Augmenting time series datasets via latent space sampling with applications in algorithmic trading

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June 2021

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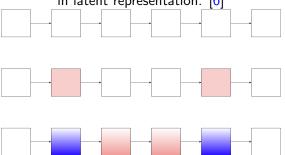
Background

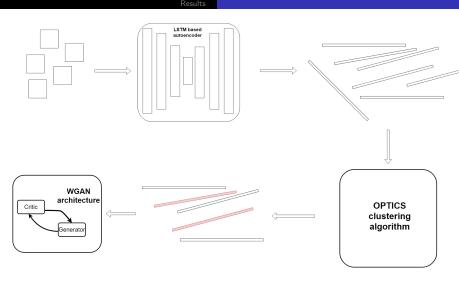
- Securities trading (e.g. stocks, options, cryptocurrencies) is increasingly an automatic, algorithmic-driven field. Three out of four foreign currency exchange trades are automatic [1]
- There is a strong interest in applying deep learning and reinforcement learning to automatic trading, moving away from euristhics [2, 3]
- Eternal struggle of a data scientist: more quality data!

Background

Approach

Autoencoder architecture is able to capture and model timeseries in latent representation. [6]





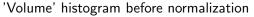
Exploring Data

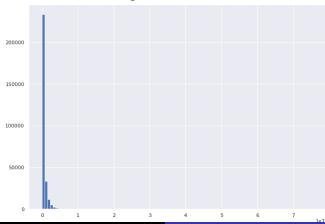
We focus on the AAPL stock price, sampled at interval of 15 minutes

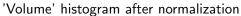
| | | date | time | open | high | low | close | volume |
|--|--------|------------|-------|----------|----------|----------|----------|--------|
| | 0 | 01/02/1998 | 09:30 | 13.6250 | 13.7500 | 13.5000 | 13.6875 | 202700 |
| | 1 | 01/02/1998 | 09:45 | 13.6875 | 13.7500 | 13.5000 | 13.6250 | 334000 |
| | 2 | 01/02/1998 | 10:00 | 13.6250 | 13.7500 | 13.5625 | 13.7500 | 299900 |
| | 3 | 01/02/1998 | 10:15 | 13.7500 | 14.0000 | 13.6250 | 14.0000 | 430201 |
| | 4 | 01/02/1998 | 10:30 | 13.9375 | 14.8125 | 13.7500 | 14.6250 | 944200 |
| | | | | | | | | |
| | 289482 | 03/12/2021 | 18:45 | 120.9900 | 121.1000 | 120.9700 | 121.0900 | 15752 |
| | 289483 | 03/12/2021 | 19:00 | 121.0600 | 121.1000 | 120.9900 | 121.0000 | 19160 |
| | 289484 | 03/12/2021 | 19:15 | 121.0000 | 121.0700 | 120.9900 | 121.0300 | 13815 |
| | 289485 | 03/12/2021 | 19:30 | 121.0100 | 121.0300 | 121.0000 | 121.0300 | 6903 |
| | 289486 | 03/12/2021 | 19:45 | 121.0300 | 121.1000 | 121.0200 | 121.0800 | 33259 |
| | | | | | | | | |

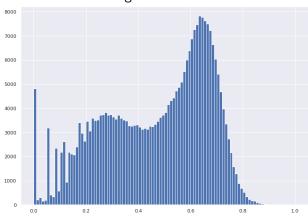
289487 rows × 7 columns

| | open | high | low | close | volume |
|-------|---------------|---------------|---------------|---------------|--------------|
| count | 289487.000000 | 289487.000000 | 289487.000000 | 289487.000000 | 2.894870e+05 |
| mean | 187.757776 | 188.038462 | 187.466230 | 187.758491 | 4.580510e+05 |
| std | 160.514466 | 160.689723 | 160.326415 | 160.513598 | 9.206810e+05 |
| min | 12.550000 | 12.950000 | 11.312500 | 12.850000 | 1.000000e+02 |
| 25% | 78.750000 | 78.920000 | 78.500000 | 78.750000 | 5.900000e+03 |
| 50% | 131.040000 | 131.330000 | 130.790000 | 131.040000 | 1.033630e+05 |
| 75% | 248.160000 | 248.605000 | 247.625000 | 248.150000 | 5.635505e+05 |
| max | 704.800000 | 705.070000 | 704.530000 | 704.800000 | 7.514145e+07 |









- Split the dataset into TIME_STEPS x 5 chunks
- Two consecutive chunks will have TIME_STEPS_COMMON common time steps
- We obtain a dataset of roughly 25000 points

Autoencoder

The autoencoder includes best practices such as Dropout layers and LeakyReLU activations [4, 5]

| Layer (type) | Output Shape | Panan # |
|----------------------------|-----------------|---------|
| input_3 (InputLayer) | [(None, 20, 5)] | 0 |
| conv1d_3 (Conv1D) | (None, 20, 32) | 672 |
| leaky_re_lu_10 (LeakyReLU) | (None, 20, 32) | 0 |
| dropout_10 (Dropout) | (None, 20, 32) | 0 |
| convid_4 (ConviD) | (None, 20, 64) | 8256 |
| leaky_re_lu_11 (LeakyReLU) | (None, 20, 64) | 0 |
| dropout_11 (Dropout) | (None, 20, 64) | 0 |
| conv1d_5 (Conv1D) | (None, 20, 128) | 32896 |
| leaky_re_lu_12 (LeakyReLU) | (None, 20, 128) | 0 |
| dropout_12 (Dropout) | (None, 28, 128) | 0 |
| lstm_5 (LSTM) | (None, 20, 128) | 131584 |
| leaky_re_lu_13 (LeakyReLU) | (None, 20, 128) | 0 |
| dropout_13 (Dropout) | (None, 28, 128) | 0 |
| lstm_6 (LSTM) | (None, 20, 64) | 49488 |
| leaky_re_lu_14 (LeakyReLU) | (None, 20, 64) | 0 |
| dropout_14 (Dropout) | (None, 20, 64) | 0 |
| lstm_7 (LSTM) | (None, 10) | 3000 |

| Model: "decoder" | | |
|---|-----------------|---------|
| Layer (type) | Output Shape | Param # |
| | [(None, 10)] | 0 |
| repeat_vector_1 (RepeatVecto | (None, 20, 10) | 0 |
| 1stm_8 (LSTM) | (None, 20, 64) | 19200 |
| leaky_re_lu_15 (LeakyReLU) | (None, 20, 64) | 0 |
| dropout_15 (Dropout) | (None, 20, 64) | 0 |
| 1stm_9 (LSTM) | (None, 20, 128) | 98816 |
| leaky_re_lu_16 (LeakyReLU) | (None, 20, 128) | 0 |
| dropout_16 (Dropout) | (None, 20, 128) | 0 |
| convld_transpose_3 (ConvlDTr | (None, 20, 128) | 65664 |
| leaky_re_lu_17 (LeakyReLU) | (None, 20, 128) | 0 |
| dropout_17 (Dropout) | (None, 20, 128) | 0 |
| convid_transpose_4 (ConviDTr | (None, 20, 64) | 32832 |
| leaky_re_lu_18 (LeakyReLU) | (None, 20, 64) | 0 |
| dropout_18 (Dropout) | (None, 20, 64) | 0 |
| convid_transpose_5 (ConviDTr | (None, 20, 32) | 8224 |
| leaky_re_lu_19 (LeakyReLU) | (None, 20, 32) | 0 |
| dropout_19 (Dropout) | (None, 20, 32) | 0 |
| time_distributed_2 (TimeDist | (None, 20, 5) | 165 |
| time_distributed_3 (TimeDist Total params: 224,901 | | 8 |
| Trainable params: 224,901 | | |

Trainable params: 224,90 Non-trainable params: 8

Autoencoder

Latent Space

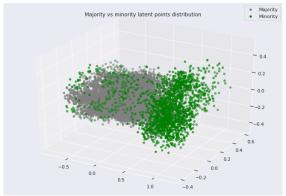
Hyperparameter tweaking concluded a latent space of dimension



Autoencoder

Latent Space

A "majority" cluster can be observed; 3-dim PCA visualization



WGAN

WGAN is an improvement over first-generation GAN architecture

Model: "generator" Laver (type) Output Shape Danam # input_6 (InputLayer) [(None, 15, 1)] dense 4 (Dense) (None, 15, 20) conv1d 9 (Conv1D) (None, 8, 16) 1296 leaky re lu 23 (LeakyReLU) (None, 8, 16) conv1d 10 (Conv1D) (None, 4, 16) 1040 leaky_re_lu_24 (LeakyReLU) (None, 4, 16) flatten 1 (Flatten) (None, 64) dense 5 (Dense) (None, 100) 6500 dense 6 (Dense) (None, 100) 10100 dense_7 (Dense) (None, 10) 1010 Total params: 19,986 Trainable params: 19,986

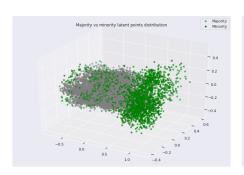
Non-trainable params: 0

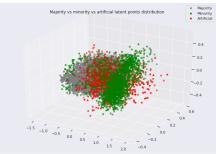
Model: "critic" Layer (type) Output Shape input 5 (InputLayer) [(None, 10, 1)] conv1d 6 (Conv1D) (None, 5, 16) 80 leaky re lu 20 (LeakyReLU) (None, 5, 16) conv1d_7 (Conv1D) (None, 3, 16) 1040 leaky re lu 21 (LeakyReLU) (None, 3, 16) conv1d 8 (Conv1D) (None, 2, 16) 1040 leaky re lu 22 (LeakyReLU) (None, 2, 16) flatten (Flatten) (None, 32) dense 2 (Dense) (None, 100) 3300 dense 3 (Dense) (None, 1) -----

Total params: 5,561 Trainable params: 5,561 Non-trainable params: 0

Generated latent points

Figure: WGAN is able to generalize new interesting points in latent space

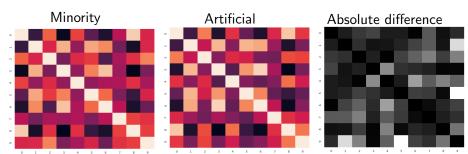




Generated latent points

Multivariate Wilcoxon test [8] indicates that the generated points are actually different from non-majority points (p=0.0186)* Figure:

The correlation maps for minority and artificial are different:



They're not even half bad!

| | open | high | low | close | volume | | open | high | low | close | volume | | open | high | low | close | volume |
|----|-----------|-----------|-----------|-----------|---------------|----|------------|------------|------------|------------|--------------|-----|-----------|-----------|-----------|-----------|---------------|
| 0 | 15.243655 | 15.253026 | 15.194520 | 15.253026 | 120136.226562 | 0 | 328.285400 | 328.611328 | 327.923828 | 328.611328 | 99.999954 | 0 | 21.104191 | 21.112183 | 21.044468 | 21.112183 | 137670.421875 |
| 1 | 15.228220 | 15.247979 | 15.180886 | 15.247979 | 99446.000000 | 1 | 326.386292 | 326.535126 | 326.086853 | 326.535126 | 783.815796 | - 1 | 20.982815 | 20.992153 | 20.921492 | 20.992153 | 223587.109375 |
| 2 | 15.276122 | 15.305717 | 15.231302 | 15.305717 | 66718.484375 | 2 | 330.967285 | 331.169830 | 330.576172 | 331.169830 | 1070.473511 | 2 | 20.982824 | 20.994345 | 20.921881 | 20.994345 | 277790.656250 |
| 3 | 15.385123 | 15.418838 | 15.341538 | 15.418838 | 54139.515625 | 3 | 332.969727 | 333.235931 | 332.445892 | 333.235931 | 1950.821655 | 3 | 20.968788 | 20.981316 | 20.907495 | 20.981316 | 353173.406250 |
| 4 | 15.219886 | 15.254024 | 15.176585 | 15.254024 | 57980.453125 | 4 | 333.611328 | 333.698517 | 333.305084 | 333.698517 | 468.448151 | 4 | 20.732935 | 20.743990 | 20.669832 | 20.743990 | 432019.812500 |
| 5 | 14.824146 | 14.858824 | 14.782189 | 14.858824 | 53399.527344 | 5 | 324.876434 | 325.506165 | 324.311035 | 325.506165 | 99.999954 | 5 | 20.392403 | 20.404743 | 20.330650 | 20.404743 | 486898.906250 |
| 6 | 14.866426 | 14.903136 | 14.825564 | 14.903136 | 43166.875000 | 6 | 329.570251 | 329.617706 | 329.417419 | 329.617706 | 302.992767 | 6 | 20.264952 | 20.278585 | 20.204550 | 20.278585 | 504092.031250 |
| 7 | 14.899176 | 14.949899 | 14.864511 | 14.949899 | 12371.279297 | 7 | 337.244415 | 337.603516 | 336.614471 | 337.603516 | 3137.767090 | 7 | 20.353367 | 20.368673 | 20.294113 | 20.368673 | 510079.812500 |
| 8 | 14.692458 | 14.761474 | 14.666427 | 14.761474 | 2728.982178 | 8 | 340.645233 | 341.047668 | 339.870667 | 341.047668 | 4611.264160 | 8 | 20.313545 | 20.329094 | 20.255043 | 20.329094 | 479180.218750 |
| 9 | 14.716473 | 14.739958 | 14.672203 | 14.739958 | 73965.726562 | 9 | 340.881500 | 341.277863 | 340.124542 | 341.277863 | 4799.050781 | 9 | 20.130693 | 20.150333 | 20.076599 | 20.150333 | 462485.562500 |
| 10 | 14.880865 | 14.886304 | 14.829742 | 14.886304 | 198242.906250 | 10 | 337.815125 | 338.226166 | 337.060516 | 338.226166 | 5621.359863 | 10 | 20.105383 | 20.132767 | 20.057438 | 20.132767 | 541669.125000 |
| 11 | 14.941760 | 14.950253 | 14.890265 | 14.950253 | 230313.250000 | 11 | 338.466064 | 338.895782 | 337.692413 | 338.895782 | 6761.752930 | 11 | 20.014164 | 20.022221 | 19.955524 | 20.022221 | 188173.484375 |
| 12 | 14.908655 | 14.916911 | 14.857006 | 14.916911 | 241238.500000 | 12 | 337.389343 | 337.804352 | 336.644196 | 337.804352 | 6170.877441 | 12 | 19.573996 | 19.652031 | 19.541817 | 19.652031 | 2278.294922 |
| 13 | 14.926683 | 14.935029 | 14.875145 | 14.935029 | 235060.812500 | 13 | 338.481079 | 338.867645 | 337.771973 | 338.867645 | 4593.961426 | 13 | 19.437897 | 19.477896 | 19.390755 | 19.477896 | 19736.904297 |
| 14 | 14.872905 | 14.882419 | 14.822306 | 14.882419 | 203394.796875 | 14 | 339.863068 | 340.254822 | 339.151520 | 340.254822 | 4806.296387 | 14 | 19.795088 | 19.859772 | 19.757679 | 19.859772 | 4509.490723 |
| 15 | 14.815712 | 14.825365 | 14.765698 | 14.825365 | 182581.171875 | 15 | 341.079346 | 341.704498 | 340.060669 | 341.704498 | 32221.625000 | 15 | 19.569996 | 19.711926 | 19.566645 | 19.711926 | 99.999954 |
| 16 | 14.743999 | 14.753530 | 14.694370 | 14.753530 | 170796.218750 | 16 | 344.108734 | 344.690247 | 343.121704 | 344.690247 | 20956.394531 | 16 | 19.494667 | 19.596134 | 19.474115 | 19.596134 | 520.183594 |
| 17 | 15.097682 | 15.106466 | 15.046432 | 15.106466 | 193027.968750 | 17 | 343.006866 | 343.571442 | 342.031799 | 343.571442 | 19307.960938 | 17 | 20.074871 | 20.155561 | 20.044037 | 20.155561 | 1793.617188 |
| 18 | 15.156822 | 15.158875 | 15.101473 | 15.158875 | 382102.812500 | 18 | 347.626007 | 348.201691 | 346.623596 | 348.201691 | 20125.775391 | 18 | 19.989128 | 20.065826 | 19.955566 | 20.065826 | 2648.292969 |
| 19 | 15.353157 | 15.355431 | 15.299351 | 15.355431 | 394814.906250 | 19 | 347.505188 | 348.110840 | 346.366669 | 348.110840 | 21908.580078 | 19 | 19.589943 | 19.685362 | 19.566496 | 19.685362 | 690.475647 |

Smoothing the points

• GAN network samples from poorly-represented regions since it maximizes critic's confusion. It is unable to represent constraints e.g. $high_t$ should be larger than col_t , $\forall col \in \{high, open, close, low\}$, $close_t == open_{t+1}$ for any timestep t

We employ Bayesian search to find the closest latent point

that satisfies the constraints. Formally for each tuple $(open_t, high_t, low_t, close_t) = ts_t$ of an arbitrary chunk we identify the maximum of a black box function f which is defined as: $\begin{cases} -\infty & invalid \\ \frac{1}{\|ts_t - ts_{gen}\|} & valid \end{cases}$, minimising the distance over all timesteps.

Integrating the points

• For each sample from the generated ones, ts_{fake} we find two consecutive time steps, ts1 and ts2, such that we minimize $\|\operatorname{close}_{ts1} - \operatorname{open}_{tsfake}\|, \|\operatorname{close}_{tsfake} - \operatorname{open}_{ts2}\|, \|\mu(\operatorname{volume}_{ts1}) - \mu(\operatorname{volume}_{tsfake})\|, \|\mu(\operatorname{volume}_{tsfake}) - \mu(\operatorname{volume}_{ts2})\|$

 Each integrated fake sample is assumed to be real after integration. Thus it is possible to have consecutive fake chunks

Results

- We employ a benchmark trading algorithm [9] based on reinforcement learning and apply it over both datasets
- We observe a 5-7% percent improvement of the algorithm's performace. These are preliminary results.
- We conclude that data augmentation is pheasible on timeseries datasets. We hypothesise that our approach can identify poorly represented intervals of a timeseries dataset.

QA time!

References

- Pratik Mulay, Nishant Poojary, Dr. Pravin Srinath Automated Trading System - A Survey. International Research Journal of Engineering and Technology, Aug 2016
- Yang, Hongyang, et al *Deep Reinforcement Learning for Automated Stock Trading: An Ensemble Strategy.* 3690996, Social Science Research Network, Sept 2020.
- Théate, Thibaut, and Damien Ernst An Application of Deep Reinforcement Learning to Algorithmic Trading. ArXiv:2004.06627, Oct 2020

References

- Geoffrey E. Hinton, Nitish Srivastava, Alex Krizhevsky, Ilya Sutskever, Ruslan R. Salakhutdinov *Dropout: A Simple Way to* Prevent Neural Networks from Overfitting arXiv:1207.0580
- Bing Xu, Naiyan Wang, Tianqi Chen, Mu Li Empirical Evaluation of Rectified Activations in Convolutional Network arXiv:1505.00853
- Neda Tavakoli, Sima Siami-Namini, Mahdi Adl Khanghah,
 Fahimeh Mirza Soltani, Akbar Siami Namin Clustering Time Series
 Data through Autoencoder-based Deep Learning Models
 arXiv:2004.07296
 - Martin Arjovsky, Soumith Chintala, Léon Bottou Wasserstein GAN arXiv:1701.07875
- Ching-Fan Sheu Suzanne O'Curry Implementation of