

JOŽEF STEFAN days, Ljubljana, 19 March 2012

ULTRAHLADNI ATOMI: MODELSKI SISTEMI ZA KVANTNE SNOVI

Ultracold atoms: Model kits for quantum matter

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University of Innsbruck
Austrian Academy of Sciences

ultracold quantum gases: introduction into the general ideas

**example #1: Efimov's mysterious
quantum states**

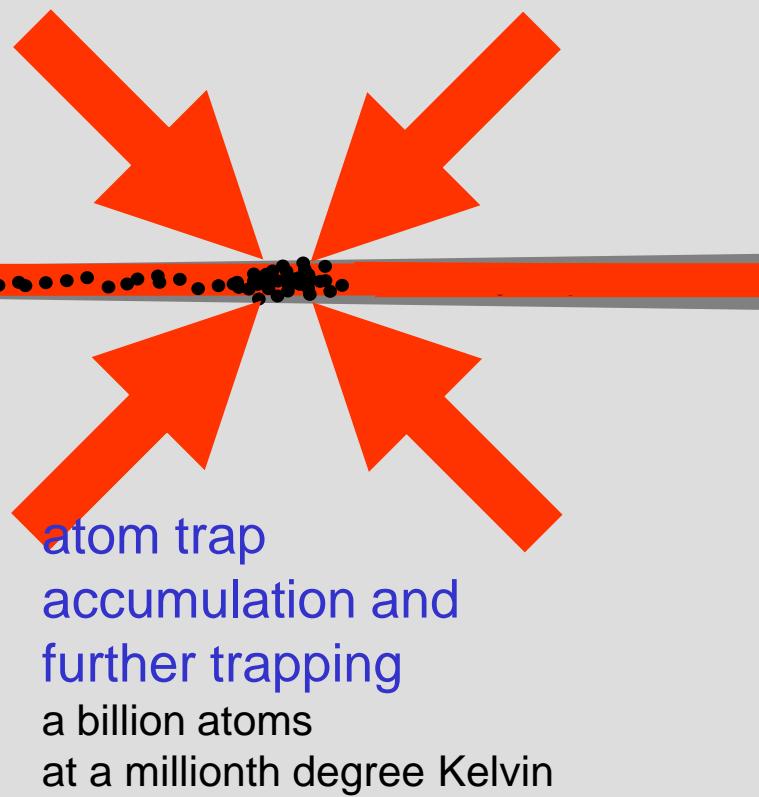
**example #2: strongly interacting
Fermi gases**

ultracold quantum gases: the general ideas

important developments: mid 80's – early 90's



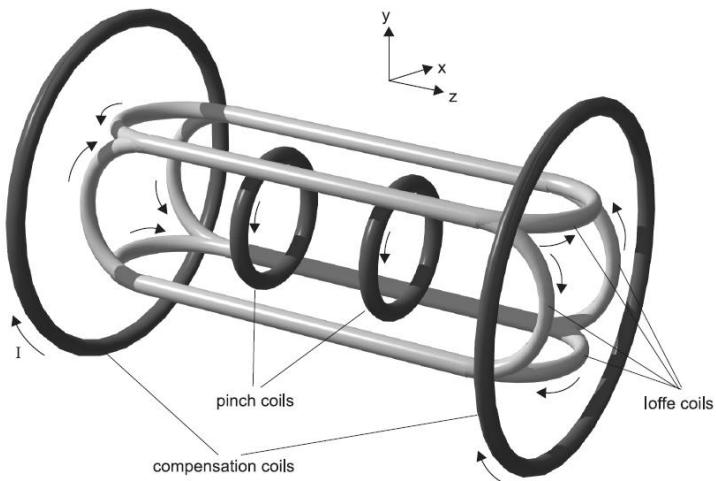
decelerated atomic beam
→ few m/s (~1K)



conservative atom traps

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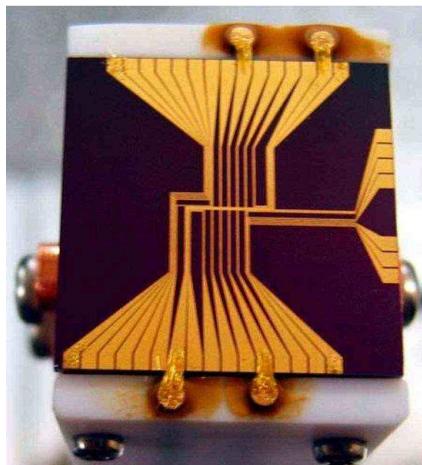
magnetic traps



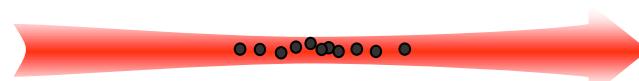
K. Dieckmann, PhD thesis, U Amsterdam, 2001

“atom chip”

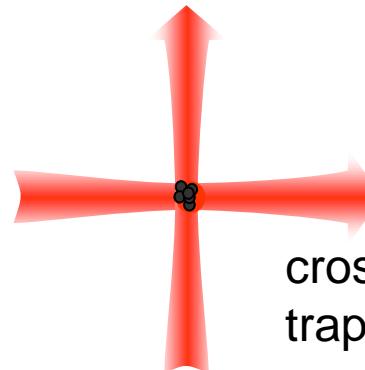
TU Vienna



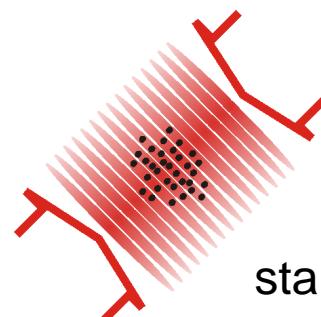
optical dipole traps



focused beam trap



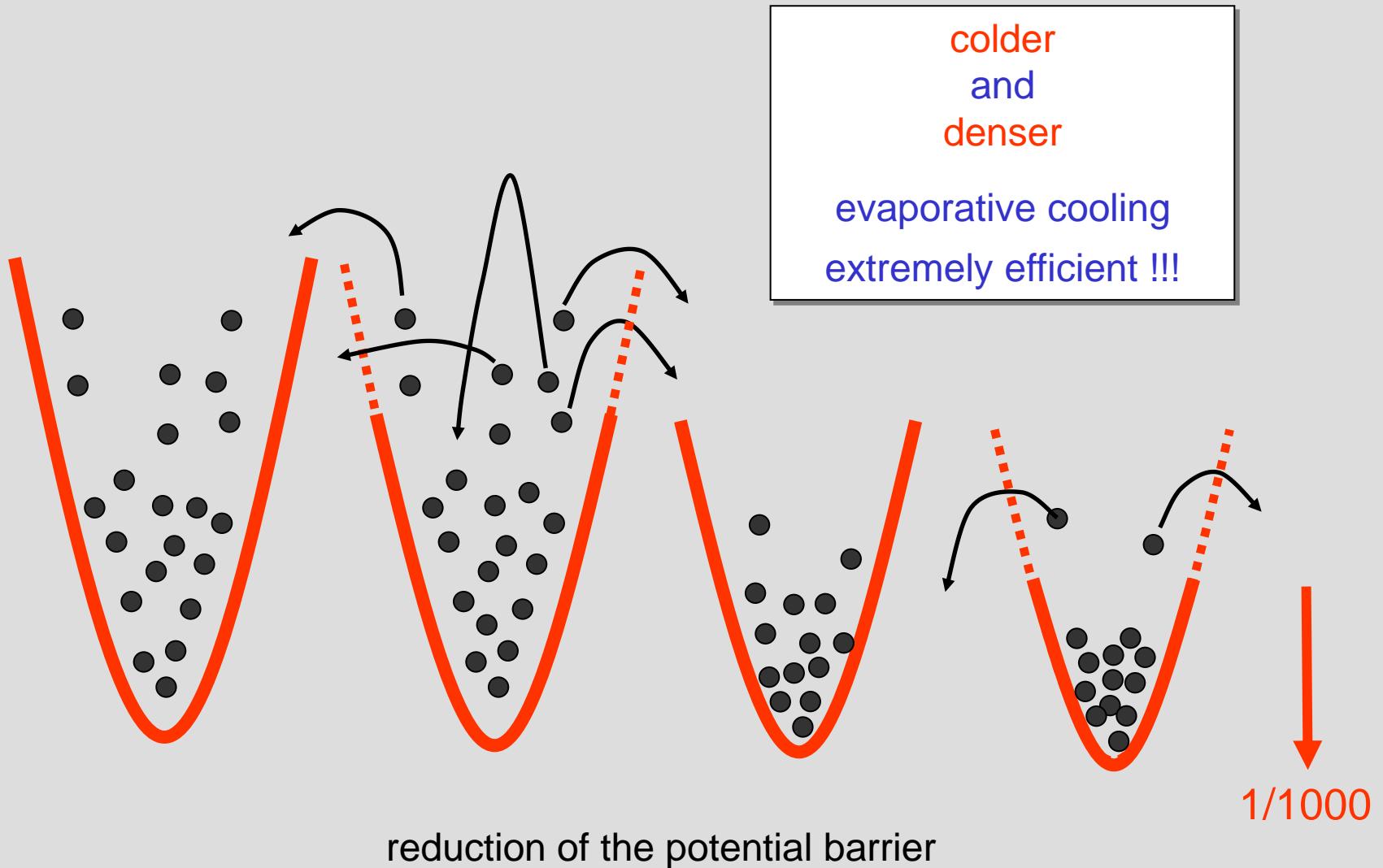
crossed-beam
trap



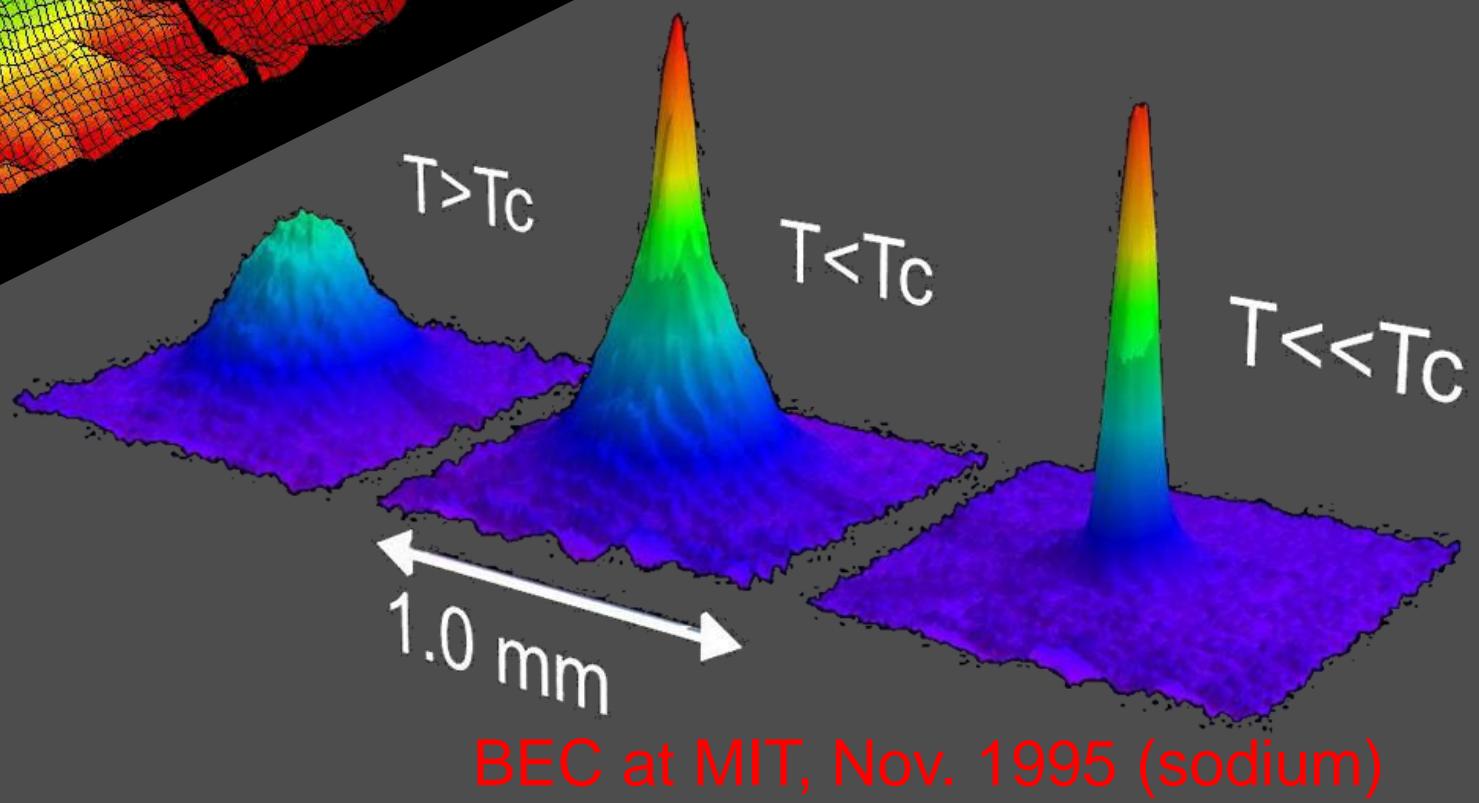
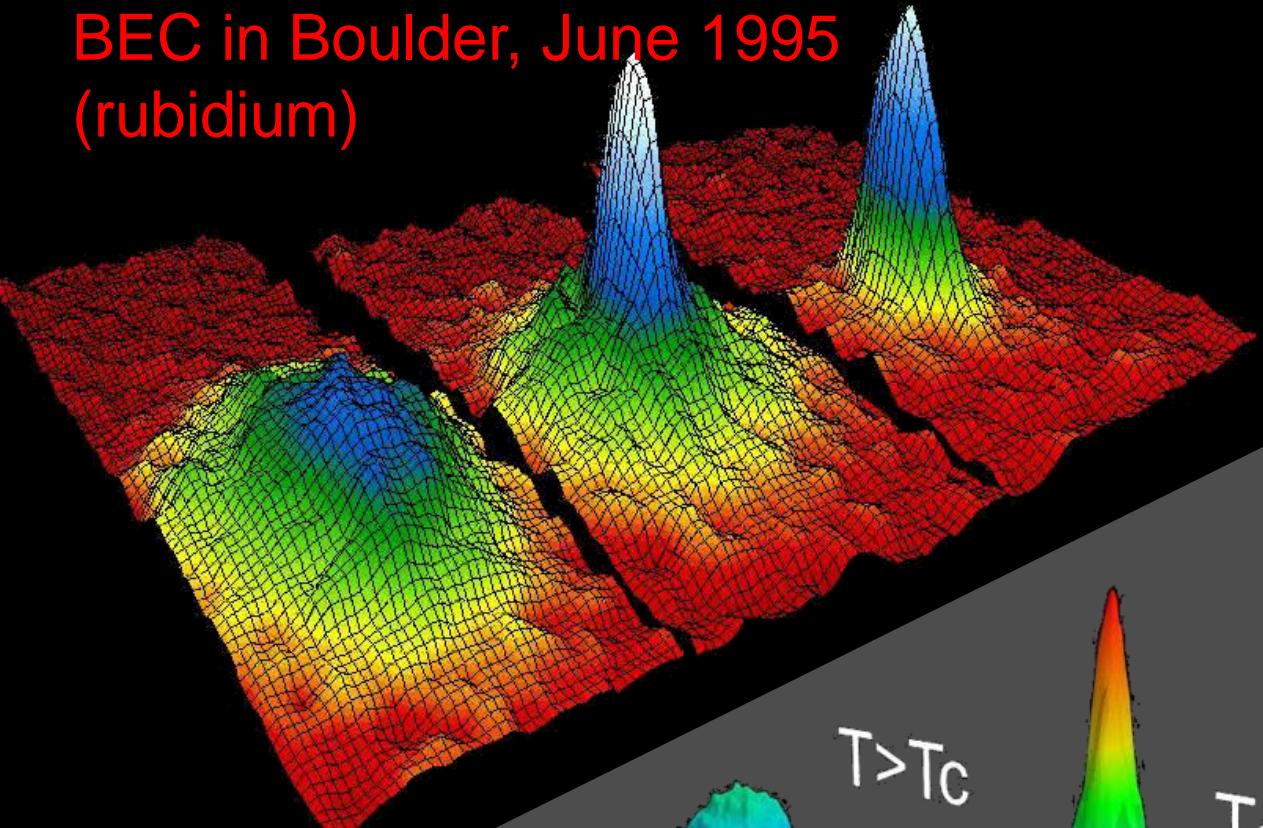
standing-wave
trap (1D lattice)

evaporative cooling: basic idea

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BEC in Boulder, June 1995
(rubidium)



Periodic Table of the Elements

		IA																O	
1		Be																He	
2		Mg	IIIIB	IVB	VB	VIB	VIIIB		VII		IB	IIB						Ne	
3		K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	
4		Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe	
5		Cs	Ba	*La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
6		Fr	Ra	+Ac	Rf	Ha	Sg	Ns	Hs	Mt	110	111	112	113	113				

* Lanthanide Series

+ Actinide Series

58	Ce	59	Pr	60	Nd	61	Pm	62	Sm	63	Eu	64	Gd	65	Tb	66	Dy	67	Ho	68	Er	69	Tm	70	Yb	71	Lu
90	Th	91	Pa	92	U	93	Np	94	Pu	95	Am	96	Cm	97	Bk	98	Cf	99	Es	100	Fm	101	Md	102	No	103	Lr

attainment of BEC

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Periodic Table of the Elements

IA												O	
1	1	2	3	4	5	6	7	8	9	10	11	12	
2	Be												
3	Mg												
4	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	
5	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	
6	Ba	*La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb
7	Fr	Ra	+Ac	Rf	Ha	Sg	Ns	Hs	Mt	110	111	112	113

* Lanthanide Series

+ Actinide Series

58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Ho	67 Tm	68 Lu			
90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr

degenerate Fermi gases

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	IA	IIA	Periodic Table of the Elements												O			
1	H	Be													He	2		
2	Li	K													Ne	10		
3	Na	Mg														18		
4	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
5	Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
6	Cs	Ba	*La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
7	Fr	Ra	+Ac	Rf	Ha	Sg	Ns	Hs	Mt	110	111	112	113	113				

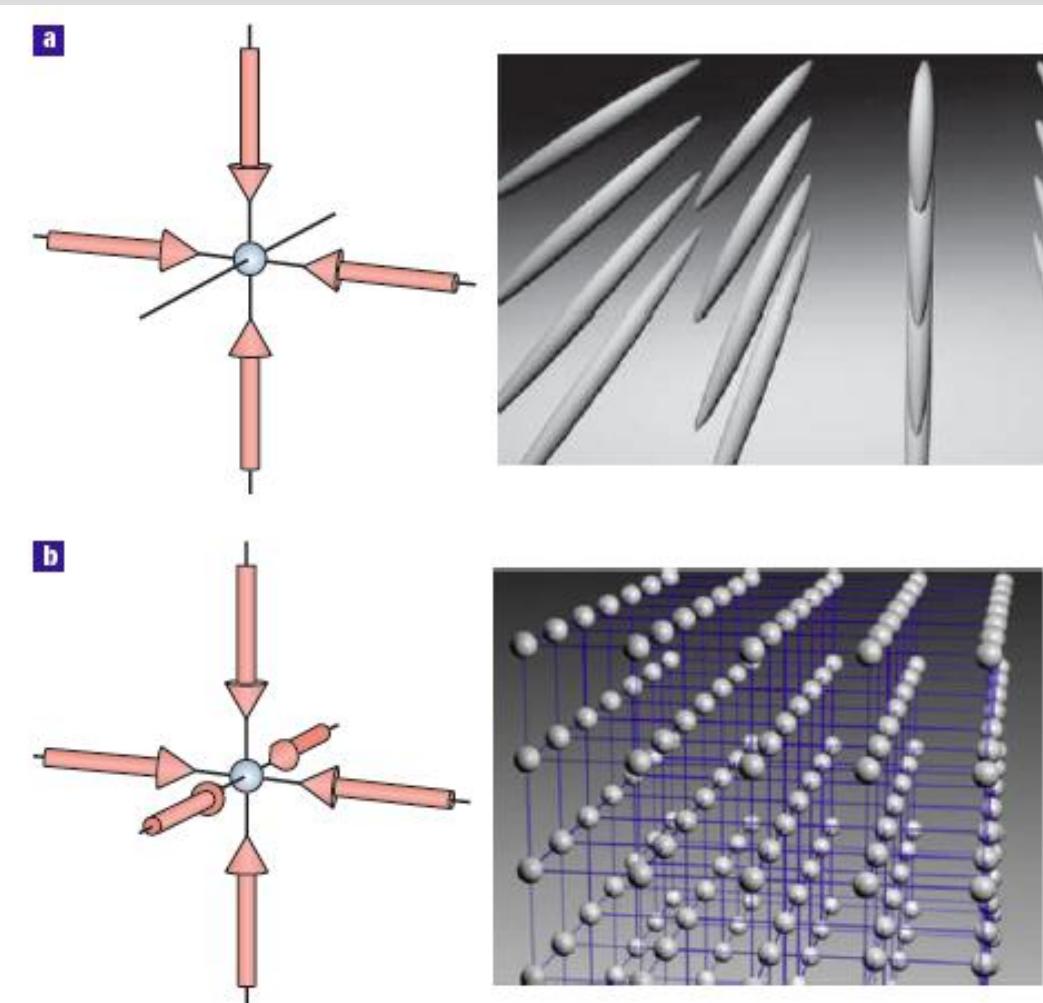
* Lanthanide Series

+ Actinide Series

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

optical lattices

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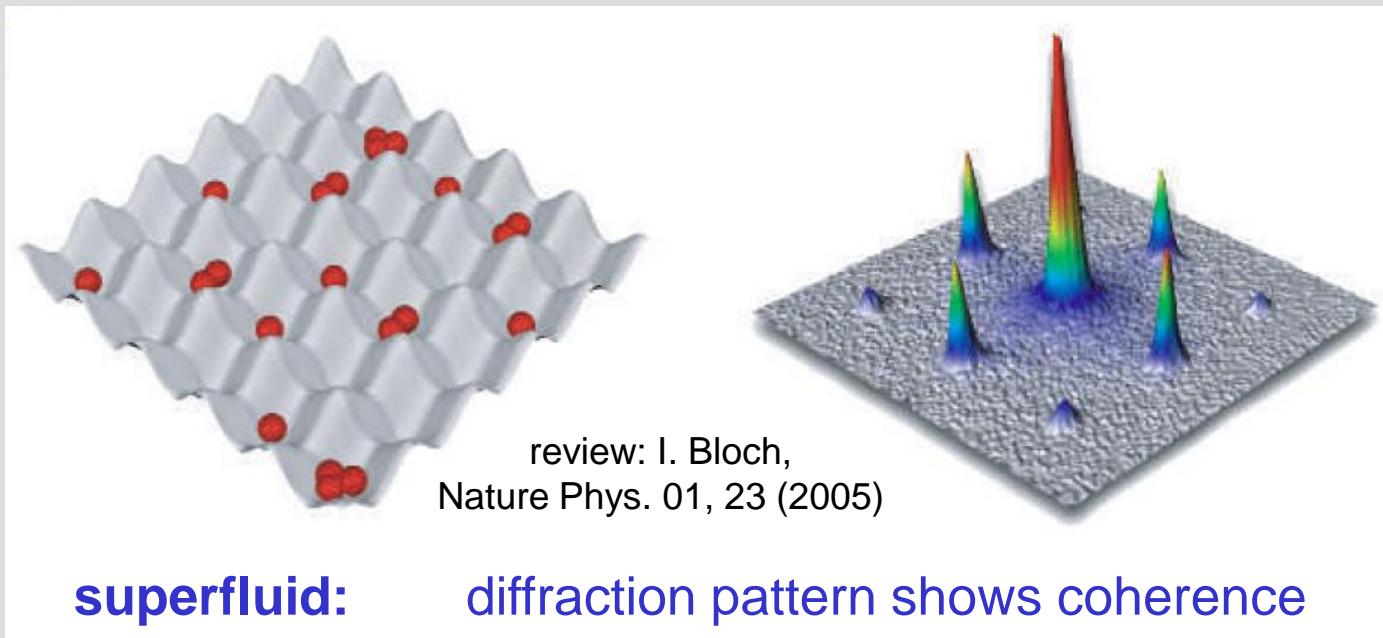


review: I. Bloch, Nature Phys. 01, 23 (2005)

Figure 1 Optical lattice potentials formed by superimposing two or three orthogonal standing waves.
a, For a 2D optical lattice, the atoms are confined to an array of tightly confining 1D potential tubes.
b, In the 3D case, the optical lattice can be approximated by a 3D simple cubic array of tightly confining harmonic oscillator potentials at each lattice site.

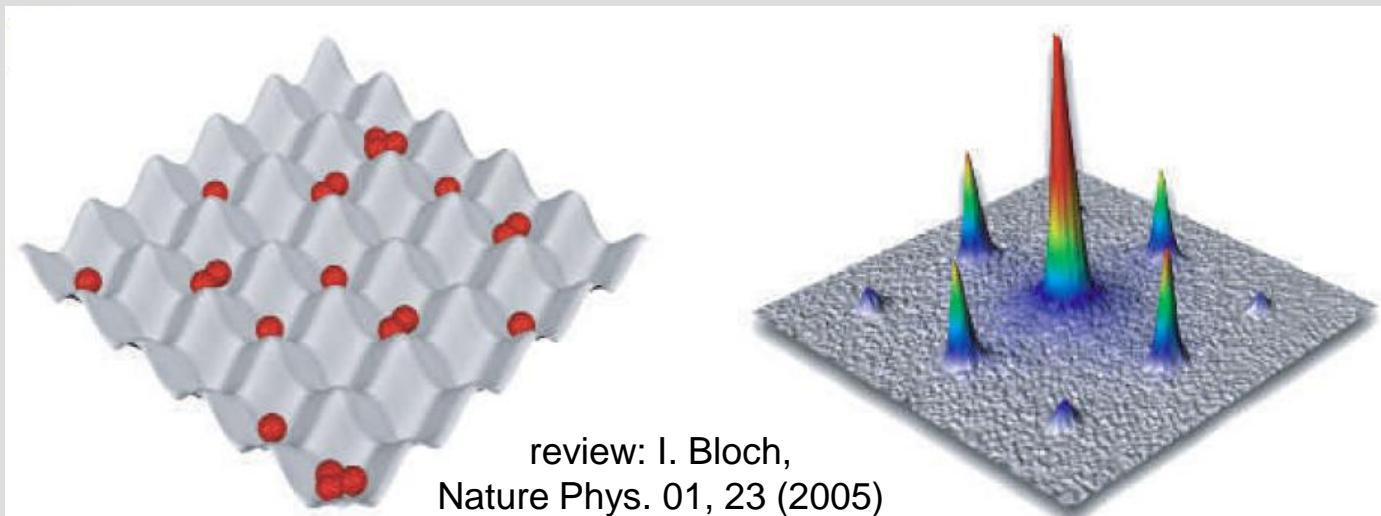
Mott insulator phase transition

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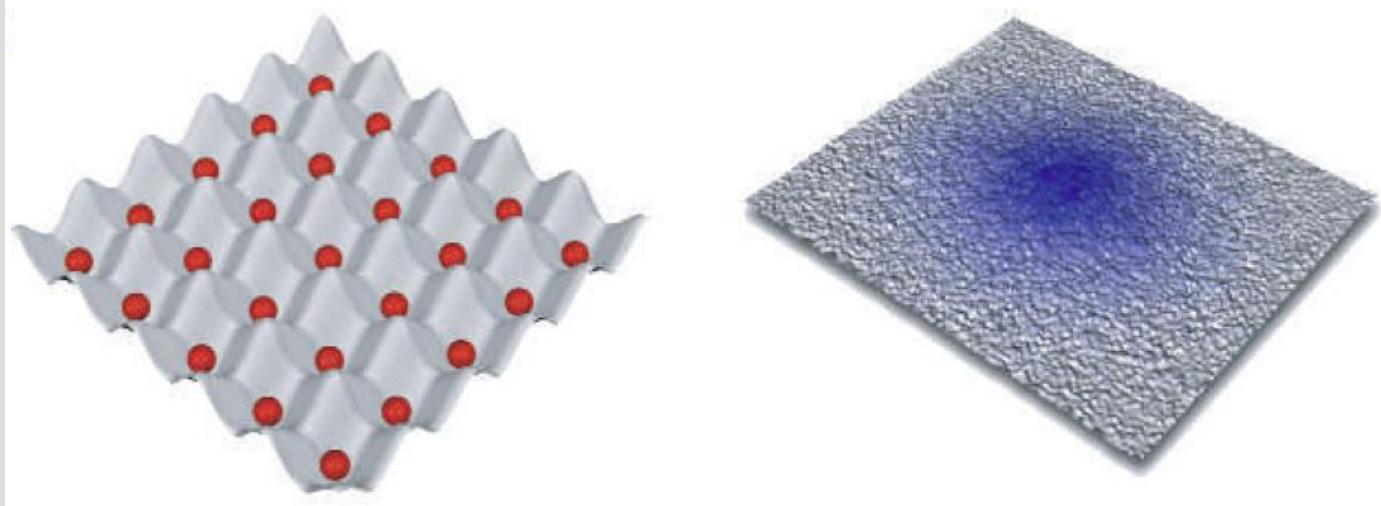
Mott insulator phase transition

ultracold.atoms



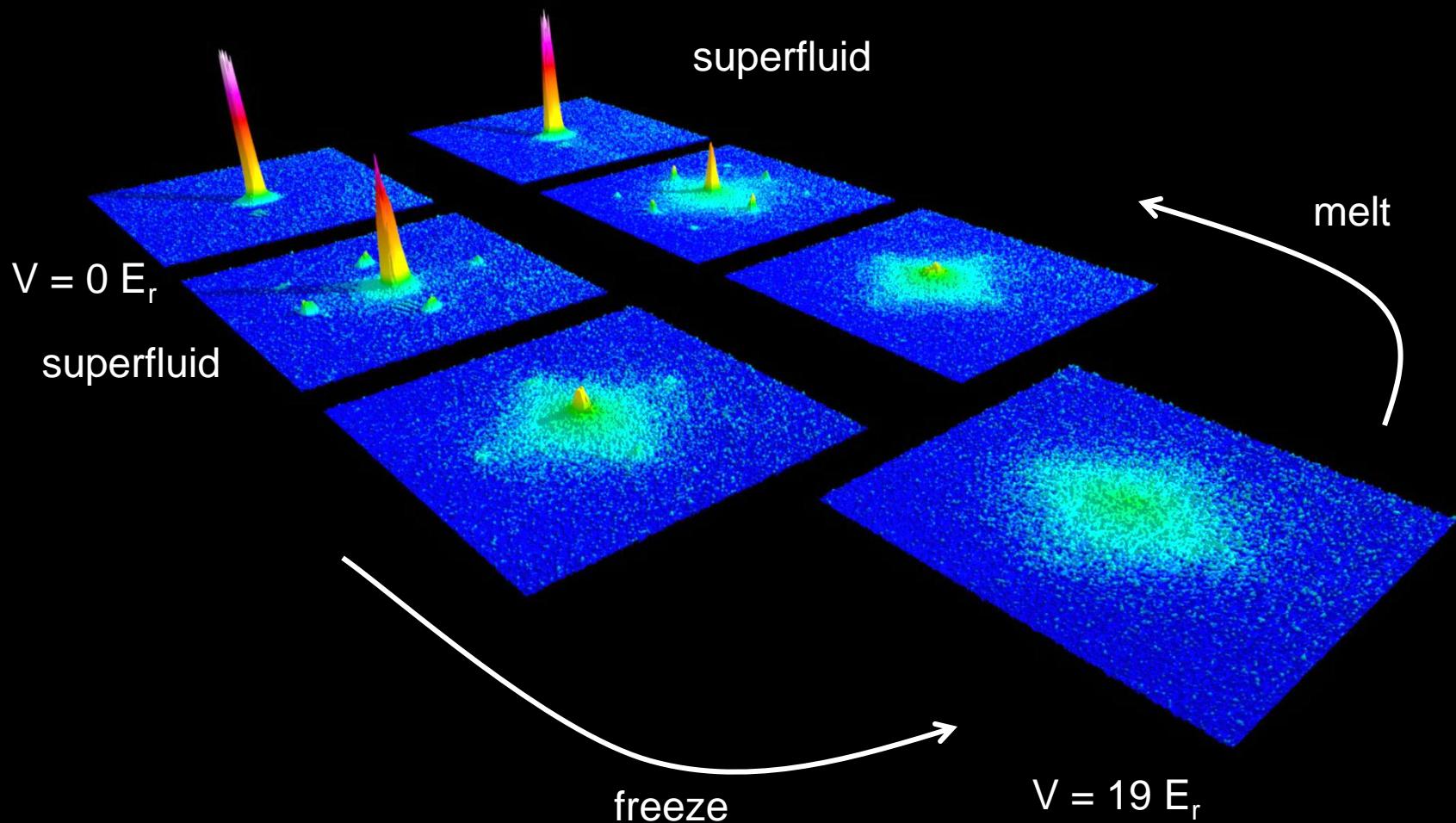
superfluid: diffraction pattern shows coherence

Mott insulator: disappearance of diffraction pattern

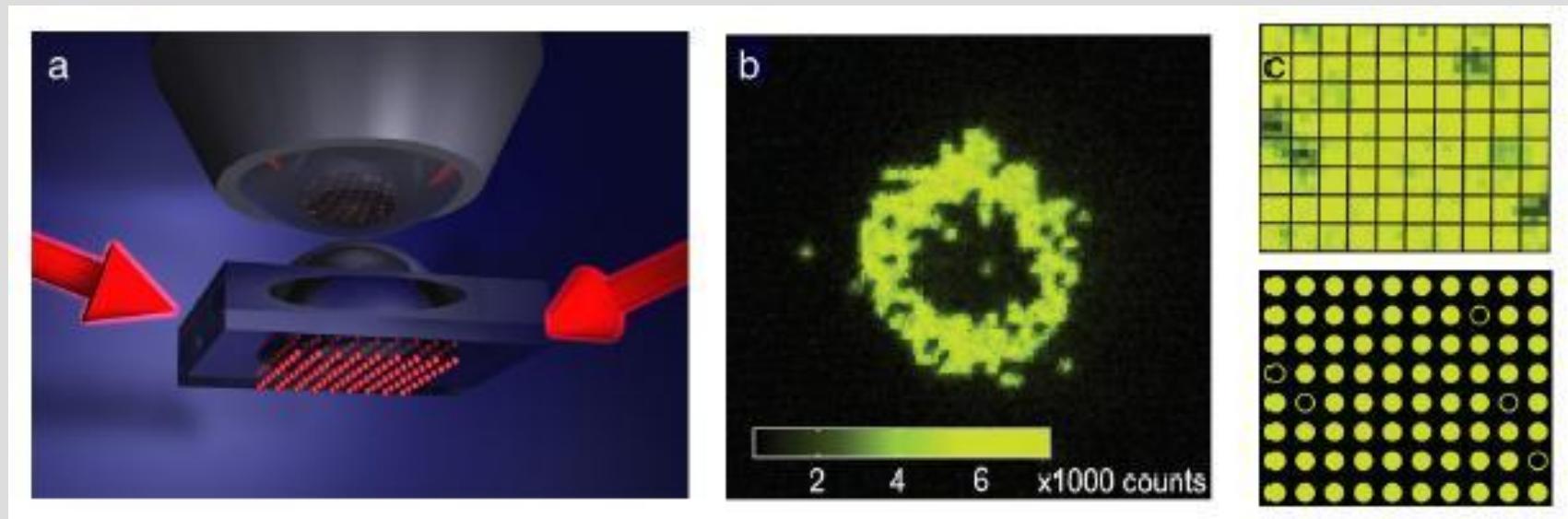


^{84}Sr Mott insulator in Innsbruck

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the high end: quantum gas microscopy



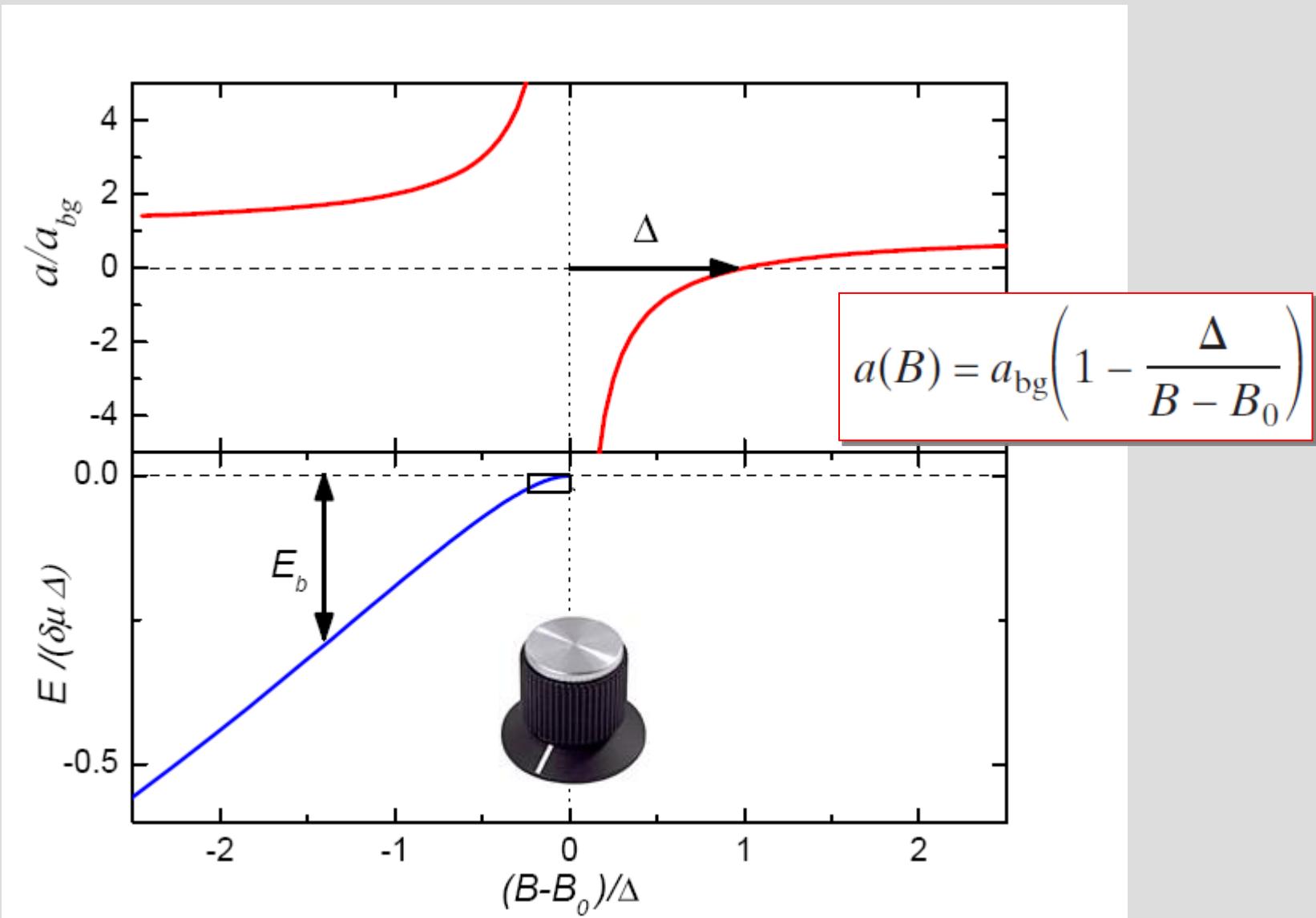
Greiner group @ Harvard

single parameter characterizes everything
s-wave scattering length a

but can we control it?



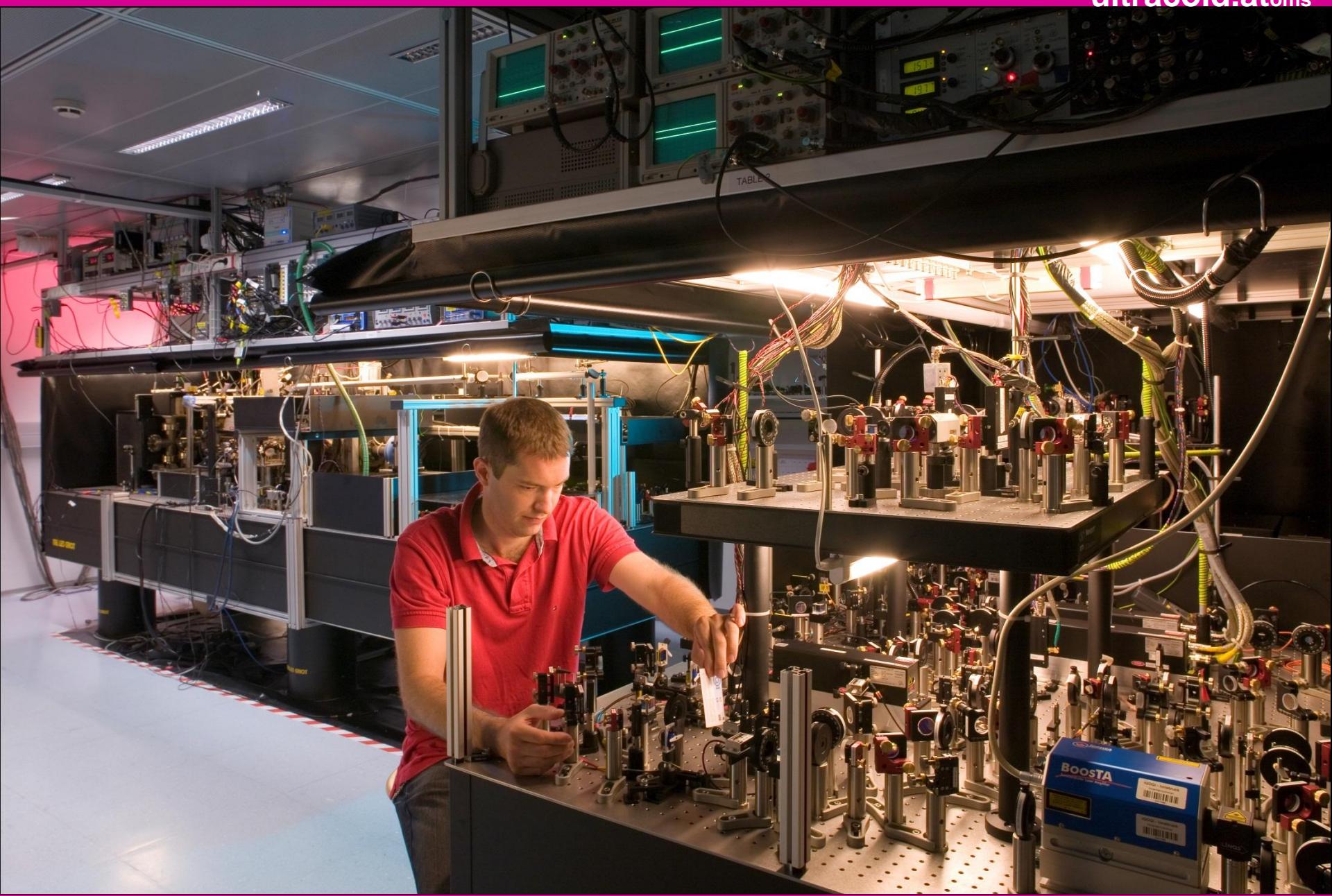
Feshbach resonance



review: Chin, Grimm, Julienne, Tiesinga, RMP 74, 1205 (2010)

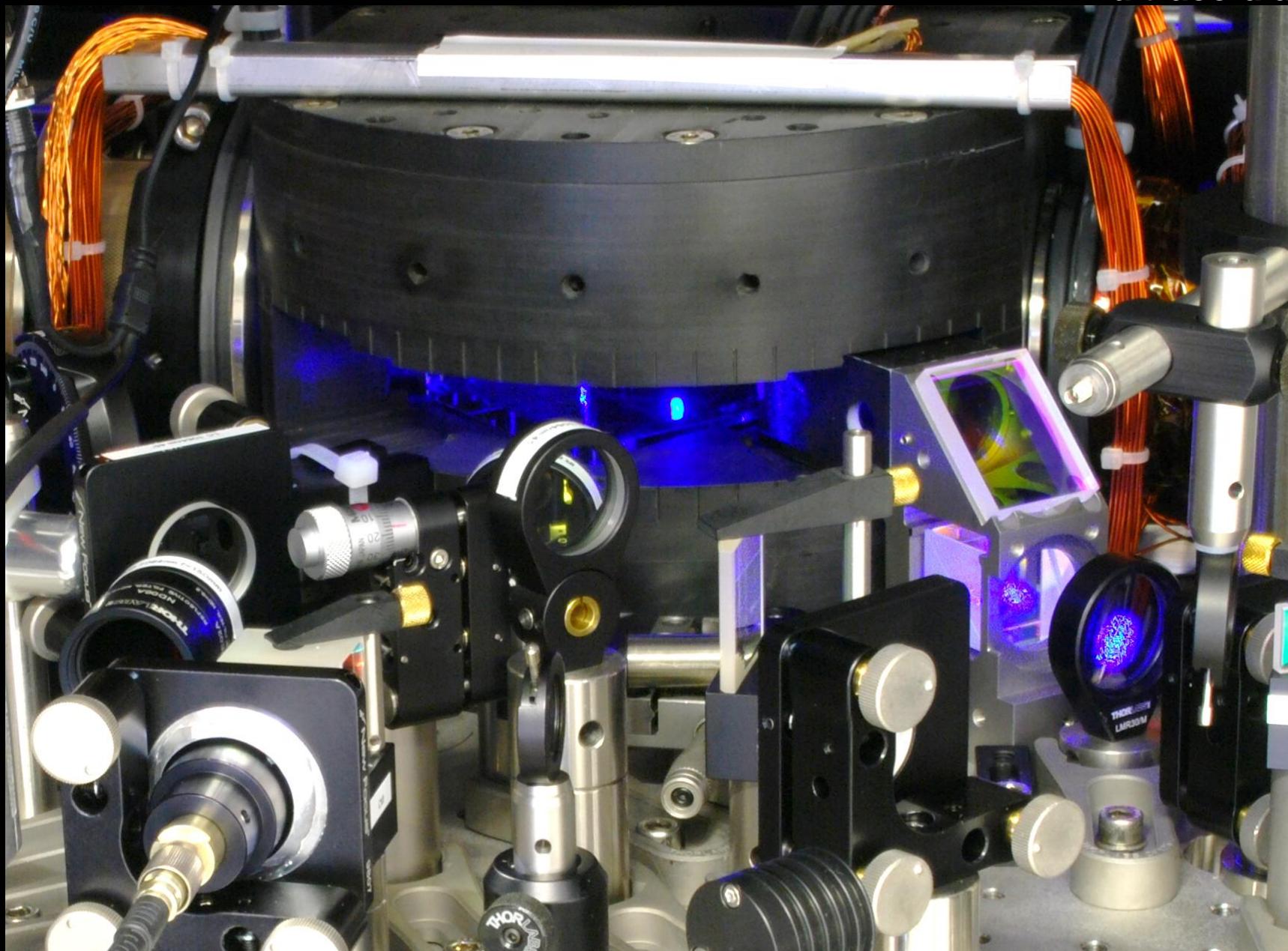
table-top set up

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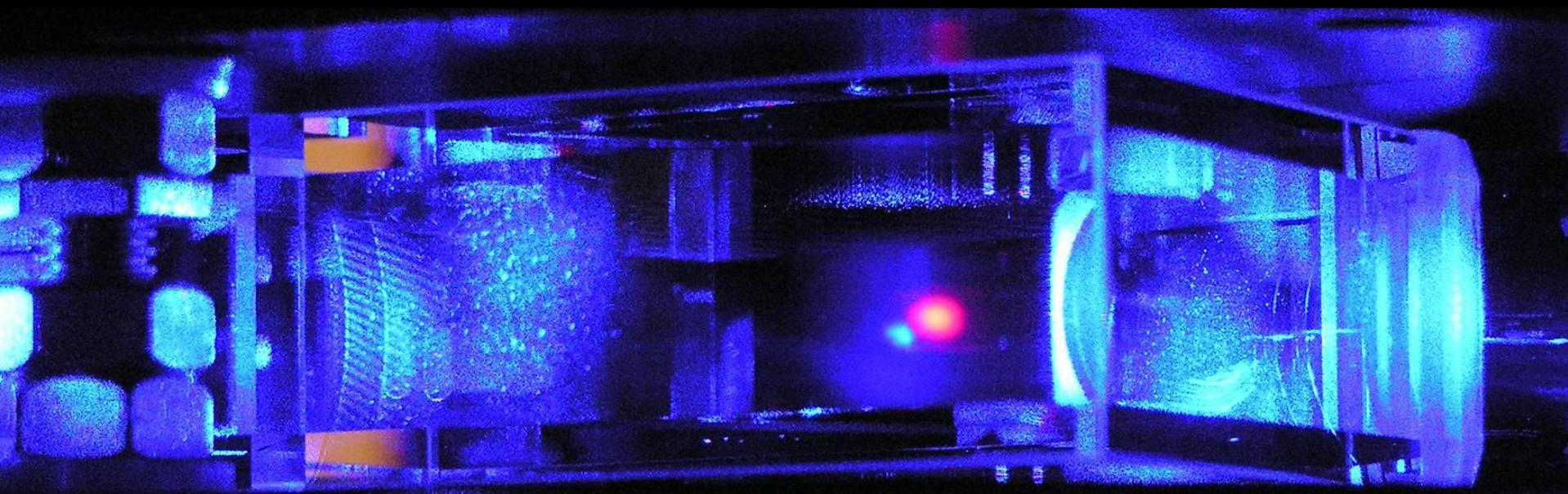
magneto-optically trapped Sr atoms (461nm)

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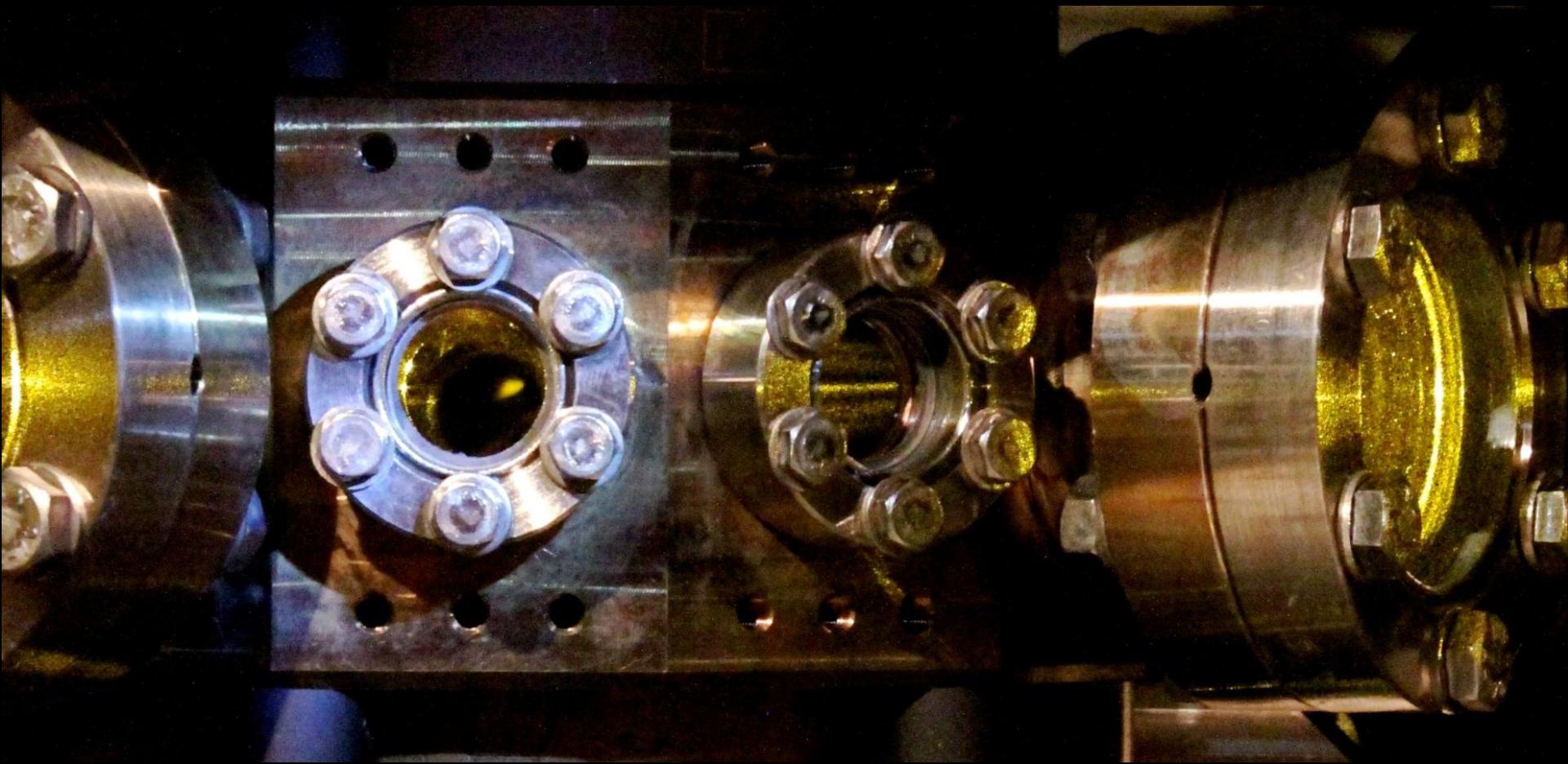
Sr and Li: two-species MOT (461nm and 671nm)

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magneto-optically trapped erbium (583nm)

ultracold.atoms



ultracold group in Innsbruck (April 2011)

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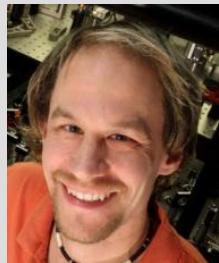


4 PIs



Hanns-Christoph Nägele

Cs - ground-state molecules
1D quantum gases
RbCs - heteronuc. molecules



Florian Schreck

Sr - quantum simulations
RbSr - ground state molecules



Francesca
Ferlaino

Er - new, strongly
dipolar quantum gas

Cs - few-body physics

LiK - Fermi-Fermi mixtures

RG



Li - fermionic spin mixtures

mysterious Efimov quantum states

СЛАБОСВЯЗАННЫЕ СОСТОЯНИЯ ТРЕХ РЕЗОНАНСНО
ВЗАИМОДЕЙСТВУЮЩИХ ЧАСТИЦ

В. И. ЕФИМОВ

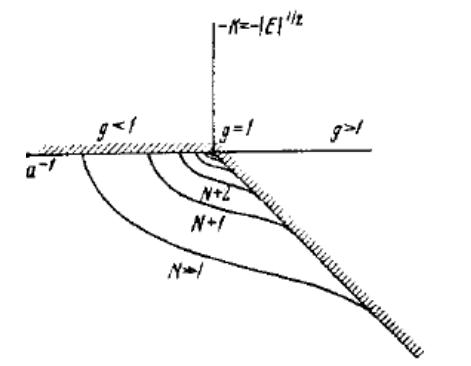
ФИЗИКО-ТЕХНИЧЕСКИЙ ИНСТИТУТ им. А. Ф. ИОФФЕ
АКАДЕМИИ НАУК СССР

(Поступила в редакцию 16 февраля 1970 г.)

Показано, что при достаточной резонансности парных сил у трех тождественных частиц возникает семейство связанных состояний малой энергии. Квантовые числа всех состояний одинаковы: для бесспиновых бозонов 0^+ , для нуклонов $1/2^+$, $T = 1/2$. Резонансные состояния лежат выше радиуса парных сил. Наиболее благоприятные условия уровней имеют место для трех бесспиновых нейтральных бозонов — для заряженных частиц и частиц со спином и изоспином — возможность существования таких уровней в системе трех а-частиц нуклонов (H^3).



Рис. 1. Спектр уровней трех бесспиновых нейтральных частиц. Штриховкой показана граница непрерывного спектра трех частиц. Соседние траектории уровней отличаются только преобразованием масштаба приблизительно в 22 раза. В целях наглядности это соотношение на рисунке не выдержано



SOVIET JOURNAL OF NUCLEAR PHYSICS

VOLUME 12, NUMBER 5

MAY, 1971

WEAKLY-BOUNDED STATES OF THREE RESONANTLY-INTERACTING PARTICLES

V. N. EFIMOV

A. F. Ioffe Physico-technical Institute, USSR Academy of Sciences

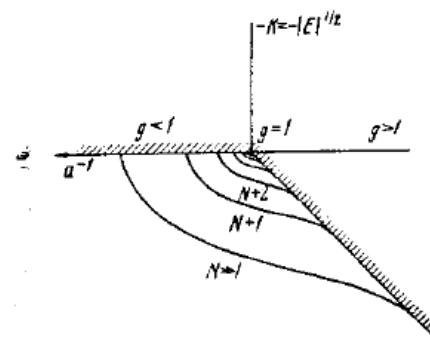
Submitted February 16, 1970

Yad. Fiz. 12, 1080–1091 (November, 1970)

It is shown that if the pair forces of three identical particles are sufficiently resonant, a family of bound states of low energy is produced. The quantum numbers of all the states are the same: for nucleons $\frac{1}{2}^+$, $T = \frac{1}{2}$. The dimension of the states is larger than the most favorable conditions for the appearance of a family of levels for neutral bosons: the conditions are less favorable for charged particles with spin. The possibility of existence of such levels in a system of three pions and of three nucleons (H^3) is considered.



FIG. 1. Level spectrum of three spinless neutral particles. The cross hatching denotes the boundary of the continuous spectrum of the three particles. Neighboring level trajectories differ only in a scale transformation by an approximate factor of 22. For clarity, this ratio is not maintained in the figure.



Efimov observations in three-body systems



three identical bosons

^{133}Cs (Innsbruck)

Kraemer et al., Nature **440**, 315 (2006)

Knoop et al., Nature Phys. **5**, 227 (2009)

^7Li (Ramat Gan, Rice)

Gross et al., PRL **103**, 163202 (2009)

Pollack et al., Science **326**, 1683 (2009)

^{39}K (Florence)

Zaccanti et al., Nature Phys. **5**, 586 (2009)

^{85}Rb (Boulder)

Wild et al., arXiv:1112.0362

three-component spin mixture of fermions

^6Li (Heidelberg, Penn State Univ., U Tokyo)

Ottenstein et al., PRL **101**, 203202 (2008)

Huckans et al., PRL **102**, 165302 (2009)

Williams et al., PRL **103**, 130404 (2009)

Lompe et al., Science **330**, 940 (2010)

Nakajima et al., PRL **106**, 143201 (2011)

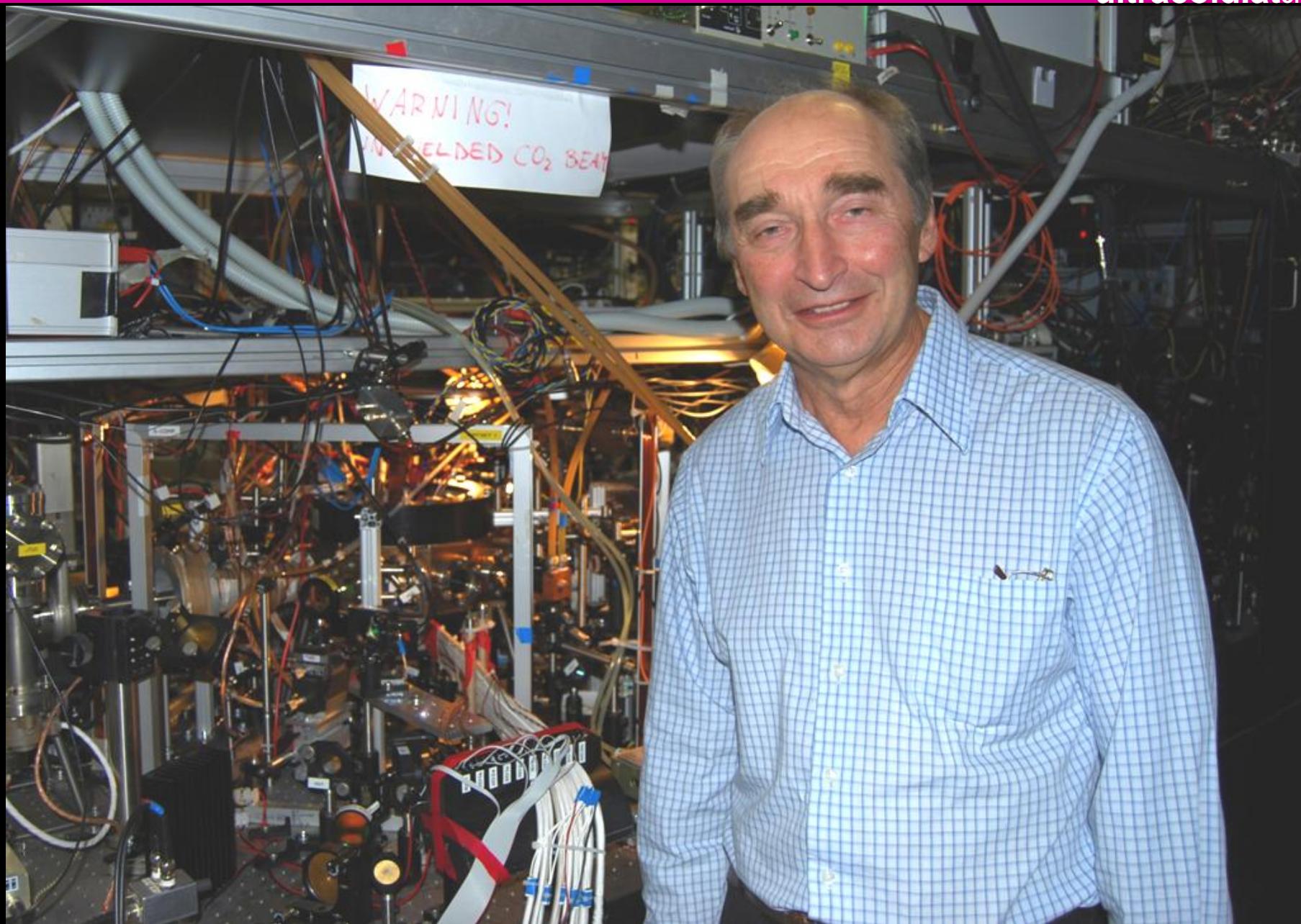
Bose-Bose mixture

$^{41}\text{K} - ^{87}\text{Rb}$ (Florence)

Barontini et al., PRL **043201** (2009)

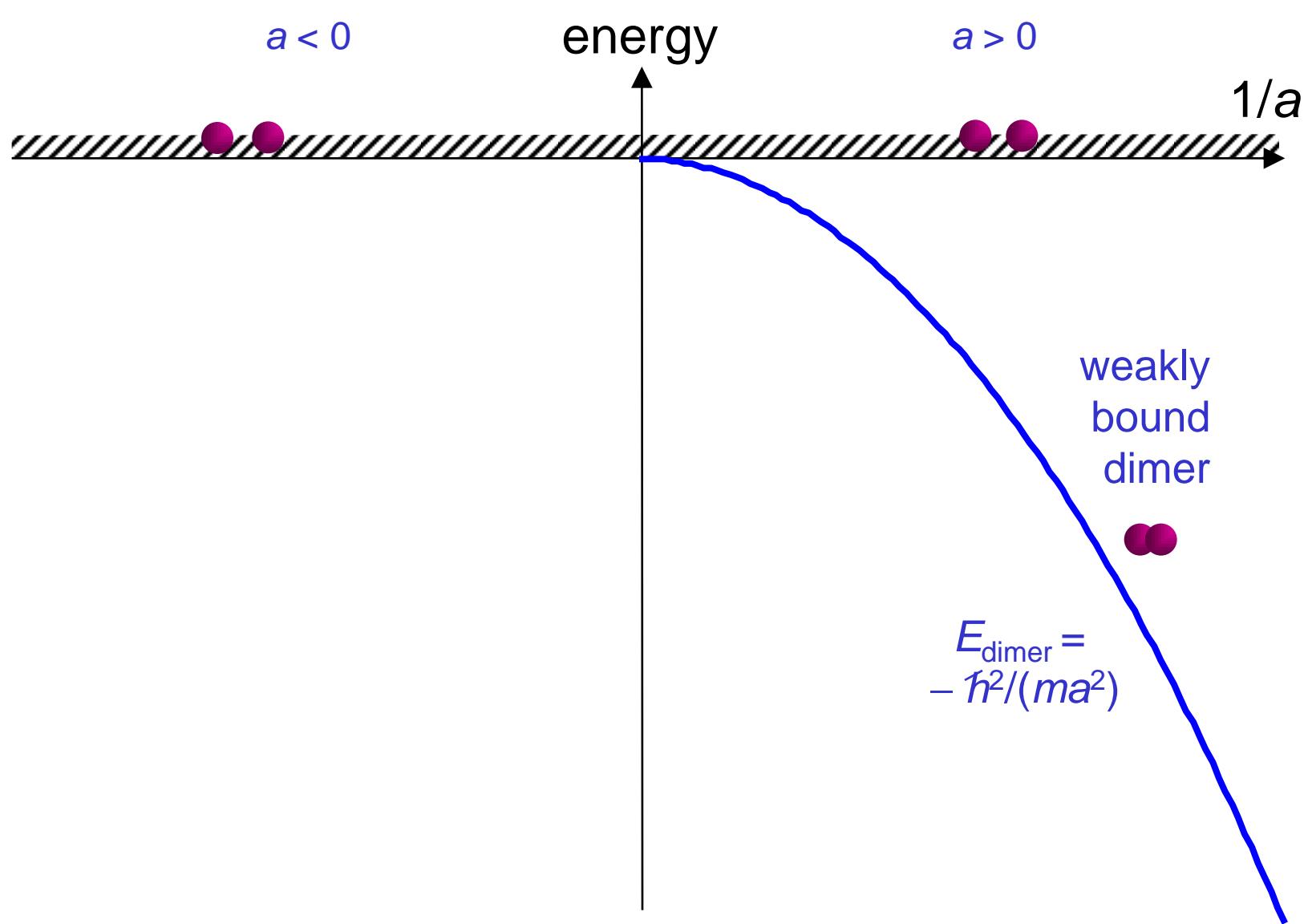
Vitaly Efimov visiting Innsbruck, 23 Oct 2009

ultracold.at_{oms}



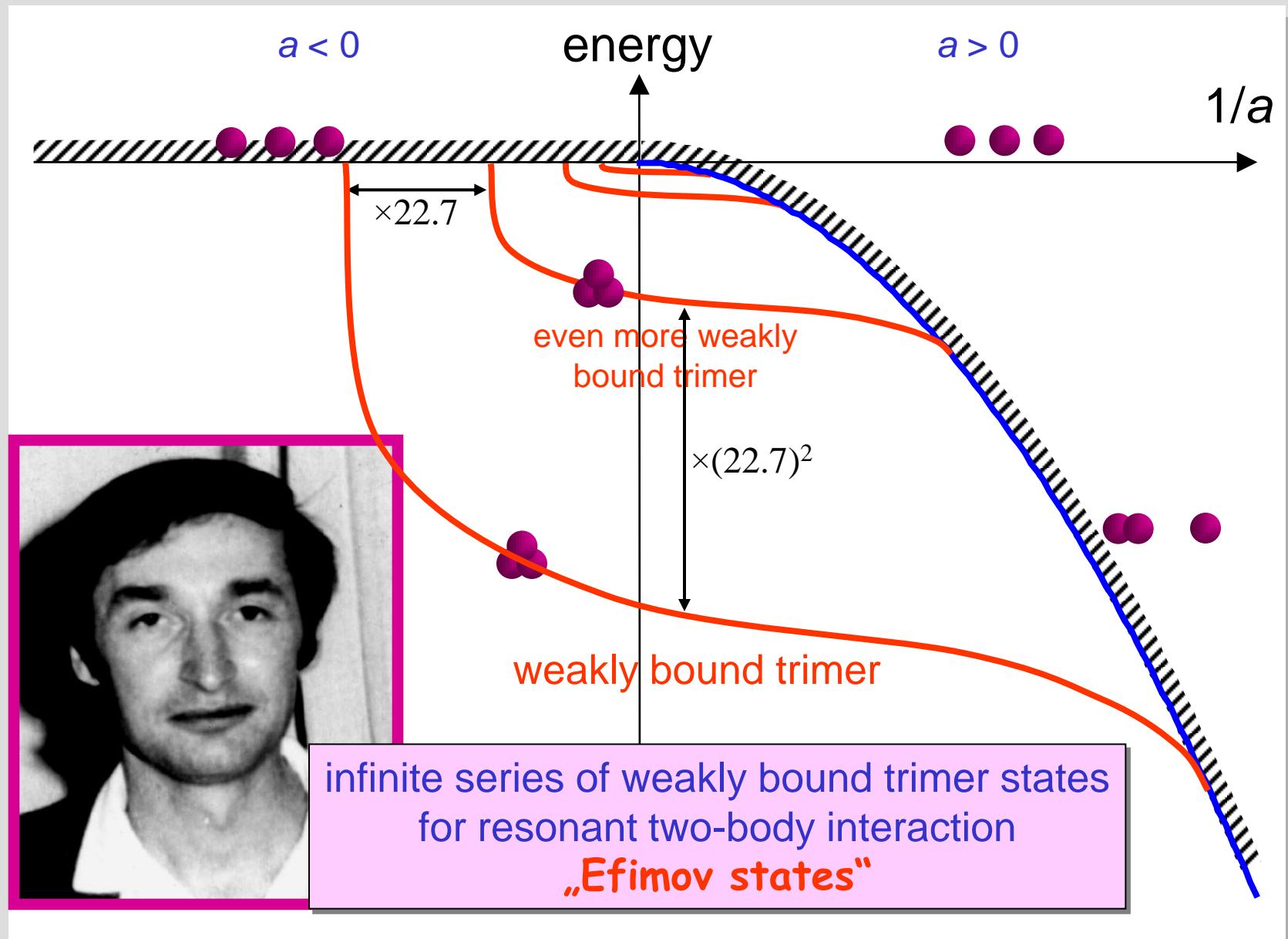
quantum states near two-body resonance

ultracold.at_{oms}



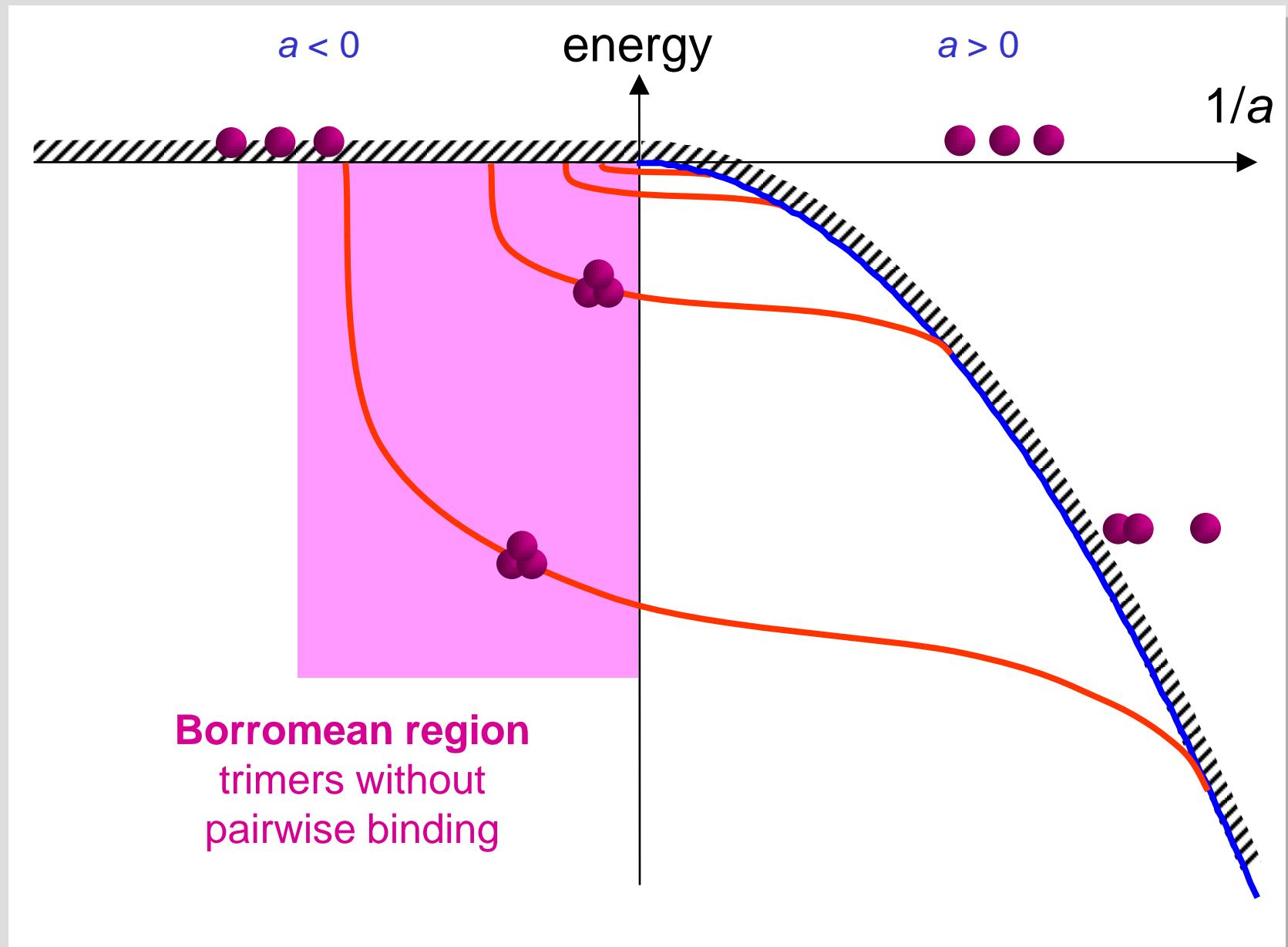
quantum states near two-body resonance

ultracold.atoms



Efimov states: Borromean region

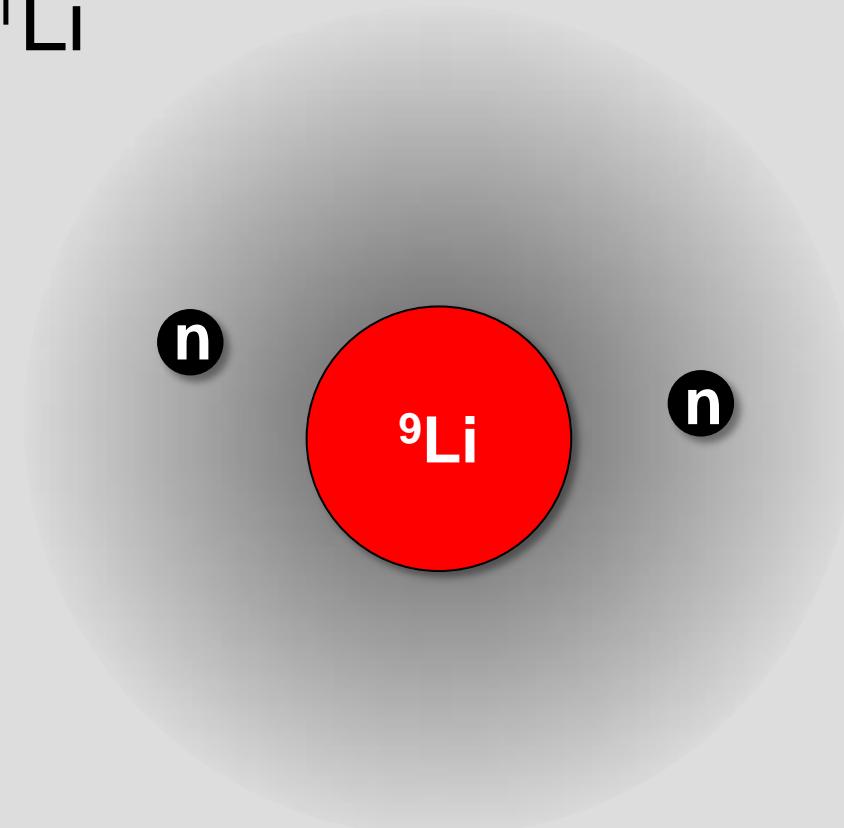
ultracold.atoms



Borromean states in nuclear physics

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^{11}Li

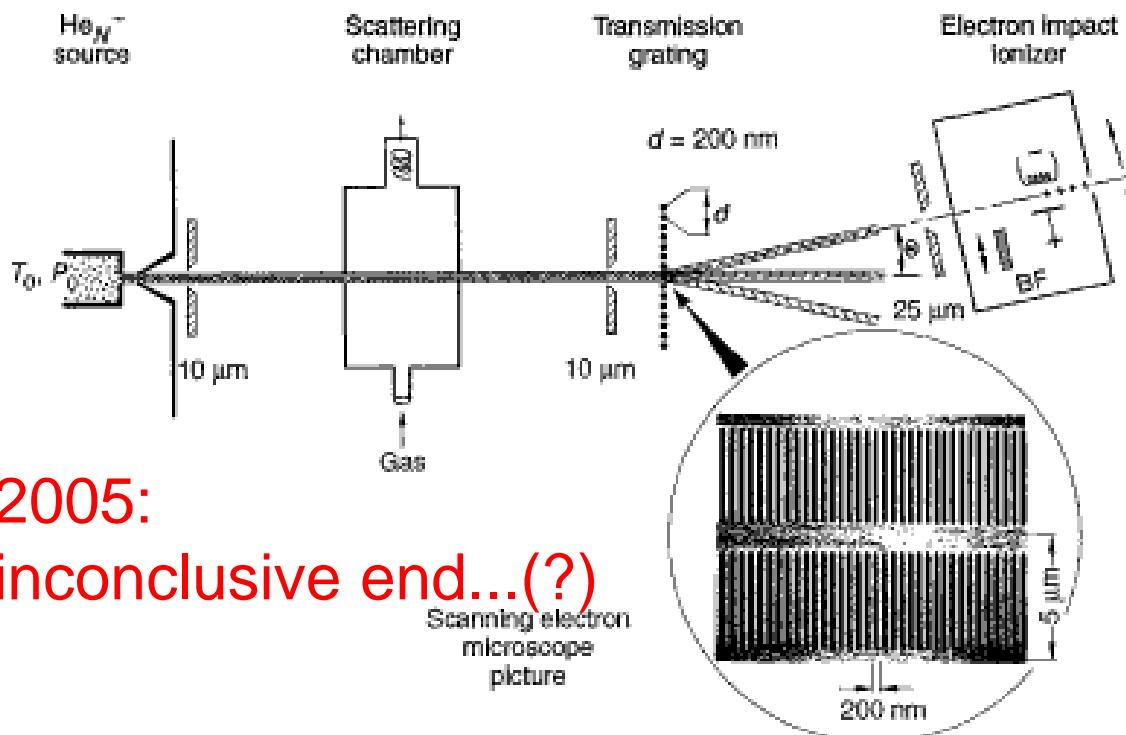


review on halo states in nuclear physics:

Jensen, Riisager, Fedorov, Rev. Mod. Phys. 76, 215 (2004)

Nondestructive Mass Selection of Small van der Waals Clusters

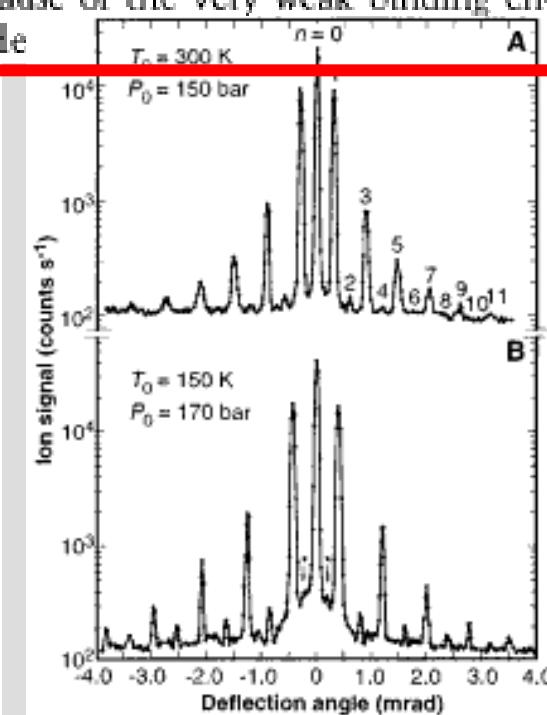
Wieland Schöllkopf and J. Peter Toennies



2005:
inconclusive end... (?)

Fig. 1. Schematic diagram of the apparatus used for diffraction of the different components in a He cluster beam. Only the vacuum system containing the ionizer is indicated. BF designates the beam flag that intercepts the incident beam in the stagnation mode measurements. The inset (bottom right) shows a scanning electron microscope picture of the grating used (10, 11).

ters. This large enhancement is of considerable interest in connection with the question of the existence of Efimov states. In 1970, Efimov (19) first predicted that three bosons will have an infinite number of special long-range bound states, which are now called Efimov states, in the limit that the two-body interaction approaches zero binding energy. So far, Efimov states have not been found in nuclear systems, but there is now some evidence that they may exist for He_3 because of the very weak binding energy of He



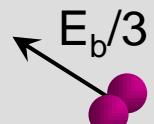
three-body recombination

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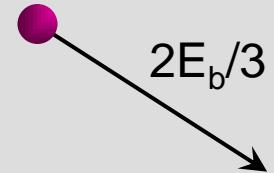
elementary
process



three atoms



dimer + free atom



$2E_b/3$

causes trap loss → our observable

three-body recomb. theory basics

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$$\dot{n} = -L_3 n^3$$

L_3 : three-body loss coefficient [cm⁶/s]

dimensional analysis

$$L_3 = 3 C \frac{\hbar}{m} \overset{\text{dimensionless}}{\underset{\uparrow}{a}}^4$$

a⁴ - scaling !
very strong
dependence on
scattering length

valid if a exceeds all other length scales
(vdW length of molecular potential, typ. 30 – 100a₀)
good near a Feshbach resonance

early theory paper:

Fedichev *et al.*, PRL 77, 2921 (1996), a⁴ scaling with $C = 3.9$

review: Braaten and Hammer, Phys. Rep. (2006)

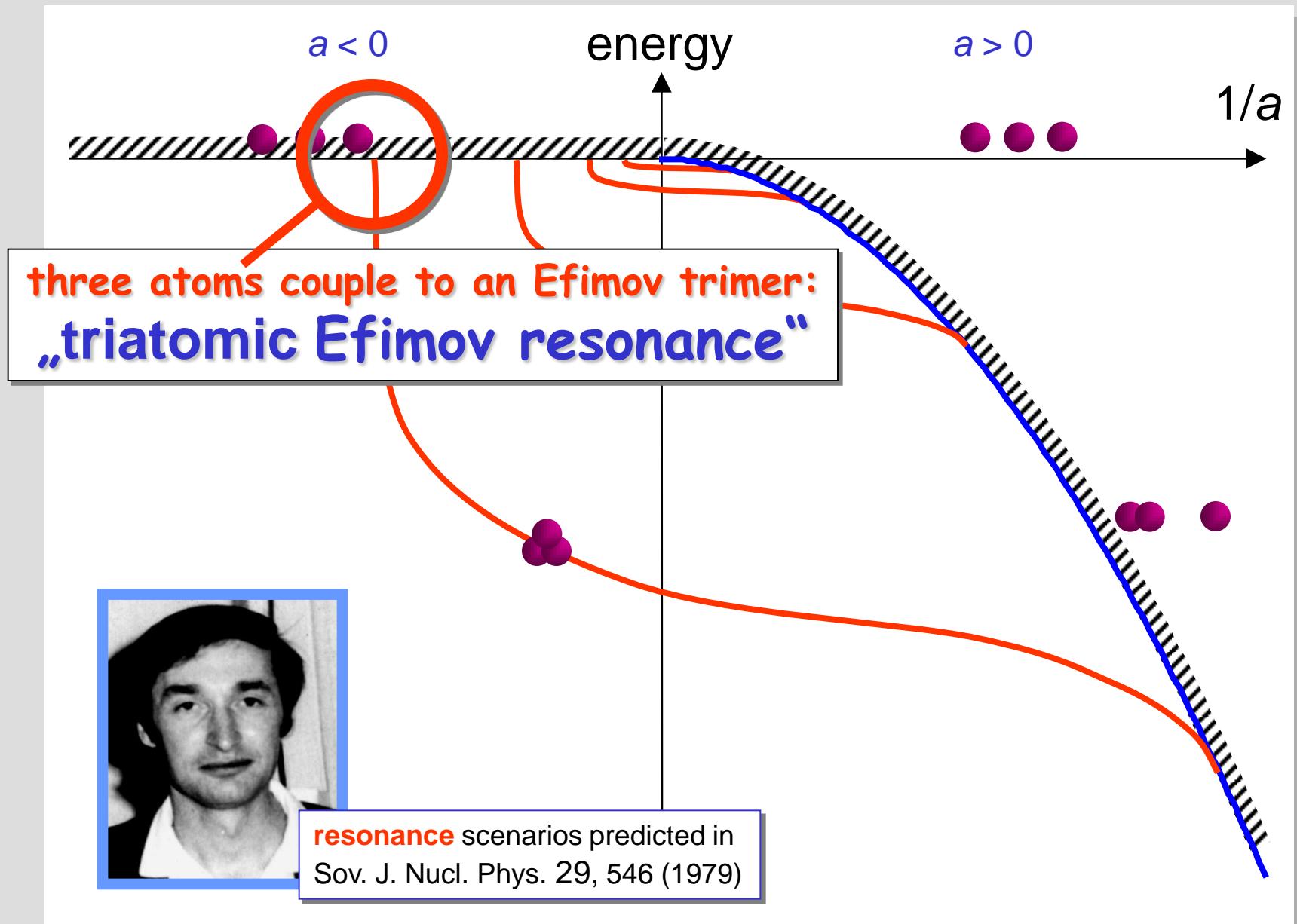
$$C(a) = C(22.7a)$$

analytic expression available, based on effective-field theory

need two parameters:
three-body parameter (universal)
decay parameter (non-universal)

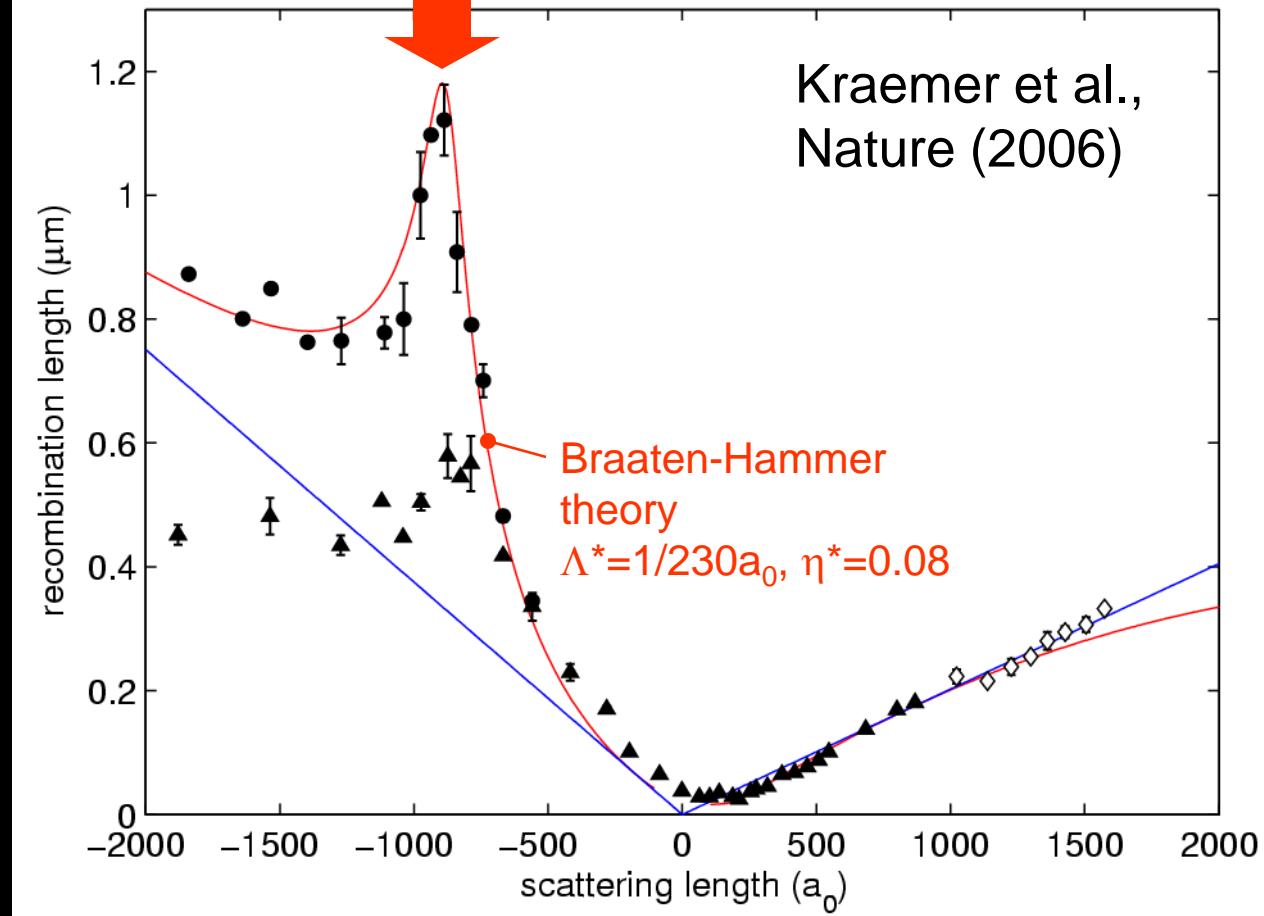
Efimov resonances

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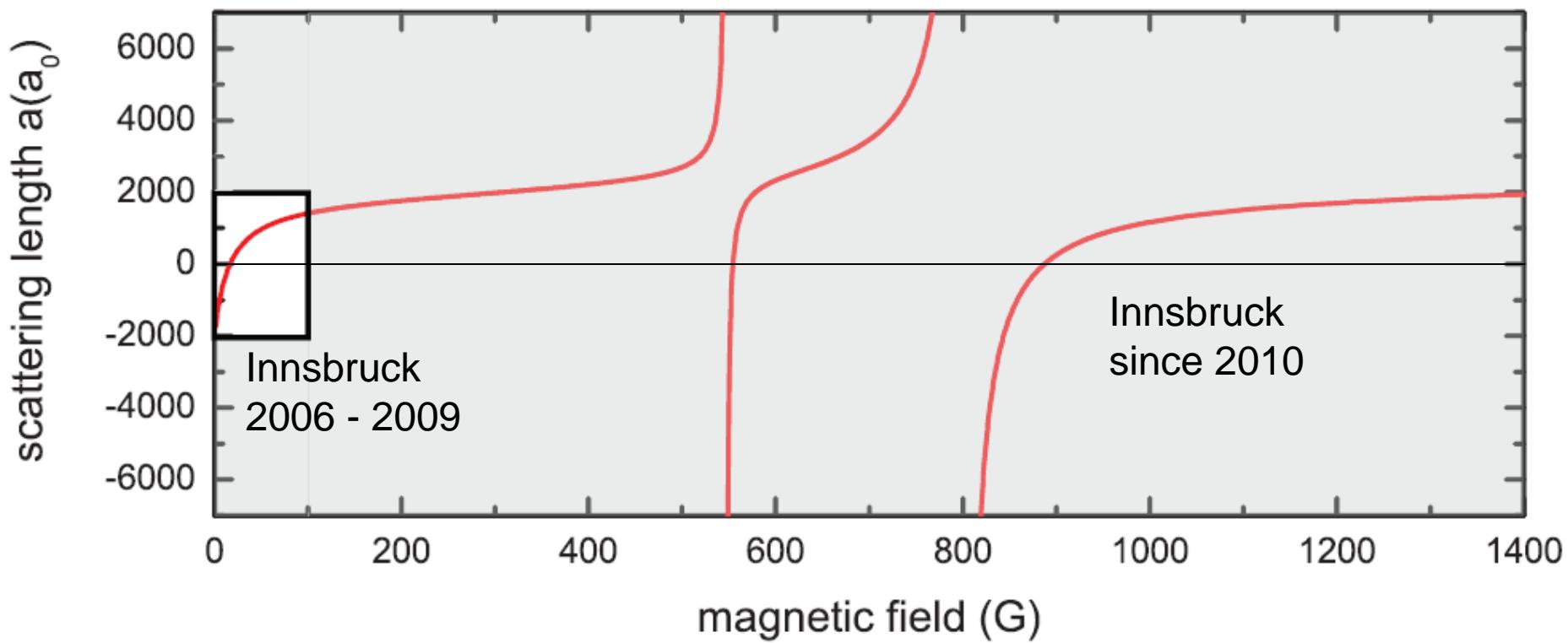


$$\rho_3 = \left(\frac{2}{\sqrt{3}} \frac{m}{\hbar} L_3 \right)^{1/4}$$

Efimov resonance

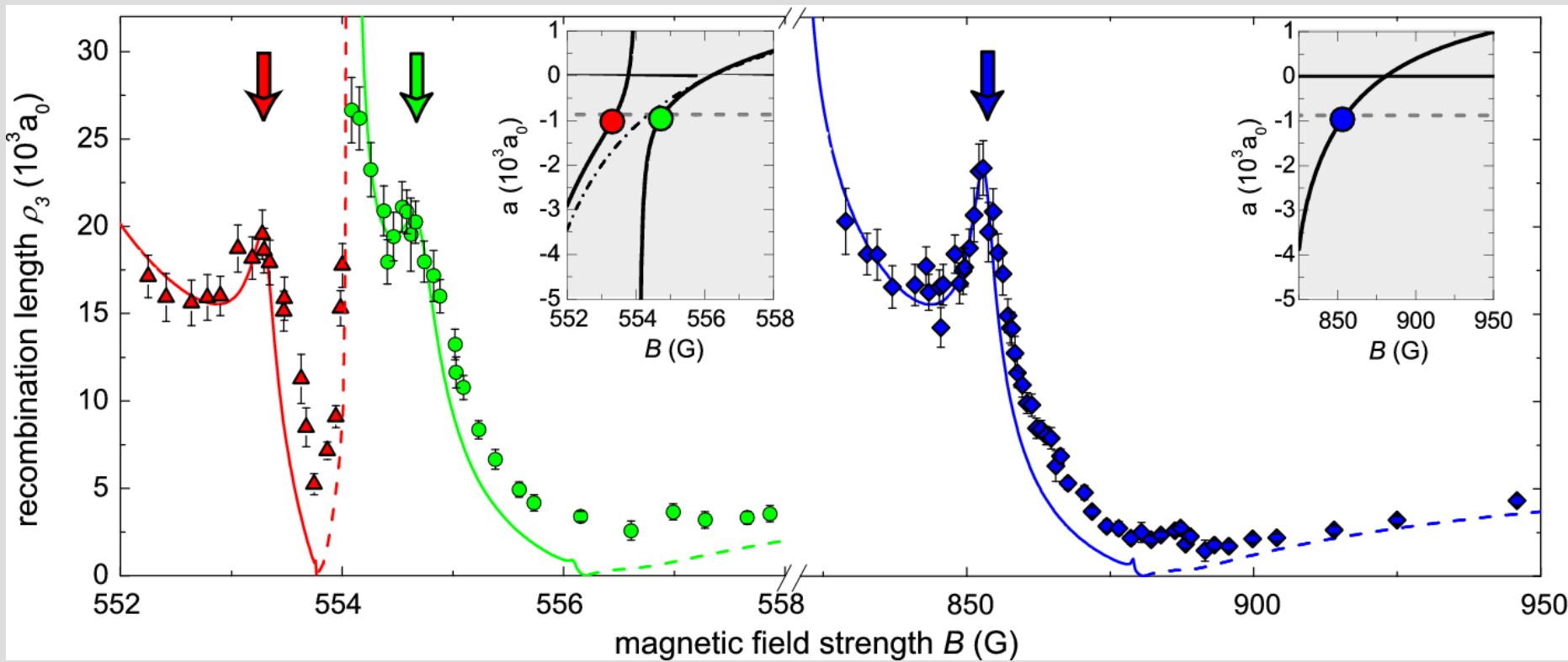


three broad s-wave FRs



plus many d- and g-wave FRs (not shown)

observation of three new Efimov resonances

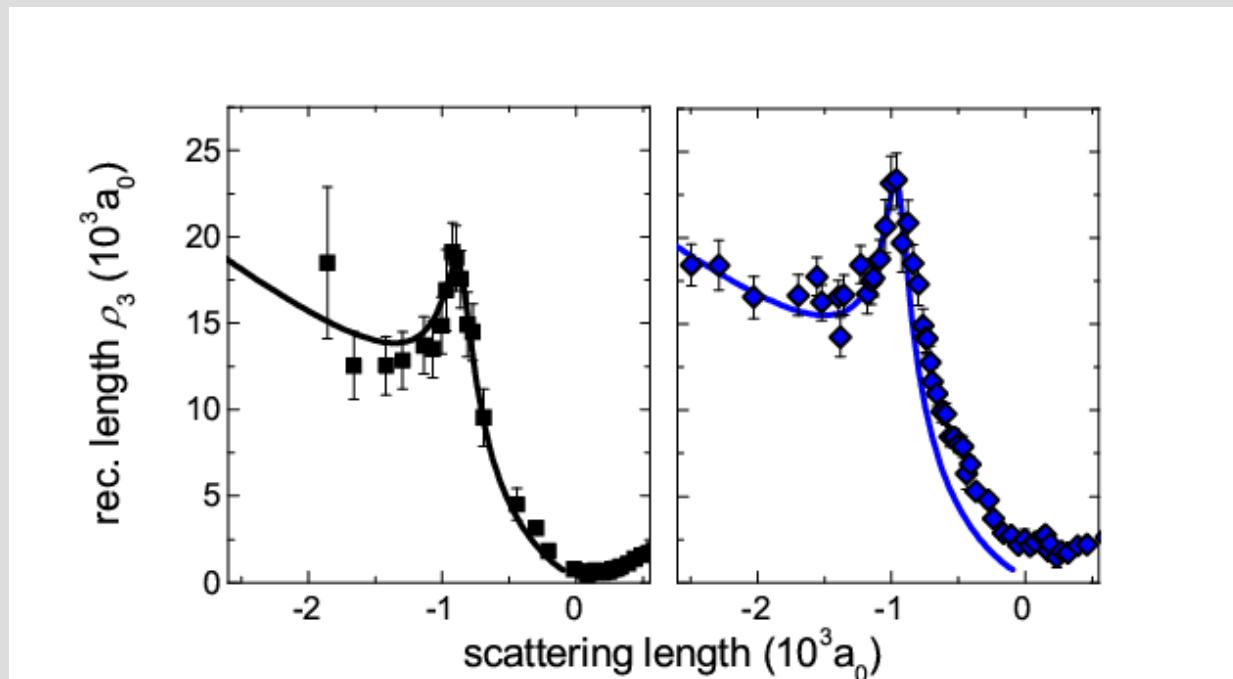


how universal is the three-body parameter?

M. Berninger et al., PRL 107, 120401 (2011)

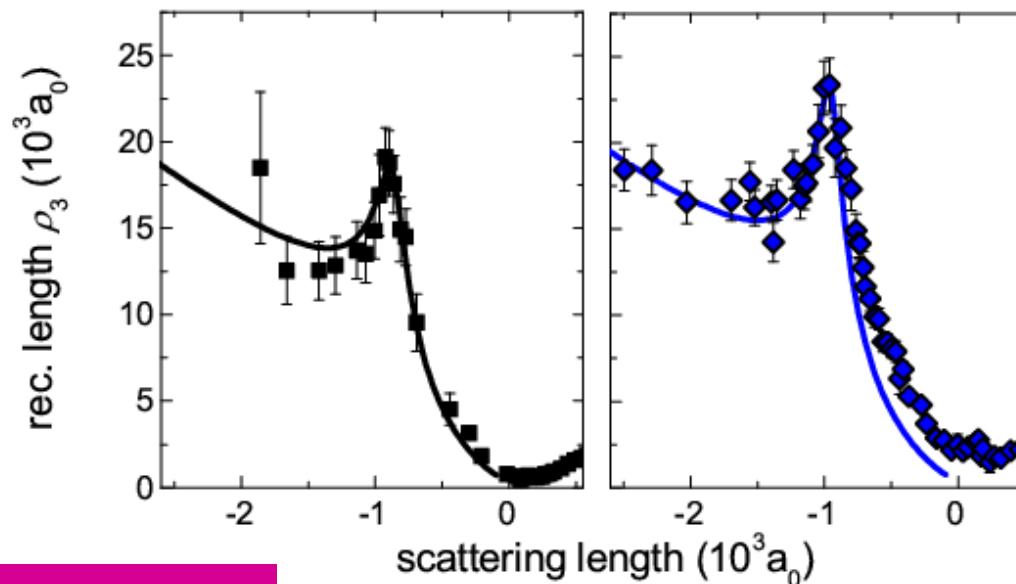
variations of the three-body parameter?

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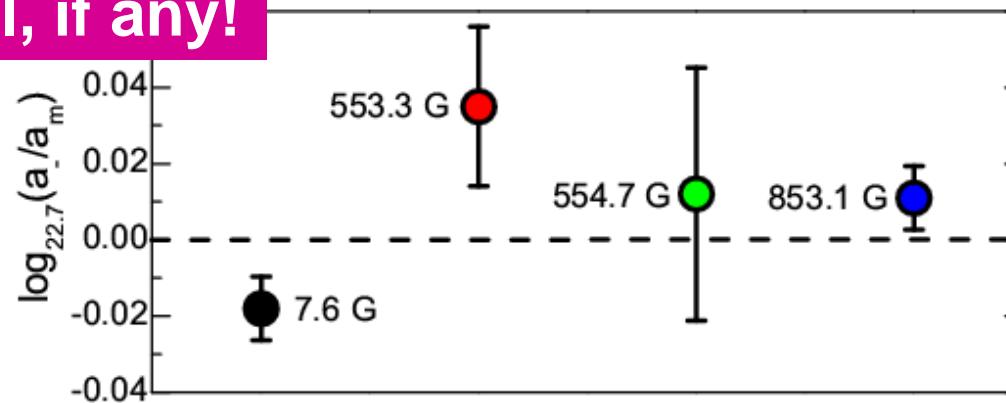


variations of the three-body parameter?

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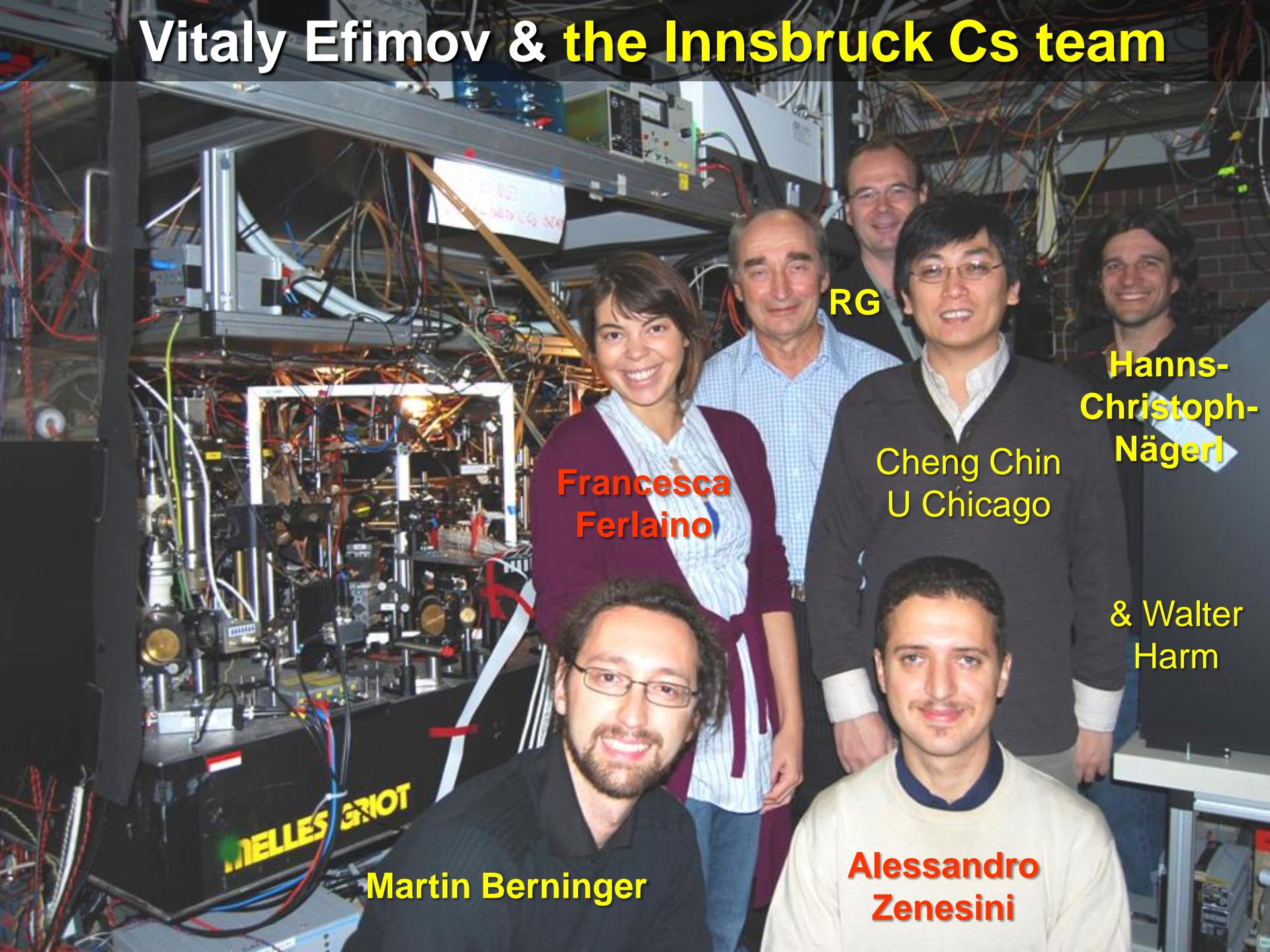


very small, if any!



one tenth of
Efimov period

Vitaly Efimov & the Innsbruck Cs team



Martin Berninger

Alessandro Zenesini

Weakly bound cluster states of Efimov character

Atomic Color Superfluid via Three-Body Loss

Javier von Stecher

A. Kantian,¹ M. Dalmonte,^{1,2} S. Diehl,¹ W. Hofstetter,³ P. Zoller,¹ and A. J. Daley¹

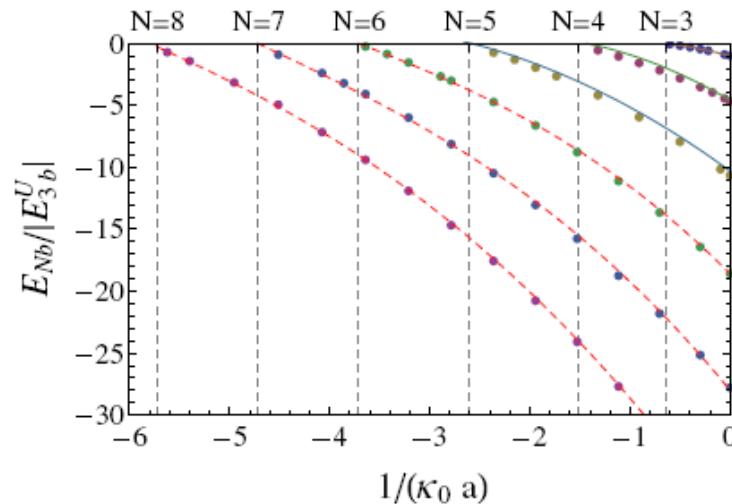


Figure 2. Boson region. Symbols: The numbers after dashed lines correspond to $N = 5$, the solid curve corresponds to CG predictions using our model Hamiltonian. Dashed curves are fits to an analytic simple form (see the text).

**few-body interactions important
to understand and control many-body physics**

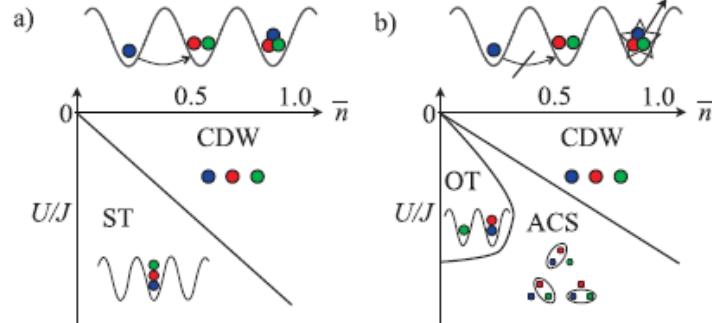
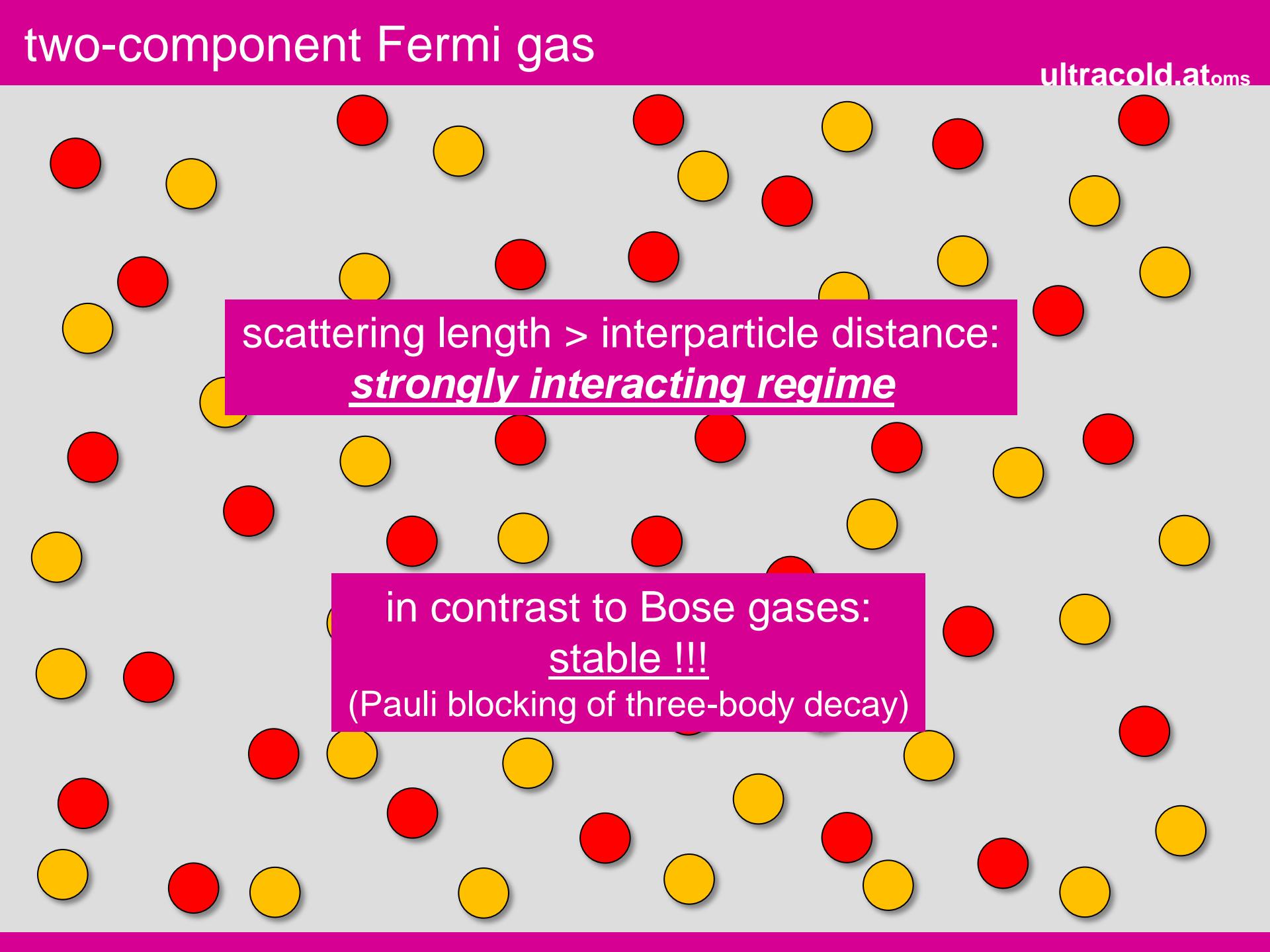


FIG. 1 (color online). Qualitative phase diagram for attractive interactions $U < 0$ and equal populations $\bar{n}/3$ of each component in a three-component 1D Fermi gas. These are shown in the SU(3) symmetric case (where all pairwise interactions between

and without and from three-competition competes a charge-density wave (CDW). The hard-core constraint suppresses trion formation, stabilizing BCS pairing in an atomic color superfluid (ACS), which competes with a CDW and off-site trions (OT).

Strongly interacting Fermi gases

two-component Fermi gas

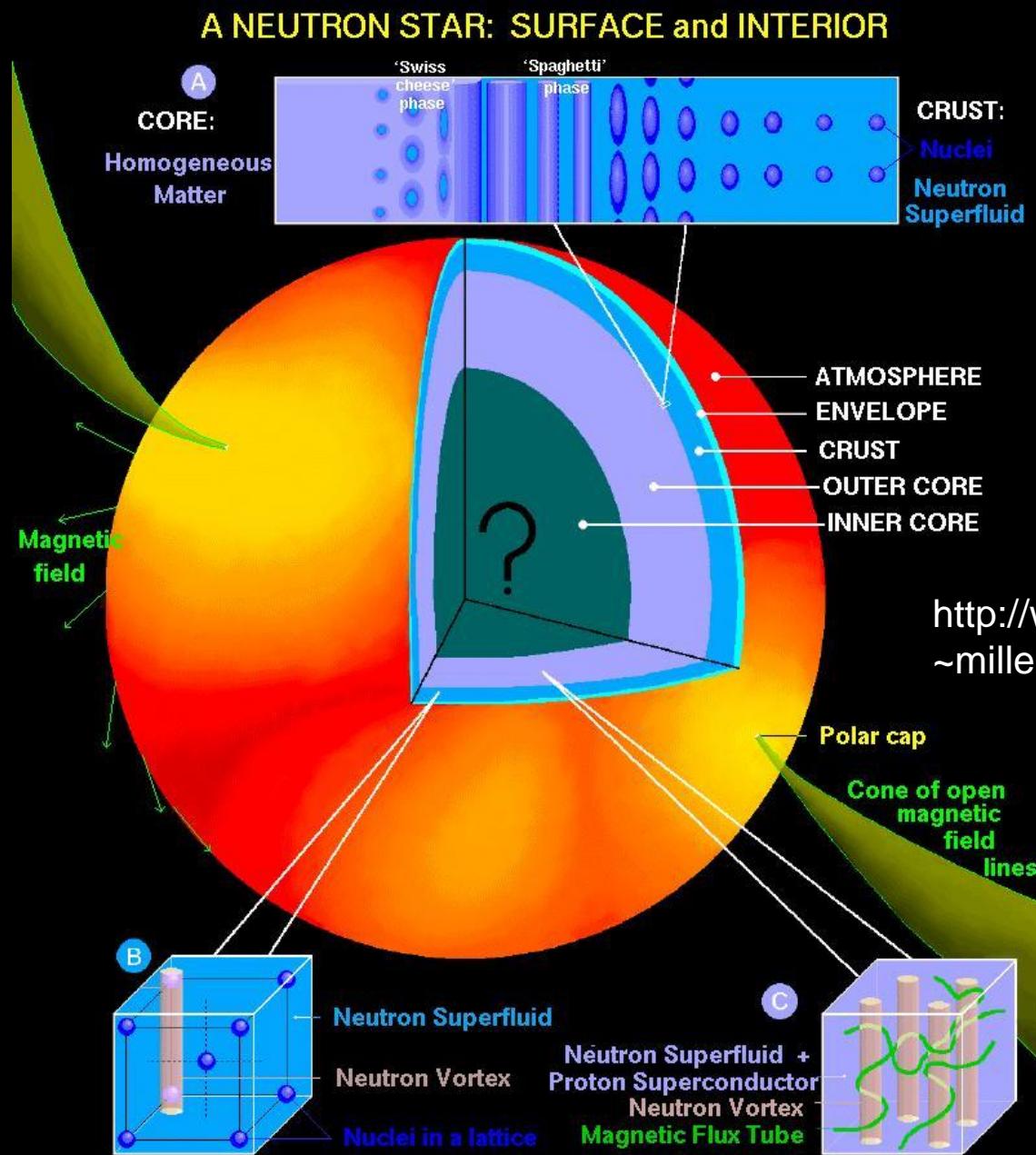


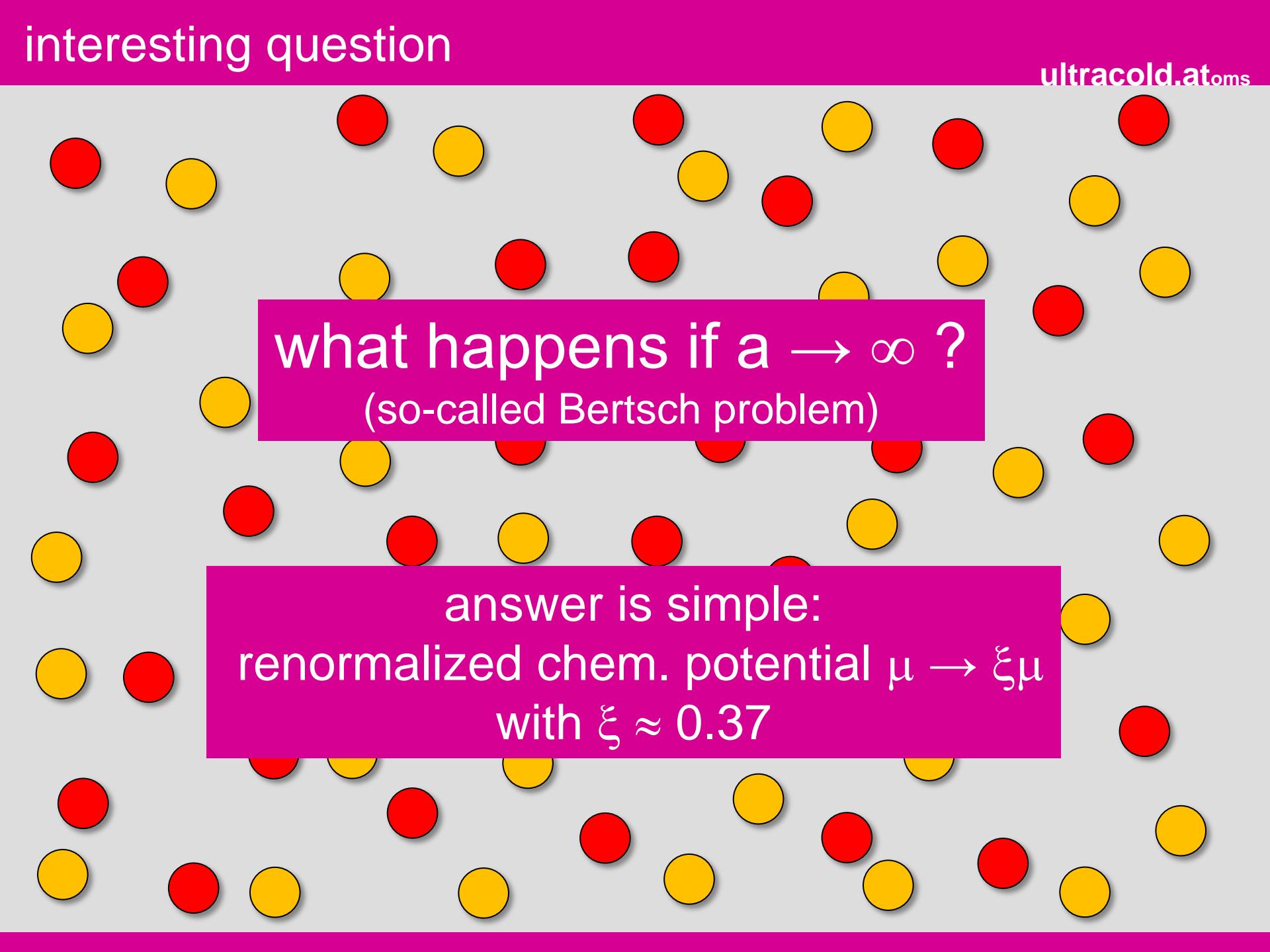
scattering length > interparticle distance:
strongly interacting regime

in contrast to Bose gases:
stable !!!
(Pauli blocking of three-body decay)

neutron star

ultracold.atoms





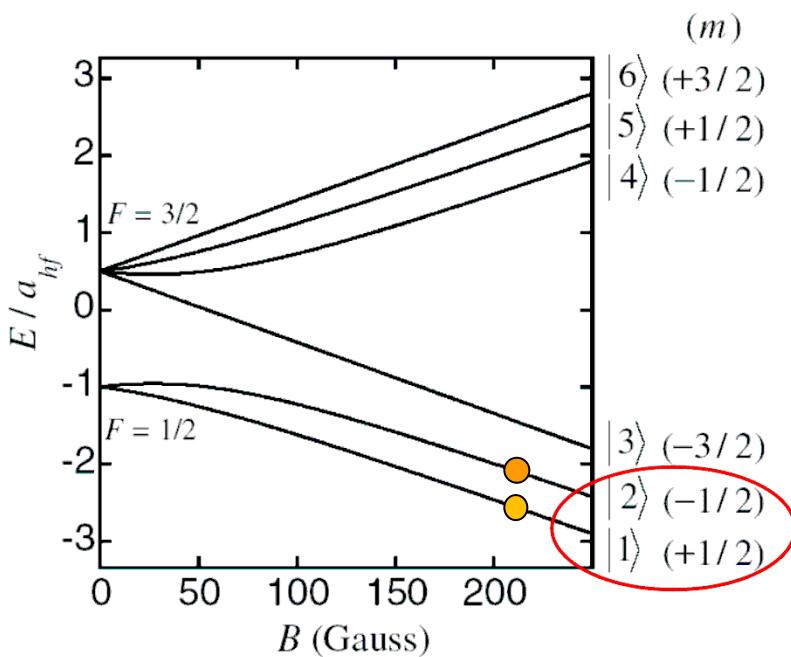
what happens if $a \rightarrow \infty$?
(so-called Bertsch problem)

answer is simple:
renormalized chem. potential $\mu \rightarrow \xi\mu$
with $\xi \approx 0.37$

^6Li spin mixture

ultracold.atoms

^6Li ground state in a magnetic field



*spin mixture of
two lowest states
stable against
two-body decay*

Feshbach resonance

prediction: Houbiers et al., PRA 57, R1497 (1998)

precise characterization:

Bartenstein et al., PRL 94, 103201 (2005)

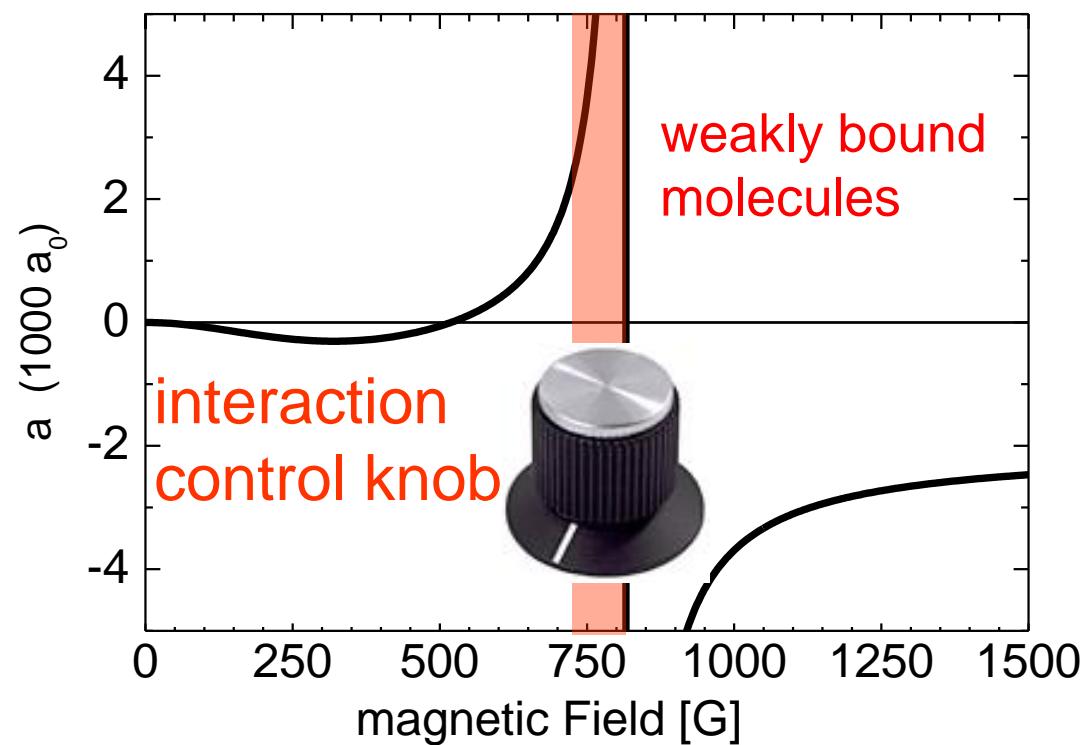
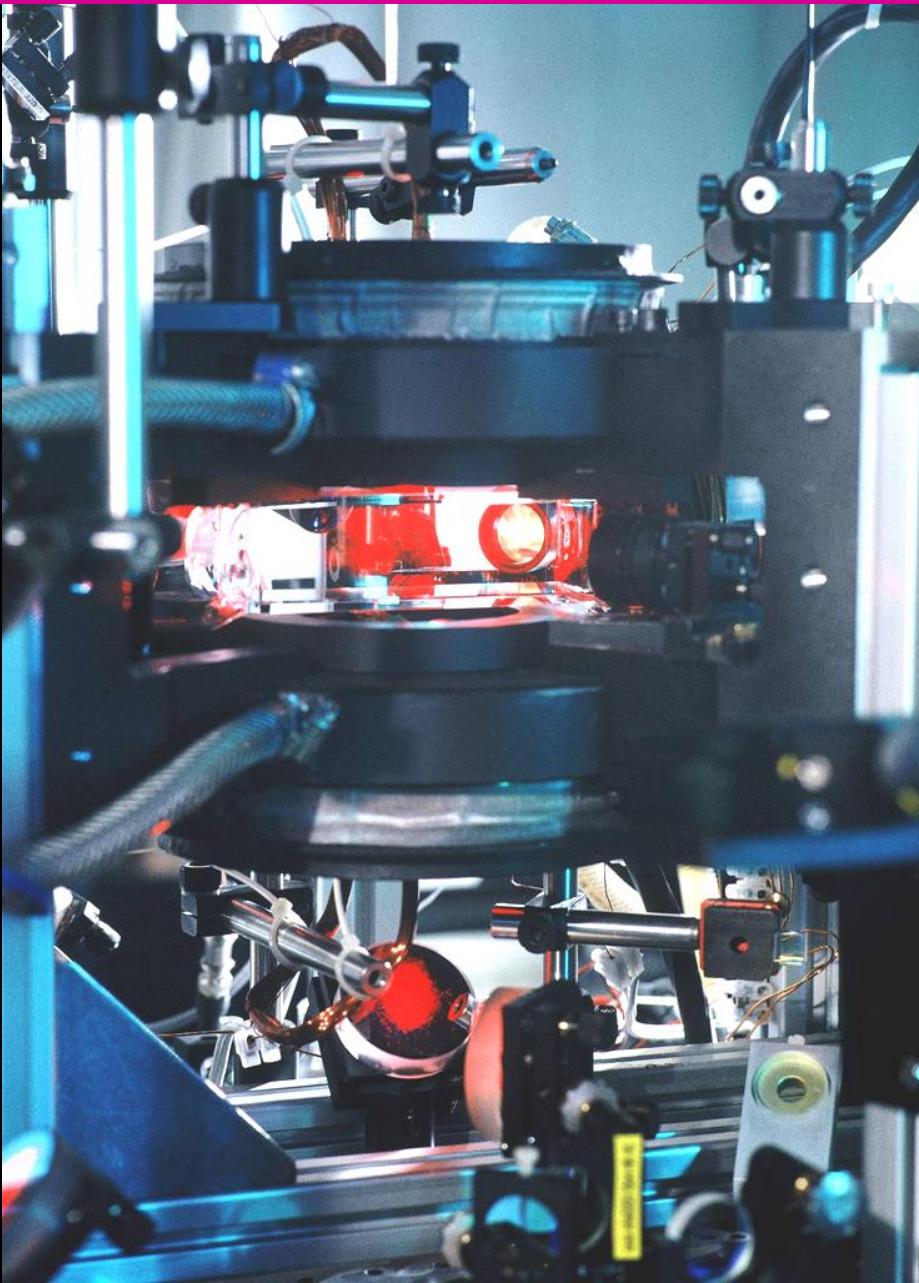


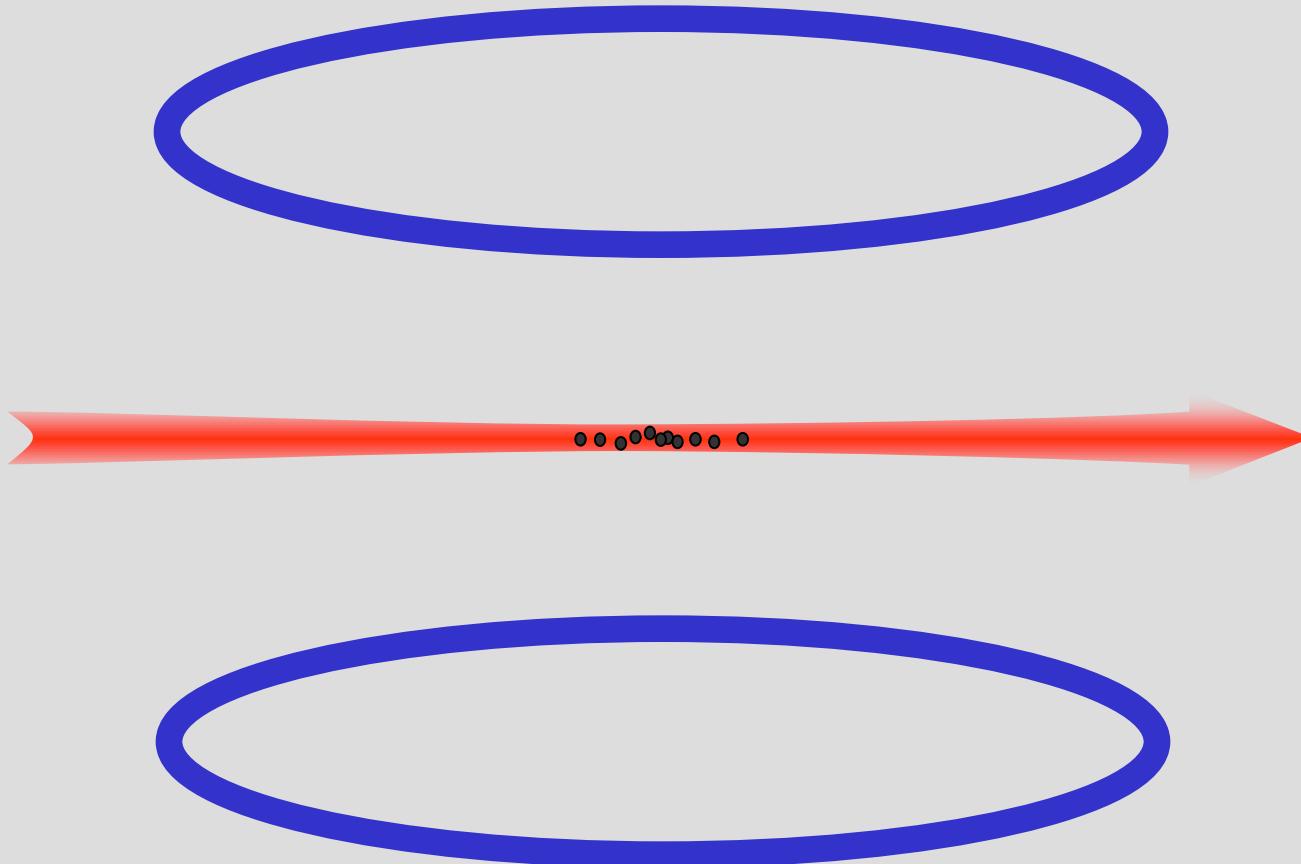
table-top trapping apparatus

ultracold.atoms



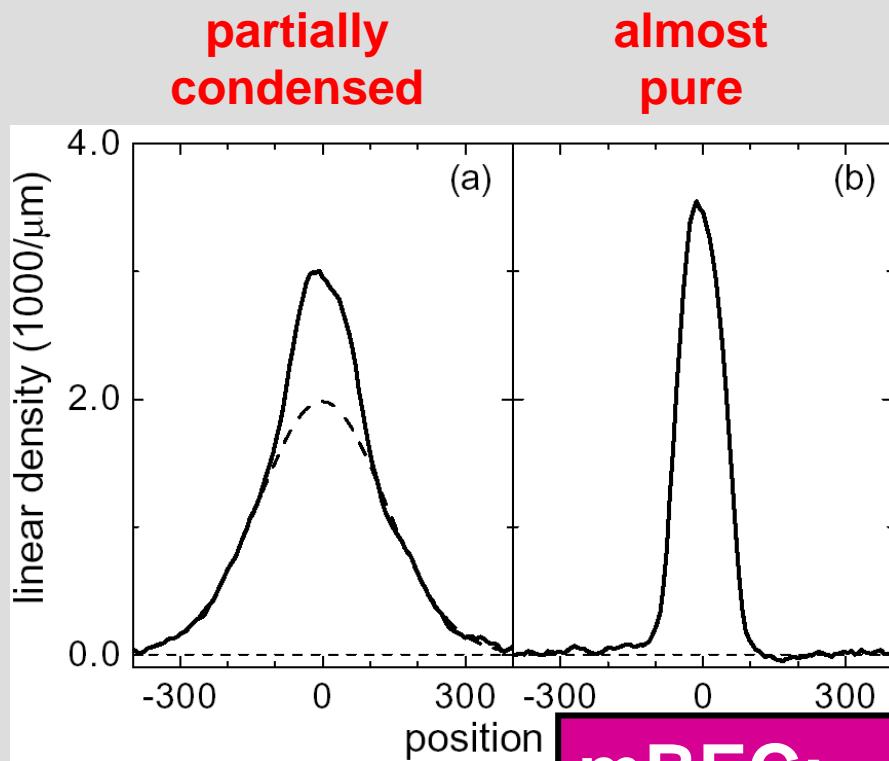
optical trap for evaporative cooling

ultracold.at_{oms}



BEC of molecules

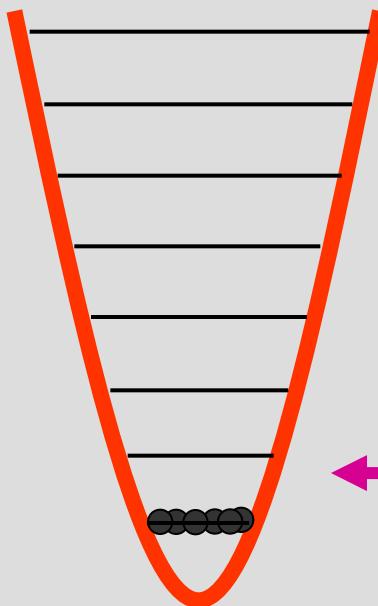
ultracold.atoms



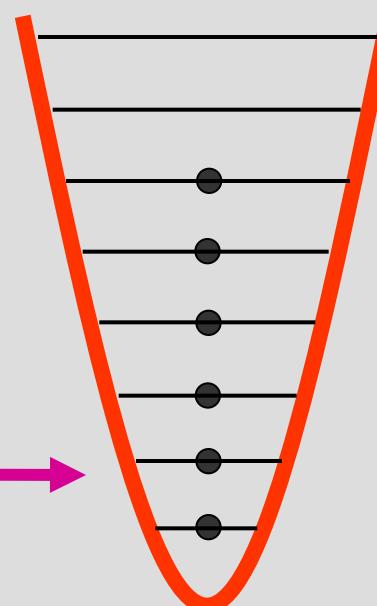
final trap power	28mW
number of molecules	400.000
temperature	430nK
condensate fraction	~20%

mBEC:
excellent starting point
for studies on
BEC-BCS crossover

Bosons
integer spin



Fermions
half-integer spin



trapped atoms
at $T=0$

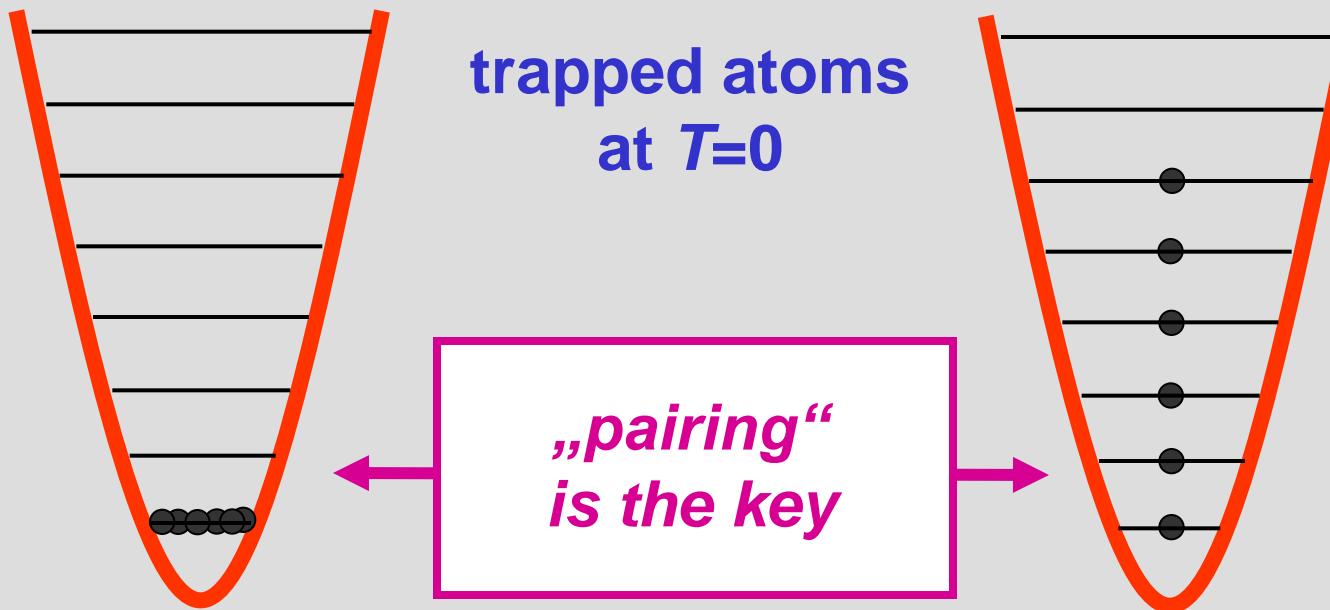
*these two
worlds
are connected !*

all in ground state:
Bose-Einstein condensate

only one particle per state:
degenerate Fermi gas

Bosons
integer spin

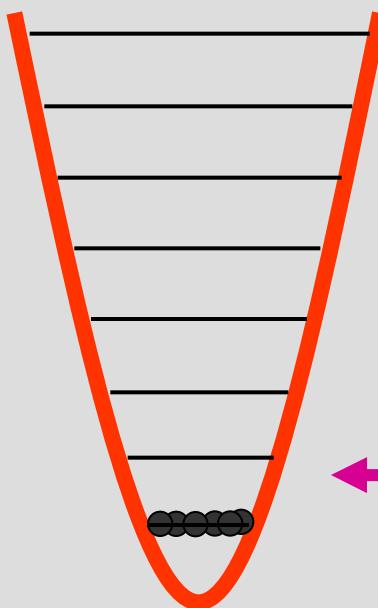
Fermions
half-integer spin



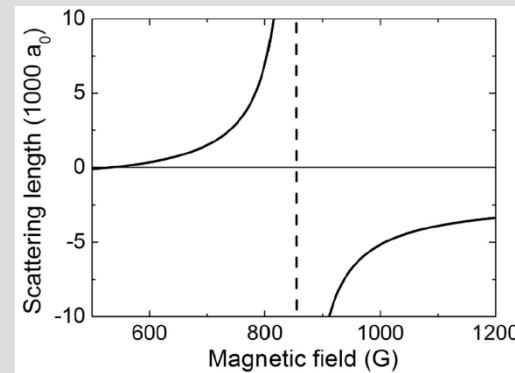
all in ground state:
Bose-Einstein condensate

only one particle per state:
degenerate Fermi gas

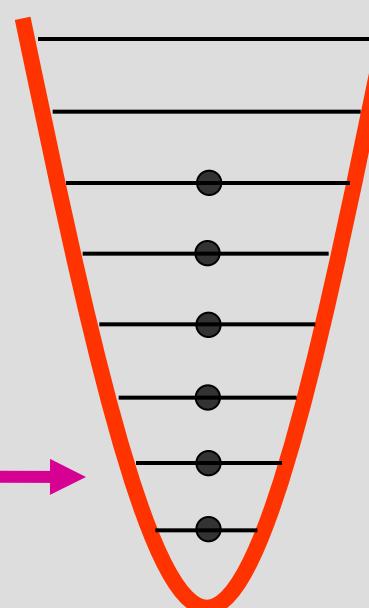
Bosons
integer spin



Feshbach resonance



Fermions
half-integer spin



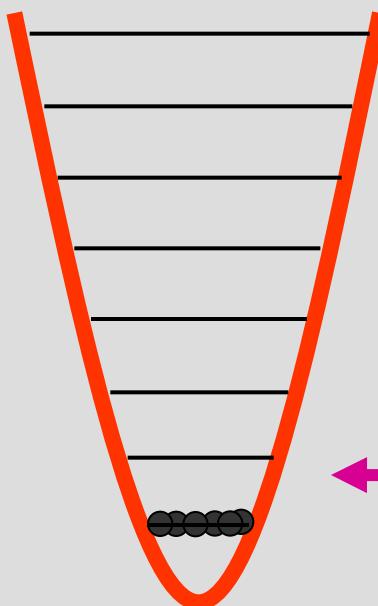
interaction control !!!

all in ground state:
Bose-Einstein condensate

only one particle per state:
degenerate Fermi gas

Bosons

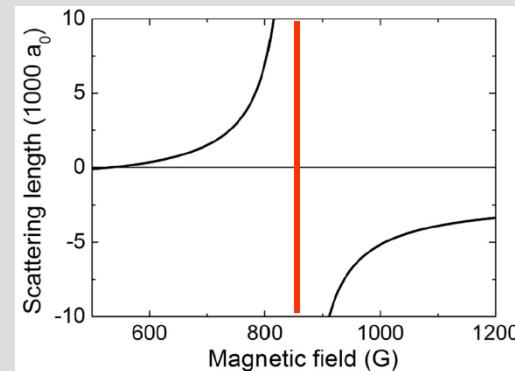
integer spin



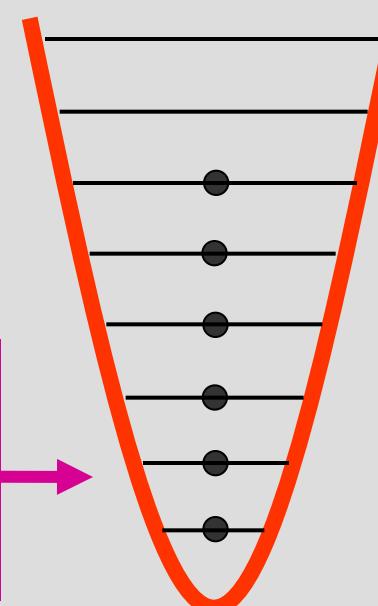
Fermions

half-integer spin

universal !!!



*interaction
control !!!*

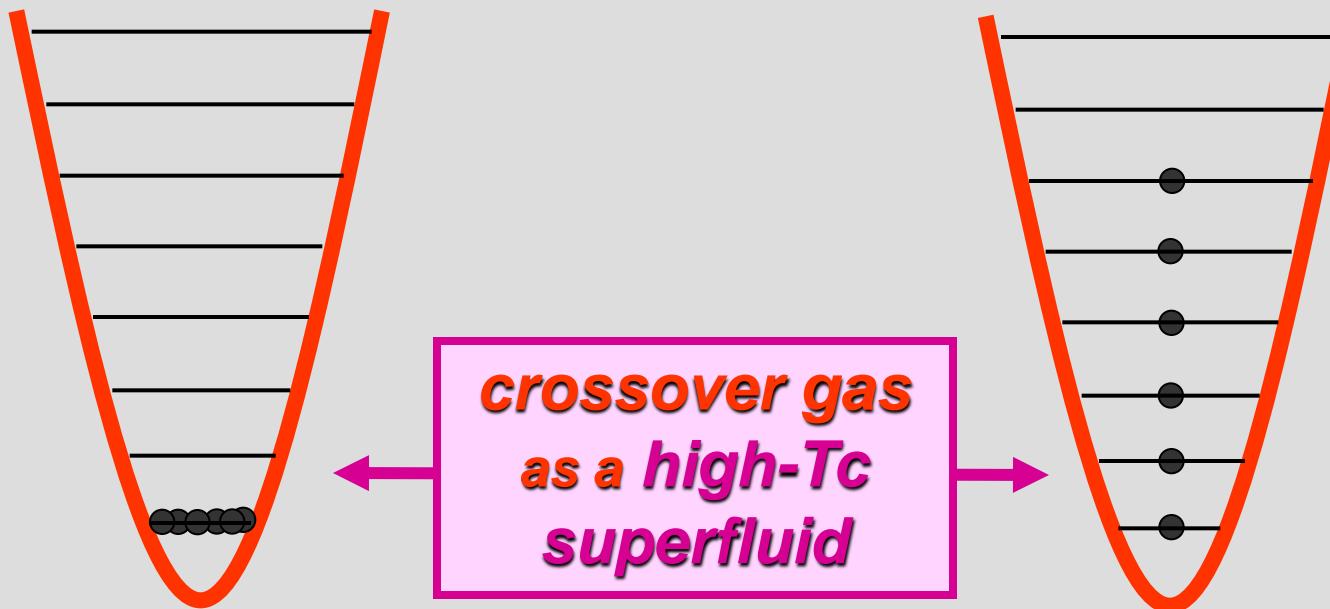


all in ground state:
Bose-Einstein condensate

only one particle per state:
degenerate Fermi gas

Bosons
integer spin

Fermions
half-integer spin



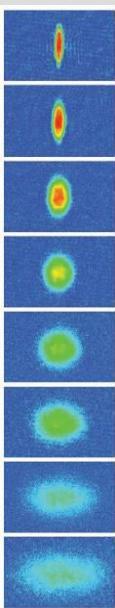
all in ground state:
Bose-Einstein condensate

only one particle per state:
degenerate Fermi gas

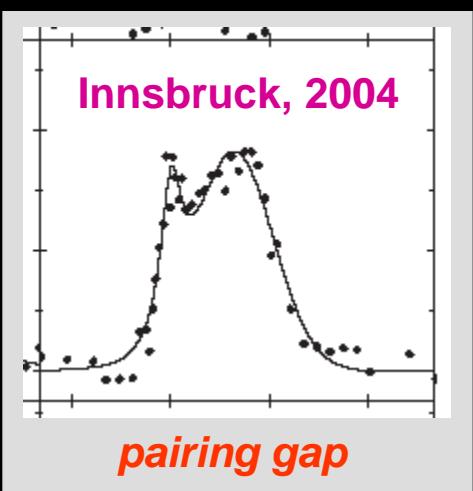
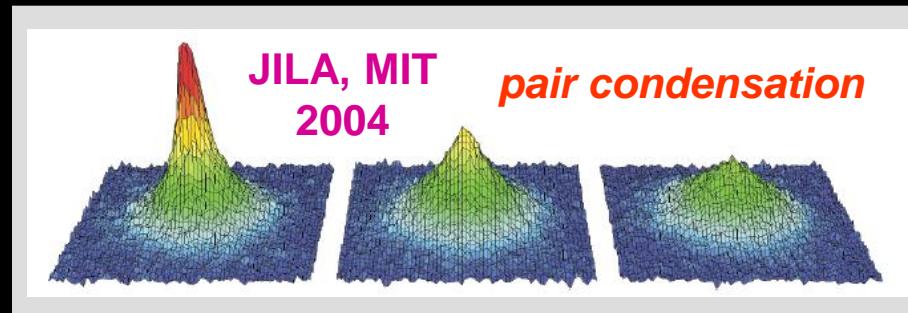
establishing superfluidity

ultracold.atoms

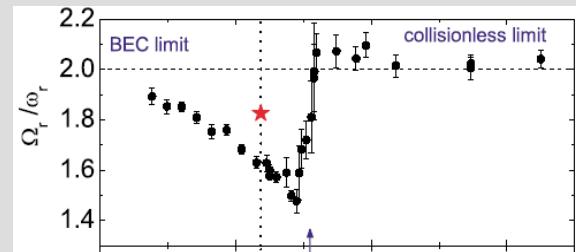
Duke, 2002



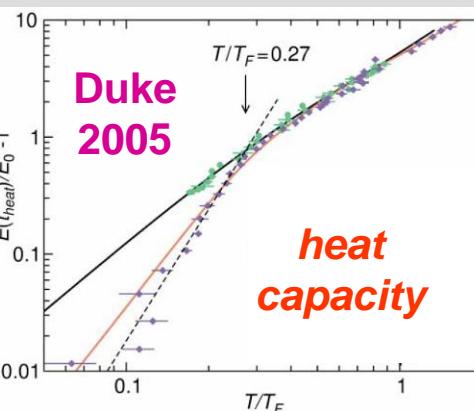
hydrodynamic
expansion



Duke, Innsbruck, 2004

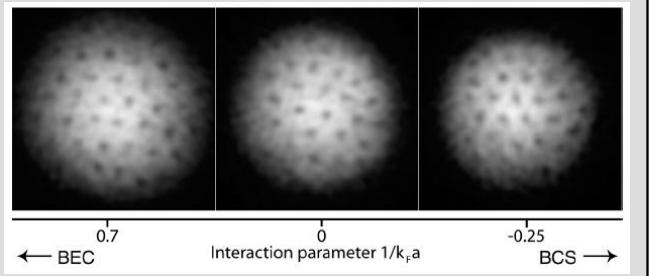


collective modes



MIT, 2005

vortices



**BEC-BCS crossover well understood,
remarkable benchmark for many-body theories**

“high-T_c” superfluidity established

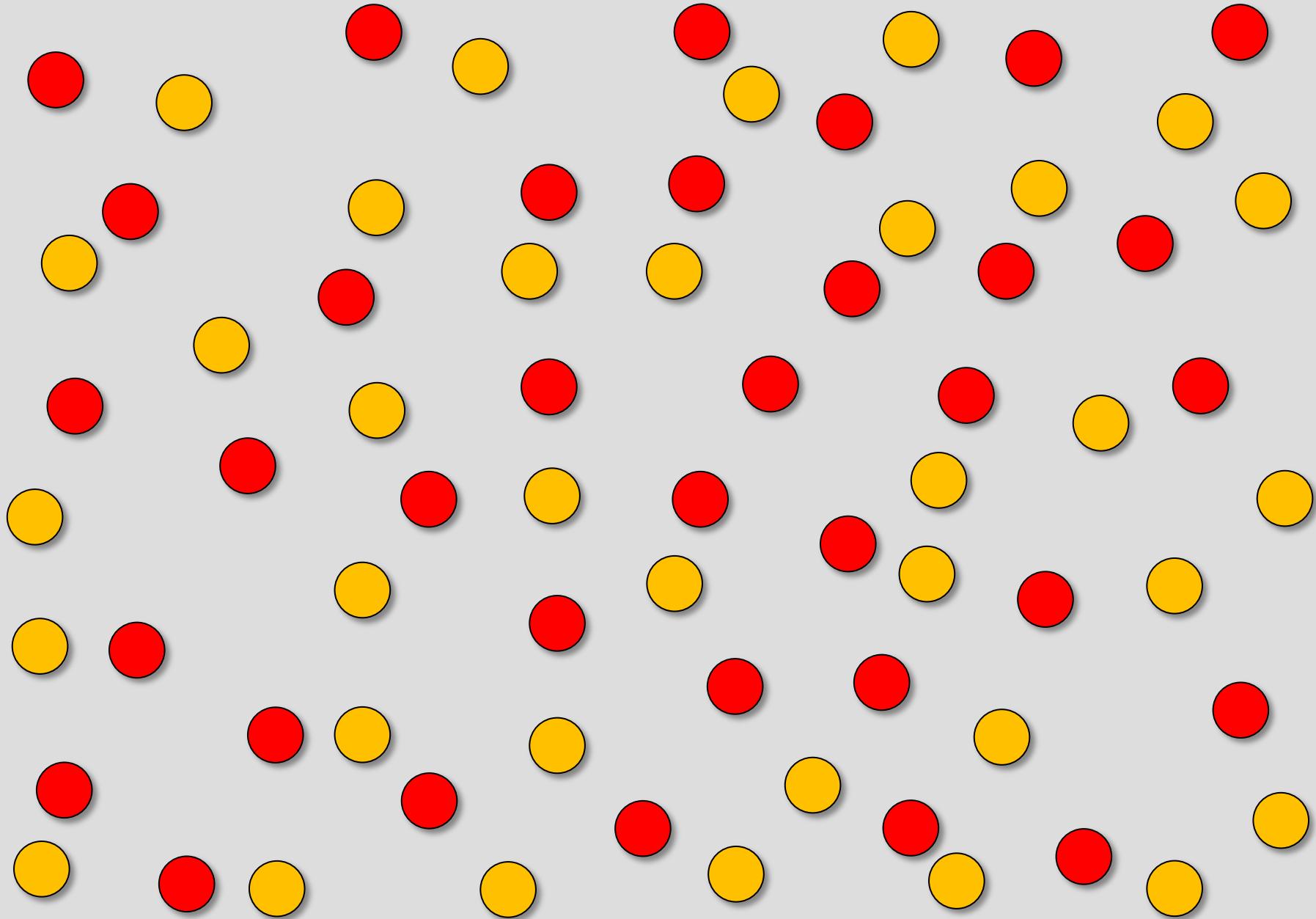
some open issues:
low-D Fermi gases, second sound...

new frontier:
strongly interacting Fermi-Fermi mixtures

experiments:
Innsbruck, Munich/Singapore, Amsterdam,
MIT, ENS Paris

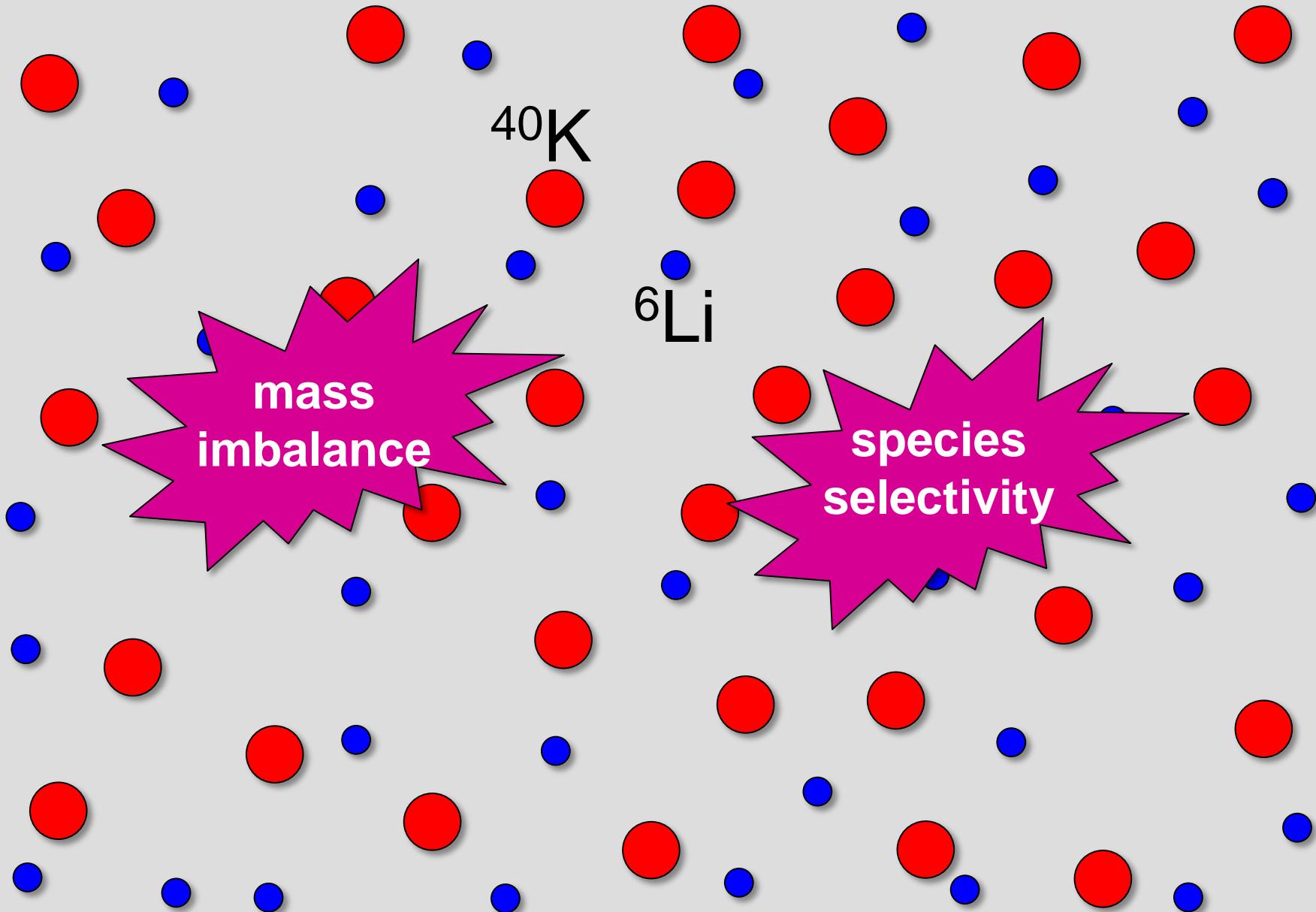
two-component Fermi system (spin mixture)

ultracold.at_{oms}



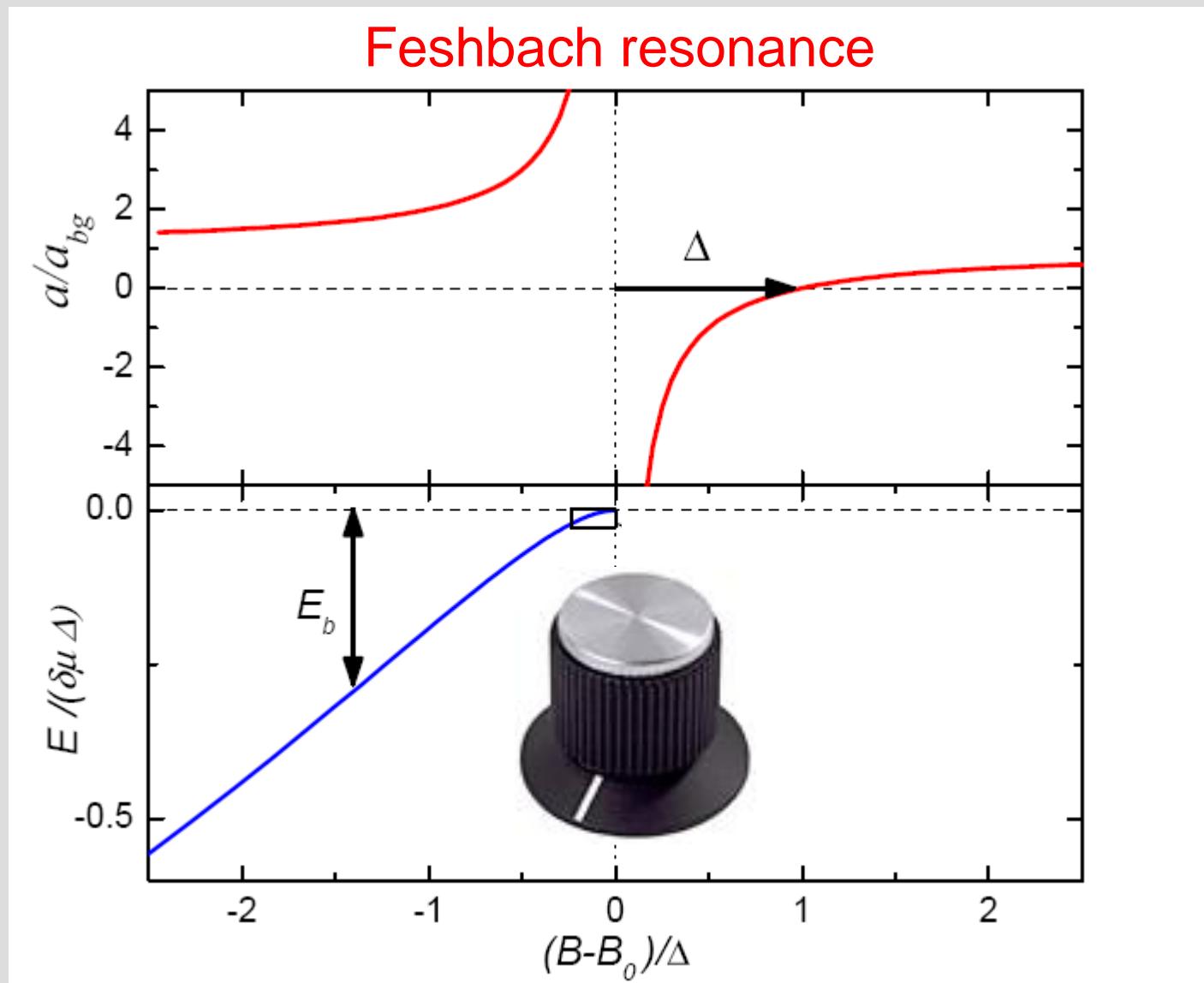
two-species: Fermi-Fermi mixture

ultracold.atoms



how about tunability?

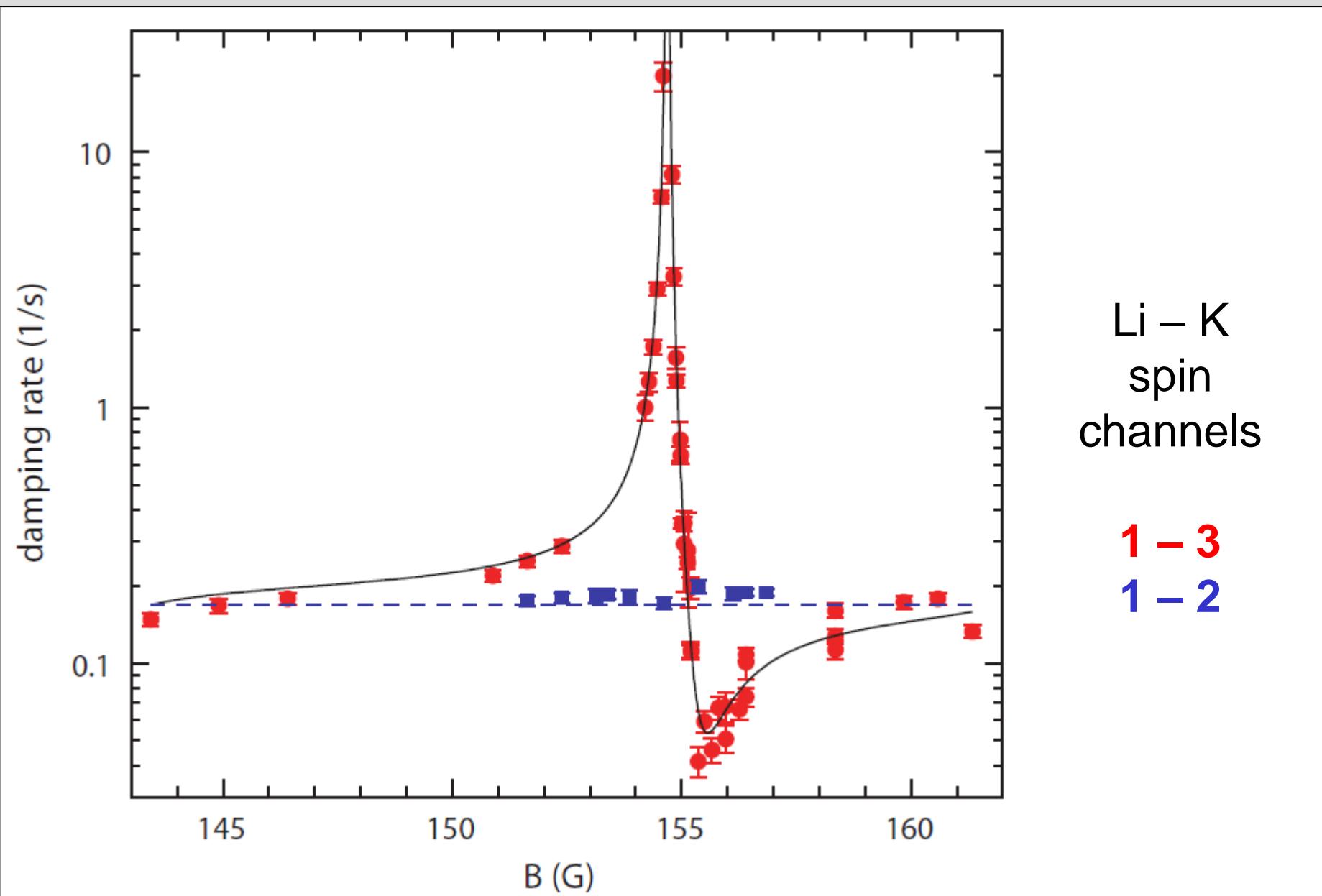
ultracold.atoms



review: Chin, Grimm, Julienne, Tiesinga, RMP 74, 1205 (2009)

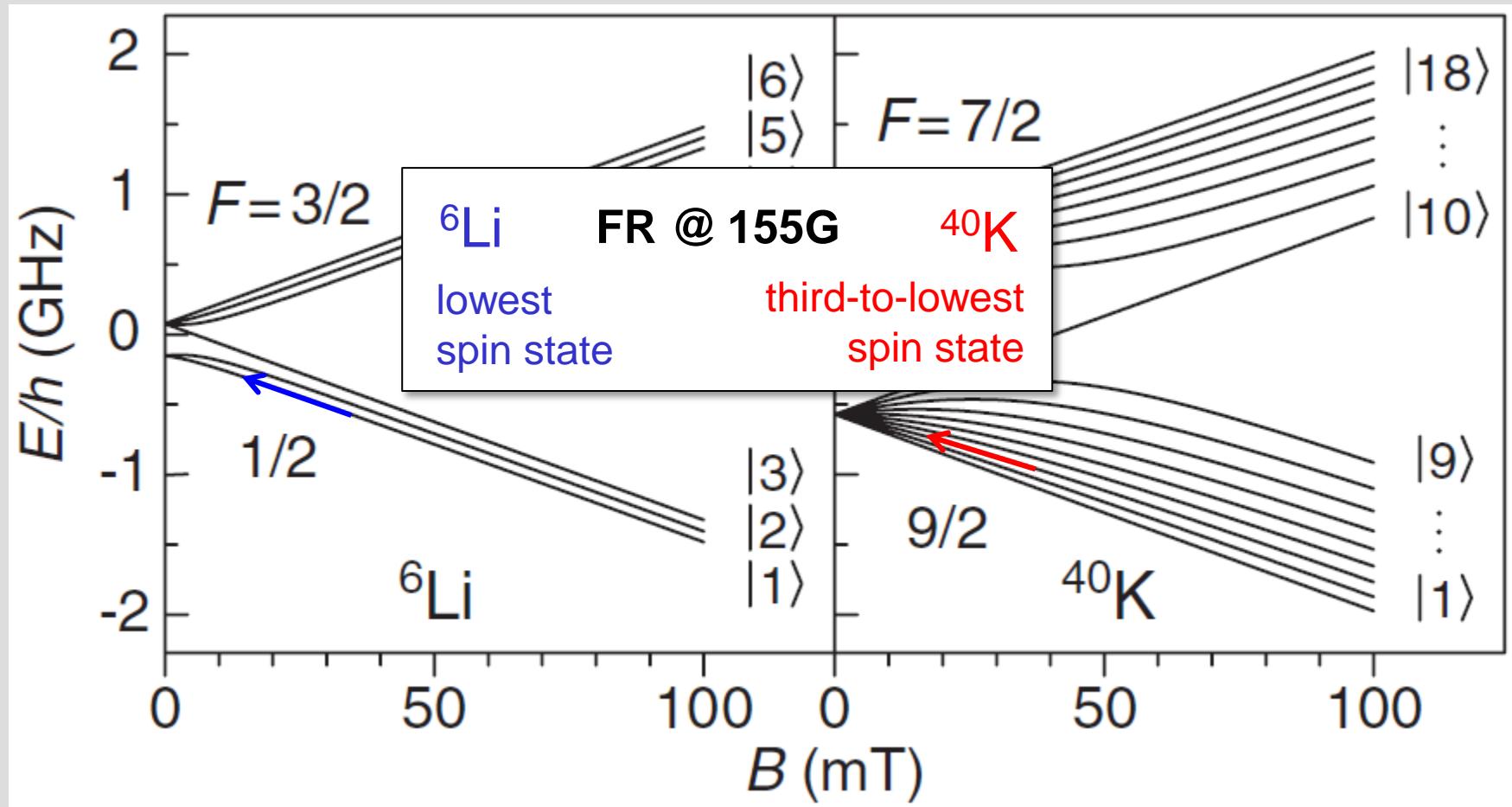
elastic scattering

ultracold.atoms



spin channels

ultracold.atoms



powerful tool-box of radio-frequency transitions

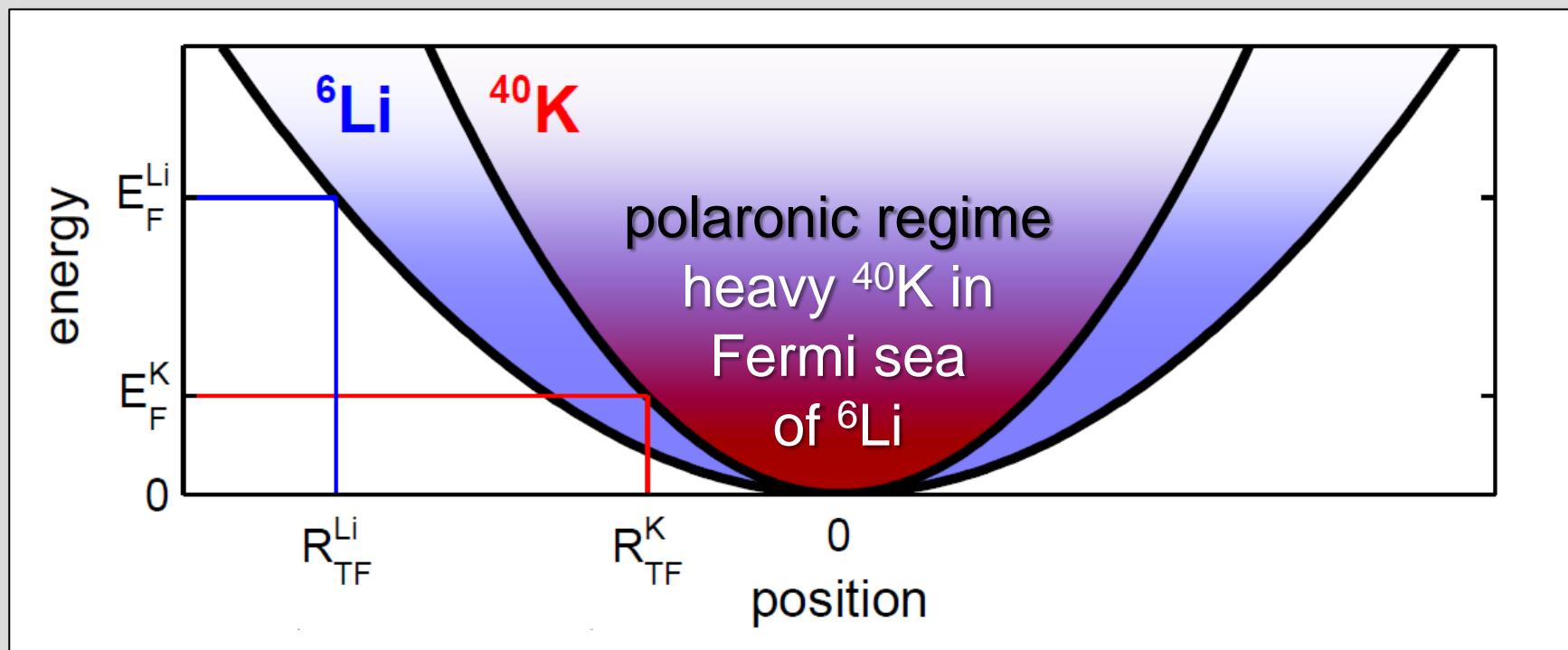
experimental parameters

ultracold.atoms

${}^6\text{Li}$: $N = 1.9 \times 10^5$
 $E_F = 1.6 \mu\text{K}$

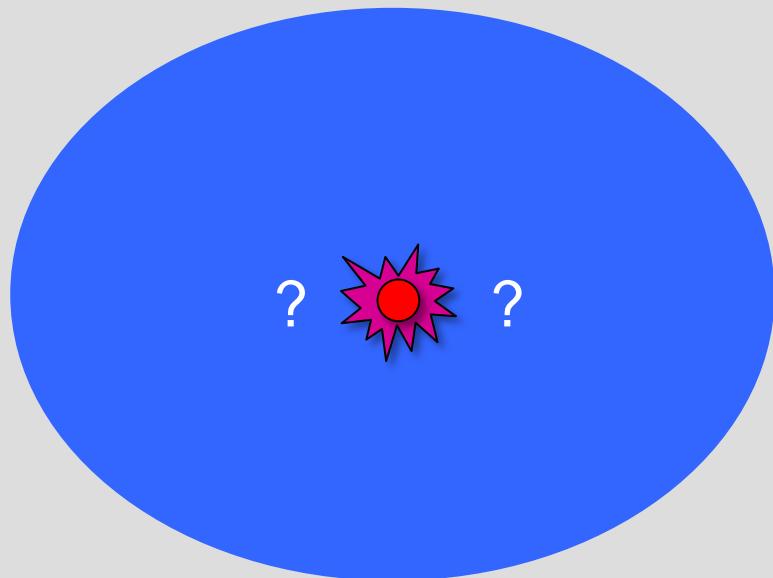
${}^{40}\text{K}$: $N = 1.2 \times 10^4$
 $E_F = 400 \text{ nK}$

$T = 330 \text{ nK}$



Li Fermi energy
our leading energy scale!

$1/k_F^{\text{Li}} \approx 3000 a_0$



weak ($k_F|a| \ll 1$): simple mean-field description

stronger: *quasi-particle* (polaron)
à la Landau Fermi liquid theory

strong ($k_F|a| > 1$): polaron or molecule?

Innsbruck Fermi-Fermi team

*Metastability and coherence of repulsive polarons
in a strongly interacting Fermi mixture*

C. Kohstall et al., Nature, in press; arXiv:1112.0020

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theory collaboration



Pietro Massignan
ICFO, Spain



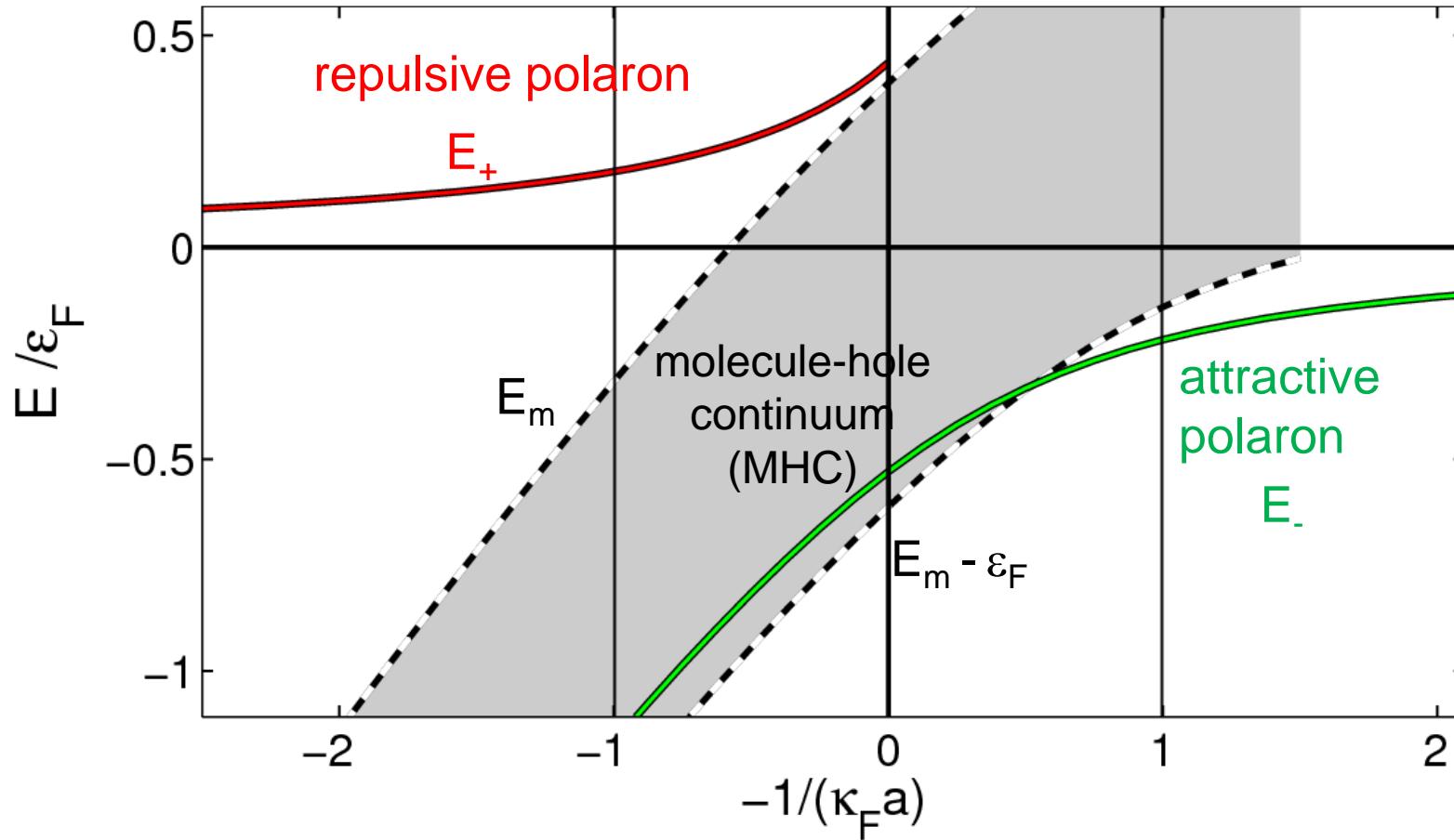
Marco Cetina



energy diagram ($T=0$)

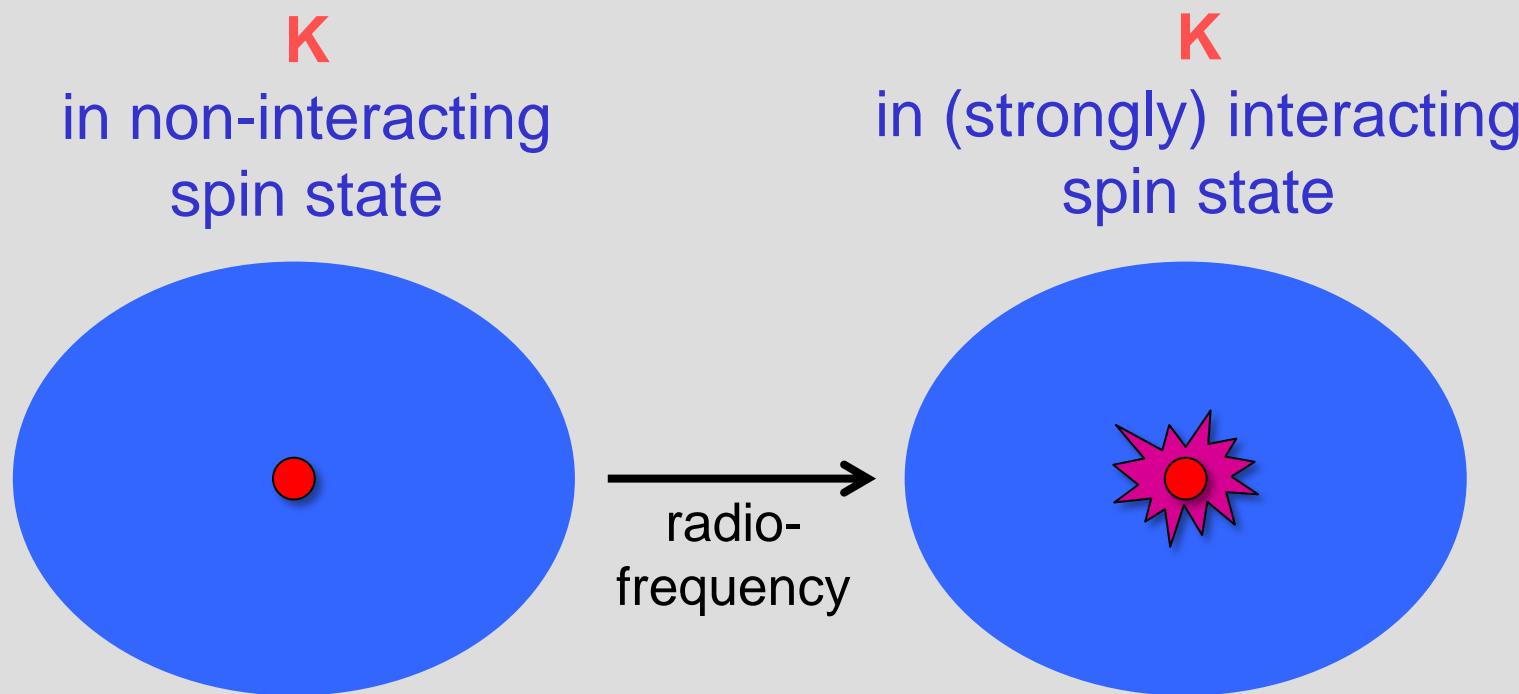
ultracold.at_{oms}

theory: P. Massignan and G. Bruun



“reverse” rf spectroscopy

ultracold.at_{oms}

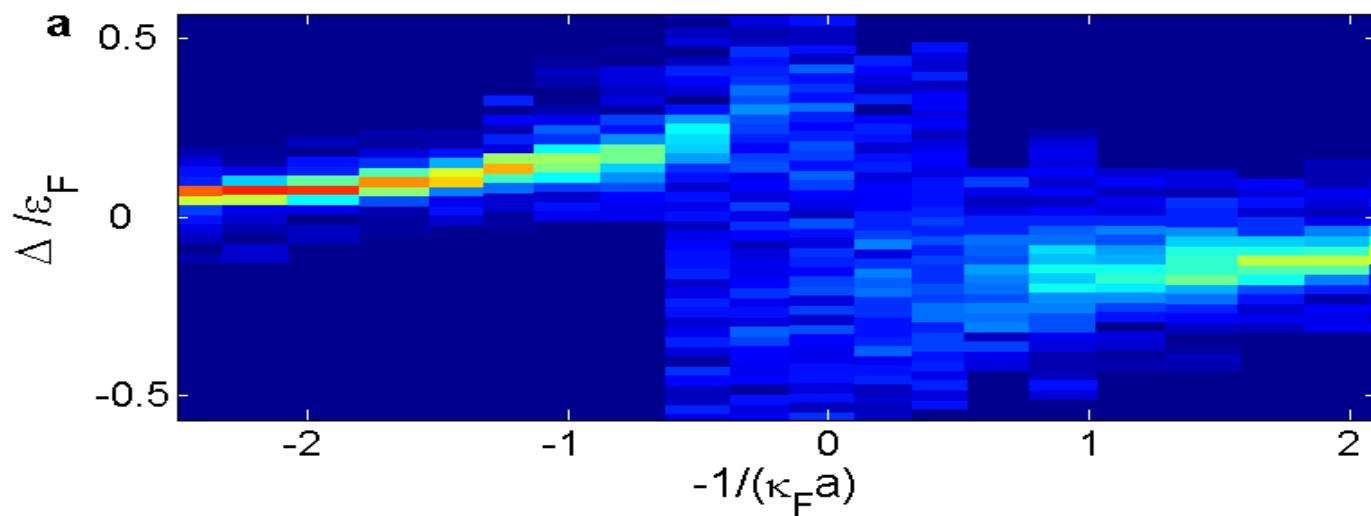


NB: different from standard rf probing !

spectral response

ultracold.atoms

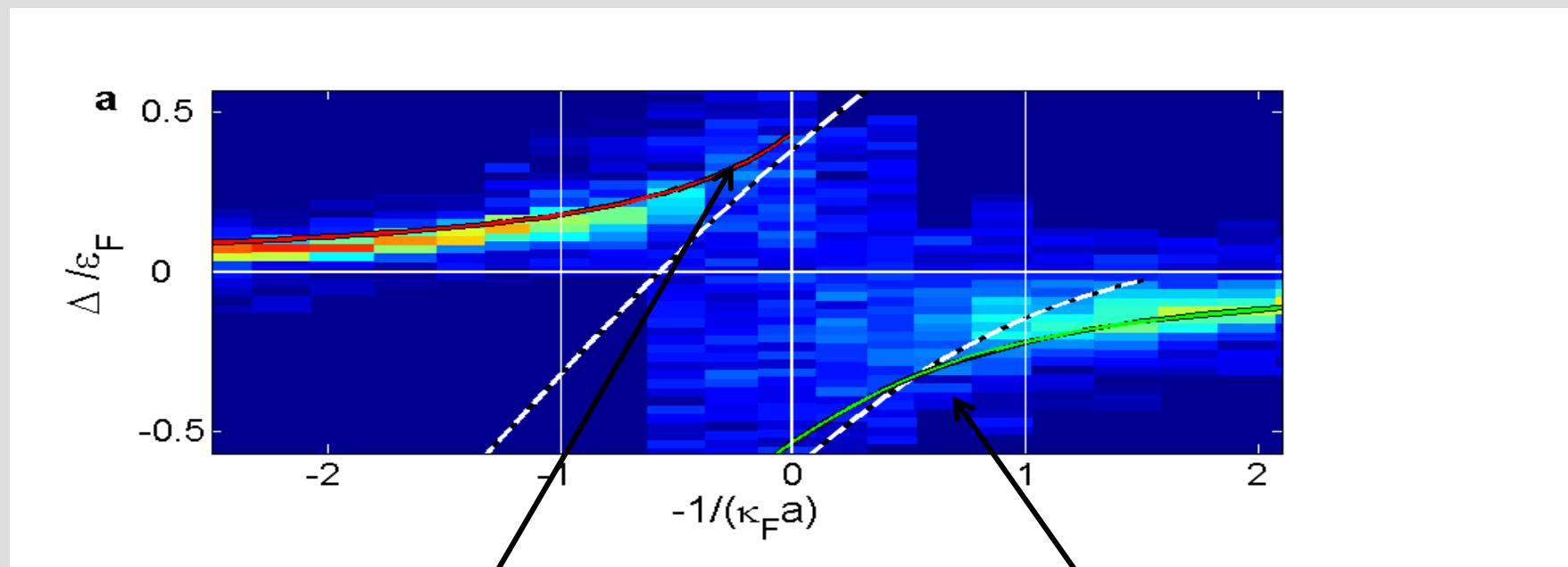
1 ms π -pulse (w/o interaction)



spectral response

ultracold.atoms

1 ms π -pulse (w/o interaction)



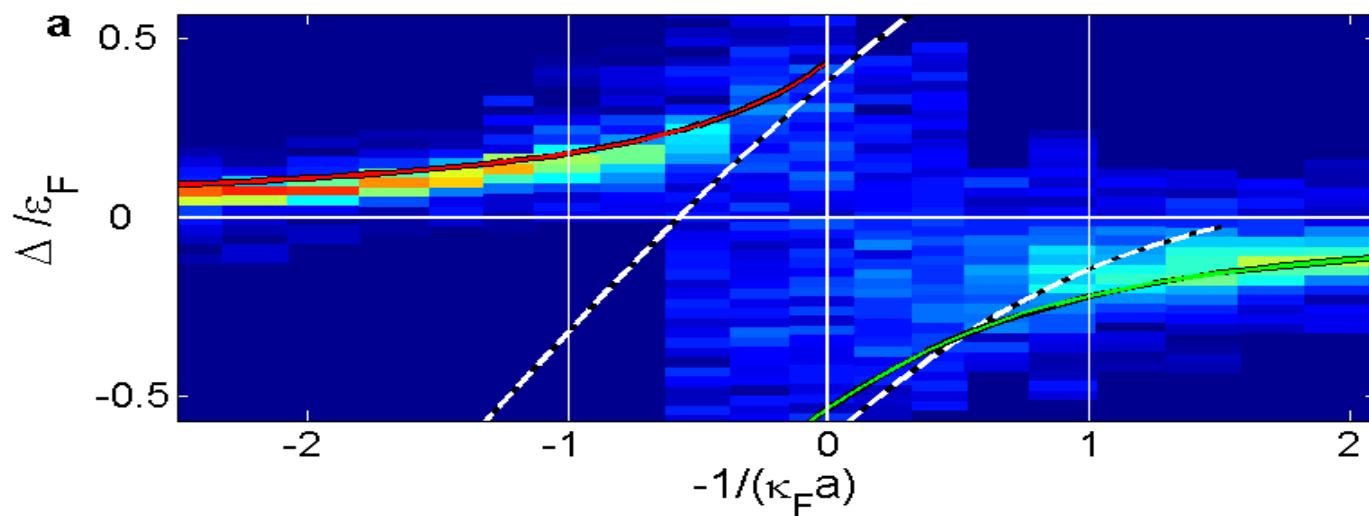
repulsive polaron
observed up to
 $-1/\kappa_F a = -0.3$

polaron-molecule
transition
 $-1/\kappa_F a = 0.6$

spectral response

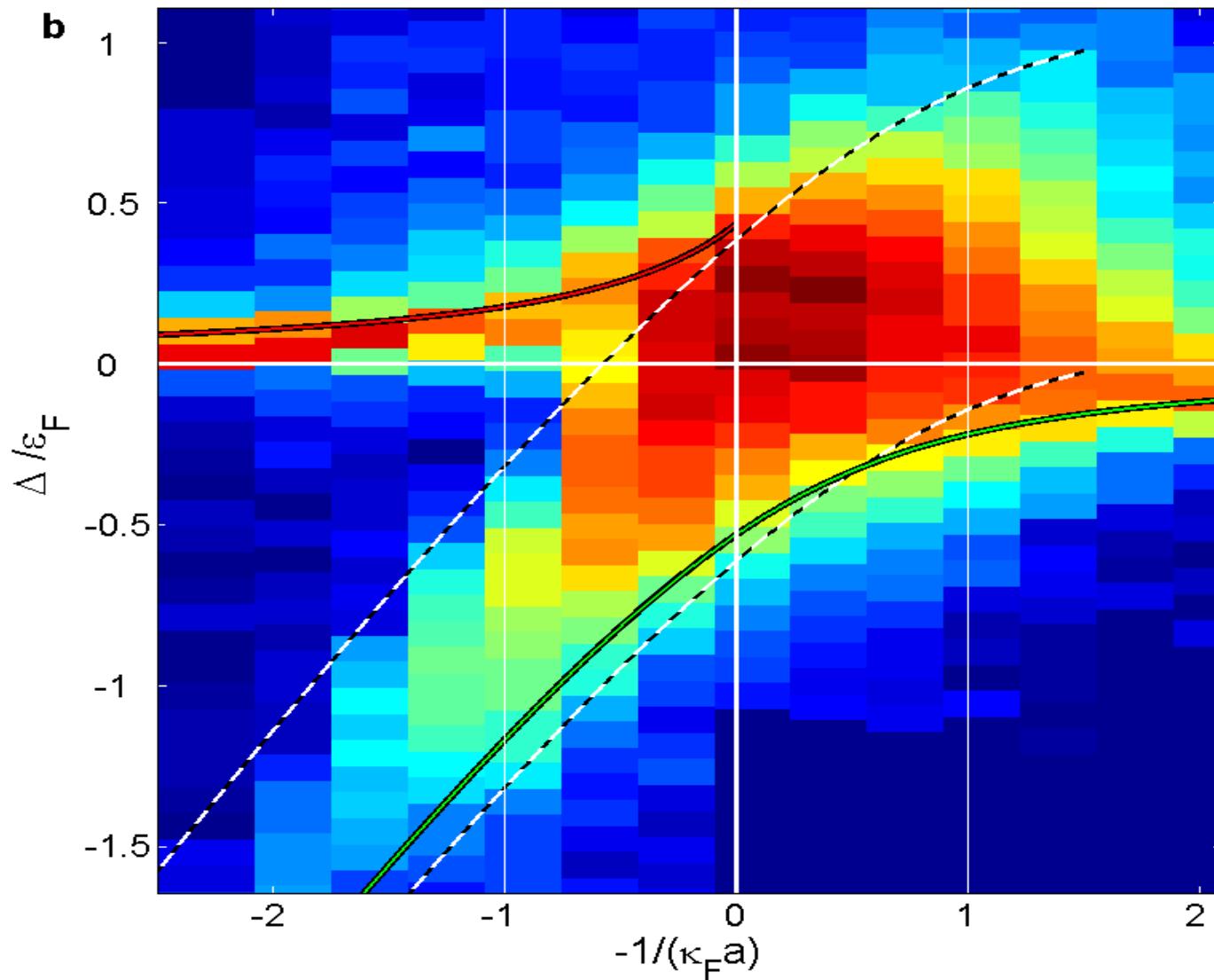
ultracold.atoms

let's crank up the rf power (100 x)



spectral response

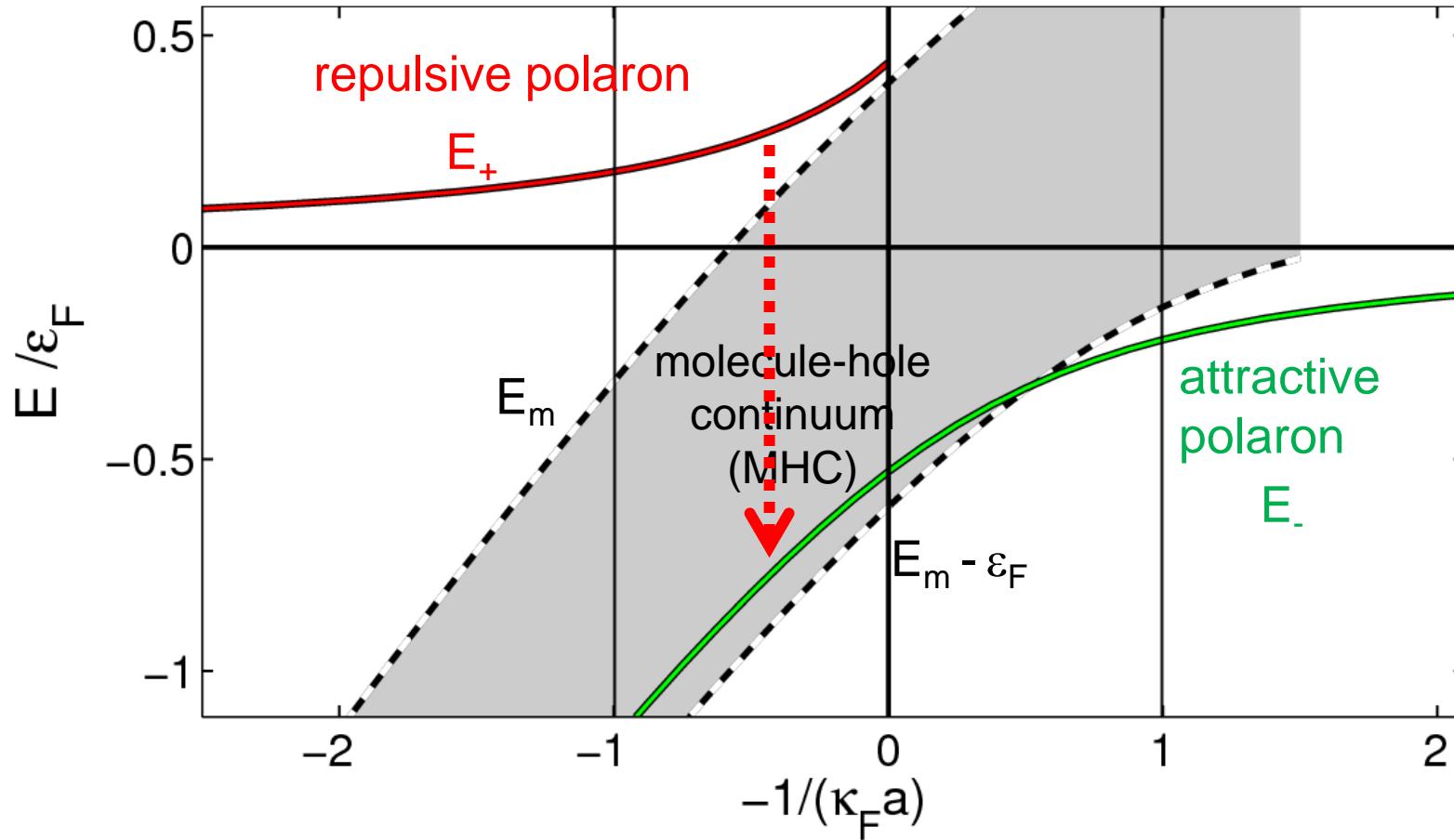
ultracold.atoms



energy diagram ($T=0$)

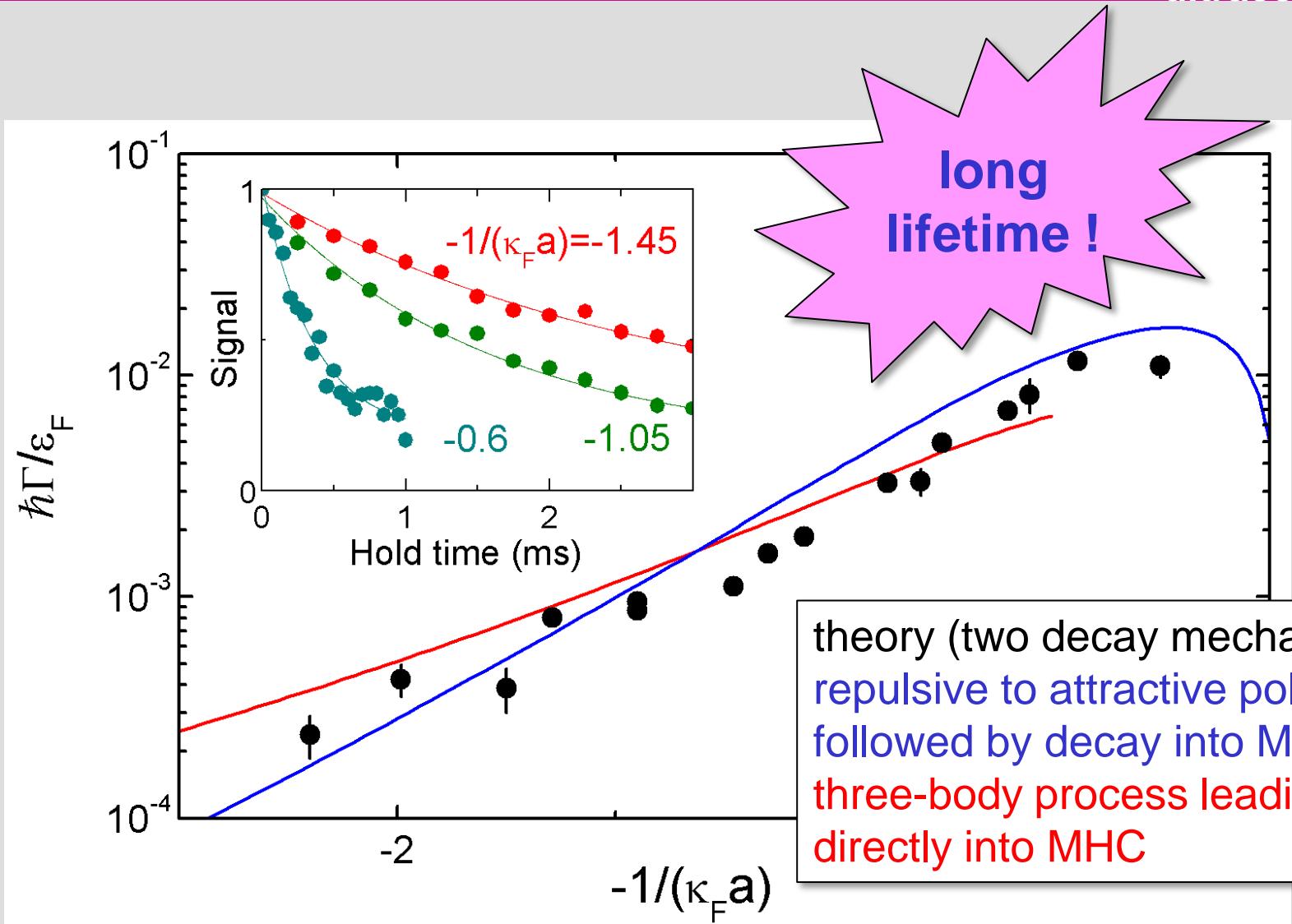
ultracold.at_{oms}

theory: P. Massignan and G. Bruun



measured decay rates

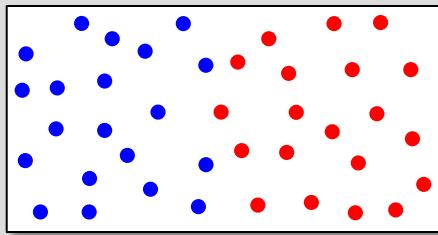
ultracold.atoms



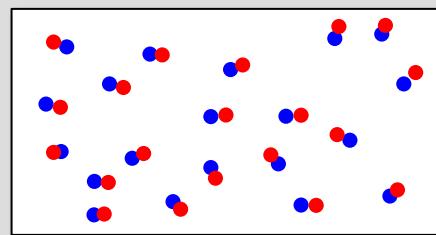
the big question

ultracold.atoms

phase separation
(ferromagnetism)



molecules



general conclusion

*ultracold atoms: unique, well-controllable model systems
for a wide range of phenomena*

- strongly interacting quantum matter
- condensed-matter physics
- few-body and many-body physics
-

exquisite benchmarks for quantum many-body theories



Der Wissenschaftsfonds.



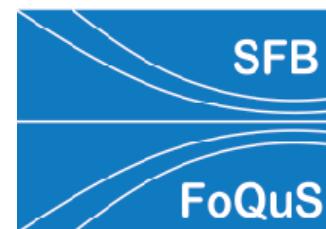
Foundations and
Applications of
Quantum Science



thank you for your attention !



Der Wissenschaftsfonds.



Foundations and
Applications of
Quantum Science

60 min (incl. disc.) seminar talk
talk way too long!!
could have stopped after the Efimov part (50min)
general intro took 20min.
could only rush through fermion part