



Computer programming

"He who loves practice without theory is like the sailor who boards ship without a ruder and compass and never knows where he may cast."

Leonardo da Vinci



Outline

- File handling
 - High level I/O
 - fopen
 - fclose
 - fread
 - fwrite
 - fsetpos, fgetpos, ftell, fseek
- Applications
 - Combinatorial generation: generating subsets
 - Cross product (Cartesian product)
 - Combinations
 - Permutations
 - Arrangements
 - Power set



High level I/O. Files and Streams

- C views each file as a sequence of bytes
 - File ends with the *end-of-file marker*
 - Or, file ends at a specified byte
- Stream created when a file is opened
 - Provide communication channel between files and programs
 - Opening a file returns a pointer to a **FILE** structure
 - Example file pointers:
 - **stdin** - standard input (keyboard)
 - **stdout** - standard output (screen)
 - **stderr** - standard error (screen)
- **FILE** structure
 - File descriptor - Index into operating system array called the open file table
 - File Control Block (FCB) - Found in every array element, system uses it to administer the file



Files and Streams

- To process a file:
 - Open file
 - Do work (read, write)
 - Close file
- Opening a file = request
 - Must check that the request was accepted. i.e. a non-NULL pointer was returned

```
myPtr = fopen("myFile.dat", "r");  
If (myPtr == NULL) {  
    // cannot continue, file not opened  
}
```



Files and Streams

- Read/Write functions in standard library
 - **fgetc** - reads one character from a file
 - Takes a **FILE** pointer as an argument
 - **fgetc(stdin)** equivalent to **getchar()**
 - **fputc** - writes one character to a file
 - Takes a **FILE** pointer and a character to write as an argument
 - **fputc('a', stdout)** equivalent to **putchar('a')**
 - **fgets** - read a line from a file
 - **fputs** - write a line to a file
 - **fscanf** / **fprintf** - file processing equivalents of **scanf** and **printf**



Creating a Sequential Access File

- C imposes no file structure
 - No notion of records in a file
 - Programmer must provide file structure
- Creating/using a file: **fopen**
 - **FILE *myPtr;** - creates a **FILE** pointer
 - **myPtr = fopen("myFile.dat", openmode);**
 - Function **fopen** returns a **FILE** pointer to file specified
 - Takes two arguments - file to open and file open mode
 - If file not opened, **NULL** returned



Creating a Sequential Access File

- **`feof(FILE pointer)`** - returns **`true`** if end-of-file indicator (no more data to process) is set for the specified file
- **`fclose(FILE pointer)`** - closes specified file
 - Performed automatically when program ends
 - Good practice to close files explicitly
- **Details**
 - Each file must have a unique name and will have a different pointer
 - All file processing must refer to the file using the pointer



- **filePointer = fopen(filePath, openmode)**
- Each mode can have a 'b' (for binary, e.g. ab, wb, rb+) after mode letter
- **openmode** given as a string ("r", "w", "rb", "wb", "r+" etc.)

Mode	Description
r	Open a file for reading.
w	Create a file for writing. If the file already exists, discard the current contents.
a	Append; open or create a file for writing at end of file.
r+	Open a file for update (reading and writing).
w+	Create a file for update. If the file already exists, discard the current contents.
a+	Append; open or create a file for update; writing is done at the end of the file.



Attaching a file to an open stream

- `freopen(const char *filename, const char *mode, FILE *stream)`
 - Most common use: associate a file with one of the standard streams
 - Example: cause program begin writing to `foo.txt`

```
if (freopen("foo.txt", "w", stdout) == NULL)
{
    // error foo.txt cannot be opened
}
```
 - Effect: close any other file previously associated to `stdout` ; then open `foo.txt` and associate it with `stdout`.



Reading Data from a Sequential Access File

- Reading a sequential access file
 - Create a **FILE** pointer, link it to the file to read

```
myPtr = fopen( "myFile.dat", "r" );
```
 - Use **fscanf** to read from the file
 - Like **scanf**, except first argument is a **FILE** pointer
- ```
fscanf(myPtr, "%d%s%f", &myInt, &myString,
&myFloat);
```
- Data read from beginning to end



# Reading Data from a Sequential Access File

---

- File position pointer - indicates number of next byte to be read/written
  - Not really a pointer, but an integer value (specifies byte location)
  - Also called byte offset
- **`rewind(myPtr)`** - repositions file position pointer to beginning of the file (byte 0)
- Cannot be modified without the risk of destroying other data



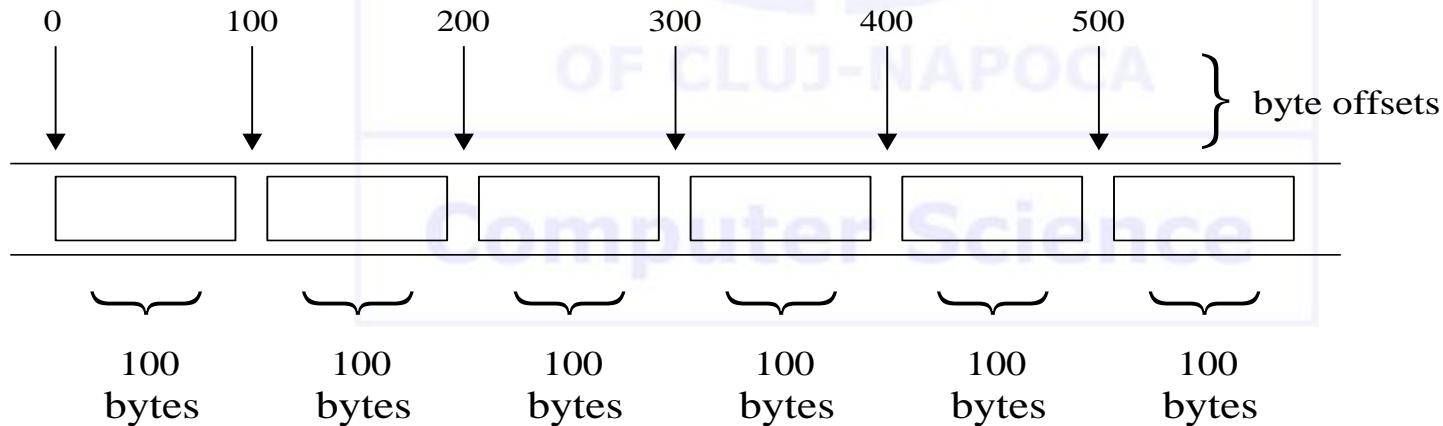
# Random Access Files

- Random access files
  - Access individual records without searching through other records
  - Instant access to records in a file
  - Data can be inserted without destroying other data
  - Data previously stored can be updated or deleted without overwriting.



## Creating a Random Access File

- Implemented using *fixed length* records
  - Sequential files do not have fixed length records
- Data unformatted (stored as "raw bytes") in random access files
  - All data of the same type (`ints`, for example) use the same memory
  - All records of the same type have a fixed length
  - Data not human readable





## Creating a Random Access File

- Unformatted I/O functions
  - **fwrite** - Transfer bytes from a location in memory to a file
  - **fread** - Transfer bytes from a file to a location in memory
  - **fwrite( &number, sizeof( int ), 1, myPtr );**
    - **&number** - Location to transfer bytes from
    - **sizeof( int )** - Number of bytes to transfer
    - **1** - For arrays, number of elements to transfer
      - In this case, "one element" of an array is being transferred
    - **myPtr** - File to transfer to or from
    - **fread** similar



# Writing Data Randomly to a Random Access File

- Writing data: **fwrite**

```
size_t fwrite(const void *ptr, size_t size, size_t
nelem, FILE *stream);
```

- **ptr** = pointer to memory area where info to write is stored
- **size** = size in bytes of one element
- **nelem** = number of elements to write

- E.g. writing **structs**

```
fwrite(&myObject, sizeof (struct myStruct), 1,
myPtr);
```

- **sizeof** - Returns size in bytes of object in parentheses

- To write several array elements

- Pointer to array as first argument
- Number of elements to write as third argument



# Reading Data Sequentially from a Random Access File. Removing a file

## ■ Reading data: `fread`

```
size_t fread(void *ptr, size_t size, size_t nelem, FILE *stream);
```

- `ptr` = pointer to memory area where read info will be stored
- `size` = size in bytes of one element
- `nelem` = number of elements to write
- Example:

```
fread(&client, sizeof (struct clientData), 1, myPtr);
```

- Can read several fixed-size array elements
  - Provide pointer to array
  - Indicate number of elements to read
- To read multiple elements, specify in third argument

## ■ Removing a file

```
int unlink(const char *path_to_file)
```

- returns 0 if successful, and -1 on error





# File position

```
/* return file position indicator */
long ftell(FILE *stream);
int fgetpos(FILE *stream, fpos_t *pos);
/* set file position indicator to zero */
void rewind(FILE *stream);
/* set file position indicator */
int fseek(FILE *stream, long offset, int ptrname);
int fsetpos(FILE *stream, const fpos_t *pos);
```

- **ftell** returns the current value (measured in characters) of the file position indicator if stream refers to a binary file.
  - For a text file, a 'magic' number is returned, which may only be used on a subsequent call to **fseek** to reposition to the current file position indicator.
  - On failure, **-1L** is returned and **errno** is set.
- **rewind** sets the current file position indicator to the start of the file indicated by stream. The file's error indicator is reset by a call of **rewind**. No value is returned.



# File position

- `int fseek(FILE *stream, long offset, int ptrname)`
- File position indicator for stream set to an arbitrary value (for binary files), or for text files, only to a position obtained from `ftell`, as follows:
  - For both functions, on success, zero is returned; on failure, non-zero is returned and `errno` is set.
  - General case: the file position indicator is set to offset bytes (characters) from a point in the file determined by the value of `ptrname`. Offset may be negative.



## File position

- The values of `ptrname` may be `SEEK_SET`, `SEEK_CUR`, and `SEEK_END`. The latter is not necessarily guaranteed to work properly on binary streams.
- For text files, offset must either be zero or a value returned from a previous call to `ftell` for the same stream, and the value of `ptrname` must be `SEEK_SET`.
- `fseek` clears the end of file indicator for the given stream and erases the memory of any `ungetc`. It works for both input and output.



# File position

- For **`ftell`** and **`fseek`** it must be possible to encode the value of the file position indicator into a **`long`**.
  - This may not work for very long files
  - **`fgetpos`** and **`fsetpos`** have been specified in a way that removes the problem.
- **`fgetpos`** stores the current file position indicator for stream in the object pointed to by **`pos`**.
  - The value stored is only used to return to the specified position for the same stream using **`fsetpos`**.
- **`fsetpos`** works as described above, also clearing the stream's end-of-file indicator and forgetting the effects of any **`ungetc`** operations.



# Example: text file

```
#include <stdio.h>
#include <stdlib.h>
int main(int argc, char *argv[])
{
 char ch, s[100], filename[]="textfile.txt";
 int i;
 FILE *fp;
 /* create file */
 fp = fopen(filename, "w");
 printf("\nInput lines of text for file. End with Ctrl/Z\n");
 while ((ch = getc(stdin)) != EOF) putc(ch, fp);
 fclose(fp);
 /* add text to file */
 fp = fopen(filename, "r+");
 fseek(fp, 0l, SEEK_END);
 printf("\nInput lines text to add to file. End with Ctrl/Z\n");
 while (fgets(s, sizeof(s), stdin) != NULL) fputs(s, fp);
 fclose(fp);
 /* display contents */
 printf("\nLines of the file (numbered):\n");
 i=1;
 fp = fopen(filename, "r");
 while (fgets(s, sizeof(s), fp) != NULL) printf("%d: %s", i++, s);
 fclose(fp);

 return 0;
}
```



# Files

- Text files
  - Characters are (usually) human readable
  - Are divided into lines
  - May contain a special “End-of-file” marker
  - Examples: source files, header files
- Binary files
  - None of the above characteristics
  - Examples: executables, object files, databases, etc.



# Error Handling

- System calls set a *global* integer called **errno** on error:
  - **extern int errno; /\* defined in errno.h \*/**
- The constants that errno may be set to are defined in **<errno.h>**.

For example:

- **EPERM** operation not permitted
- **ENOENT** no such file or directory (not there)
- **EIO** I/O error
- **EEXIST** file already exists
- **ENODEV** no such device exists
- **EINVAL** invalid argument passed

```
#include <stdio.h>
```

```
void perror(const char * s);
```

- E.G. if **errno==EINVAL**, then **perror("EINVAL: ")** ; prints:  
**EINVAL: : Invalid argument**



## File status

- `int stat(const char * pathname, struct stat *buf) ;`
- The `stat()` system call returns a structure (into a buffer you pass in) representing all the stat values for a given filename. This information includes:
  - the file's mode (permissions)
  - inode number (in Unix)
  - number of hard links
  - user id of owner of file
  - group id of owner of file
  - file size
  - last access, modification, change times
  - see header file `stat.h` and `sys/types.h` (`S_IFMT`, `S_IFCHR`, etc.)





# File status example

```
#include <stdio.h>
#include <stdlib.h>
#include <sys/stat.h>
#include <time.h>
int main(int argc, char *argv[])
{
 char *fname="main.c";
 struct stat statBuf;

 if (0==stat(fname, &statBuf))
 {
 printf("\nFile: %s", fname);
 if (S_ISDIR (statBuf.st_mode))
 puts("\n\tdirectory");
 if (S_ISCHR(statBuf.st_mode))
 puts("\n\tcharacter special file");
 if (S_ISBLK(statBuf.st_mode))
 puts("\n\tblock special file");
 if (S_ISREG(statBuf.st_mode))
 puts("\n\tregular file");
 if (S_ISFIFO(statBuf.st_mode))
 puts("\n\tFIFO special file, or a pipe");

 printf("\n\tinode=%u\n\tdevice=%c", statBuf.st_ino,
 statBuf.st_dev+'A');

 printf("\n\tlinks=%d\n\tuid=%d\n\tgid=%d\n\tsize=%ld",
 statBuf.st_nlink,
 statBuf.st_uid, statBuf.st_gid,
 statBuf.st_size);
 printf("\n\taccess time=%s\tcontents mod time=%s",
 ctime(&statBuf.st_atime),
 ctime(&statBuf.st_mtime),
 ctime(&statBuf.st_ctime));
 }
 else perror(0);
 system("PAUSE");
 return 0;
}
```



# File status example

- Program output example:

```
File: main.c
 regular file
 inode=0
 device=D:
 links=1
 uid=0
 gid=0
 size=1007
 access time=Thu Dec 21 08:47:51 2005
 contents mod time=Thu Dec 21 08:47:51 2005
 attrib mod time=Thu Dec 21 08:47:51 2005
```



# Algorithm examples

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- Cross product
- Combinations
- Permutations
- Power set



# Cross product

- Consider  $n$  sets of positive integers:  $A_1, A_2, \dots, A_n$ .
  - Set  $A_i$ , for  $i=1, 2, \dots, n$  has  $n_i$  elements
  - The cross product (Cartesian product, set direct product, product set) is required. i.e.

$$A_1 \times A_2 \times \dots \times A_n = \prod_{i=1}^n A_i$$

- having  $\prod_{i=1}^n n_i$  elements which will

be generated in a vector,  $p = [p_1 p_2 \dots p_n]$



## Cross product algorithm

- Set every element of vector  $p$  to 1.
  - This is the first element of the cross product
- Find next element as follows:
  - Find the highest index  $i$  for which  $p_i < n_i$ .  
If such an index cannot be found then all elements have been generated. Stop
  - Find next element of the cross product as  $\{p_1, p_2, p_{i-1}, p_{i+1}, 1, 1, \dots, 1\}$



# Cross product implementation. Non recursive

```
#include <stdio.h>
#define MAXN 10
void listProduct(int n, int prodNb, int p[])
{
 int i;
 printf("\n%3d ", prodNb);
 for (i = 1; i <= n; i++)
 printf(" %2d", p[i]);
 if (prodNb % 20 == 0)
 getch();
}
void crossProdNonRec(int n,
 int nElem[])
/* n = number of sets;
 nElem = vector with number
 of elements per set */
{
 int i, prodNb, p[MAXN];
 prodNb = 1;
 for (i = 1; i <= n; i++) p[i] = 1;
 listProduct(n, prodNb, p);
 i = n;
 while (i > 0)
 {
 p[i]++; // find highest such as p[i] > nElem[i]
 if (p[i] > nElem[i])
 {
 p[i] = 1;
 i--;
 }
 else
 {
 prodNb++;
 listProduct(n, prodNb, p);
 i = n;
 }
 }
}
```



# Cross product implementation. Non recursive

```
int main(int argc, char *argv[])
{
 int i, n, nElem[MAXN];
 printf("\nNumber of sets [<%d]= ", MAXN); scanf("%d", &n);
 for (i = 1; i <= n; i++)
 {
 printf("Number of elements in set %d=", i);
 scanf("%d", &nElem[i]);
 }
 printf("\nThe members of the cross product");
 printf("\nNo. Elements");
 crossProdNonRec(n, nElem);
 getchar();
 return 0;
}
```



# Cross product implementation. Recursive

```
#include <stdio.h>
#include <conio.h>
#define MAXN 10
int prodNb, p[MAXN],
 nElem[MAXN];
void listProduct(int n)
{
 int i;

 printf("\n%3d ", prodNb);
 for (i = 1; i <=n; i++)
 printf(" %2d", p[i]);
 if (prodNb % 20 == 0)
 getch();
}

void crossProdRec(int n, int i)
/* n = number of sets; nElem =
 vector with number of elements
 per set */
{
 int j;

 for (j = 1; j <=nElem[i]; j++)
 {
 p[i] = j;
 if (i< n) crossProdRec(n, i+1);
 else
 {
 prodNb++;
 listProduct(n);
 }
 }
}
```





# Cross product implementation. Recursive

```
int main(int argc, char *argv[])
{
 int i, n;
 printf("\nNumber of sets [<%d]=", MAXN); scanf("%d", &n);
 for (i = 1; i <= n; i++)
 {
 printf("Number of elements in set %d=", i);
 scanf("%d", &nElem[i]);
 }
 printf("\nThe members of the cross product");
 printf("\nNo. Elements");
 crossProdRec(n, 1);
 getch();
 return 0;
}
```



# Combinations

- Let  $P$  be a set of  $n$  elements
- All ways of picking  $k$  unordered elements of the  $n$  elements = generating all subsets with  $k \leq n$  elements of  $P$  such as any two subsets are distinct
  - The number of subsets is the *binomial coefficient* or *choice number* and read " $n$  choose  $k$ "



# Combinations algorithm

- First subset is  $p = \{1, 2, \dots, k\}$
- Given a subset, its successor is found as follows:
  - Going from  $k$  down to 1 find index  $i$  which satisfies the relationships
$$\begin{aligned}p_i &< n - k + i \\p_{i+1} &= n - k + i + 1 \\&\dots \\p_{k-1} &= n - 1 \\p_k &= n\end{aligned}$$
  - Successor set is:
$$\{p_1, p_2, \dots, p_i + 1, p_i + 2, \dots, p_i + n - k + 1\}$$
  - The last subset is:
$$\{n - k + 1, n - k + 2, \dots, n - 1, n\}$$



# Combinations algorithm implementation. Non recursive

```
void combinNonRec(int n, int k)
{
 int p[MAXN];
 int i, j, combinNb;
 for (i=1; i <=k; i++) p[i]=i; /* first combination */
 listCombin(k, combinNb, p);
 i = k;
 while (i > 0) /* generate the next combinations */
 {
 p[i]++; // find index satisfying relation set
 if (p[i] > n - k + i) i--;
 else
 {
 for (j = i + 1; ; j <= k; j++) p[j]=p[j-1] + 1;
 combinNb++;
 listCombin(k, combinNb, p);
 i = k;
 }
 }
}
```



# Combinations algorithm implementation. Recursive

```
void combinRec(int n, int k, int i)
{
 int j;
 for (j = p[i-1]+1; j <= n-k+i; j++)
 {
 p[i] = j;
 if (i < k) combinRec(n, k, i+1);
 else
 {
 combinNb++;
 listCombin(k, combinNb, p);
 }
 }
}
```

## ■ Notes

- Array **p**, and **combinNb** must be global
- Invocation is: **combinRec(n, k, 1)**



# Generating Permutations

- For instance 35241 is the permutation that maps 1 to 3, 2 to 5, 3 to 2, 4 to 4, and 5 to 1.
- We know that there are  $7!$  permutations on  $\{1,2,3,4,5,6,7\}$ .
  - Suppose we want to list them all. Is there an efficient way to do so? It turns out to be fairly simple to list them lexicographically.
  - The only hard question is, given one permutation, how do we find the next one?

- The lexicographically first permutation is

$$1 \ 2 \ \dots \ n$$

- and the last is

$$n \ n-1 \ \dots \ 1$$



# Generating Permutations

- It is intuitively reasonable that if the final digits of a permutation are in descending order, then no rearrangement will make them larger.
  - For instance in *1257643* we cannot produce a larger number by rearranging the 7643.
  - Instead we must increase the next most significant digit (the 5) by the next larger digit in 7643 (the 6).
  - Then the remaining digits (the 5 and the 743) must be arranged to form the smallest number possible.
  - Thus the next permutation in lexicographic order is *1263457*.



# Generating permutations in lexicographical order

- a. First permutation is  $p = \{1, 2, \dots, n\}$
- b. Given vector  $p = [p_1 \ p_2 \ \dots \ p_n]$  the next permutation is found as follows:

1. Look from  $n$  down to 1 for the highest valued index which satisfies the relationships:

$$p_i < p_{i+1}$$

$$p_{i+1} > p_{i+2} > \dots > p_n$$

2. Find the maximum element,  $p_k > p_i$  of  $p_{i+1}, p_{i+2}, \dots, p_n$
3. Swap  $p_k$  with  $p_i$
4. Revert  $p_{i+1}, p_{i+2}, \dots, p_n$  by swapping  $p_{i+1}$  and  $p_n$ ,  $p_{i+2}$  and  $p_{n-1}$ , a.s.o.





# Permutations implementation. Non recursive

```
void permNonRec(int n) {
 int p[MAXN];
 int i, k, permNb = 0;

 /* first permutation, step a */
 for (i = 1; i <= n; i++) p[i] = i;
 listPerm(n, ++permNb, p);
 do /* generate the next permutations */
 {
 i = n - 1;
 while (p[i] > p[i+1] && i > 0) i--; /*
step b1 */
 if (i > 0) {
 for (k = n; p[i] > p[k]; k--); /*
step b2 */
 swap(&p[i], &p[k]); /* step b3 */
 revert(p, i, n, (n - i) / 2);
 listPerm(n, ++permNb, p);
 }
 } while (i > 0);
}

void swap(int *i, int *j)
{
 int temp;
 temp = *i;
 *i = *j;
 *j = temp;
}

void revert(int p[], int i, int n,
 int k)
{
 int j;
 for (j = 1; j <= k; j++)
 swap(p[i+j], p[n+1-j]);
}
```



# A note on swapping

## ■ Swapping integers in place

```
void swap(int *i, int *j)
{
 *i += *j; // i == i + j
 *j = *i - *j; // j == i + j - j == i
 *i -= *j; // i == i + j - i == j
}

void swap(int *i, int *j)
{
 *i ^= j; // a == a^b;
 *j ^= *i; // b == b^(a^b)
 *i ^= *j; // a == (a^b)^(b^(a^b))
}
```

final b

final a

| $a$ | $b$ | $a^b$ | $b^{(a^b)}$ | $(a^b)^{(b^{(a^b)})}$ |
|-----|-----|-------|-------------|-----------------------|
| 0   | 0   | 0     | 0           | 0                     |
| 0   | 1   | 1     | 0           | 1                     |
| 1   | 0   | 1     | 1           | 0                     |
| 1   | 1   | 0     | 1           | 1                     |

Second version  
based on proof on the  
nearby table, where  $a$   
and  $b$  are bit positions



# Permutations implementation. Recursive

```
void permRec(int nb)
{
 int i, j;

 if (nb == 1)
 {
 permNb++;
 listperm();
 }
 else
 {
 permRec(nb - 1);
 for (i = 1; i <= nb - 1; i++)
 {
 swap(p[i], p[nb]);
 permRec(nb - 1);
 swap(p[i], p[nb]);
 }
 }
}
```

## ■ Notes

- Generates recursively permutations of elements  $p_1 p_2 \dots p_{n-1}$  with  $p_n$  in position  $n$
- Then swaps  $p_i$  with  $p_n$  for  $i = 1..n-1$ , and generates all permutations
- Array **p**, **n**, and **permNb** must be globals
- First permutation must be initialized separately
- Invocation: **permRec(n)**
- Order is not loxicographic



## Generating $k$ permutations of $n$

- For set  $p = \{1, 2, \dots, n\}$  and  $k \leq n$ , positive
  - generate all  $k$ -subsets such any two subsets must differ either in the composing elements or in their order
- Algorithm idea:
  - generate all combinations of  $n$  elements taken  $k$ , and, for each combination
    - generate the  $k!$  permutations



# Generating $k$ permutations of $n$ implementation

```
void arrange(int n, int m, int i) {
 int j, k, r;
 for (j = p[i-1] + 1; j <= n - m + i; j++) // recursively generate combinations
 {
 p[i] = j;
 if (i < m) arrange(n, m, i + 1);
 else
 {
 arrNb++;
 listArrang(m, p);

 for (k = 1; k <= m; k++) v[k] = p[k]; // save combination
 do // nonrecursively permute combination
 {
 k = m - 1;
 while (v[k] > v[k + 1] && k > 0) k--;
 if (k > 0) {
 for (r = m; v[k] > v[r]; r--);
 swap(&v[k], &v[r]);
 revert(k, m, (m - k) / 2);
 arrNb++;
 listArrang(m, v);
 }
 }
 while (k > 0);
 }
 }
}
```



# Generating a power set

- We wish to generate all  $2^n$  subsets of set  $A = \{a_1, \dots, a_n\}$  (power set)
  - All subsets of  $A = \{a_1, \dots, a_n\}$  can be divided to two groups
    - Ones that contain  $a_n$
    - Ones that does not contain  $a_n$
  - Ones that does not contain  $a_n$  are all subsets of  $\{a_1, \dots, a_{n-1}\}$ 
    - When we have all subsets of  $\{a_1, \dots, a_{n-1}\}$  we can create all subsets of  $\{a_1, \dots, a_n\}$  by adding all elements with  $a_n$  inserted



# Generating a power set

- Again, we try to generate all subsets without generating power sets of smaller sets
- We can associate  $2^n$  subsets of  $n$  elements set  $A = \{a_1, \dots, a_n\}$  with  $2^n$  bit strings  $b_1 \dots b_n$ 
  - $b_i = 1$  if  $a_i$  is element of set
  - $b_i = 0$  if  $a_i$  is not element of set
- For 3 elements set  $\{a_1, a_2, a_3\}$ 
  - 000 – the empty set
  - 111 – the set itself
  - 110 – subset  $\{a_1, a_2\}$
- We can create bit strings by generating binary numbers from 0 to  $2^n - 1$
- Example:

|             |             |       |       |            |       |            |            |                 |
|-------------|-------------|-------|-------|------------|-------|------------|------------|-----------------|
| Bit strings | 000         | 001   | 010   | 011        | 100   | 101        | 110        | 111             |
| Subsets     | $\emptyset$ | $a_3$ | $a_2$ | $a_2, a_3$ | $a_1$ | $a_1, a_3$ | $a_1, a_2$ | $a_1, a_2, a_3$ |



# Generating a power set. Non recursive

```
void allSubsetsNR(int n)
{
 int i, setNb, p[MAXN]; // p[i]=1 if element i is a member,
 // i.e p is a characteristic vector
 setNb=1;
 for (i=1; i<=n; i++) p[i]=0; /*empty set */
 listSet(n, setNb, p);
 for (i=n; i>0;) /* generate next subsets */
 {
 if (p[i] == 0)
 {
 p[i] = 1;
 setNb++;
 listSet(n, setNb, p);
 i = n;
 }
 else
 {
 p[i] = 0;
 i--;
 }
 }
}
```





# Generating a power set. Recursive

```
void allSubsetsRec(int n, int i)
{
 int j;
 for (j=0; j <= 1; j++)
 {
 p[i] = j;
 if (i < n)
 allSubsetsRec(n, i+1);
 else
 {
 setNb++;
 listSet(n, setNb);
 }
 }
}
```

```
void listSet(int n, int
setNb)
{
 int i;

 printf("\n%3d { ", setNb);
 for (i = 1; i <=n; i++)
 if (p[i] == 1)
 printf(" %2d,", i);
 printf("\b }");
 if (setNb % 20 == 0)
 getch();
}
```

- Note that array **p** and variable **setNb** must be global



## Reading

- Deitel: chapter 11
- Prata: chapter 13
- King: chapter 22
- Supplemental:
  - R. Sedgewick:  
[http://www.cs.princeton.edu/~rs/talks/perms.p  
df](http://www.cs.princeton.edu/~rs/talks/perms.pdf)



# Summary

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- File handling
  - High level I/O
    - fopen
    - fclose
    - fread
    - fwrite
    - fsetpos, fgetpos, ftell, fseek
- Applications
  - Combinatorial generation: generating subsets
    - Cross product (Cartesian product)
    - Combinations
    - Permutations
    - Arrangements
    - Power set