

## Seminar 9

### week 9 (23 November 2020 – 27 November 2020)

#### Toy language syntax:

**Type ::= int**

| **bool**

| **string**

| **Ref Type**

| **void**

**Stmt ::= Stmt; Stmt**

| **Id = Exp**

| **Type Id**

| **print(Exp)**

| **If Exp Then Stmt1 else Stmt2**

| **Nop**

| **openRFile(Exp)**

| **readFile(Exp, id)**

| **closeRFile(Exp)**

| **new(Id, Exp)**

| **wH(Id, Exp)**

| **while Exp Stmt**

| **fork(Stmt)**

**Value ::= Number**

| **True**

| **False**

| **String**

| **(value, Type) //ref value**

**Exp ::= Value**

| **id**

| **rH(Exp)**

| **Exp1 + Exp2**

| **Exp1 - Exp2**

| **Exp1 \* Exp2**

| **Exp1 / Exp2**

| **Exp1 and Exp2**

| **Exp1 or Exp2**

| **Exp1 < Exp2**

| **Exp1 <= Exp2**

| **Exp1 == Exp2**

| **Exp1 != Exp2**

| **Exp1 > Exp2**

| **Exp1 >= Exp2**

## Types

**2 : int**

**id : type (given by the programmer)**

## Type rules

**1: int    2:int**

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**1 + 2 : int**

**is reading as:**

**-- 1+2 has type int IF 1 has type int and 2 has type int**

**or**

**-- IF 1 has type int and 2 has type int THEN 1+2 has type int**

**1: int    v:??**

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**1 + v : int**

**G- type environment, defined as a list of pairs (id:type)**

**G|-1: int    G|-v:int**

-----    where G=[v:int]  
**G|-1 + v : int**

## Type rules for Values

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**G|- Number : int**

-----  
**G|-True:bool**

-----  
**G|-False:bool**

-----  
**G|-String:string**

**G|- val: int**

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**G|-(val,type) : Ref type**

### Type rules for Expressions

(id:t) is in G

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$G \vdash \text{id} : t$

$G \vdash e1 : \text{int} \quad G \vdash e2 : \text{int}$

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$G \vdash e1 + e2 : \text{int}$

the same rule for -,\*,/

$G \vdash e1 : \text{bool} \quad G \vdash e2 : \text{bool}$

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$G \vdash e1 \text{ and } e2 : \text{bool}$

the same rule for or

$G \vdash e1 : \text{int} \quad G \vdash e2 : \text{int}$

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$G \vdash e1 < e2 : \text{bool}$

the same rule for <=,==,!=,>, >=

$G \vdash e1 : \text{Ref } t1$

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$G \vdash \text{rH}(e1) : t1$

### Type rules for Statements

$G \vdash s1 : \text{void}, G1 \quad G1 \vdash s2 : \text{void}, G2$

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$G \vdash s1; s2 : \text{void}, G2$

$G \vdash \text{id} : t1 \quad G \vdash \text{exp} : t2 \quad t1 == t2$

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$G \vdash \text{id} = \text{exp} : \text{void}, G$

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$G \vdash \text{type id} : \text{void}, G + [(\text{id} : \text{type})]$

**G|- exp:t**

-----  
**G|- print(exp): void,G**

**G|- e : bool**

**G|- s1:void,G1**

**G|- s2:void,G2**

-----  
**G|- if e then s1 else s2 : void,G**

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**G|- nop:void, G**

**G|- exp:string   G|-id:int**

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**G|- readFile(exp,id):void,G**

**G|- exp:string**

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**G|- openRFile(exp):void, G**

**G|- exp:string**

-----  
**G|- closeRFile(exp):void, G**

**G|- exp:t   G|- id:Ref t**

-----  
**G|- new(id,exp):void, G**

**G|- exp:t   G|- id:Ref t**

-----  
**G|- wH(id,exp):void, G**

**G|- exp:bool   G|- stmt:void,G1**

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**G|- while exp stmt:void, G**

**G|- stmt:void,G1**

-----  
**G|- fork(stmt):void, G**