

VII The electric current

1. The electric current intensity

1.1. Definition

Def. The ordered motion of electric charge particle is called electric current.

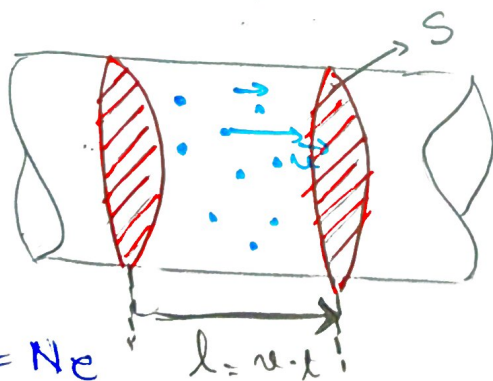
- two types of electric current

- of conduction

- electrons in conductors;
- electrons and holes in semiconductor;
- ions, electrons in plasma/gases;

- of convection

1.2.



$$Q = Ne$$

$$l = v \cdot t$$

Note: $n = \frac{N}{V}$ ($n = \frac{dN}{dV}$ *)

$$N = n \cdot V = n \cdot S \cdot l = n \cdot S \cdot v \cdot t$$

$$Q = n \cdot e \cdot v \cdot S \cdot t$$

Def:
$$I = \frac{dQ}{dt}$$

$$I = \frac{d}{dt} (n \cdot e \cdot v \cdot S \cdot t) = \frac{n \cdot e \cdot v \cdot S \cdot dt}{dt}$$

$$I = n \cdot e \cdot v \cdot S$$

Note:
$$\vec{j} = \frac{dI}{dS}$$
 — the electric current density

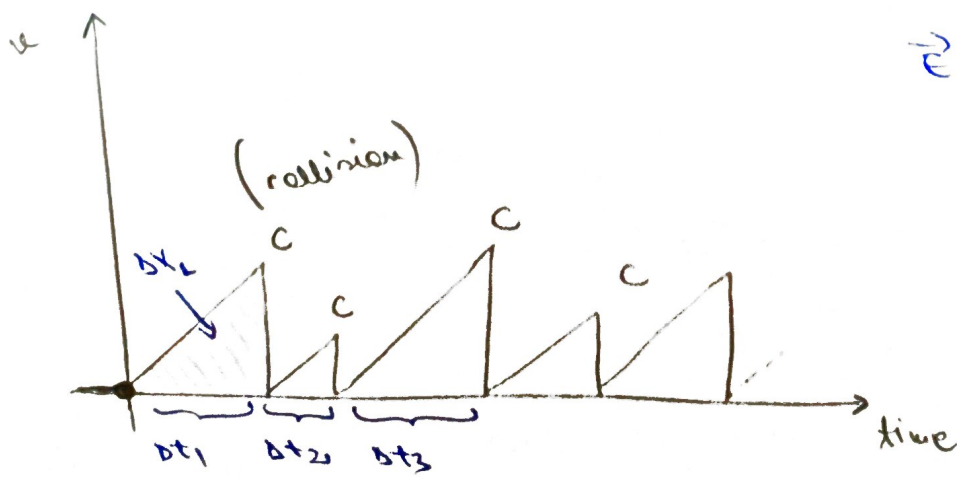
$$\vec{j} = \frac{d(n \cdot e \cdot v \cdot S)}{dS} \Rightarrow$$

$$\vec{j} = n \cdot e \cdot \vec{v}$$

$$dI = \vec{j} \cdot d\vec{S} \quad | \quad \int \Rightarrow \int dI = \int_S \vec{j} \cdot d\vec{S} \Rightarrow$$

$$\Rightarrow I = \int_S \vec{j} \cdot d\vec{S}$$

2. The Ohm's law



(note)

$$\vec{E} = -\nabla V$$

$$\vec{F}_e = e\vec{E}$$

$$\vec{F}_e = m_e \cdot \vec{a}$$

$$\vec{a} = \frac{e\vec{E}}{m_e}$$

m_e : a universal constant

$$\Delta x_i = \frac{a \cdot \Delta t_i^2}{2} \Rightarrow \Delta x = \sum_{i=1}^n \Delta x_i = \frac{eE}{2m_e} \sum_{i=1}^n \Delta t_i^2$$

$$n = \frac{\Delta x}{\Delta t} = \frac{eE}{2m_e} \frac{\sum_{i=1}^n \Delta t_i^2}{\Delta t}$$

Note: $\tau = \frac{\sum_{i=1}^n \Delta t_i^2}{\Delta t}$ - the average time between two collisions

$$\vec{v} = \frac{e \cdot \tau}{2m_e} \cdot \vec{E} \quad \Rightarrow$$

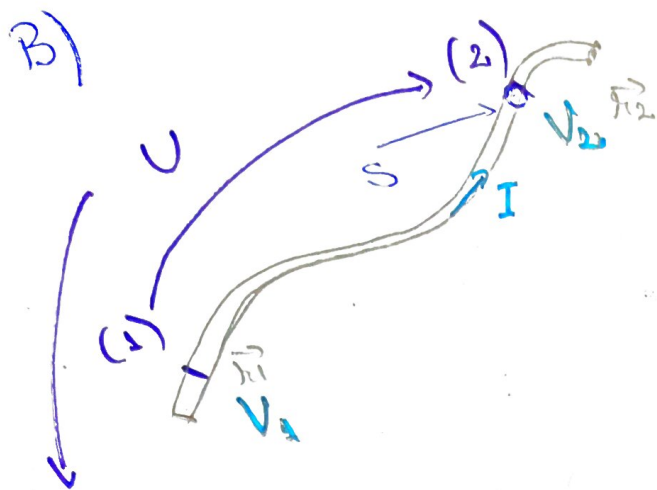
$$\vec{j} = n \cdot e \cdot \vec{v}$$

$$\Rightarrow \vec{j} = \frac{n \cdot e^2 \tau}{2m_e} \vec{E}$$

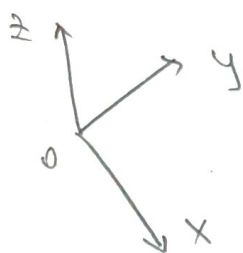
Note: $\sigma = \frac{n e^2 \tau}{2m_e}$ - the electric conductivity

$$\boxed{\vec{j} = \sigma \cdot \vec{E}}$$

The local form of the OHM's law



electric tension (a drop of potential)



$$\rho = \frac{I}{S}$$

Note $\rho = \frac{1}{\sigma}$ electric the resistivity

$$\Delta V = - \int_{r_1}^{r_2} \vec{E} \cdot d\vec{r}$$

$$U = V_1 - V_2 = - \Delta V \Rightarrow U = \int_{r_1}^{r_2} E \, dr = E \int_{r_1}^{r_2} dr$$

\uparrow \uparrow
 high low
 potential potential

$$U = E \cdot l \Rightarrow \boxed{E = \frac{U}{l}}$$

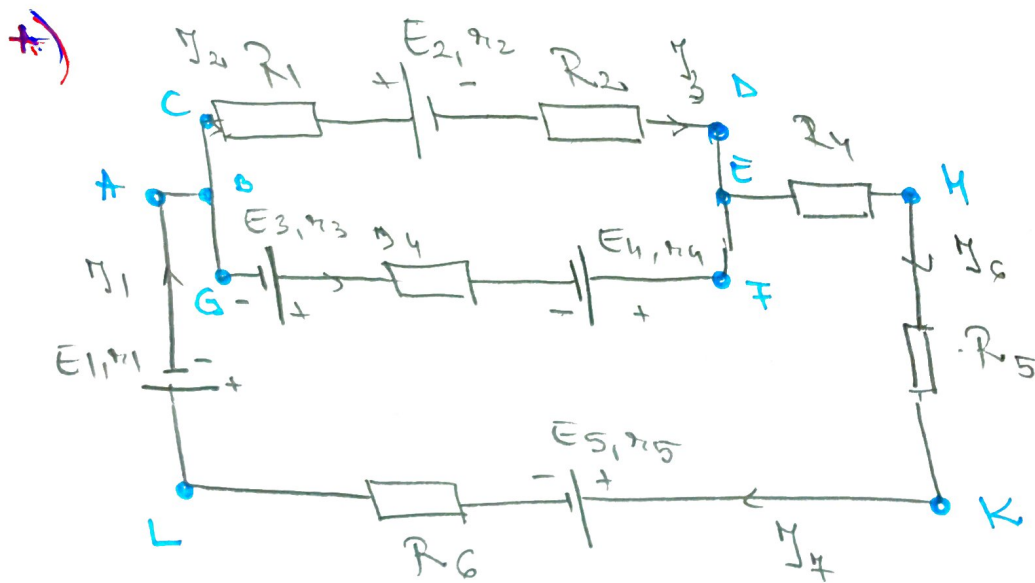
$$\frac{I}{S} = \frac{1}{\rho} \cdot \frac{U}{l} \Rightarrow U = \rho \cdot \frac{l}{S} I$$

Note: $R = \rho \cdot \frac{l}{S}$ - electric resistance

$$U = R \cdot I$$

Ohm's law.
for a part of an electric circuit

2. The elements of an electric circuit



Kirchhoff's laws

L_1 :

R, E : nodes

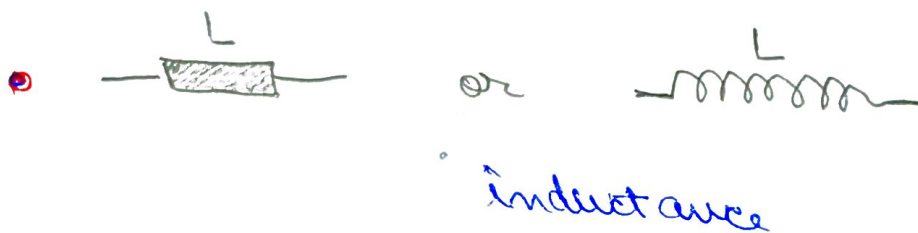
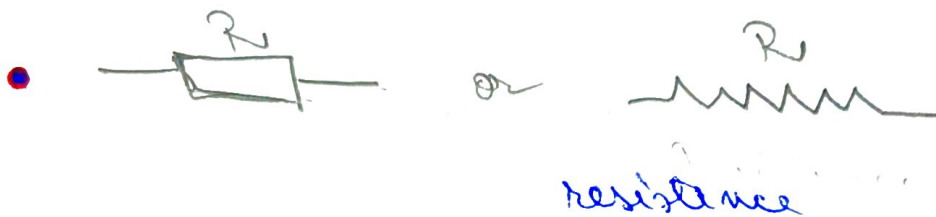
$$\sum_i I_i = 0$$

L_2 - refers to an eye of an electric circuit
a close loop

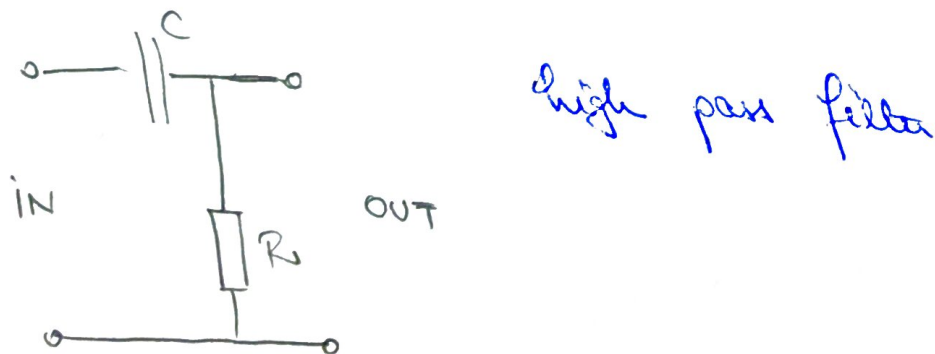
(C, D, E, F, G, B, C) - an eye

$$\sum_{i=1}^N \mathcal{E}_i = \sum_{j=1}^N R_j I_j$$

B)

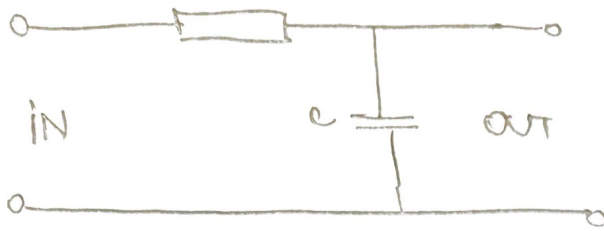


C)



$$\omega_c = \frac{1}{2\pi RC}$$

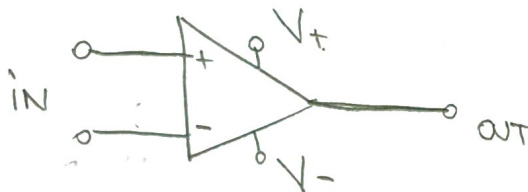
A) low pass filter



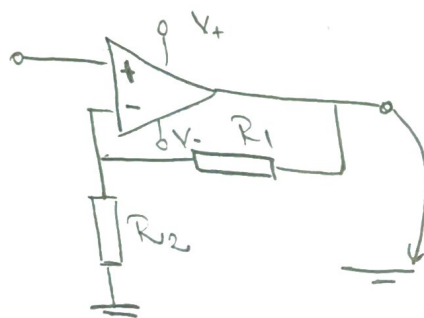
$$V_c = \frac{1}{2\pi RC}$$

III) **DAC** (digital to analog converter)
ADC (analog to digital converter)

IV) Ops Amp
 (operational amplifiers)



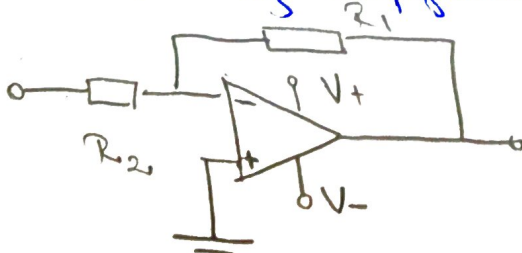
Project Idea.



$$A = 1 + \frac{R_1}{R_2}$$

Amplification
(GAIN)

• inverting configuration



$$A = -\frac{R_1}{R_2}$$

(choose the right values for R_1, R_2)