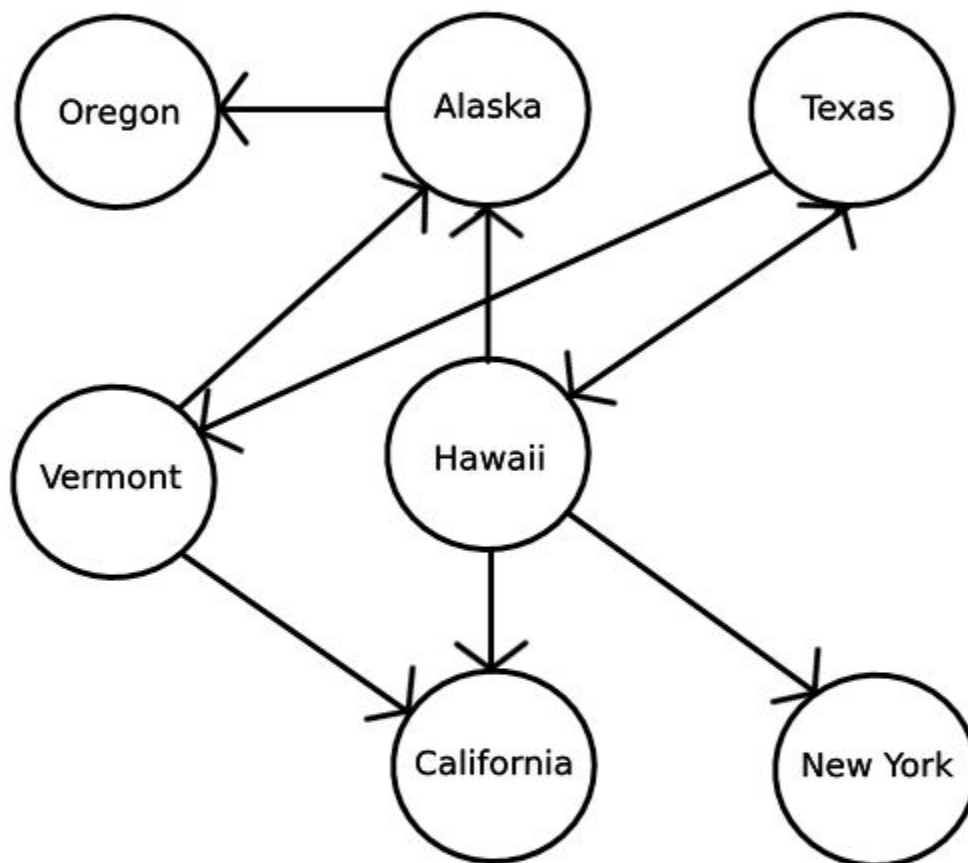


$V(\text{StateGraph}) = \{\text{Oregon, Alaska, Texas, Hawaii, Vermont, New York, California}\}$

$E(\text{StateGraph}) = \{(\text{Alaska, Oregon}), (\text{Hawaii, Alaska}), (\text{Hawaii, Texas}), (\text{Texas, Hawaii}), (\text{Hawaii, California}), (\text{Hawaii, New York}), (\text{Texas, Vermont}), (\text{Vermont, California}), (\text{Vermont, Alaska})\}$

1. Draw the StateGraph



1. Describe the graph pictured above, using the formal graph notation.

$V(\text{StateGraph}) = \{\text{Alaska, California, Hawaii, New York, Oregon, Texas, Vermont}\}$

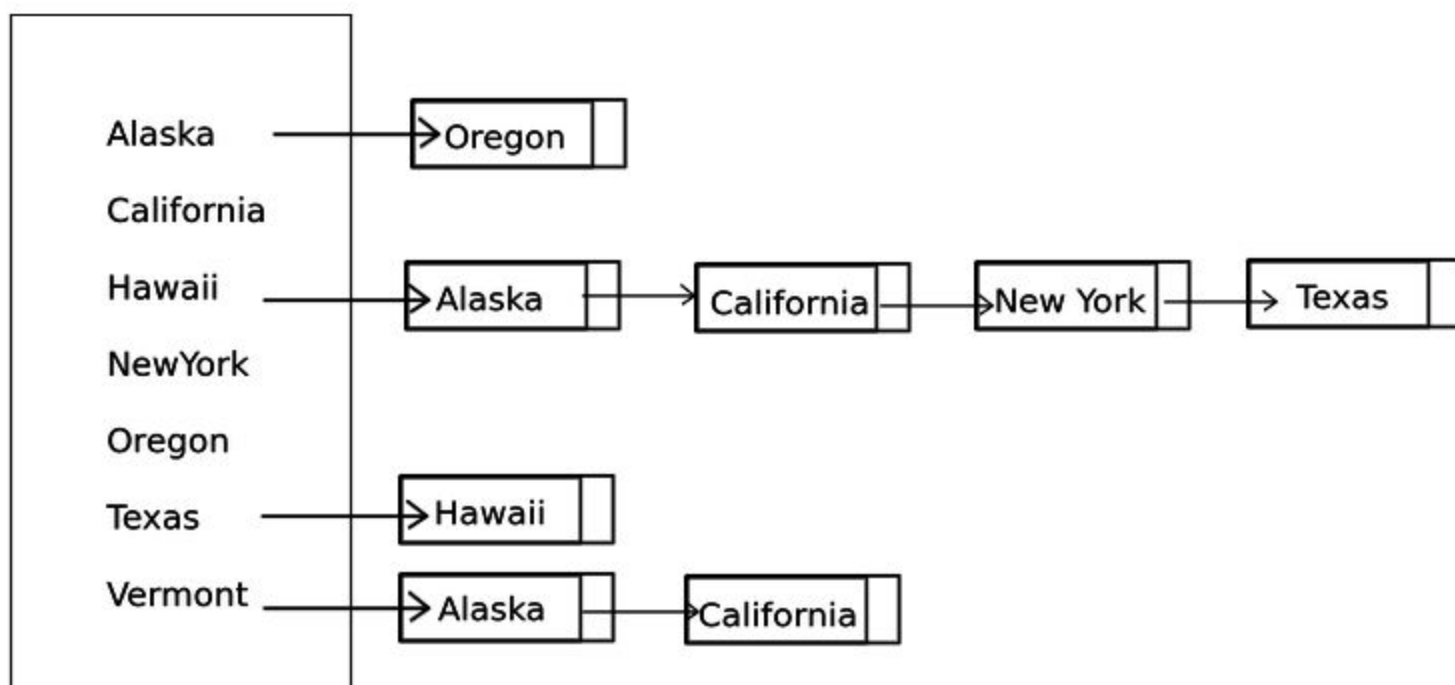
$E(\text{StateGraph}) = \{\text{ao, ha, ht, th, hc, hn, tv, vc, va}\}$

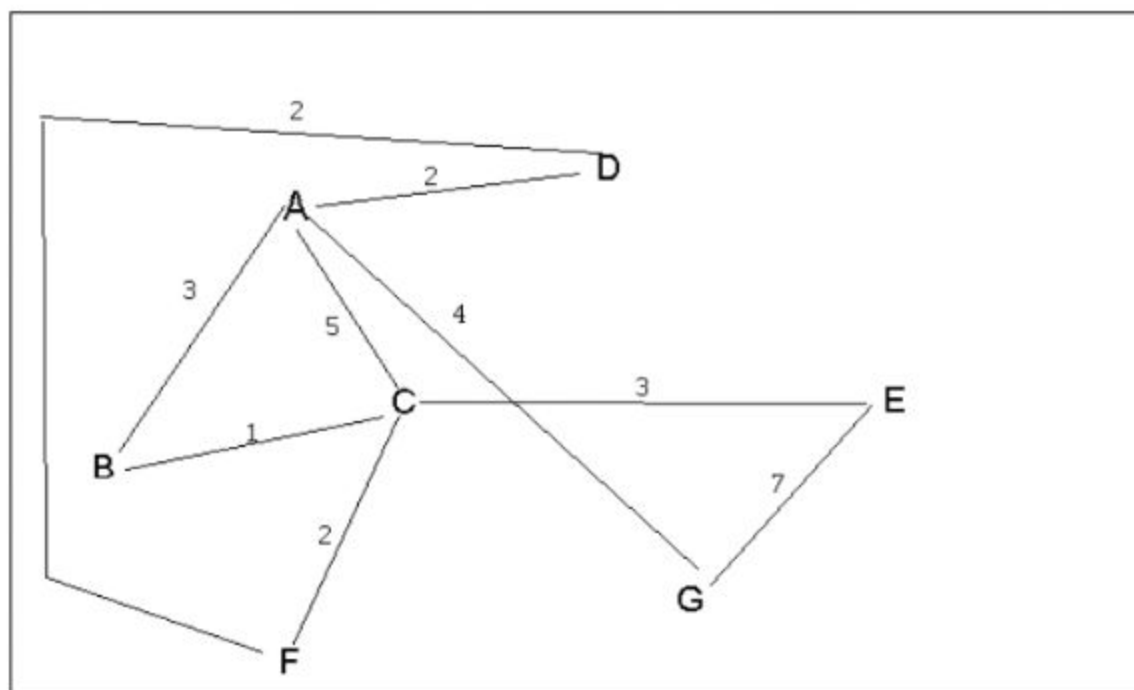
2. a. Is there a path from Oregon to any other state in the graph? No
- b. Is there a path from Hawaii to every other state in the graph? No
- c. From which state(s) in the graph is there a path to Hawaii? Texas

3. a. Show the adjacency matrix that would describe the edges in the graph.
Store the vertices in alphabetical order

| States | A K | C A | H I | N Y | O R | T X | V T |
|------------|-----|-----|-----|-----|-----|-----|-----|
| Alaska | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| California | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Hawaii | 1 | 1 | 0 | 1 | 0 | 1 | 0 |
| NewYork | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Oregon | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Texas | 0 | 0 | 1 | 0 | 0 | 0 | 1 |
| Vermont | 1 | 1 | 0 | 0 | 0 | 0 | 0 |

3. b. Show the adjacency lists
that would describe the edges in the graph



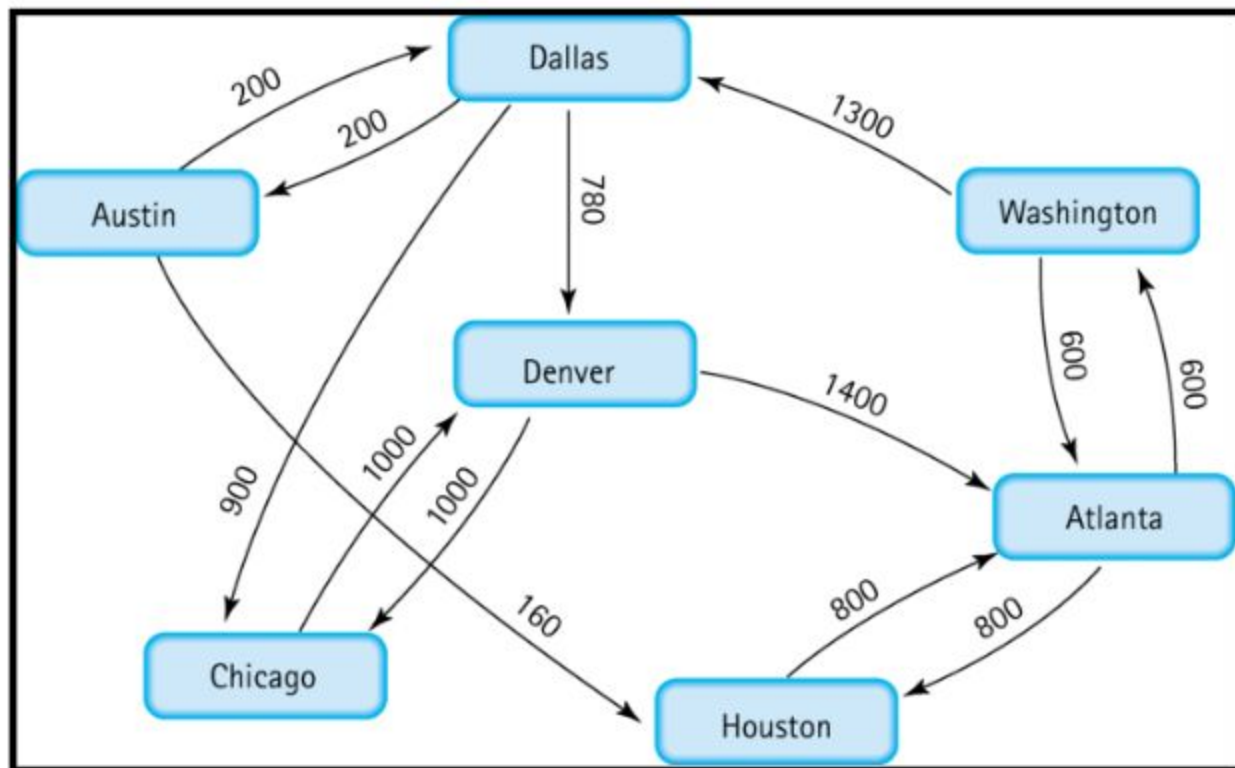


4 a. Which of the following lists the graph nodes in depth first order beginning with E?

- A) E, G, F, C, D, B, A
- B) G, A, E, C, B, F, D
- ☒ C) E, G, A, D, F, C, B
- D) E, C, F, B, A, D, G

4 b. Which of the following lists the graph nodes in breadth first order beginning at F?

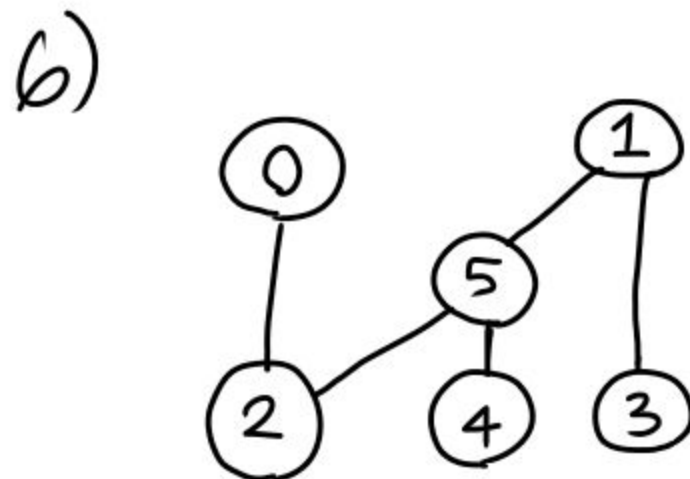
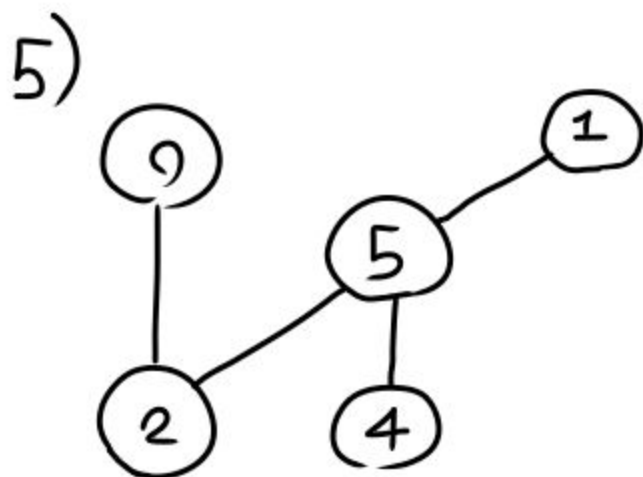
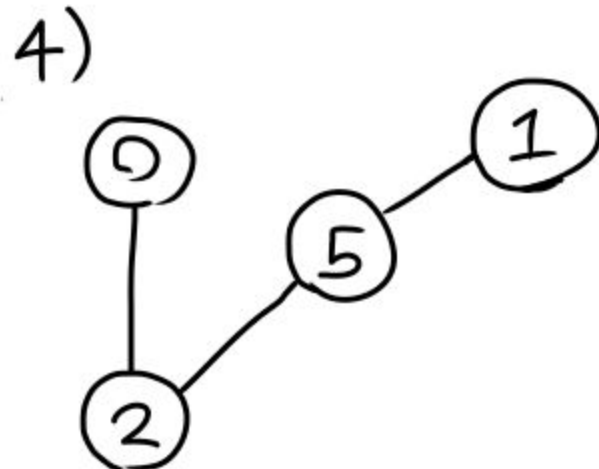
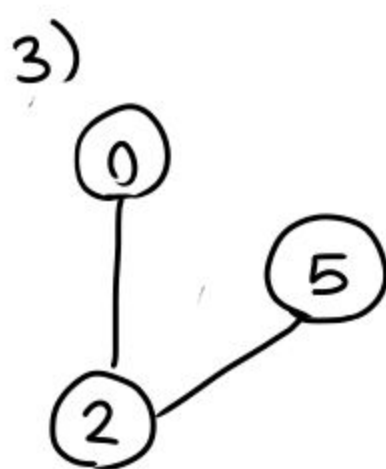
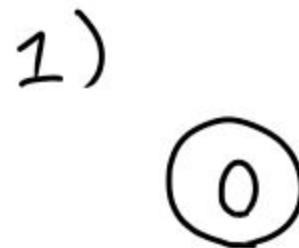
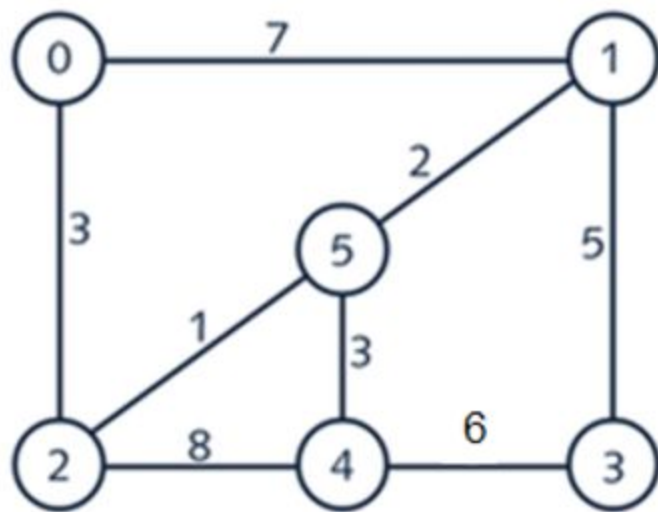
- ☒ A) F, C, D, A, B, E, G
- B) F, D, C, A, B, C, G
- C) F, C, D, B, G, A, E
- D) a, b, and c are all breadth first traversals



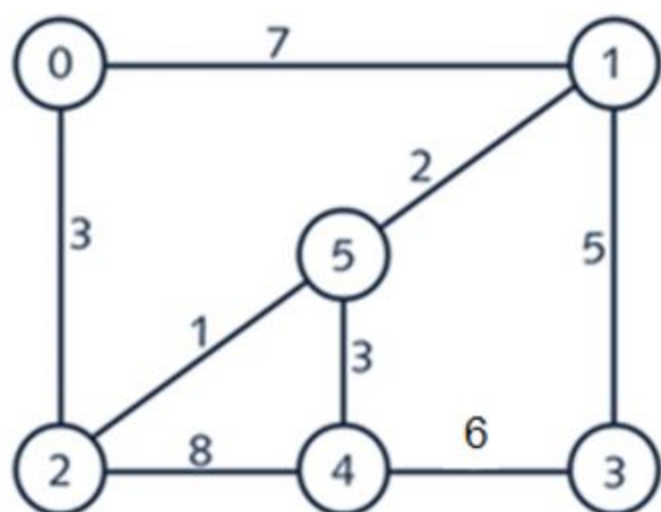
5. Find the shortest distance from Atlanta to every other city

Austin: Atlanta -> Washington -> Dallas -> Austin = $(600 + 1300 + 200) = 2100$
 Chicago: Atlanta -> Washington -> Dallas -> Chicago = $(600 + 1300 + 900) = 2800$
 Dallas: Atlanta -> Washington -> Dallas = $(600 + 1300) = 1900$
 Denver: Atlanta -> Washington -> Dallas -> Denver = $(600 + 1300 + 780) = 2680$
 Houston: Atlanta -> Houston = 800
 Washington: 600

6. Find the minimal spanning tree using Prim's algorithm. Use 0 as the source vertex . Show the steps.

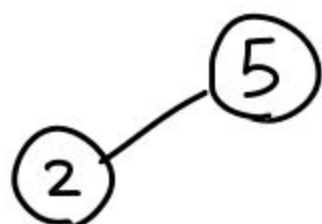


7. Find the minimal spanning tree using Kruskal's algorithm. Show the weights in order and the steps.

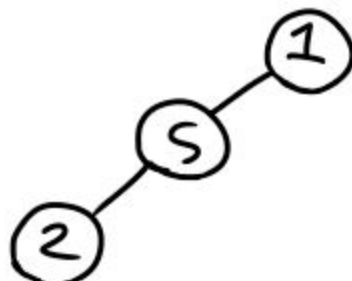


| edges | Weights |
|-------|---------|
| 2-5 | 1 |
| 1-5 | 2 |
| 4-5 | 3 |
| 0-2 | 3 |
| 1-3 | 5 |
| 3-4 | 6 |
| 0-1 | 7 |
| 2-4 | 8 |

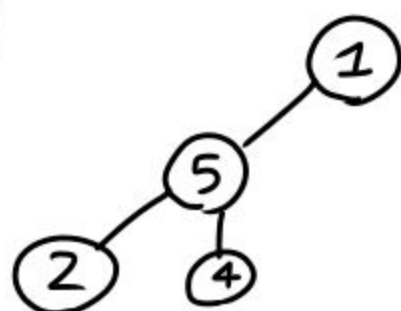
1)



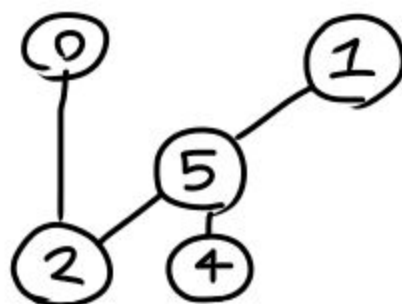
2)



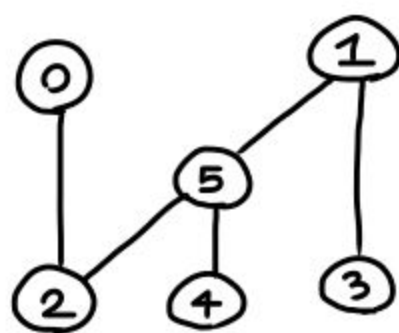
3)



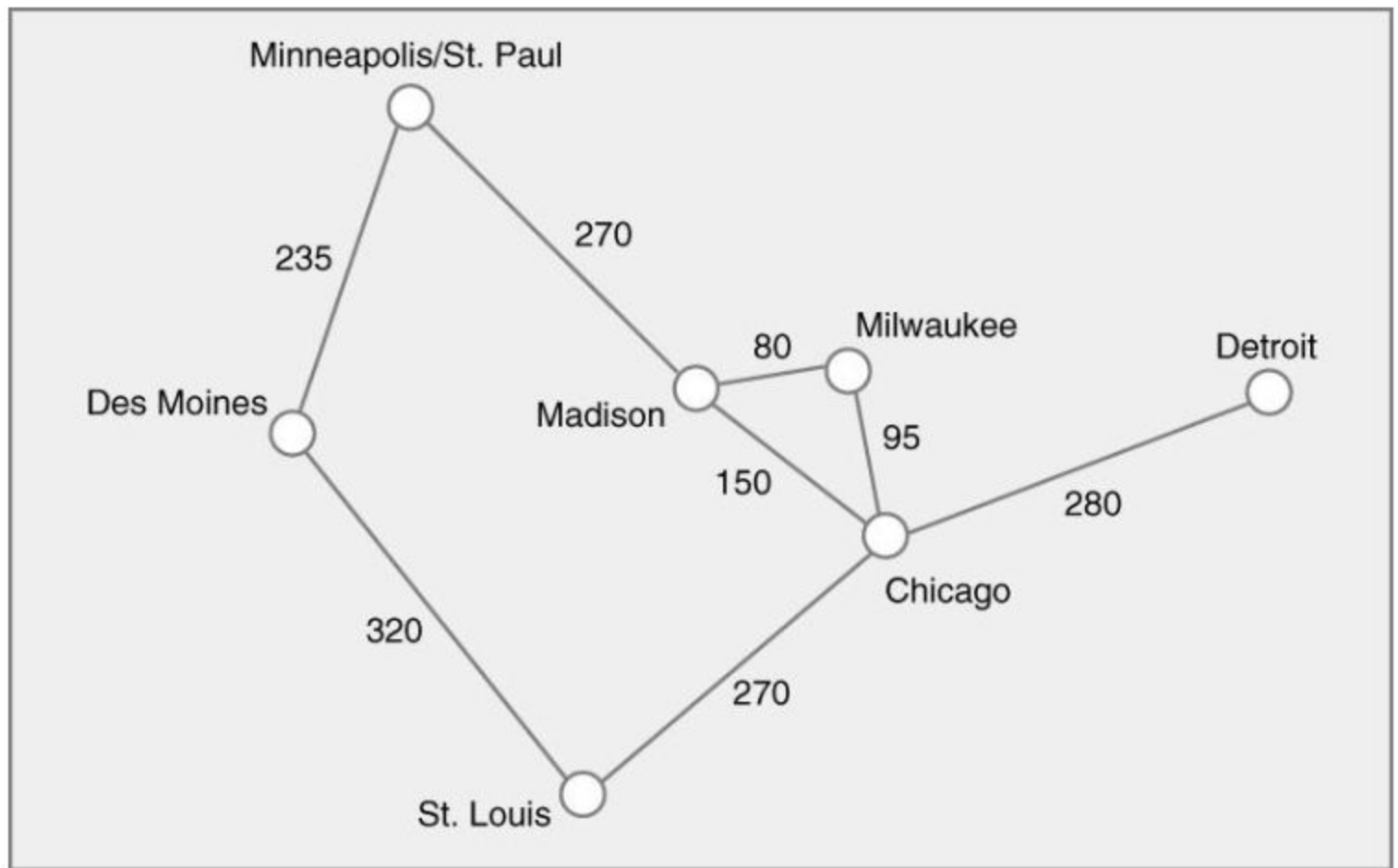
4)



5)

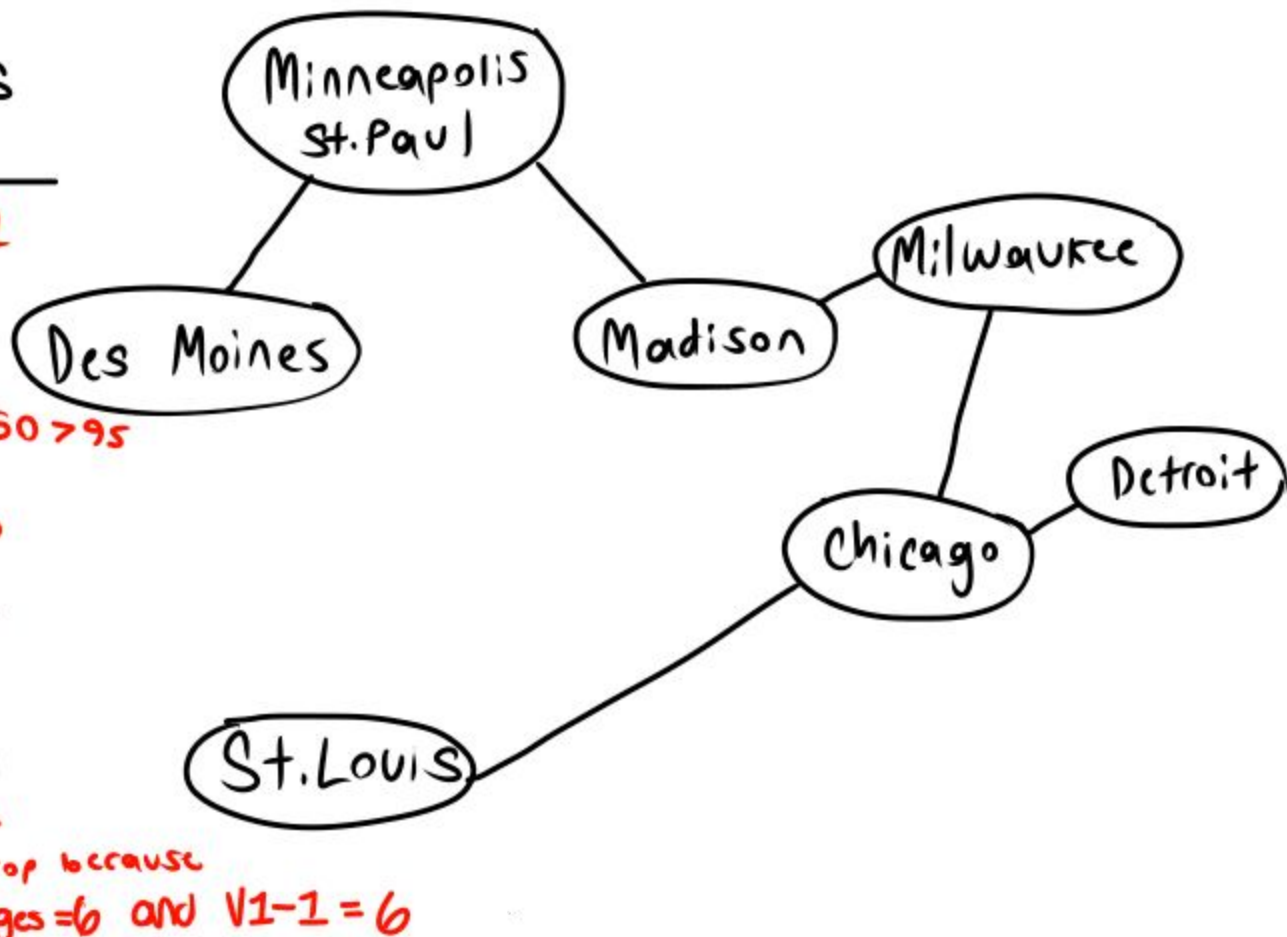


8. Find the minimal spanning tree using the algorithm you prefer. Use Minneapolis/St. Paul as the source vertex

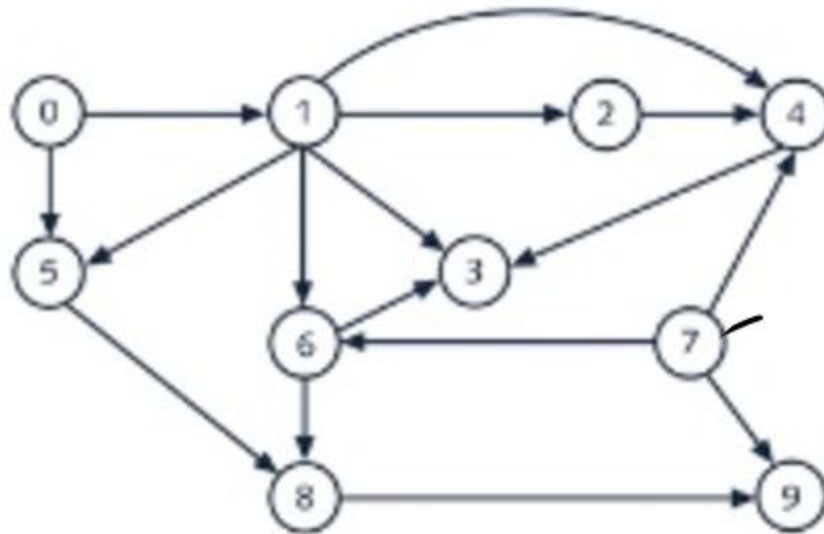


Kruskal's

| edges | Weights |
|-------|----------------------------|
| Ma-Mi | 80 ¹ |
| Mi-Ch | 95 ² |
| Ma-Ch | 150 ^{150 > 95} |
| Sp-Dm | 235 ³ |
| Sp-Ma | 270 ⁴ |
| Ch-Sl | 270 ⁵ |
| Ch-De | 280 ⁶ |
| DM-Sl | 320 |



9. List the nodes of the graph in a breadth first topological ordering. Show the steps using arrays predCount, topologicalOrder and a queue



predCount

Topological order

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|---|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|---|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 0 | 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|---|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 1 |
|---|---|---|---|---|---|---|---|---|---|

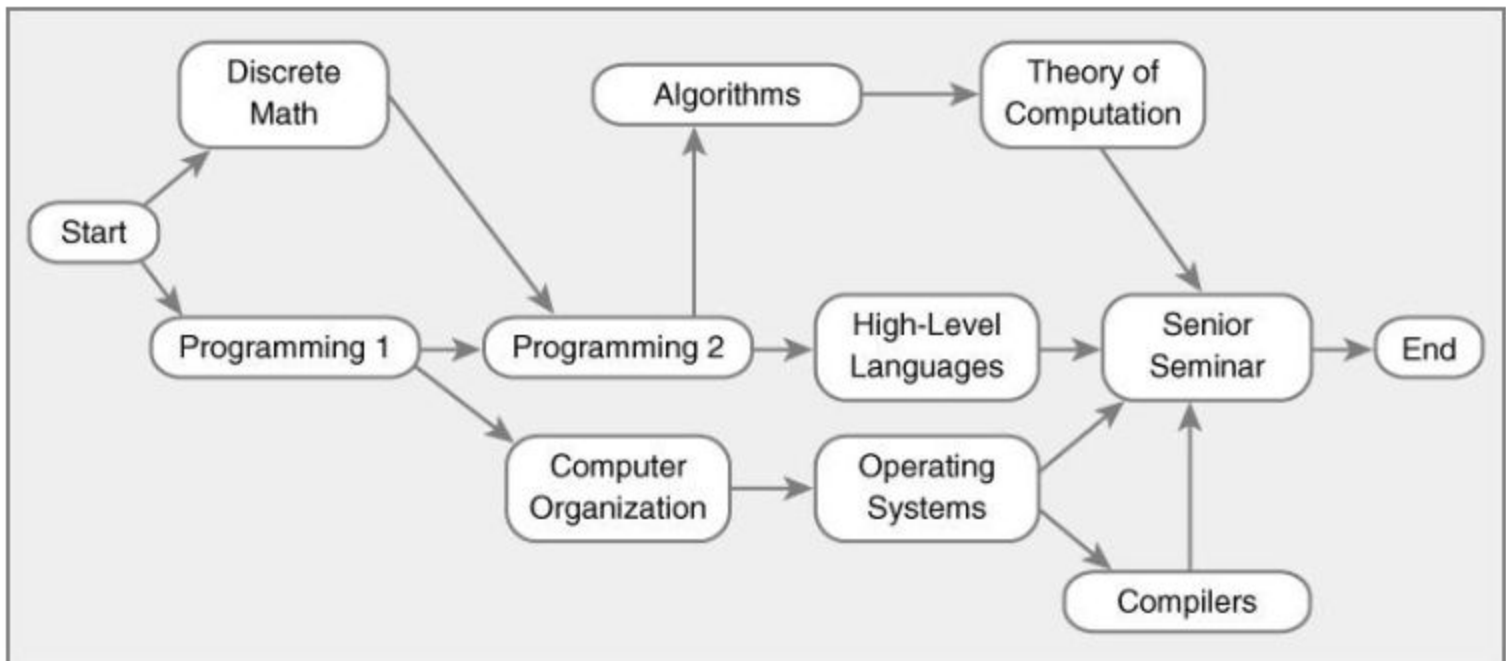
| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 0 | 7 | 1 | 5 | 4 | 6 | 9 | 0 | 0 | 0 |
|---|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 1 | 1 | 1 | 3 | 2 | 1 | 1 | 1 | 2 | 1 |
|---|---|---|---|---|---|---|---|---|---|

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 0 | 7 | 1 | 5 | 4 | 6 | 9 | 2 | 3 | 8 |
|---|---|---|---|---|---|---|---|---|---|

Queue - 0 7 1 5 4 6 9 2 3 8

10. List the nodes of the graph in a breadth first topological ordering.



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