## Programming Paradigms

#### Lecture 7

Slides are from Prof. Chin Wei-Ngan from NUS

Types, ADT, Components

#### Reminder of Last Lecture

- Tupled Recursion
- Exceptions

#### Overview

- Types
- Abstract Data Types
- Haskell
- Design Methodology

## Dynamic Typing

- Oz/Scheme uses dynamic typing, while Java uses static typing.
- In dynamic typing, each value can be of arbitrary types that is only checked at runtime.
- Advantage of dynamic types
  - no need to declare data types in advance
  - more flexible
- Disadvantage
  - errors detected late at runtime
  - less readable code

## Type Notation

Every value has a type which can be captured by:

```
e :: type
```

- Type information helps program development/documentation
- Many functions are designed based on the type of the input arguments

## List Type

- Based on the type hierarchy
  - □ (Value), (Record),...
  - □ ⟨Record⟩ ⊂ ⟨Value⟩
    - The Record type is a subtype of the Value type
  - List is either nil or X | Xr where xr is a list and x is an arbitrary value
  - □ ⟨List⟩ ::= nil | ⟨Value⟩' | '⟨List⟩

## Polymorphic List

- Usually all elements of the same type
- Polymorphic list with elements of T type \(\langle \text{List T} \rangle ::= \text{nil} \ \langle \text{T} \rangle' \rangle' \text{List T} \rangle
  - T is a type variable
  - □ (List ?) is a type constructor
  - □ ⟨List ⟨Int⟩⟩ : a list whose elements are integers
  - □ ⟨List ⟨Value⟩⟩ is equal to ⟨List⟩

#### Polymorphic Binary Tree

Binary trees

- Binary tree representing a dictionary mapping keys to values
- Binary tree is:
  - either a leaf (atom leaf), or
  - an internal node with label tree, with left and right subtrees, a key and a value
- Key is of literal type and the value is of type T

#### Types for procedures and functions

The type of a procedure where T<sub>1</sub> ... T<sub>n</sub> are the types of its arguments can be represented by:

```
\langle \text{proc } \{\$ \ T_1 \ ... \ T_n \} \rangle

or

\{T_1 \ ... \ T_n\} \longrightarrow ()
```

## On Types: procedures and functions

The type of a function where T<sub>1</sub> ... T<sub>n</sub> are the types of the arguments, and T is the type of the result is:

```
\langle \text{fun } \{ \$ \ T_1 \ ... \ T_n \} \ \vdots \ T \rangle
\{ T_1 \ ... \ T_n \} \ \longrightarrow \ T
```

or

Append ::{⟨List⟩ ⟨List⟩} →⟨List⟩
or precisely ::{⟨List A⟩ ⟨List A⟩} →⟨List A⟩

- Programs that takes lists has a form that corresponds to the list type
- Code should also follow type, e.g:

```
case Xs of
   nil then (expr1) % base case
[] X|Xr then (expr2) % recursive call
end
```

- Helpful when the type gets complicated
- Nested lists are lists whose elements can be lists
- Exercise: "Find the number of elements of a nested list"

```
Xs = [[1 2] 4 nil [[5] 10]]
{Length Xs} = 5
```

```
declare
Xs1=[[1 2] 4 nil]
{Browse Xs1} → [[1 2] 4 nil]
Xs2=[[1 2] 4]|nil
{Browse Xs2} → [[[1 2] 4]]
```

- Nested lists type declaration

#### General structure:

```
case Xs
  of nil then \( \) expr1 \( \) \( \) base case
[] X|Xr andthen \( \) IsList X\( \) then
  \( \) \( \) recursive calls for X and Xr
[] X|Xr then
  \( \) \( \) recursive call for Xr
end
```

```
Length :: \{\langle NList T \rangle\} \rightarrow \langle Int \rangle
  fun {Length Xs}
      case Xs
      of nil then 0 % base case
       [] X|Xr andthen {IsList X} then
              {Length X} + {Length Xr}
       [] X|Xr then
             1+{Length Xr}
      end
  end
fun {IsList L}
      L == nil orelse
       \{Label L\} == ' \mid ' and then \{Width L\} == 2
  end
```

## Summary so far

- Type Notation
- Polymorphic Types
- Function types
- Constructing programs from type

# Abstract Data Types

#### Data Types

- Data type
  - set of values
  - operations on these values
- Primitive data types
  - records
  - numbers
  - **.**...
- Abstract data types
  - completely defined by its operations (interface)
  - implementation can be changed without changing use

#### Motivation

Sufficient to understand interface only

 Software components can be developed independently when they are used through interfaces.

 Developers need not know implementation details

#### Outlook

How to define abstract data types

How to organize abstract data types

How to use abstract data types

#### Abstract data types (ADTs)

- A type is abstract if it is completely defined by its set of operations/functionality.
- Possible to change the implementation of an ADT without changing its use
- ADT is described by a set of procedures
  - Including how to create a value of the ADT
- These operations are the only thing that a user of ADT can assume

#### Example: stack

- Assume we want to define a new data type (stack T) whose elements are of any type T
- We define the following operations (with type definitions)

```
⟨fun {NewStack}: ⟨stack T⟩⟩
⟨fun {Push ⟨stack T⟩ ⟨T⟩ }: ⟨stack T⟩⟩
⟨proc {Pop ⟨stack T⟩ ?⟨T⟩ ?⟨stack T⟩}⟩
⟨fun {IsEmpty ⟨stack T⟩}: ⟨Bool⟩⟩
```

## Example: stack (algebraic properties)

- Algebraic properties are logical relations between ADT's operations
- Operations normally satisfy certain laws (properties)
- { IsEmpty {NewStack}} = true
- For any stack S, {IsEmpty {Push S}} = false
- For any E and S, {Pop {Push S E} E S} holds
- For any stack S, {Pop {NewStack} S} raises error

#### stack (implementation I) using lists

```
fun {NewStack} nil end
fun {Push S E} E|S end
proc {Pop E|S ?E1 ?S1}
  E1 = E
  S1 = S
end
fun {IsEmpty S} S==nil end
```

## stack (implementation II) using tuples

```
fun {NewStack} emptyStack end
fun {Push S E} stack(E S) end
proc {Pop stack(E S) E1 S1}
  E1 = E
  S1 = S
end
fun {IsEmpty S} S==emptyStack end
```

#### Why is Stack Abstract?

 A program that uses the stack will work with either implementation (gives the same result)

```
declare Top S4
% ... either implementation
S1={NewStack}
S2={Push S1 2}
S3={Push S2 5}
{Pop S3 Top S4}
{Browse Top} → 5
```

#### What is a Dictionary?

- A dictionary is a finite mapping from a set of simple constants to a set of language entities.
- The constants are called keys because they provide a unique the path to each entity.
- We will use atoms or integers as constants.
- Goal: create the mapping dynamically, i.e., by adding new keys during the execution.

#### Example: Dictionaries

Designing the interface of Dictionary

```
MakeDict :: \{\} \rightarrow Dict
    returns new dictionary
DictMember :: {Dict Feature} \rightarrow Bool
    tests whether feature is member of dictionary
DictAccess :: {Dict Feature} → Value
    return value of feature in Dict
DictAdjoin :: {Dict Feature Value} \rightarrow Dict
    return adjoined dictionary with value at feature
```

Interface depends on purpose, could be richer.

## Implementing the Dict ADT

- Two possible implementations are
  - based on pairlists
  - based on records
- Regardless of implementation, programs using the ADT should work!
  - the interface is a contract between use and implementation

#### Dict: List of Pairs

```
fun {MakeDict}
   nil
end
fun {DictMember D F}
   case D of nil then false
       [] G#X|Dr then if G==F then true
                    else {DictMember Dr F} end
   end
end
```

Example: telephone book

[name1#62565243 name2#67893421 taxi1#65221111...]

#### Dict: Records

#### end

Example: telephone book

```
d(name1:62565243 name2:67893421 taxi1:65521111...)
```

#### Example: Frequency Word Counting

```
local
   fun {Inc D X}
      if {DictMember D X} then
          {DictAdjoin D X {DictAccess D X}+1}
      else {DictAdjoin D X 1}
      end
   end
          {Inc mr(a:3 b:2 c:1) b} \rightarrow mr(a:3 b:3 c:1)
in
   fun {Cnt Xs}
       % returns dictionary
       {FoldL Xs Inc {MakeDict}}
   end
end
```

#### Evolution of ADTs

- Important aspect of developing ADTs
  - start with simple (possibly inefficient) implementation
  - refine to better (more efficient) implementation
  - refine to carefully chosen implementation
    - hash table
    - search tree
- Evolution is local to ADT
  - no change to external programs needed!

#### Theoretically

Polymorphic type is related to Universal Type

```
fun {Id X} X end
Id :: A \rightarrow A
Universal type : \forall A. A \rightarrow A
```

- ADT can be implemented using existential type.
  - ∃A. type
  - where A is considered to be hidden/abstracted

#### Example

Say we want to Peano-number ADT

Can make into existential type using:

# Haskell

Typeful and Lazy Functional Language

## Typeful Programs

- Every expression has a statically determined type that can be declared or inferred
- Equations defined by pattern-matching equations

```
fact :: Integer \rightarrow Integer
fact 0 = 1
fact n | n>0 = n * fact (n-1)
```

### Lazy Evaluation

 Each argument is not evaluated before the call but evaluated when needed (e.g. when matched against patterns)

```
andThen :: Bool -> Bool -> Bool
andThen True x = x
andThen False x = False
```

#### Type Declaration

Data types have to be declared/enumerated.

```
data Bool = True | False
data ListInt = Nil | Cons Integer ListInt
type PairInt = (Integer, Integer)
```

#### Polymorphic Types

Generic types can be defined with type variables.

## Currying

Functions with multiple parameters may be partially applied.

```
add :: Integer -> Integer
add x y = x+y
addT :: (Integer, Integer) -> Integer
addT(x,y) = x+y
```

#### Valid Expressions:

```
(add 1 2) = addT(1,2)

(add 1) = y -> addT(1,y)
```

# Type Classes

- Some functions work on a set of types. For example, sorting works on data values that are comparable.
- Wrong to use polymorphic types!

```
sort :: (List a) -> (List a)
```

Use type class ord a instead.

```
sort :: Ord a => (List a) -> (List a)
```

### Type Classes

Class is characterized by a set of methods

```
class Eq a
== :: a -> a -> Bool
class Eq a => Ord a
>, >= :: a -> a -> Bool
a>=b = (a>b) or (a==b)
```

### Type Classes

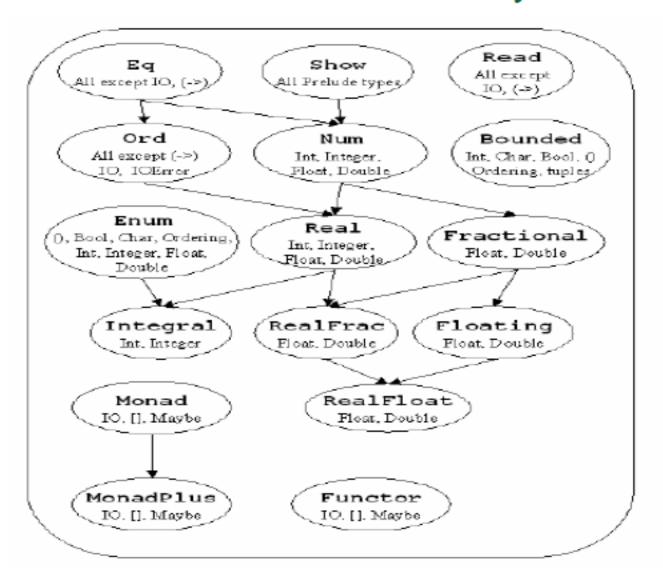
Need to define instances of given class

```
instance Ord Int
  a>b = a ><sub>Int</sub> b

instance Ord a => Ord [a]
  [] > ys = False
  x:xs > [] = True
  x:xs > y:ys = x>y or (x==y & xs>ys)
```

lexicographic ordering

#### Classes in Standard Library



#### Multi-Parameter Type Classes

Can support generic type constructors

```
class Functor f where
  fmap :: (a → b) → f a → f b

instance Functor Tree where
  fmap f (Leaf x) = Leaf (f x)
  fmap f (Node l r)
  = Node (fmap f l) (fmap f r)
```

# Design methodology

Standalone applications

### Design methodology

- "Programming in the large"
  - Written by more than one person, over a long period of time
- "Programming in the small"
  - Written by one person, over a short period of time

#### Design methodology. Recommendations

- Informal specification: inputs, outputs, relation between them
- Exploration: determine the programming technique;
   split the problem into smaller problems
- Structure and coding: determine the program's structure; group related operations into one module
- Testing and reasoning: test cases/formal semantics
- Judging the quality: Is the design correct, efficient, maintainable, extensible, simple?

### Software components

- Split the program into modules (also called logical units, components)
- A module has two parts:
  - An interface = the visible part of the logical unit. It is a record that groups together related languages entities: procedures, classes, objects, etc.
  - An implementation = a set of languages entities that are accessible by the interface operations but hidden from the outside.

#### Module

```
declare MyList in
local
  proc {Append ... } ... end
  proc {Sort ... } ... end
in
 MyList = 'export' (append: Append
                      sort : Sort
end
```

### Modules and module specifications

- A module specification (e.g. functor) is a template that creates a module (component instance) each time it is instantiated.
- In Oz, a functor is a function whose arguments are the modules it needs and whose result is a new module.
  - Actually, the functor takes module interfaces as arguments, creates a new module, and returns that module's interface!

#### Functor

```
fun {MyListFunctor}
proc {Append ... } ... end
 proc {Sort ... } ... end
in
 'export' (append: Append
             sort : Sort
               ... )
end
```

#### Modules and module specifications

- A software component is a unit of independent deployment, and has no persistent state.
- A module is the result of installing a functor in a particular module environment.
- The module environment consists of a set of modules, each of which may have an execution state.

#### Functors

- A functor has three parts:
  - an import part = what other modules it needs
  - an export part = the module interface
  - a define part = the module implementation including initialization code.
- Functors in the Mozart system are compilation units.
  - source code (i.e., human-readable text, .oz)
  - object code (i.e., compiled form, .ozf).

#### Standalone applications (1)

- It can be run without the interactive interface.
- It has a main functor, evaluated when the program starts.
- Imports the modules it needs, which causes other functors to be evaluated.
- Evaluating (or "installing") a functor creates a new module:
  - The modules it needs are identified.
  - The initialization code is executed.
  - The module is loaded the first time it is needed during execution.

#### Standalone applications (2)

- This technique is called dynamic linking, as opposed to static linking, in which the modules are already loaded when execution starts.
- At any time, the set of currently installed modules is called the module environment.
- Any functor can be compiled to make a standalone program.

#### Functors. Example (GenericFunctor.oz)

```
functor
export generic:Generic
define
  fun {Generic Op InitVal N}
    if N == 0 then InitVal
    else {Op N {Generic Op InitVal (N-1)}}
    end
end
```

end

The compiled functor GenericFunctor.ozf is created:

```
□ ozc -c GenericFunctor.oz
```

#### Functors (Standalone Application)

```
GenericFunctor
                                          Browser
functor
                                    imported
import
  GenericFunctor
                                  GenericFact
  Browser
define
                                       executable
   fun {Mul X Y} X*Y end
   fun {FactUsingGeneric N}
       {GenericFunctor.generic Mul 1 N}
   end
   {Browser.browse {FactUsingGeneric 5}}
end
```

The executable functor GenericFact.exe is created:

```
ozc -x GenericFact.oz
```

#### Functors. Interactive Example

```
declare
[GF]={Module.link ['GenericFunctor.ozf']}
fun {Add X Y} X+Y end
fun {GenGaussSum N} {GF.generic Add 0 N} end
{Browse {GenGaussSum 5}}
```

- Function Module.link is defined in the system module Module.
- It takes a list of functors, load them from the file system, links them together
  - (i.e., evaluates them together, so that each module sees its imported modules),
- and returns a corresponding list of modules.

#### Summary

- Type Notation
  - Constructing programs by following the type
- Haskell
- Design methodology
  - modules/functors