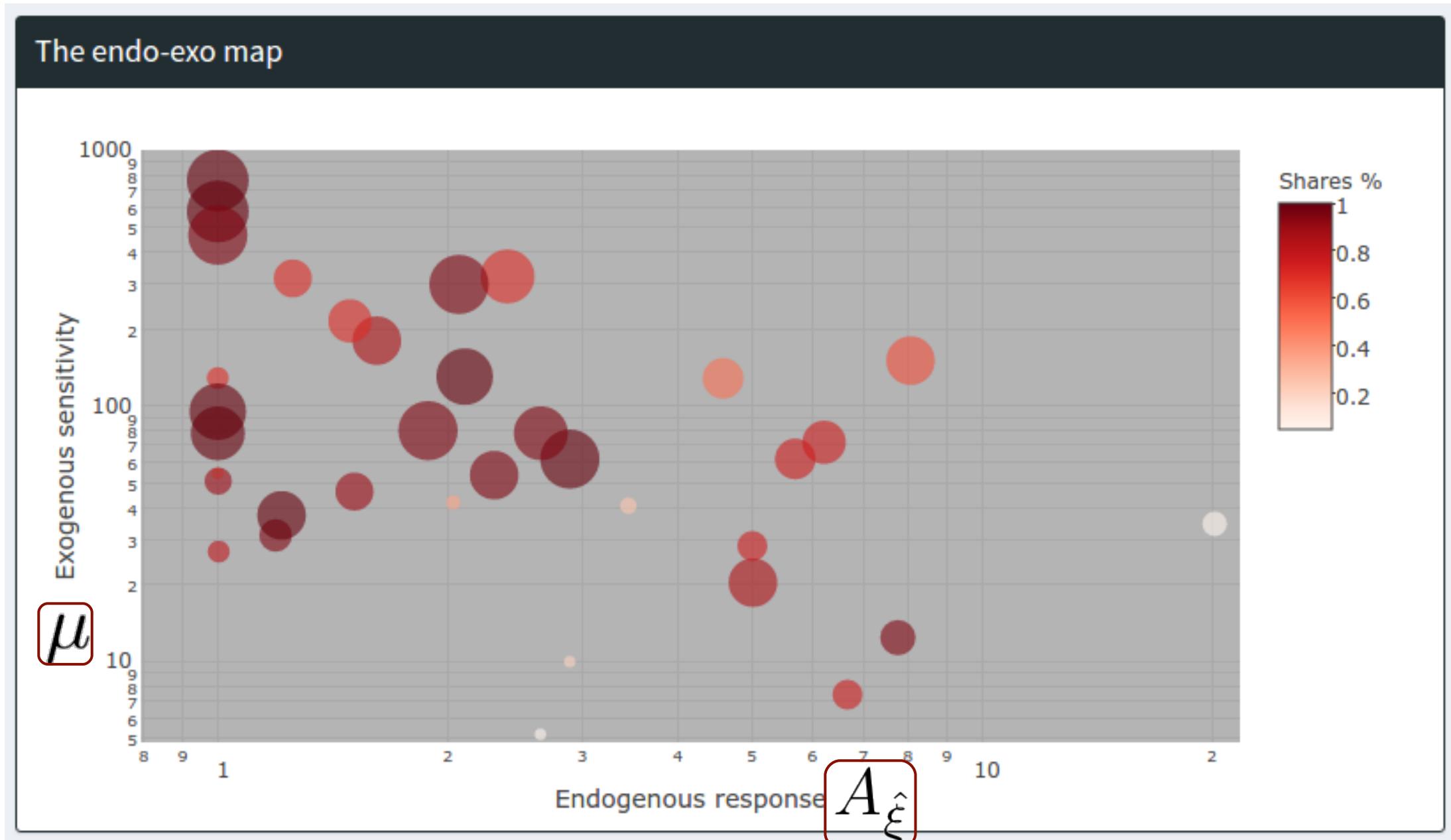
response



$$\xi(t) = \boxed{\mu} s(t) + C \int_0^t \xi(t - \tau) \hat{\tau}^{-(1+\theta)} d\tau$$

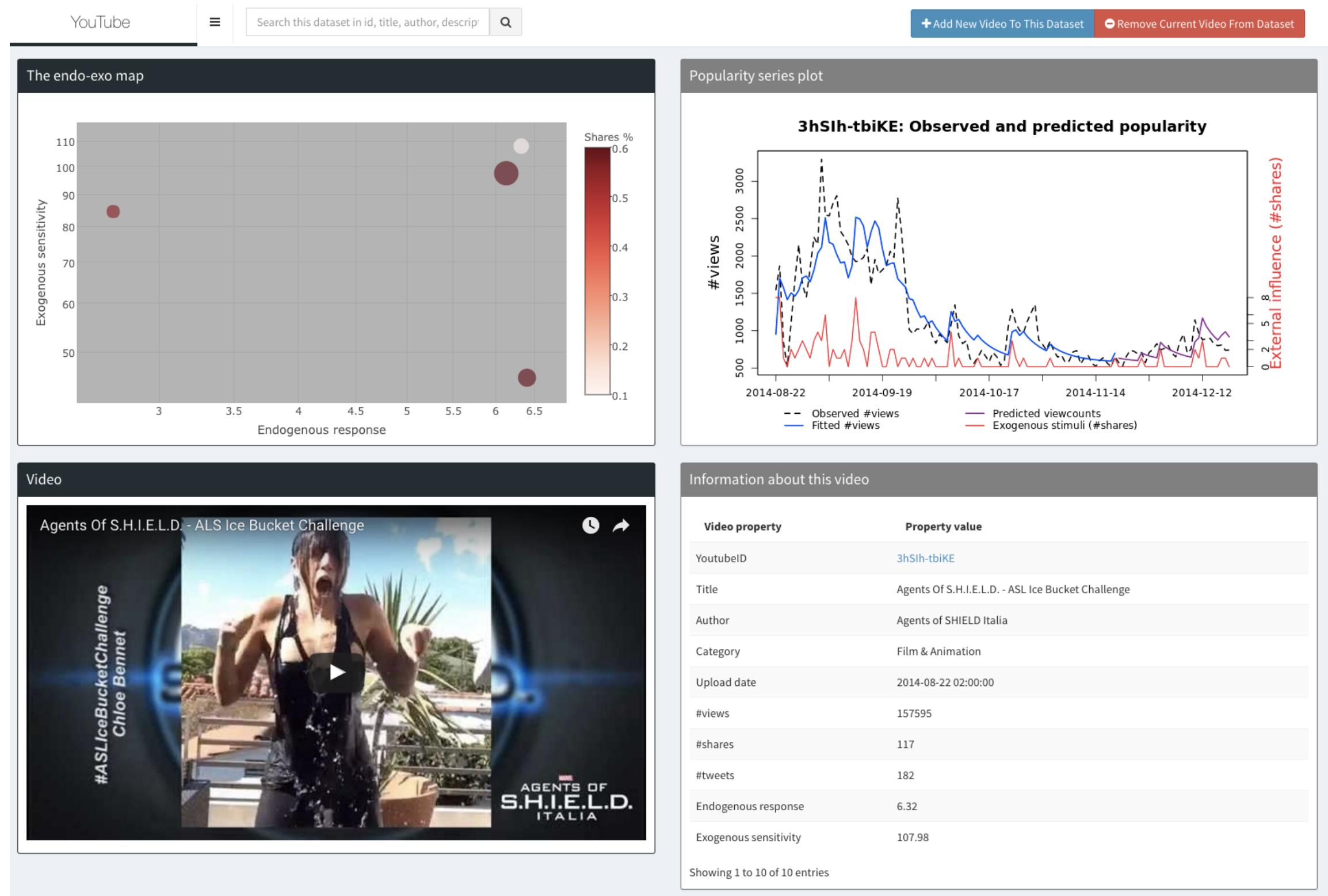
popularity \downarrow exogenous sensitivity \downarrow exogenous stimuli \downarrow endogenous reaction

The “endo-exo” map



Explain popularity dynamics

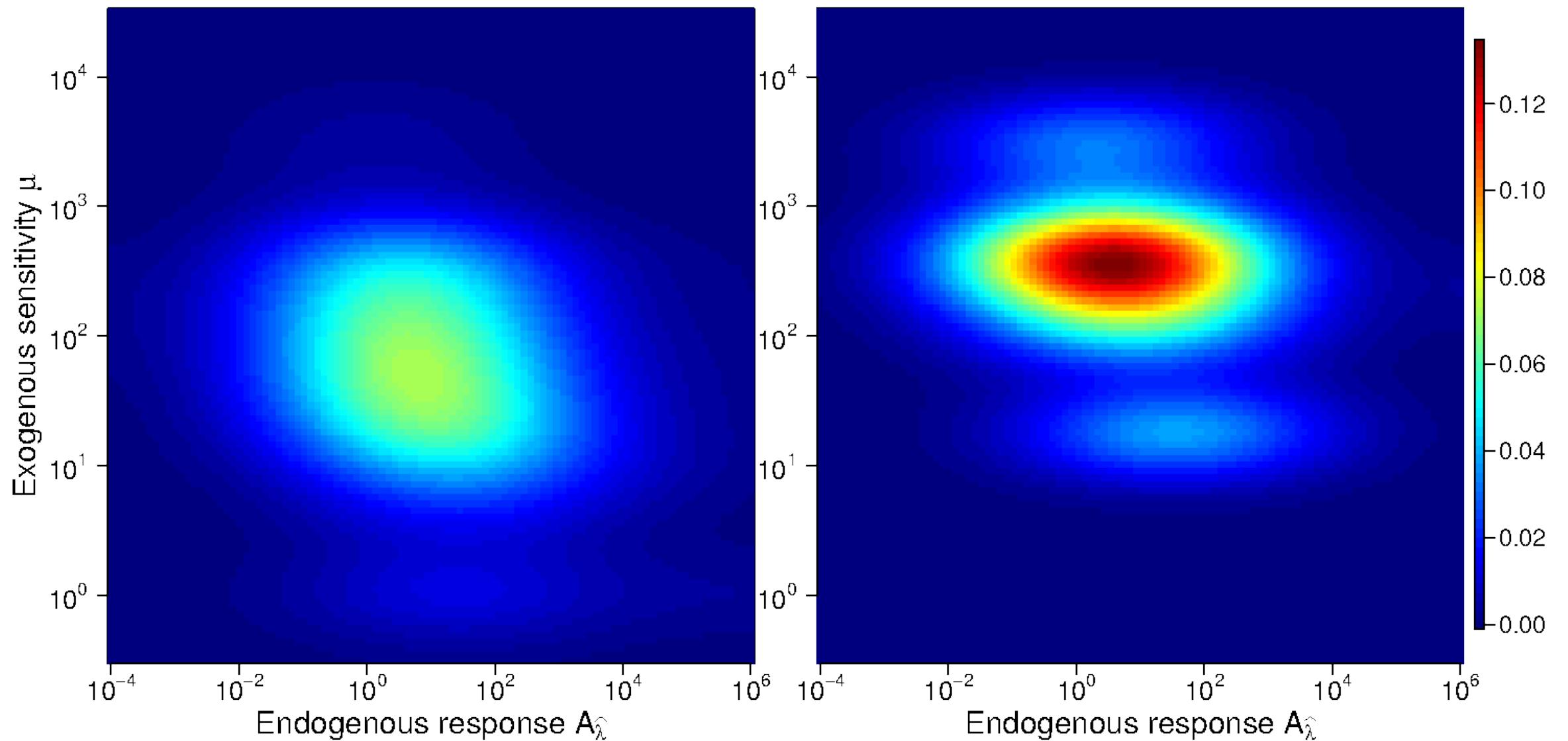
[Kong et al, WWW'18]



Explain popularity – all vs top 5%

Film and Animation:

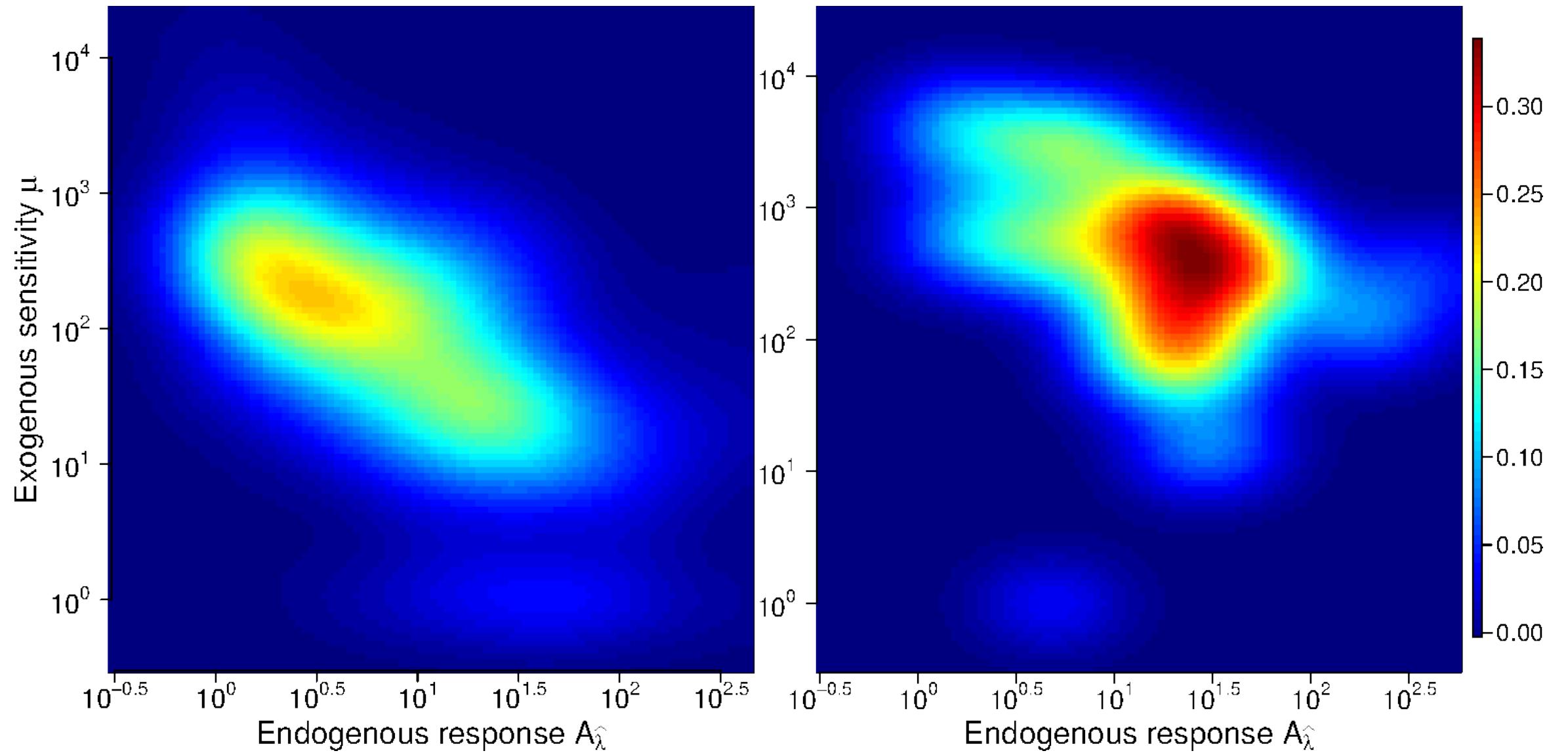
more popular videos have higher sensitivity



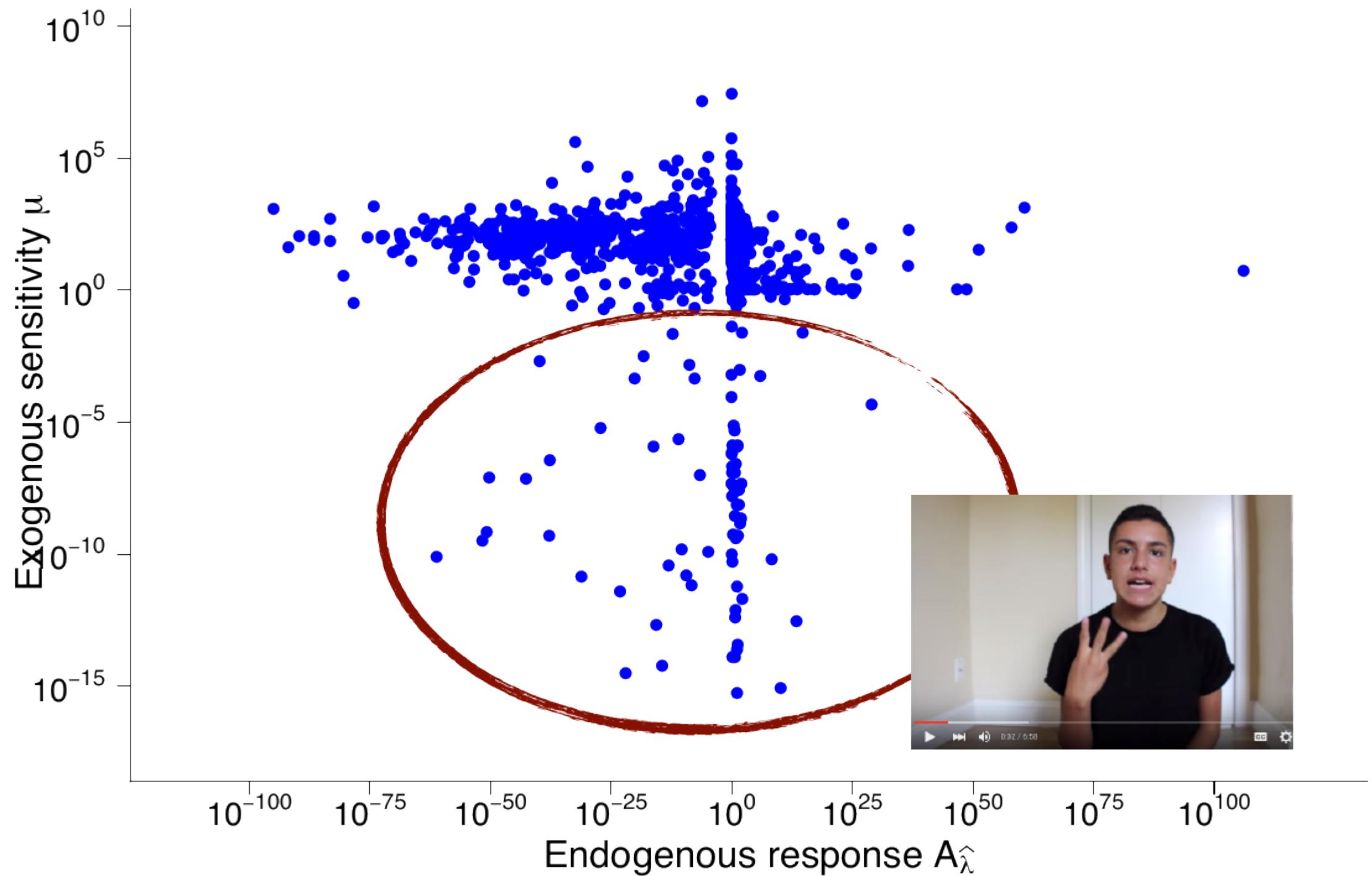
Explain popularity – all vs top 5%

Games:

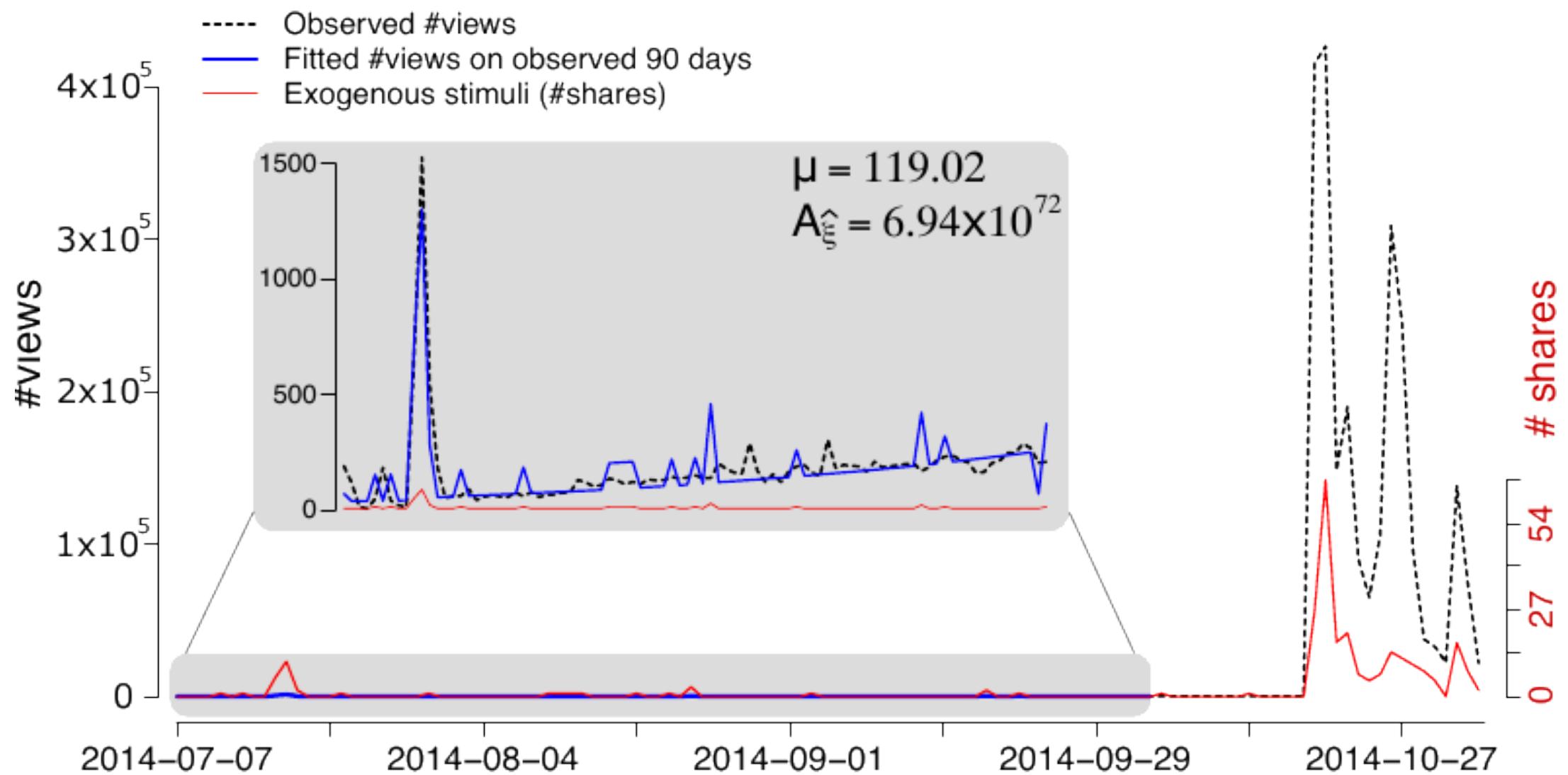
more popular videos have higher endogenous response



Which videos are un-promotable?



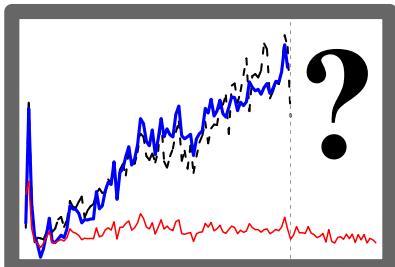
“Potentially viral” video



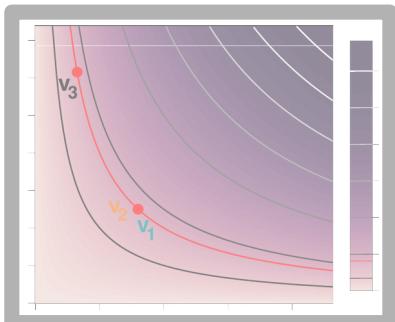
Presentation outline



Modeling popularity with HIP



A progression of two problems relating to predicting popularity under promotion

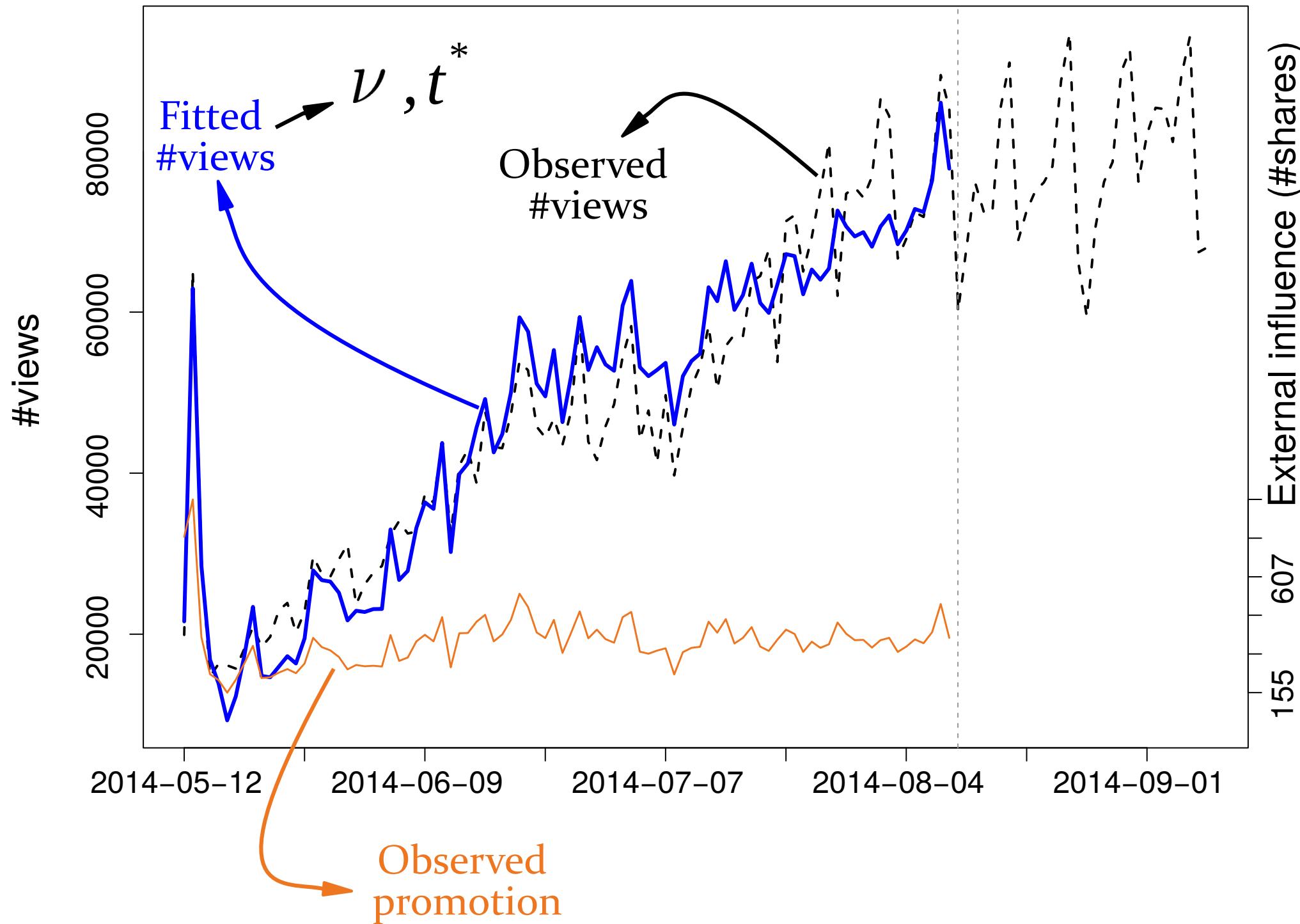


Content virality and maturity time

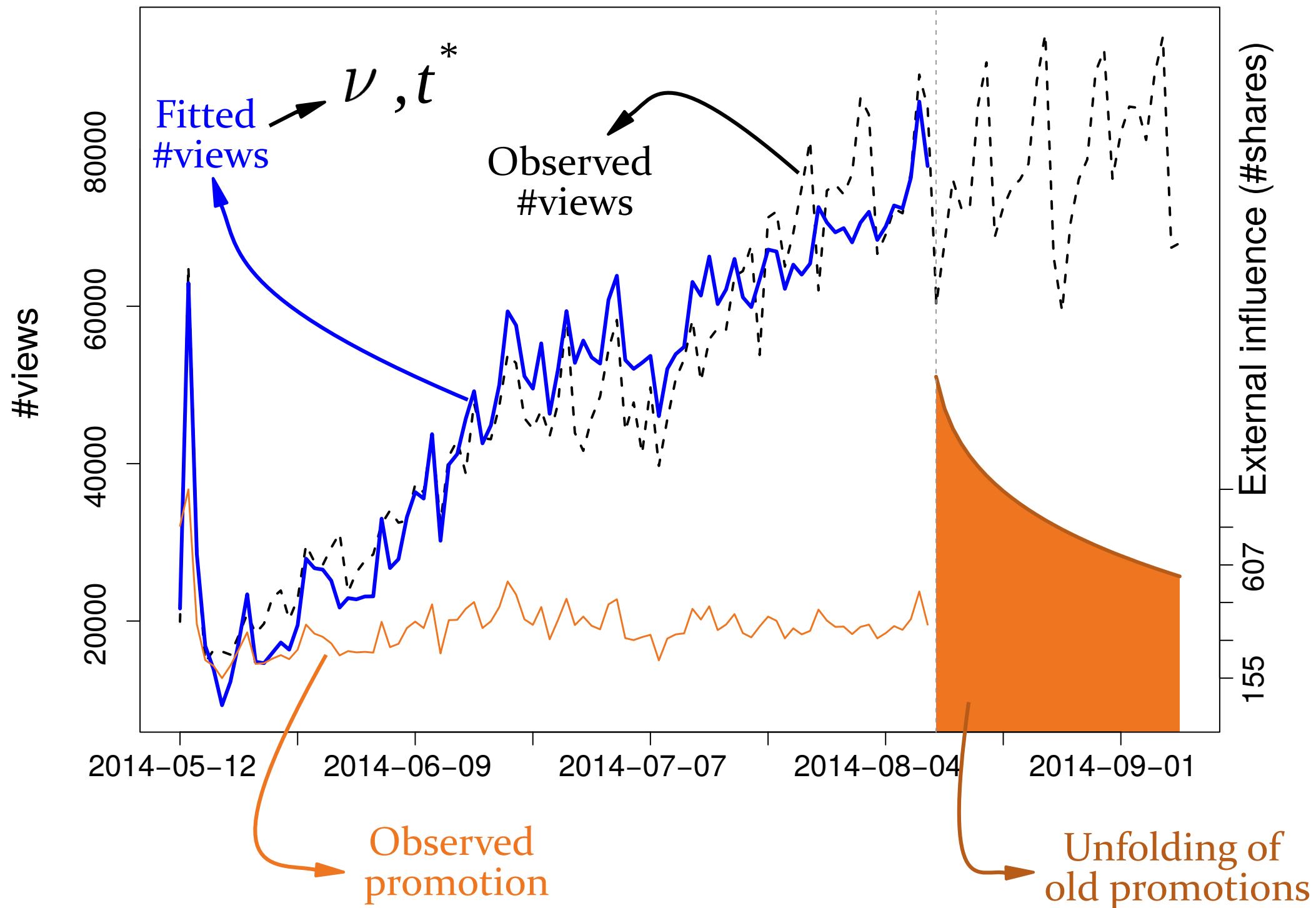


Promotions schedules and memory lengthening through promotion

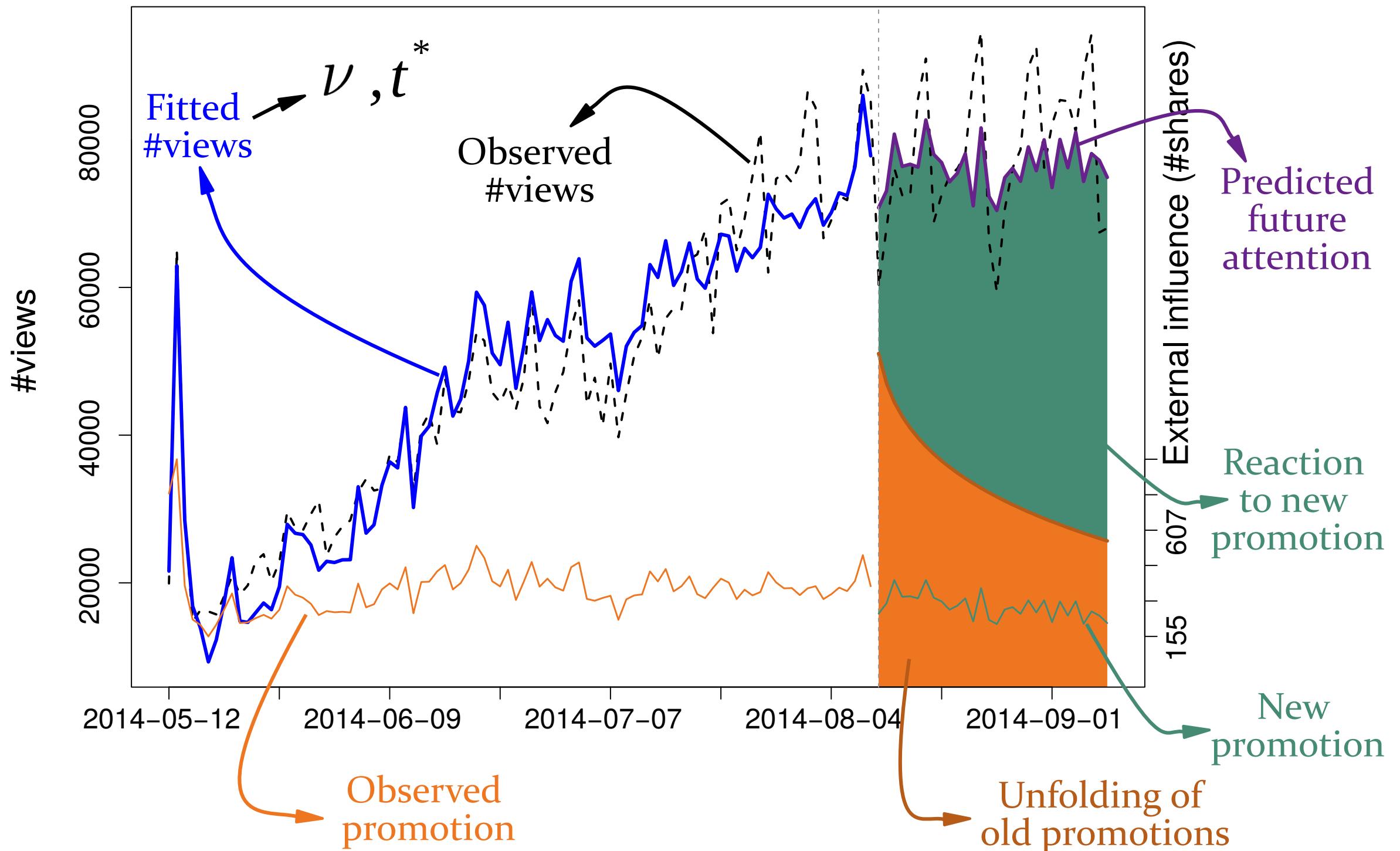
Forecasting future views (1)



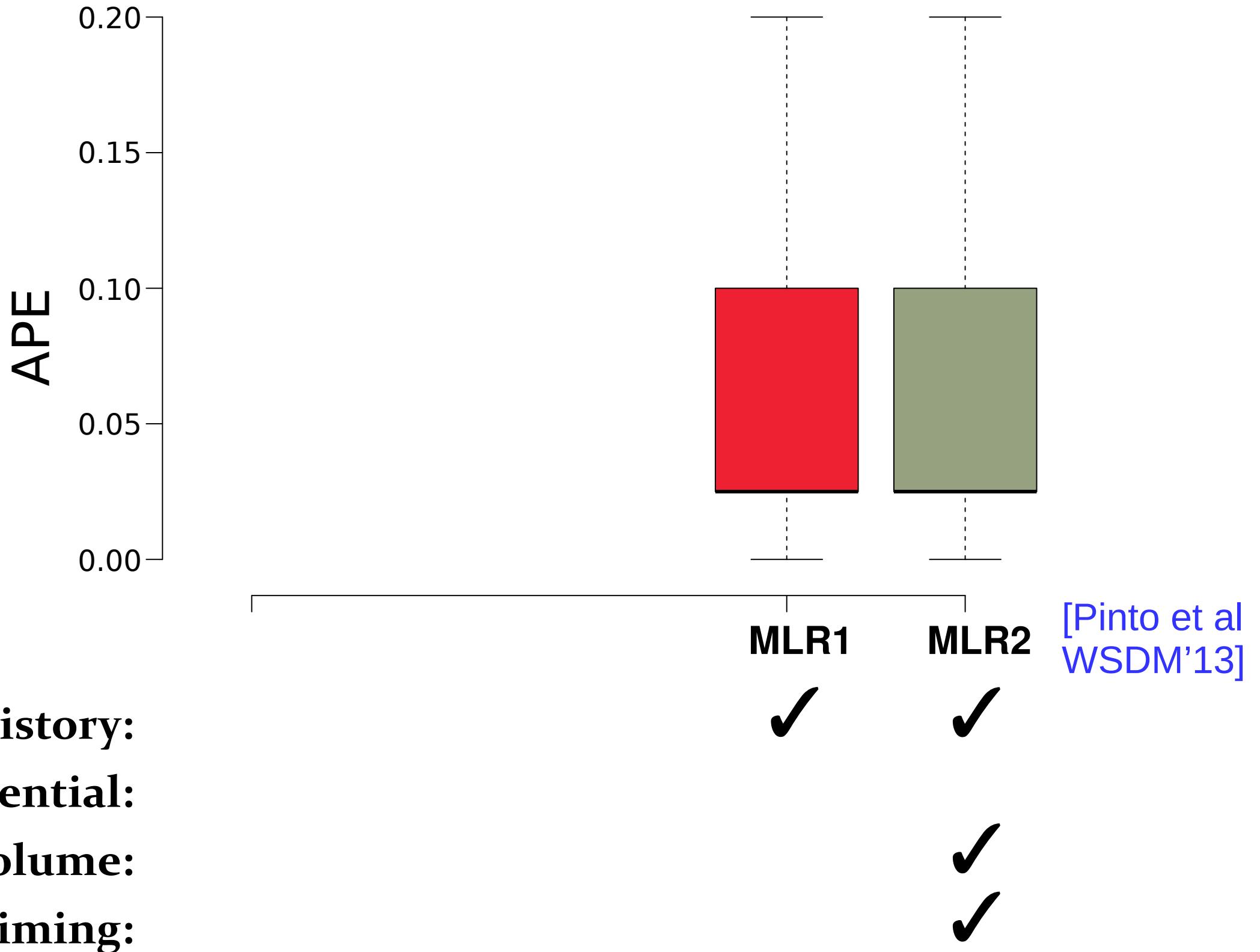
Forecasting future views (1)



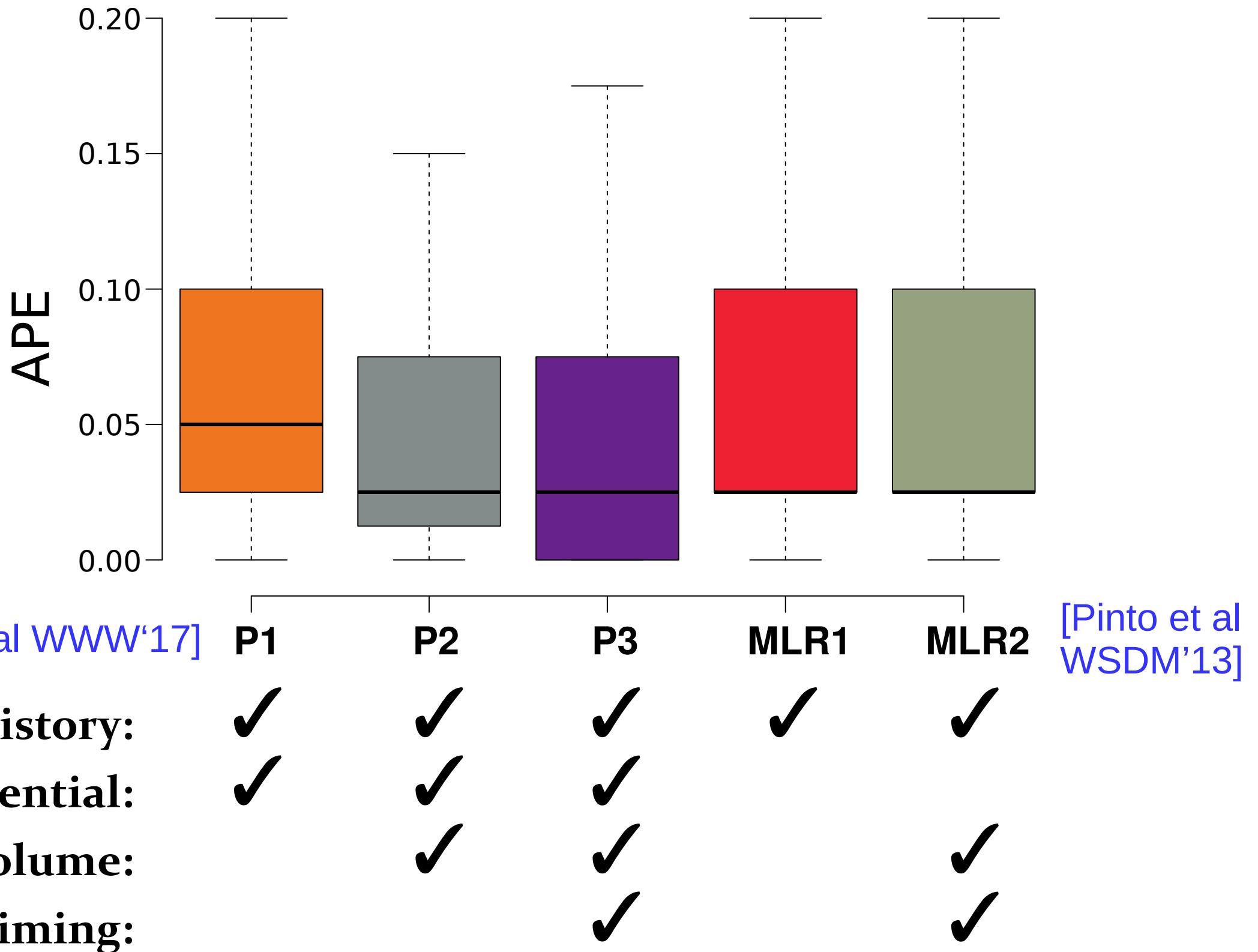
Forecasting future views (1)



Forecasting future views (2)

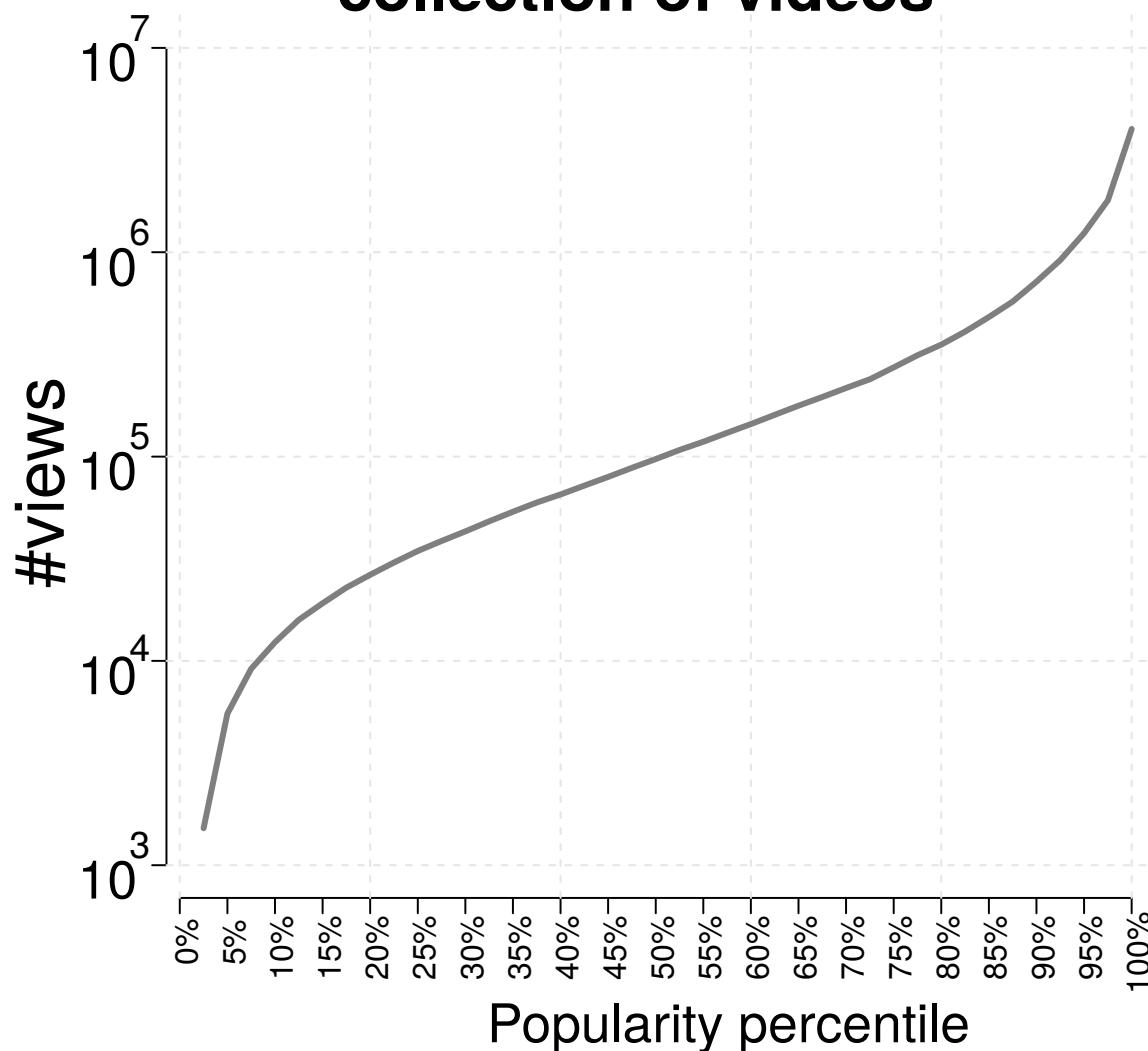


Forecasting future views (2)

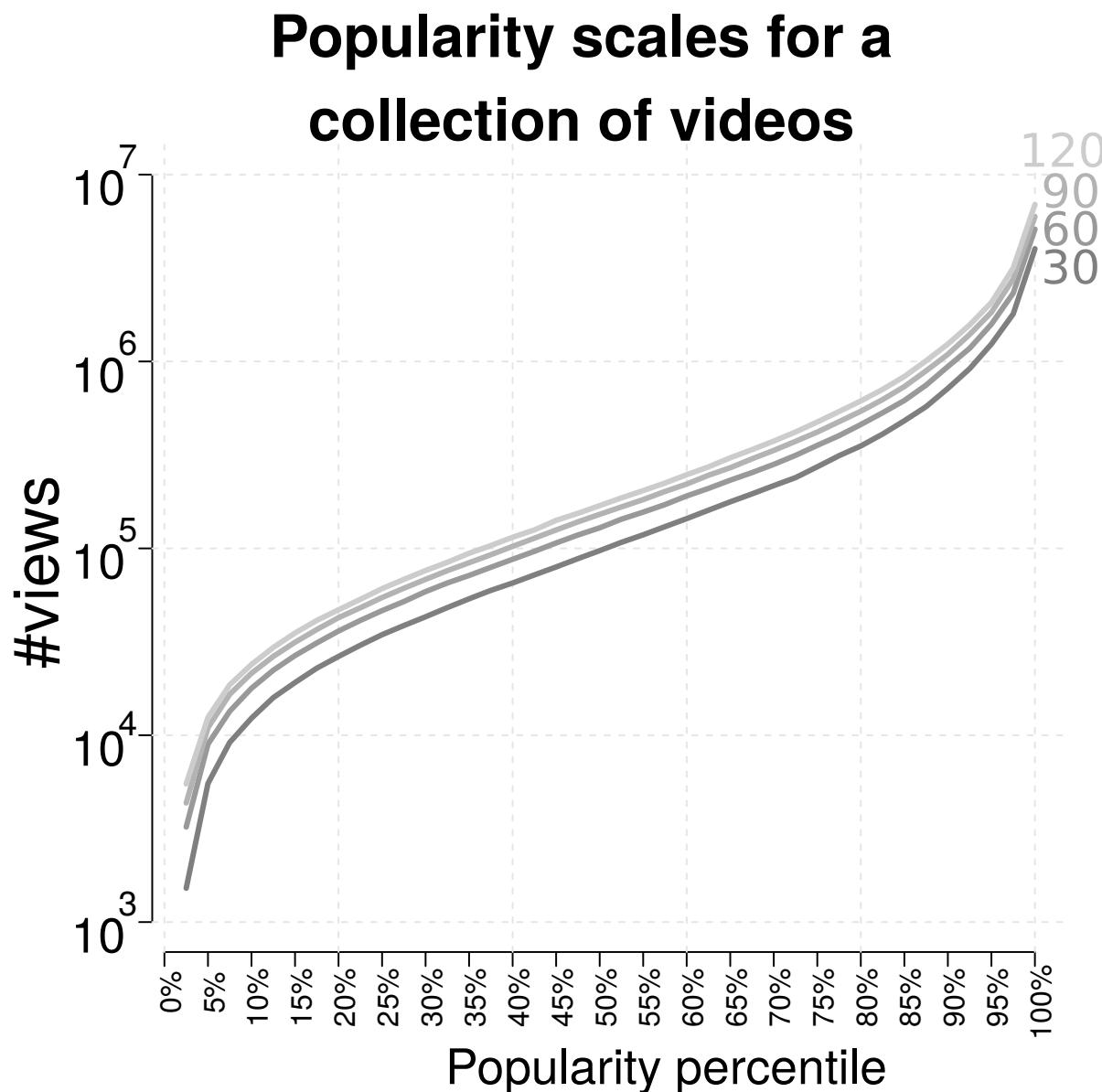


Popularity scale over time

**Popularity scales for a
collection of videos**

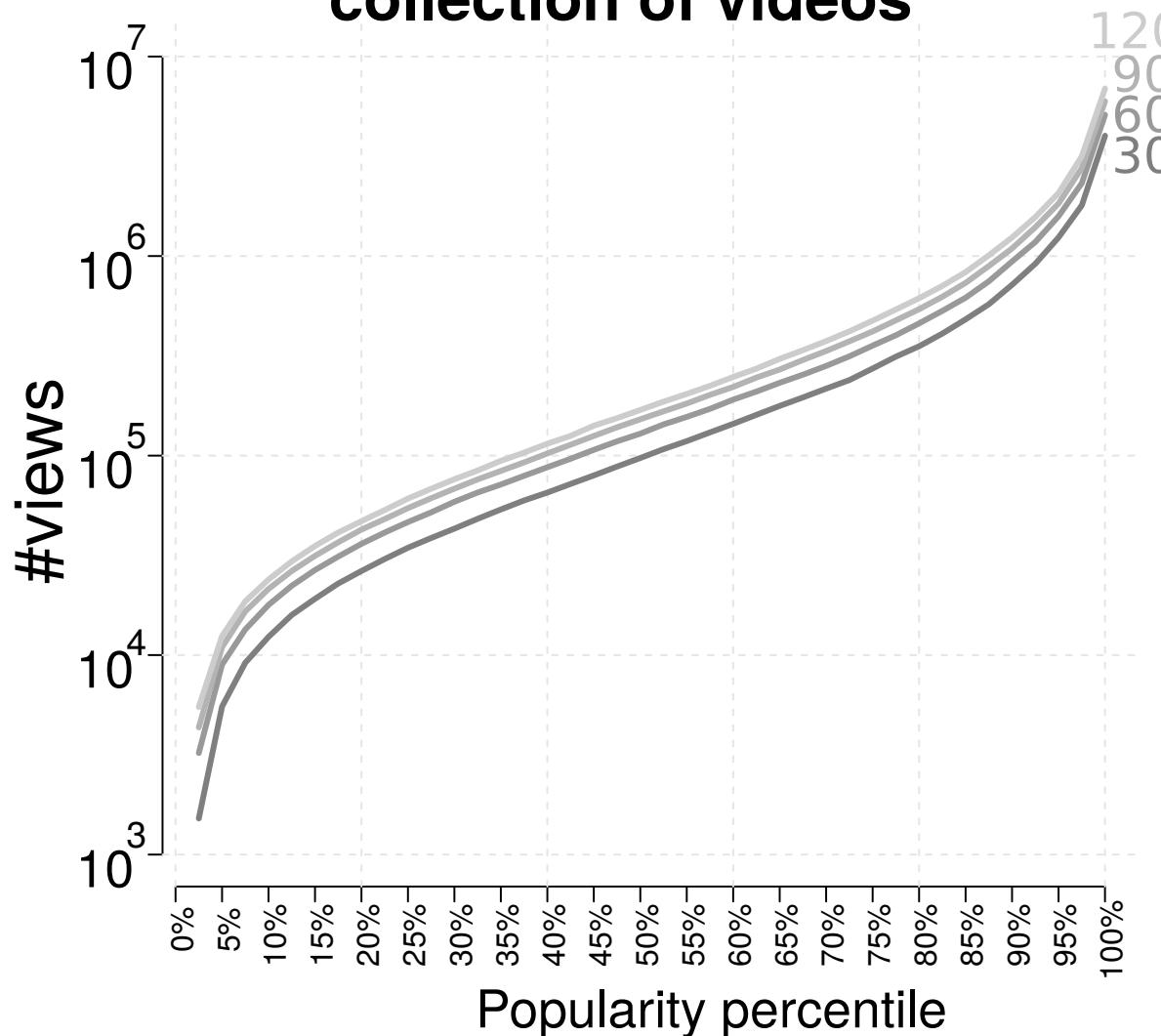


Popularity scale over time

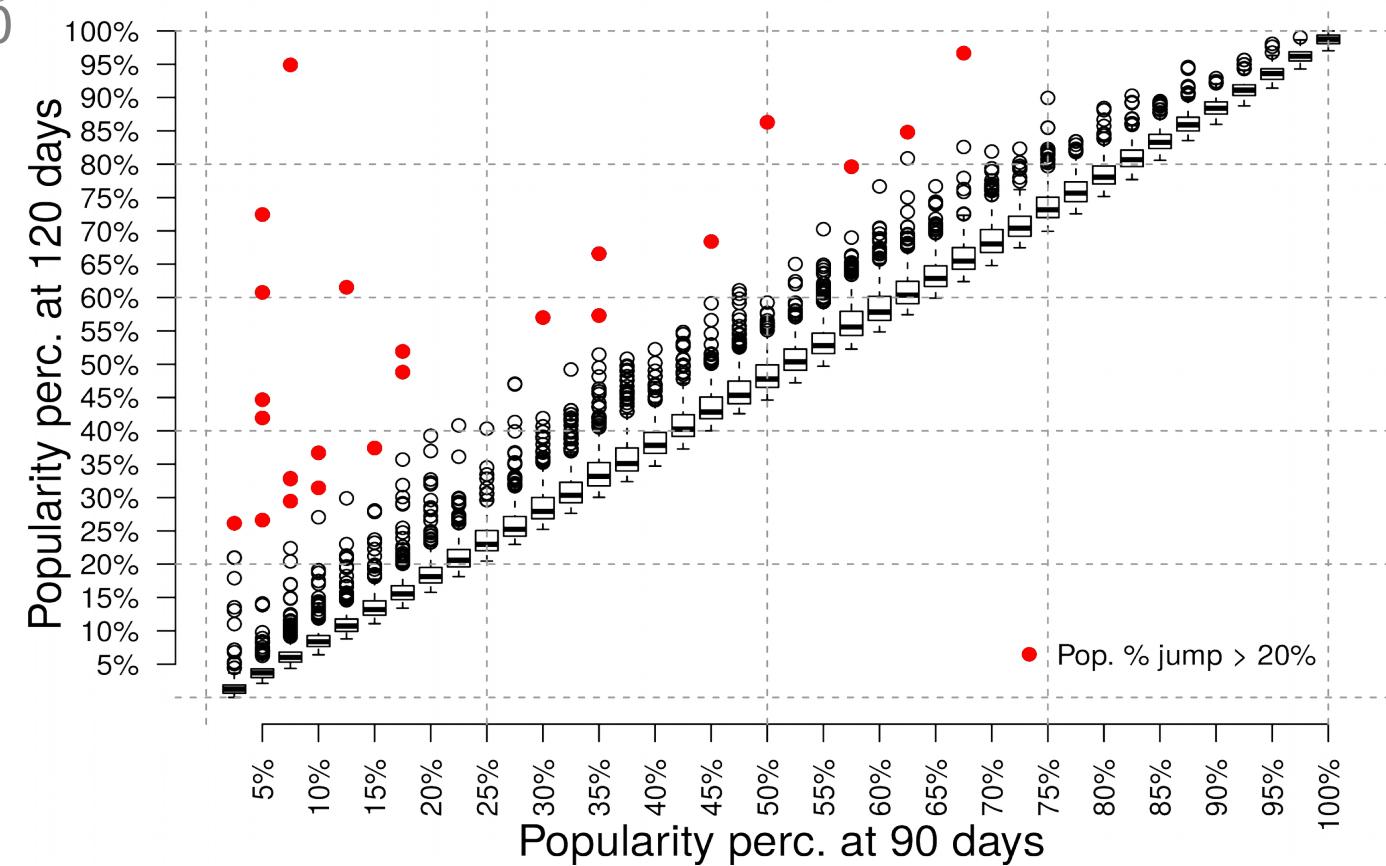


Popularity scale over time

Popularity scales for a collection of videos

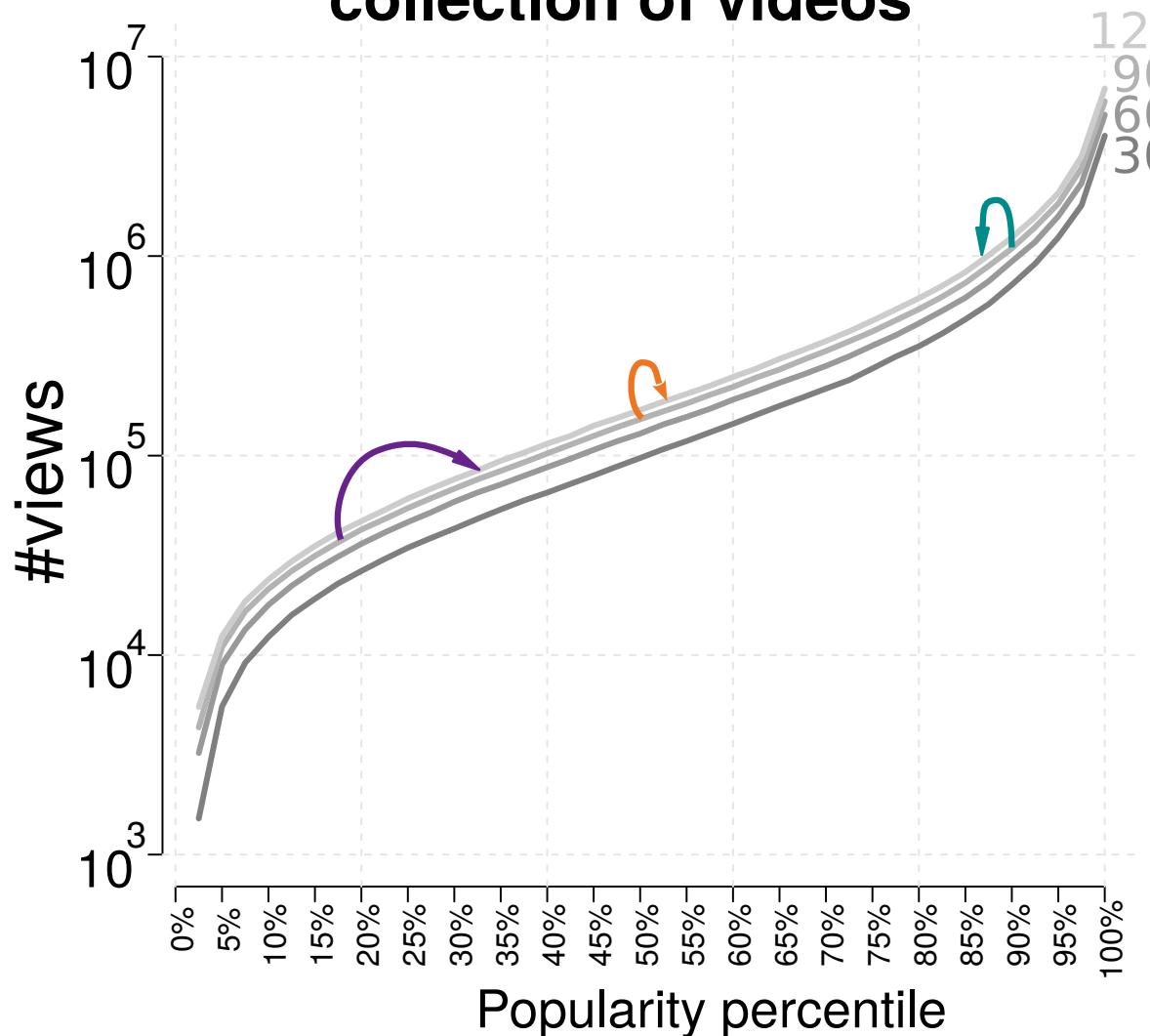


Individual video pop. % at 90 days vs. 120 days

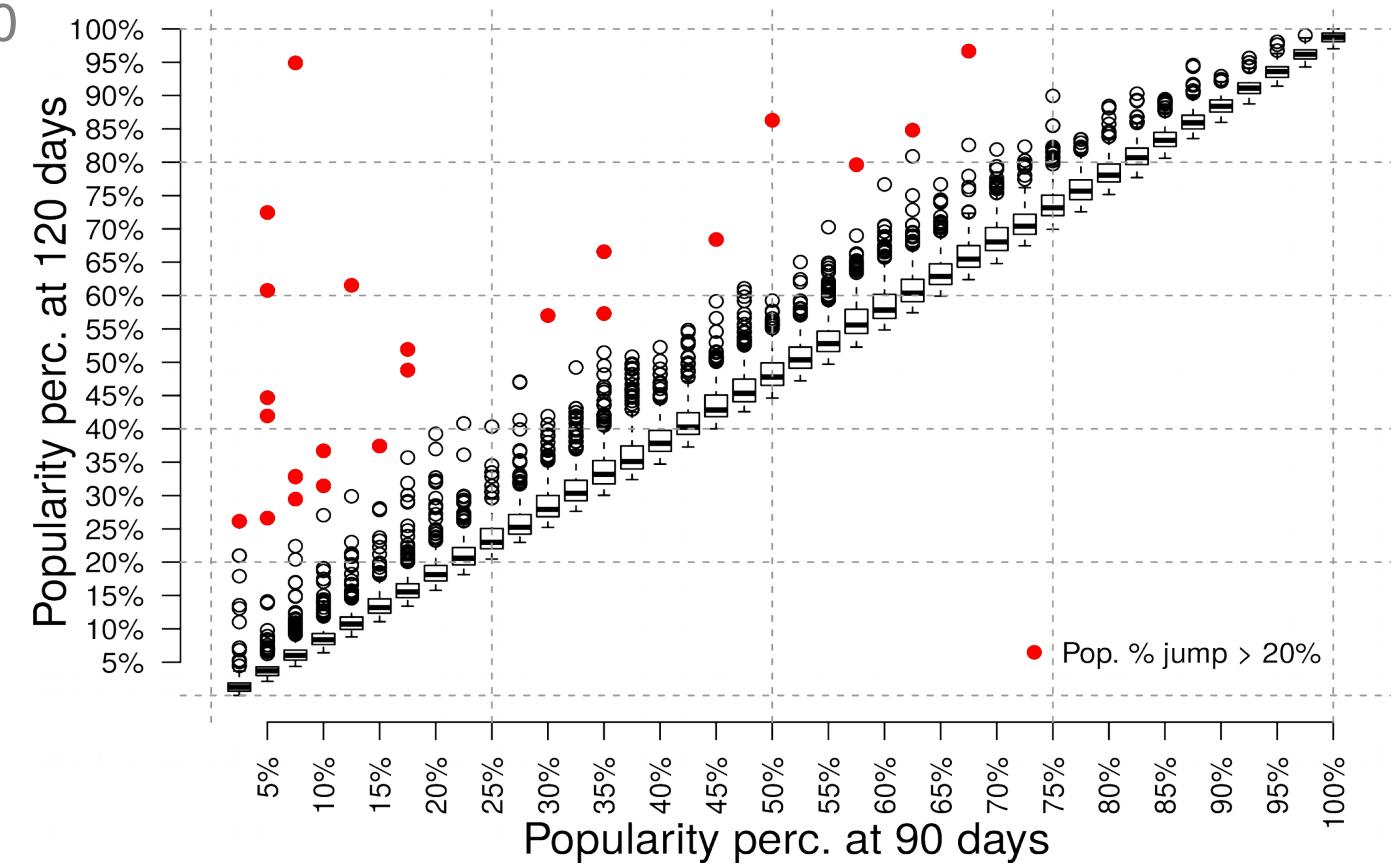


Popularity scale over time

Popularity scales for a collection of videos



Individual video pop. % at 90 days vs. 120 days



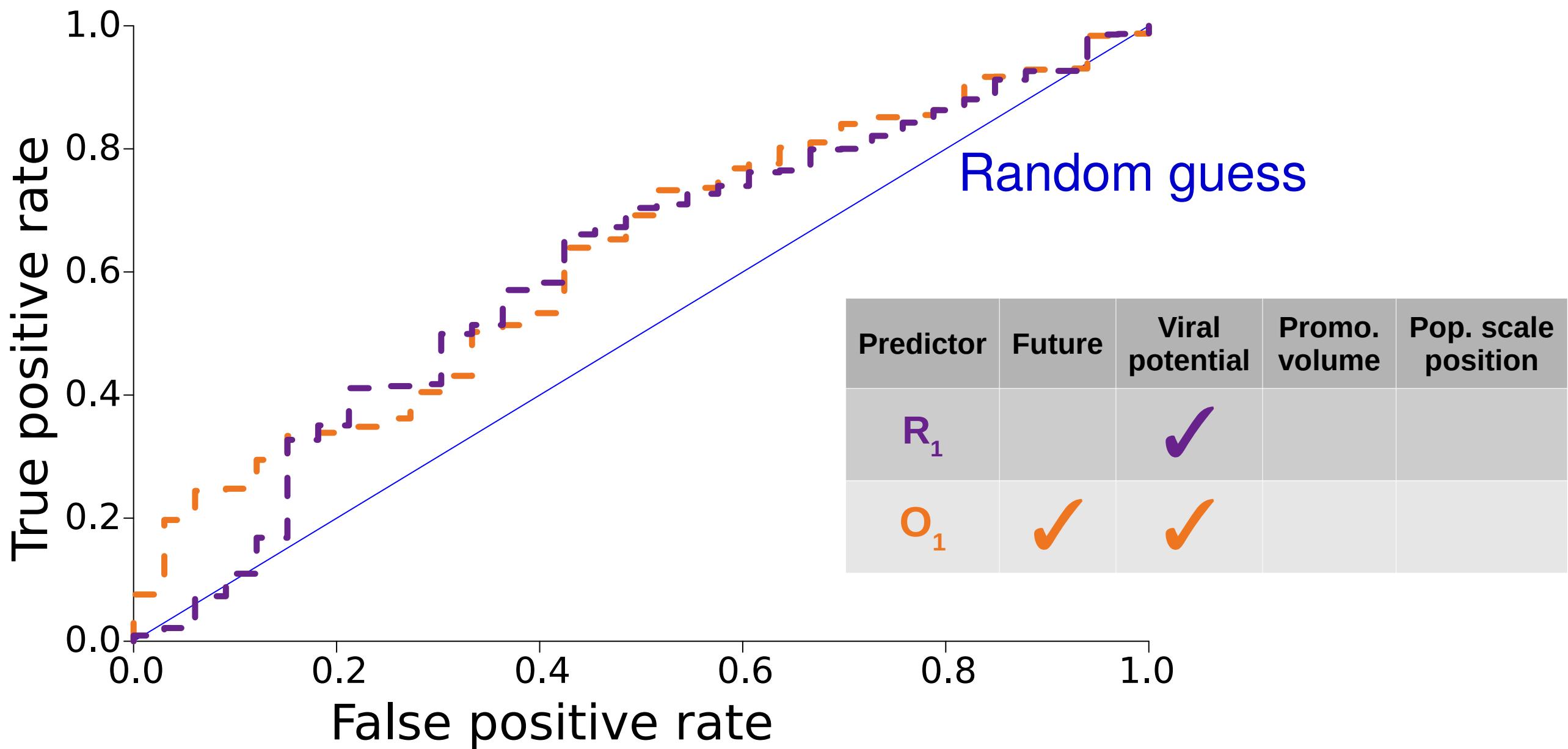
Impact of 40k views:

start at 17.5% → +15%

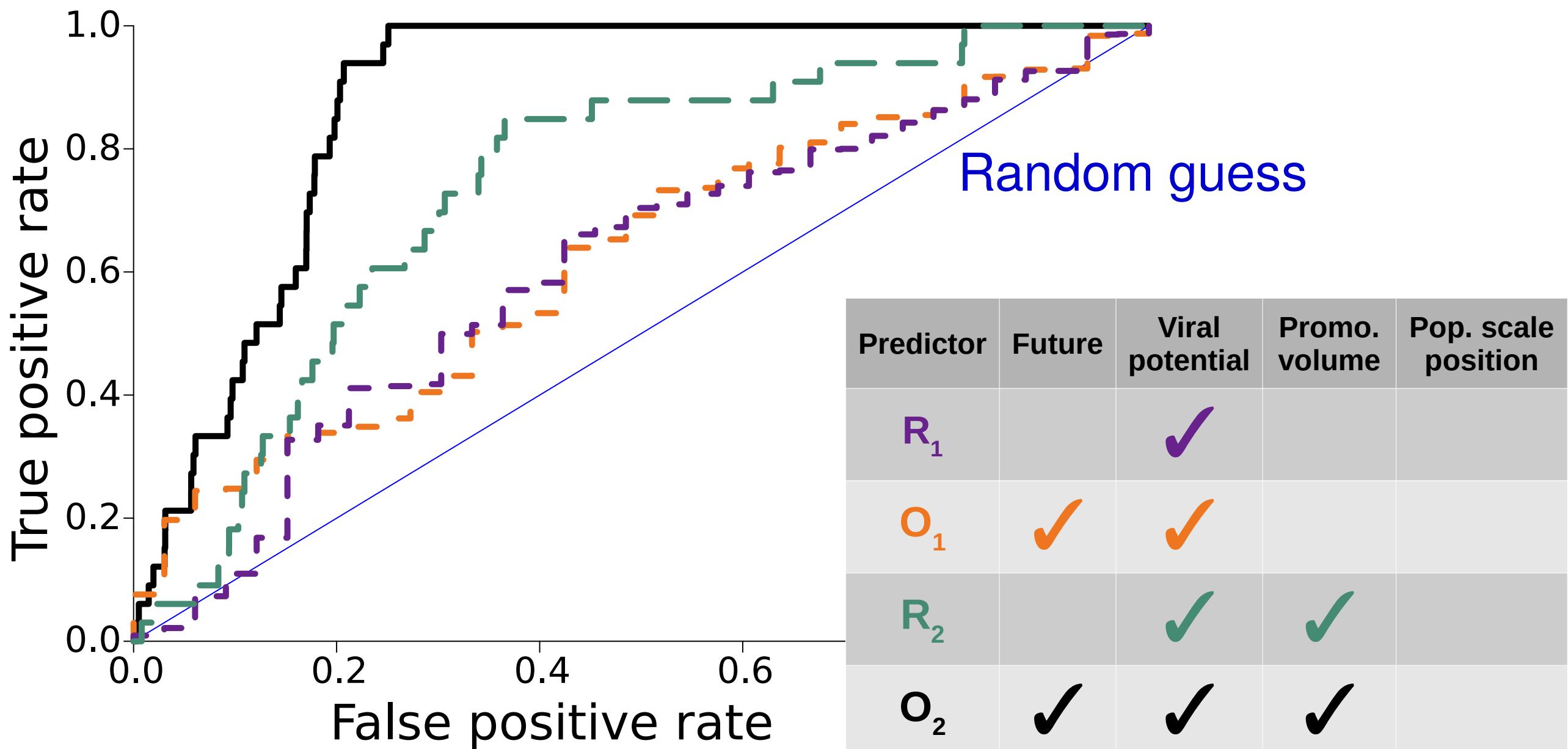
start at 50% → +2.5%

start at 90% → -2.5%

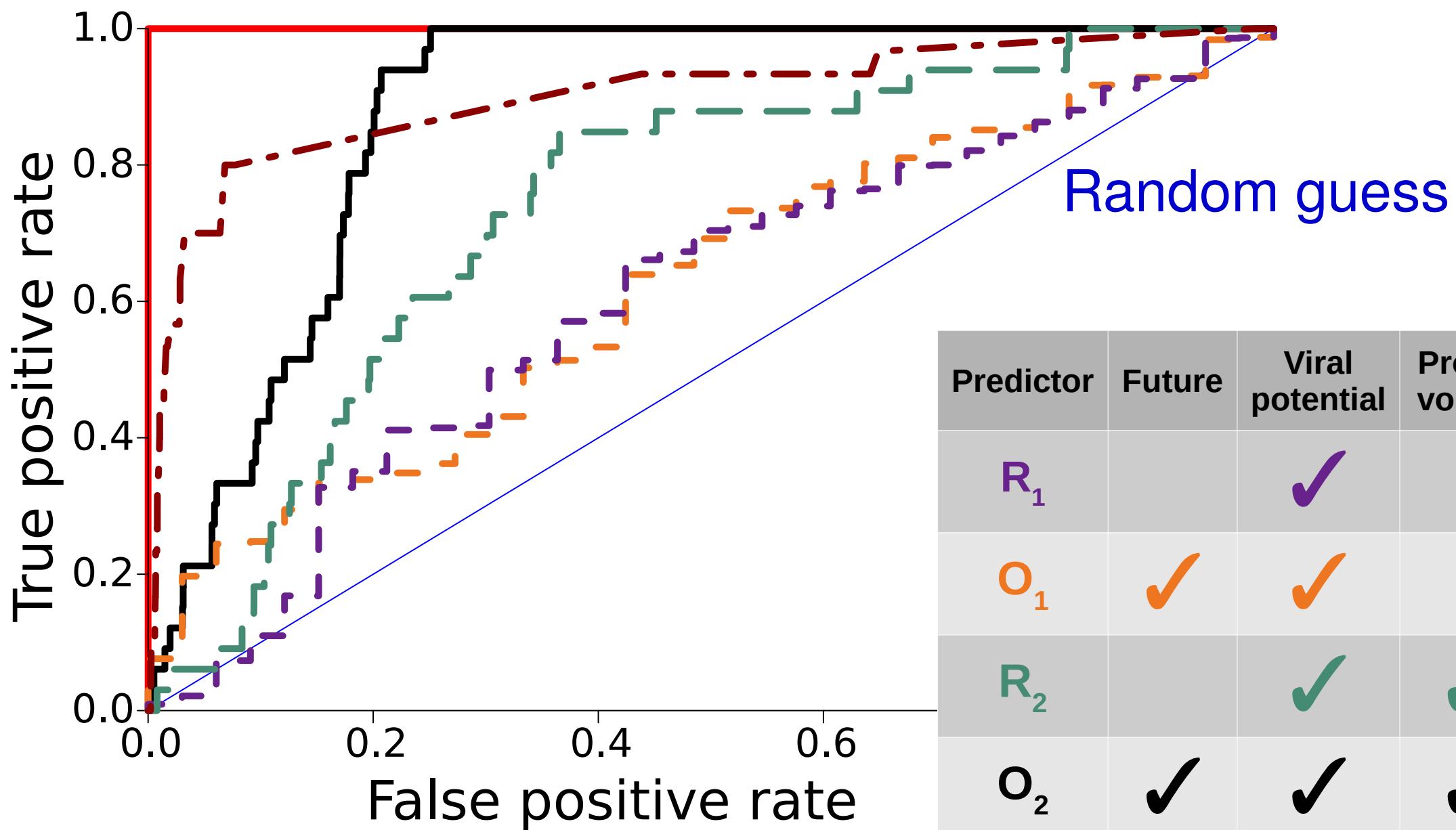
ROC curves for videos that jump



ROC curves for videos that jump

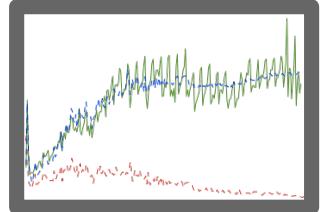


ROC curves for videos that jump

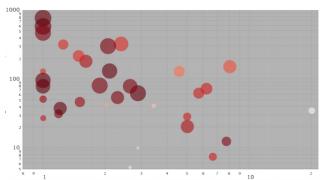


Predictor	Future	Viral potential	Promo. volume	Pop. scale position
R_1		✓		
O_1	✓	✓		
R_2		✓	✓	
O_2	✓	✓	✓	
R_3		✓	✓	✓
O_3	✓	✓	✓	✓

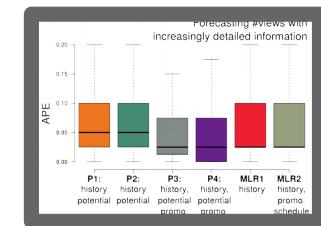
Summary



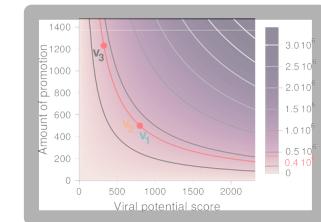
HIP: a mathematical model linking promotion and popularity



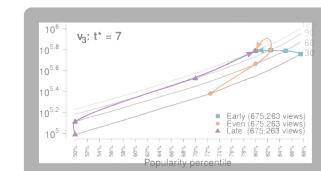
Explain popularity dynamics and identify potentially viral videos



Important factors for forecasting popularity: *virality score*, *promotion volume* and *popularity scale position*

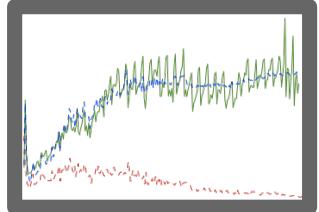


Two measures: *virality score* and *maturity time*

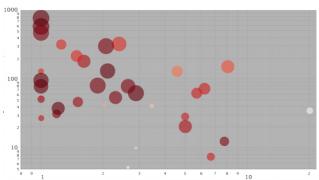


Maturity time influences the cost-effectiveness of promotion schedules

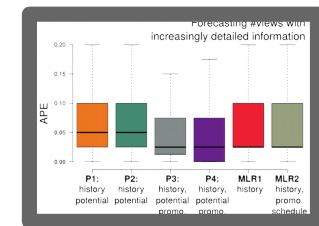
Summary



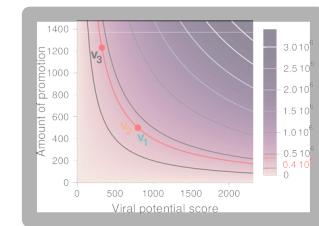
HIP: a mathematical model linking promotion and popularity



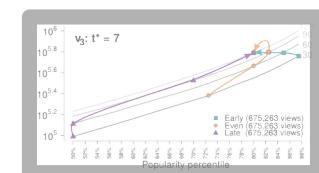
Explain popularity dynamics and identify potentially viral videos



Important factors for forecasting popularity: *virality score*, *promotion volume* and *popularity scale position*



Two measures: *virality score* and *maturity time*



Maturity time influences the cost-effectiveness of promotion schedules

Limitations & future work:

unobserved sources of external influence, seasonality, network structure, reaction to past and future promotions is the same.

Thank you!

References:

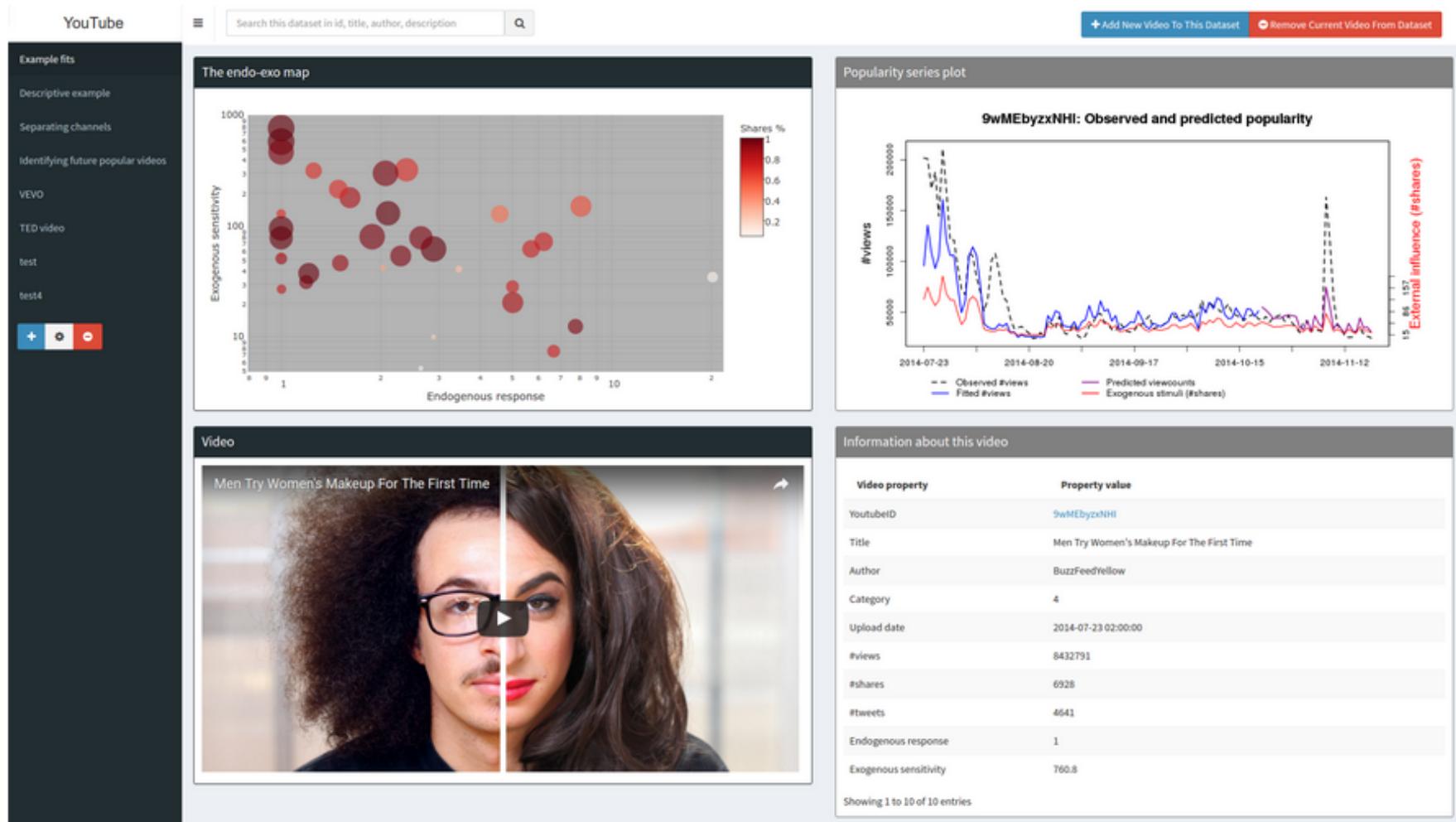
Rizoiu, M.-A., Xie, L., Sanner, S., Cebrian, M., Yu, H., & Van Hentenryck, P. **Expecting to be HIP: Hawkes Intensity Processes for Social Media Popularity**. In *26th International Conference on World Wide Web - WWW '17*, pp. 735-744, Perth, Australia, 2017. doi: [10.1145/3038912.3052650](https://doi.org/10.1145/3038912.3052650)
[pdf at arxiv with supplementary material](#)

Rizoiu, M.-A., & Xie, L. (2017). **Online Popularity under Promotion: Viral Potential, Forecasting, and the Economics of Time**. In *11th International AAAI Conference on Web and Social Media - ICWSM '17*, p. 10, Montréal, Canada, 2017.
[pdf at arxiv with supplementary material](#)

HIP visualization system

This is an *interactive* visualization of the plots in the paper: the endo-exo map, observed and fitted popularity series and video metadata. It has additional visualizations of TED videos and VEVO musicians. Furthermore, it allows users to add and compare their own videos.

(access the visualizer by clicking on the thumbnail below)

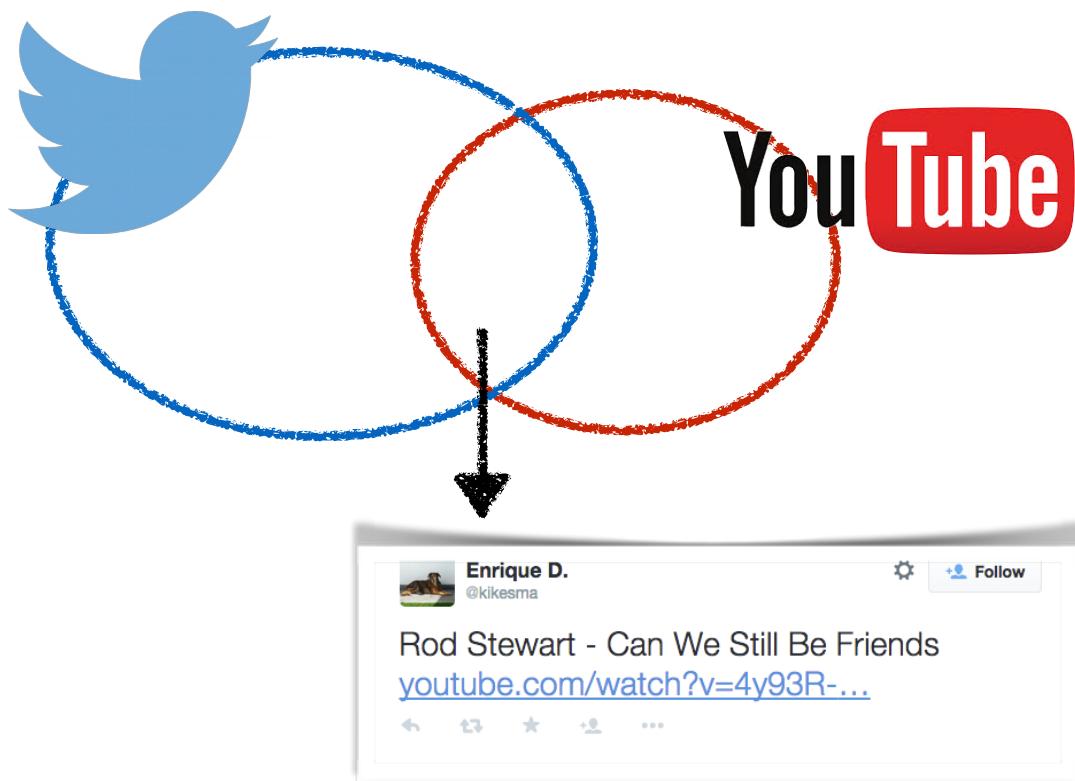


Links:

Code, dataset
and interactive
visualizer:

<https://github.com/andre-i-rizoiu/hip-popularity>

Twitter videos dataset



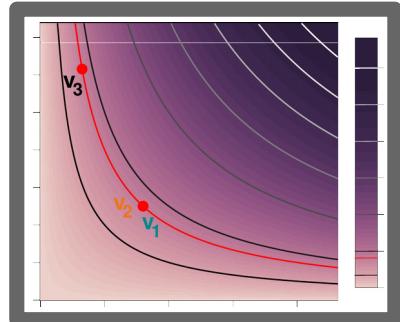
2014.06 - 2014.12
1.061B tweets, 5.89M/day
64.3M users;
81.9M YouTube videos

Category	#vids	Category	#vids
Comedy	865	Music	3549
Education	298	News & Politics	1722
Entertainment	2422	Nonprofits & Activism	333
Film & Animation	664	People & Blogs	1947
Gaming	882	Science & Technology	262
Howto & Style	180	Sports	614
Total:			13,738

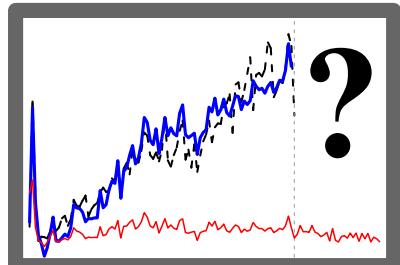
Presentation outline



Modeling popularity with HIP



Content virality and maturity time



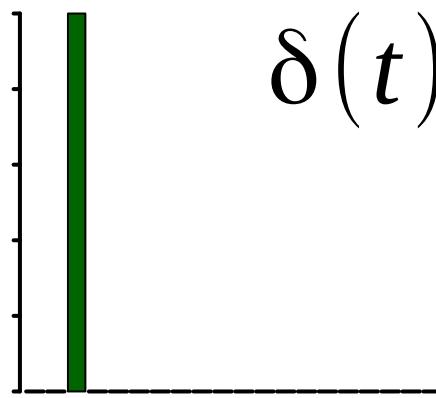
Forecasting popularity under promotion



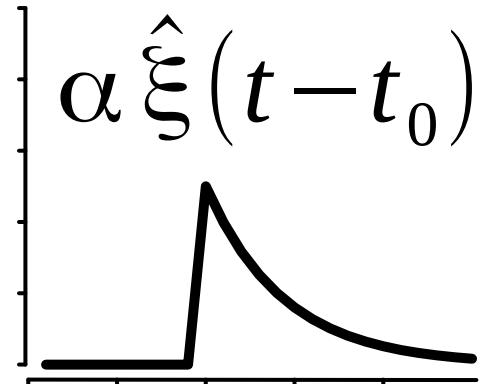
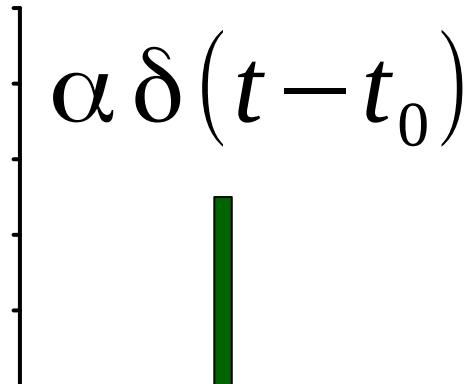
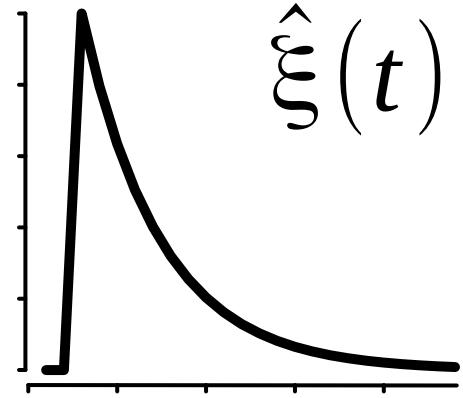
Promotions schedules and memory lengthening through promotion

HIP as a Linear Time-Invariant system

promotion

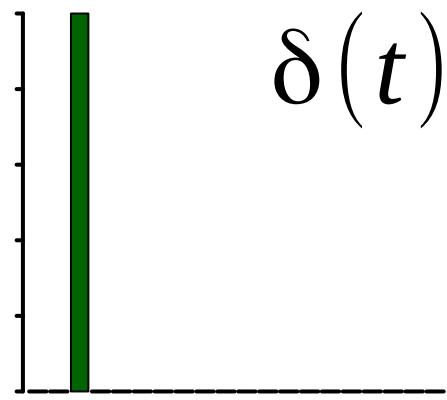


response

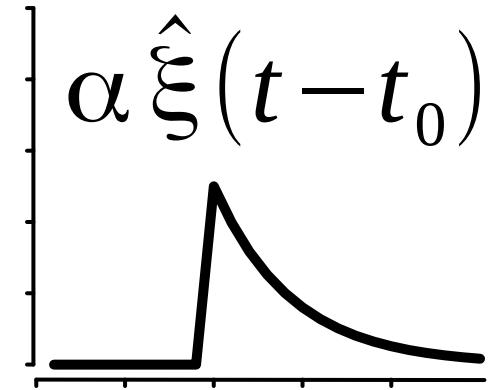
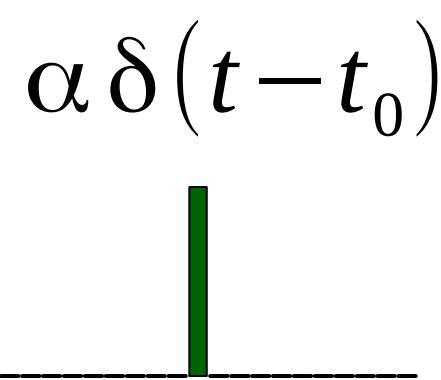
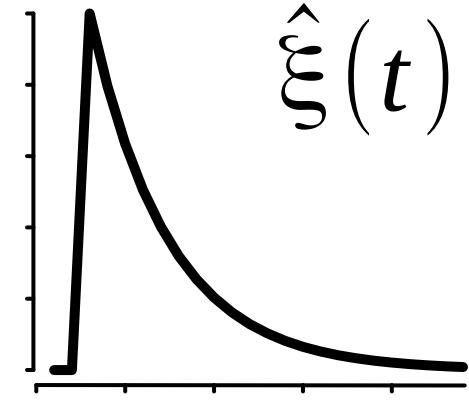


HIP as a Linear Time-Invariant system

promotion

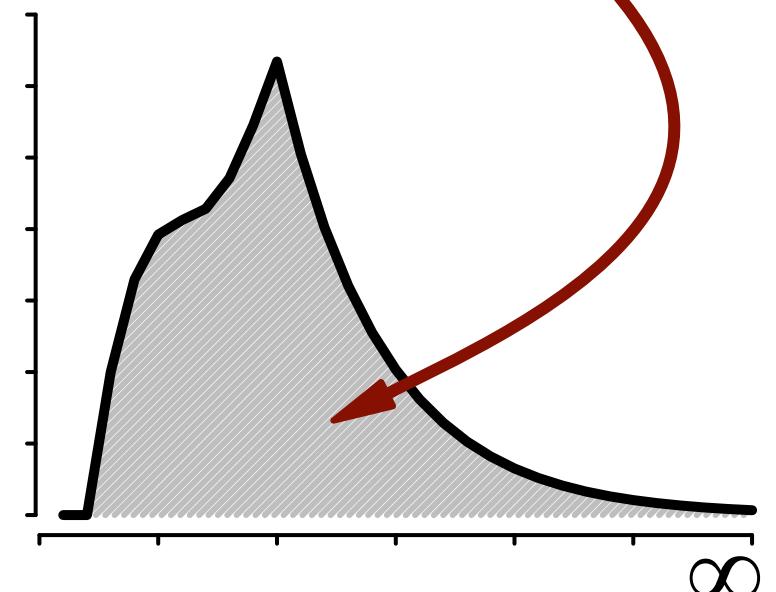
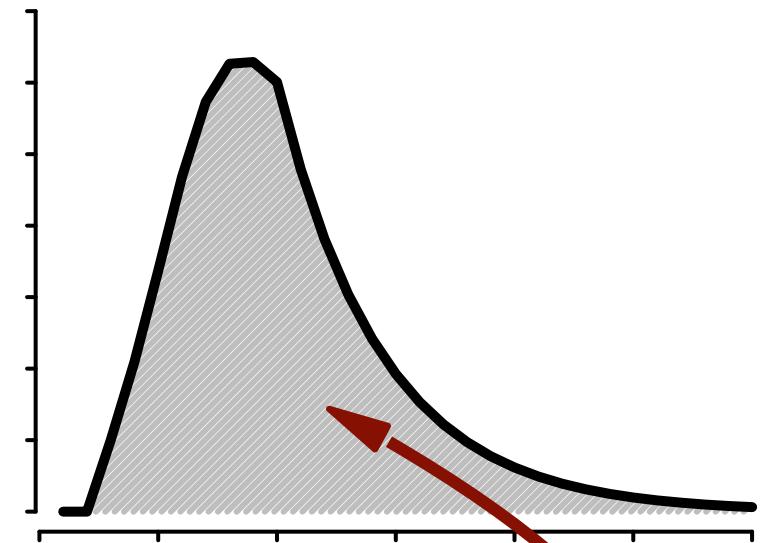
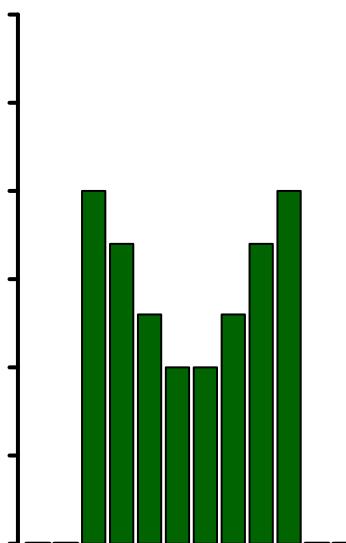
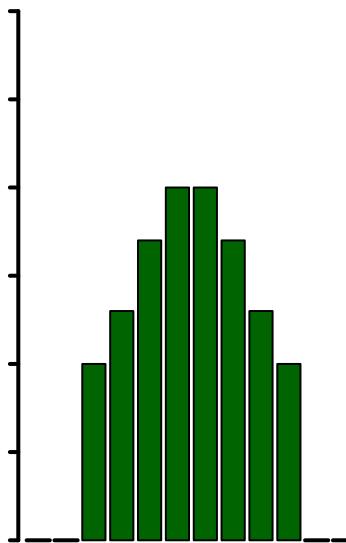


response



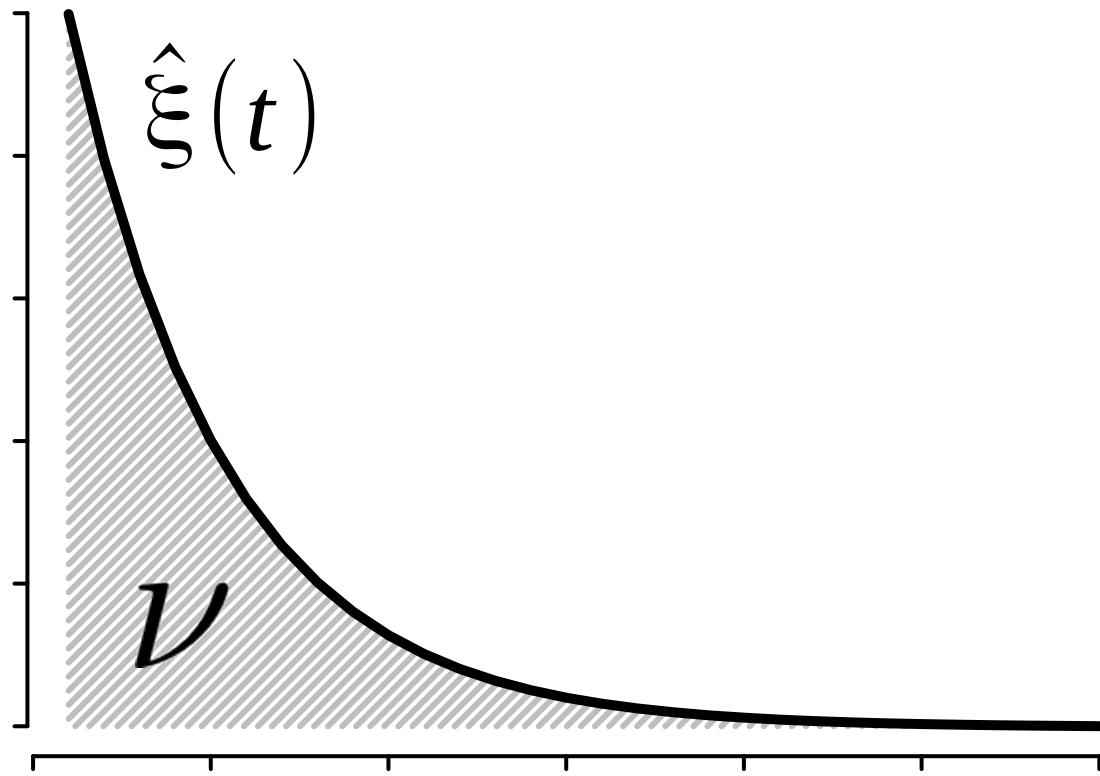
Corollary:

same
budget



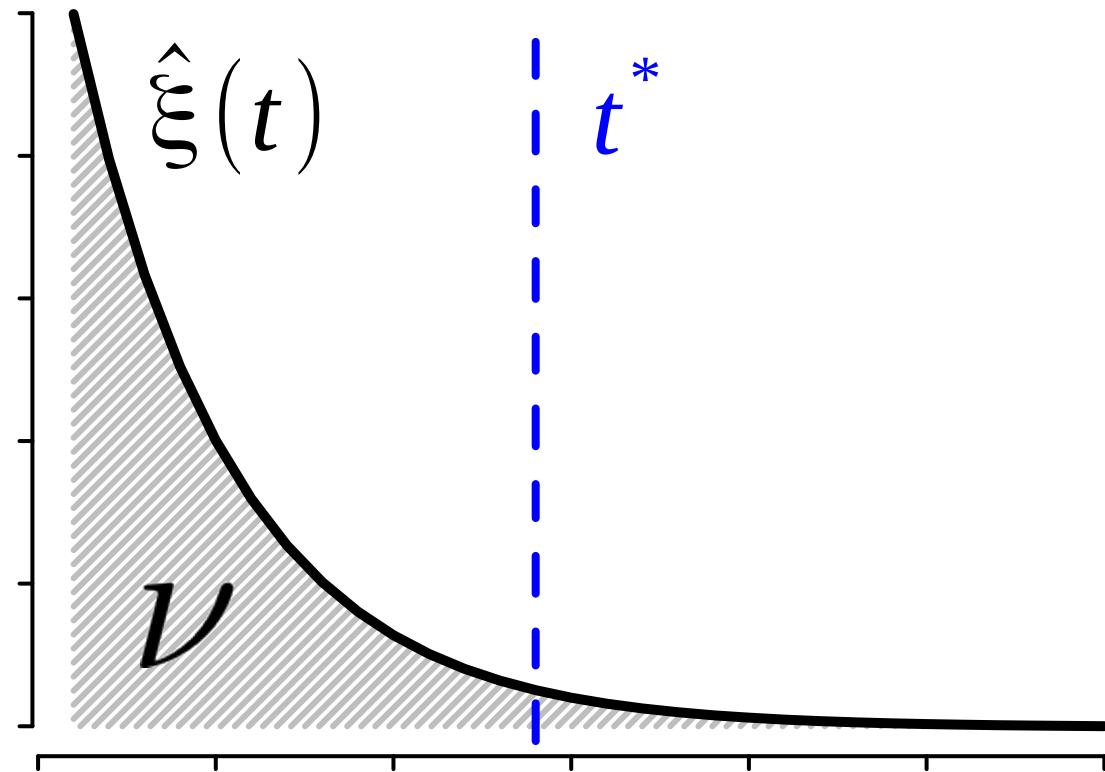
same
return

Viral potential and maturity time



Viral potential
score: $\nu = \int_0^\infty \mu \hat{\xi}(t) = \mu A_{\hat{\xi}}$

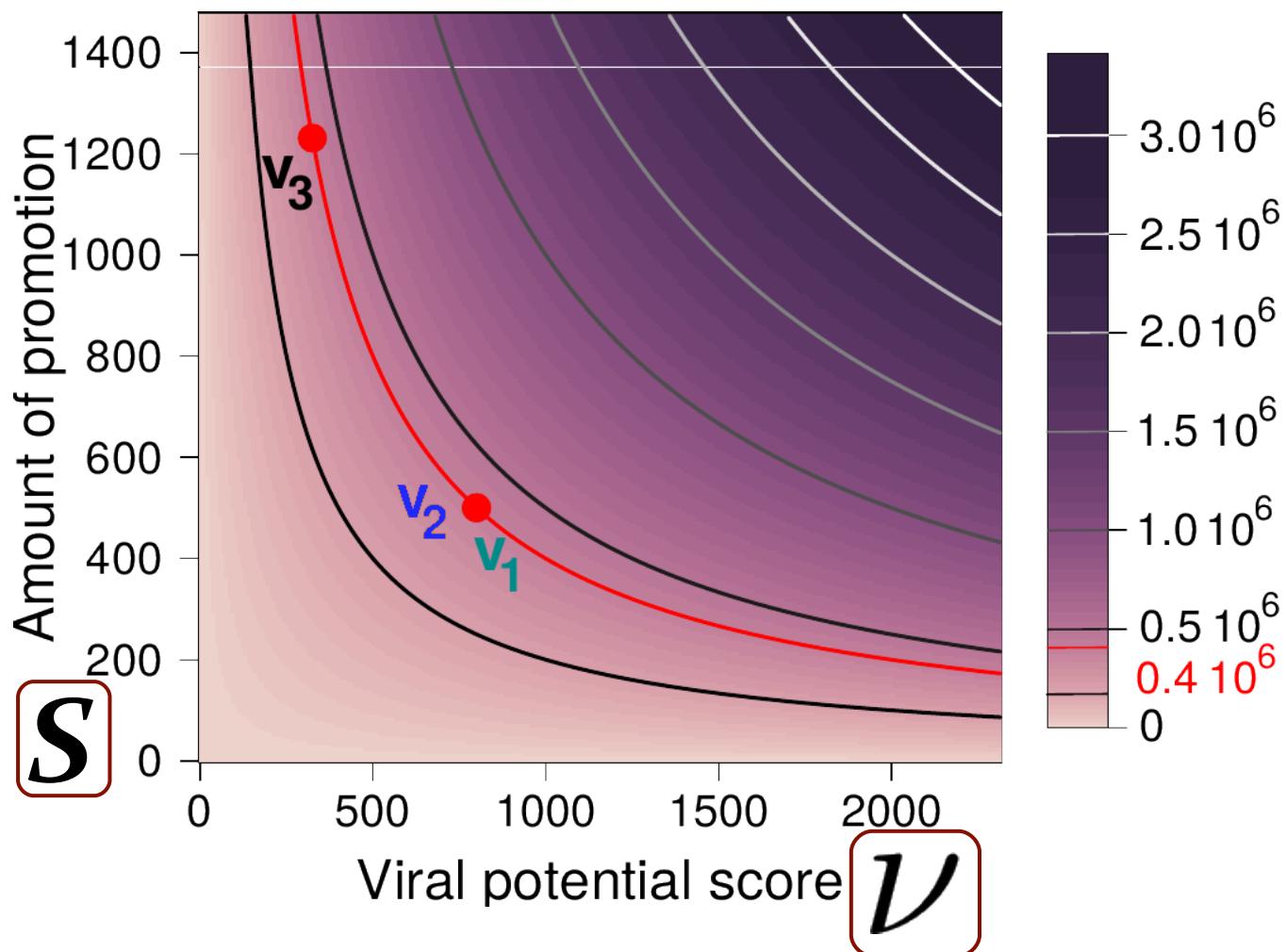
Viral potential and maturity time



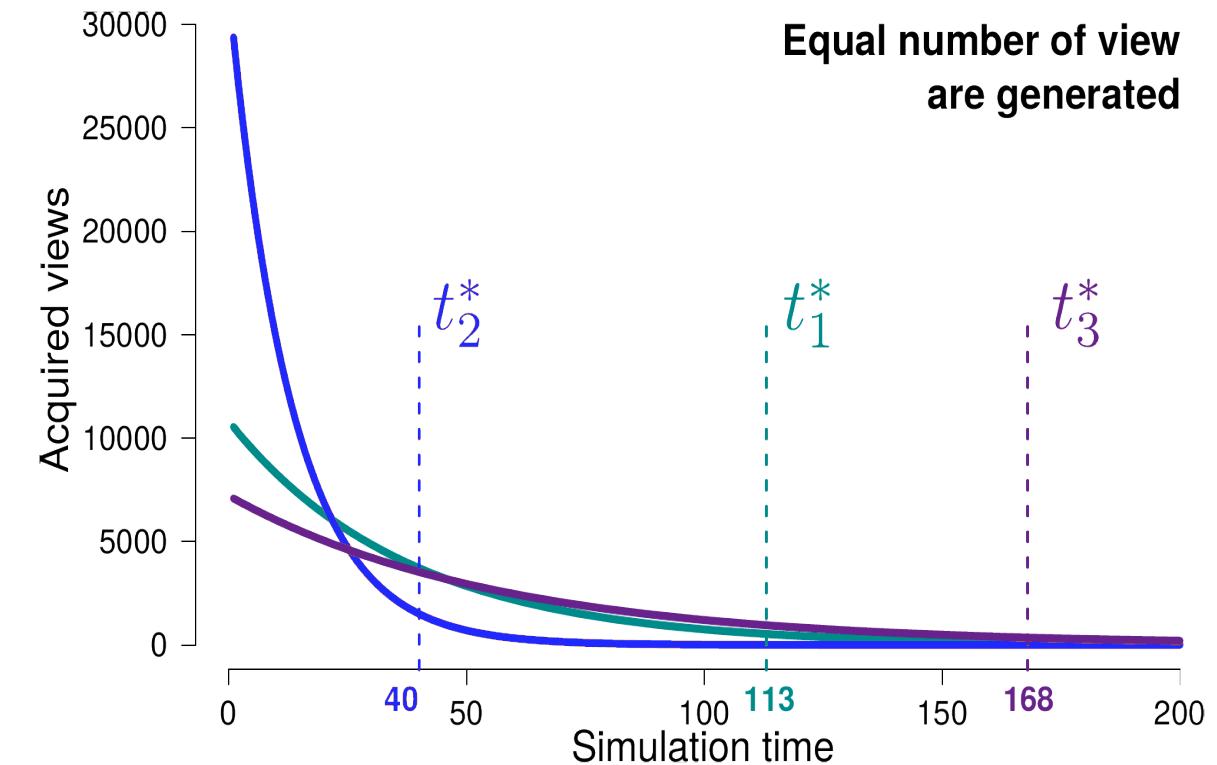
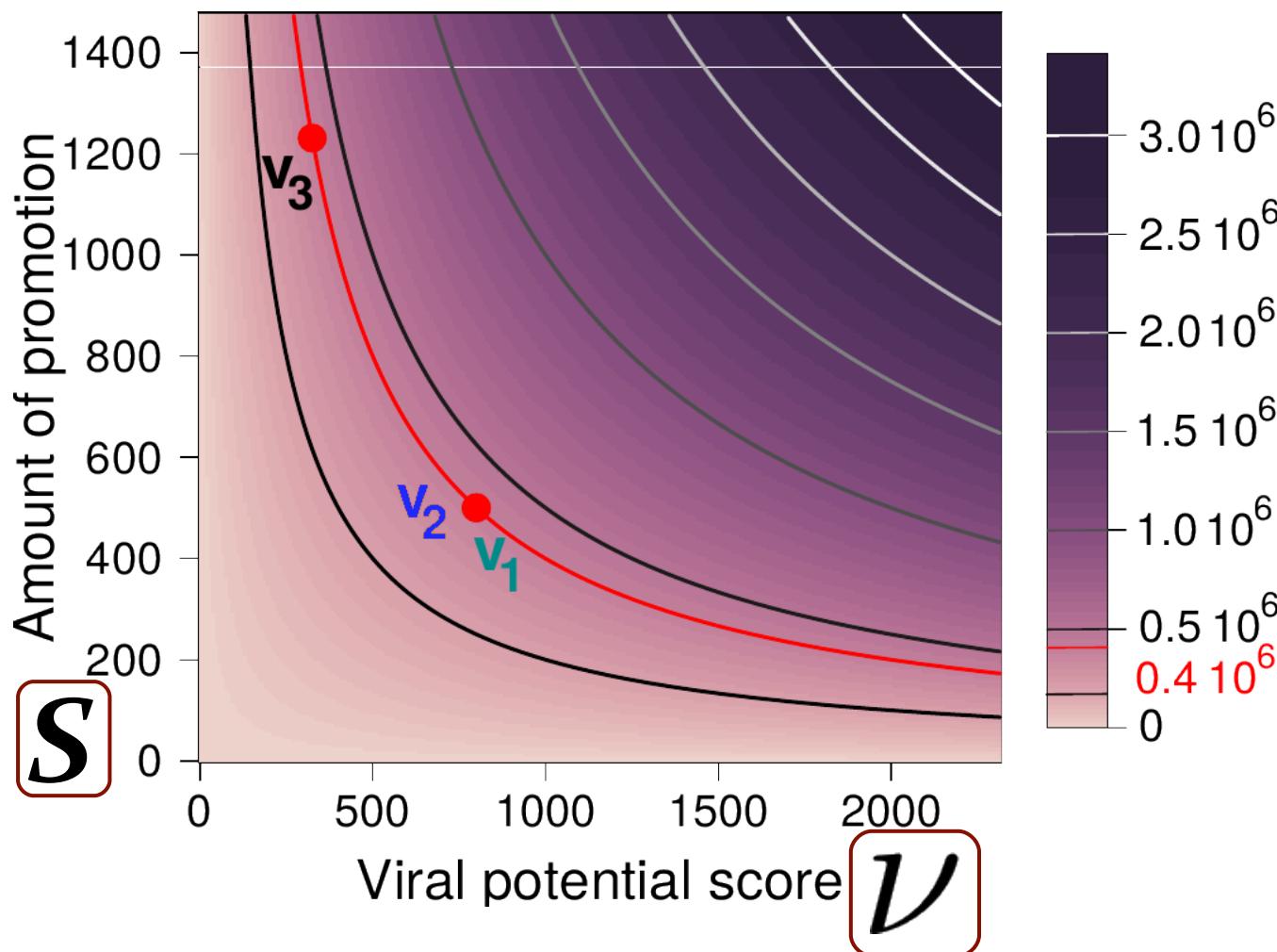
Viral potential score: $\nu = \int_0^\infty \mu \hat{\xi}(t) dt = \mu A_{\hat{\xi}}$

Maturity time: $t^* = \min \left\{ t \geq 0 \mid \int_0^t \hat{\xi}(s) ds \geq 0.95\nu \right\}$

Virality map



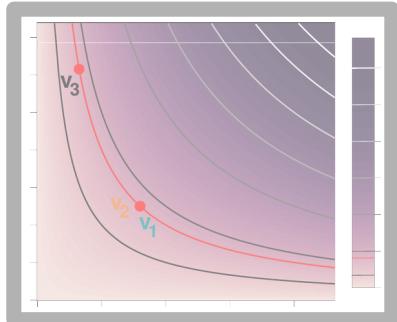
Virality map



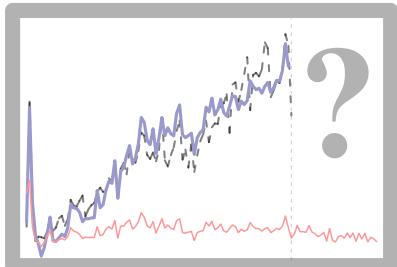
Presentation outline



Modeling popularity with HIP



Content virality and maturity time



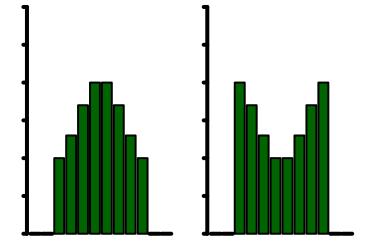
Forecasting popularity under promotion



When does promotion timing matter?
Why do people prefer constant promotion?

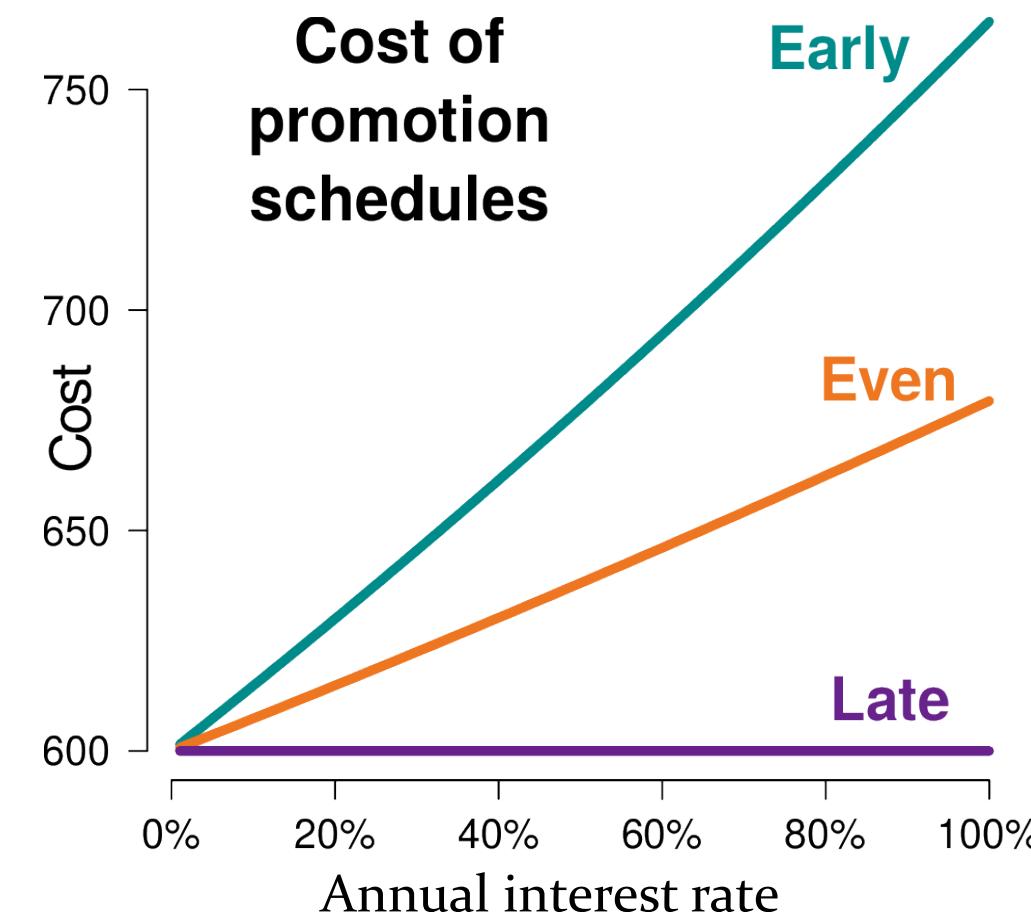
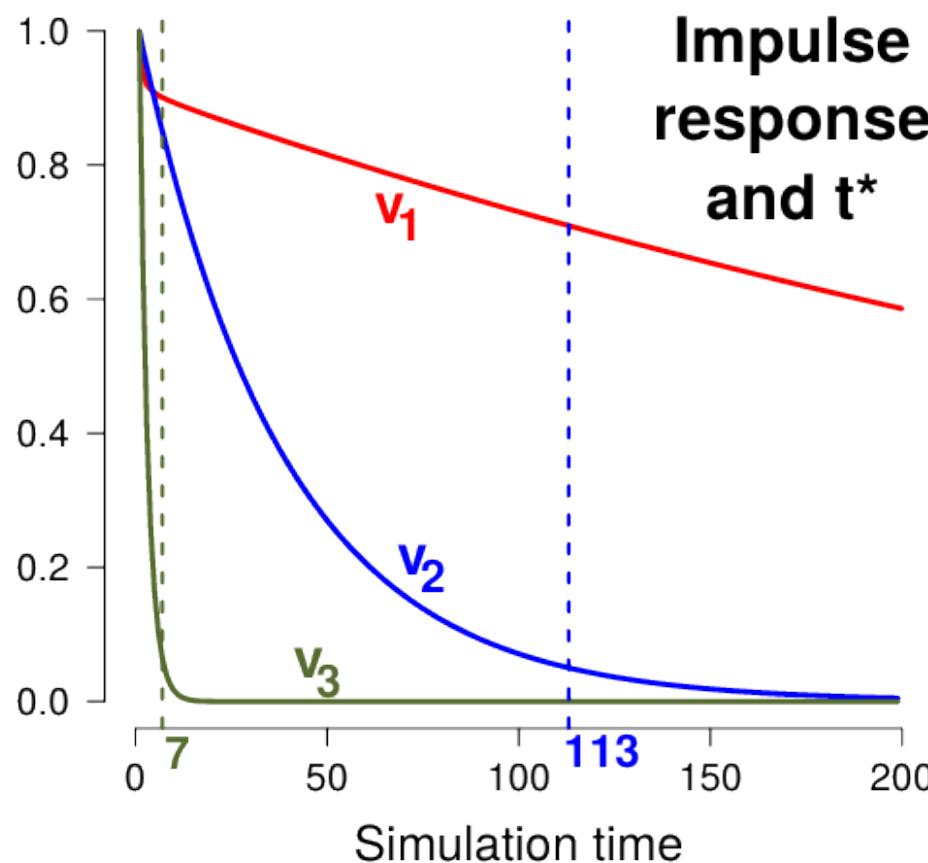
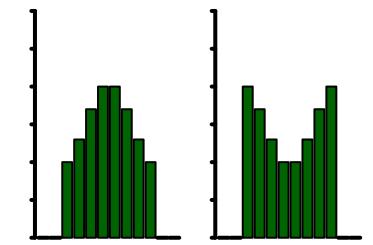
Designing promotion schedules

LTI corollary: **same budget, same return!**

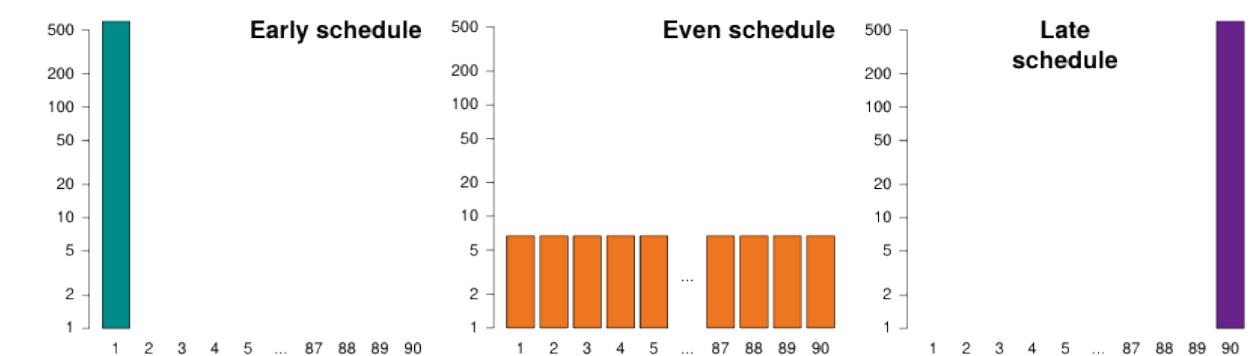


Designing promotion schedules

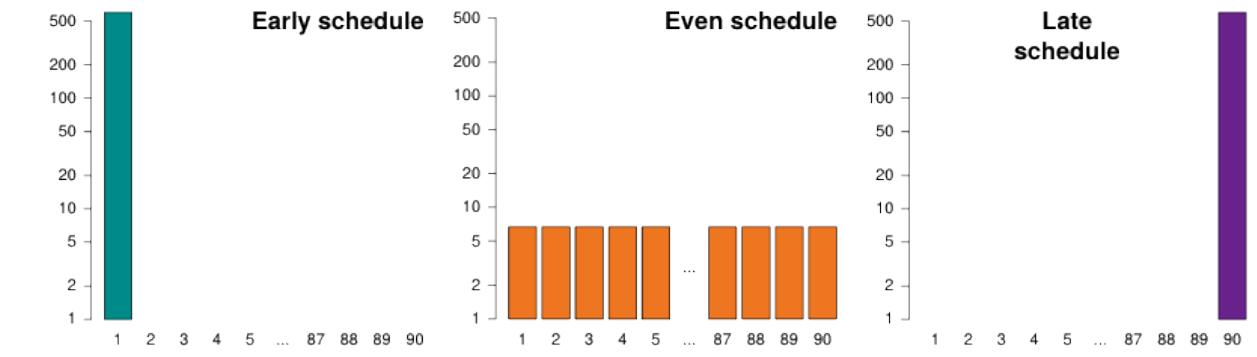
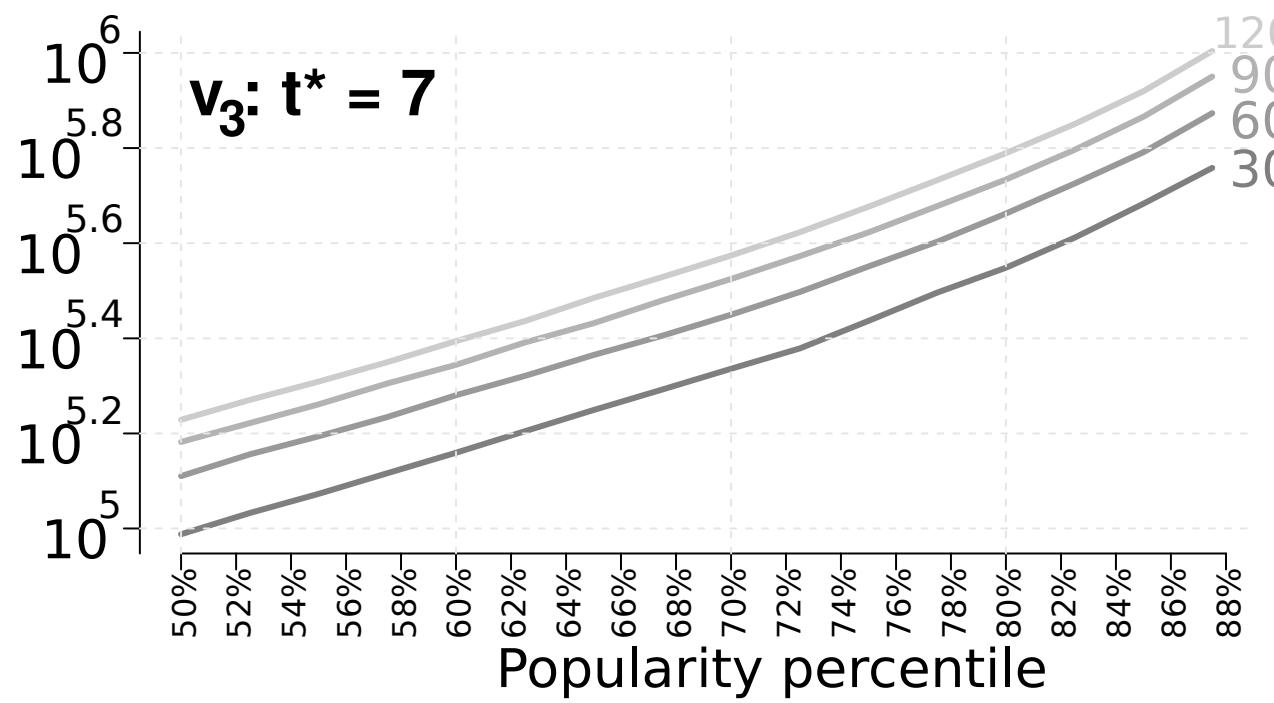
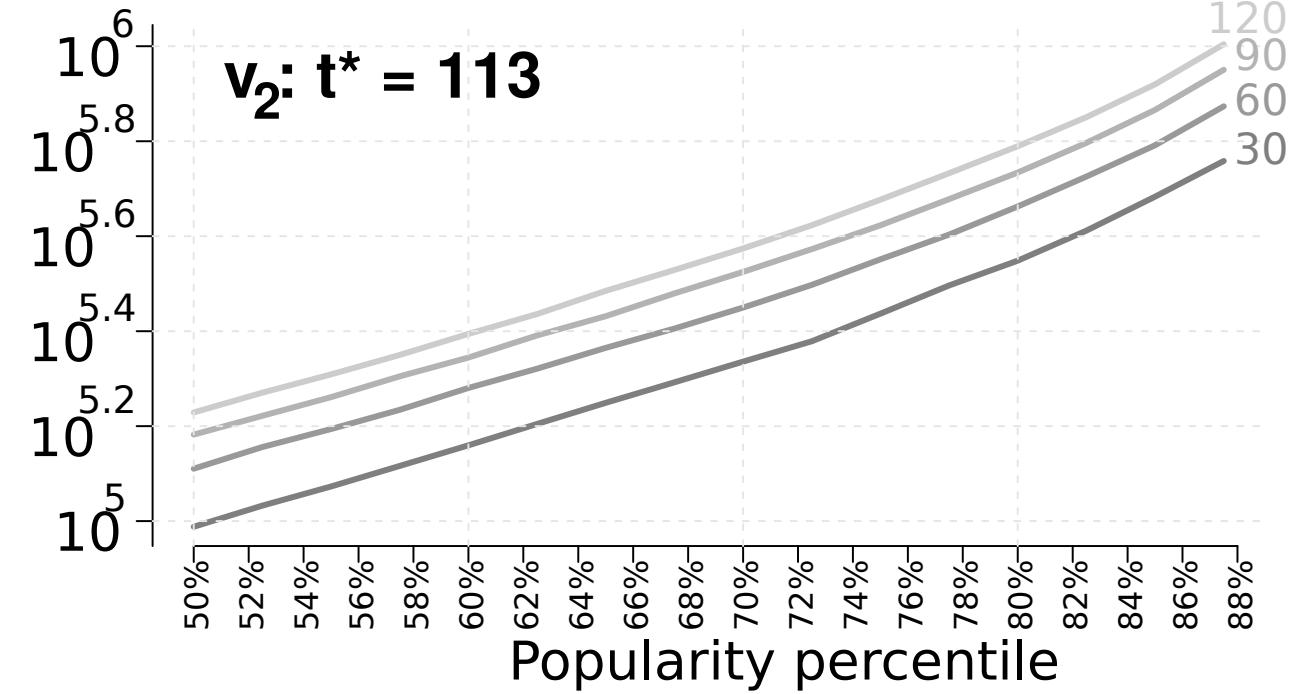
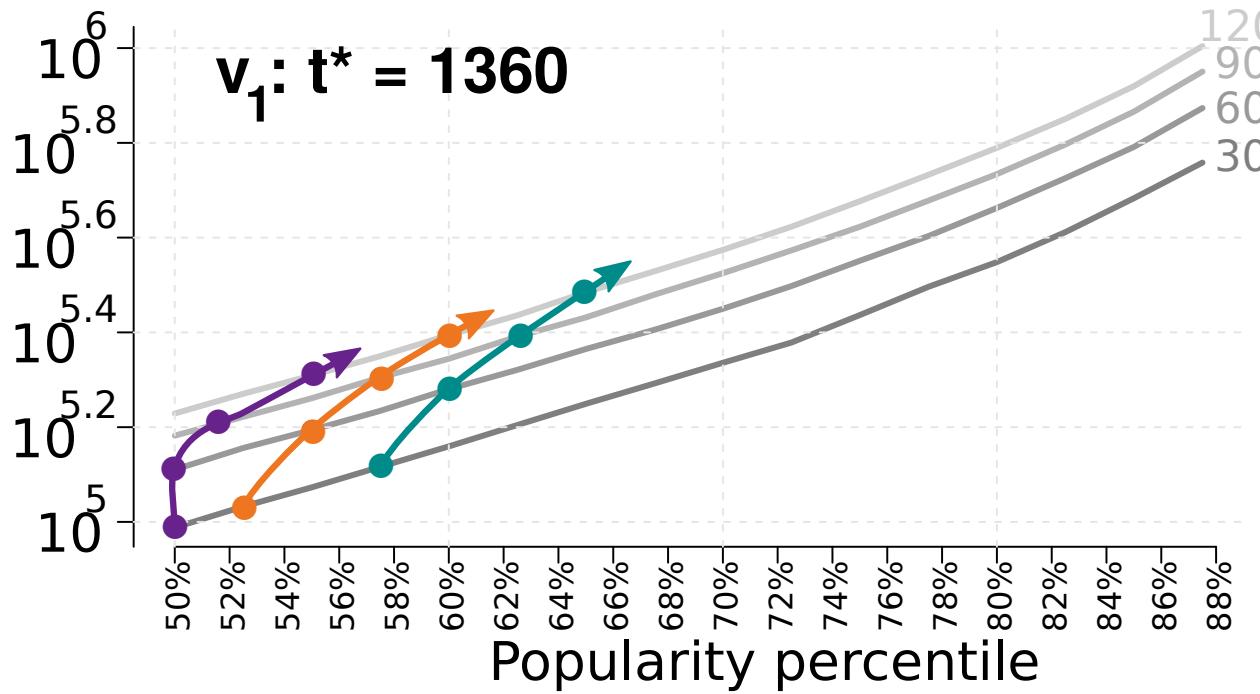
LTI corollary: same budget, same return!



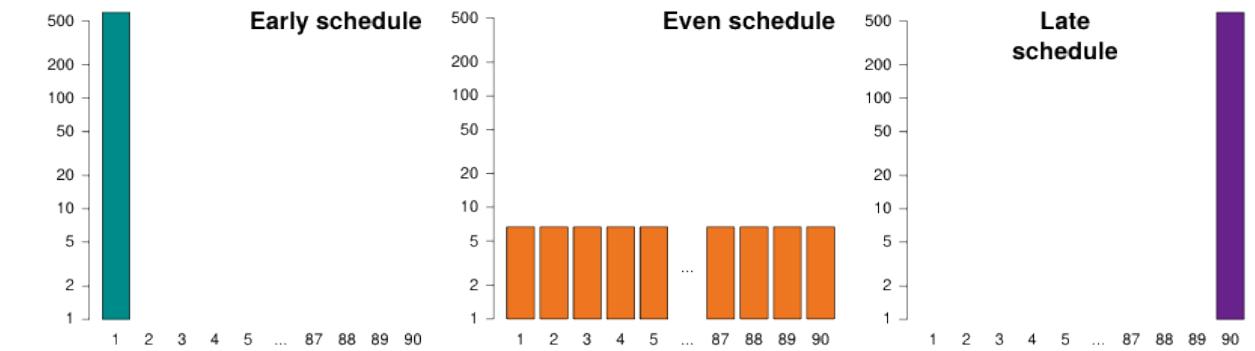
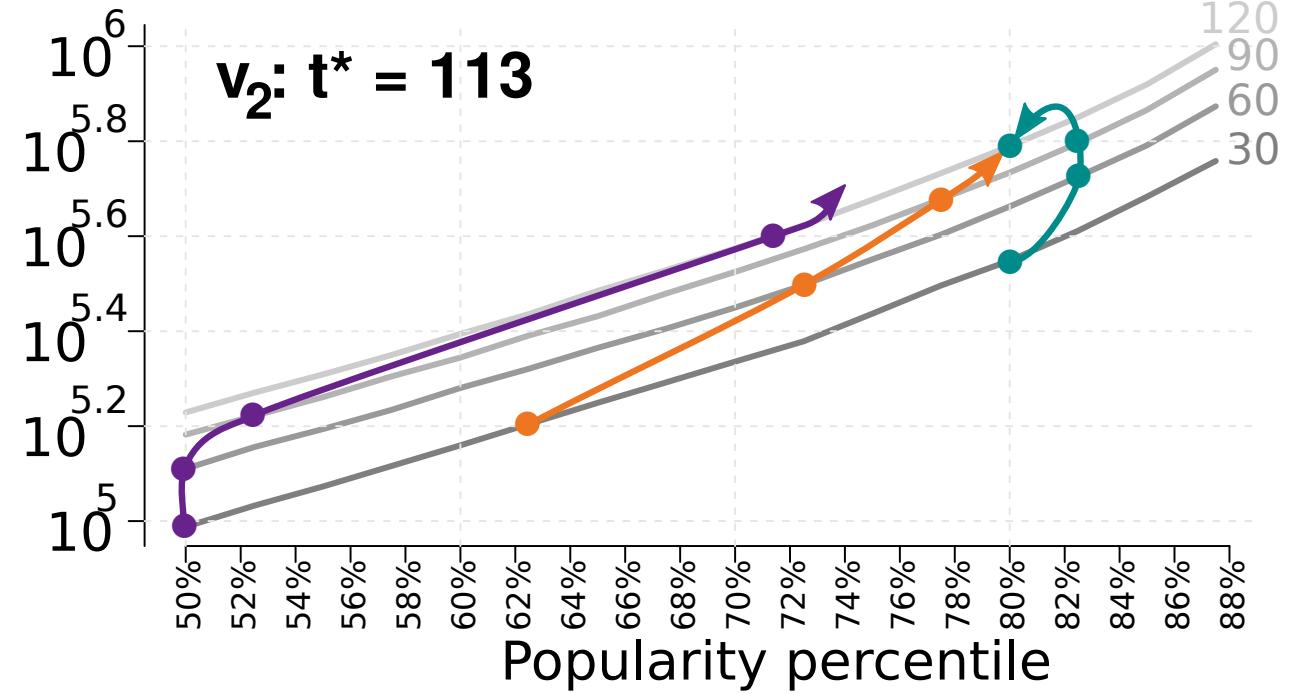
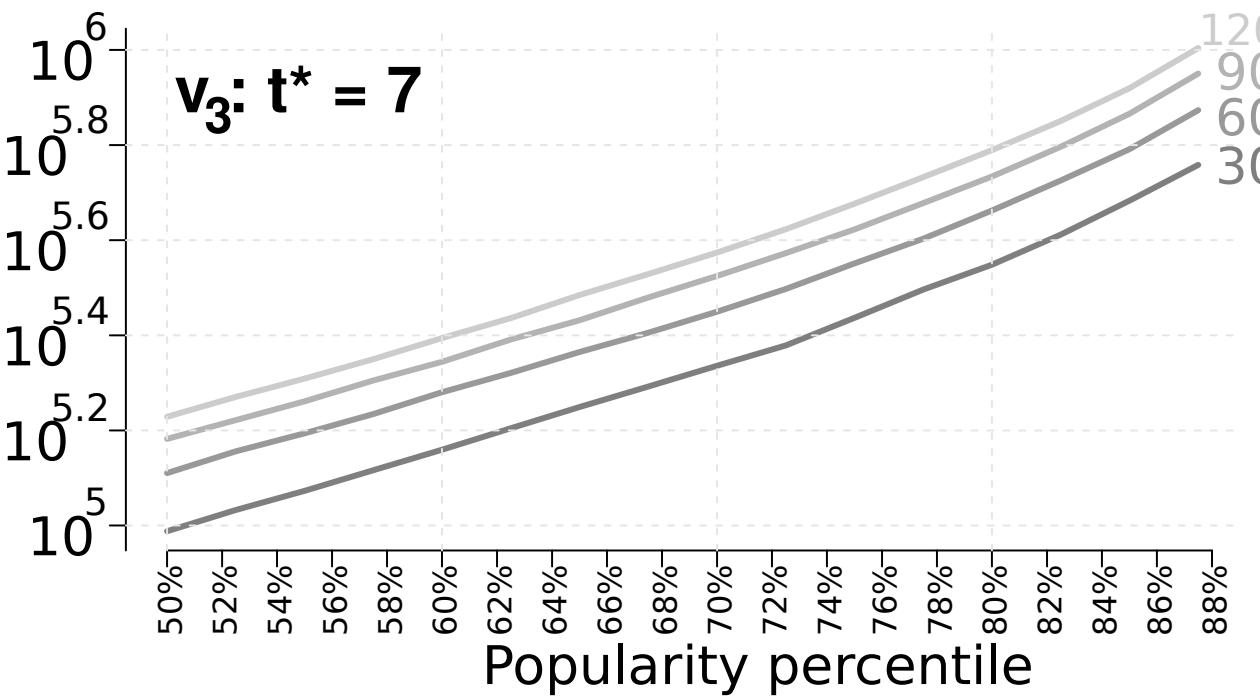
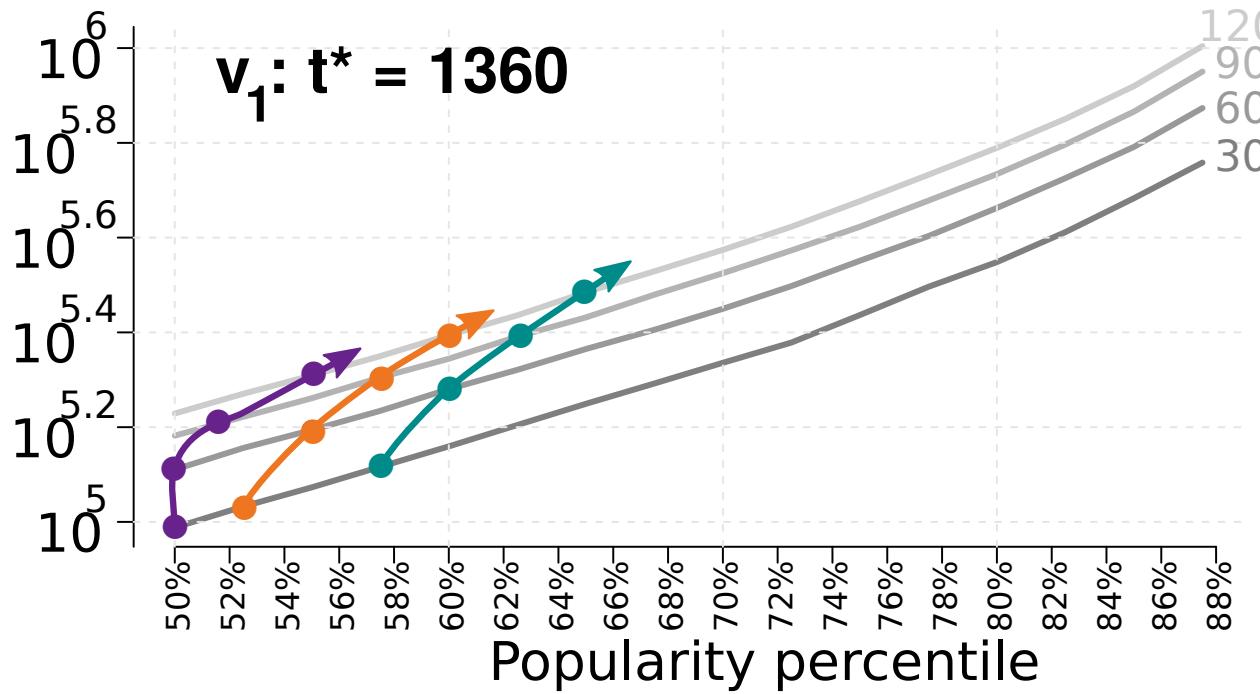
Compounding interest: $cost = (1+a)^k$



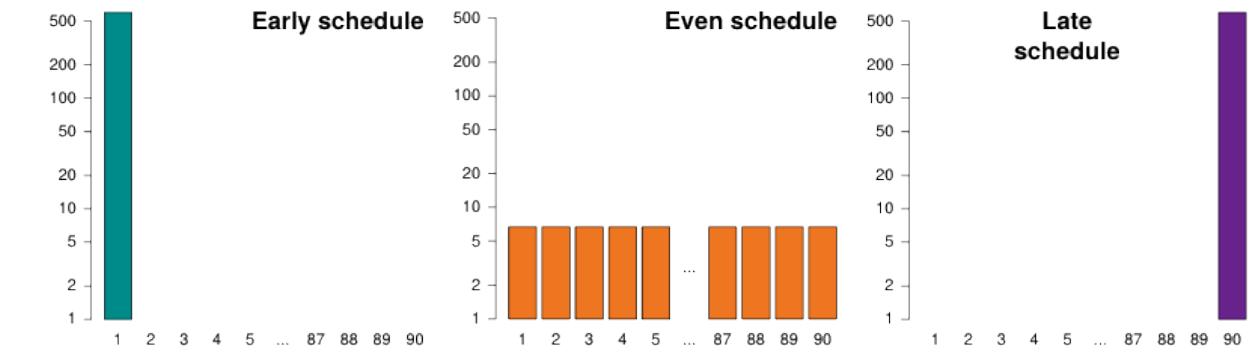
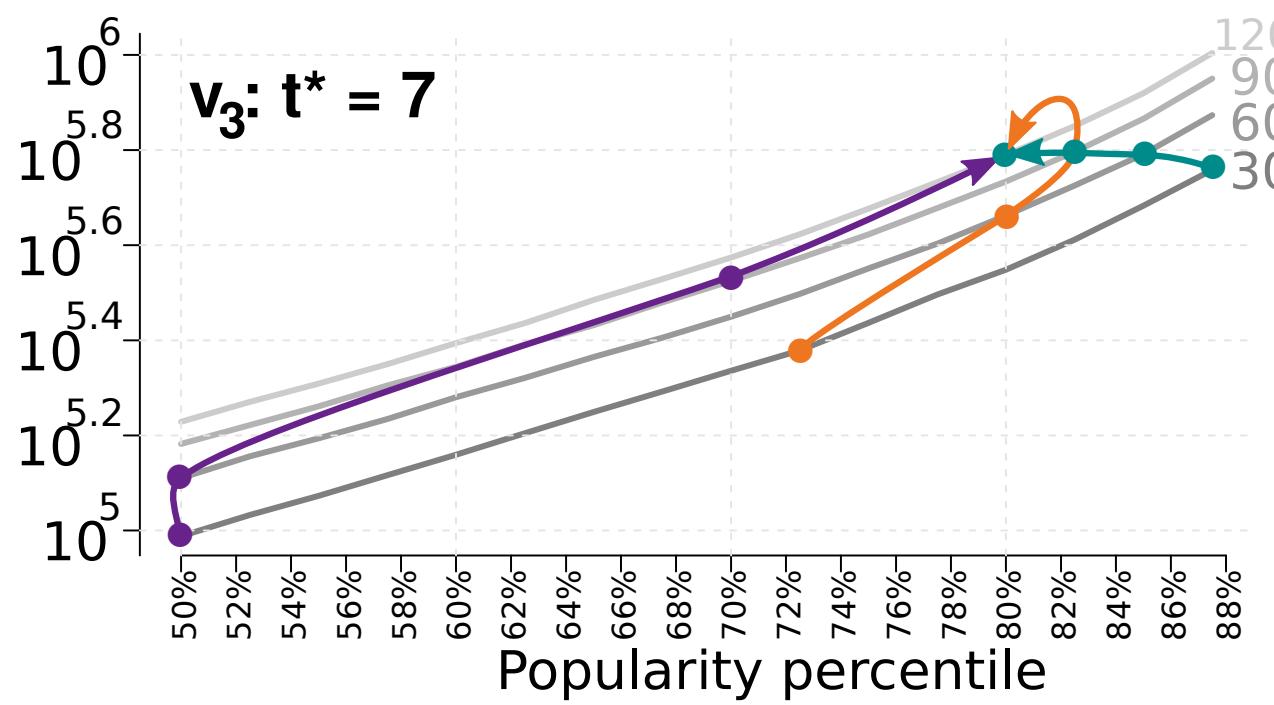
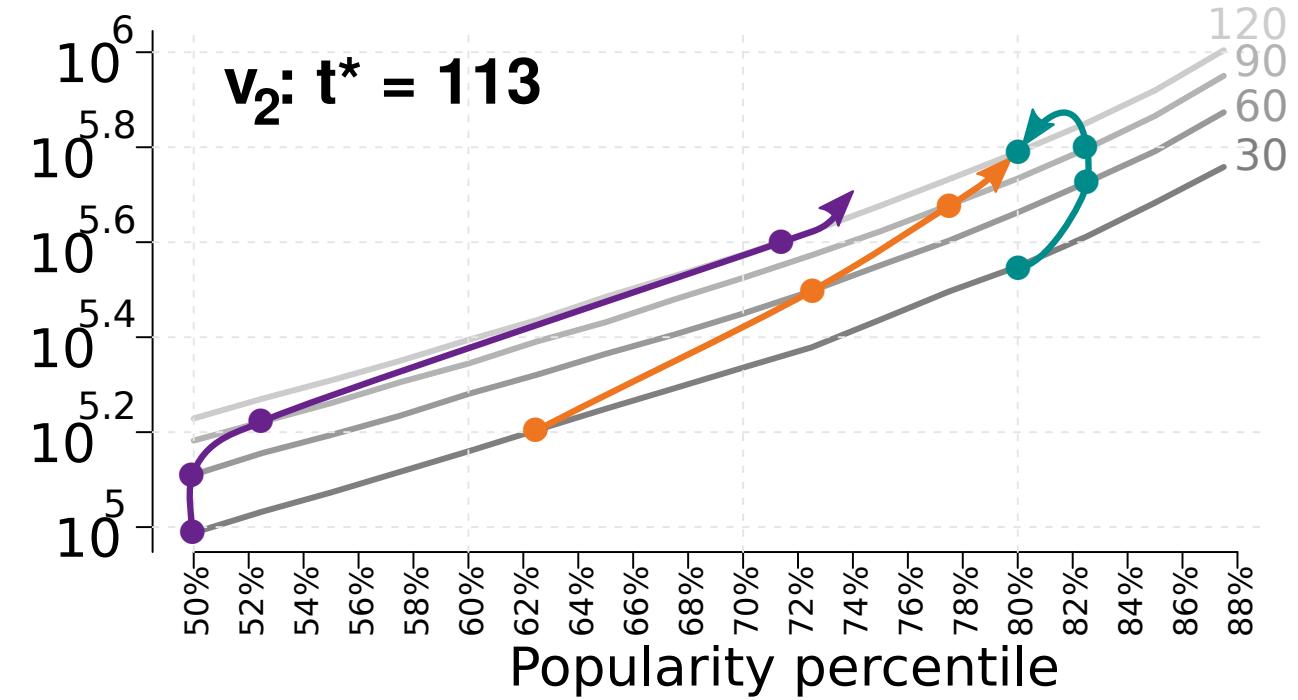
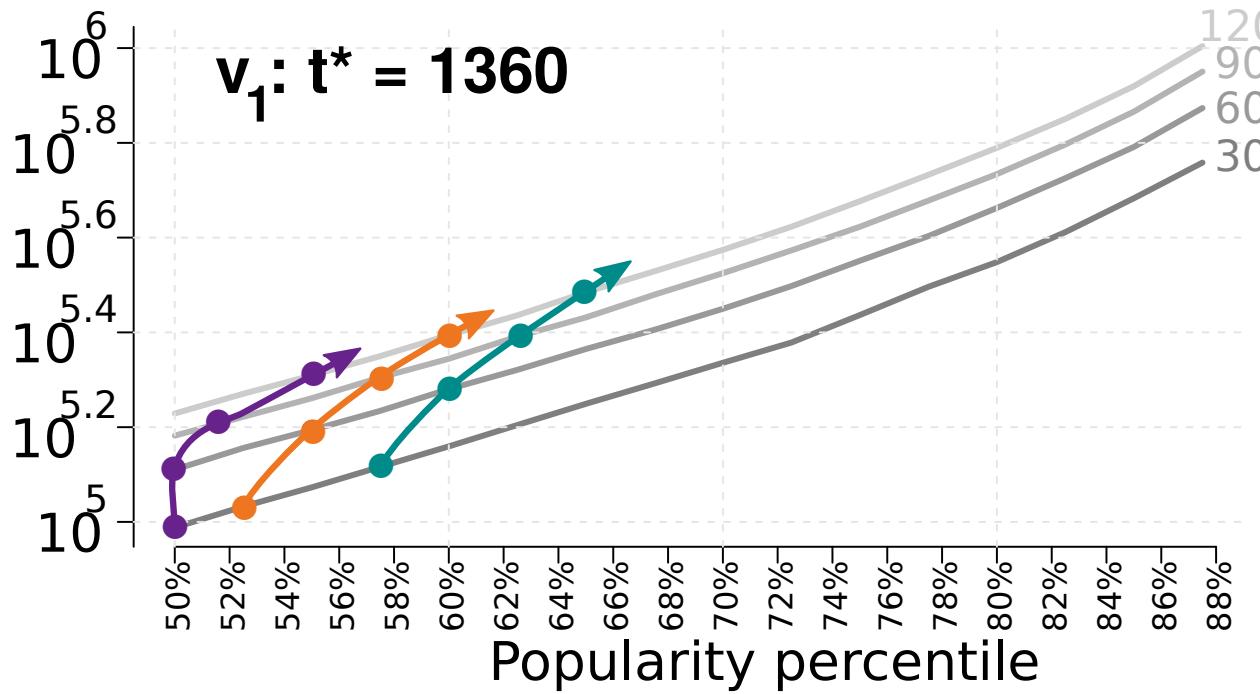
Interplay of 2 temporal factors



Interplay of 2 temporal factors



Interplay of 2 temporal factors



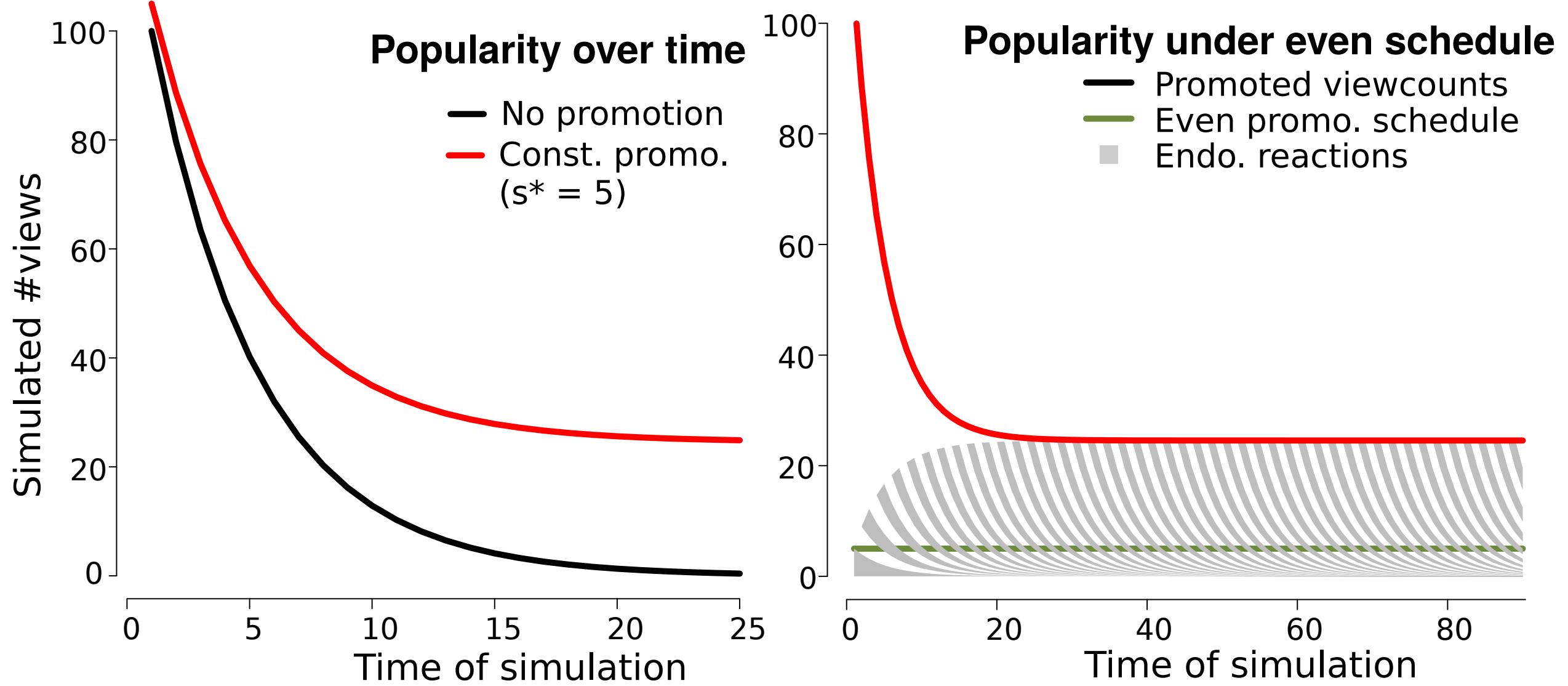
Why is constant promotion desirable?

LTI corollary: the effects of daily promotion add up over time!

Explains why TV commercials appear at fixed intervals, every day.



Memory lengthening through promotion



Constant promotion leads to an apparent
memory lengthening.

Prior work and gaps

1) Modeling popularity

power-law shapes [Crane & Sornette PNAS'08]

power-law decays with periodicity [Matsubara et al KDD'12]

collection of recurrence peaks [Cheng et al WWW'16]

How would popularity evolve under continuous external influence?

2) Explaining virality

diffusion history [Cheng et al WWW'14]

positive sentiment [Bakshy et al WSDM'11]

Can something go viral if promoted?

3) Predicting future popularity

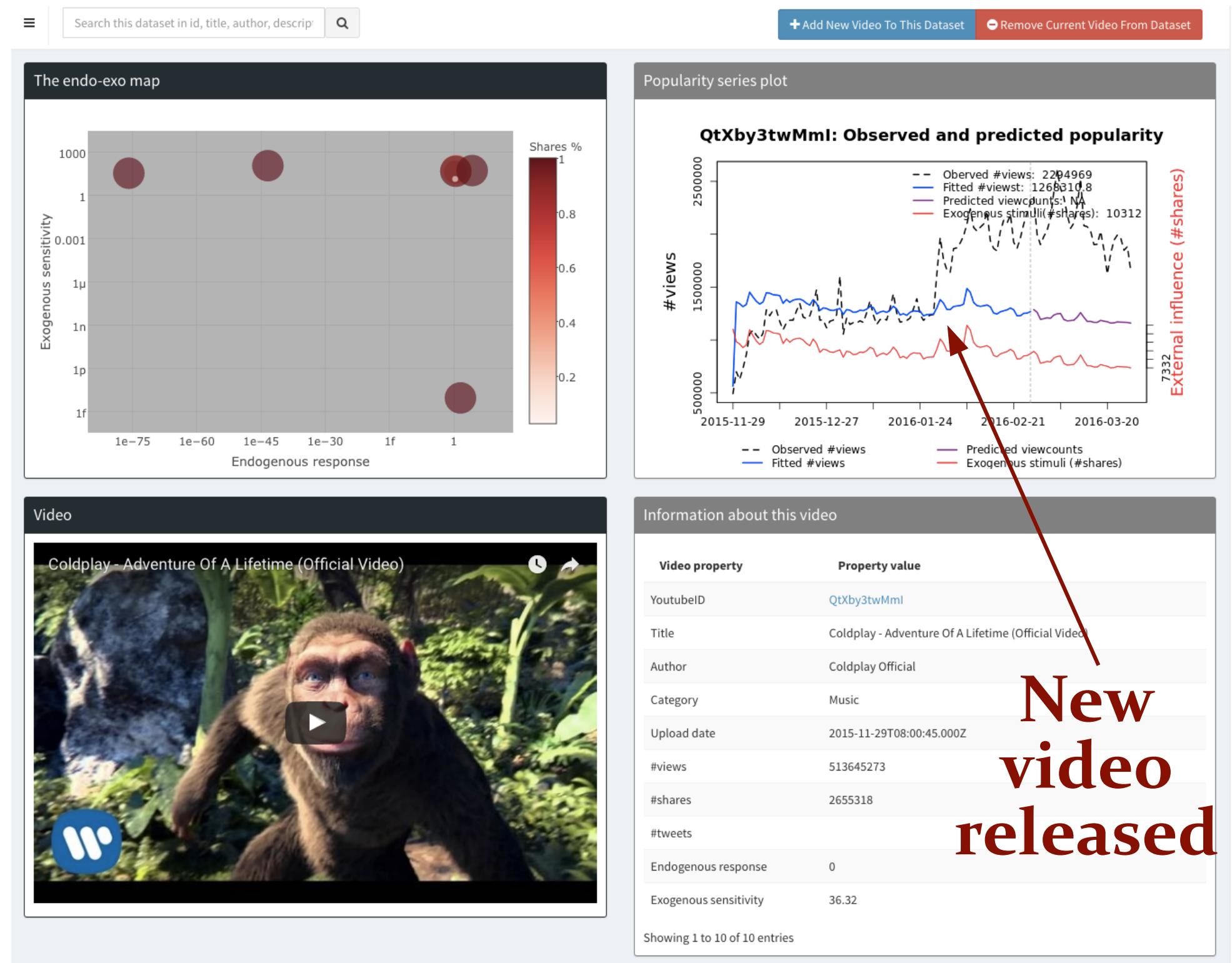
popularity history [Pinto et al WSDM'13] [Szabo and Huberman Comm.ACM 10]

timing features [Cheng et al WWW'14]

How to forecast future popularity given planned promotions?

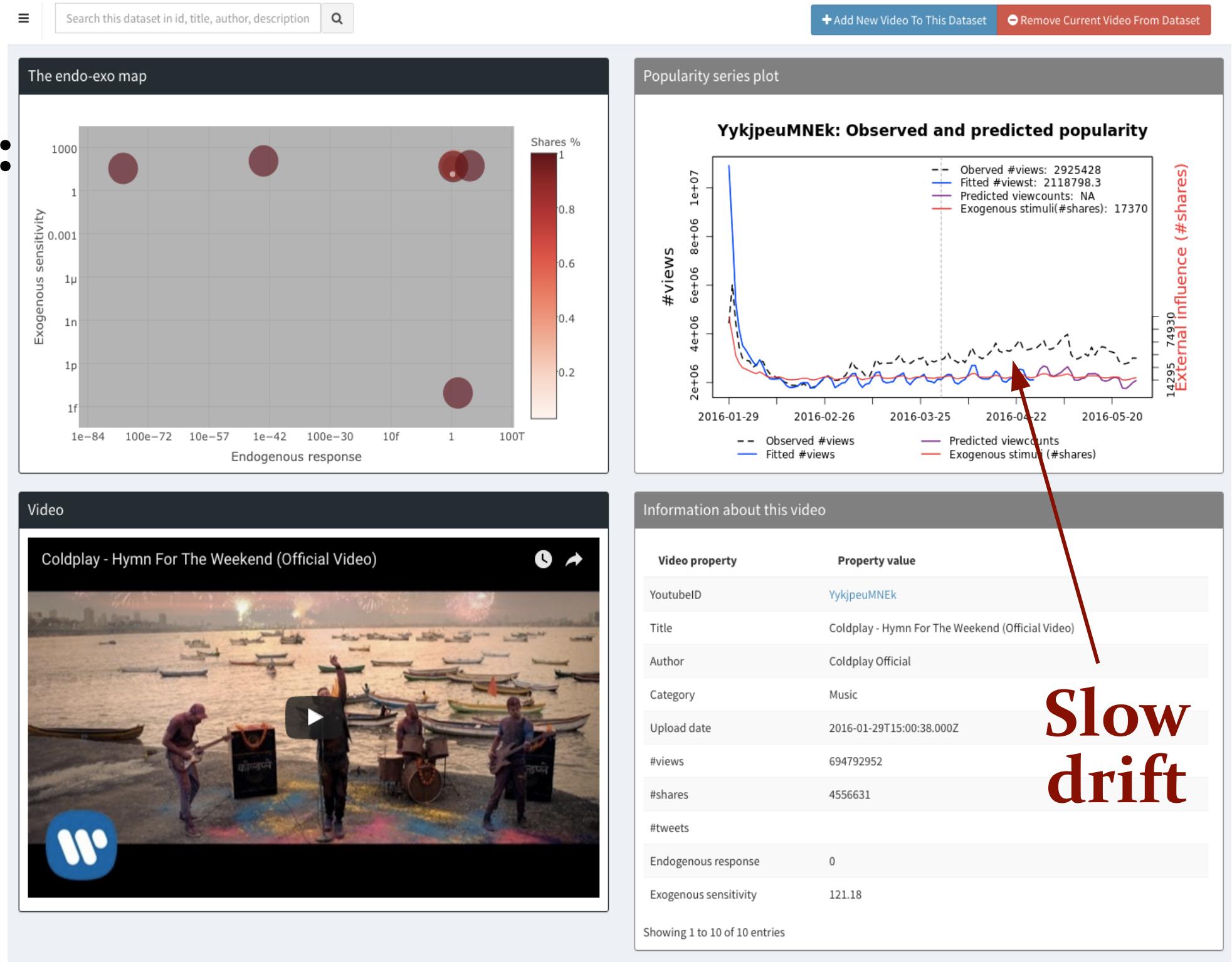
Supp: when HIP fails the fitting (1)

Relations
between
videos:

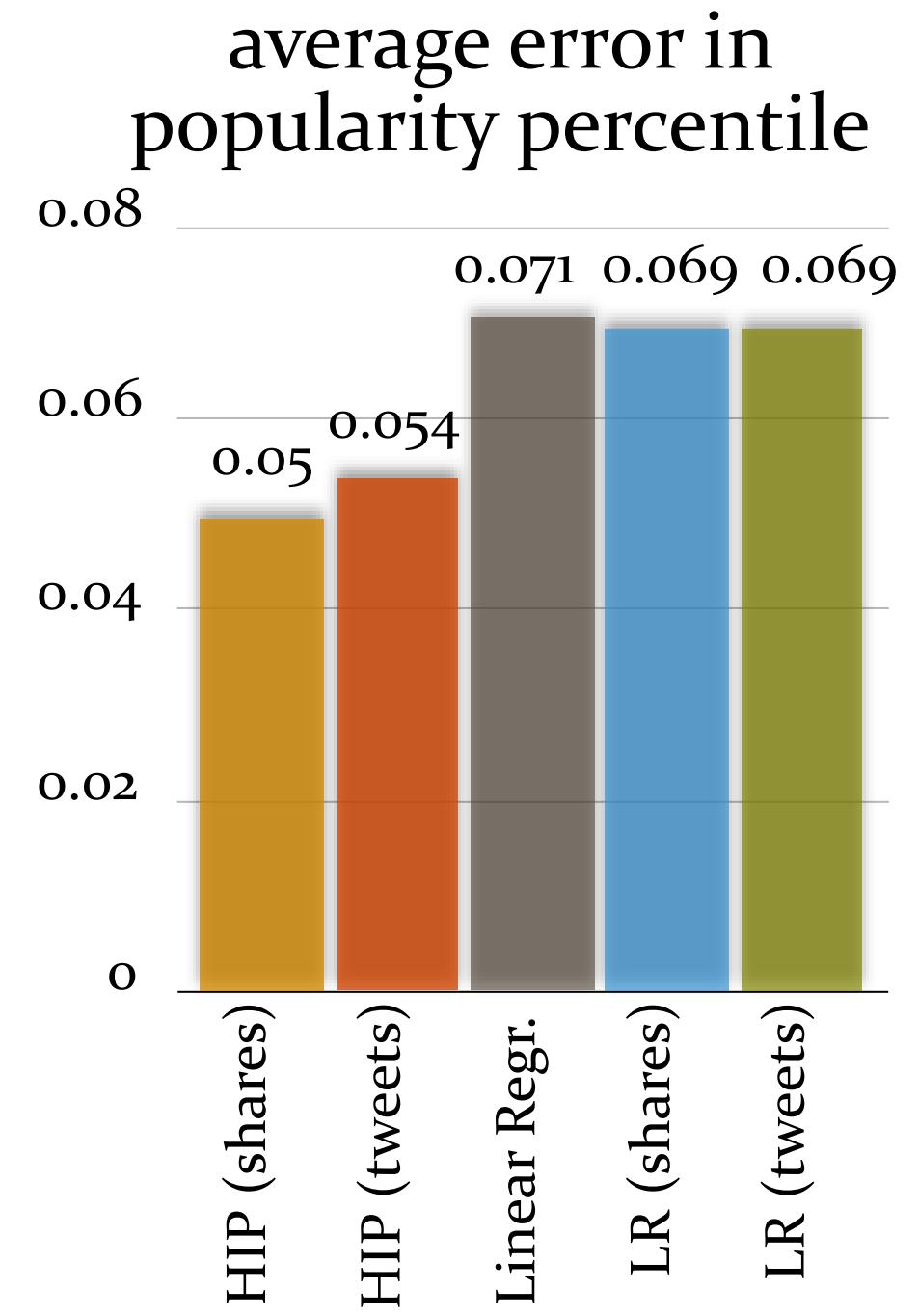
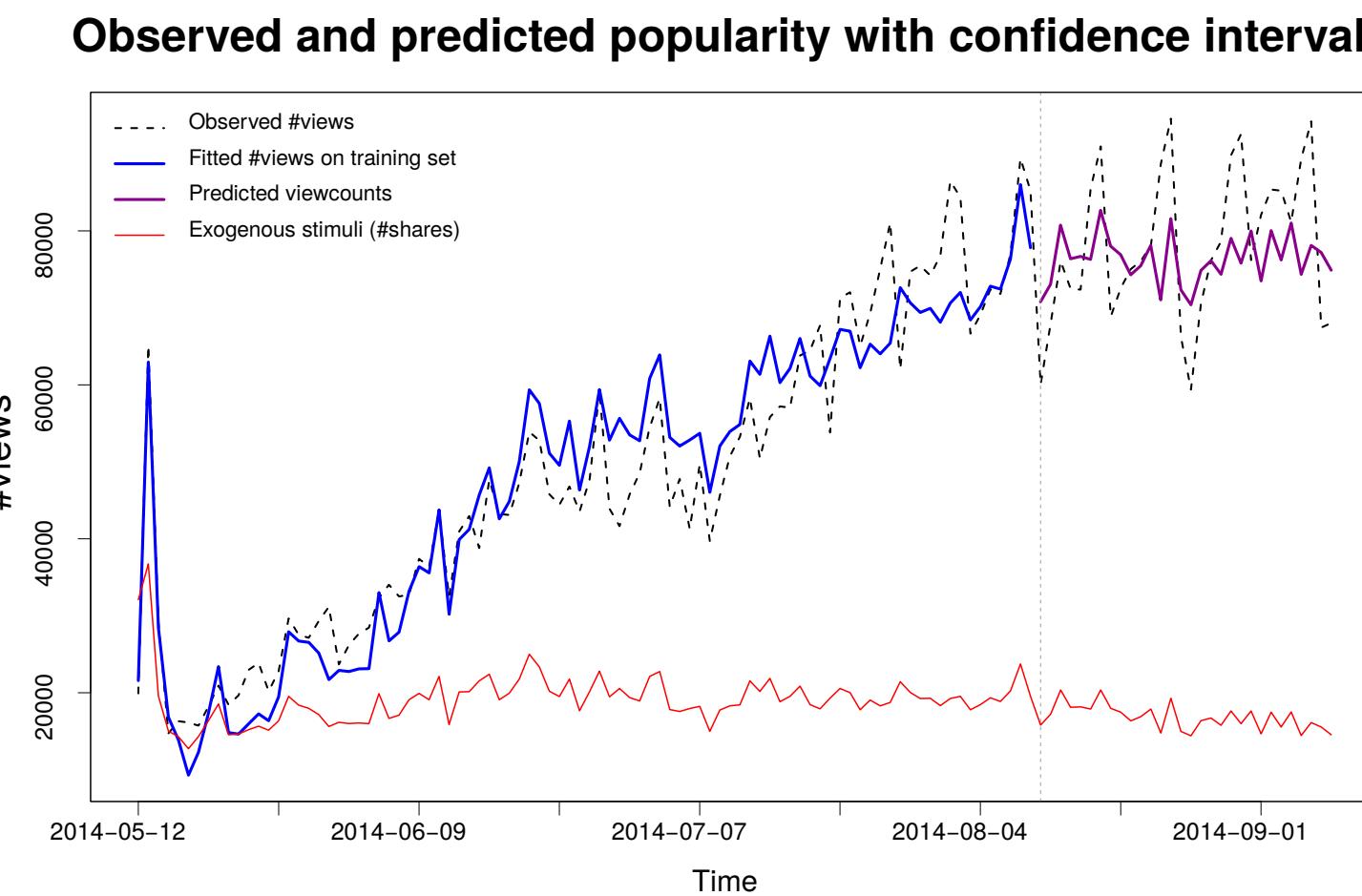


Supp: when HIP fails the fitting (2)

Long term evolutions:



Forecasting the effect of promotions



[Szabo & Huberman Comm. ACM'13] [Yu et al ICWSM'15]

[Pinto et al WSDM'13]