

ACOUSTICS

1. Definition

Acoustics is part of physics that studies the creation, propagation, reception and properties of sound.

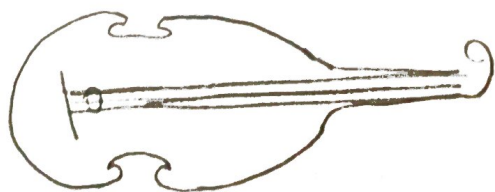
A mechanical wave capable to impress to human hearing organ is called sound.

2. Sound characteristics

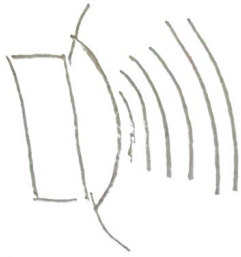
- to be produced by a sound source ;
- the existence of an elastic medium between source and receiver ;
- The mechanical wave frequency should be larger than 16 Hz and smaller than 20 kHz ; $16 \text{ Hz} \leq \nu \leq 20 \text{ kHz}$.
- the power of mechanical wave should be high enough to produce an auditive sensation
- The sound intensity should be higher than the threshold $I = I_0 = 10^{-12} \text{ W/m}^2$;
- the duration of a mechanical oscillation should be larger than 0.05 s ; $t_s \geq 0.05 \text{ s}$.

3. Sound sources

3.1. Vibrating cordes



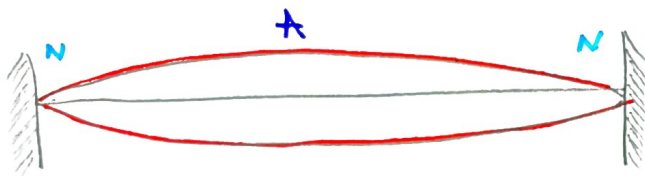
3.2 Vibrating membranes



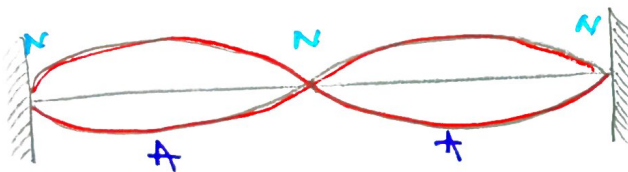
3.3 Vibrating air columns



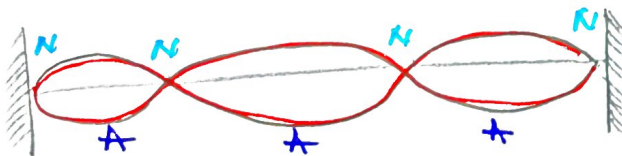
4. Fundamental sound and superior harmonics



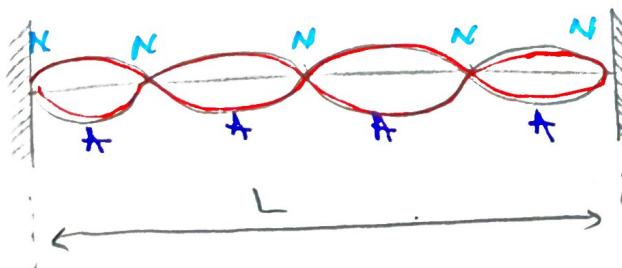
$$\lambda_1 = \frac{2L}{1}$$



$$\lambda_2 = \frac{2L}{2}$$



$$\lambda_3 = \frac{2L}{3}$$



$$\lambda_4 = \frac{2L}{4}$$

$$\lambda_n = \frac{2L}{n}$$

$$v_n = \frac{v}{\lambda_n}$$

\Rightarrow

$$v_n = \frac{v}{2L} n$$

$$v_1 = \frac{v}{2L}$$

fundamental frequency

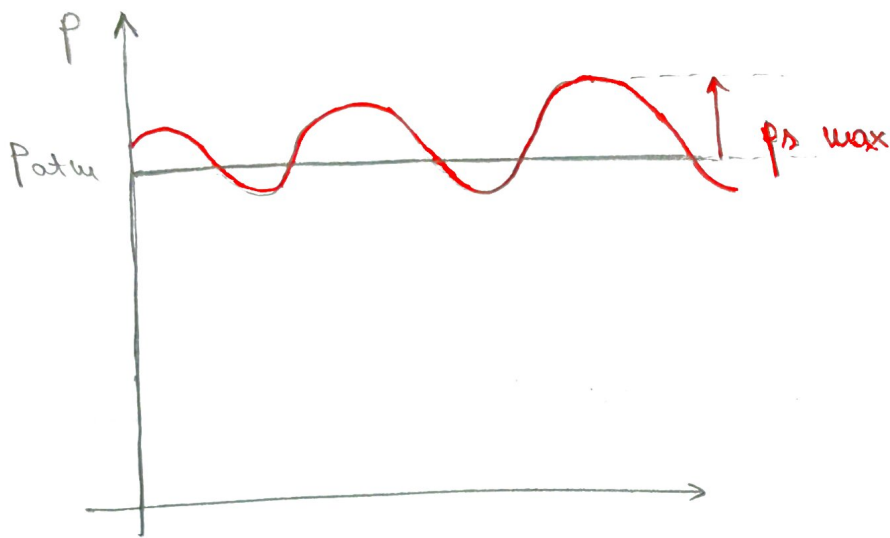
$$V_m = n \cdot V_L$$

superior harmonics

$$n = 2, 3, 4, \dots$$

5. The sound properties

5.1 The sound pressure



$$p_s(t) = p_{s, \max} \sin(\omega t) ;$$

$$p_{s, \max} = \rho \cdot v \cdot A \cdot \omega$$

ρ : the density
 v : velocity

the elastic media

A : amplitude

ω : pulsation

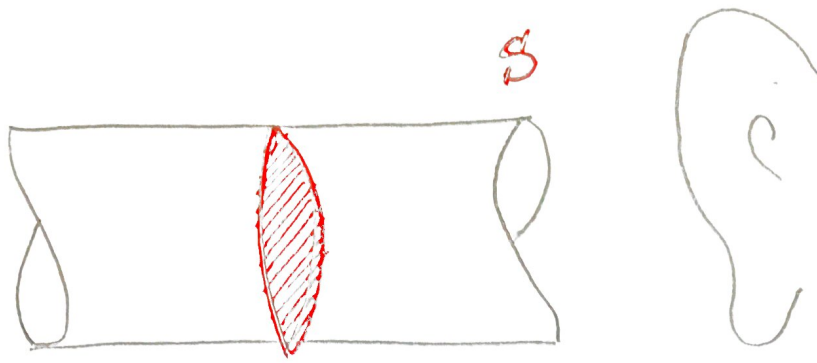
external perturbation
(harmonic oscillation)

5.2 The sound intensity

$$I = \frac{1}{S} \left\langle \frac{dW}{dt} \right\rangle_t ; [I]_{is} = \frac{W}{m^2 \cdot s}$$

$\langle \rangle_t$ - the time average

W : energy



$$I = \frac{1}{2} \rho v A^2 \omega^2$$

$$I = \frac{\rho v A^2 \omega^2}{2 \rho v}$$

$$I = \frac{(\rho v A \omega)^2}{2 \rho v}$$

$$I = \frac{P_{s, \max}^2}{2 \rho v}$$

Note: $Z = \rho v$ - the acoustic impedance.

$$I = \frac{P_{s, \max}^2}{2 Z}$$

$$P_{s, \text{eff}} = \frac{P_{s, \max}}{\sqrt{2}}$$

$P_{s, \text{eff}}$ - (effective quantity) major value

$$P_{s, \text{eff}}^2 = \frac{P_{s, \max}^2}{2}$$

$$I = \frac{P_{s, \text{eff}}^2}{Z}$$

5.3 The sound level

$$I_0 = 10^{-12} \frac{W}{m^2} \leq I \leq 10^4 \frac{W}{m^2}$$

$$\log_{10} \left(\frac{I}{I_0} \right) = 14$$

$$N_s = 10 \log_{10} \left(\frac{I}{I_0} \right) \text{ (dB)}$$

5.4 The acoustic level

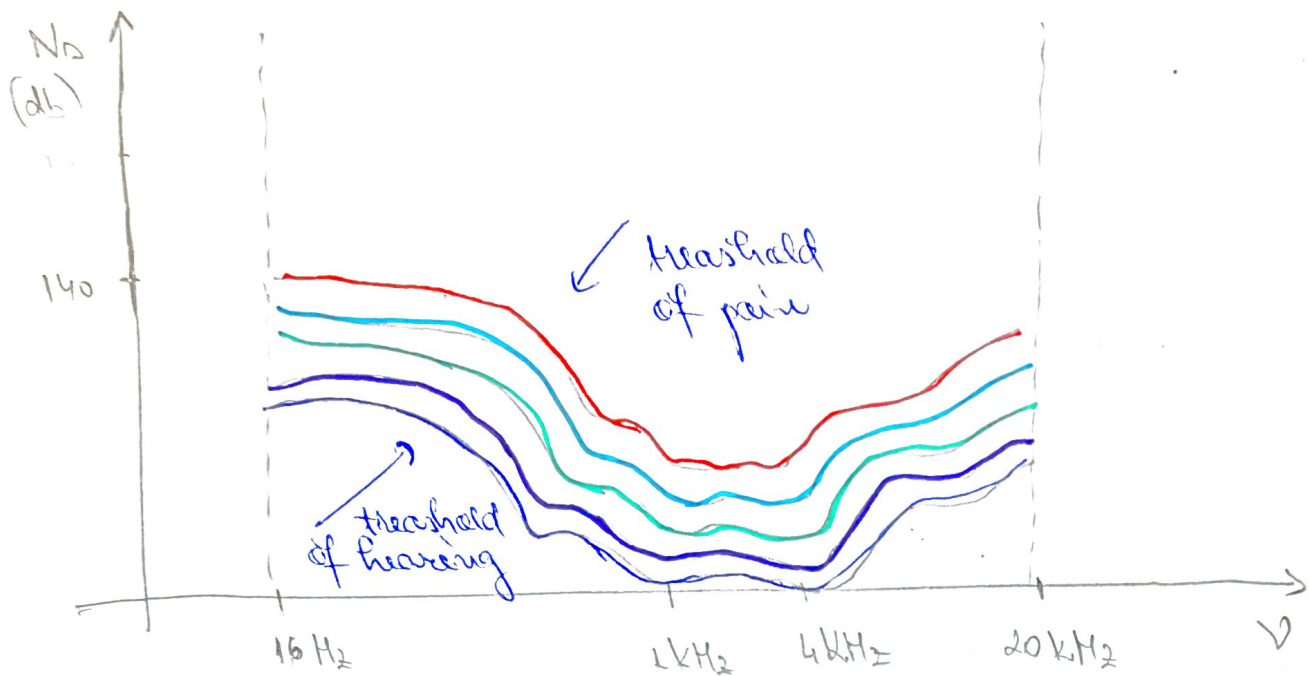
$$N_a = 10 \lg \left(\frac{I_a}{I_0} \right)$$



6. The sound parameters

6.1. The loudness

→ The physiological parameter of a sound related to its intensity.



6.2. The Pitch

↳ highness or lowness of a musical tone related to the sound frequency

6.3. The timbre

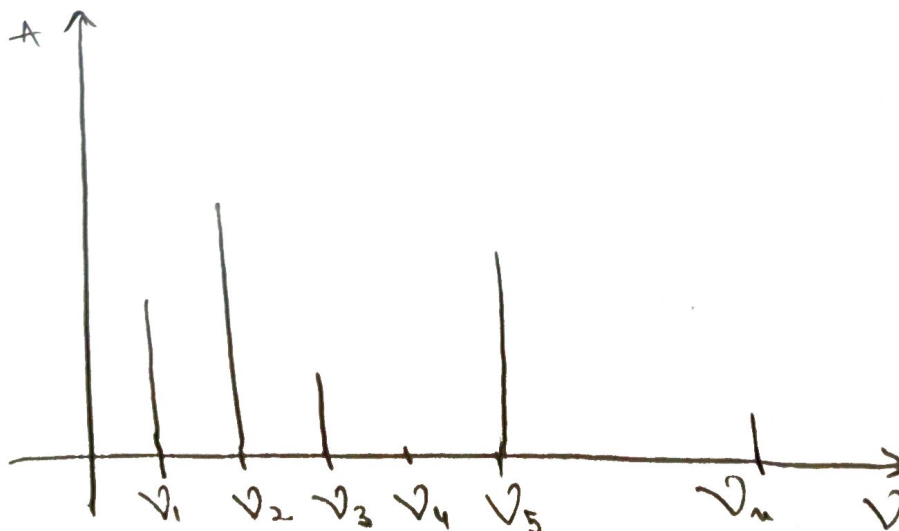
$$S(t) = A_1 \sin(\omega_1 t) + A_2 \sin(\omega_2 t) + A_3 \sin(\omega_3 t) + \dots$$

$$\omega = 2\pi v$$

$$v_n = n \cdot v_1$$

$$S(t) = \sum_{n=1}^N A_n \sin(2\pi n v_1 t)$$

Fourier transformation →

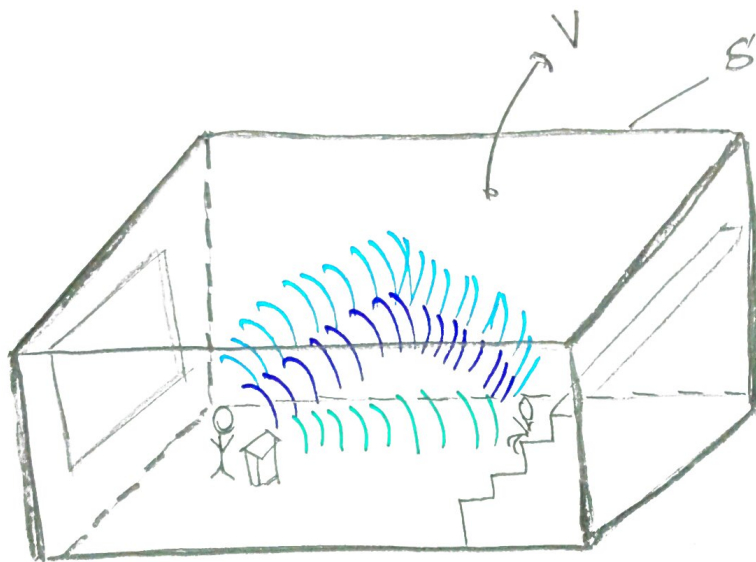


6.4. The noise

Def. A sound which contains too many components is called a noise.

7. The Reverberation

Ⓐ



Def. The collection of reflected sounds into an enclosure like an auditorium room is called reverberation.

Ⓑ The reverberation time, t_R

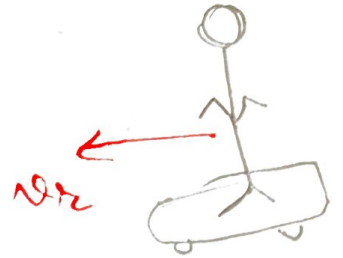
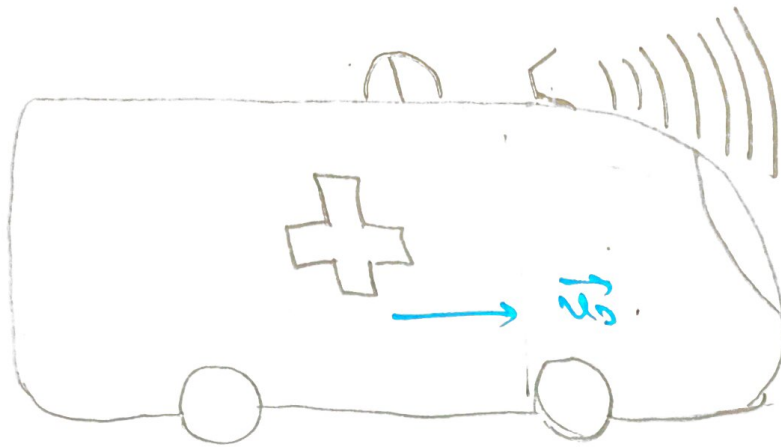
Def. The reverberation time is the time in which the sound level decreases with 60 dB or the intensity increases with 10^6 .

$$t_R = 0.16 \frac{V}{L \cdot S}$$

V - volume, S - surface (area of the surface);
 L - the absorption coefficient;

If $t_R > 0.1s \Rightarrow$ BAD ACOUSTICS

8. The Doppler effect



v_s : velocity of the sound source

C : the sound velocity

v_r - receiver velocity

$$V = V_0 \frac{C \pm v_r}{C \mp v_s}$$

The upper sign should be used if the distance between the source and receiver decreases,

The lower sign should be used if the distance between the source and receiver decreases,