Part IX.
Syntax Directed Translation and Intermediate Code

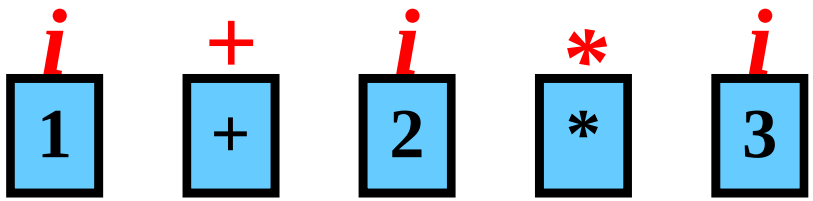
Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }

Rule: **Action:**



Syntax-Directed Translation

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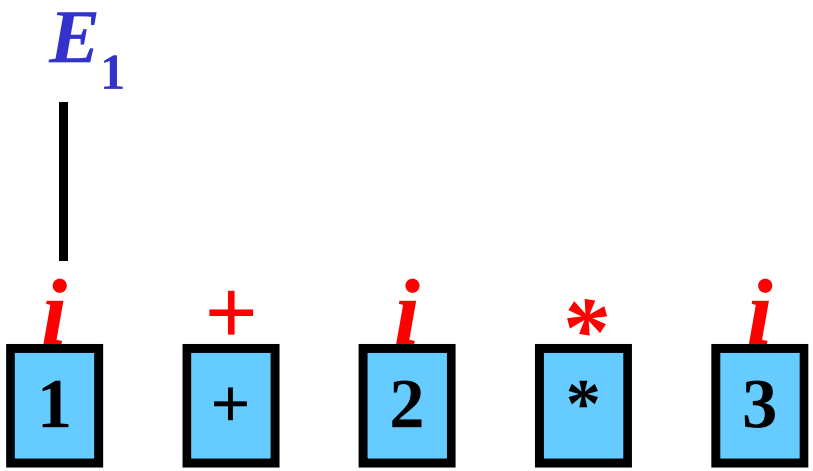
Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ Ei.a := Ej.a + Ek.a}
$E_i \rightarrow E_j * E_k$	{ Ei.a := Ej.a * Ek.a}
$E_i \rightarrow (E_j)$	{ Ei.a := Ej.a }
$E_i \rightarrow i$	{ Ei.a := i.val }

Rule: **Action:**

$E_1 \rightarrow i$



Syntax-Directed Translation

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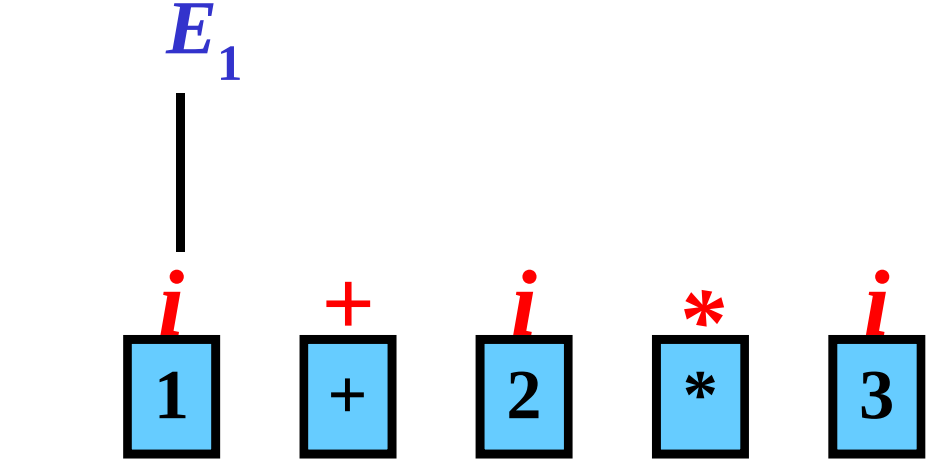
Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }

Rule: $E_1 \rightarrow i$ **Action:** E_1.a := i.val

E_1.a = 1



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Example:

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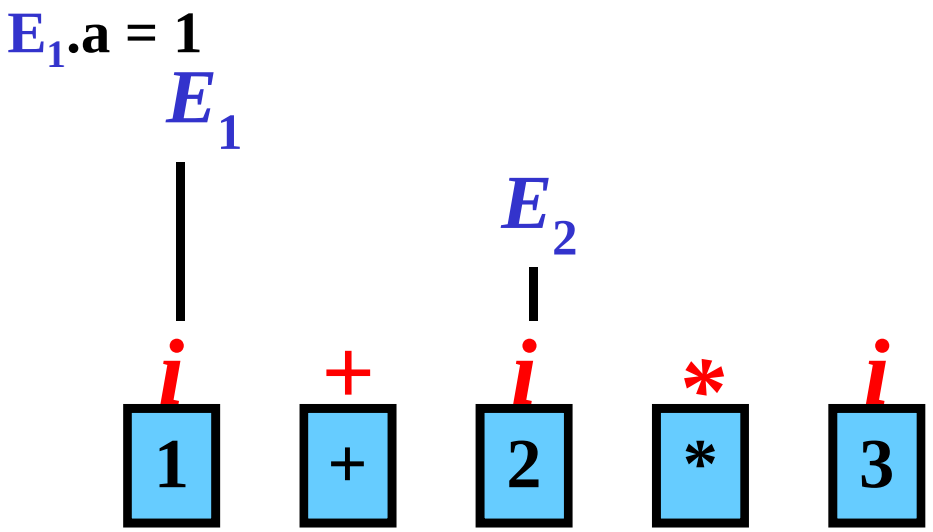
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	

Syntax-Directed Translation

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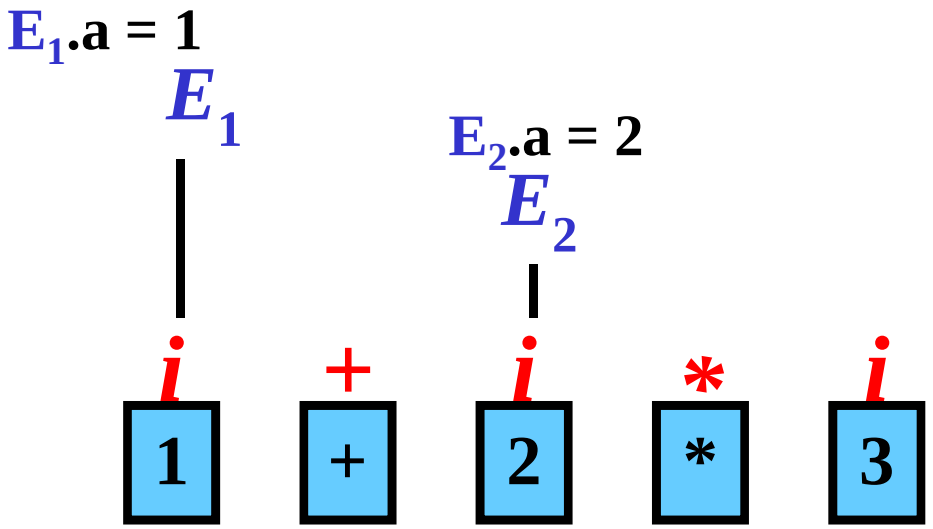
Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	E_2.a:= i.val

Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
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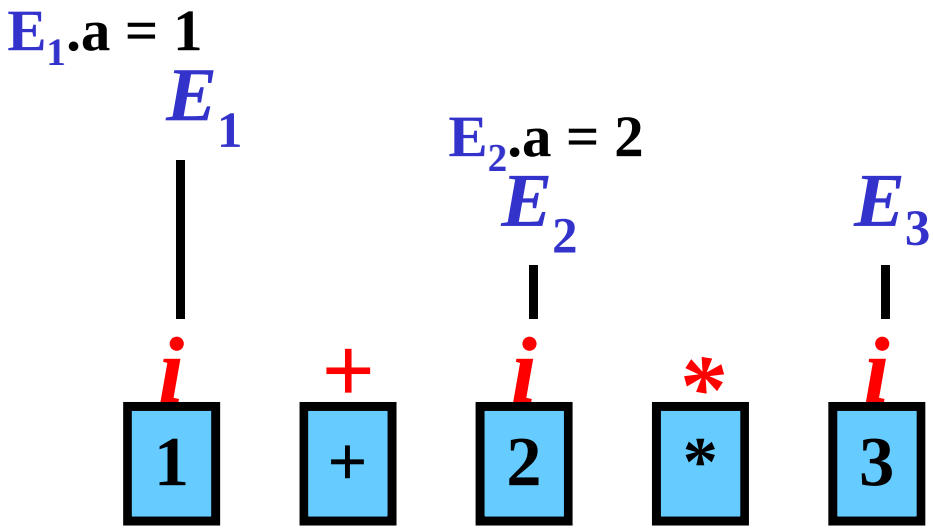
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



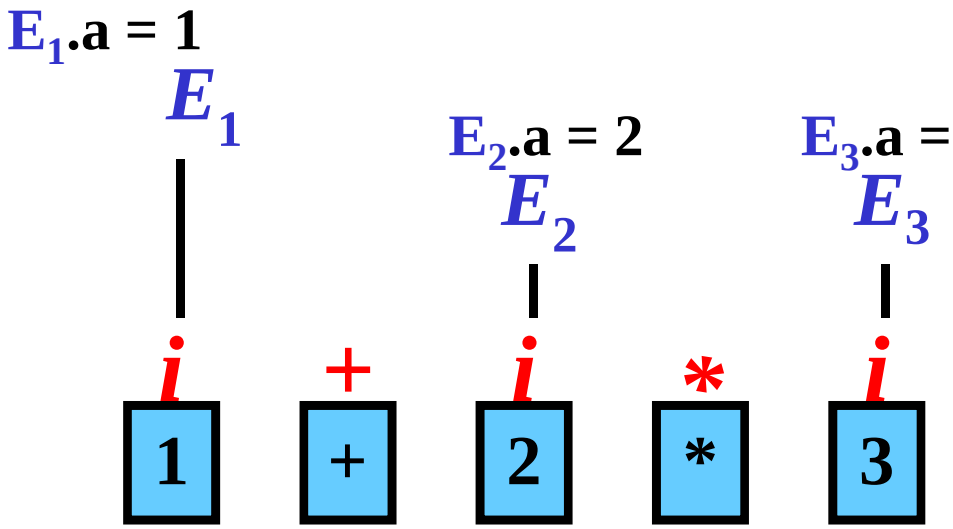
Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	E_2.a:= i.val
$E_3 \rightarrow i$	

Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



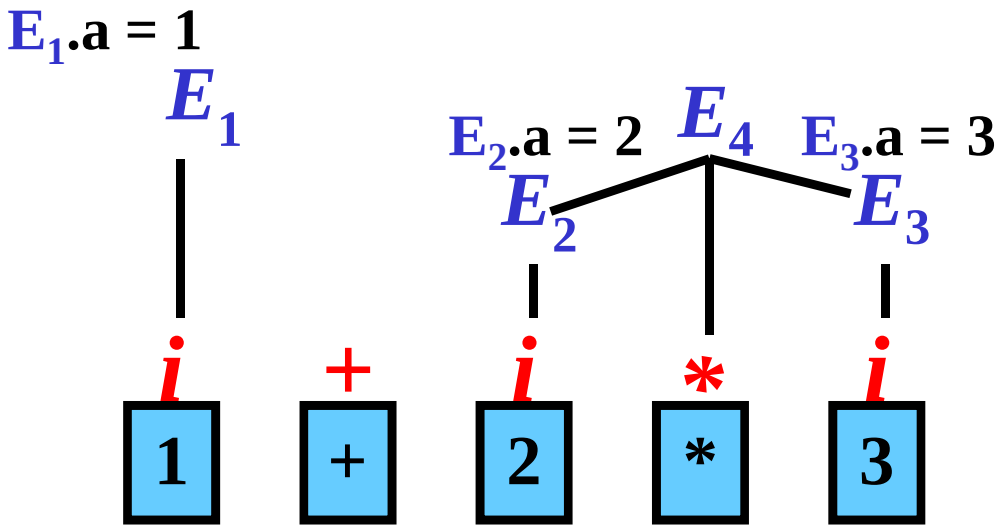
Rule:	Action:
$E_1 \rightarrow i$	E_1.a := i.val
$E_2 \rightarrow i$	E_2.a := i.val
$E_3 \rightarrow i$	E_3.a := i.val

Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



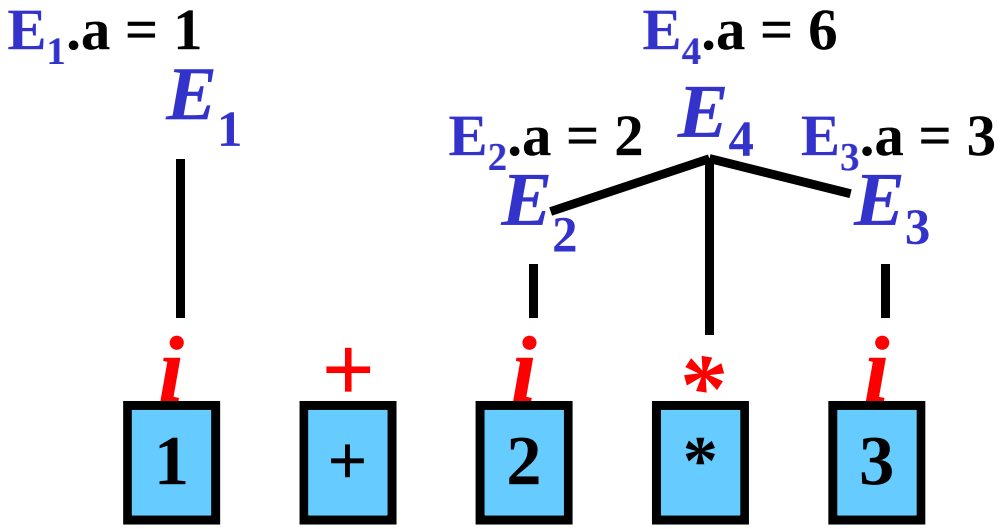
Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	E_2.a:= i.val
$E_3 \rightarrow i$	E_3.a:= i.val
$E_4 \rightarrow E_2 * E_3$	

Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



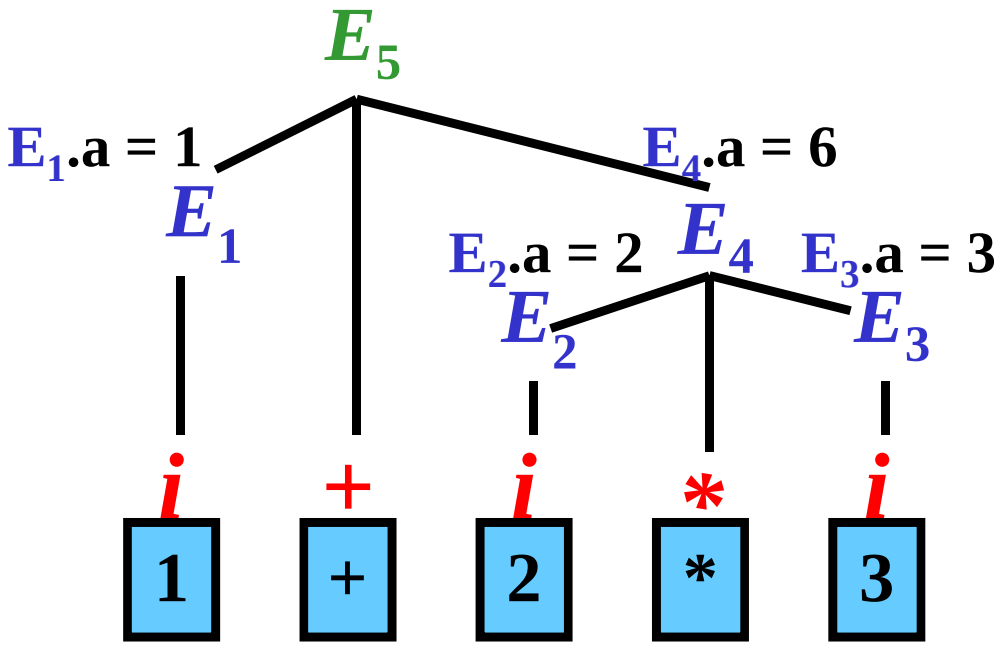
Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	E_2.a:= i.val
$E_3 \rightarrow i$	E_3.a:= i.val
$E_4 \rightarrow E_2 * E_3$	E_4.a:= E_2.a*E_3.a

Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



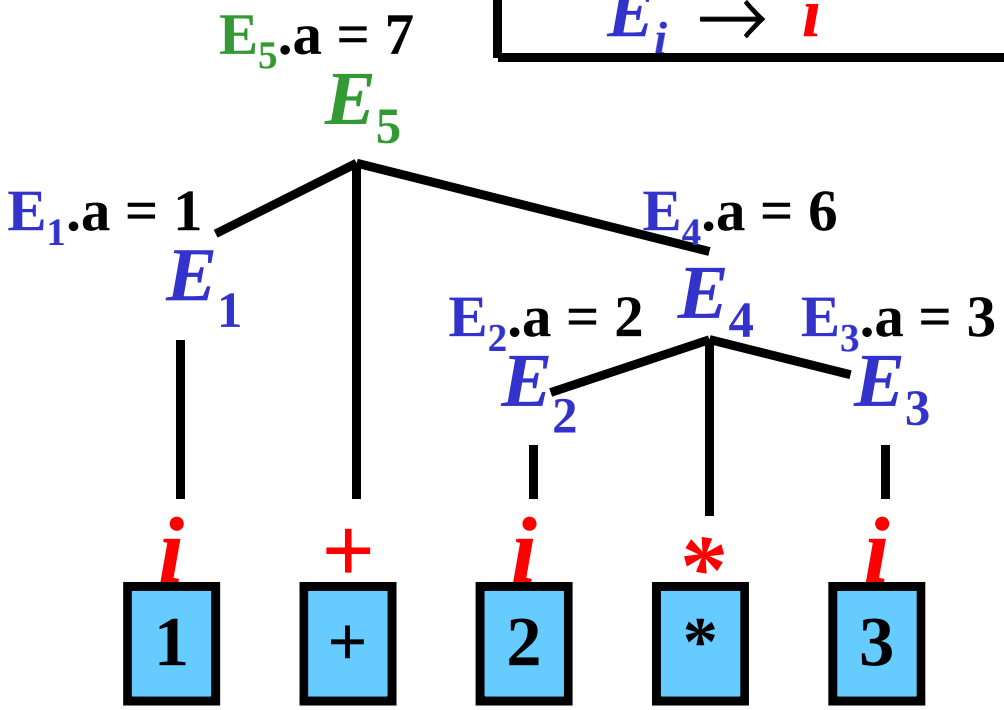
Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	E_2.a:= i.val
$E_3 \rightarrow i$	E_3.a:= i.val
$E_4 \rightarrow E_2 * E_3$	E_4.a:= E_2.a*E_3.a
$E_5 \rightarrow E_1 + E_4$	

Syntax-Directed Translation

Gist: *Semantic actions* are attached to gramatical rules. Most importantly, these actions make intermediate code generation and type checking.

Example:

Rule:	Semantic Action:
$E_i \rightarrow E_j + E_k$	{ E_i.a := E_j.a + E_k.a}
$E_i \rightarrow E_j * E_k$	{ E_i.a := E_j.a * E_k.a}
$E_i \rightarrow (E_j)$	{ E_i.a := E_j.a }
$E_i \rightarrow i$	{ E_i.a := i.val }



Rule:	Action:
$E_1 \rightarrow i$	E_1.a:= i.val
$E_2 \rightarrow i$	E_2.a:= i.val
$E_3 \rightarrow i$	E_3.a:= i.val
$E_4 \rightarrow E_2 * E_3$	E_4.a:= E_2.a*E_3.a
$E_5 \rightarrow E_1 + E_4$	E_5.a:= E_1.a+E_4.a

Intermediate Code: Three–Address Code

- Instruction in **three–address code** (**3AC**) has the form:

(o, ☛a, ☛b, ☛r)

- **o** – operator (+, –, *, …)
- **a** – operand 1 (☛***a*** = address of ***a***)
- **b** – operand 2 (☛***b*** = address of ***b***)
- **r** – result (☛***r*** = address of ***r***)

Examples:

```
(:=   ,  a,   , c )  …  c := a
(+    ,  a,  b, c )  …  c := a + b
(not  ,  a,   , b )  …  b := not(a)
(goto,   ,   , L1)  …  goto L1
(goto,   a,   , L1)  …  if a = true then goto L1
(lab  , L1,   ,   )  …  label L1:
```

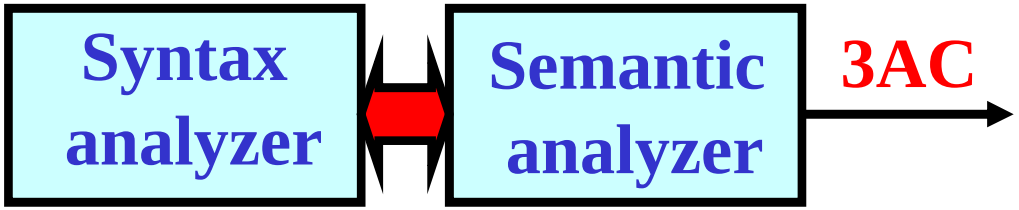
Syntax-Directed Generation of 3AC

Basic approaches:

1) Parser directs the creation of an ***abstract-syntax tree* (AST)** , which is then converted to **3AC**.

2) Parser directs the creation of a ***postfix notation* (PN)** , which is then converted to **3AC**.

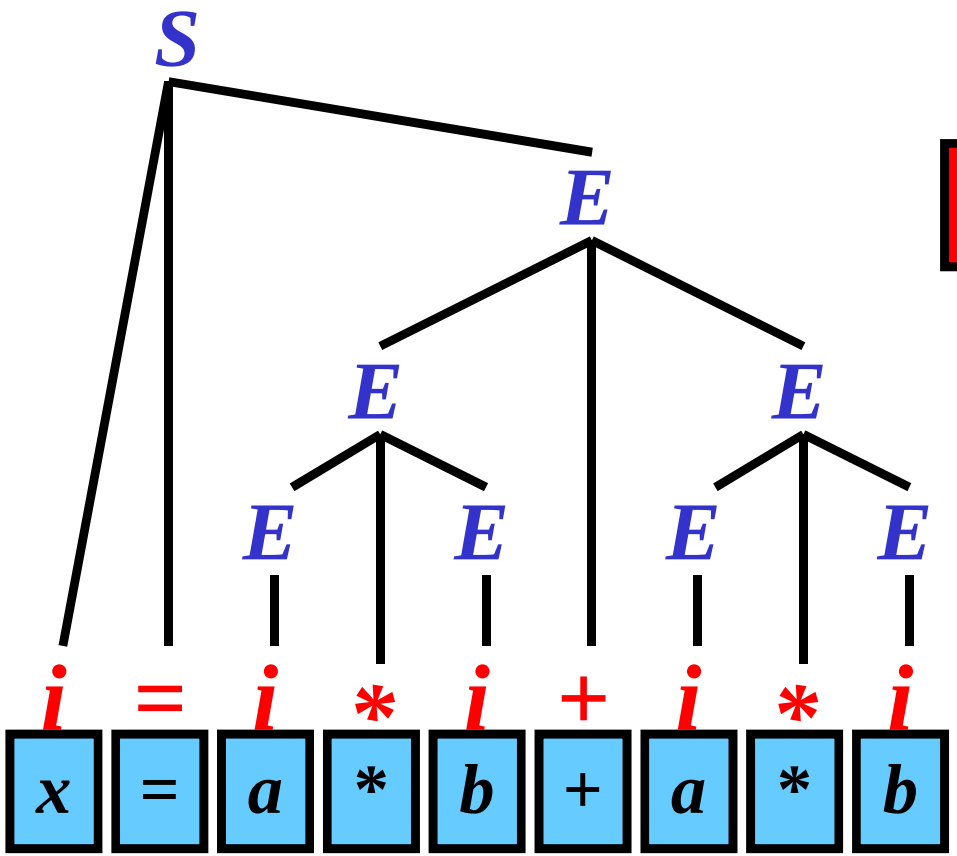
3) A parser directs the creation of **3AC.**



From a Parse Tree (PT) to an AST: Example

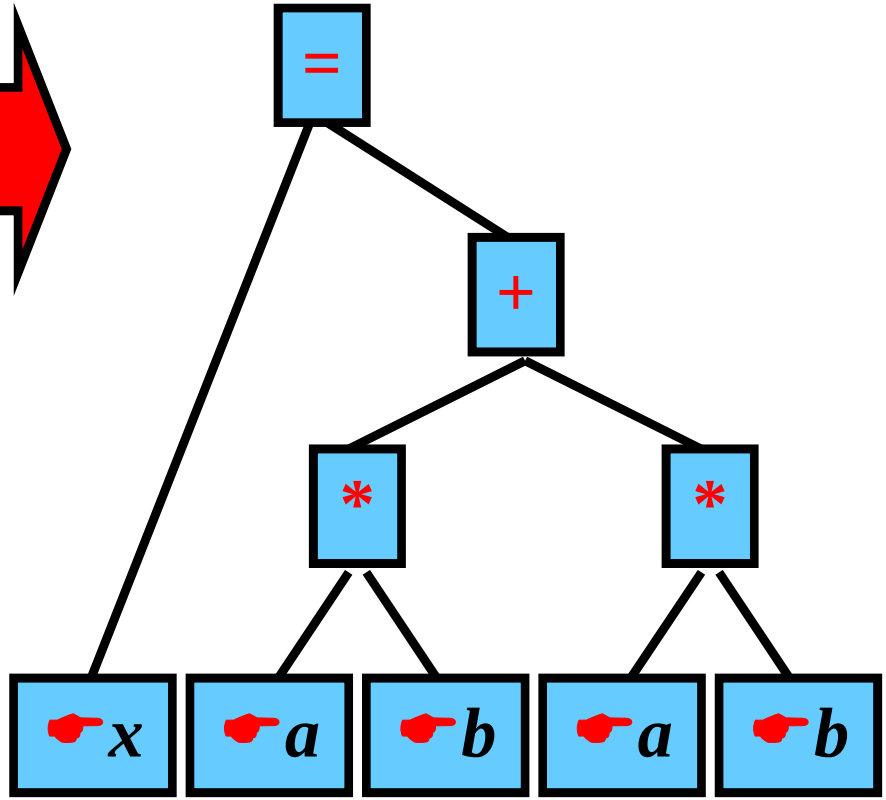
- **PT for**

  ***x = a*b + a*b*:**



- **AST for**

  ***x = a*b + a*b*:**



Generation of AST

Gist: A parser simulates the construction of PT and, simultaneously, calls some semantic actions to create AST.

Example:

Rule:	Semantic Action:
$S \rightarrow i := E_k$	{ $S.a$:= MakeTree('=', $i.a$, $E_k.a$) }
$E_i \rightarrow E_j + E_k$	{ $E_i.a$:= MakeTree('+', $E_j.a$, $E_k.a$) }
$E_i \rightarrow E_j * E_k$	{ $E_i.a$:= MakeTree('*', $E_j.a$, $E_k.a$) }
$E_i \rightarrow (E_j)$	{ $E_i.a$:= $E_j.a$ }
$E_i \rightarrow i$	{ $E_i.a$:= MakeLeaf($i.a$) }

Notes:

• **MakeTree(*o*, *a*, *b*)** creates a new node ***o***, attaches sons ***a*** (left) and ***b***, and returns a pointer to node ***o***

• **MakeLeaf(*i.a*)** creates a new node ***i.a*** (***i.a*** is a symbol-table address) and returns a pointer to this new node

AST Generation: Example 1/2

Pushdown	Input	Rule	Semantic action
$	$i = (i + i) * i$$		
$$i$	$= (i + i) * i$$		
$$i =$	$(i + i) * i$$		
$$i = ($	$i + i) * i$$		
$$i = (i$	$+ i) * i$$	$E_1 \rightarrow i$	$E_1.a$:= MakeLeaf($i.a$)
$$i = (E_1$	$+ i) * i$$		
$$i = (E_1 +$	$i) * i$$		
$$i = (E_1 + i$	$) * i$$	$E_2 \rightarrow i$	$E_2.a$:= MakeLeaf($i.a$)
$$i = (E_1 + E_2$	$) * i$$	$E_3 \rightarrow E_1+E_2$	$E_3.a$:=MakeTree(‘+’, $E_1.a$, $E_2.a$)
$$i = (E_3$	$) * i$$		
$$i = (E_3)$	$* i$$	$E_4 \rightarrow (E_3)$	$E_4.a$:= $E_3.a$
$$i = E_4$	$* i$$		
$$i = E_4 *$	$i$$		
$$i = E_4 * i$	$$	$E_5 \rightarrow i$	$E_5.a$:= MakeLeaf($i.a$)
$$i = E_4 * E_5$	$$	$E_6 \rightarrow E_4*E_5$	$E_6.a$:=MakeTree(‘*’, $E_4.a$, $E_5.a$)
$$i = E_6$	$$	$S \rightarrow i = E_6$	$S.a$:= MakeTree(‘=’, $i.a$, $E_6.a$)
$$S$	$$		

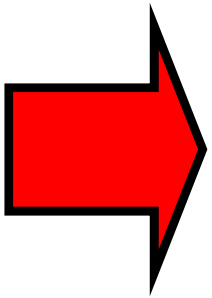
Bottom-Up parsing **Semantic actions**

AST Generation: Example 2/2

Rule:	Semantic Action:

Simulated Parse tree:

Abstract syntax tree:

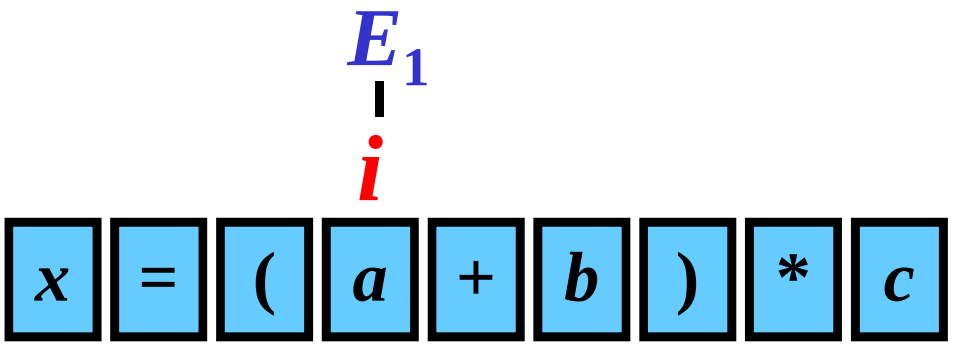


x	=	(	*a*	+	*b*	)	*	*c*

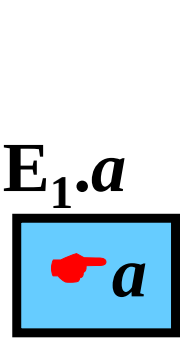
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$	$E_1.a$:= MakeLeaf($i.a$)

Simulated Parse tree:



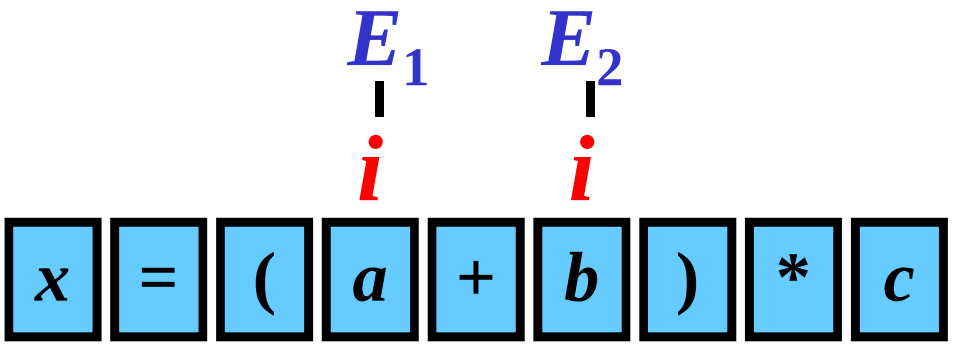
Abstract syntax tree:



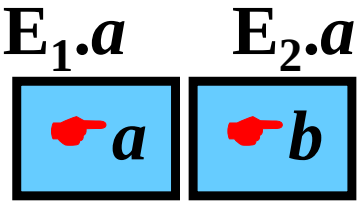
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$ $E_2 \rightarrow i$	$E_1.a$:= MakeLeaf($i.a$) $E_2.a$:= MakeLeaf($i.a$)

Simulated Parse tree:



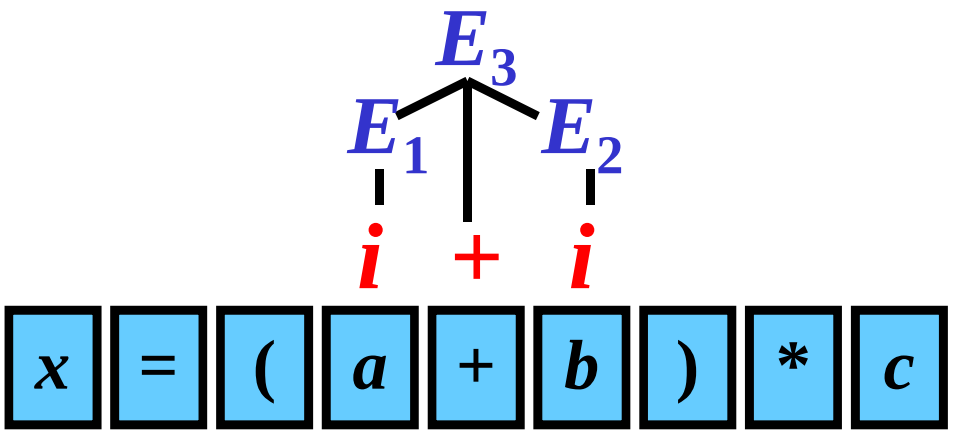
Abstract syntax tree:



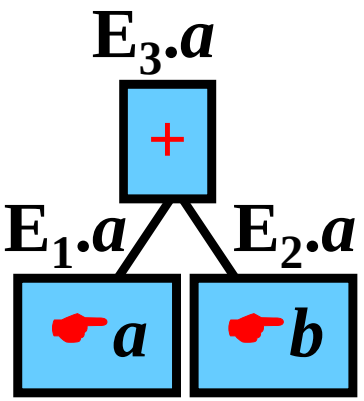
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$ $E_2 \rightarrow i$ $E_3 \rightarrow E_1 + E_2$	$E_1.a$:= MakeLeaf($i.a$) $E_2.a$:= MakeLeaf($i.a$) $E_3.a$:= MakeTree(‘+’, $E_1.a, E_2.a$)

Simulated Parse tree:



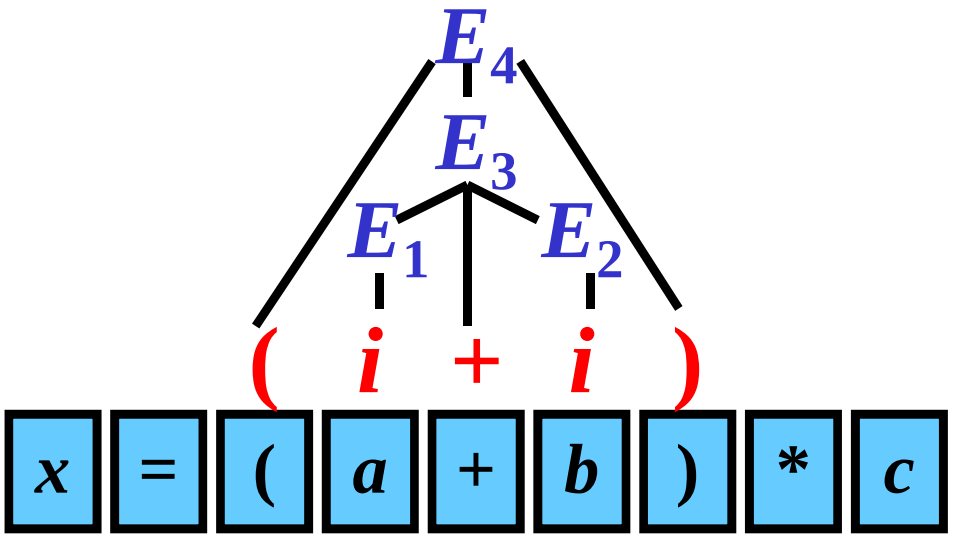
Abstract syntax tree:



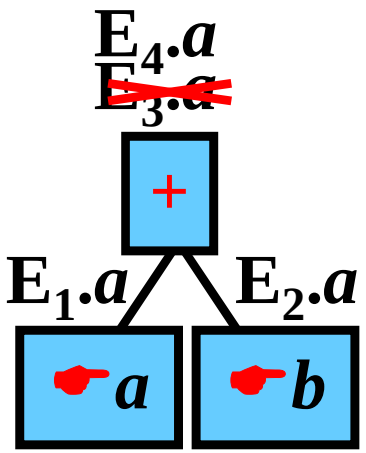
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$ $E_2 \rightarrow i$ $E_3 \rightarrow E_1 + E_2$ $E_4 \rightarrow (E_3)$	$E_1.a$:= MakeLeaf($i.a$) $E_2.a$:= MakeLeaf($i.a$) $E_3.a$:= MakeTree(‘+’, $E_1.a$, $E_2.a$) $E_4.a$:= $E_3.a$

Simulated Parse tree:



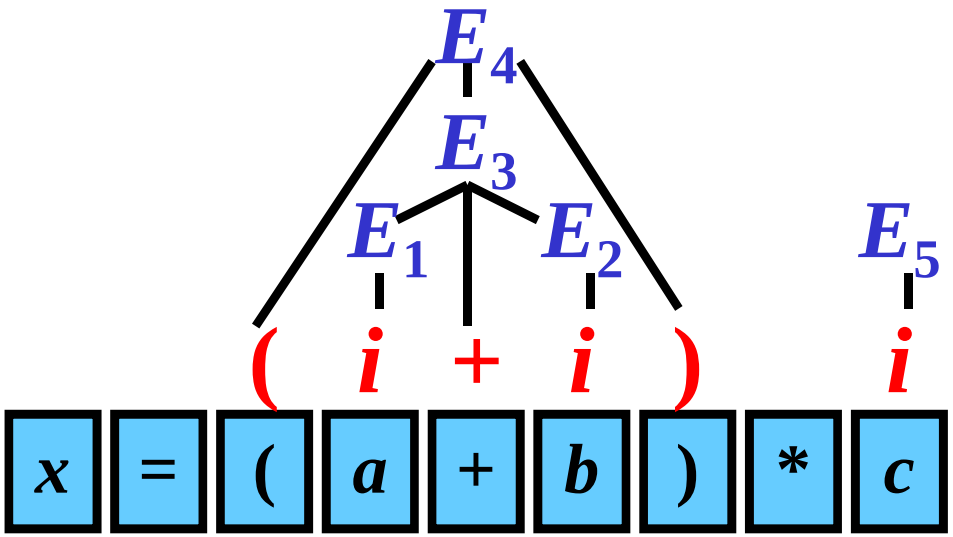
Abstract syntax tree:



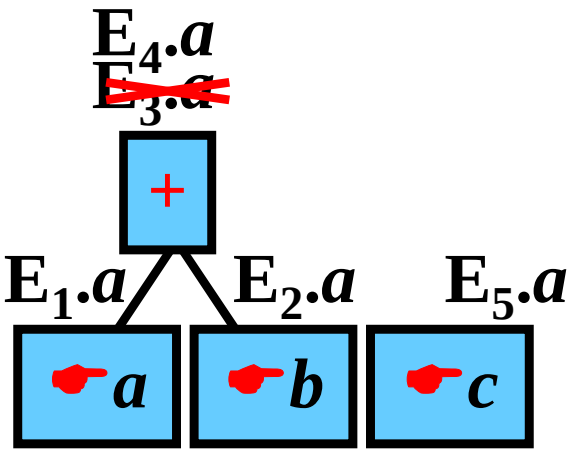
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$	$E_1.a$:= MakeLeaf($i.a$)
$E_2 \rightarrow i$	$E_2.a$:= MakeLeaf($i.a$)
$E_3 \rightarrow E_1 + E_2$	$E_3.a$:= MakeTree(‘+’, $E_1.a$, $E_2.a$)
$E_4 \rightarrow (E_3)$	$E_4.a$:= $E_3.a$
$E_5 \rightarrow i$	$E_5.a$:= MakeLeaf($i.a$)

Simulated Parse tree:



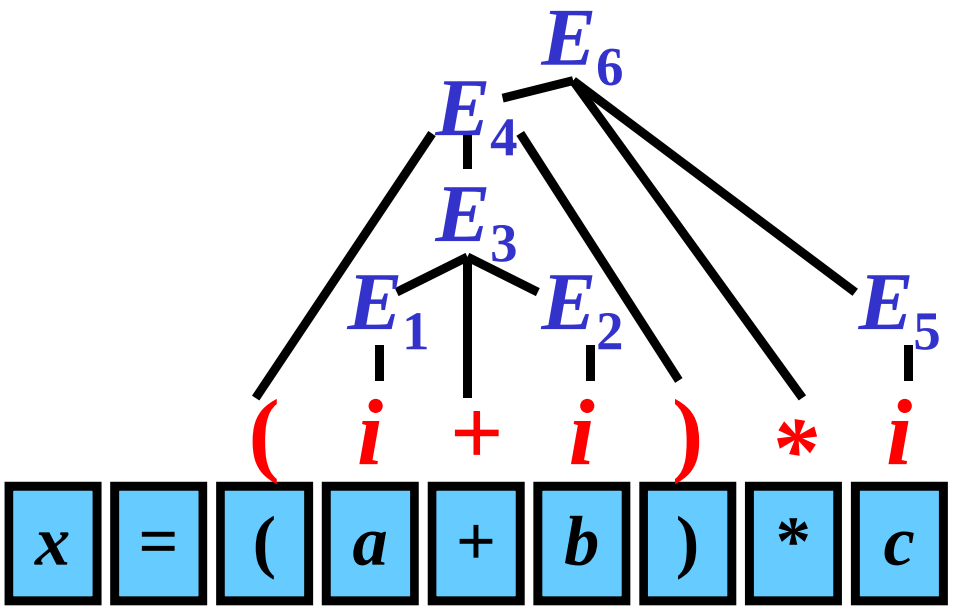
Abstract syntax tree:



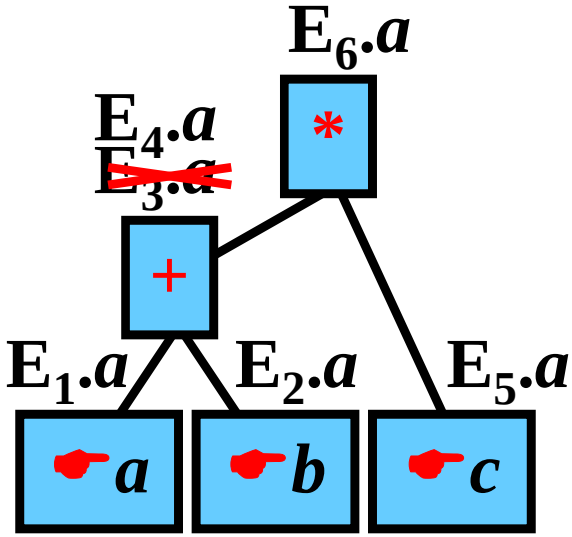
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$	$E_1.a$:= MakeLeaf($i.a$)
$E_2 \rightarrow i$	$E_2.a$:= MakeLeaf($i.a$)
$E_3 \rightarrow E_1 + E_2$	$E_3.a$:= MakeTree(‘+’, $E_1.a$, $E_2.a$)
$E_4 \rightarrow (E_3)$	$E_4.a$:= $E_3.a$
$E_5 \rightarrow i$	$E_5.a$:= MakeLeaf($i.a$)
$E_6 \rightarrow E_4 * E_5$	$E_6.a$:= MakeTree(‘*’, $E_4.a$, $E_5.a$)

Simulated Parse tree:



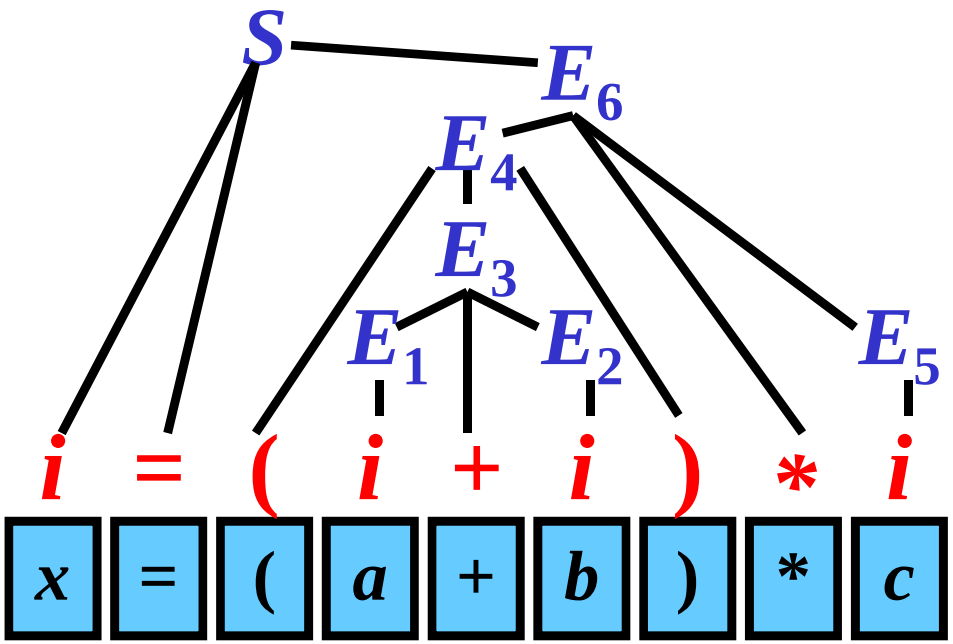
Abstract syntax tree:



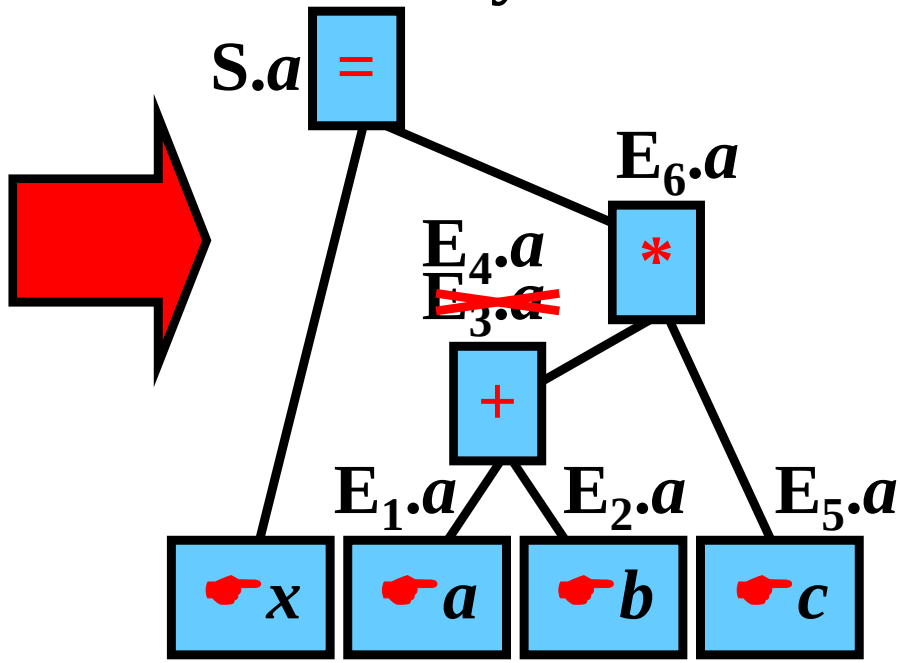
AST Generation: Example 2/2

Rule:	Semantic Action:
$E_1 \rightarrow i$	$E_1.a$:= MakeLeaf($i.a$)
$E_2 \rightarrow i$	$E_2.a$:= MakeLeaf($i.a$)
$E_3 \rightarrow E_1 + E_2$	$E_3.a$:= MakeTree('+', $E_1.a$, $E_2.a$)
$E_4 \rightarrow (E_3)$	$E_4.a$:= $E_3.a$
$E_5 \rightarrow i$	$E_5.a$:= MakeLeaf($i.a$)
$E_6 \rightarrow E_4 * E_5$	$E_6.a$:= MakeTree('*', $E_4.a$, $E_5.a$)
$S \rightarrow i = E_6$	$S.a$:= MakeTree('=', $i.a$, $E_6.a$)

Simulated Parse tree:

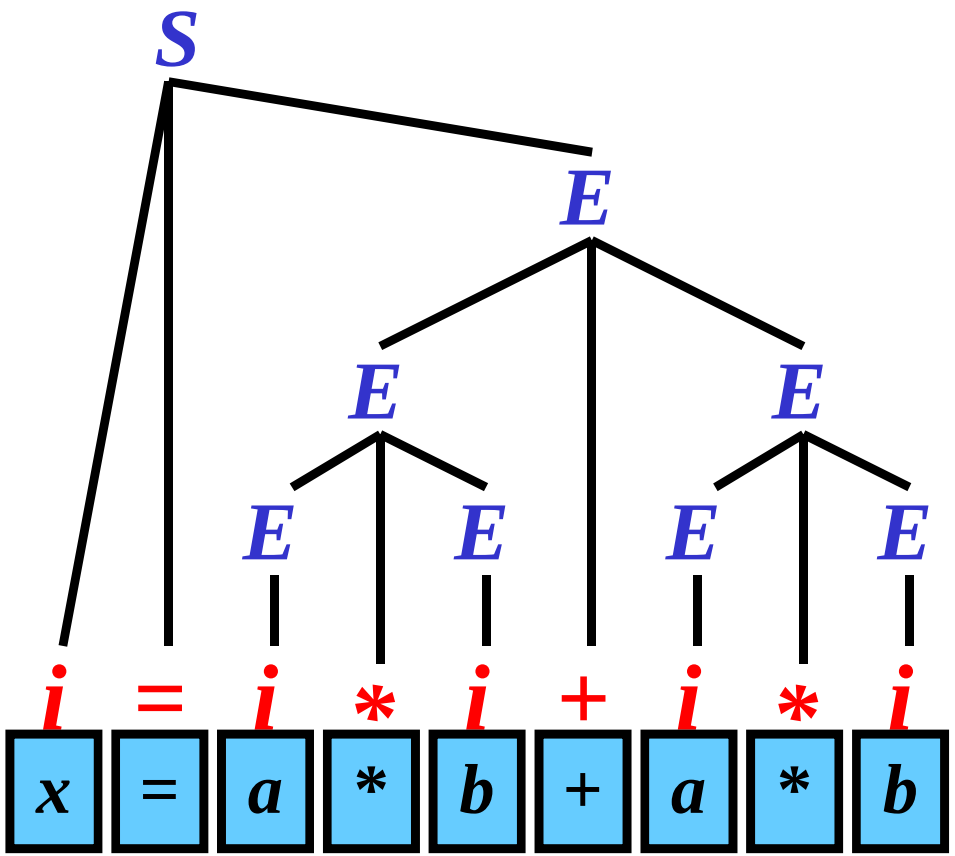


Abstract syntax tree:

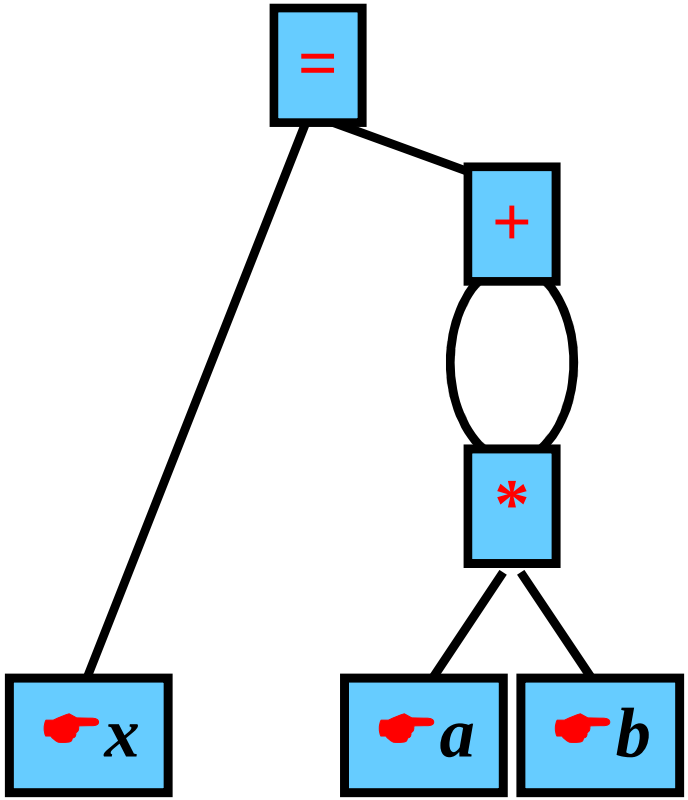


Direct Acyclic Graph(DAG): Example

- **Parse tree for**
  ***x = a*b + a*b*:**



- **DAG for**
  ***x = a*b + a*b*:**



Note: DAG has no redundant nodes.

Postfix Notation

Gist: Every operator occurs behind its operands.

Example:

Infix notation	Postfix notation
$a + b$	$a\ b\ +$
$a = b$	$a\ b\ =$
if C **then** S_1 **else** S_2	$C\ S_1\ S_2$ **if-then-else**

Note: Postfix notation is achievable by the postorder traversal of AST.

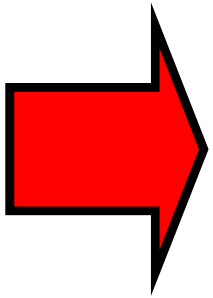
Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

Example:

Rule:	Semantic Action:
1: $E \rightarrow E+E$	{*generate*(‘+’)}
2: $E \rightarrow E*E$	{*generate*(‘*’)}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{*generate*(*i.a*) }

Input: *a* + *b* * *c*



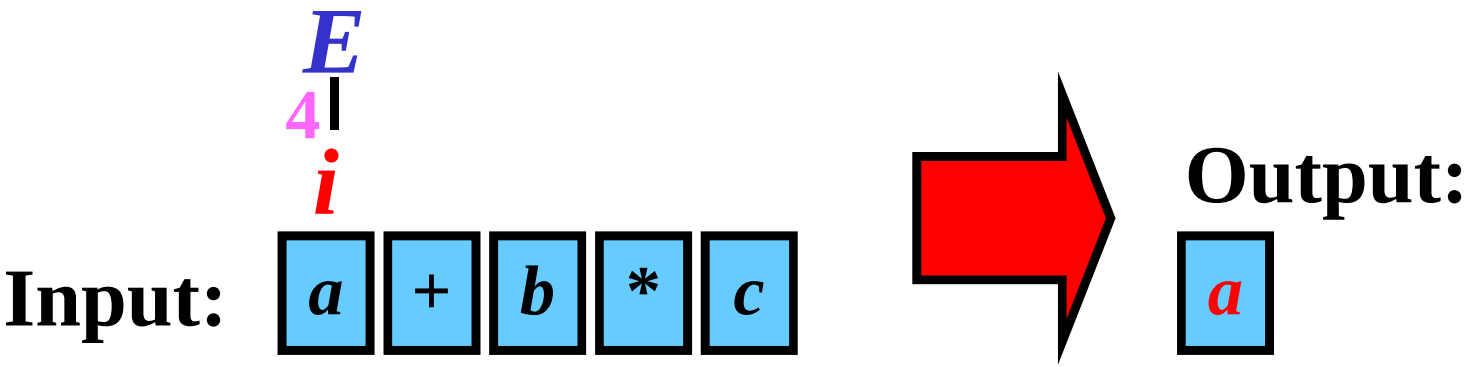
Output:

Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

Example:

Rule:	Semantic Action:
1: $E \rightarrow E+E$	{*generate*(‘+’)}
2: $E \rightarrow E*E$	{*generate*(‘*’)}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{*generate*(*i.a*) }



Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

Example:

Rule:	Semantic Action:
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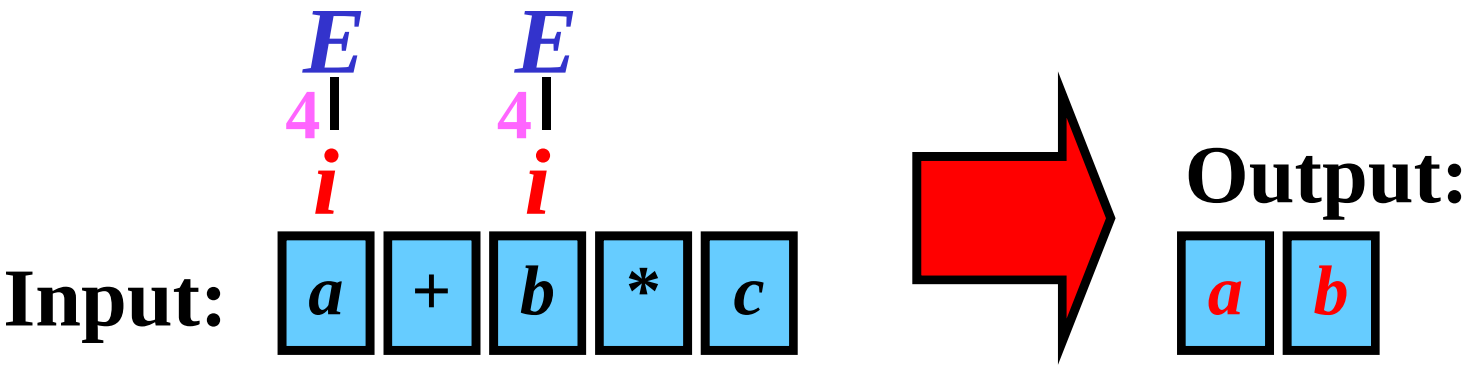
2: $E \rightarrow E*E$	{*generate*(‘*’)}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{*generate*(*i.a*) }

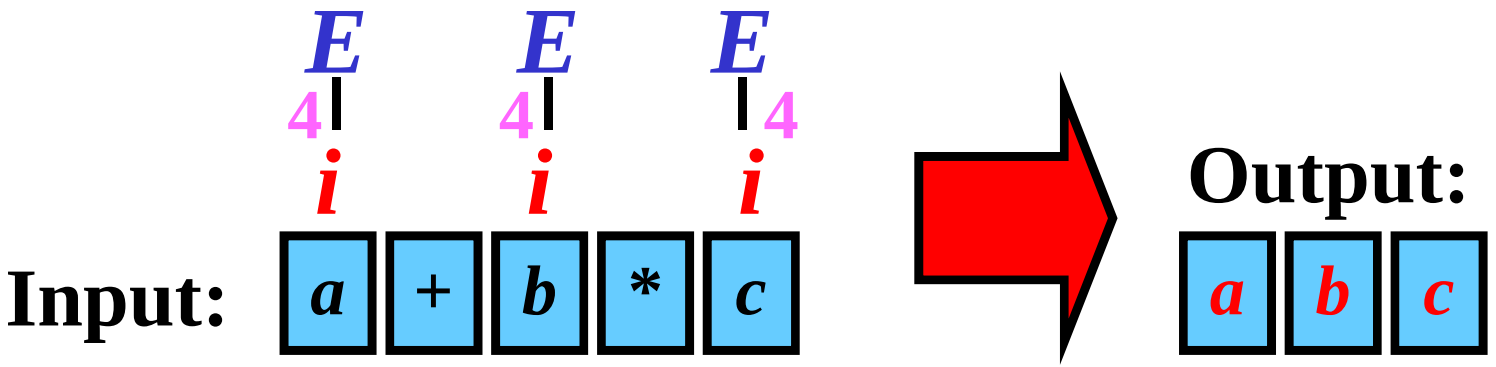


Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

Example:

Rule:	Semantic Action:
1: $E \rightarrow E+E$	{*generate*('+')}
2: $E \rightarrow E*E$	{*generate*('*')}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{*generate*(*i.a*) }

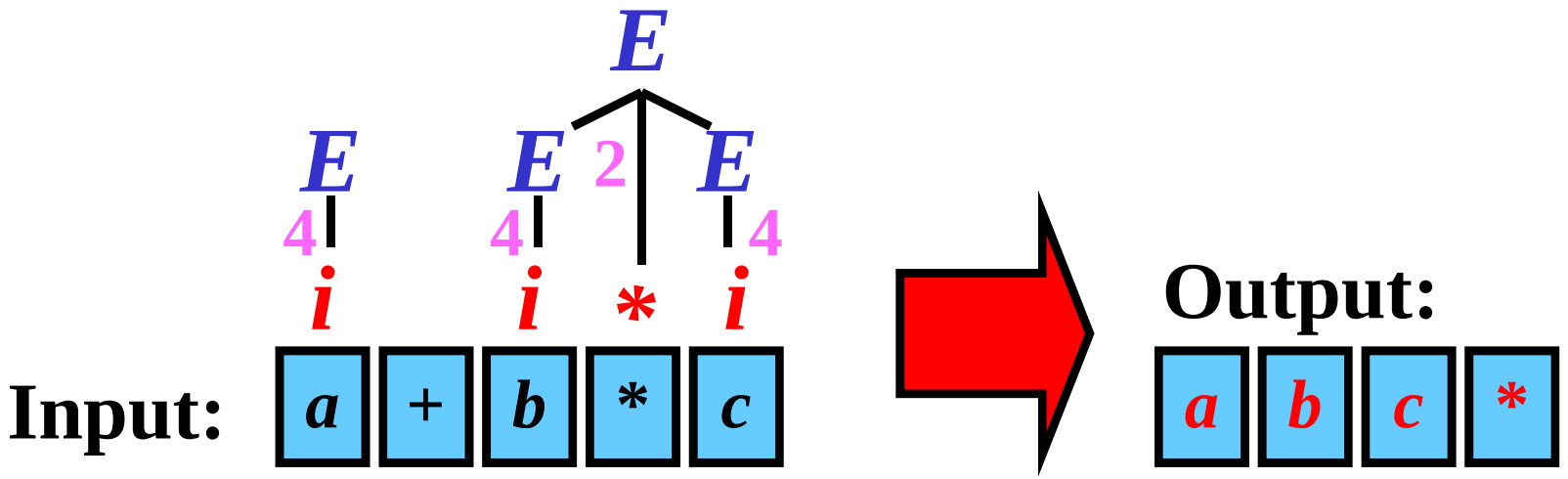


Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

Example:

Rule:	Semantic Action:
1: $E \rightarrow E+E$	{*generate*(‘+’)}
2: $E \rightarrow E*E$	{*generate*(‘*’)}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{*generate*(*i.a*) }

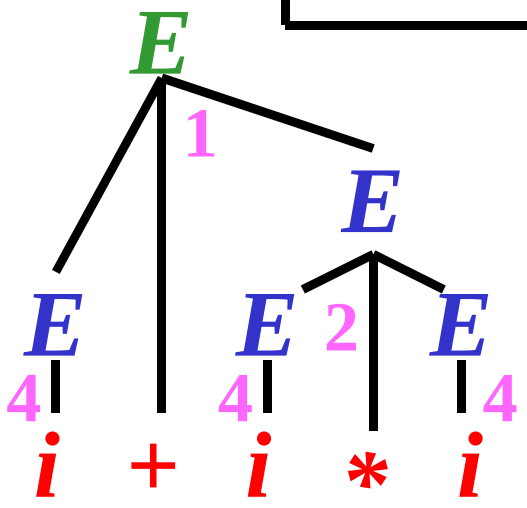


Infix to Postfix Directed by a BU Parser

Gist: Semantic actions produce the postfix version of the tokenized source program.

Example:

Rule:	Semantic Action:
1: $E \rightarrow E+E$	{*generate*(‘+’)}
2: $E \rightarrow E*E$	{*generate*(‘*’)}
3: $E \rightarrow (E)$	{ - }
4: $E \rightarrow i$	{*generate*(*i.a*) }



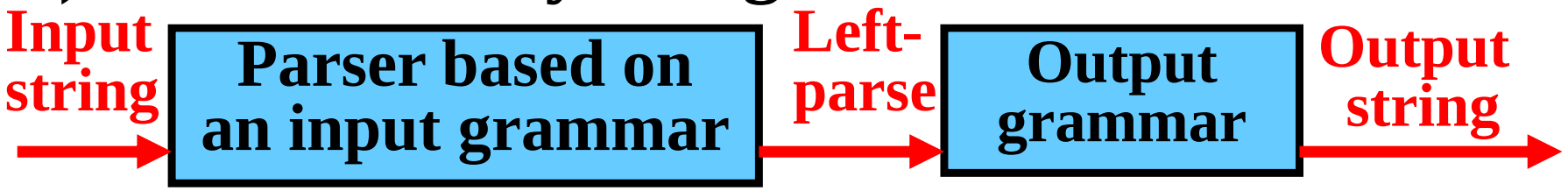
Input: a + b * c

Output: a b c * +

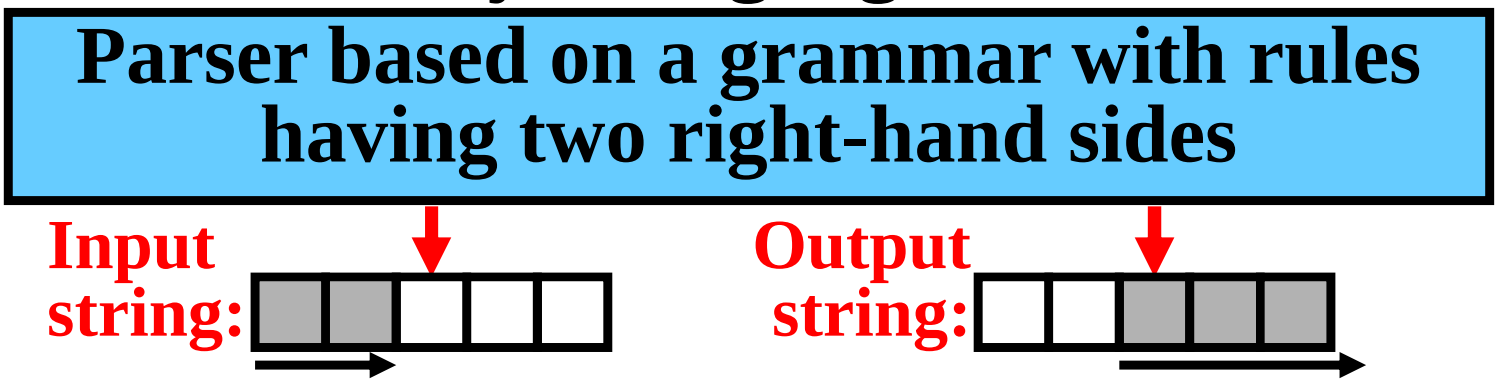
Translation Grammars

Gist: Translation grammars translate input strings to output strings

1) Translation by two grammars:



2) Translation by a single grammar



Note: During the parse of an input string, a simultaneous generation f an output string occurs

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$

E E

Left parse:

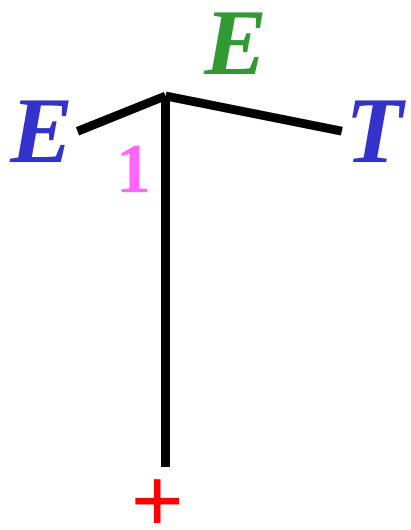
Input: *a* + *b* * *c*

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
1

E

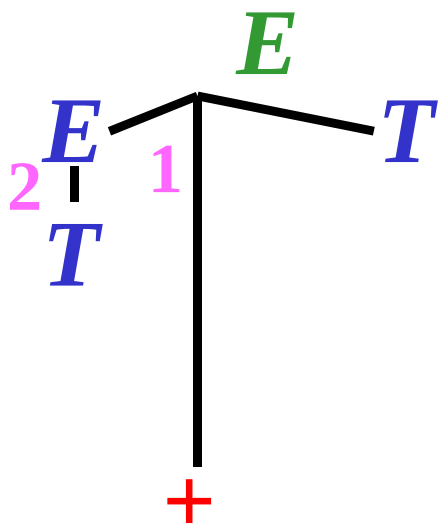
Input: a + b * c

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12

E

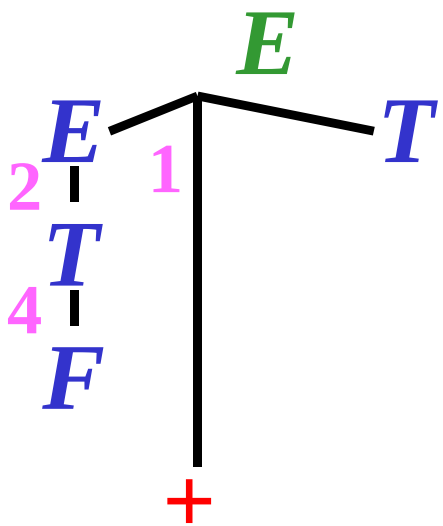
Input: a + b * c

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
124

E

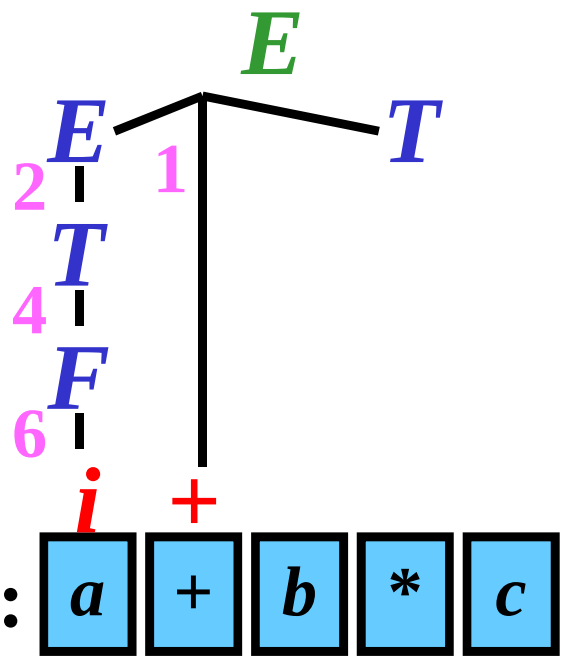
Input: a + b * c

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
1246

E

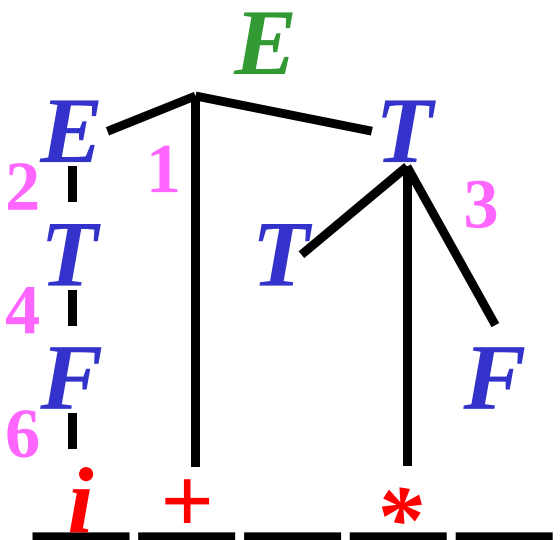
Input: a + b * c

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12463

E

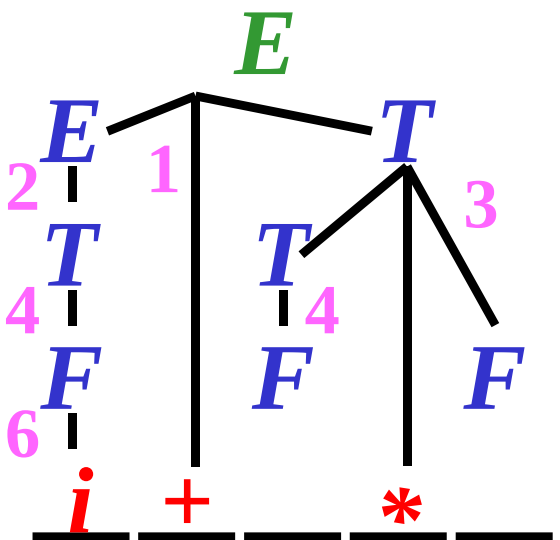
Input: a + b * c

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
124634

Input: *a* + *b* * *c*

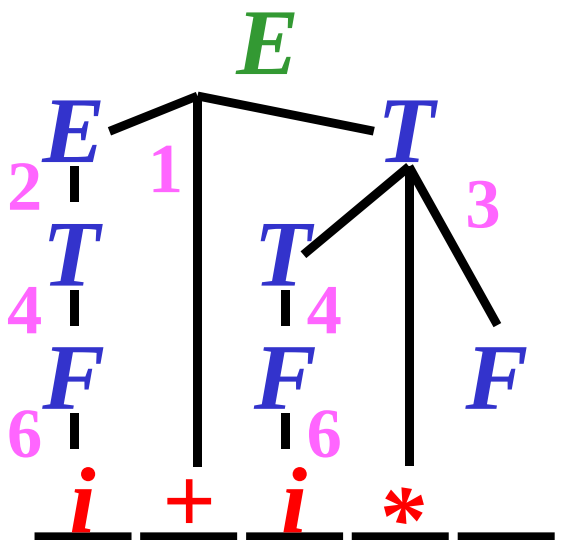
Output:

E

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
1246346

E

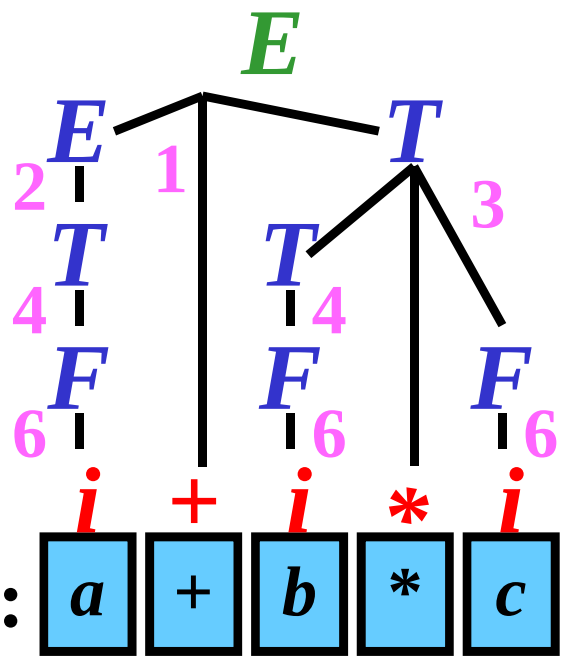
Input: a + b * c

Output:

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12463466

Input: *a* + *b* * *c*

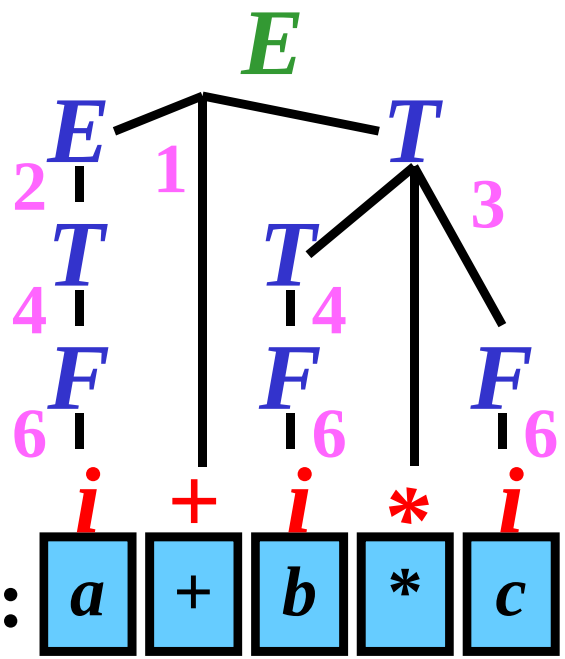
Output:

E

Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12463466

Input: *a* + *b* * *c*

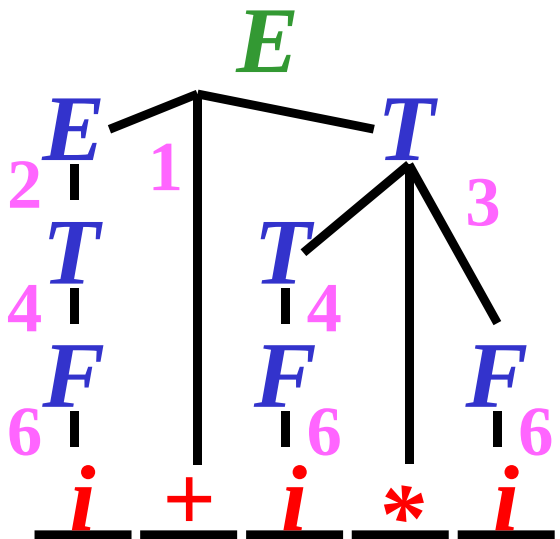
Output:

E

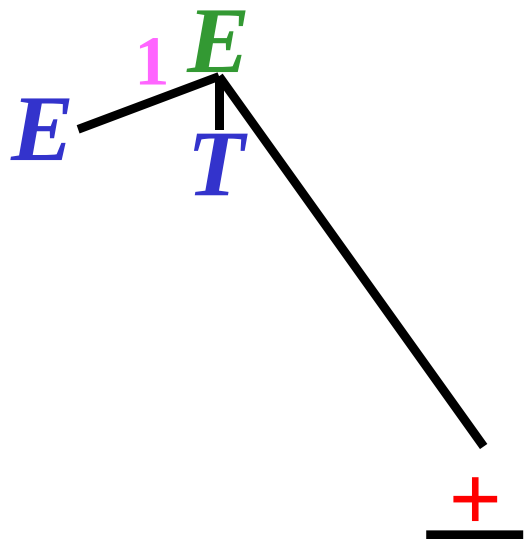
Two-Grammar Translation

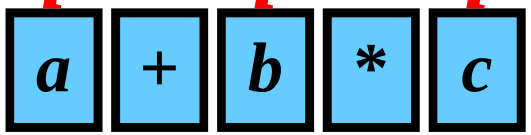
Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12463466



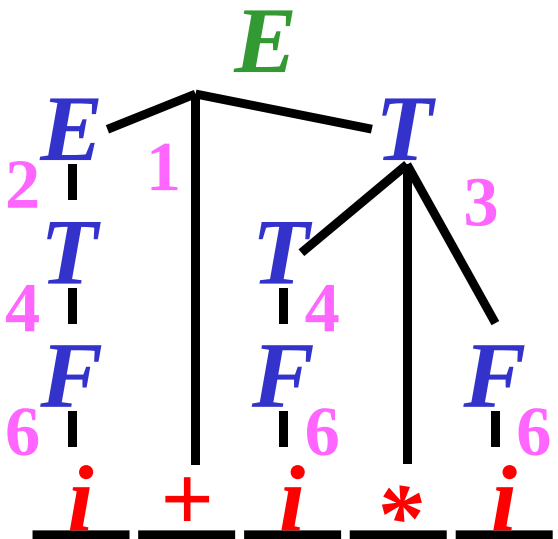
Input: 

Output: 

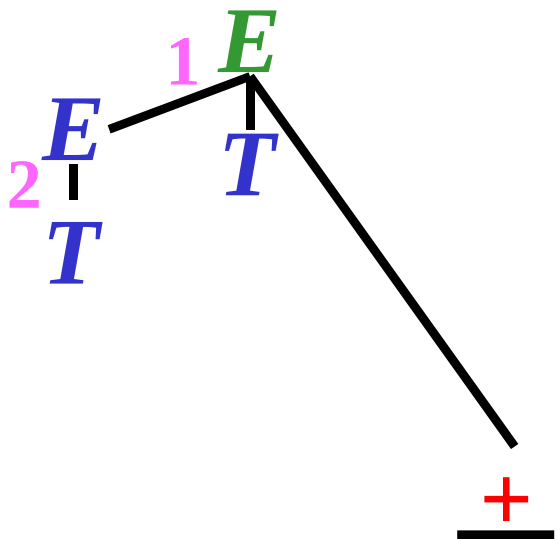
Two-Grammar Translation

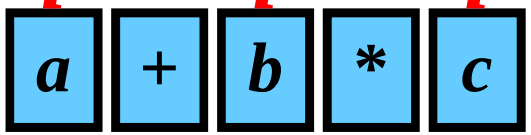
Infix to postfix translation:

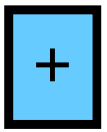
Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12463466



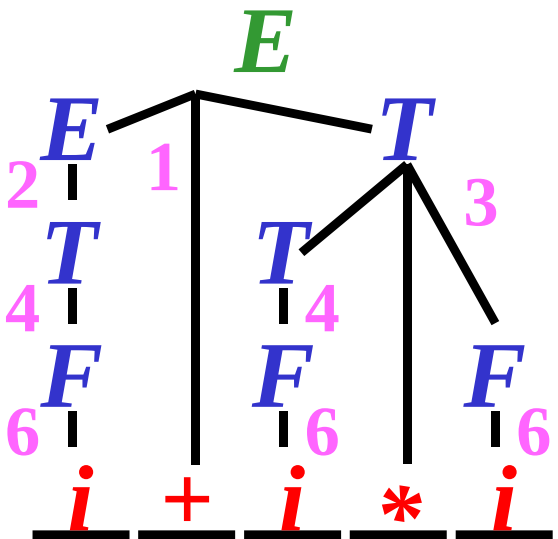
Input: 

Output: 

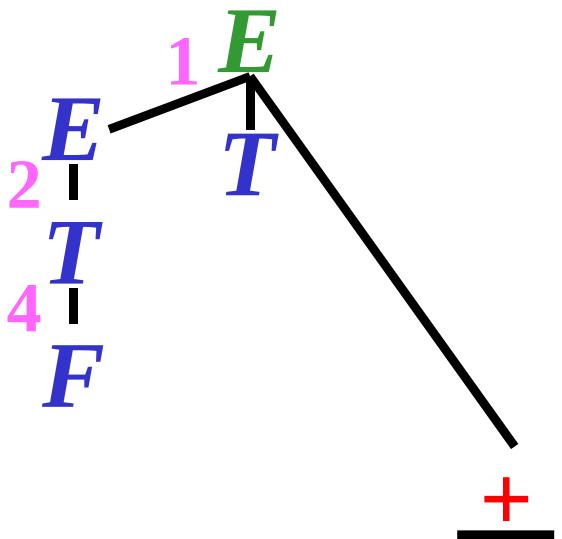
Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Left parse:
12463466



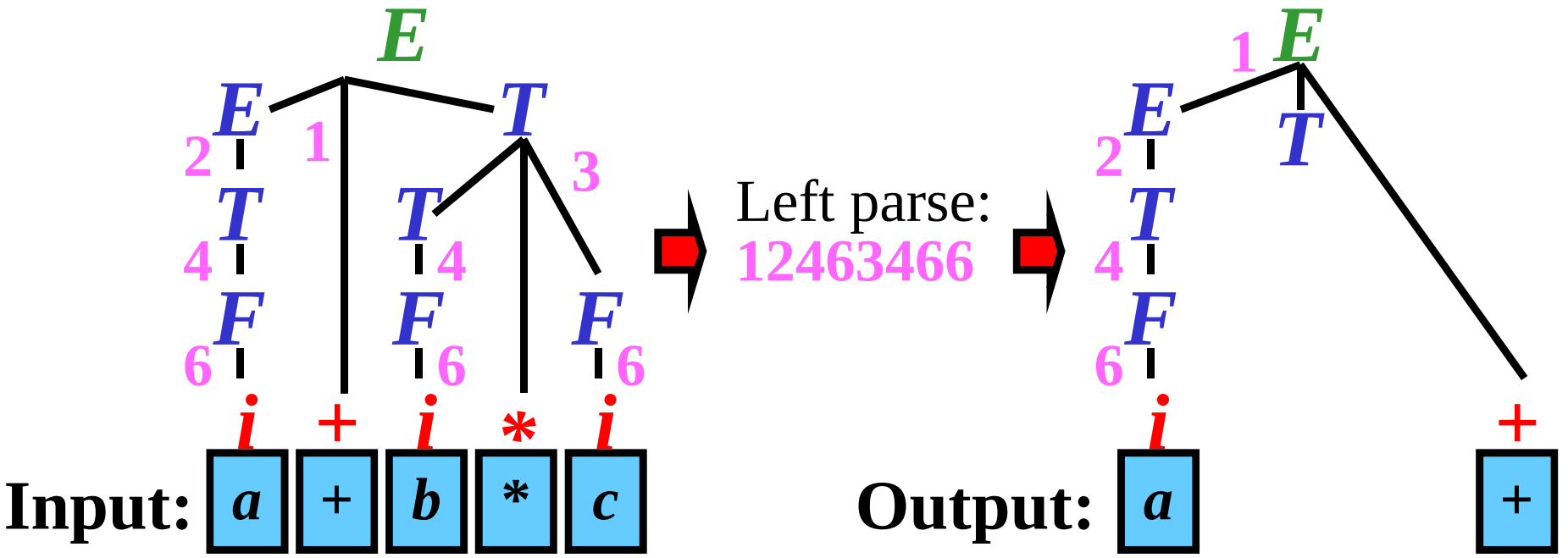
Input: *a* + *b* * *c*

Output: +

Two-Grammar Translation

Infix to postfix translation:

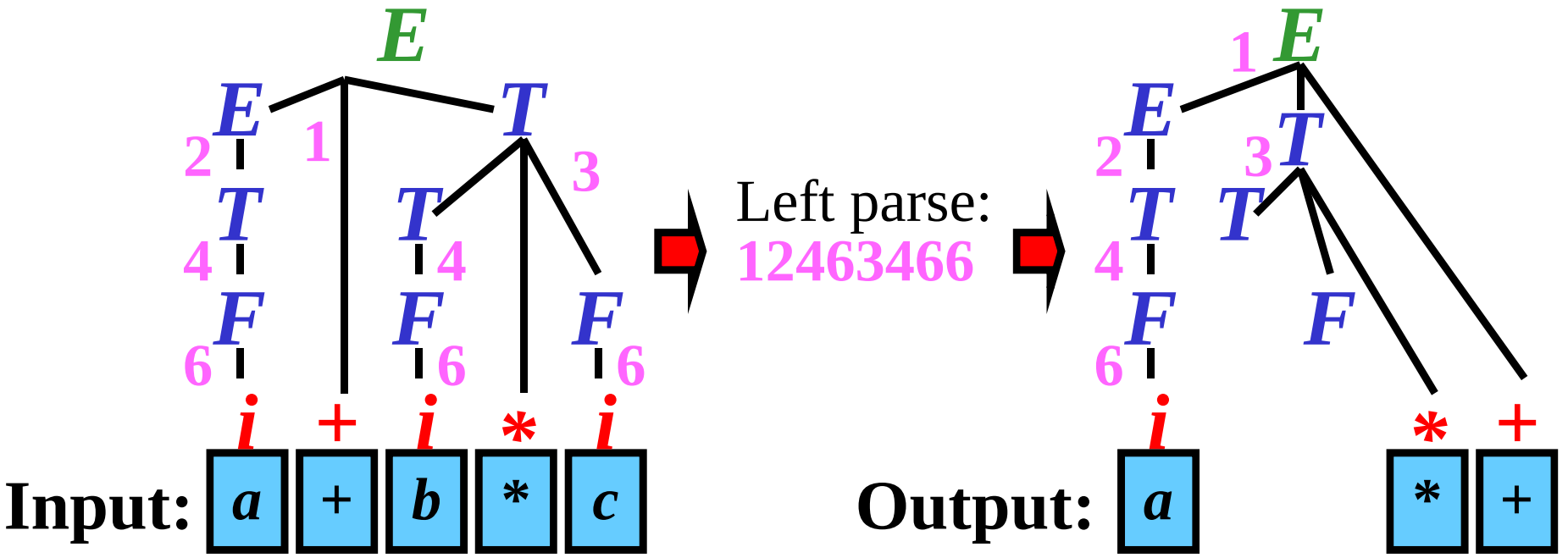
Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Two-Grammar Translation

Infix to postfix translation:

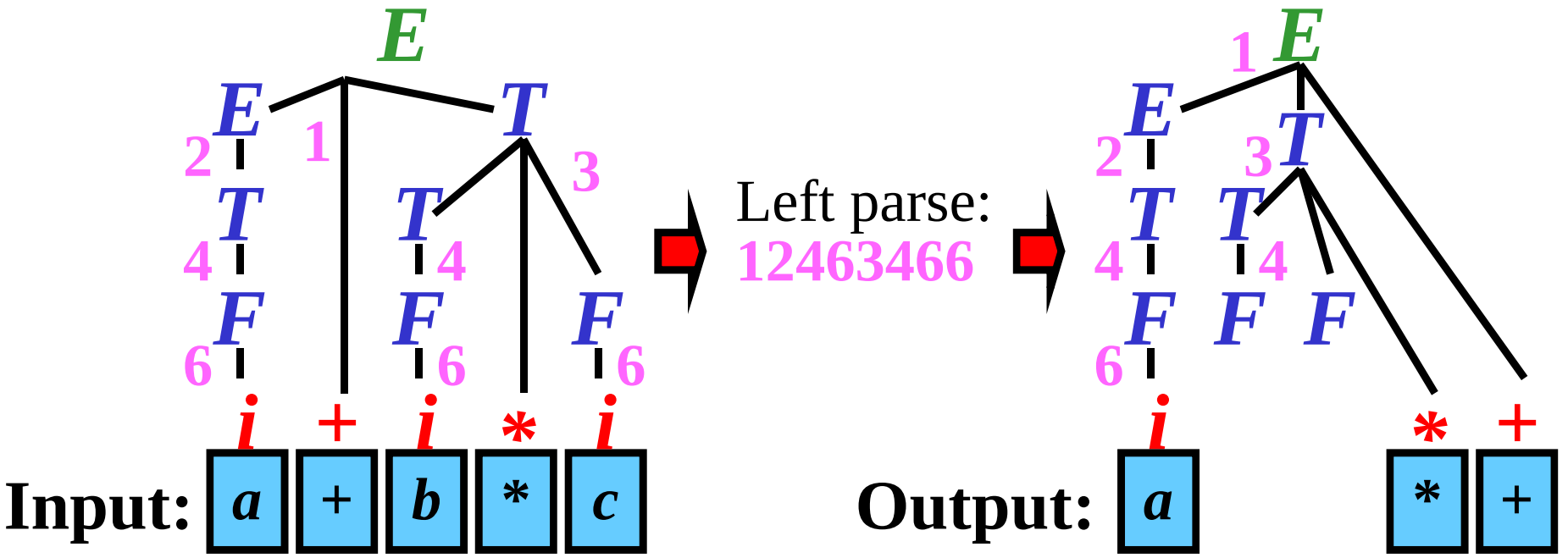
Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Two-Grammar Translation

Infix to postfix translation:

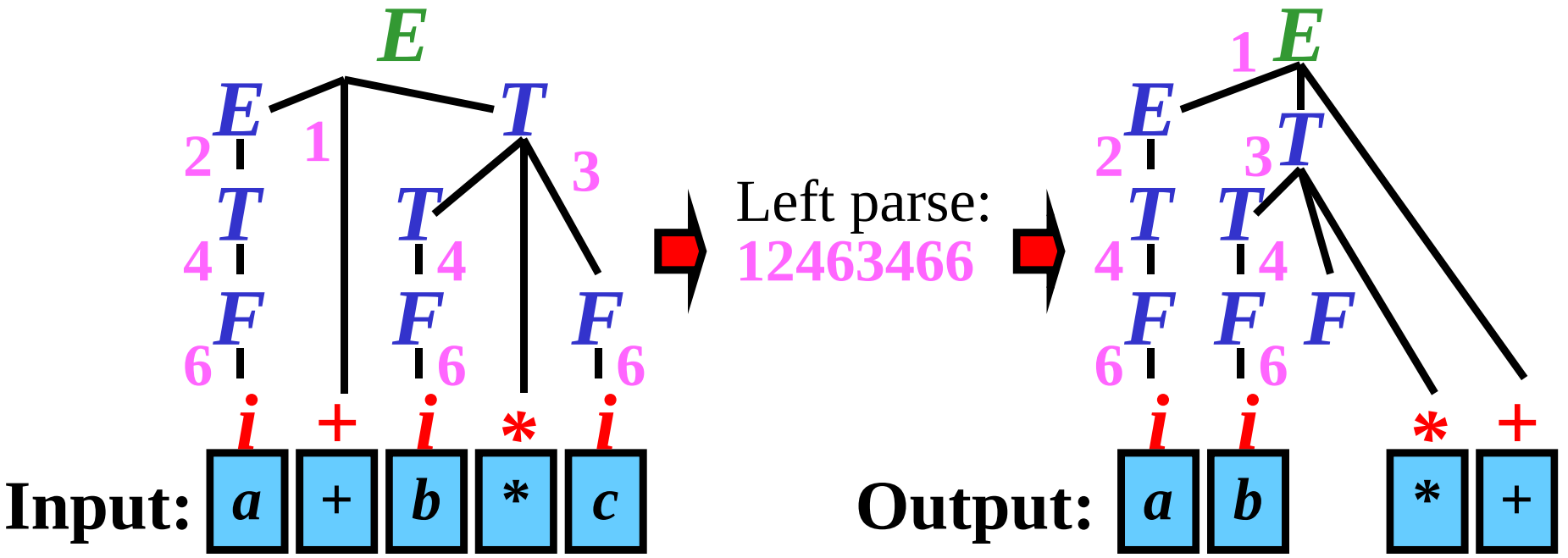
Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Two-Grammar Translation

Infix to postfix translation:

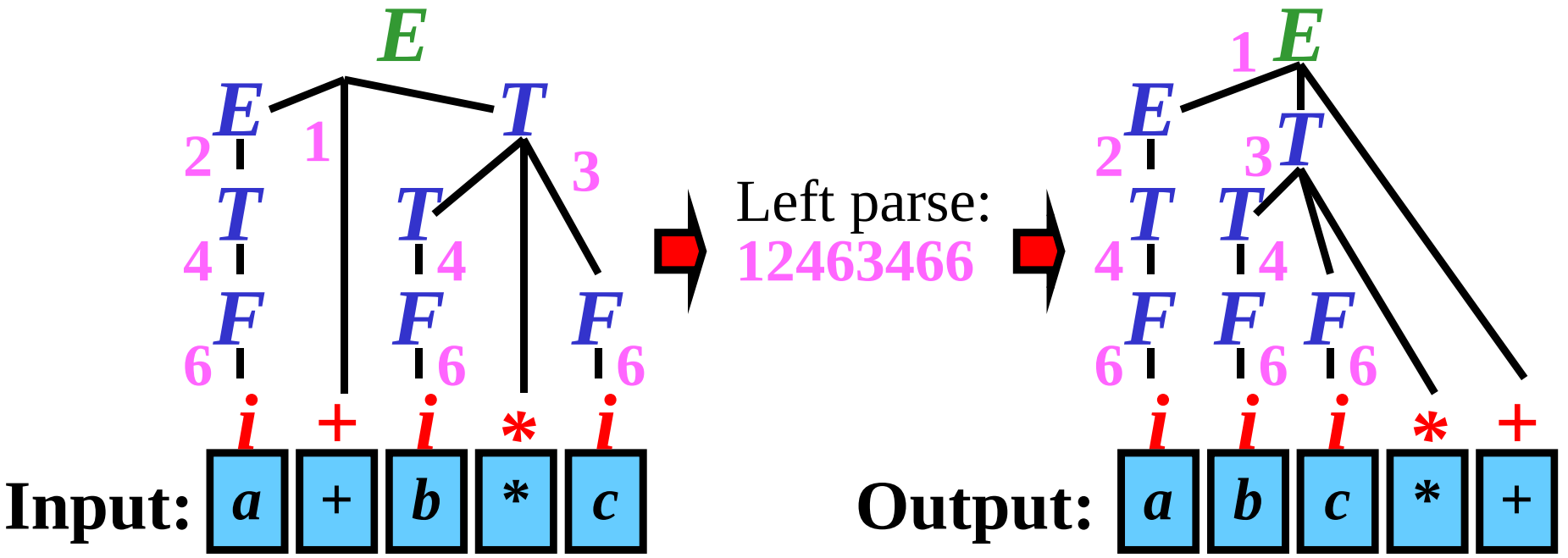
Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$



Two-Grammar Translation

Infix to postfix translation:

Rules of G_1	Rules of G_2
1: $E \rightarrow E+T$	1: $E \rightarrow ET+$
2: $E \rightarrow T$	2: $E \rightarrow T$
3: $T \rightarrow T*F$	3: $T \rightarrow TF*$
4: $T \rightarrow F$	4: $T \rightarrow F$
5: $F \rightarrow (E)$	5: $F \rightarrow E$
6: $F \rightarrow i$	6: $F \rightarrow i$

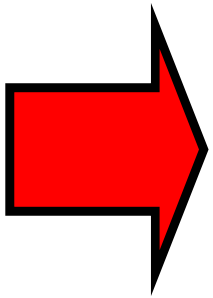


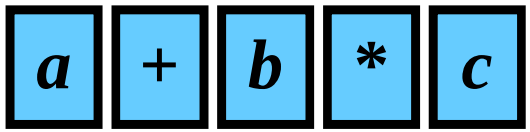
One-Grammar Translation

Infix to postfix translation:

Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i

E E



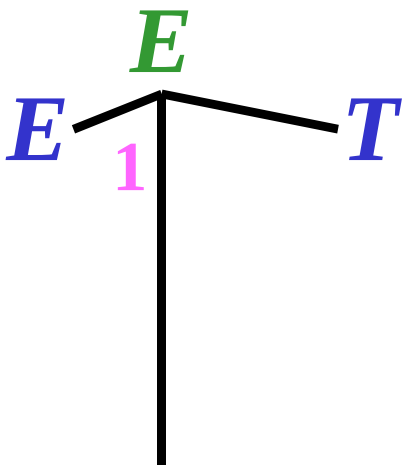
Input: 

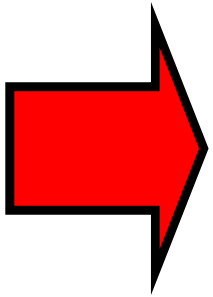
Output:

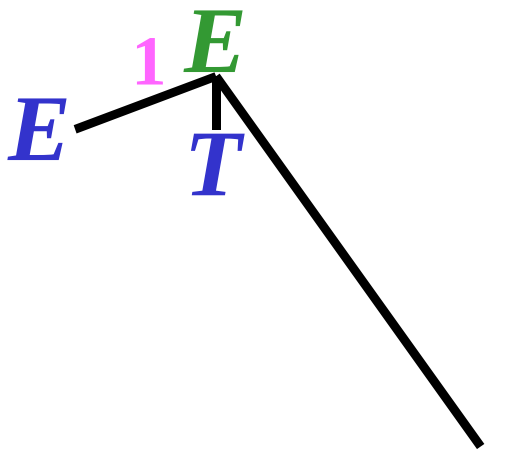
One-Grammar Translation

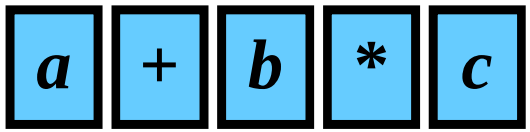
Infix to postfix translation:

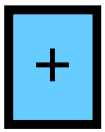
Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i







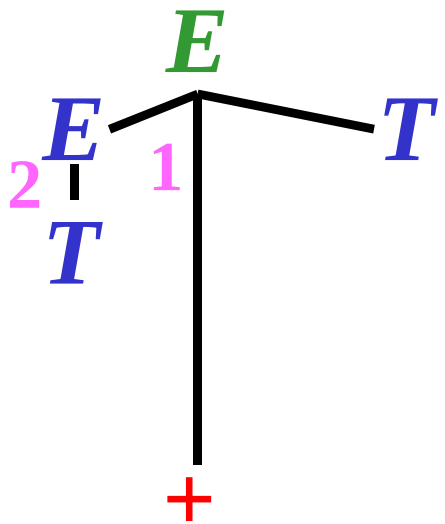
Input: 

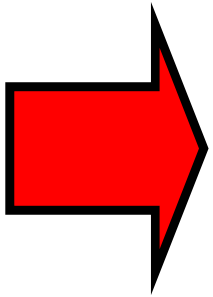
Output: 

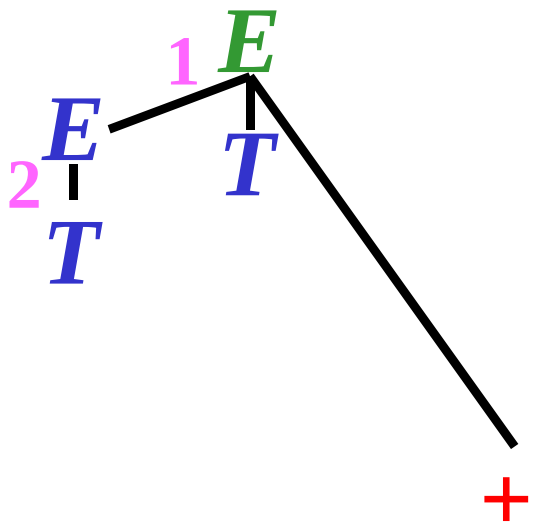
One-Grammar Translation

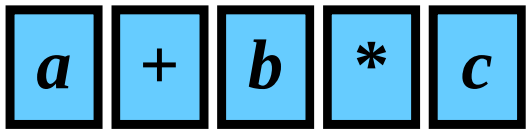
Infix to postfix translation:

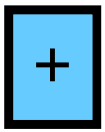
Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i







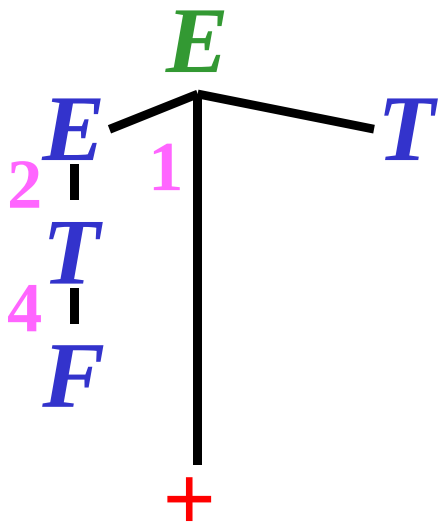
Input: 

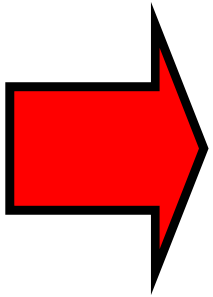
Output: 

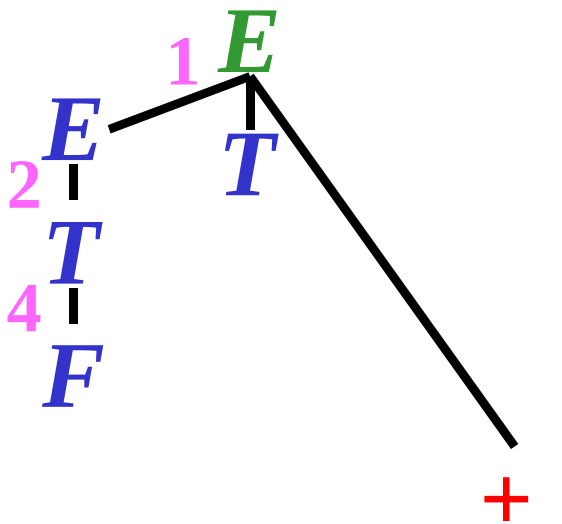
One-Grammar Translation

Infix to postfix translation:

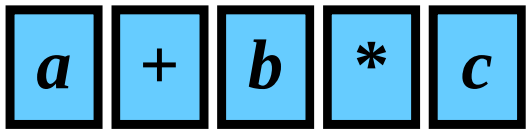
Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



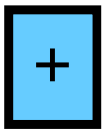




Input:



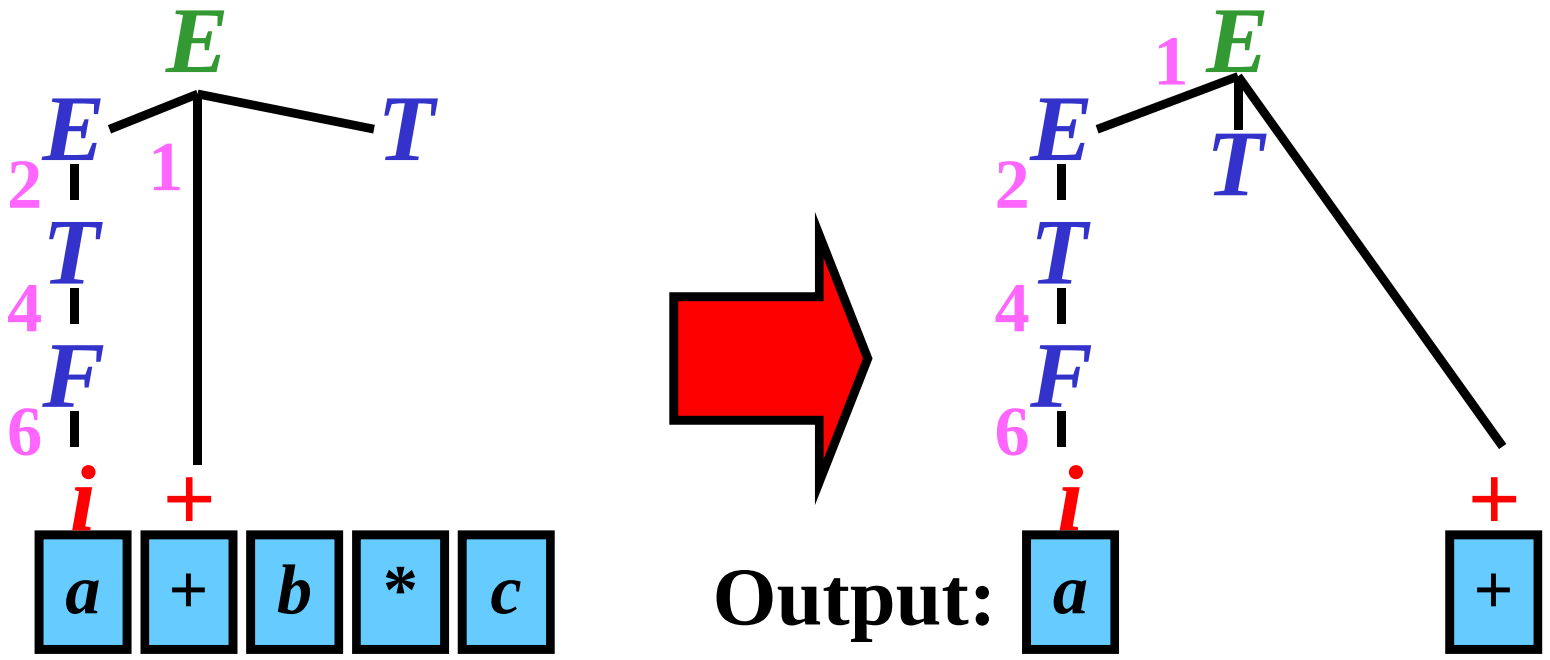
Output:



One-Grammar Translation

Infix to postfix translation:

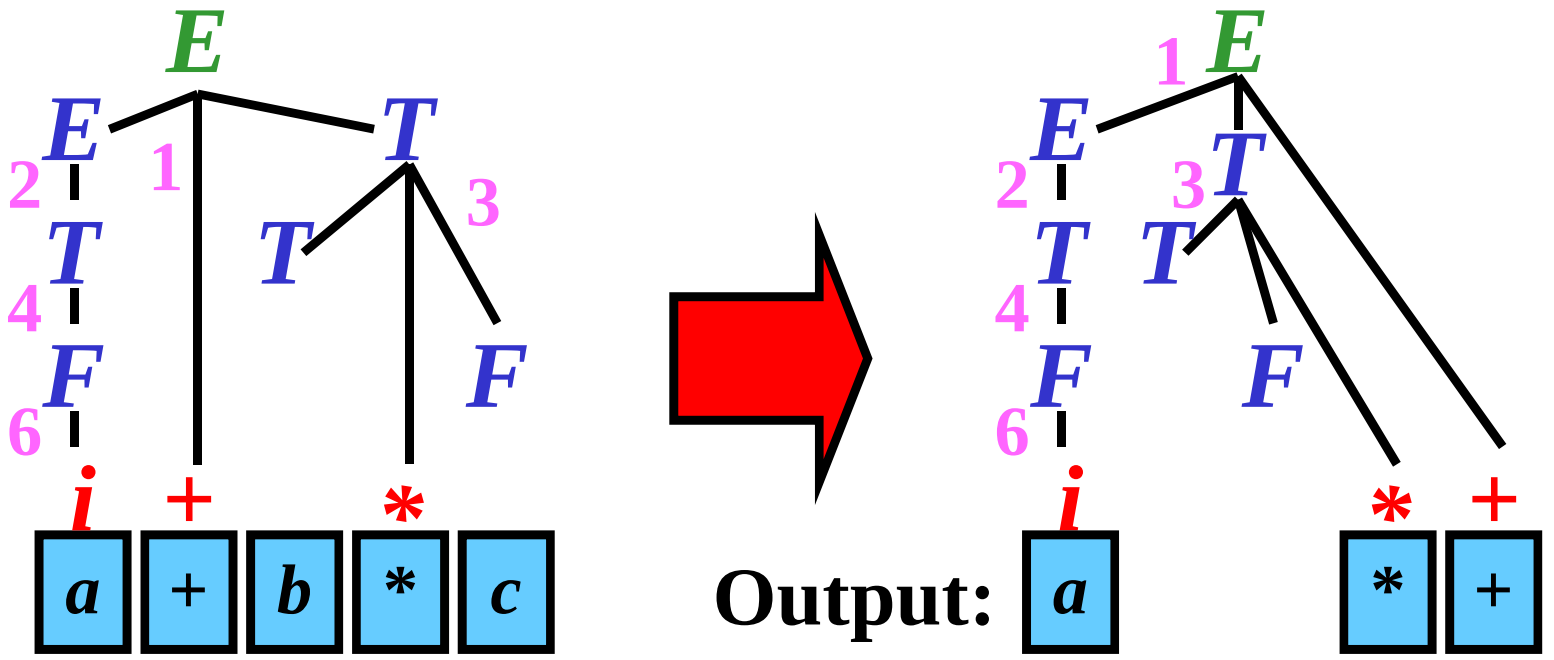
Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



One-Grammar Translation

Infix to postfix translation:

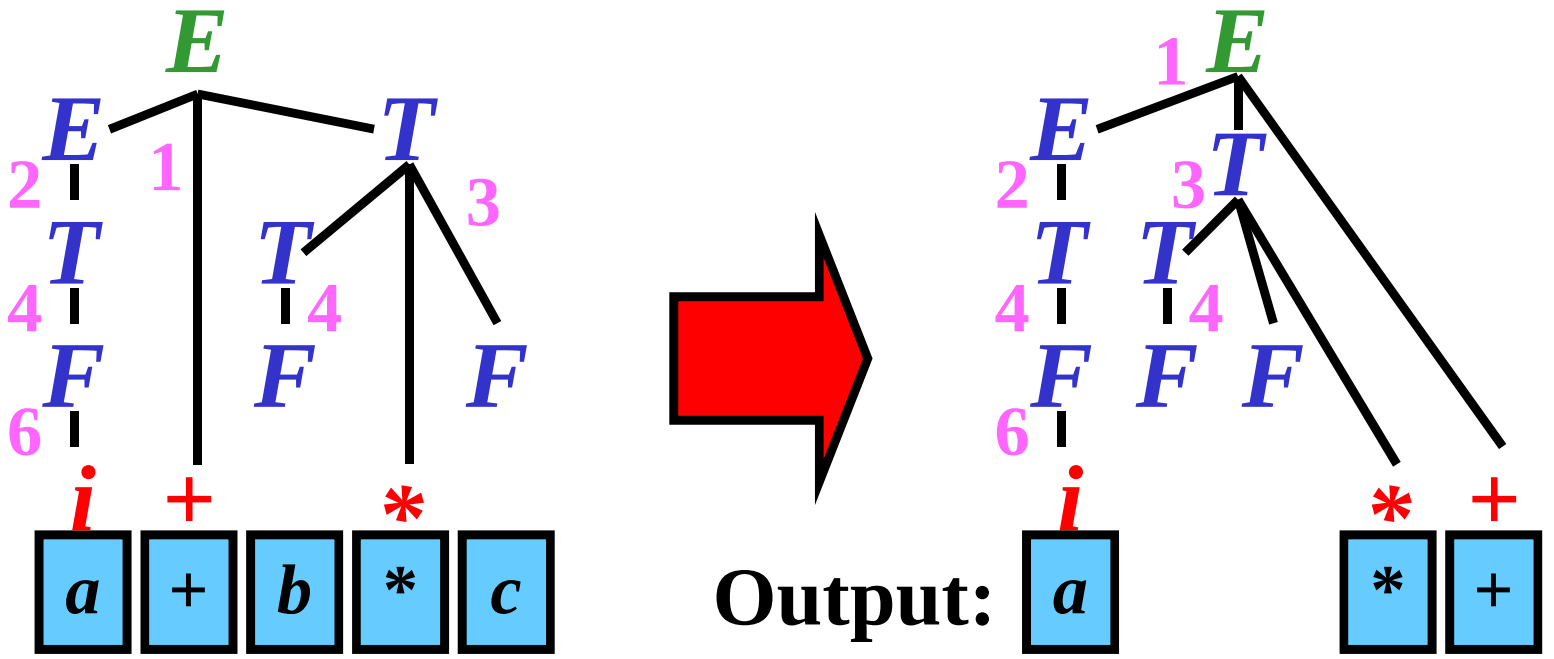
Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



One-Grammar Translation

Infix to postfix translation:

Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



One-Grammar Translation

Infix to postfix translation:

Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
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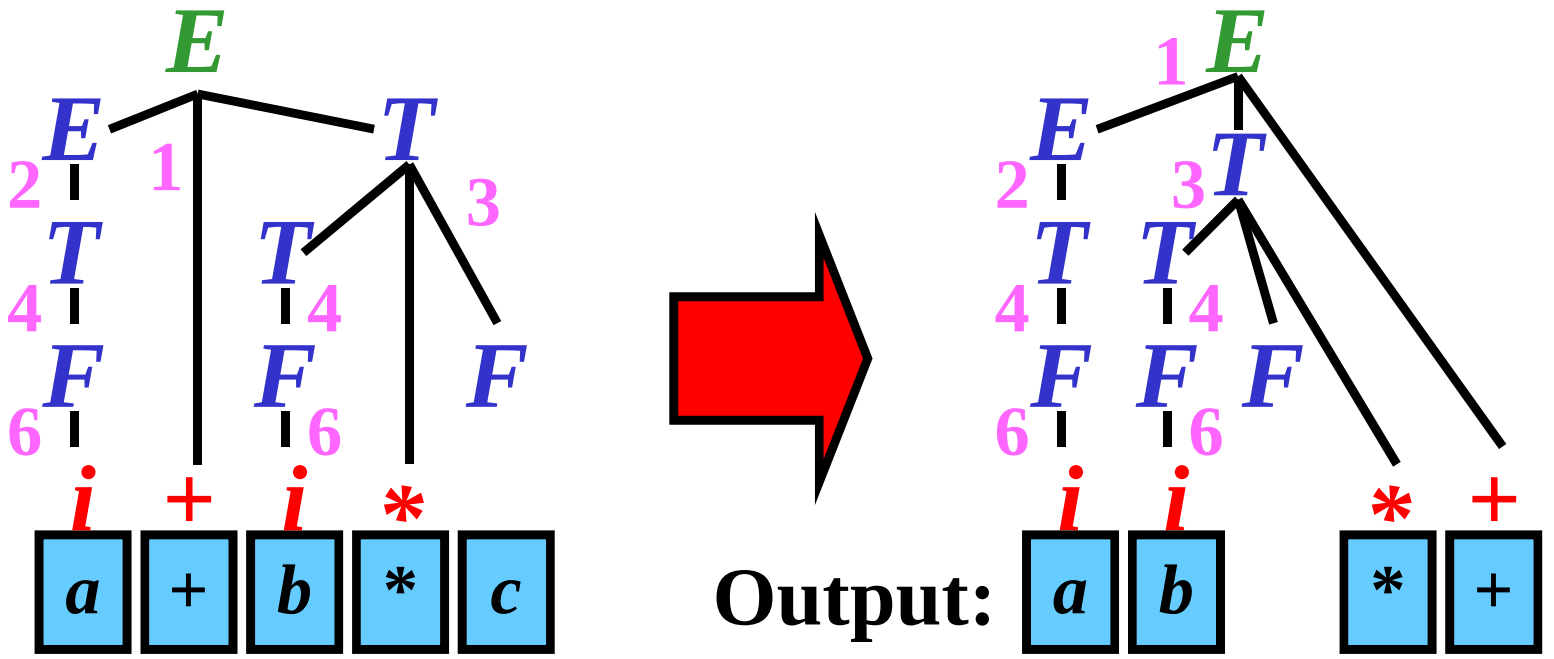
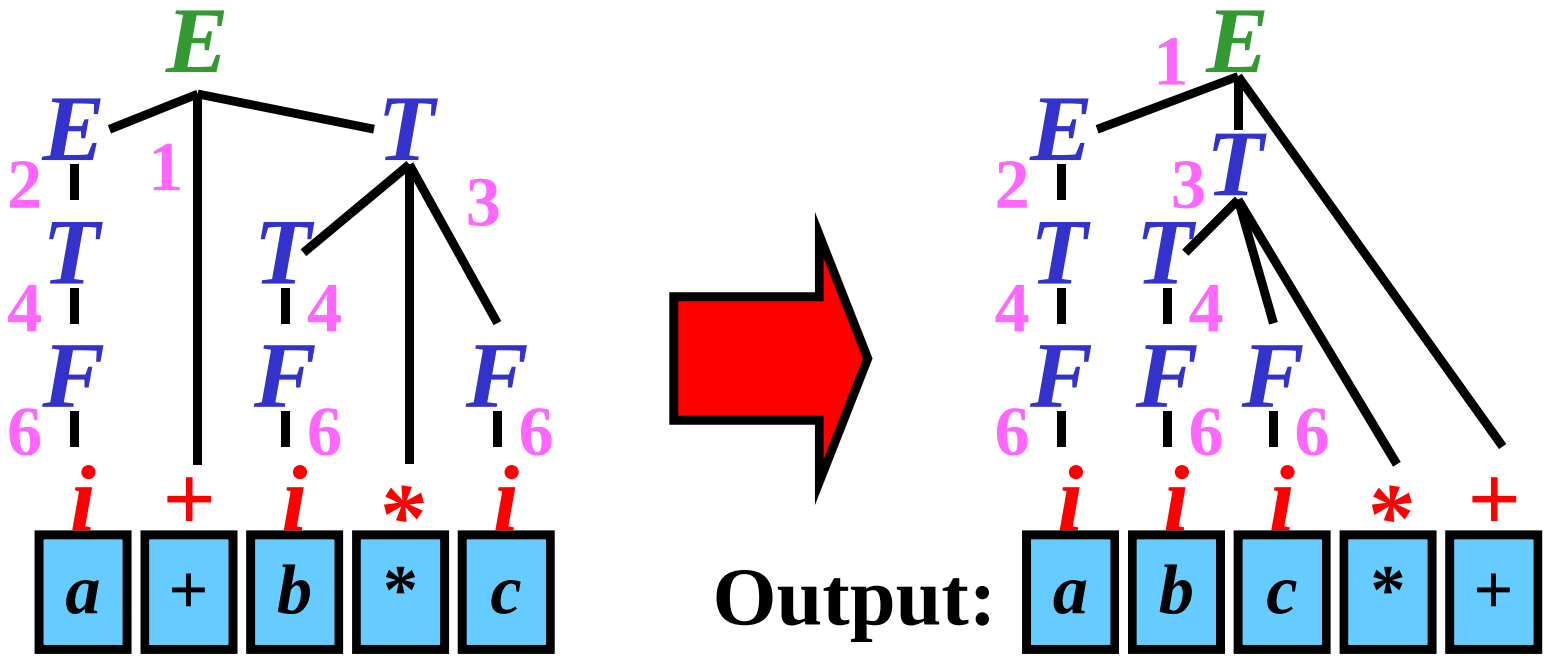
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



One-Grammar Translation

Infix to postfix translation:

Rule	Tran. Element
1: $E \rightarrow E+T$	$ET+$
2: $E \rightarrow T$	T
3: $T \rightarrow T*F$	$TF*$
4: $T \rightarrow F$	F
5: $F \rightarrow (E)$	E
6: $F \rightarrow i$	i



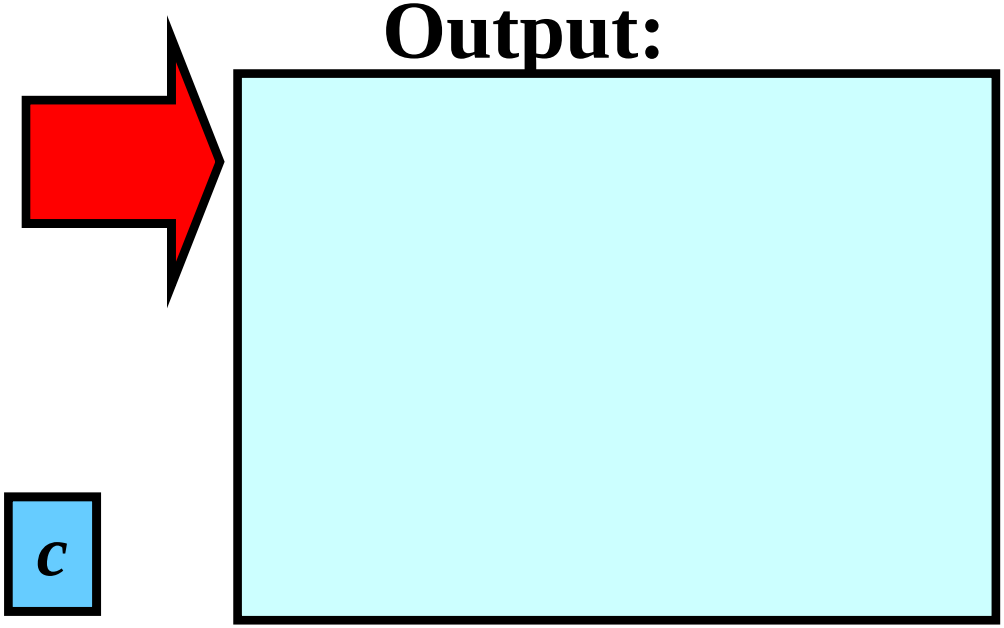
Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.*loc*, , *i.loc*)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.*loc*, , E_i.*loc*)}
5: $E_i \rightarrow i$	{ generate('=', *i.loc*, , E_i.*loc*)}

Output:



Input: *x* | = | *a* | + | *b* | * | *c*

Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.*loc*, , *i.loc*)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.*loc*, , E_i.*loc*)}
5: $E_i \rightarrow i$	{ generate('=', *i.loc*, , E_i.*loc*)}

Output:

('=', ☛*a*, , E_1.*loc*)

E_1

5 |

i

Input: | *x* | = | *a* | + | *b* | * | *c* |

Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.*loc*, , *i.loc*)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.*loc*, , E_i.*loc*)}
5: $E_i \rightarrow i$	{ generate('=', *i.loc*, , E_i.*loc*)}

Output:

('=', ☛*a*, , E_1.*loc*)
('=', ☛*b*, , E_2.*loc*)

E_1 E_2
5 5
i *i*

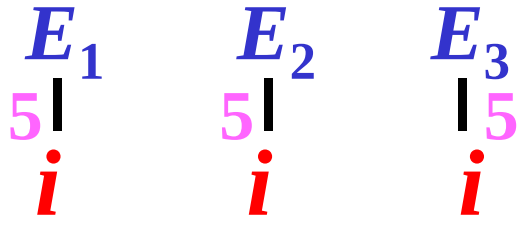
Input: | *x* | = | *a* | + | *b* | * | *c* |

Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.*loc*, , *i.loc*)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.*loc*, E_k.*loc*, E_i.*loc*)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.*loc*, , E_i.*loc*)}
5: $E_i \rightarrow i$	{ generate('=', *i.loc*, , E_i.*loc*)}



Input: *x* | = | *a* | + | *b* | * | *c*

Output:

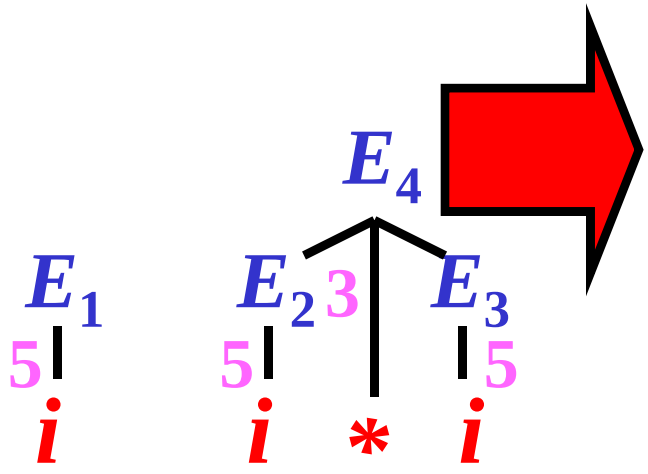
('=', ☛*a*, , E_1.*loc*)
('=', ☛*b*, , E_2.*loc*)
('=', ☛*c*, , E_3.*loc*)

Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.loc, , i.loc)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.loc, E_k.loc, E_i.loc)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.loc, E_k.loc, E_i.loc)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.loc, , E_i.loc)}
5: $E_i \rightarrow i$	{ generate('=', i.loc, , E_i.loc)}



Output:

('=', ☛a, , E_1.loc)
('=', ☛b, , E_2.loc)
('=', ☛c, , E_3.loc)
('*', E_2.loc,E_3.loc,E_4.loc)

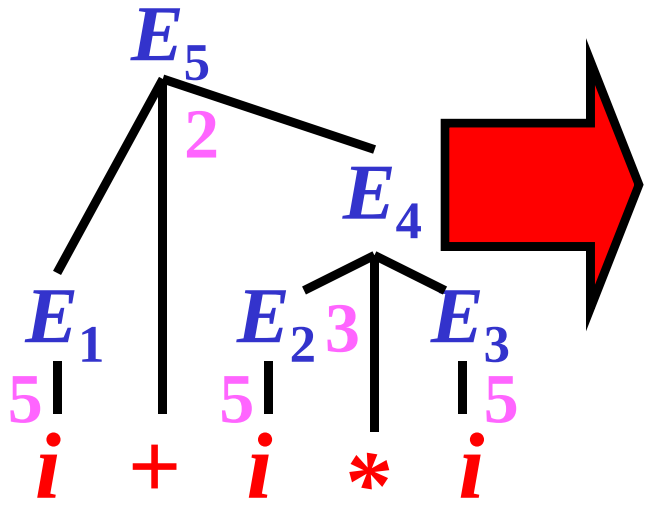
Input: | x | = | a | + | b | * | c |

Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.loc, , i.loc)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.loc, E_k.loc, E_i.loc)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.loc, E_k.loc, E_i.loc)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.loc, , E_i.loc)}
5: $E_i \rightarrow i$	{ generate('=', i.loc, , E_i.loc)}



Input: x = a + b * c

Output:

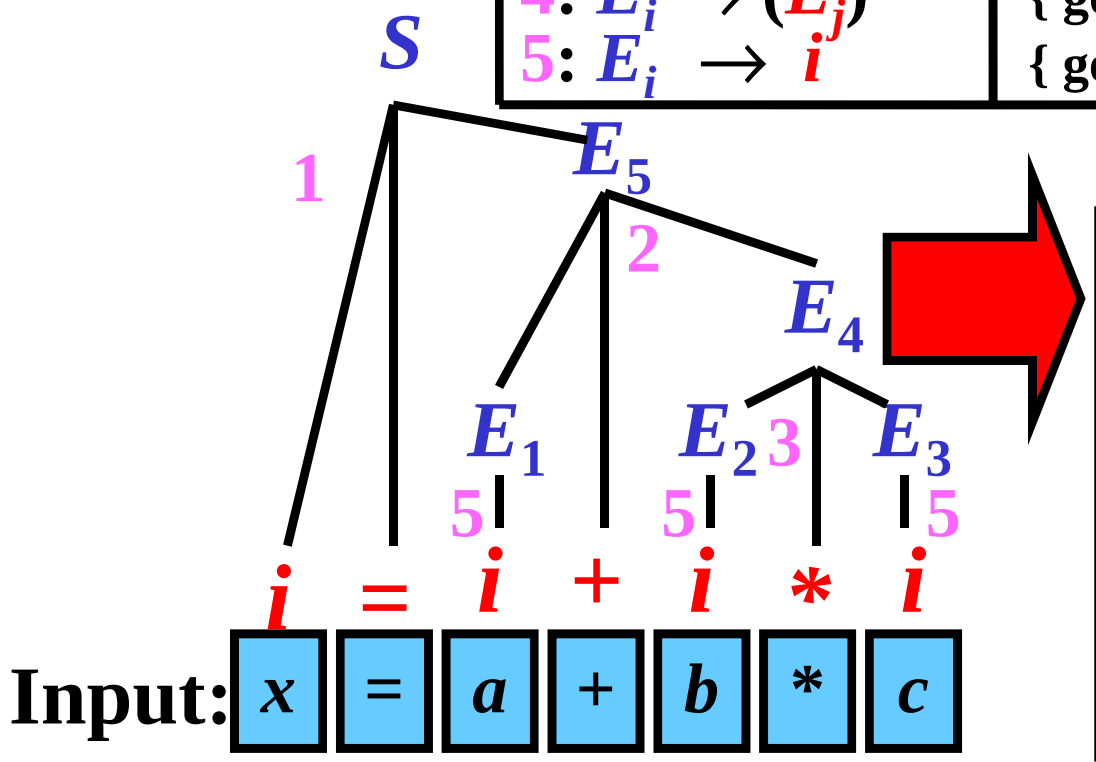
('=', a, , E_1.loc)
('=', b, , E_2.loc)
('=', c, , E_3.loc)
('*', E_2.loc,E_3.loc,E_4.loc)
('+', E_1.loc,E_4.loc,E_5.loc)

Direct Generation of 3AC

Gist: BU parser directs the generation of 3AC directly.

Example:

Rule:	Semantic Action:
1: $S \rightarrow i = E_k$	{ generate('=', E_k.loc, , i.loc)}
2: $E_i \rightarrow E_j + E_k$	{ generate('+', E_j.loc, E_k.loc, E_i.loc)}
3: $E_i \rightarrow E_j * E_k$	{ generate('*', E_j.loc, E_k.loc, E_i.loc)}
4: $E_i \rightarrow (E_j)$	{ generate('=', E_j.loc, , E_i.loc)}
5: $E_i \rightarrow i$	{ generate('=', i.loc, , E_i.loc)}

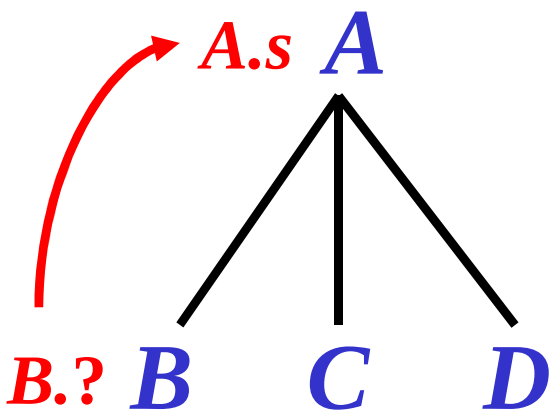


Output:

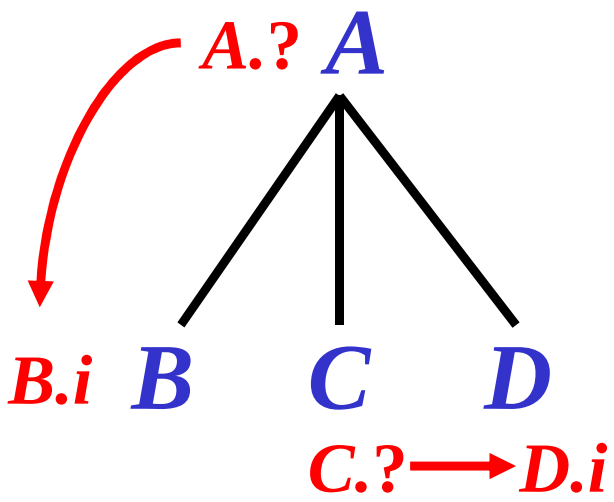
('=', ☛a, , E_1.loc)
('=', ☛b, , E_2.loc)
('=', ☛c, , E_3.loc)
('*', E_2.loc,E_3.loc,E_4.loc)
('+', E_1.loc,E_4.loc,E_5.loc)
('=', E_5.loc, , ☛x)

Top-Down Translation: Introduction

- **LL-grammar with attributes**
- **Two pushdown:**
  - **parser pushdown × semantic pushdown**
- **Two type of attributes:**
  - **synthesized:**
    (from children to parent)



iherited:
(from parent to children
or between siblings)

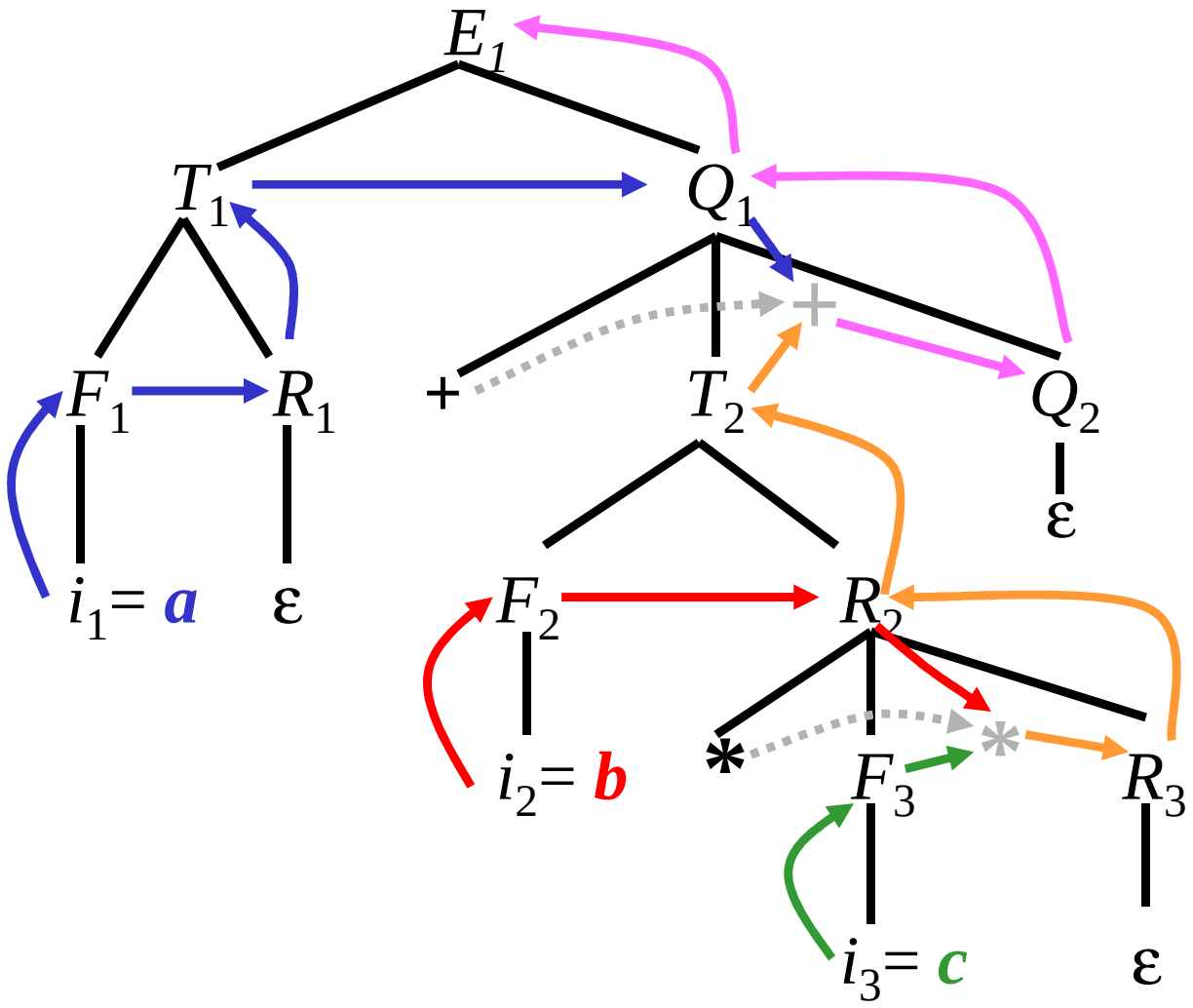


Top-Down Translation: Expressions

Grammar:

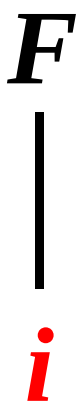
$E \rightarrow TQ$
$Q \rightarrow +TQ$
$Q \rightarrow \varepsilon$
$T \rightarrow FR$
$R \rightarrow *FR$
$R \rightarrow \varepsilon$
$F \rightarrow (E)$
$F \rightarrow i$

Parse tree for *a* + *b* * *c*:



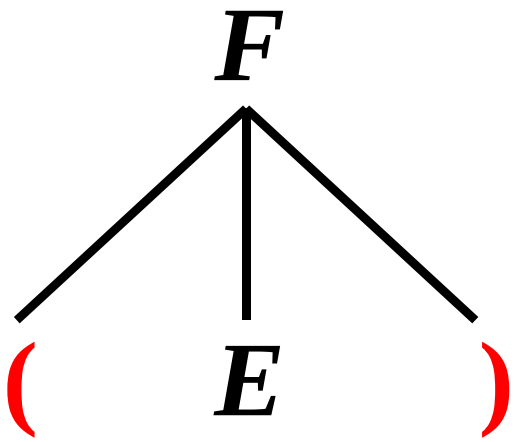
Expressions: Variable & Parentheses

Variable:



$F \rightarrow i$

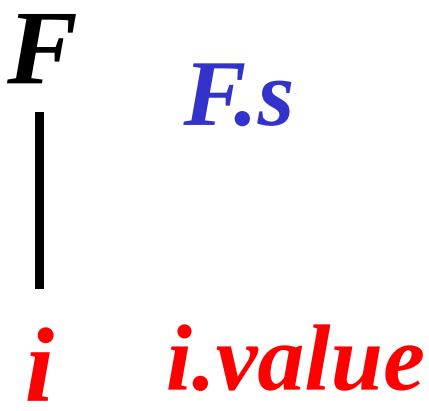
Parentheses:



$E \rightarrow (F)$

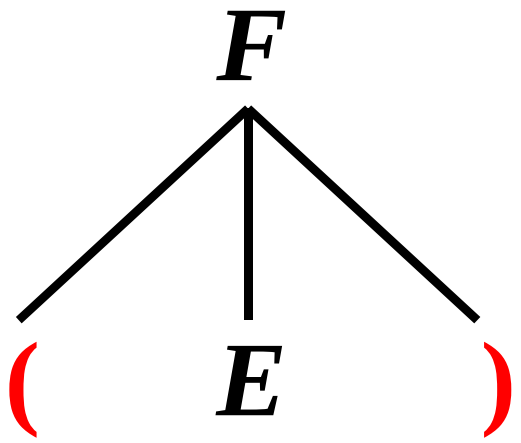
Expressions: Variable & Parentheses

Variable:



$F \rightarrow i$

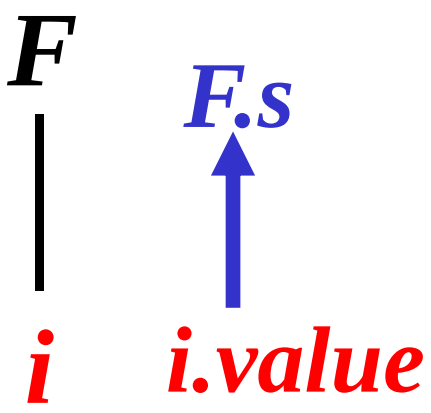
Parentheses:



$E \rightarrow (F)$

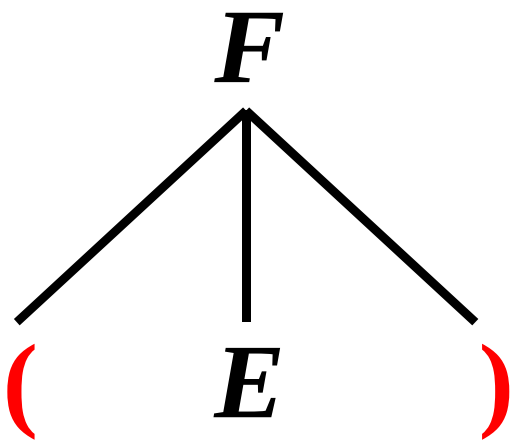
Expressions: Variable & Parentheses

Variable:



$F \rightarrow i \ \{F.s := i.value\}$

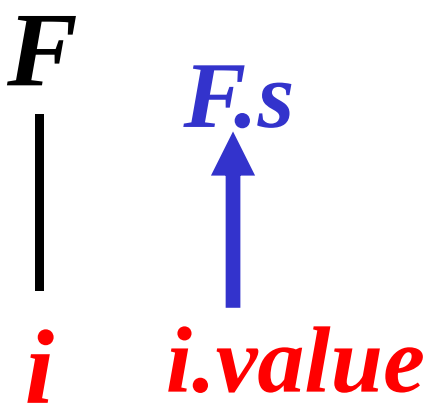
Parentheses:



$E \rightarrow (F \qquad)$

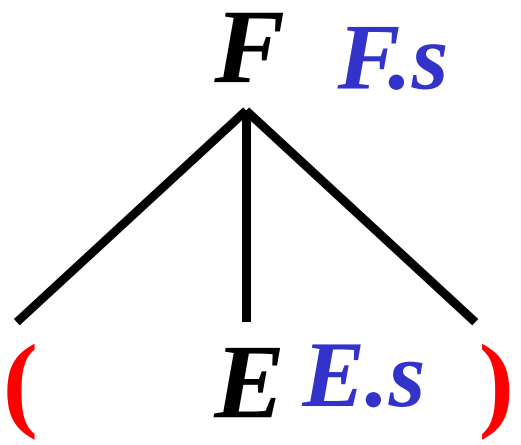
Expressions: Variable & Parentheses

Variable:



$F \rightarrow i \ \{F.s := i.value\}$

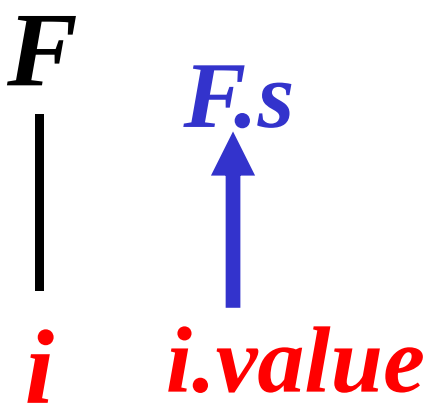
Parentheses:



$E \rightarrow (F \quad)$

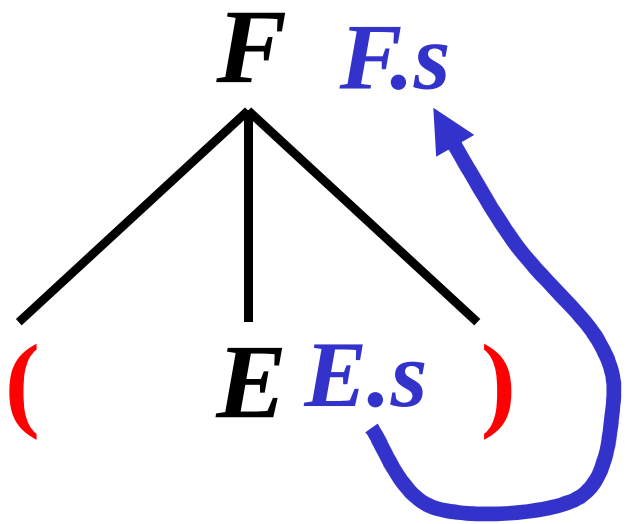
Expressions: Variable & Parentheses

Variable:



$F \rightarrow i \ \{F.s := i.value\}$

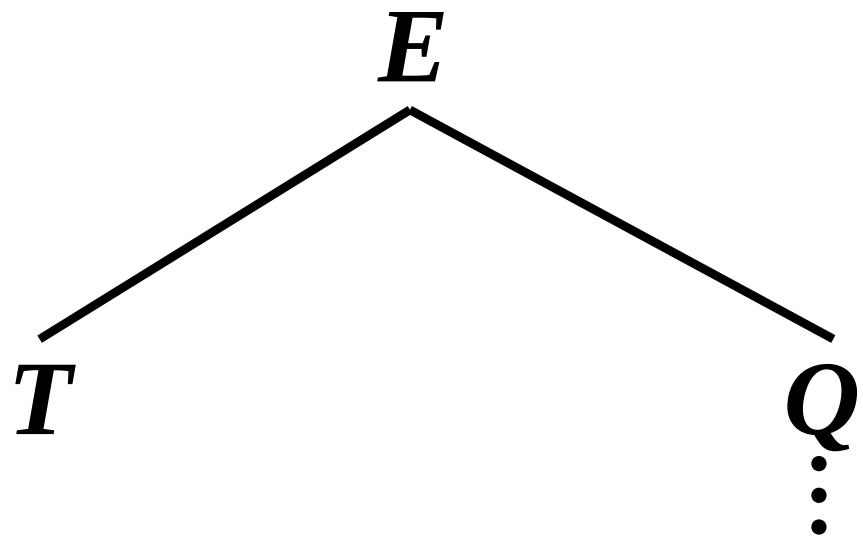
Parentheses:



$E \rightarrow (F \ \{F.s := E.s\} \ )$

Expressions: Addition 1/4

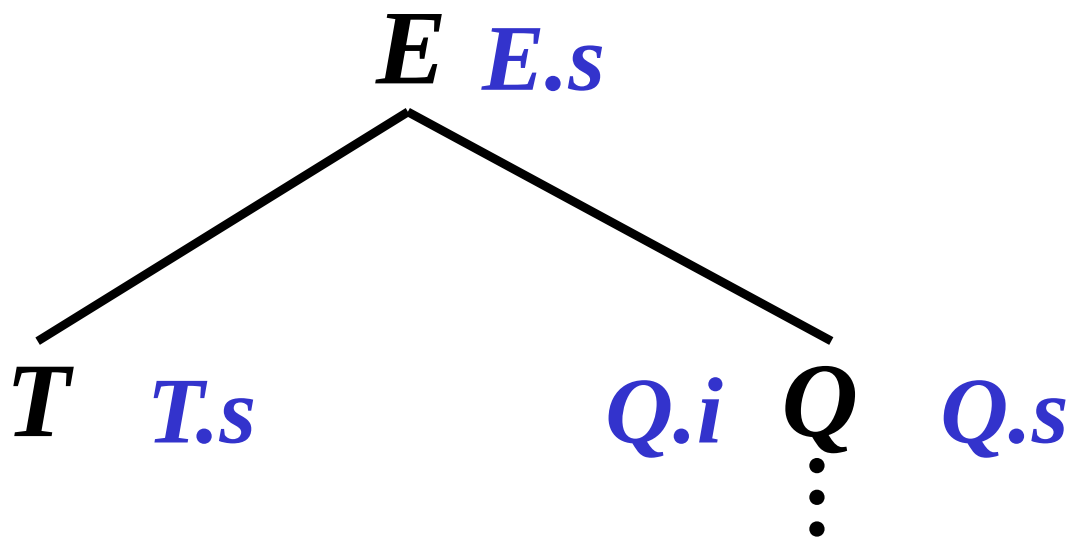
I.



$E \rightarrow T$ Q

Expressions: Addition 1/4

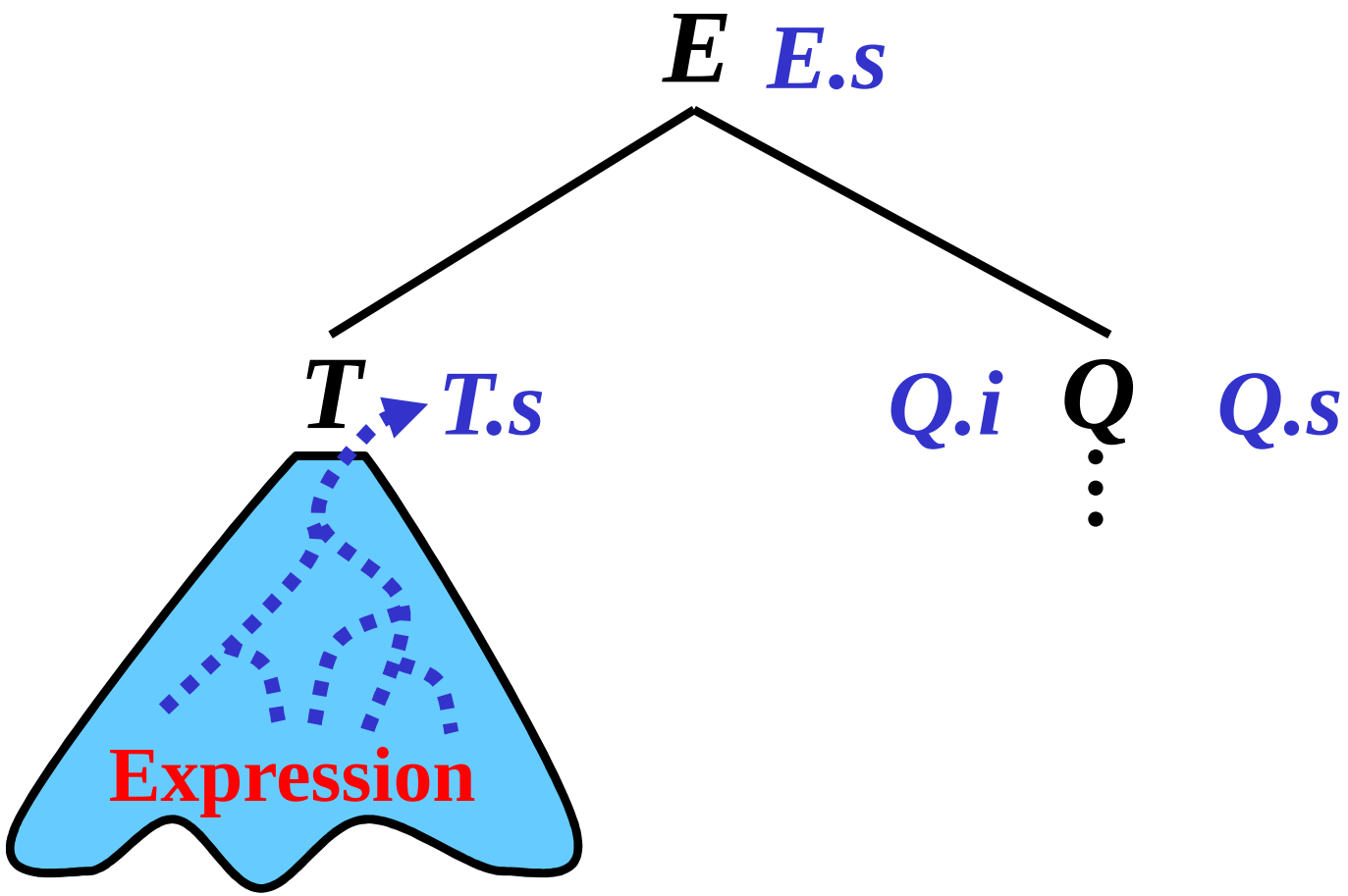
I.



$E \rightarrow T$ Q

Expressions: Addition 1/4

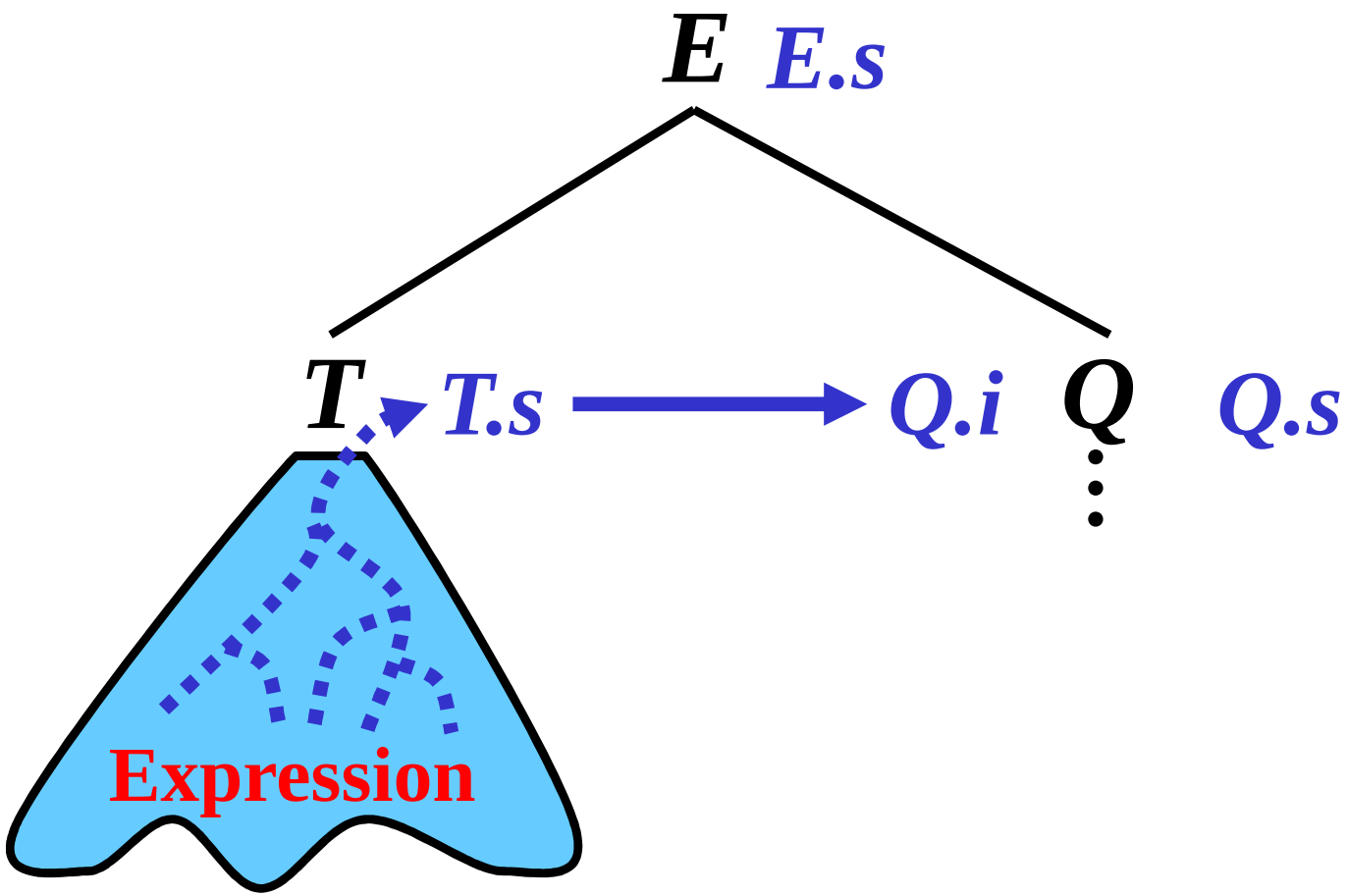
I.



$E \rightarrow T$ Q

Expressions: Addition 1/4

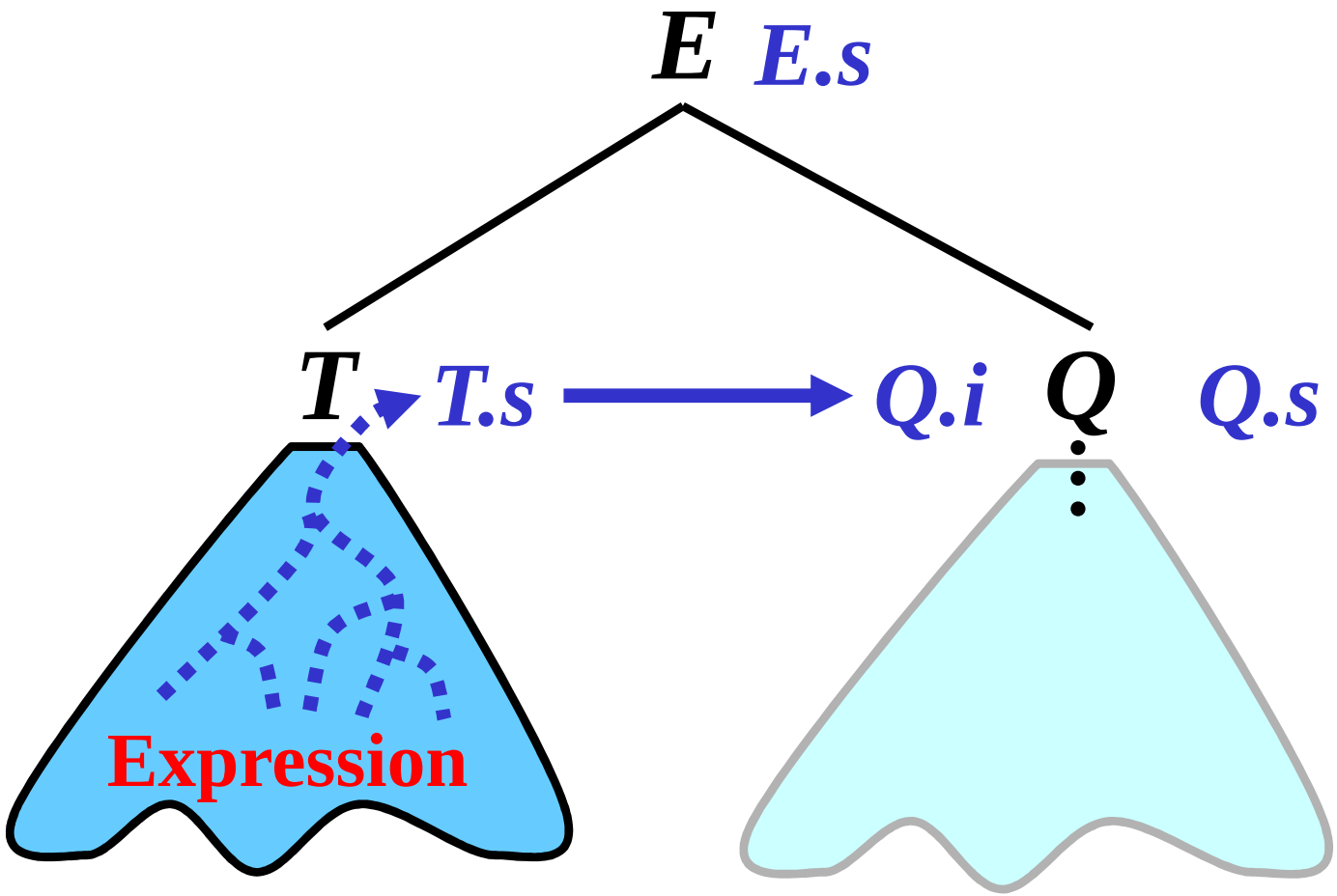
I.



$$E \rightarrow T \{ Q.i := T.s \} \; Q$$

Expressions: Addition 1/4

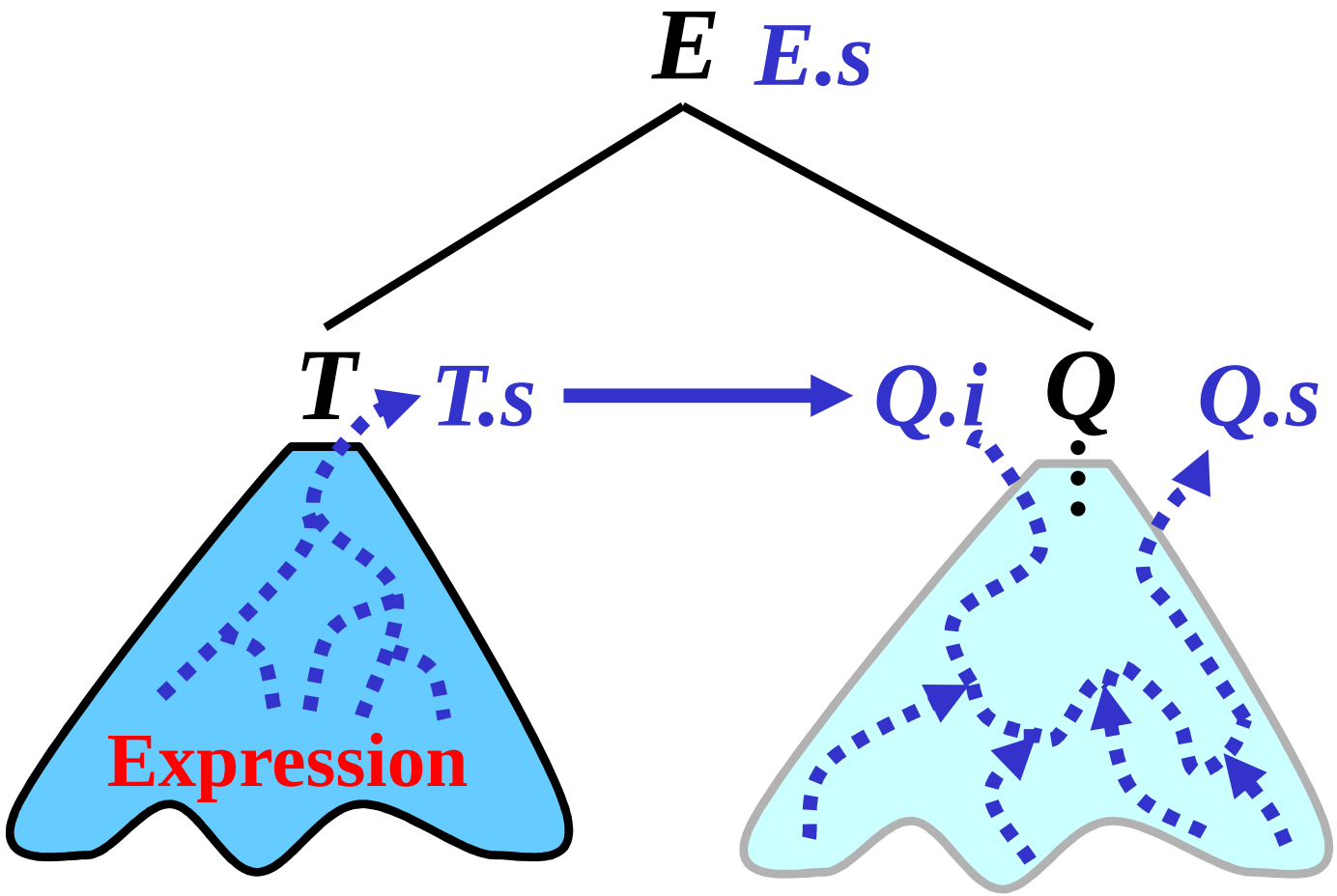
I.



$$E \rightarrow T \{ Q.i := T.s \} \; Q$$

Expressions: Addition 1/4

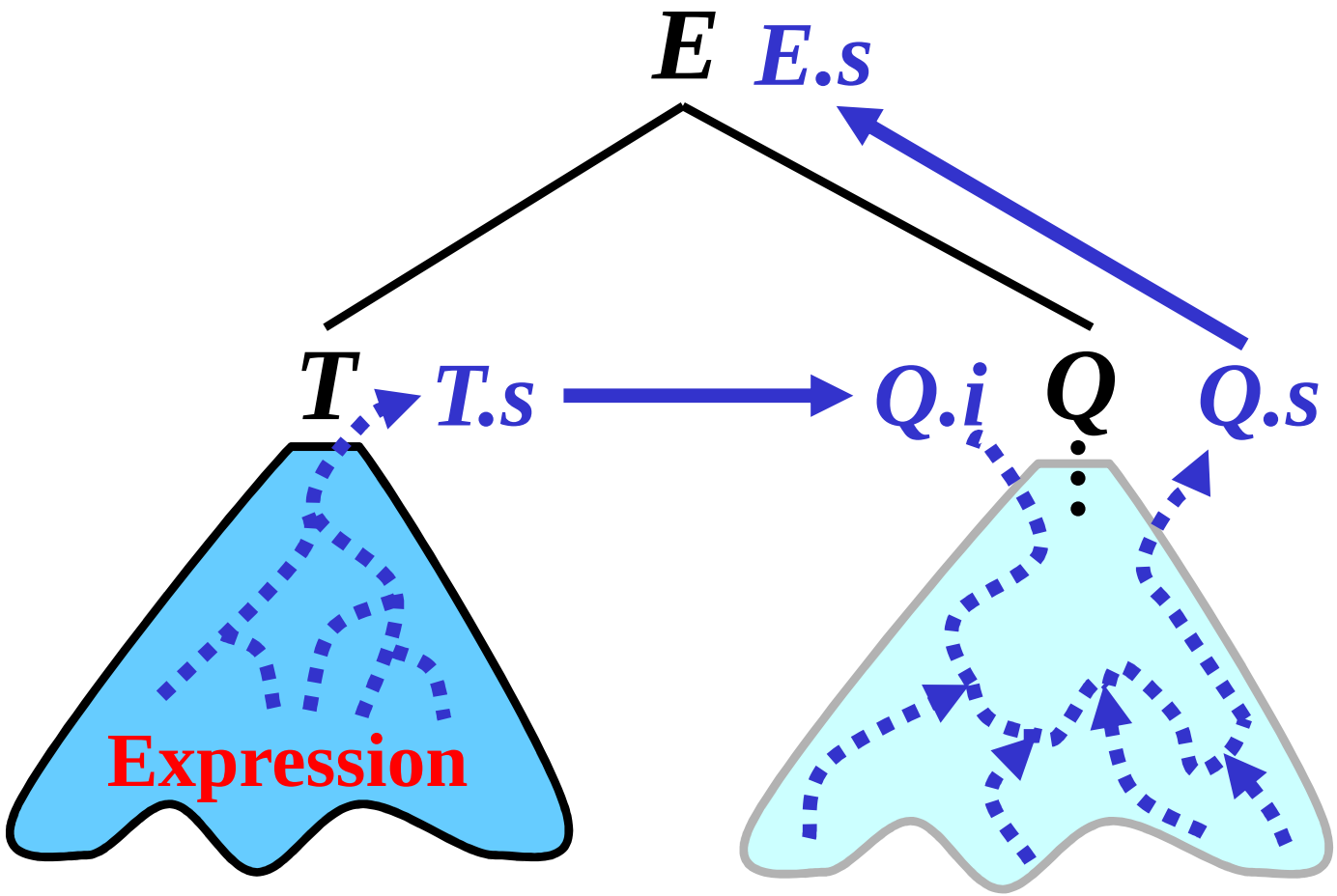
I.



$$E \rightarrow T \{ Q.i := T.s \} \; Q$$

Expressions: Addition 1/4

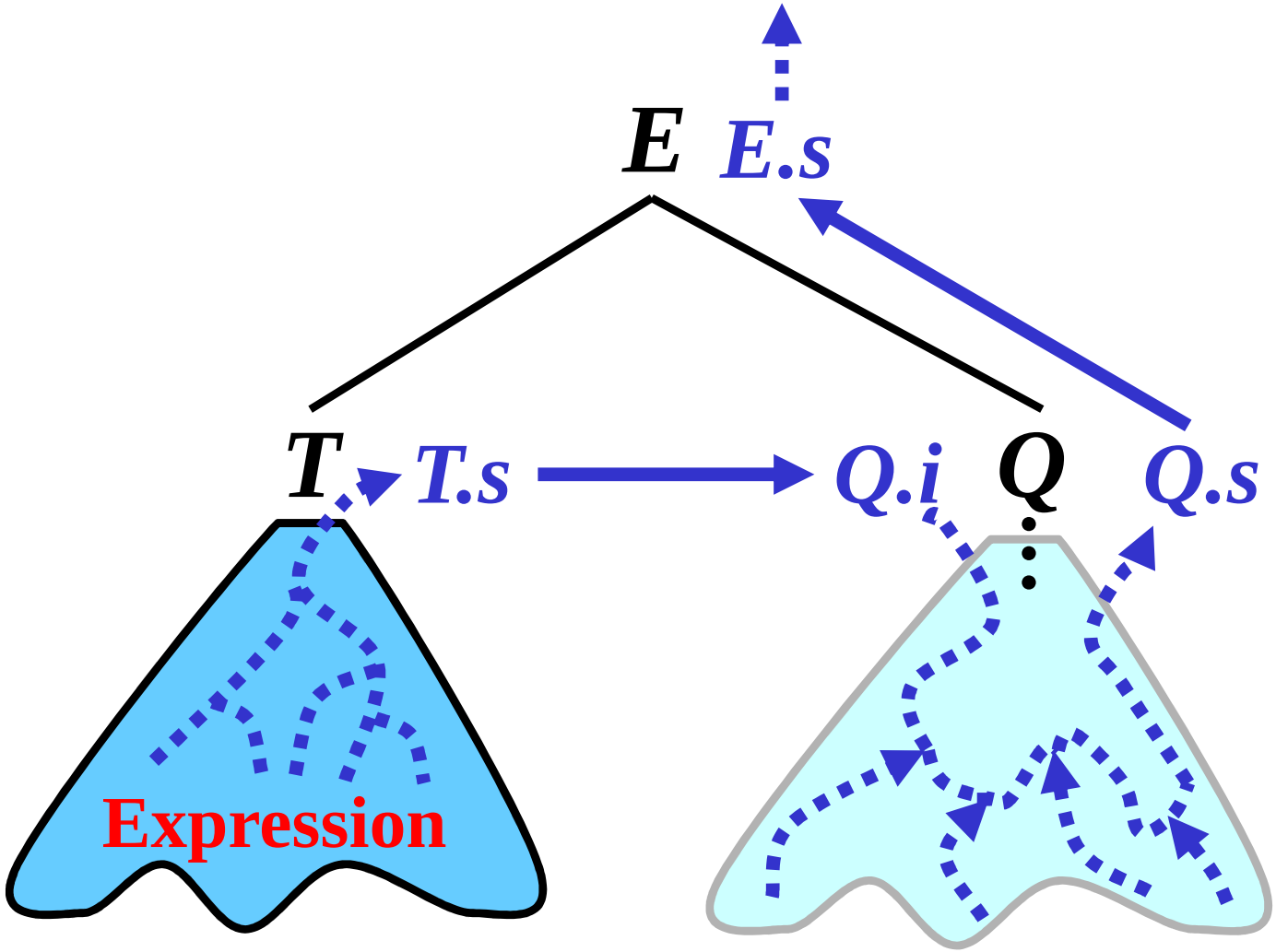
I.



$$E \rightarrow T \{ Q.i := T.s \}\ Q \{ E.s := Q.s \}$$

Expressions: Addition 1/4

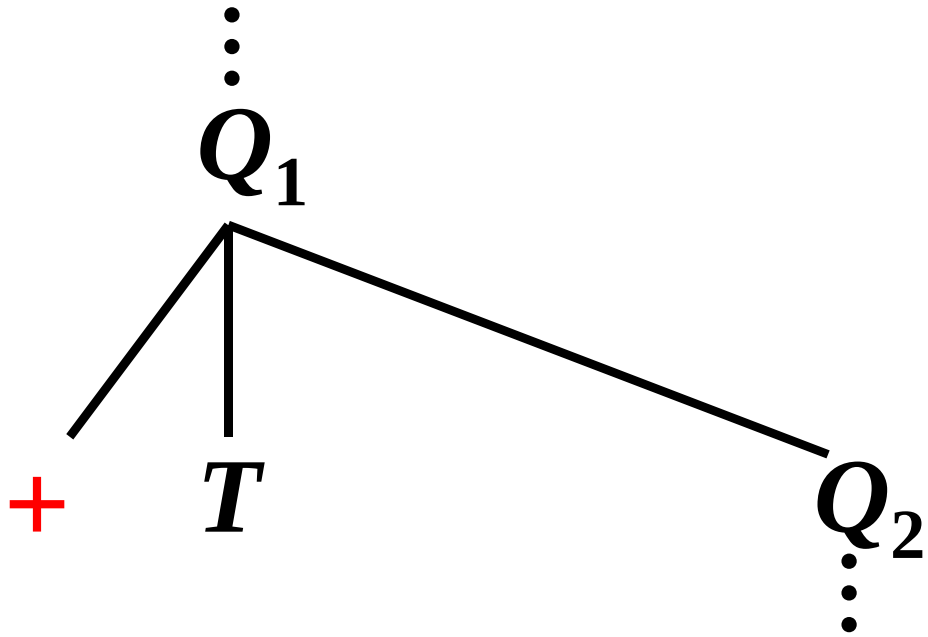
I.



$$E \rightarrow T \{ Q.i := T.s \}\ Q \{ E.s := Q.s \}$$

Expressions: Addition 2/4

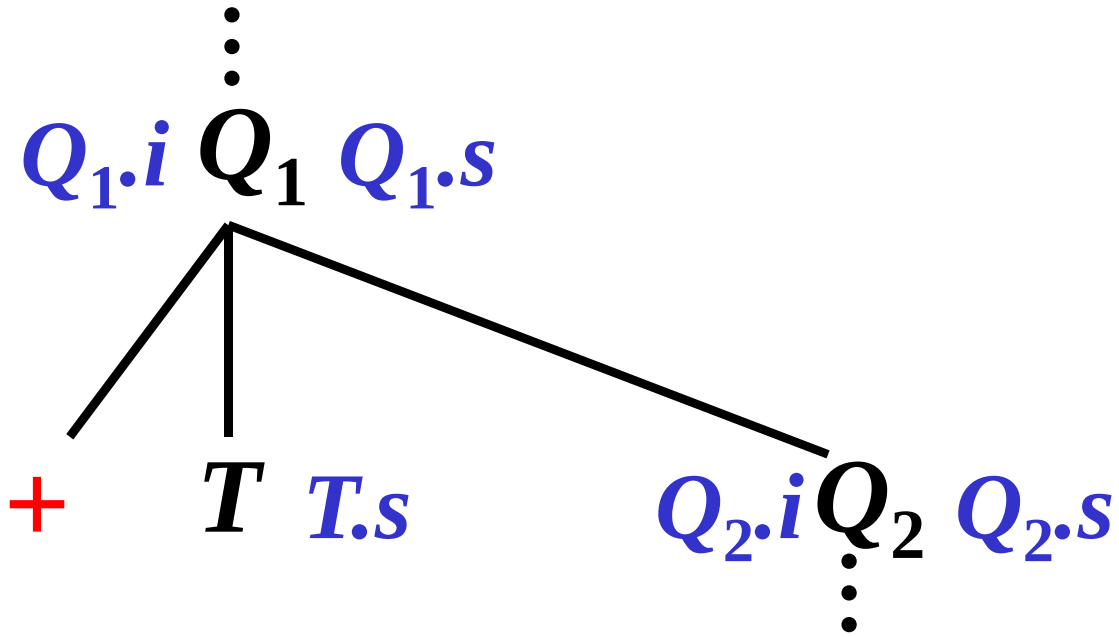
II.



$Q_1 \rightarrow +T$ Q_2

Expressions: Addition 2/4

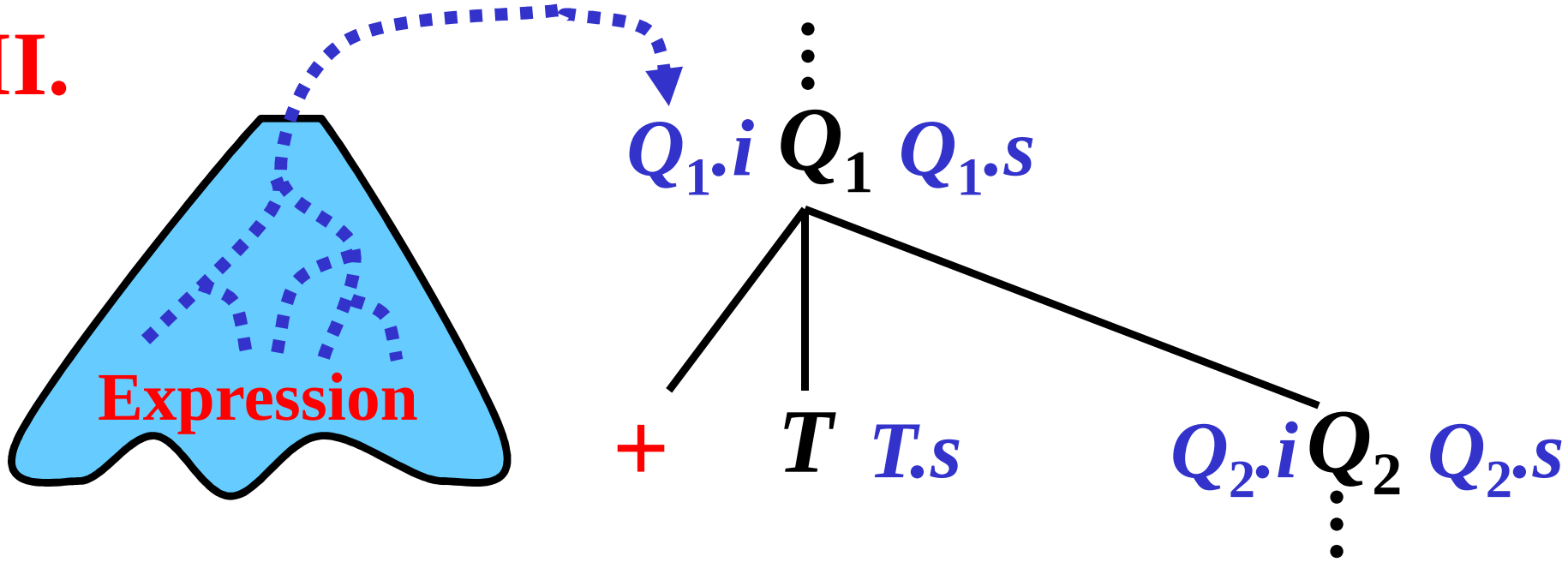
II.



$Q_1 \rightarrow +T$ Q_2

Expressions: Addition 2/4

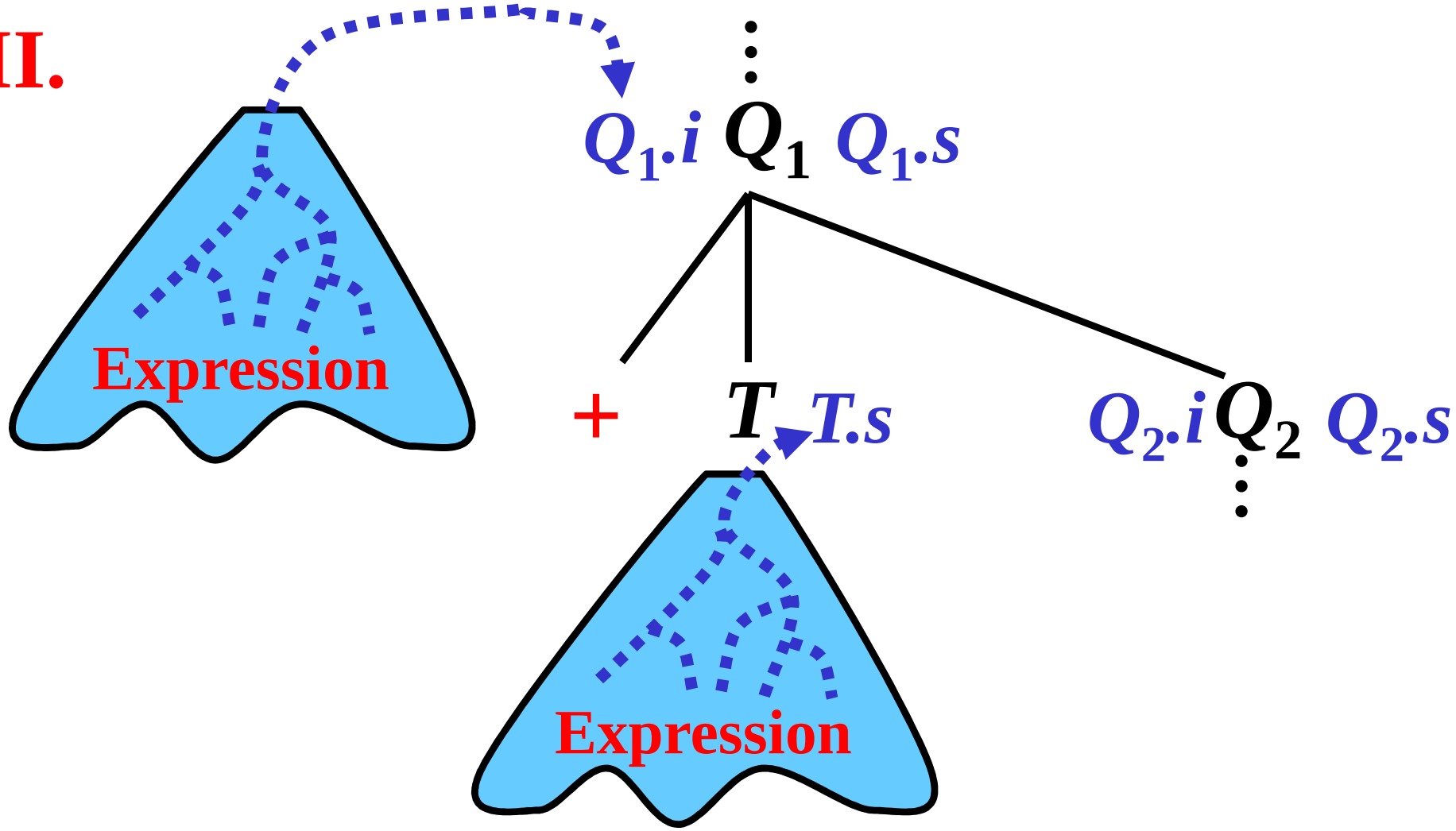
II.



$Q_1 \rightarrow +T$ Q_2

Expressions: Addition 2/4

II.

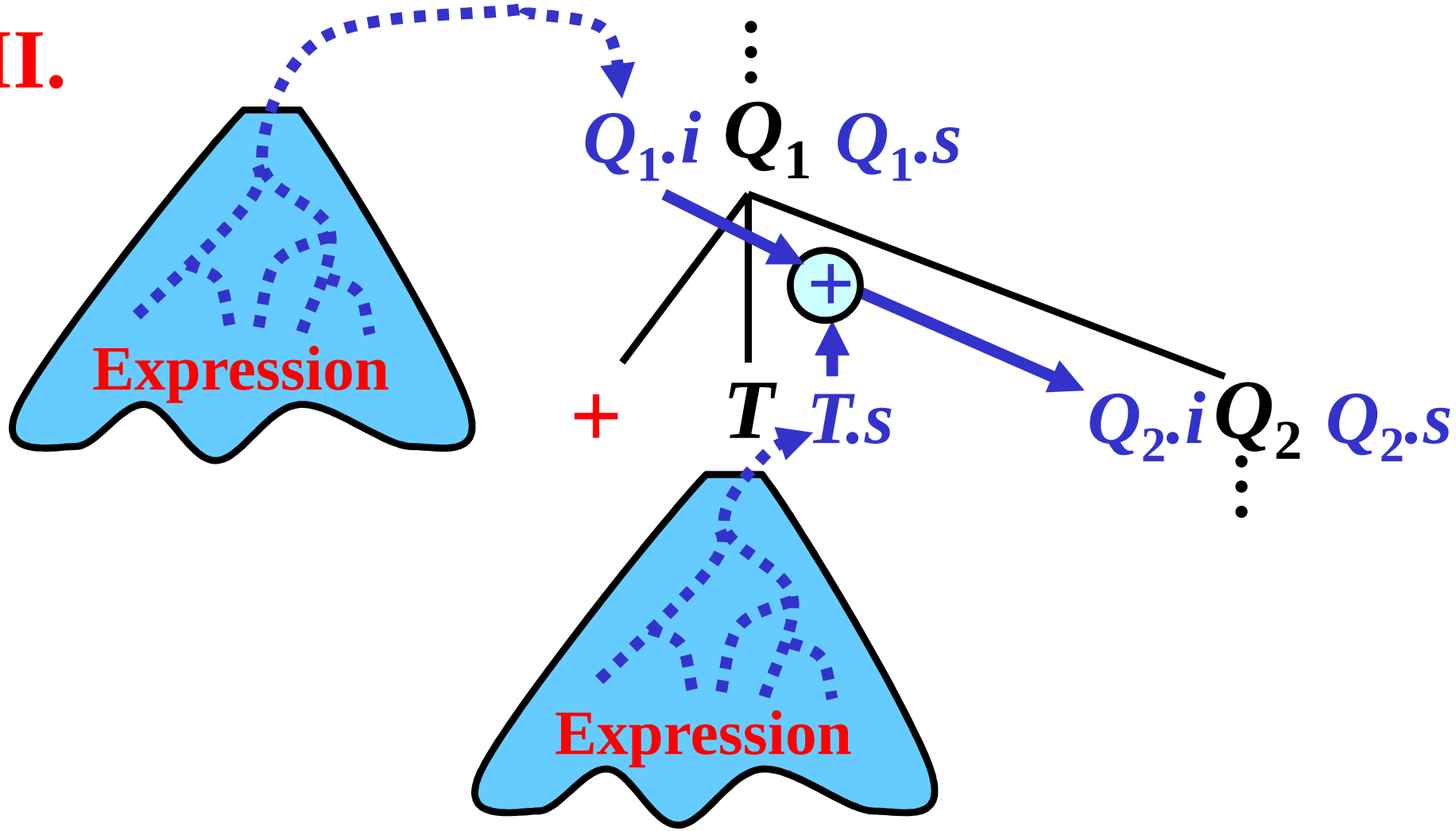


$Q_1 \rightarrow +T$

Q_2

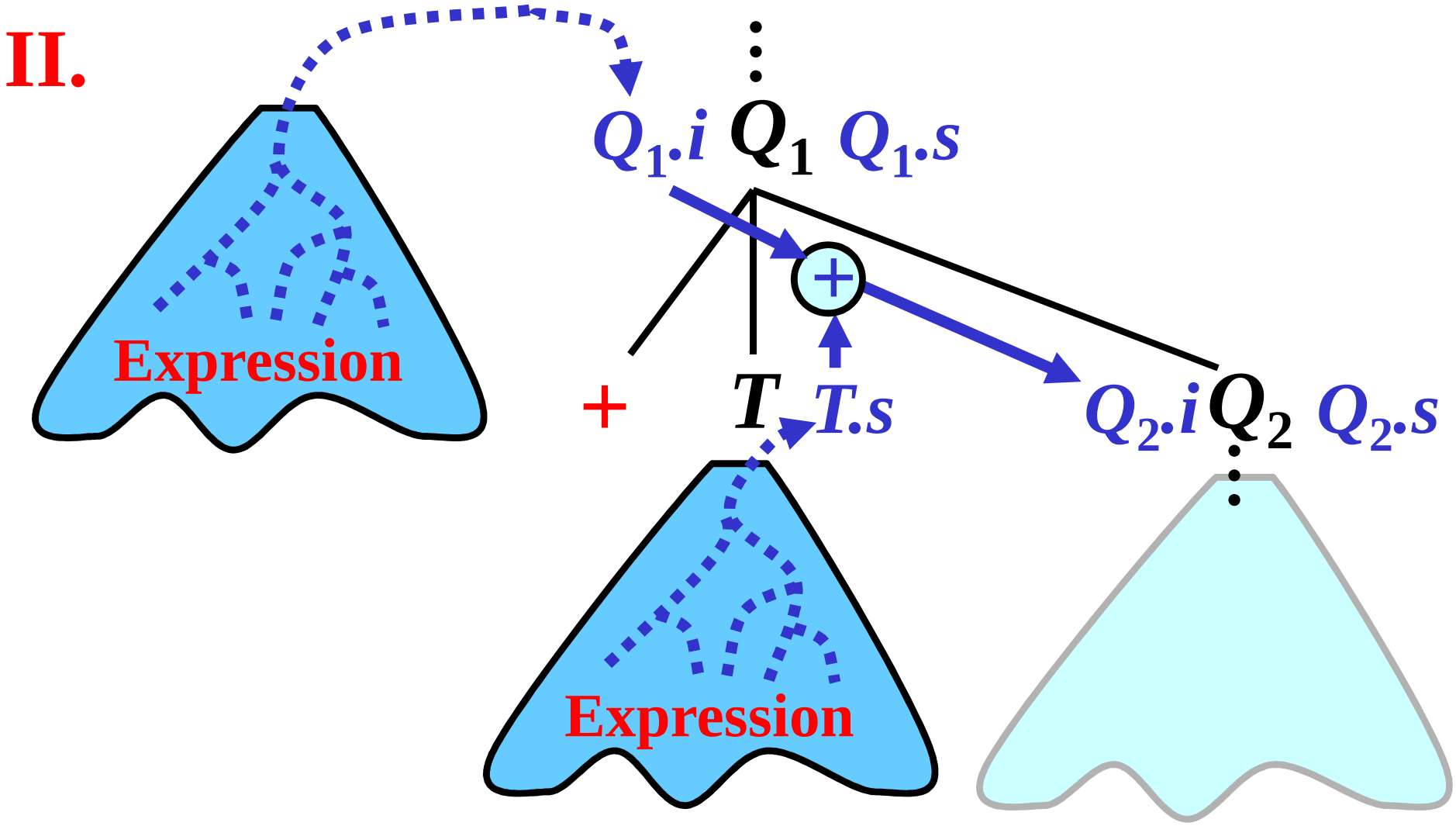
Expressions: Addition 2/4

II.



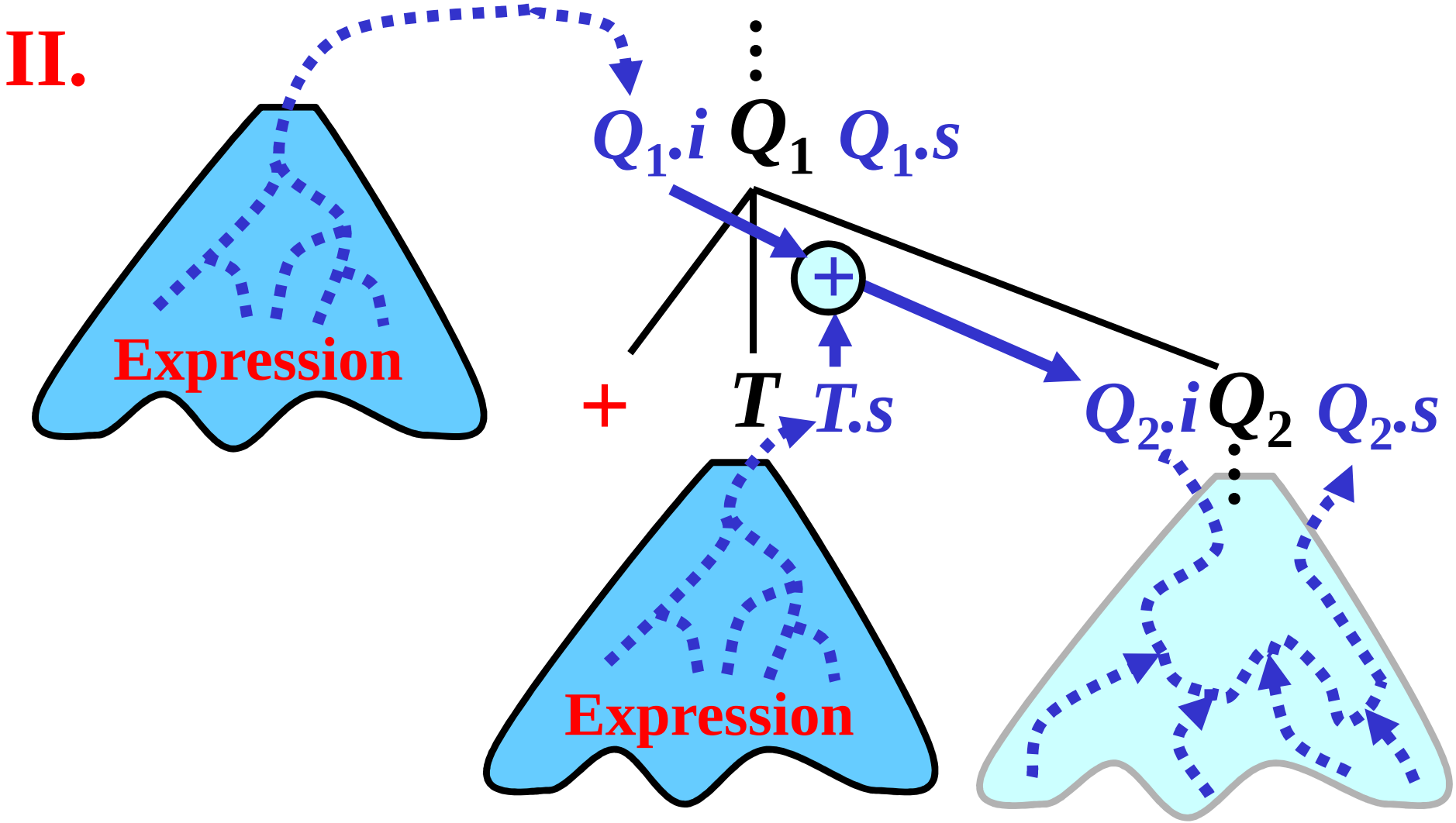
$$Q_1 \rightarrow +T \{ Q_2.i := Q_1.i + T.s \} Q_2$$

Expressions: Addition 2/4



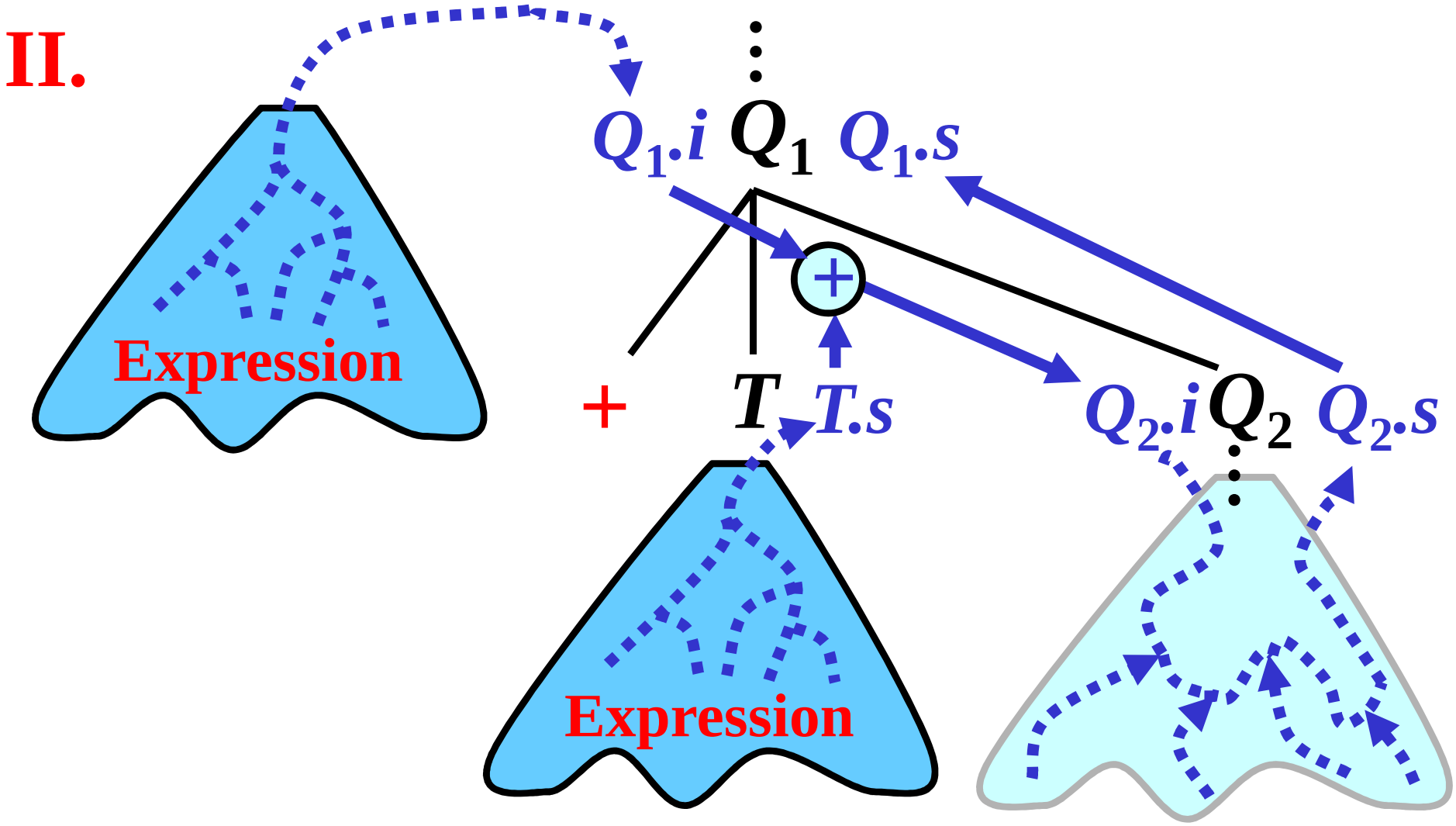
$$Q_1 \rightarrow +T \{ Q_2.i := Q_1.i + T.s \} Q_2$$

Expressions: Addition 2/4



$$Q_1 \rightarrow +T \{ Q_2.i := Q_1.i + T.s \} Q_2$$

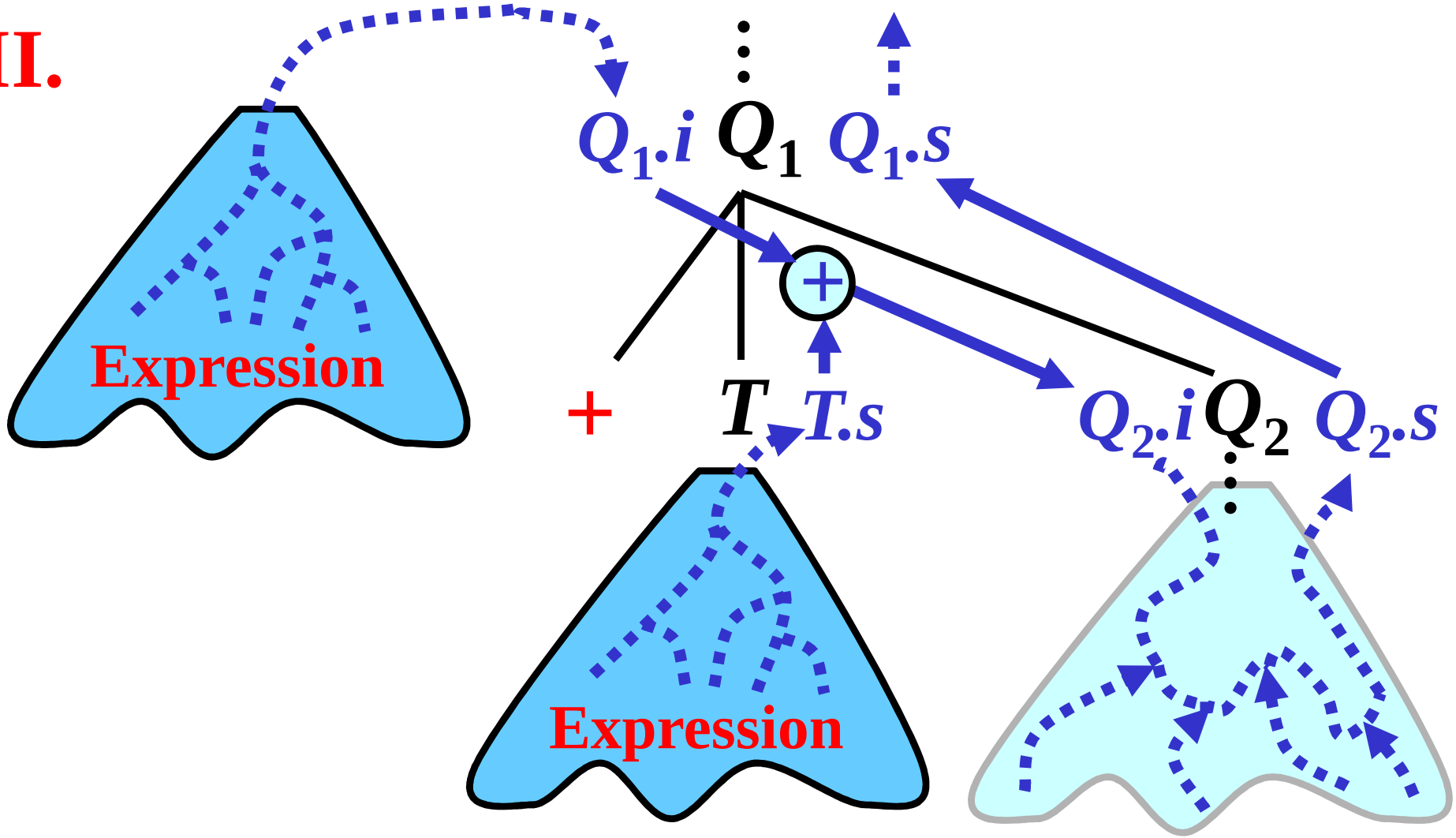
Expressions: Addition 2/4



$$Q_1 \rightarrow +T \{ Q_2.i := Q_1.i + T.s \} Q_2 \{ Q_1.s := Q_2.s \}$$

Expressions: Addition 2/4

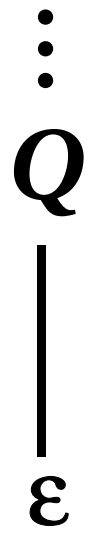
II.



$$Q_1 \rightarrow +T \{ Q_2.i := Q_1.i + T.s \} Q_2 \{ Q_1.s := Q_2.s \}$$

Expressions: Addition 3/4

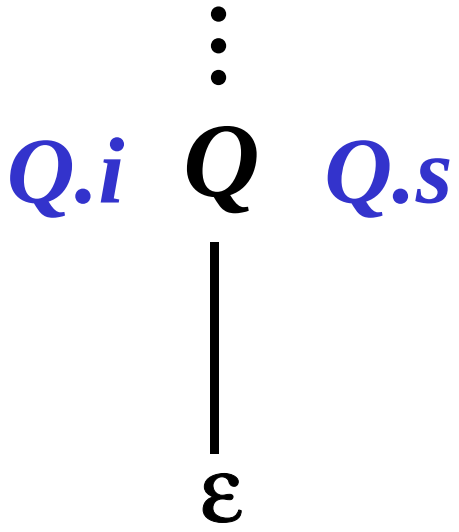
III.



$Q \rightarrow \varepsilon$

Expressions: Addition 3/4

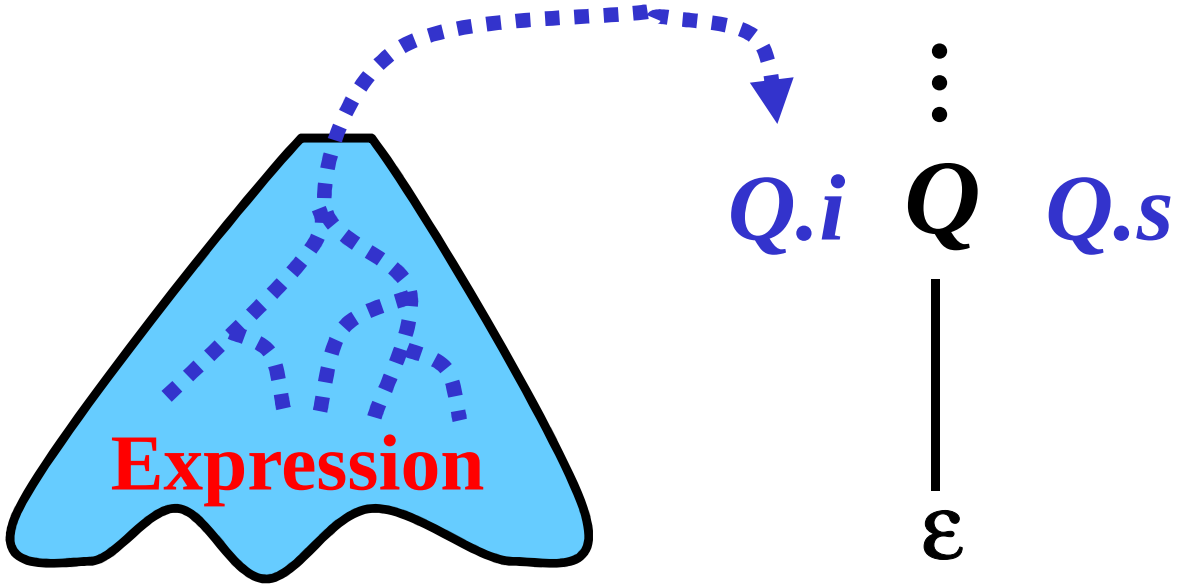
III.



$$Q \rightarrow \varepsilon$$

Expressions: Addition 3/4

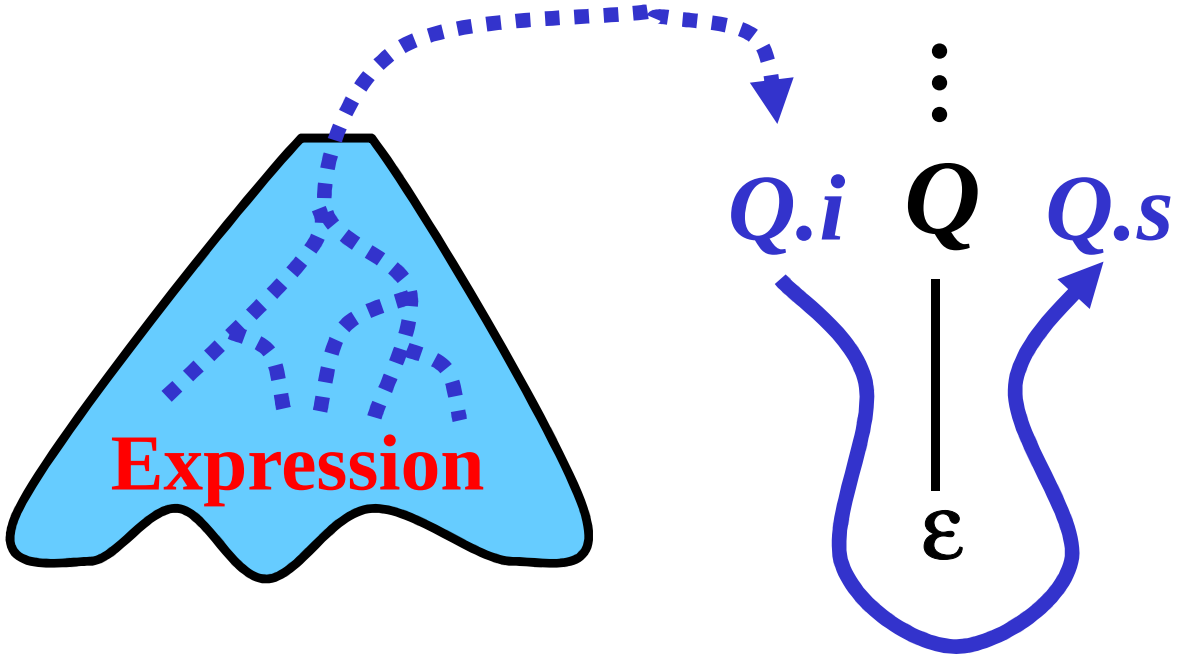
III.



$$Q \rightarrow \varepsilon$$

Expressions: Addition 3/4

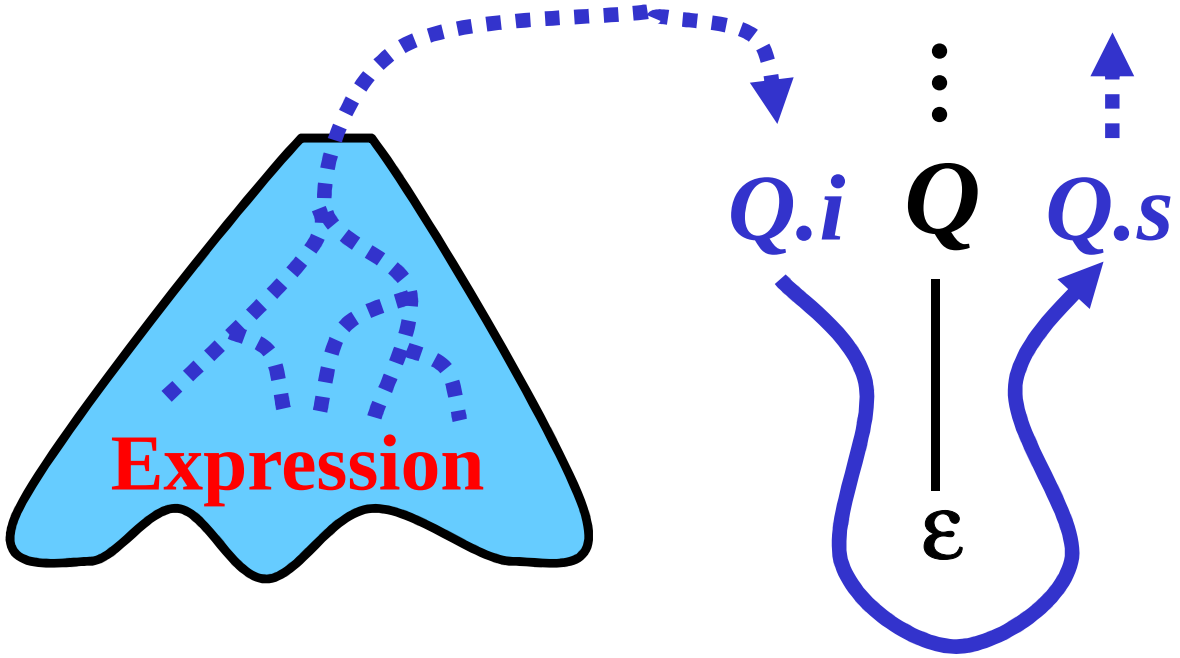
III.



$Q \rightarrow \varepsilon$ $\{Q.s := Q.i\}$

Expressions: Addition 3/4

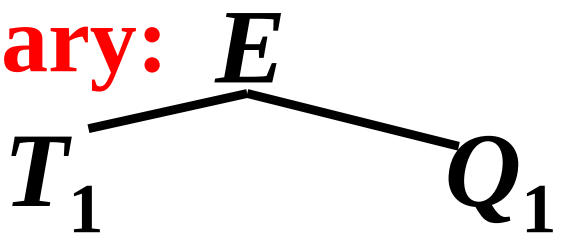
III.



$Q \rightarrow \varepsilon \quad \{Q.s := Q.i\}$

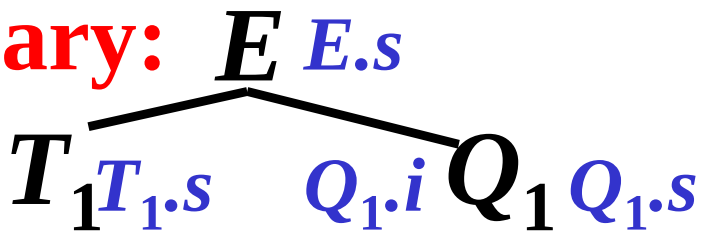
Expressions: Addition 4/4

Summary:



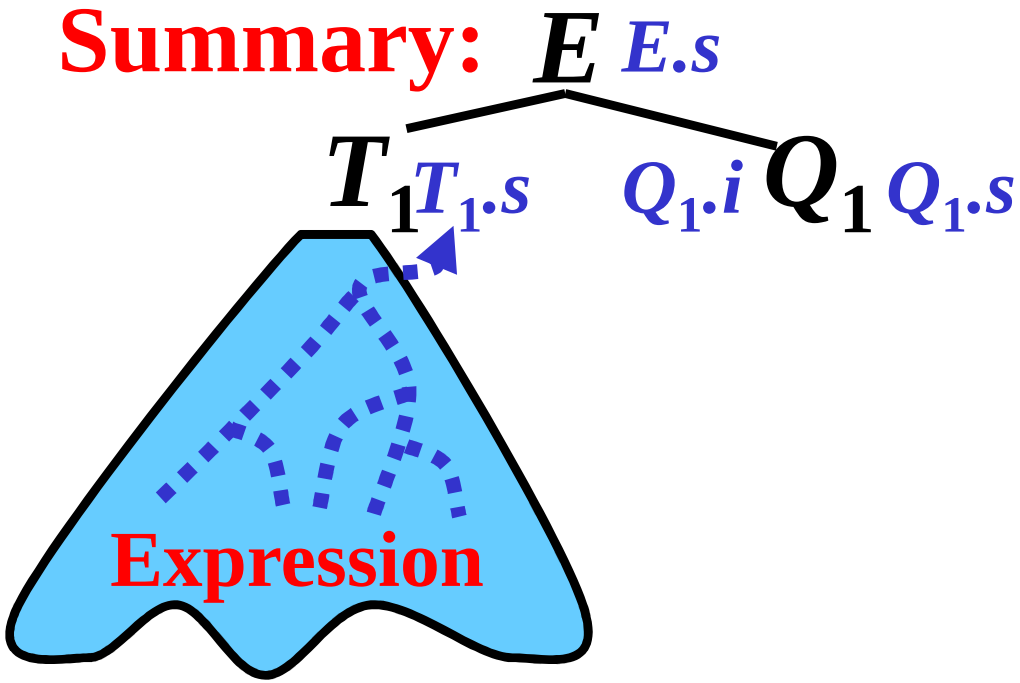
Expressions: Addition 4/4

Summary:



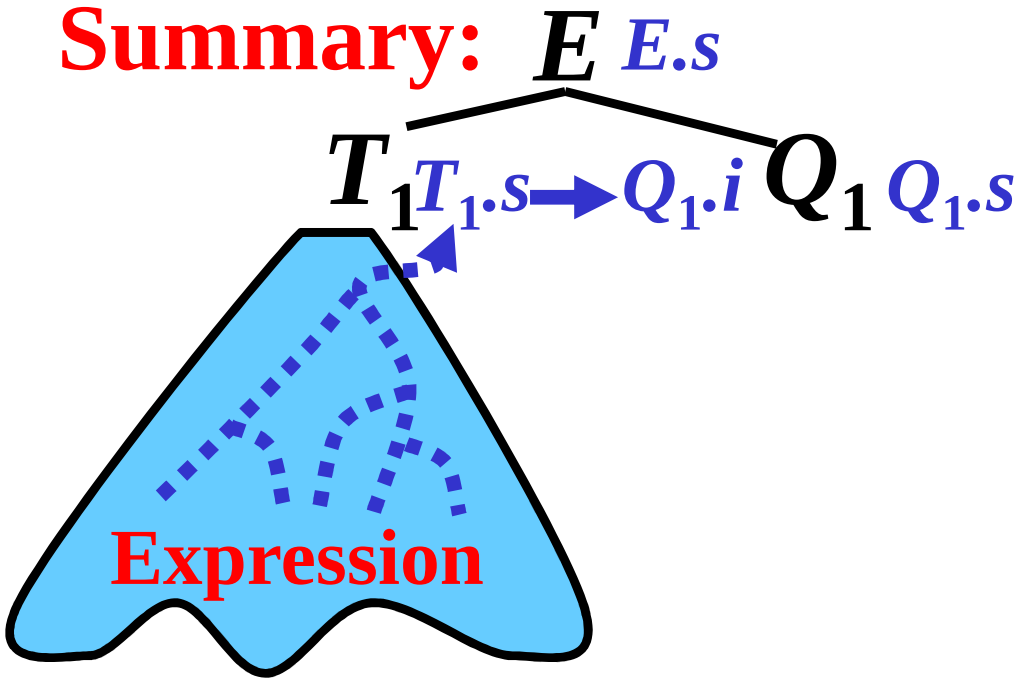
Expressions: Addition 4/4

Summary:



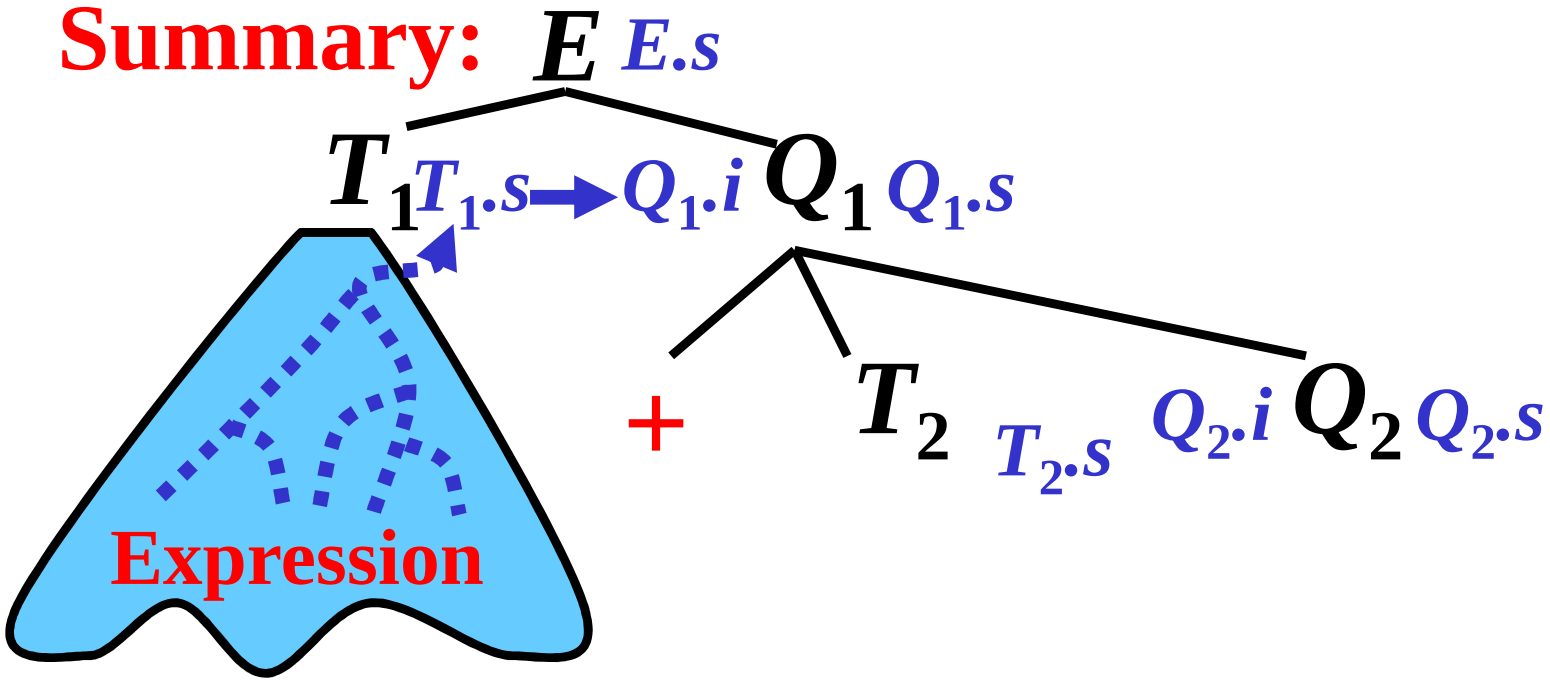
Expressions: Addition 4/4

Summary: E $E.s$



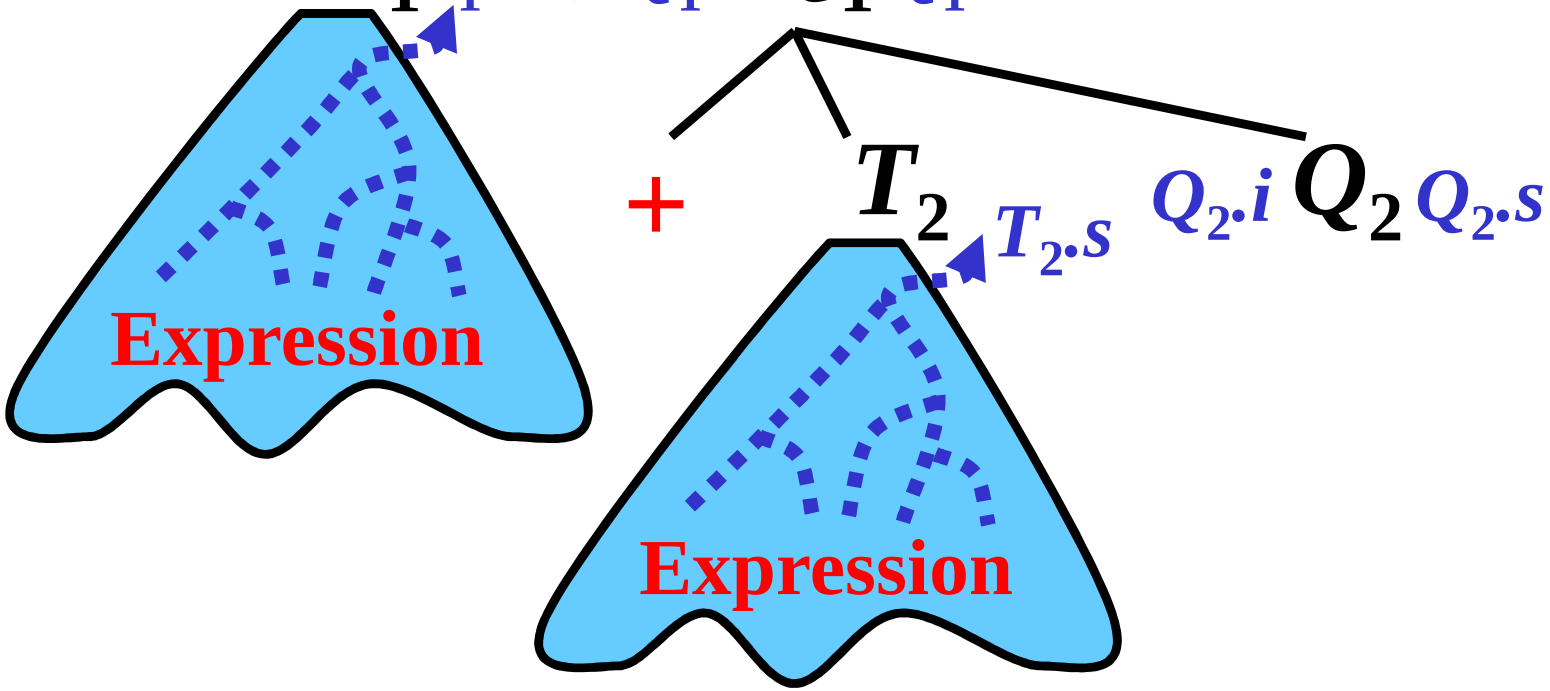
Expressions: Addition 4/4

Summary: E $E.s$



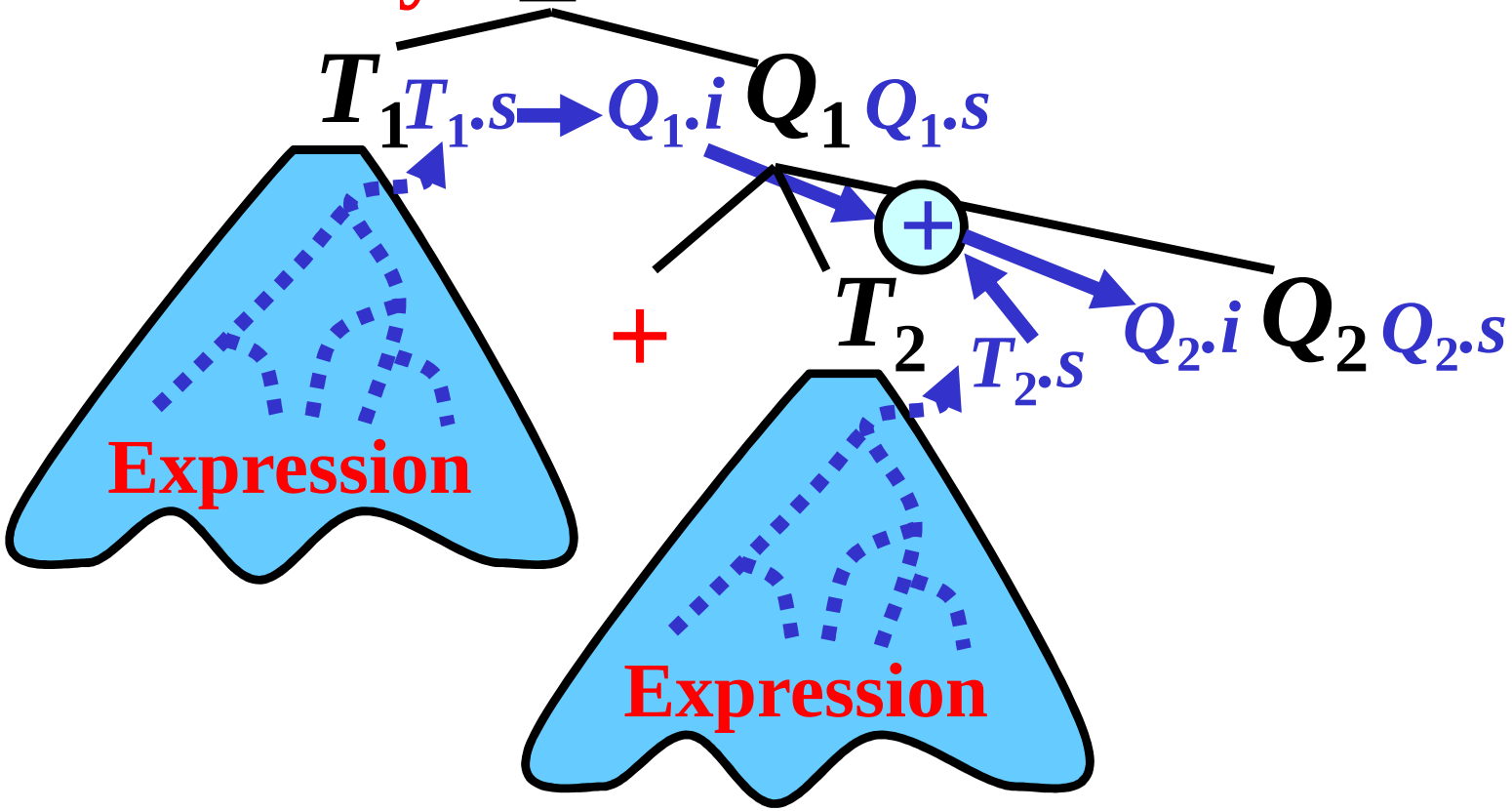
Expressions: Addition 4/4

Summary: E $E.s$



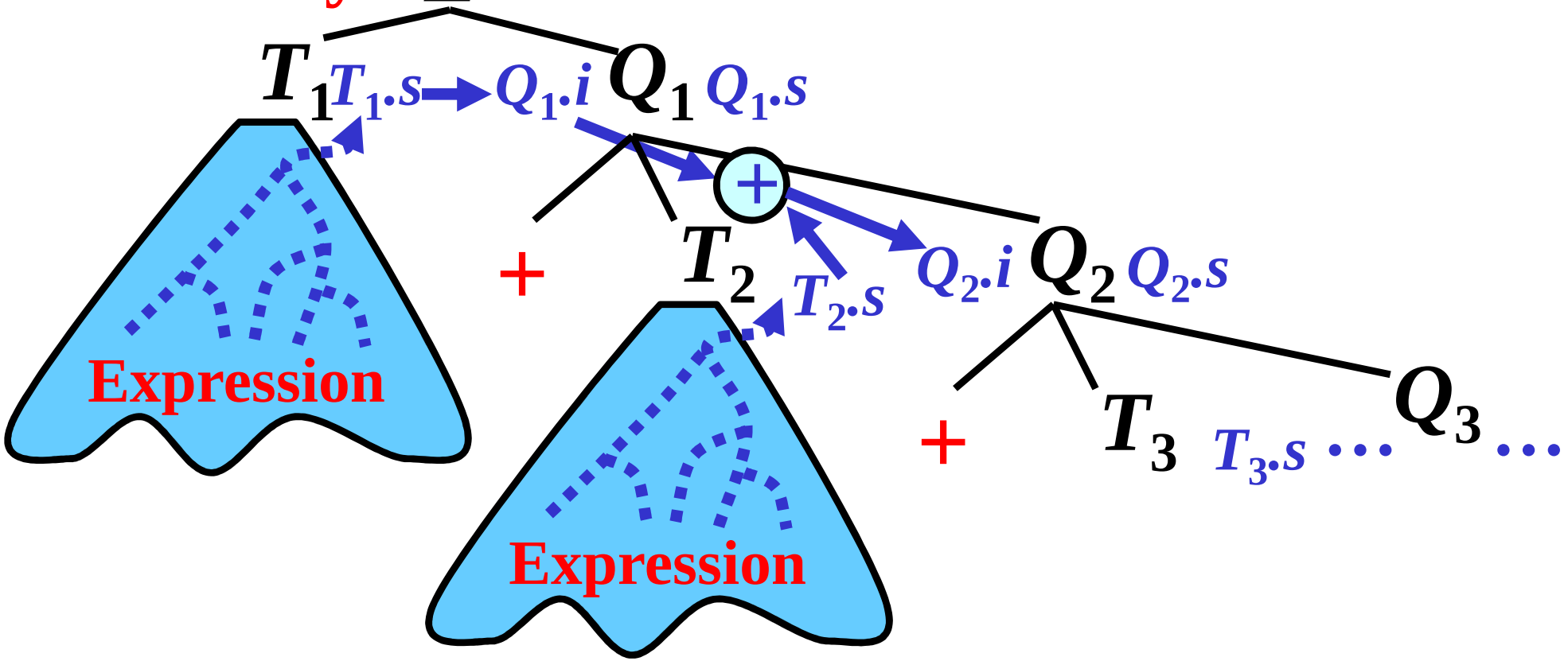
Expressions: Addition 4/4

Summary: E $E.s$



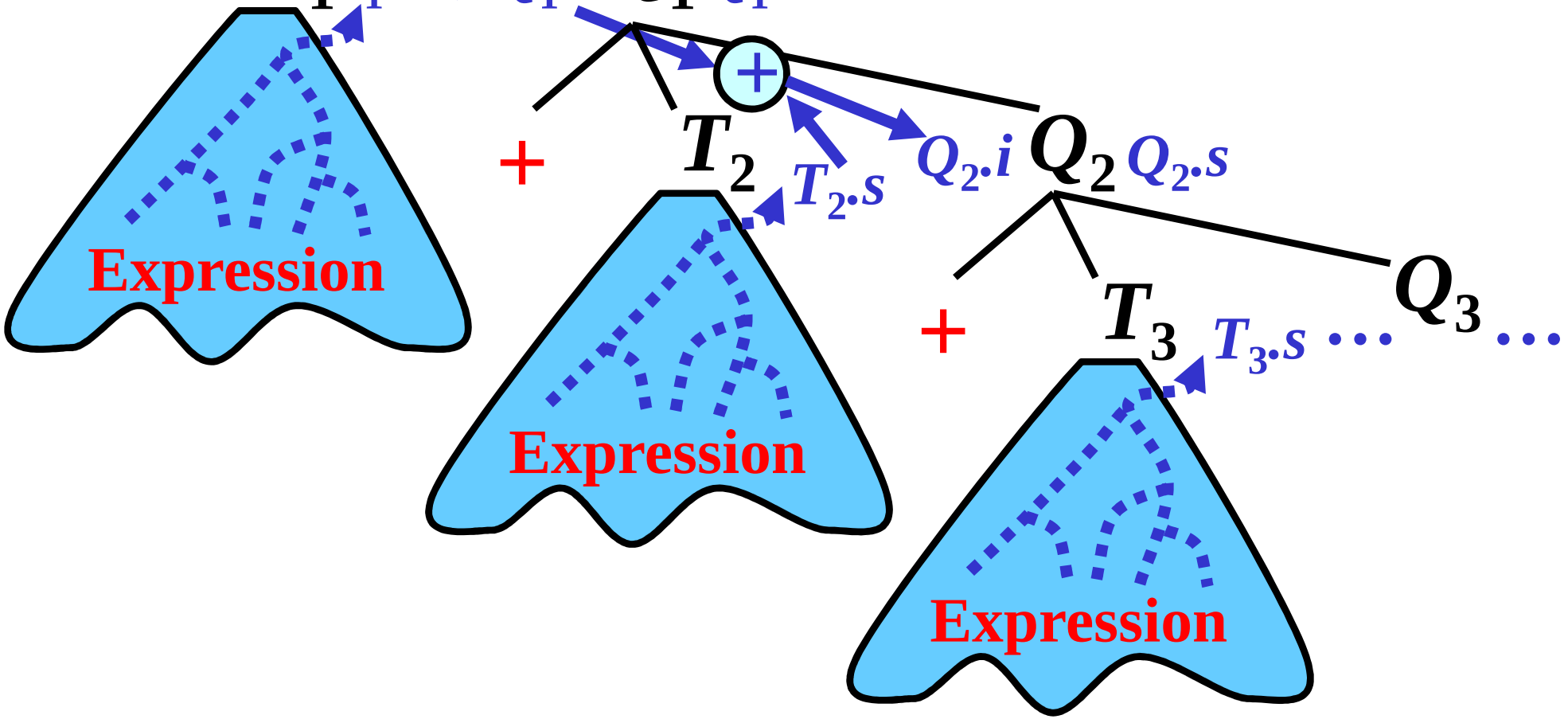
Expressions: Addition 4/4

Summary: E $E.s$



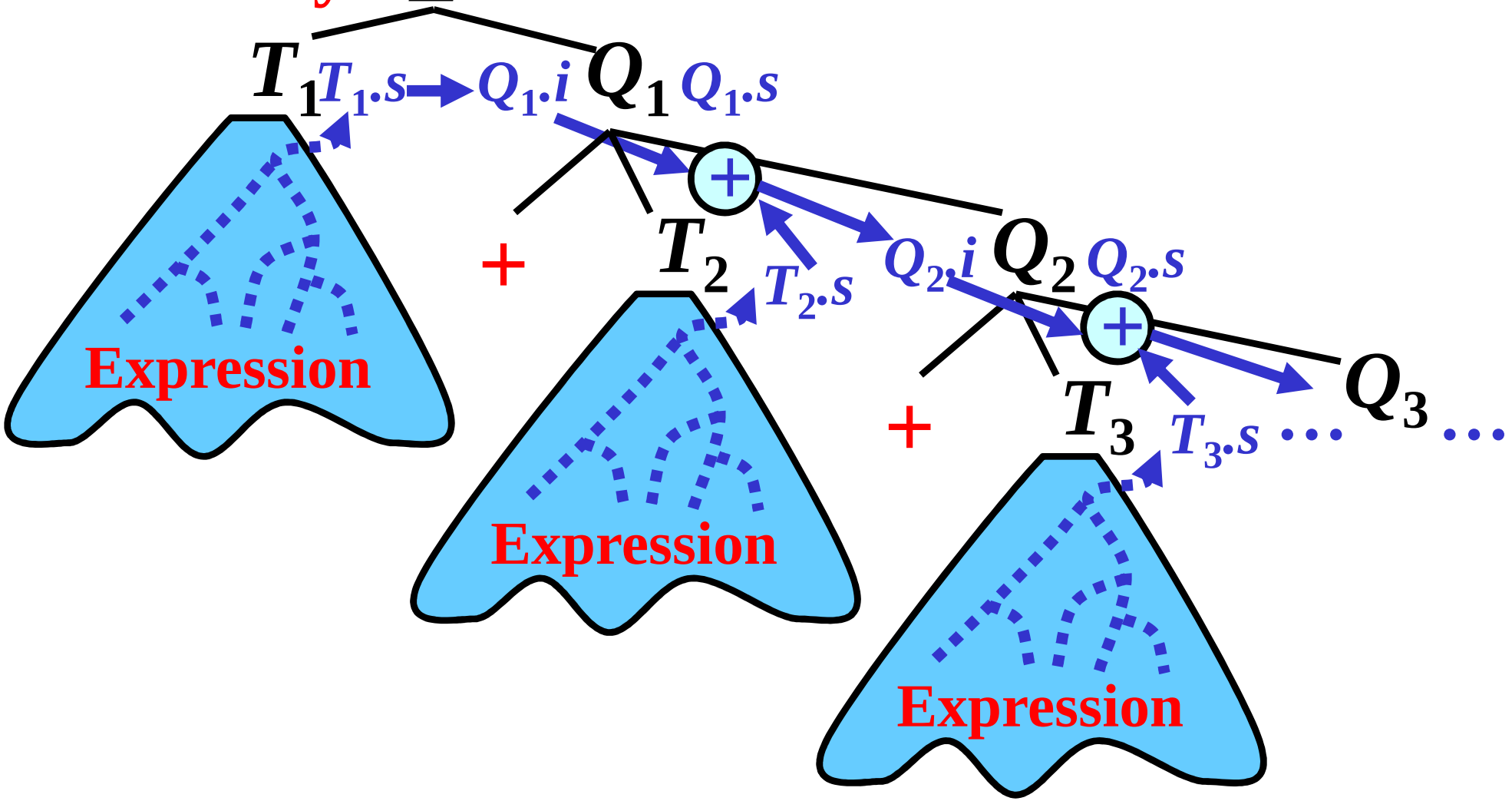
Expressions: Addition 4/4

Summary: E $E.s$

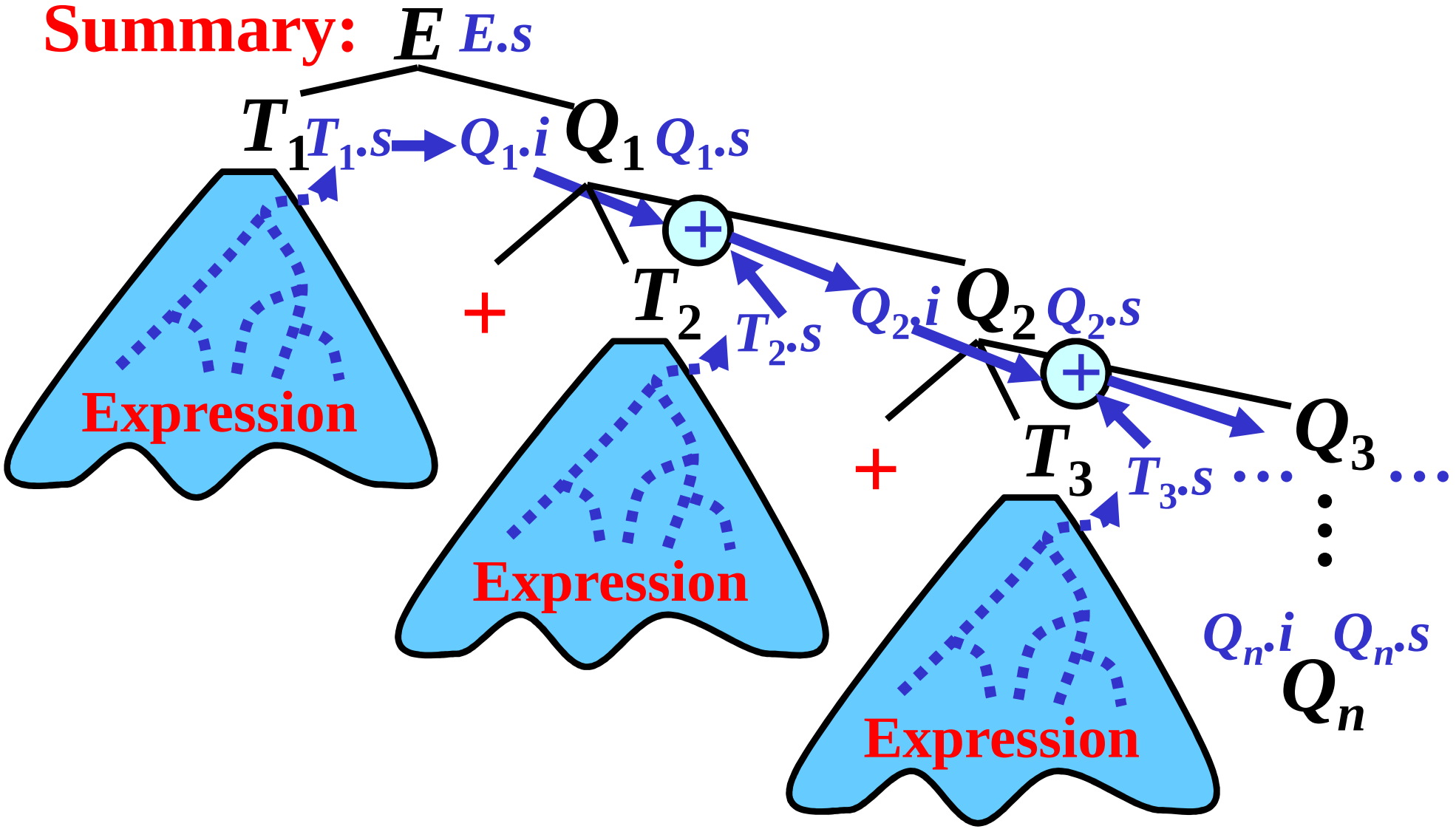


Expressions: Addition 4/4

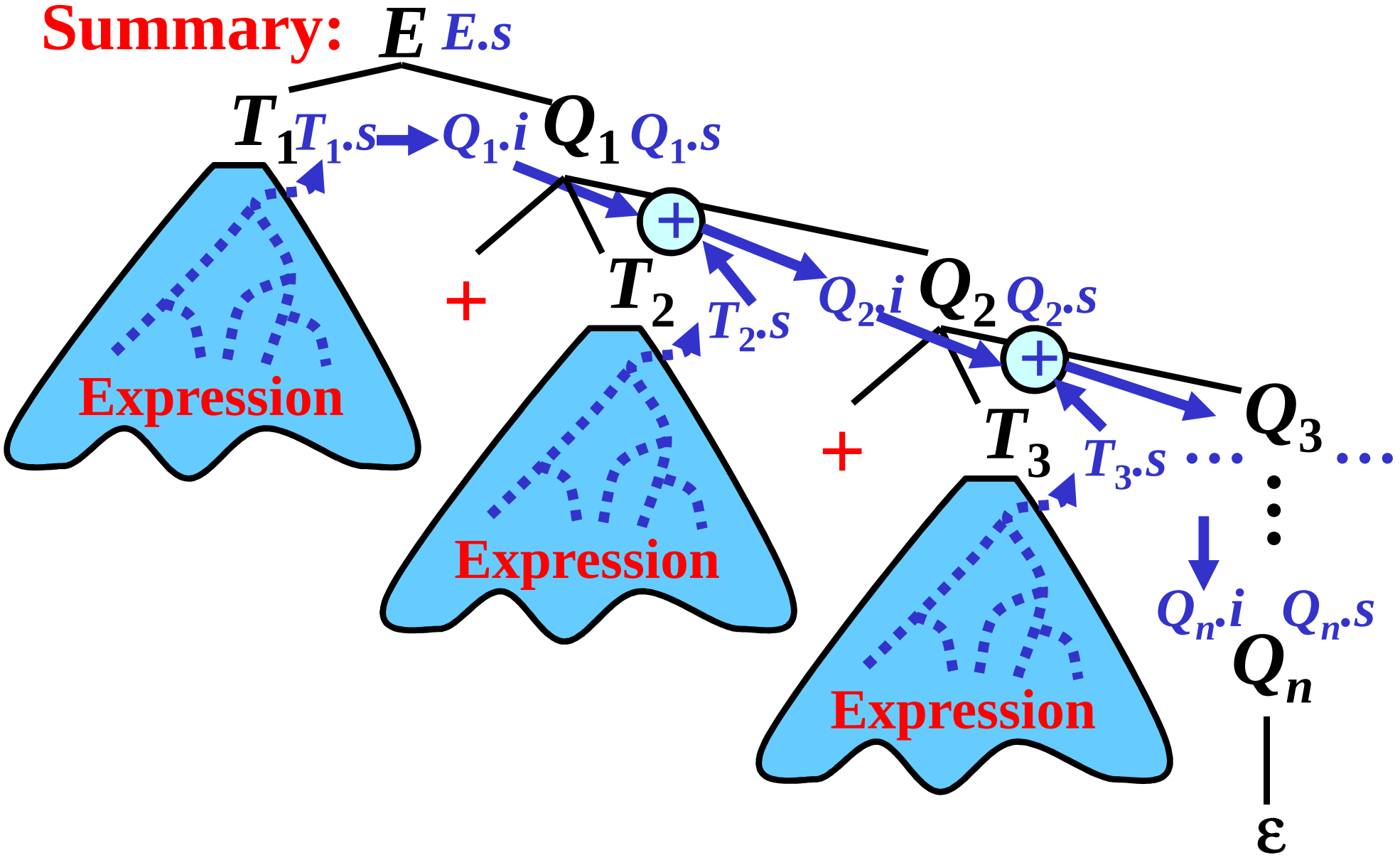
Summary: E $E.s$



Expressions: Addition 4/4

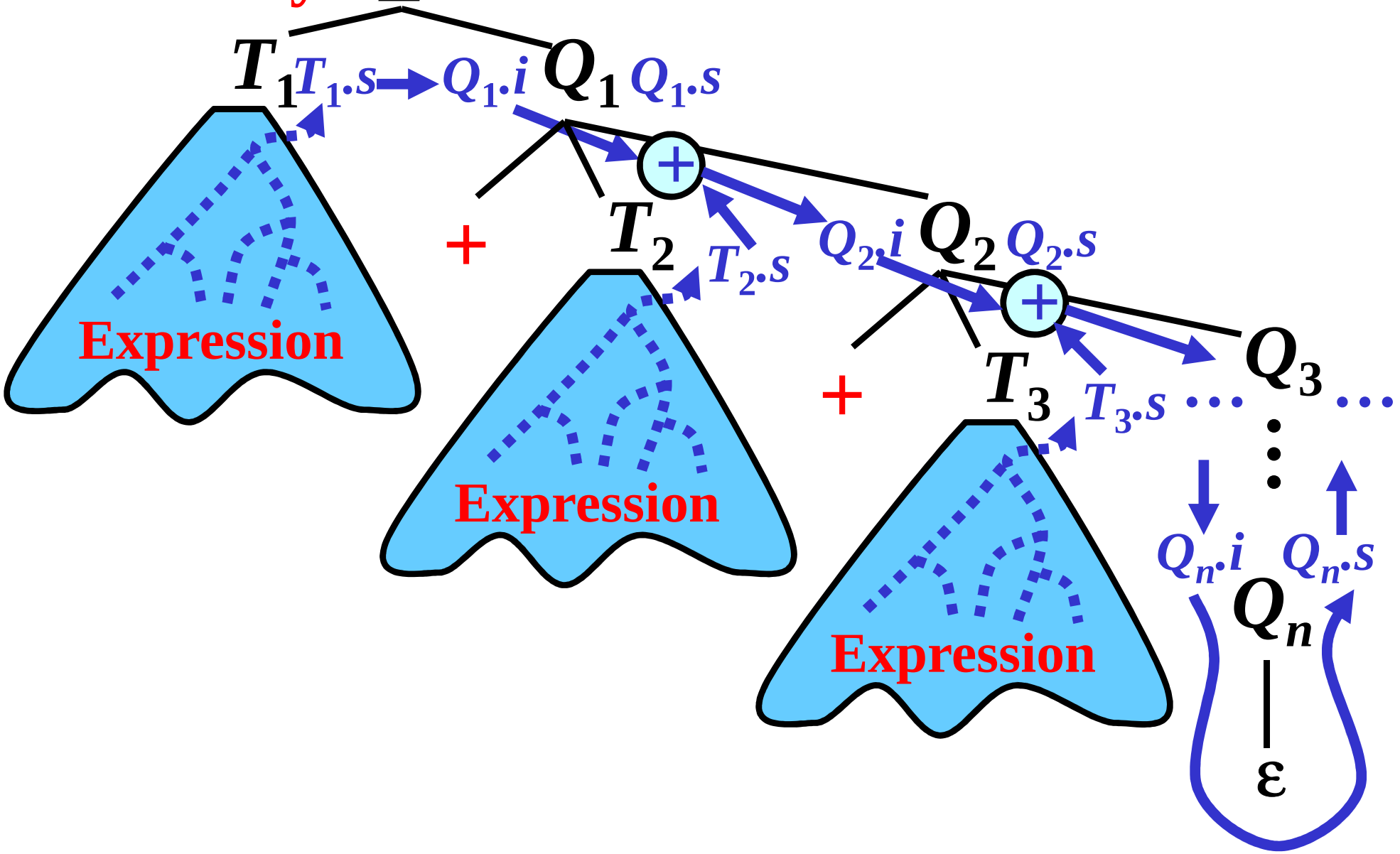


Expressions: Addition 4/4



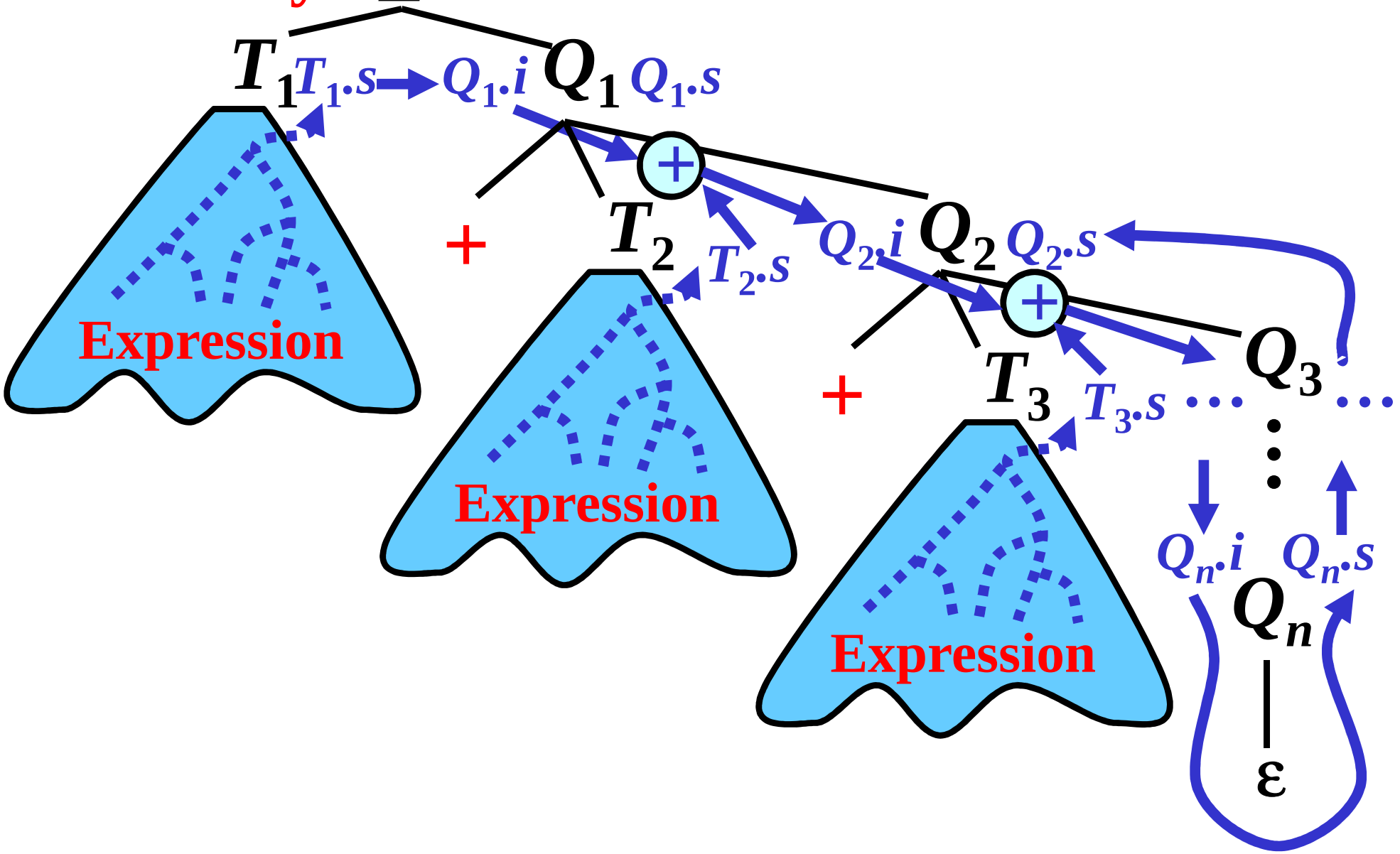
Expressions: Addition 4/4

Summary: E $E.s$



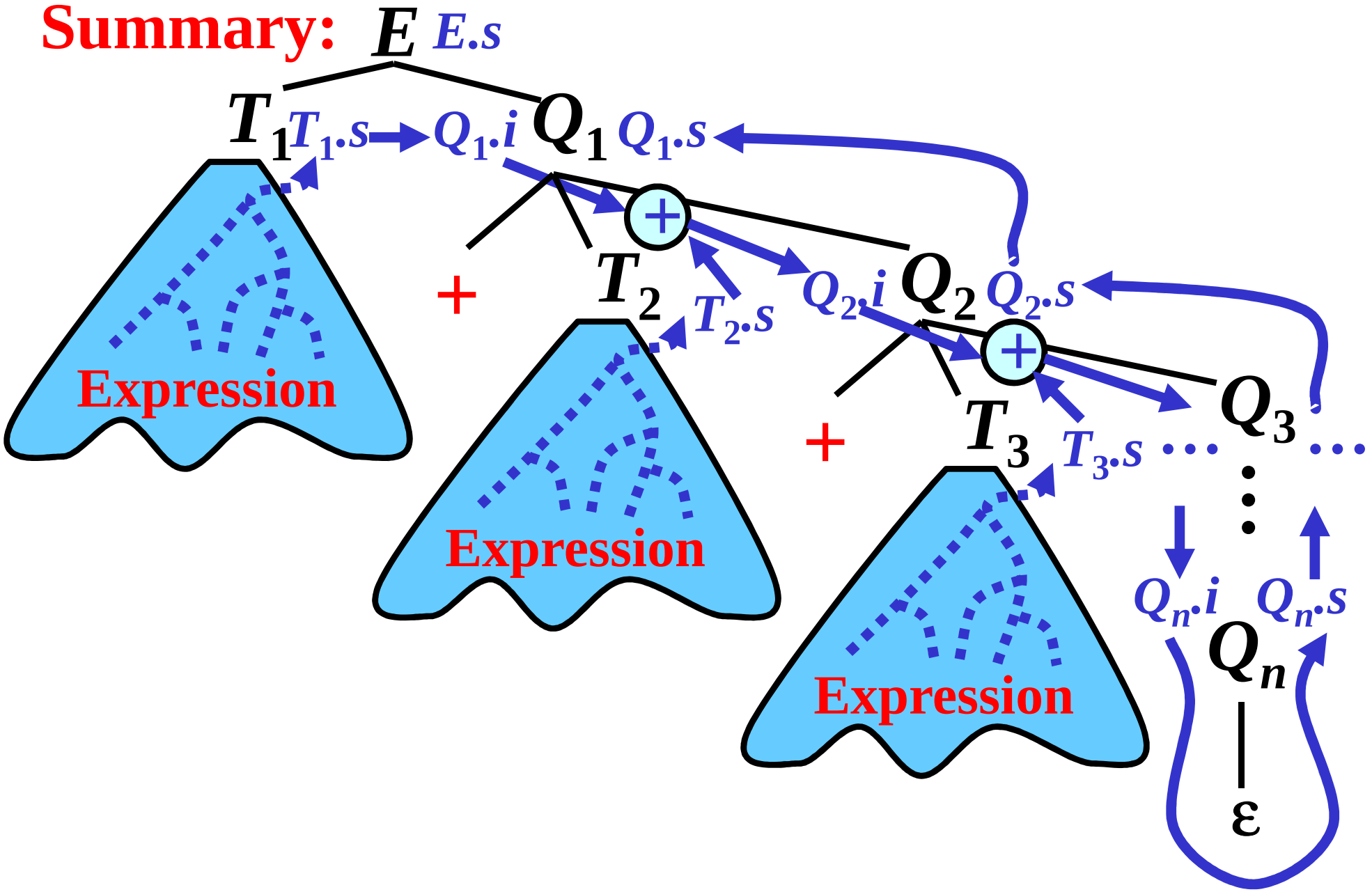
Expressions: Addition 4/4

Summary: E $E.s$



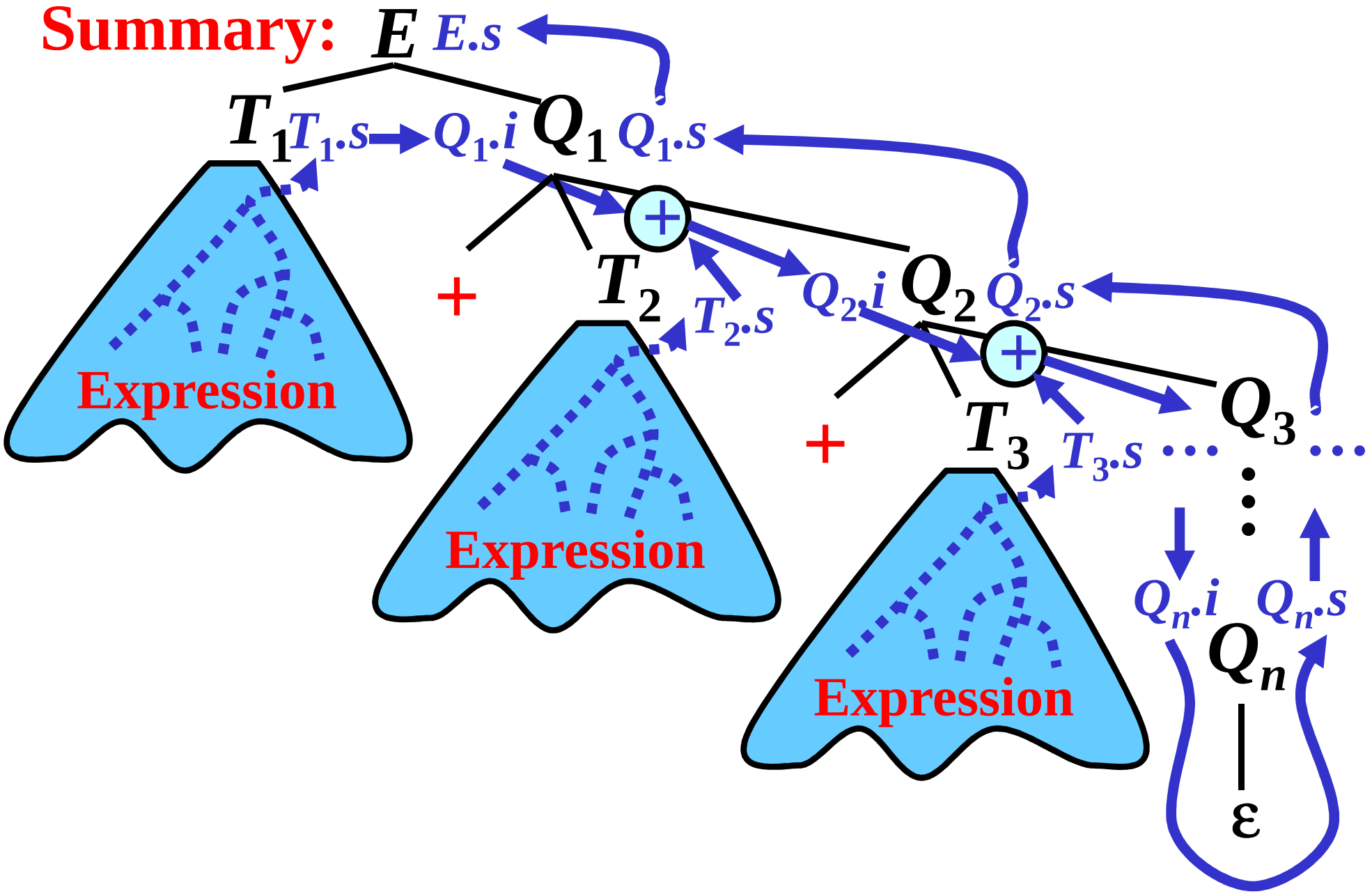
Expressions: Addition 4/4

Summary: E $E.s$



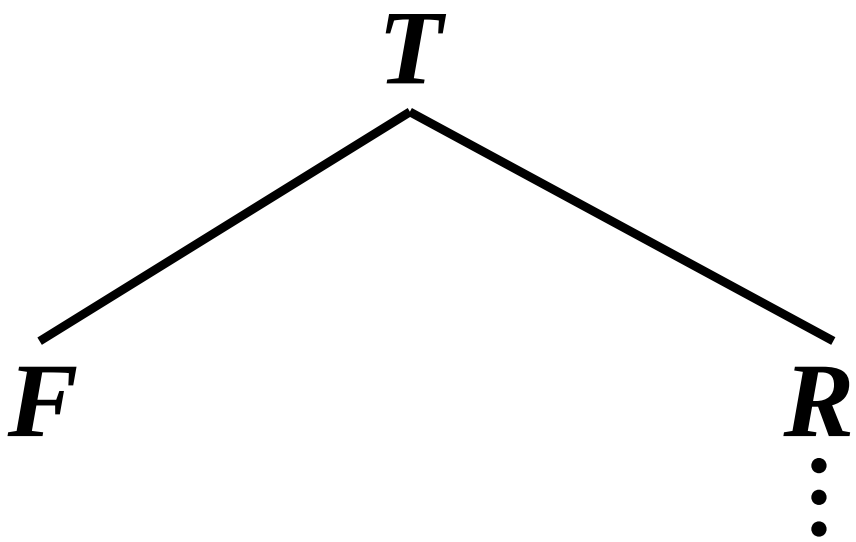
Expressions: Addition 4/4

Summary:



Expressions: Multiplication 1/4

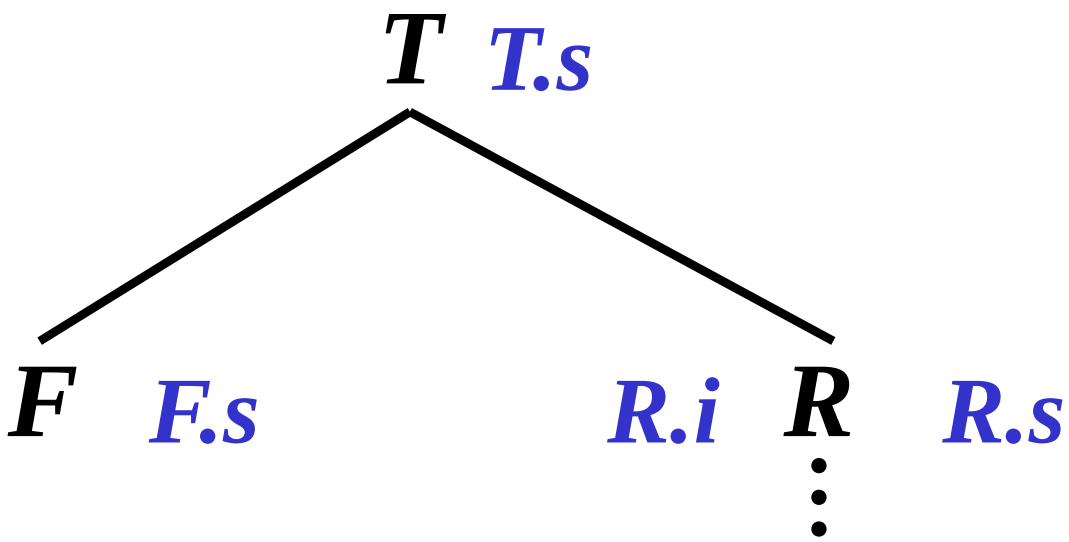
I.



$T \rightarrow F$ R

Expressions: Multiplication 1/4

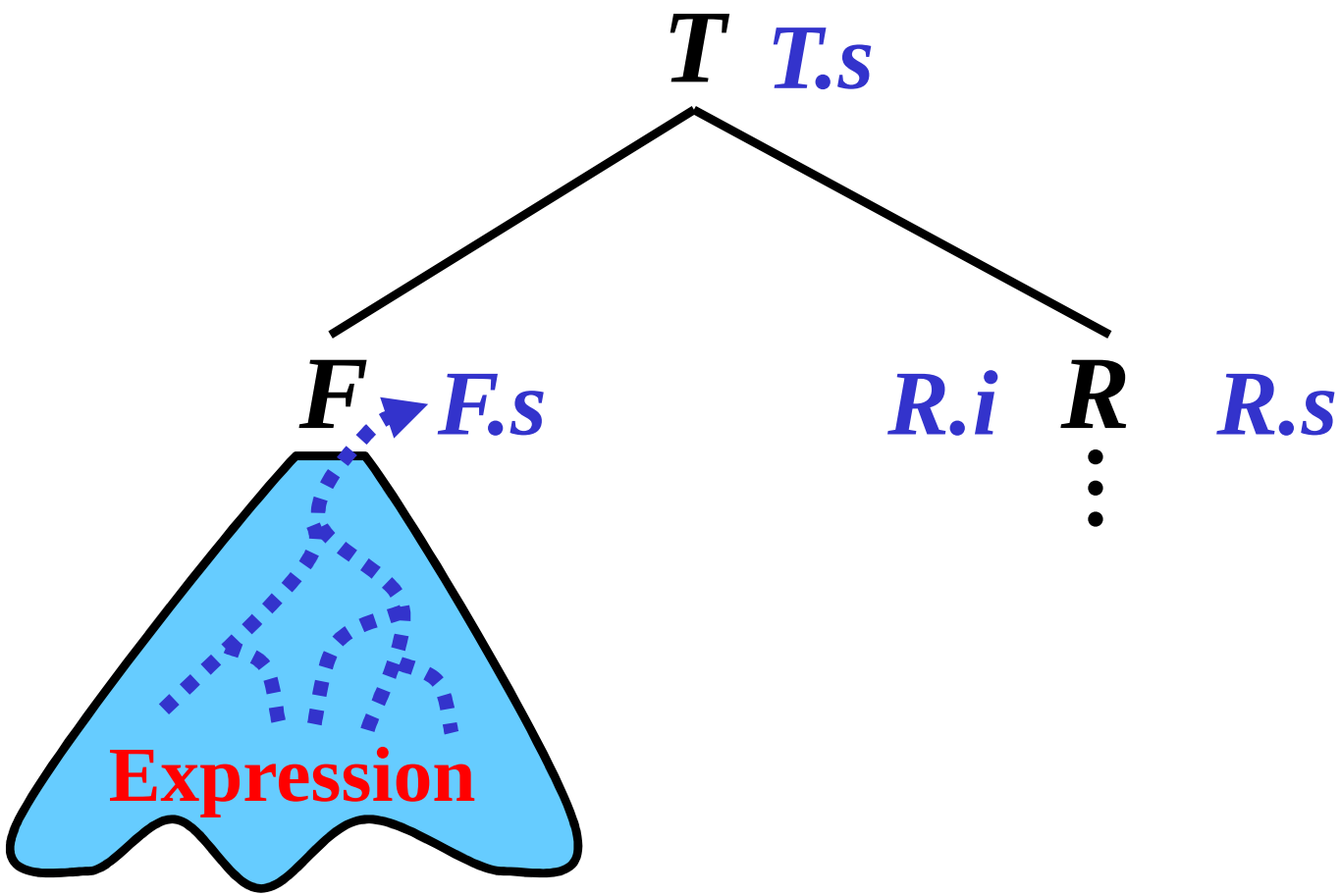
I.



$T \rightarrow F$ R

Expressions: Multiplication 1/4

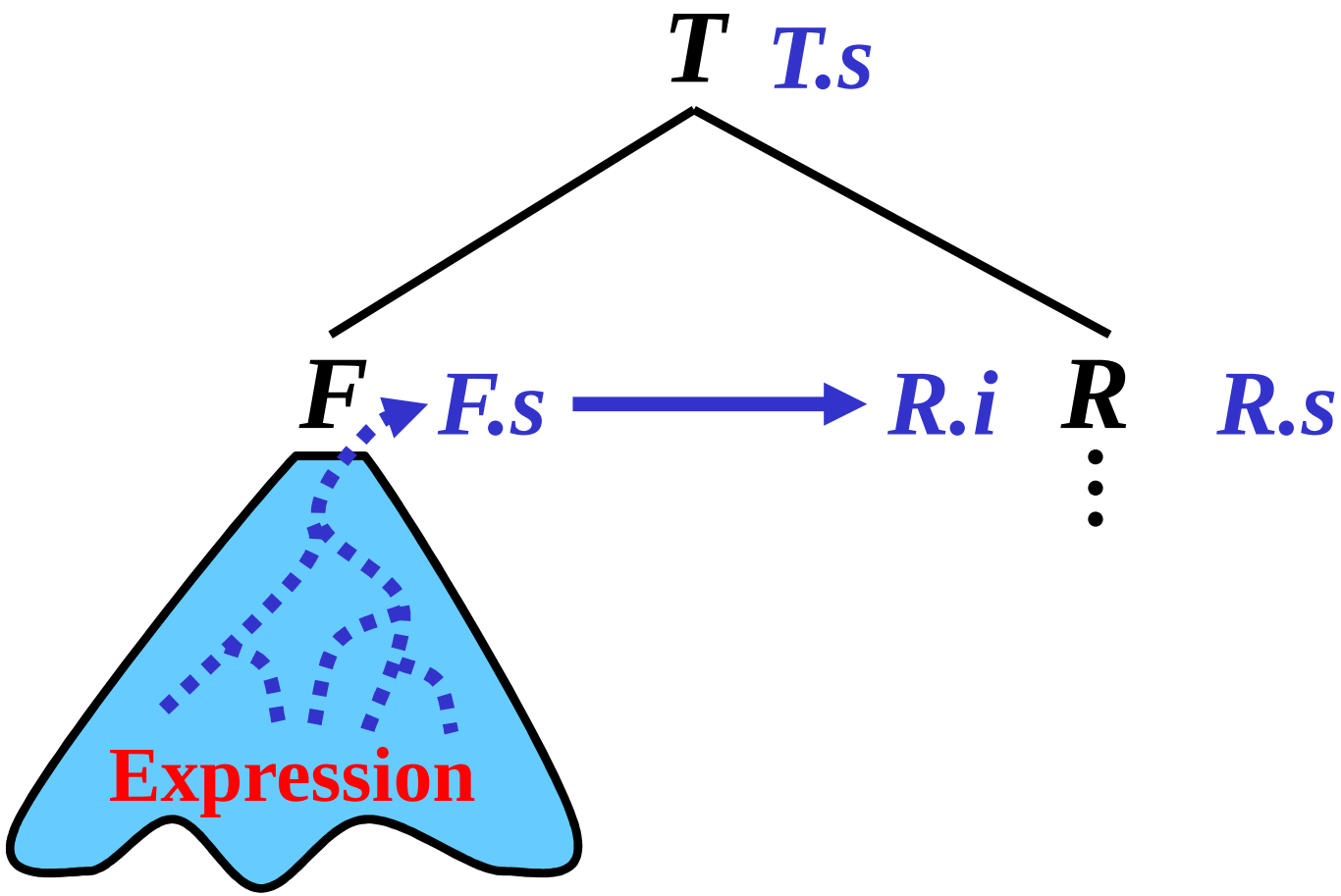
I.



$T \rightarrow F$ R

Expressions: Multiplication 1/4

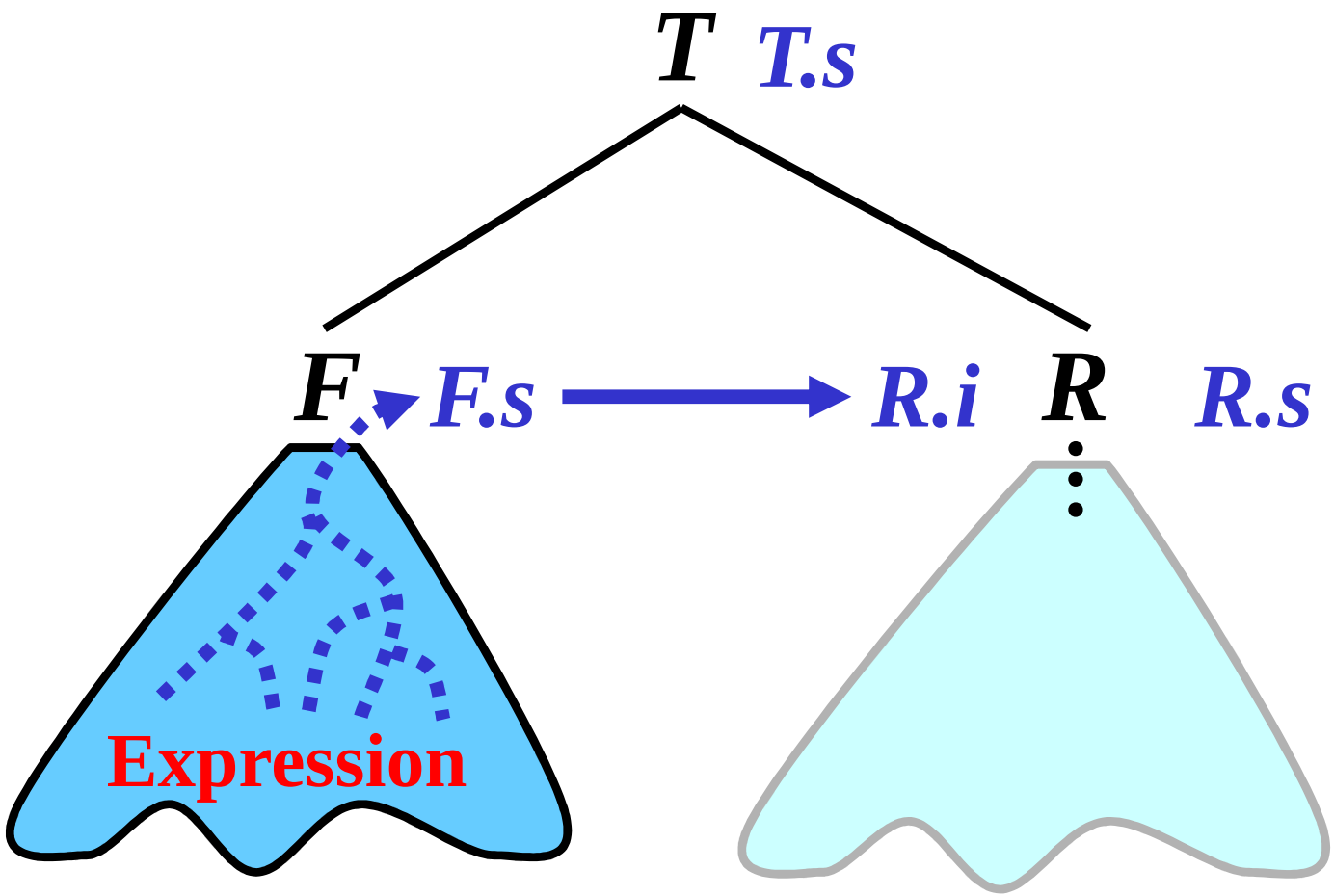
I.



$$T \rightarrow F \{ R.i := F.s \} \; R$$

Expressions: Multiplication 1/4

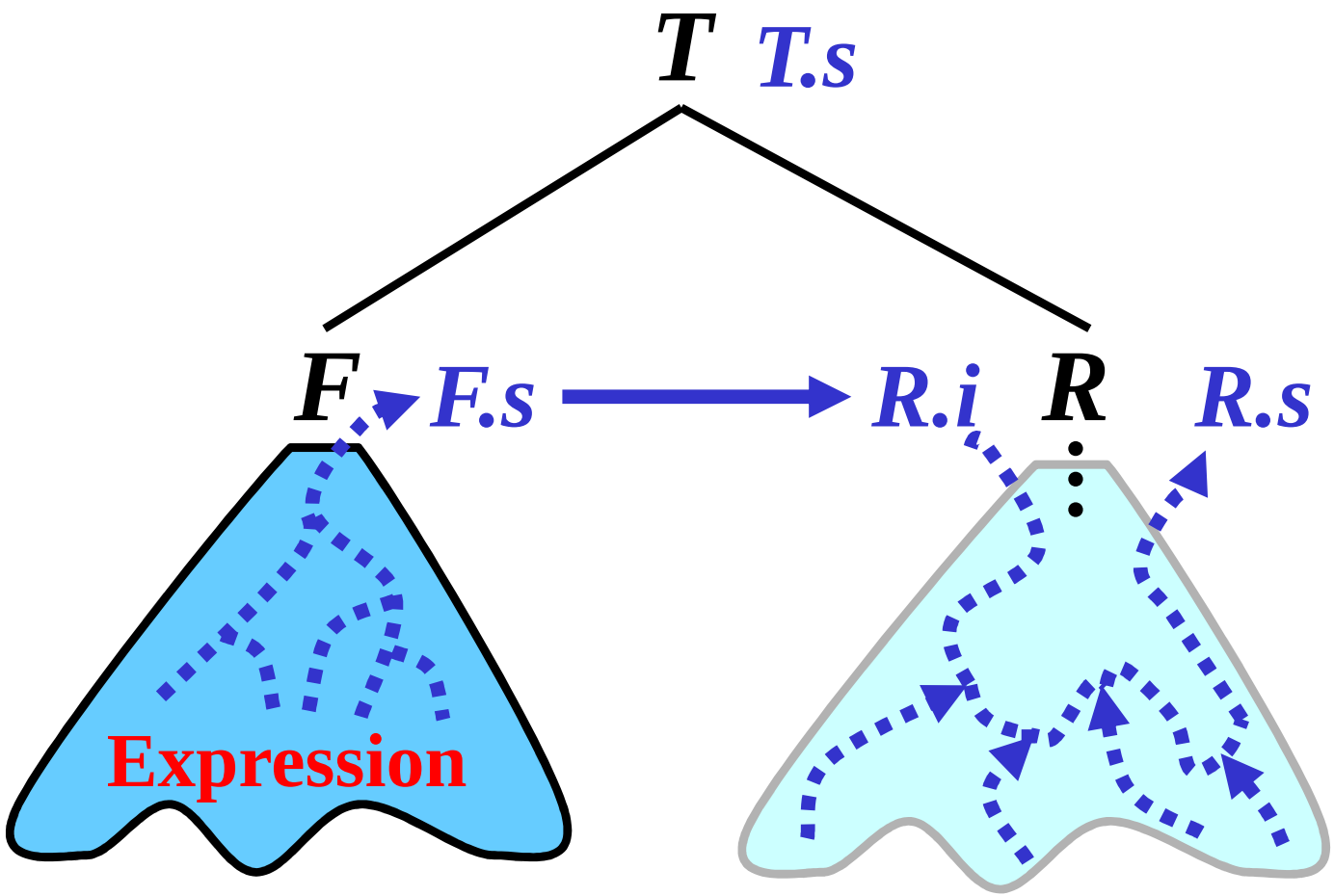
I.



$$T \rightarrow F \{ R.i := F.s \} \; R$$

Expressions: Multiplication 1/4

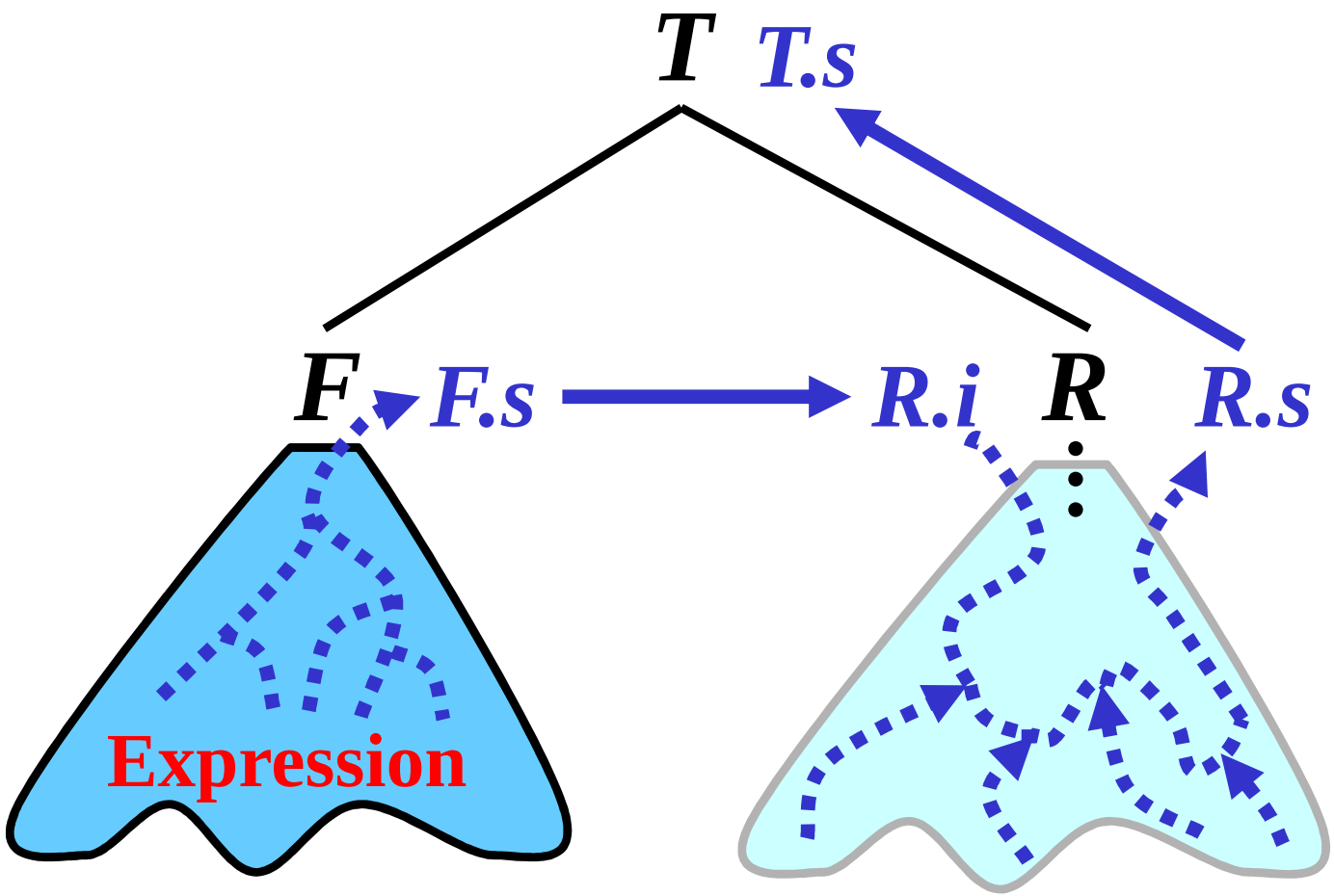
I.



$$T \rightarrow F \{ R.i := F.s \} R$$

Expressions: Multiplication 1/4

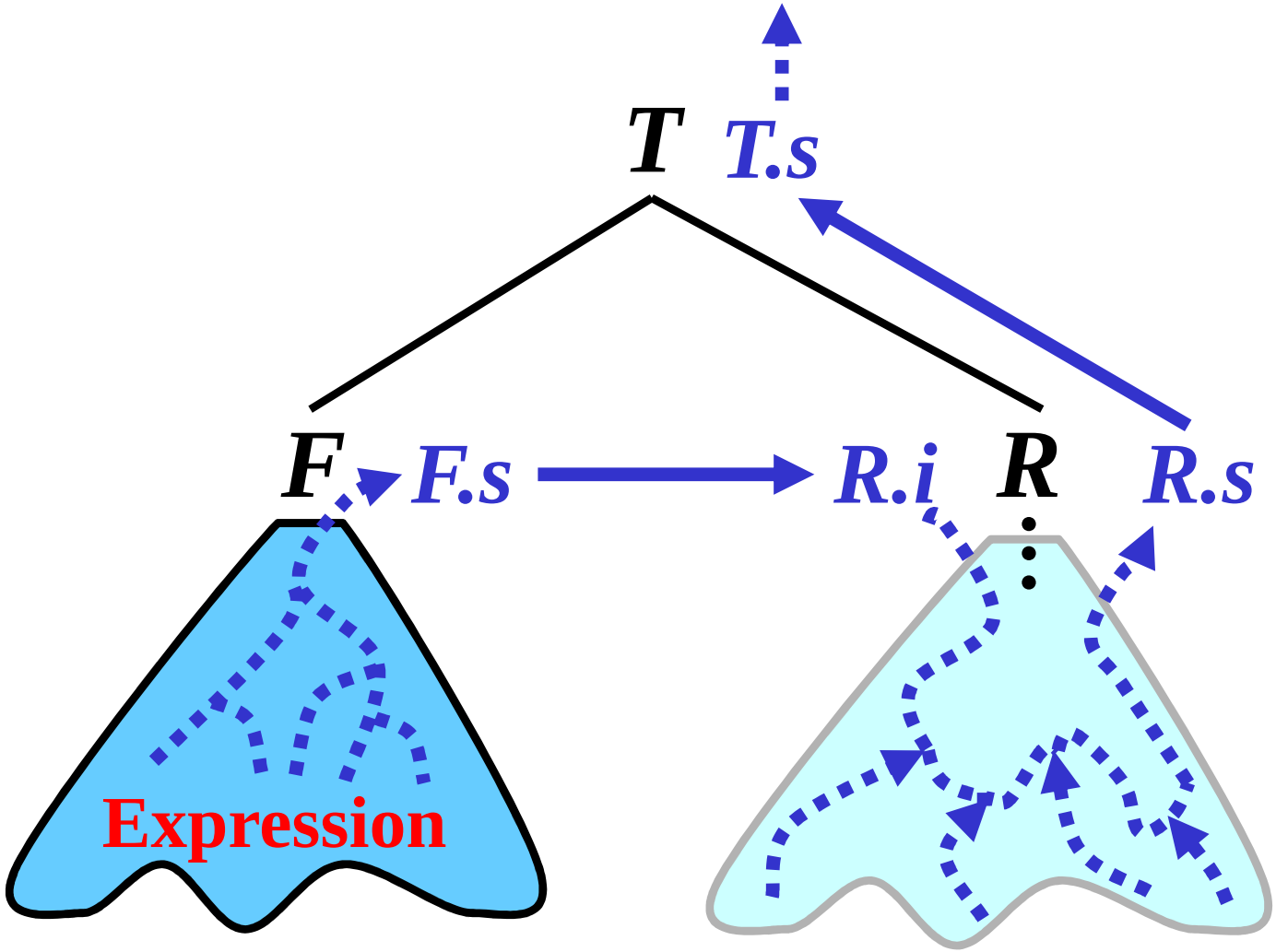
I.



$$T \rightarrow F \{ R.i := F.s \} \; R \{ T.s := R.s \}$$

Expressions: Multiplication 1/4

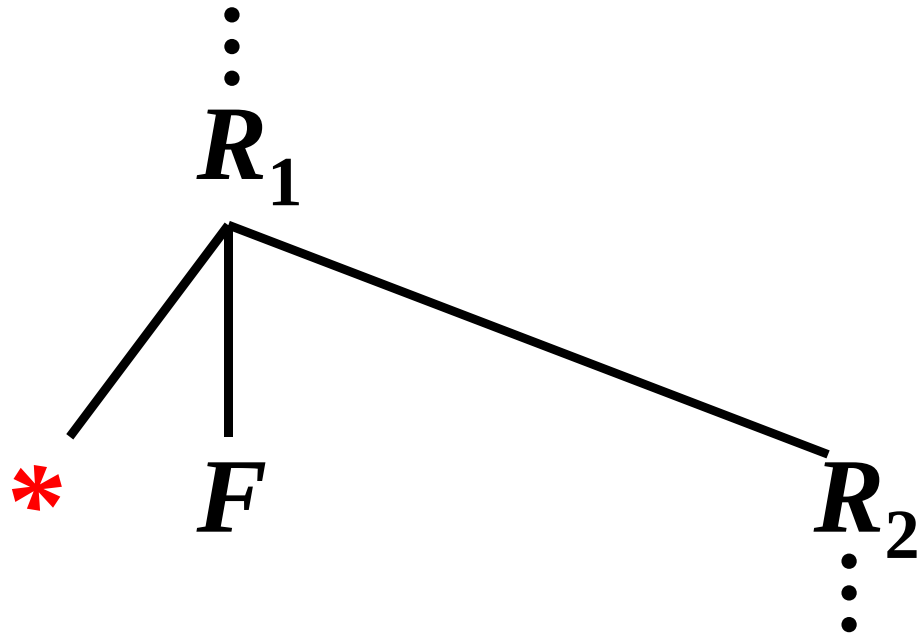
I.



$$T \rightarrow F \{ R.i := F.s \} \; R \{ T.s := R.s \}$$

Expressions: Multiplication 2/4

II.

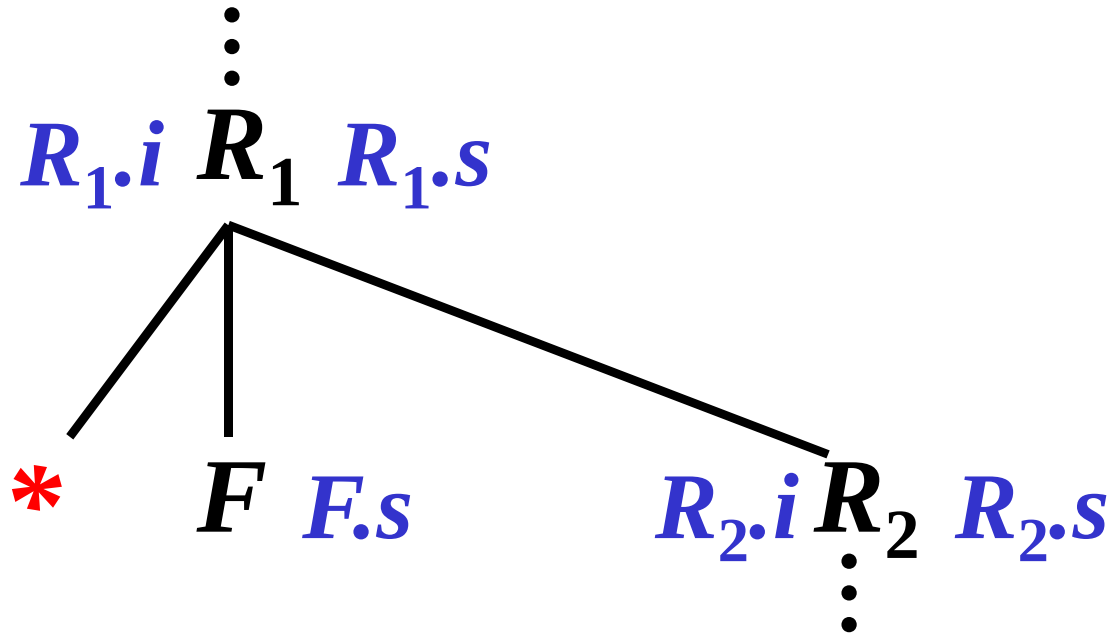


$R_1 \rightarrow {*}F$

Q_2

Expressions: Multiplication 2/4

II.

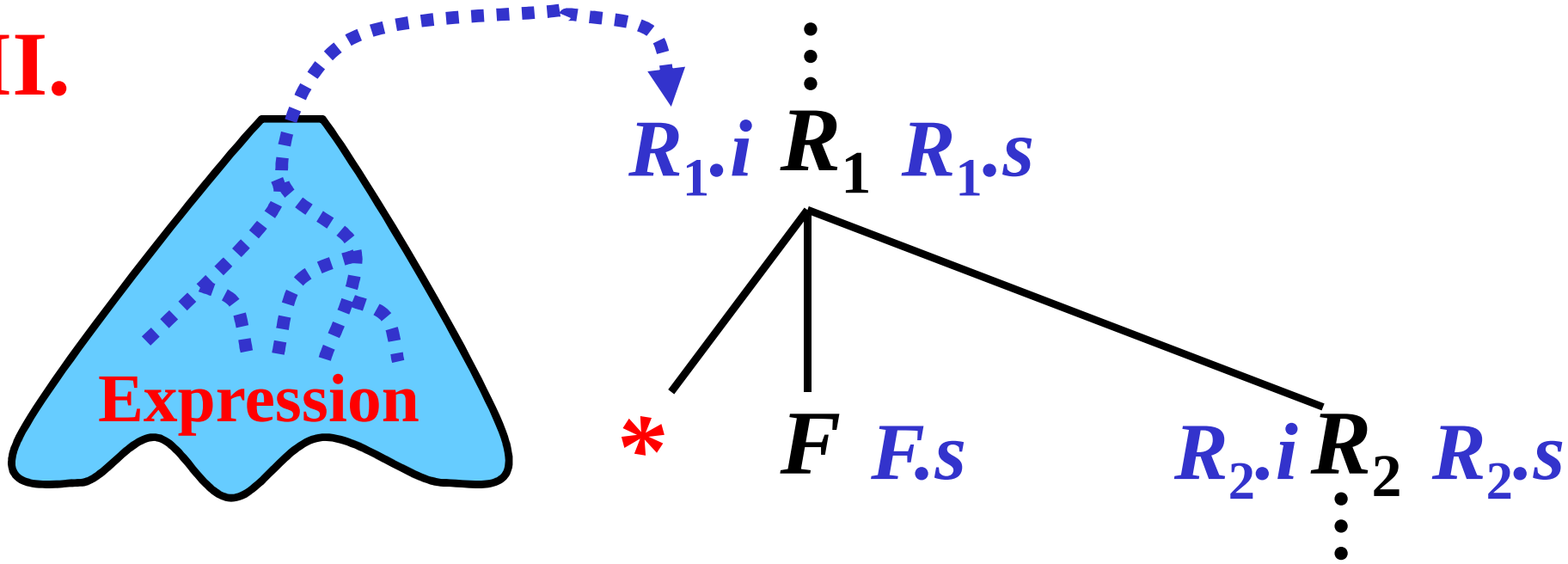


$R_1 \rightarrow {*}F$

Q_2

Expressions: Multiplication 2/4

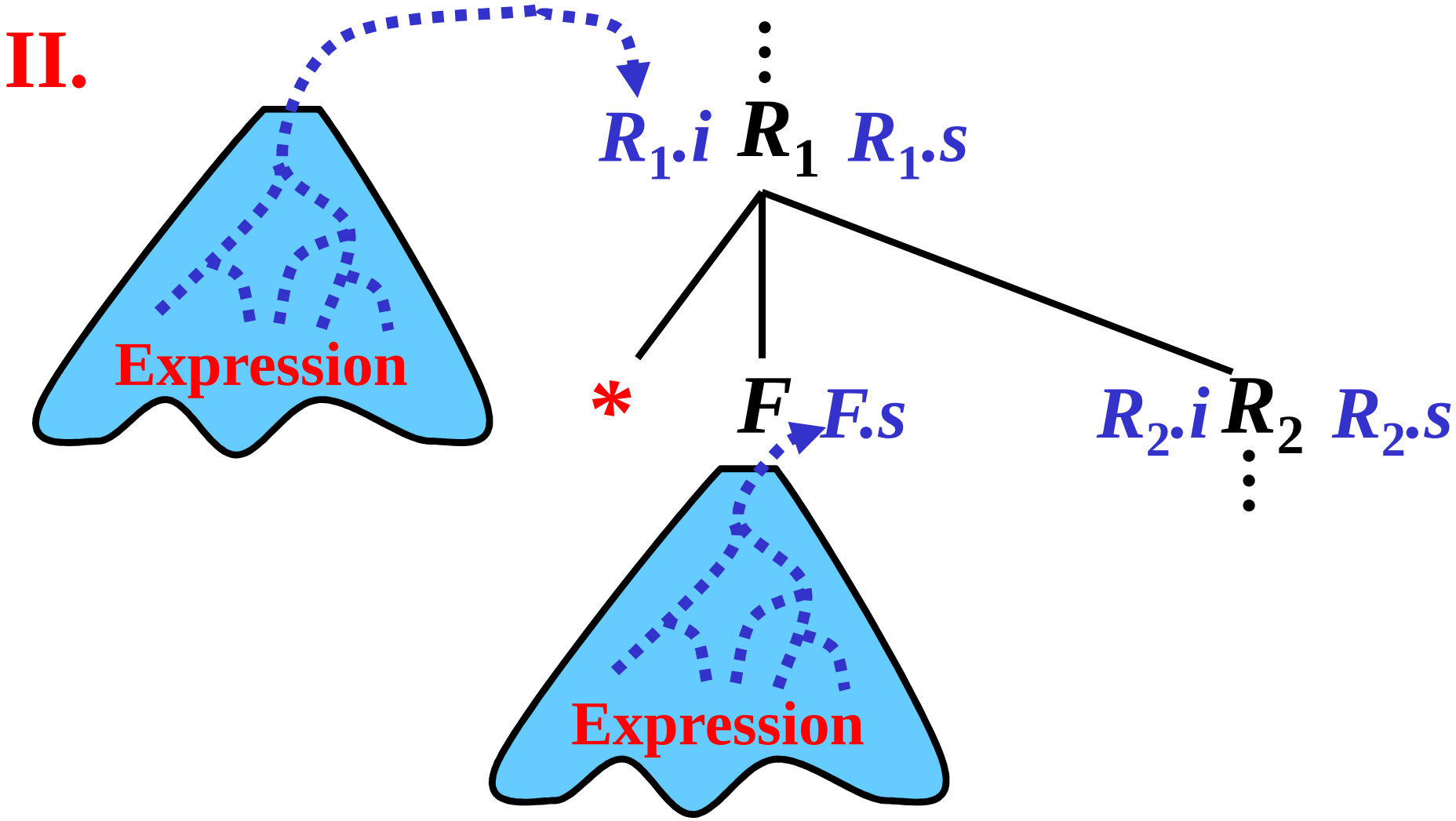
II.



$R_1 \rightarrow {*}F$

Q_2

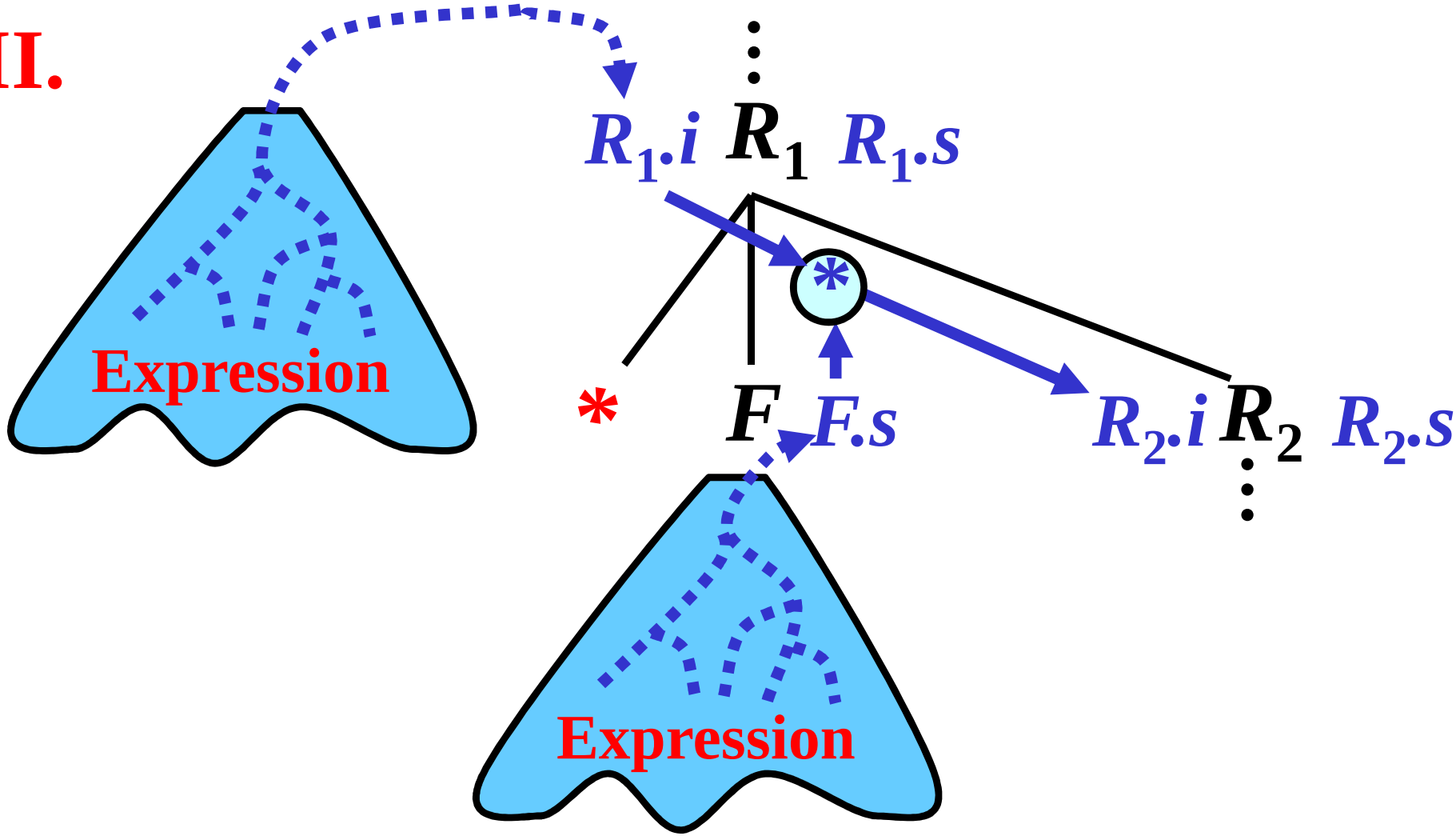
Expressions: Multiplication 2/4



$R_1 \rightarrow {*}F$ Q_2

Expressions: Multiplication 2/4

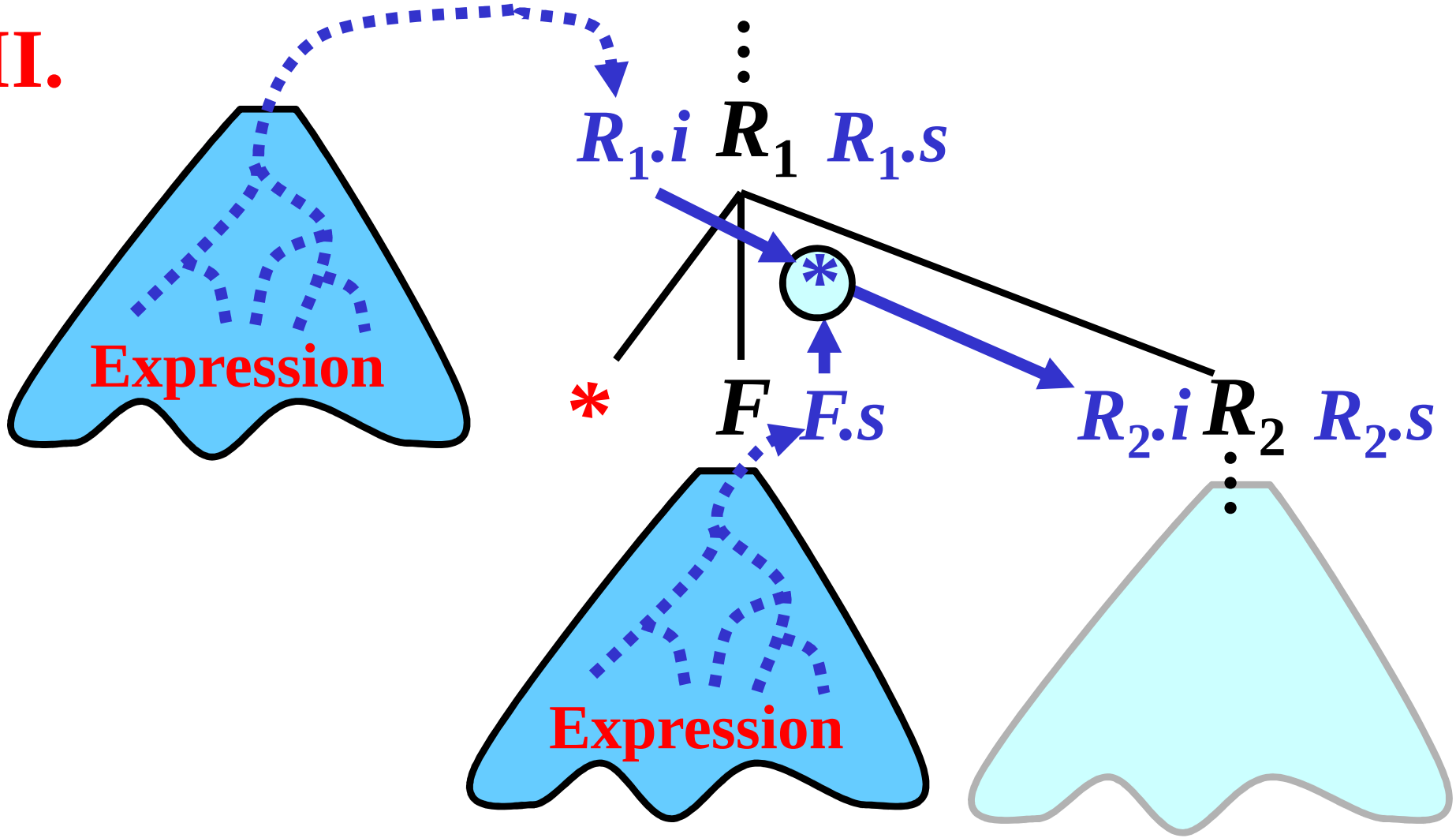
II.



$$R_1 \rightarrow {*}F \ \{ \ R_2.i := R_1.i * F.s \ \} \ Q_2$$

Expressions: Multiplication 2/4

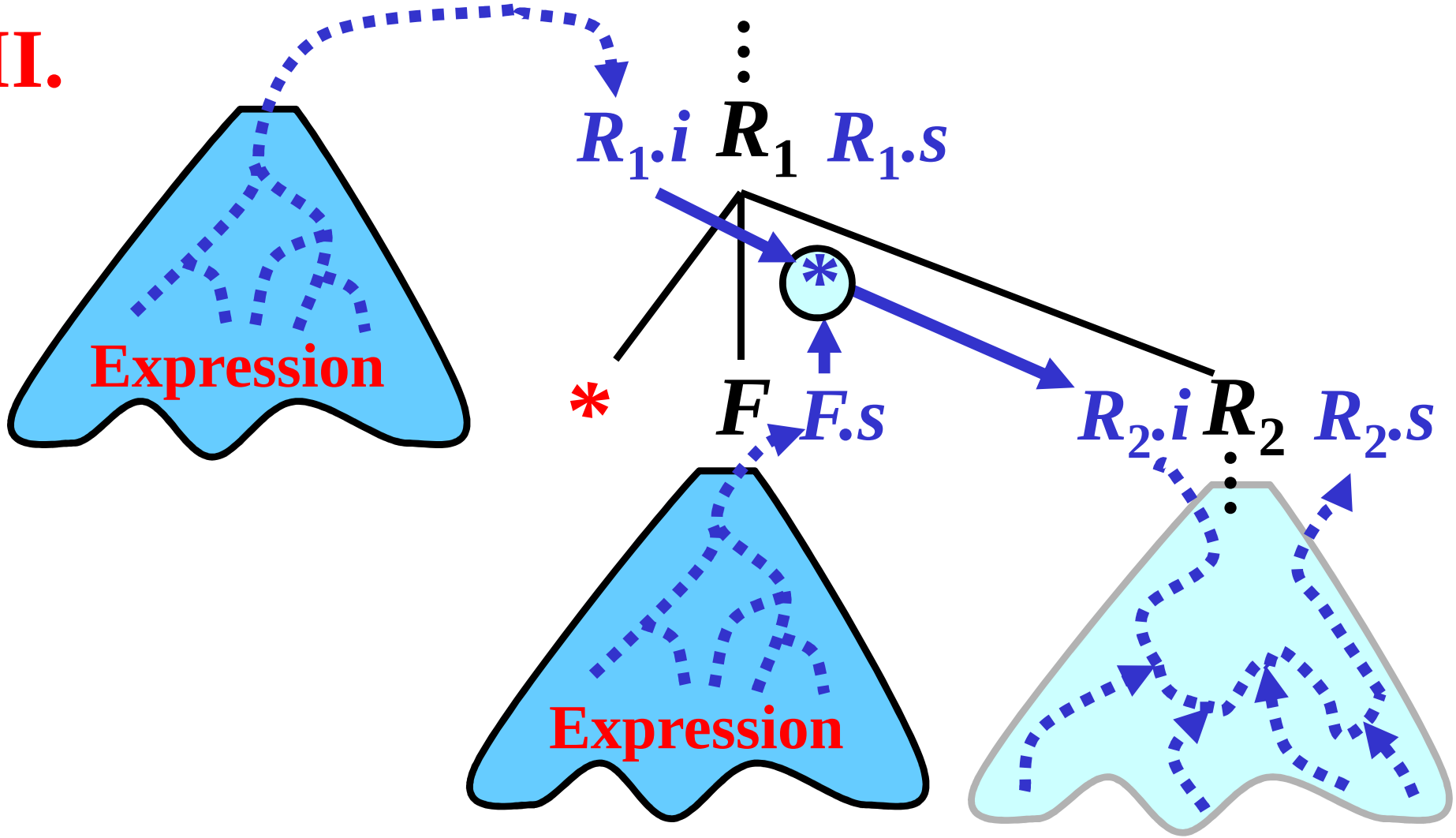
II.



$$R_1 \rightarrow {*}F \ \{ \ R_2.i := R_1.i * F.s \ \} \ Q_2$$

Expressions: Multiplication 2/4

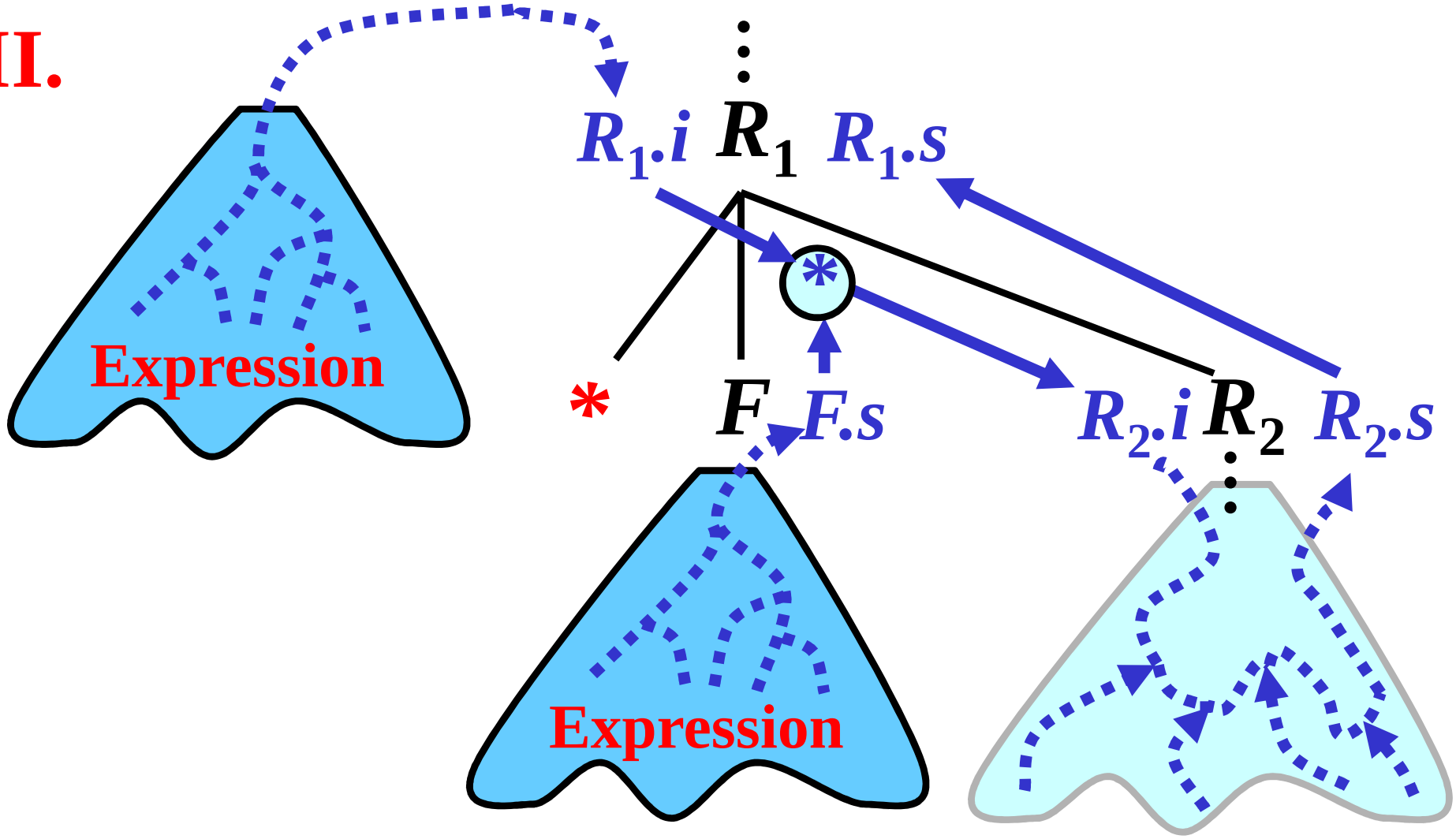
II.



$$R_1 \rightarrow {*}F \ \{ \ R_2.i := R_1.i * F.s \ \} \ Q_2$$

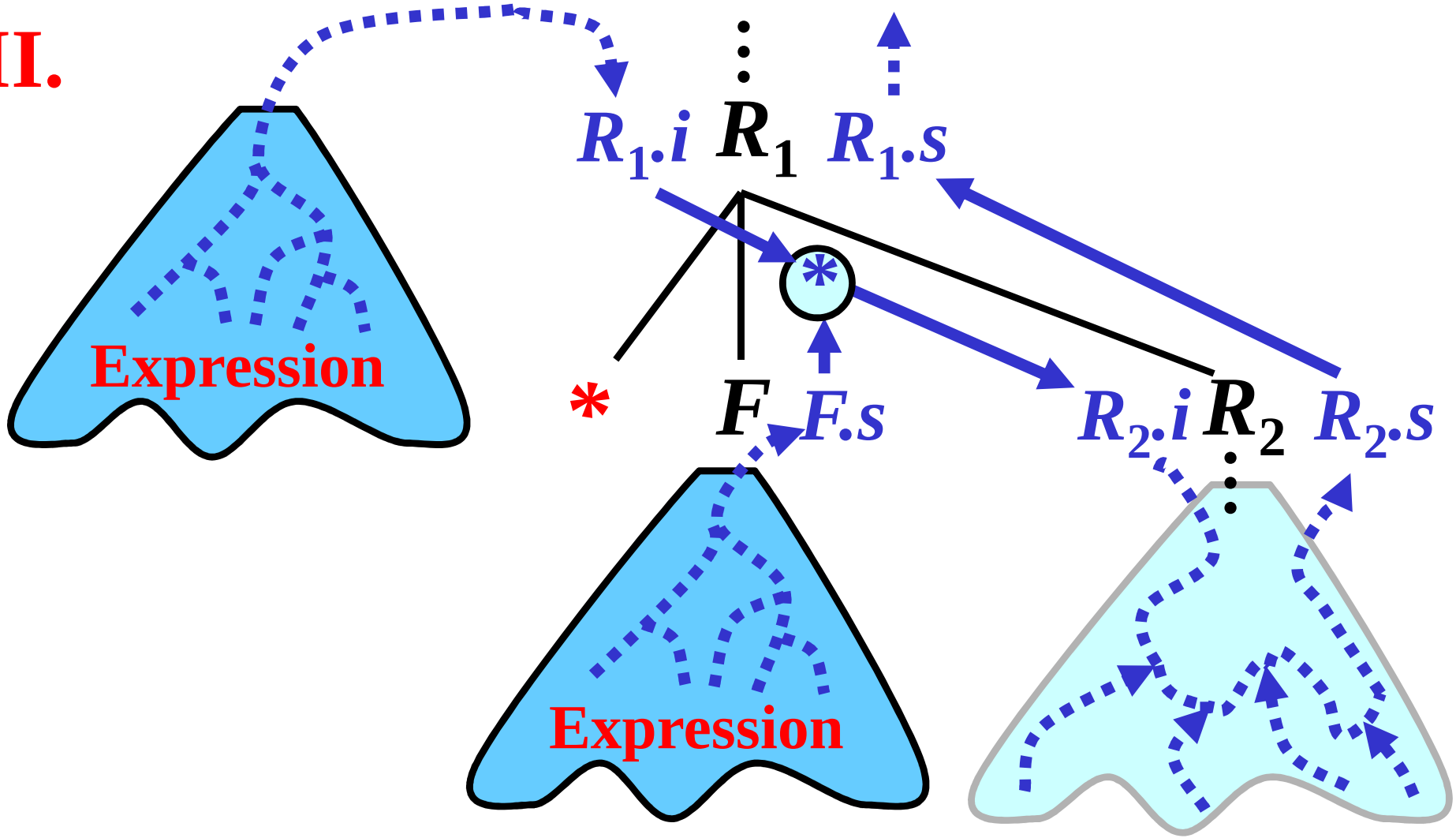
Expressions: Multiplication 2/4

II.



$$R_1 \rightarrow {*}F \ \{ \ R_2.i := R_1.i * F.s \ \} \ Q_2 \{ R_1.s := R_2.s \ \}$$

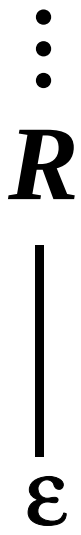
Expressions: Multiplication 2/4



$$R_1 \rightarrow {*}F \{ R_2.i := R_1.i * F.s \} \; Q_2 \{ R_1.s := R_2.s \}$$

Expressions: Multiplication 3/4

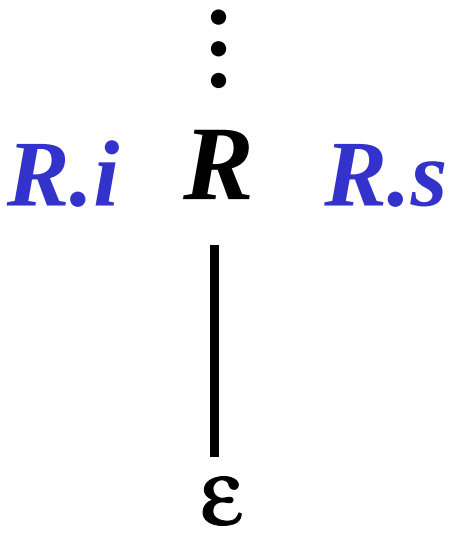
III.



$$R \rightarrow \varepsilon$$

Expressions: Multiplication 3/4

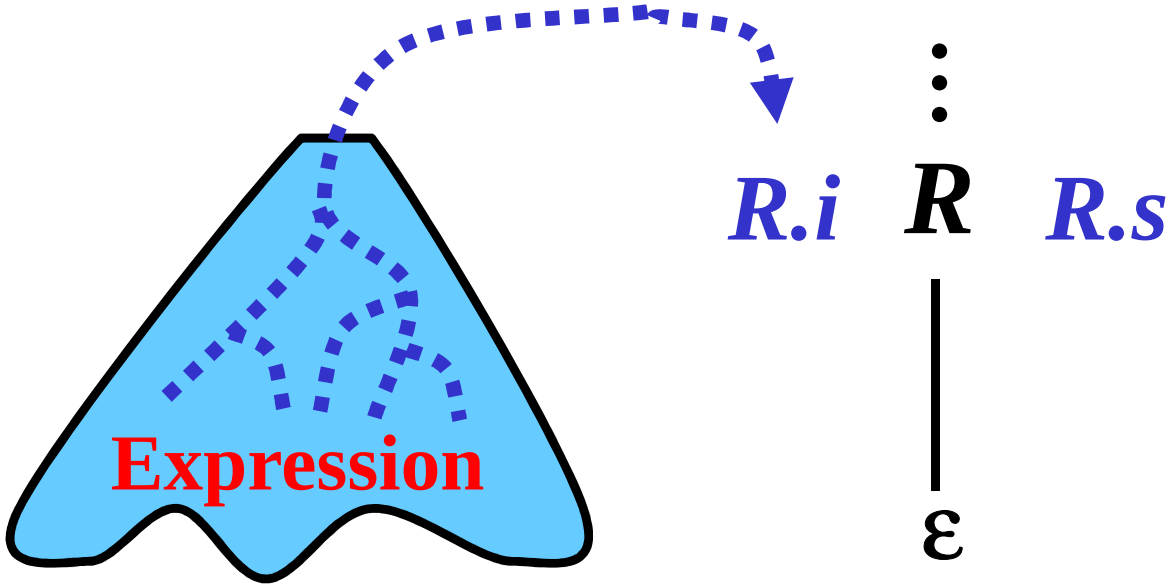
III.



$$R \rightarrow \varepsilon$$

Expressions: Multiplication 3/4

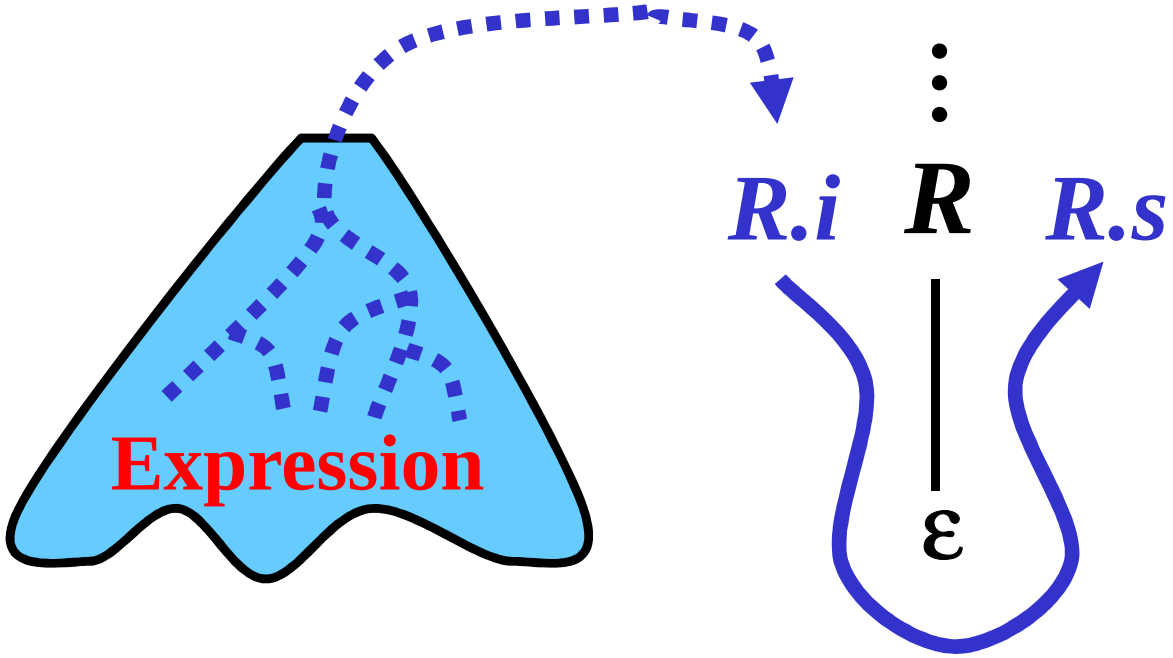
III.



$$R \rightarrow \varepsilon$$

Expressions: Multiplication 3/4

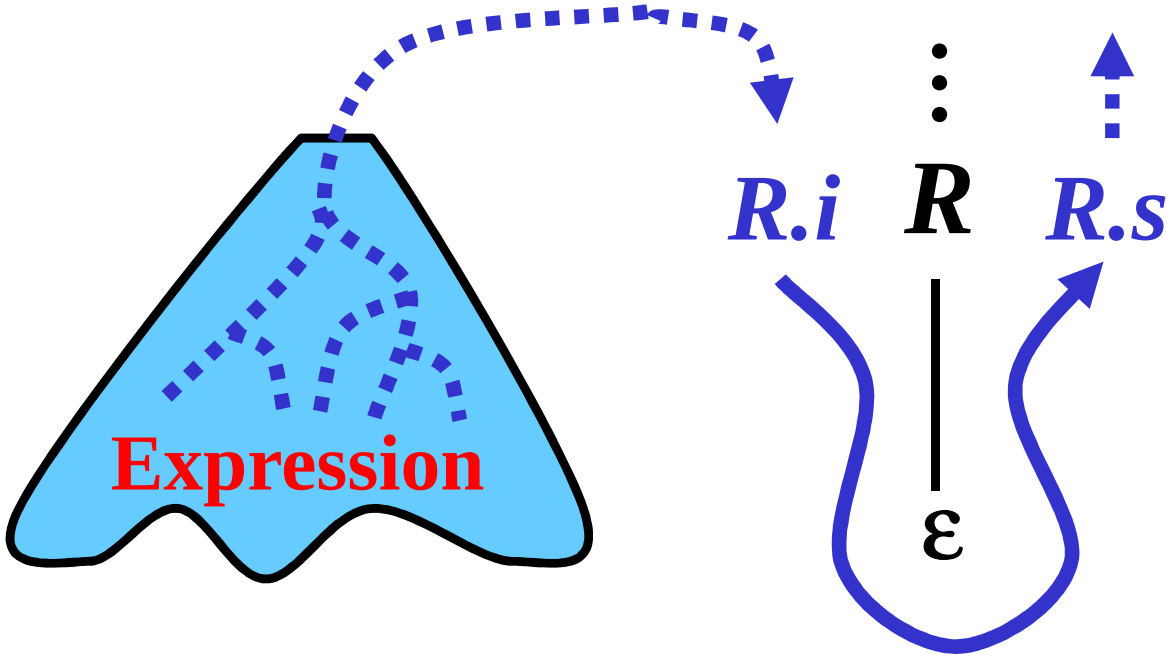
III.



$R \rightarrow \varepsilon \quad \{R.s := R.i\}$

Expressions: Multiplication 3/4

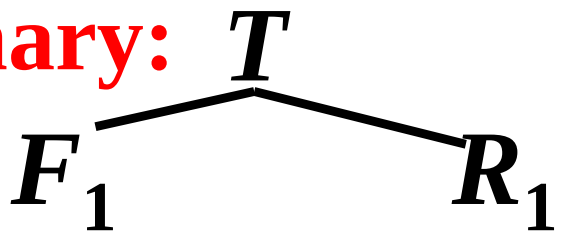
III.



$R \rightarrow \varepsilon \quad \{R.s := R.i\}$

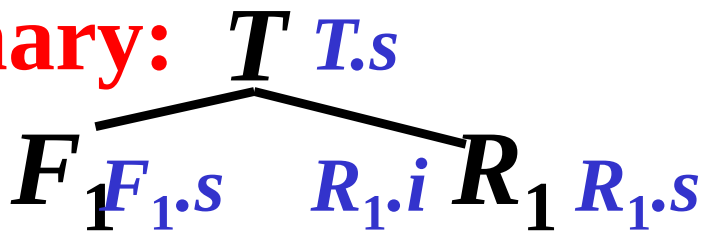
Expressions: Multiplication 4/4

Summary:



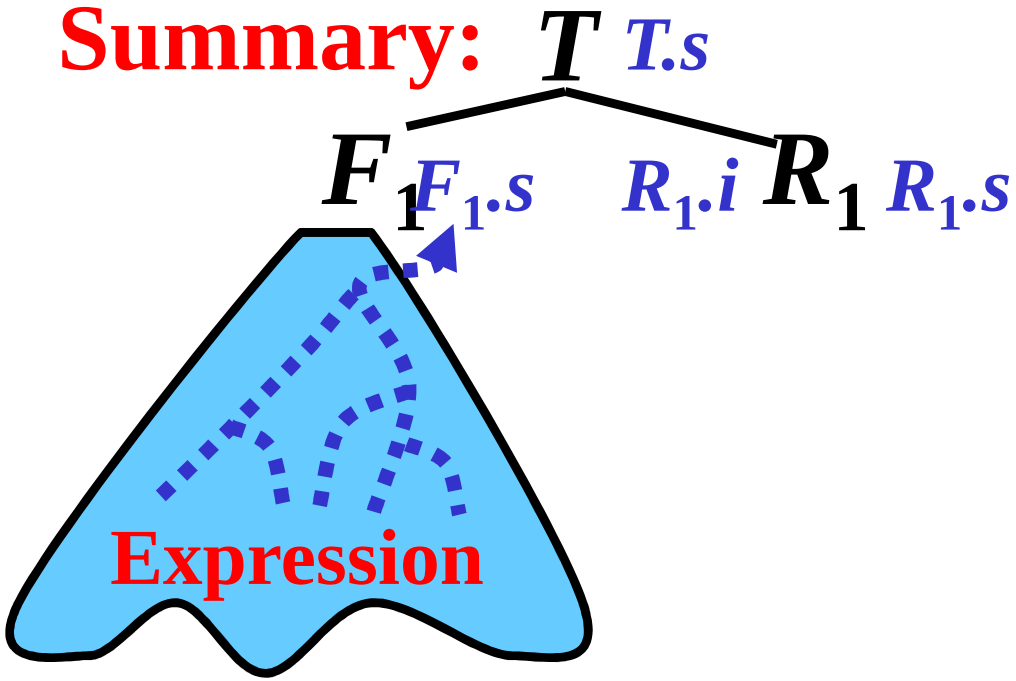
Expressions: Multiplication 4/4

Summary:



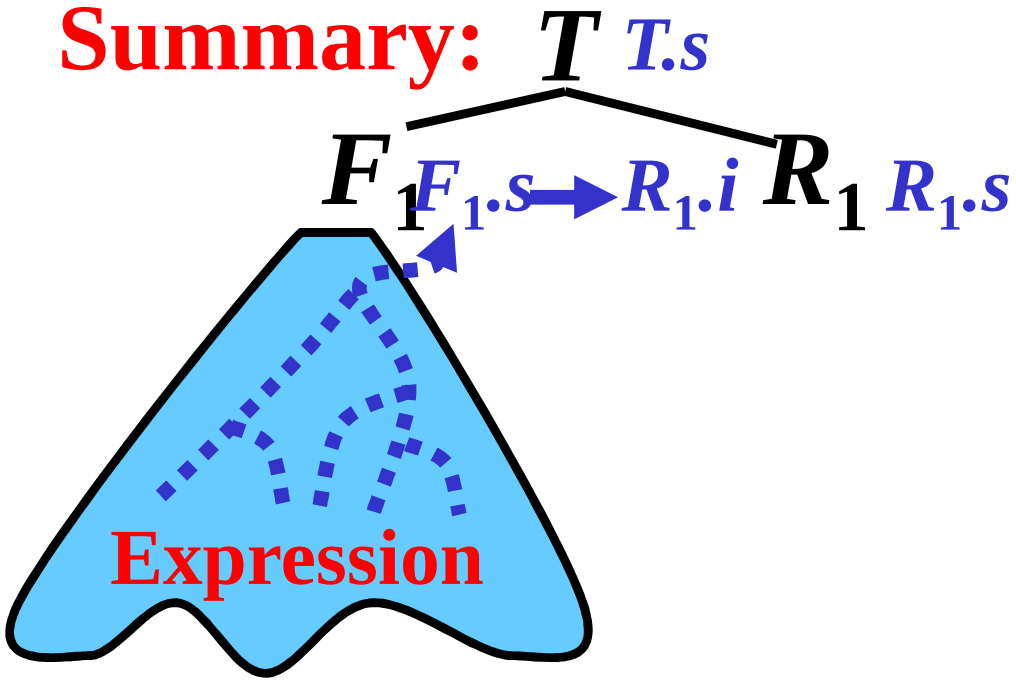
Expressions: Multiplication 4/4

Summary:



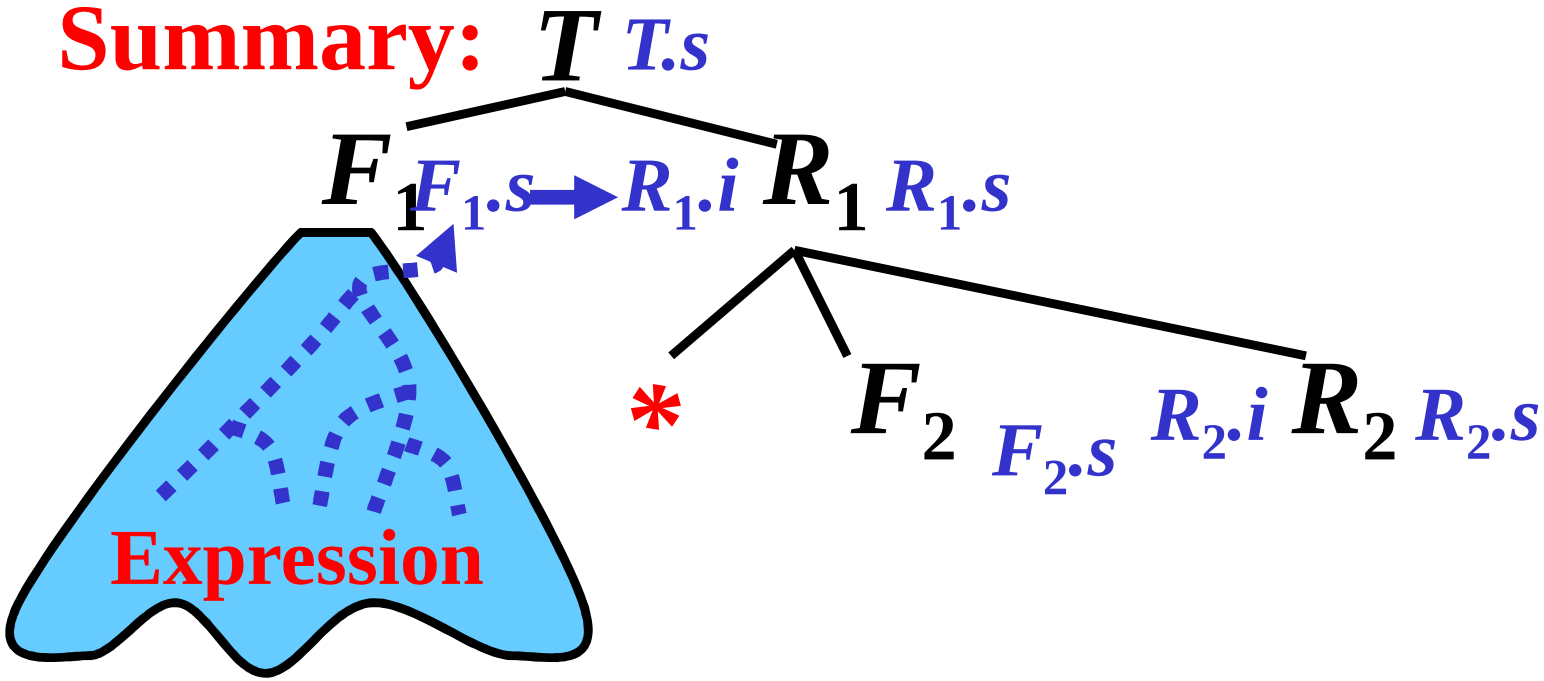
Expressions: Multiplication 4/4

Summary:



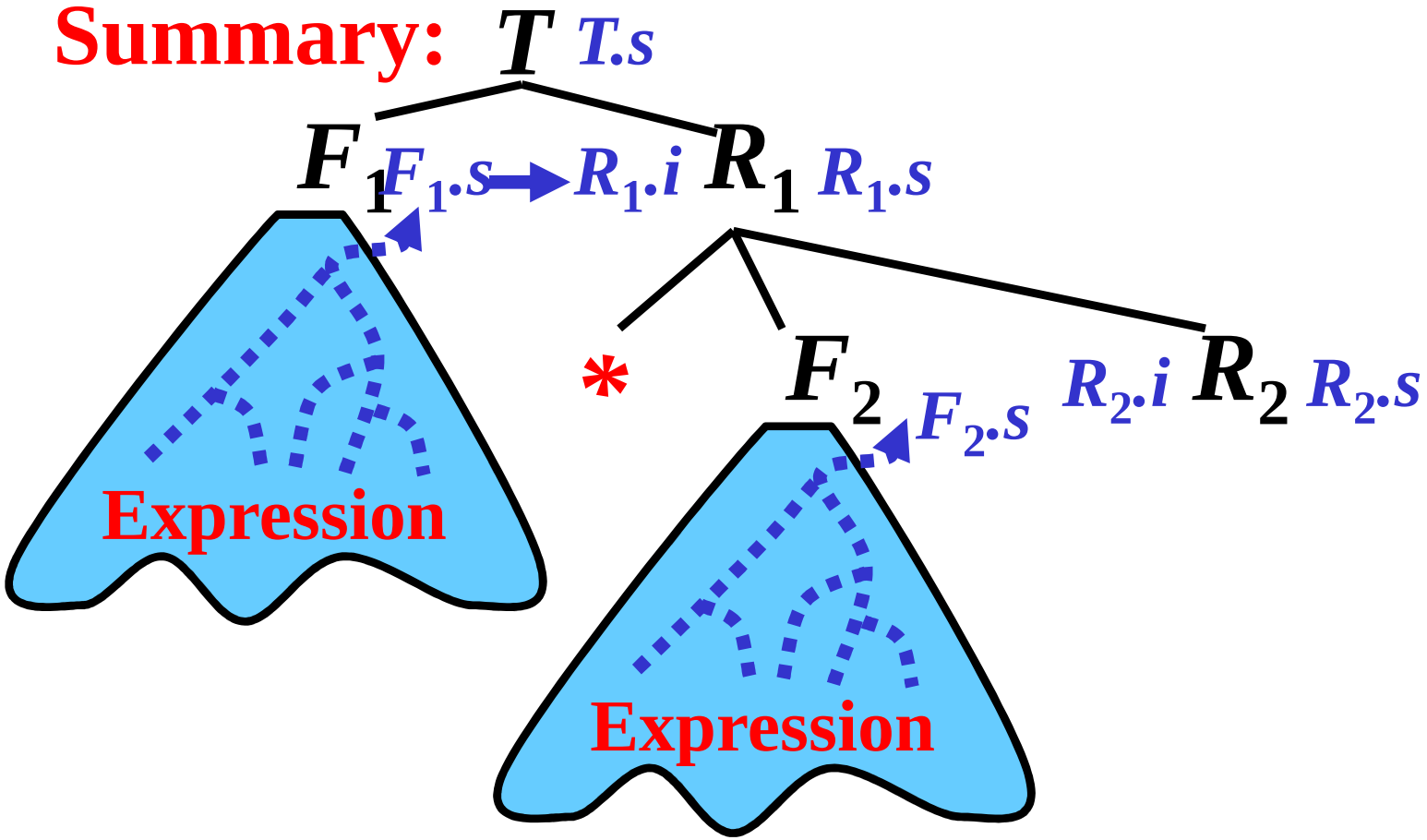
Expressions: Multiplication 4/4

Summary:



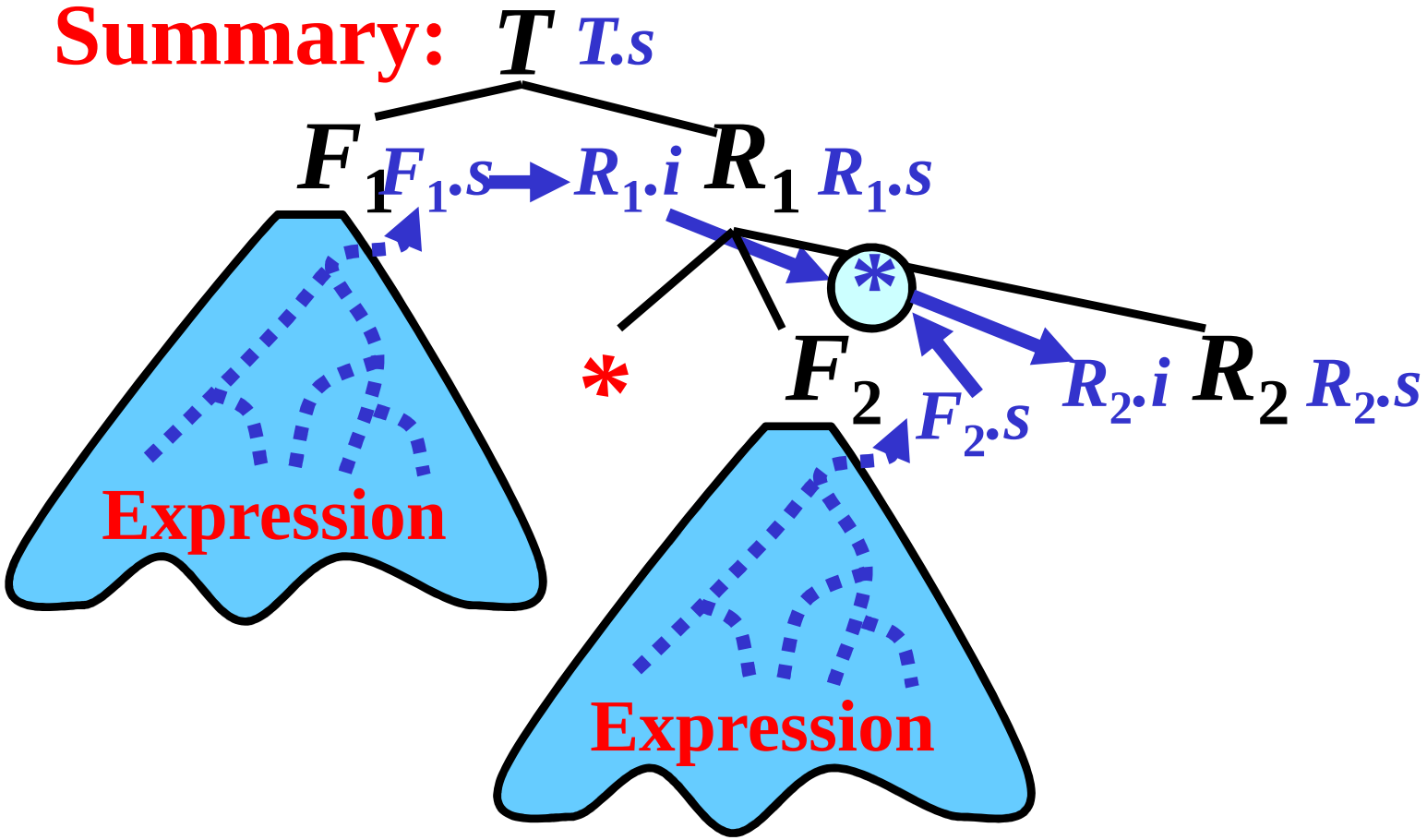
Expressions: Multiplication 4/4

Summary:



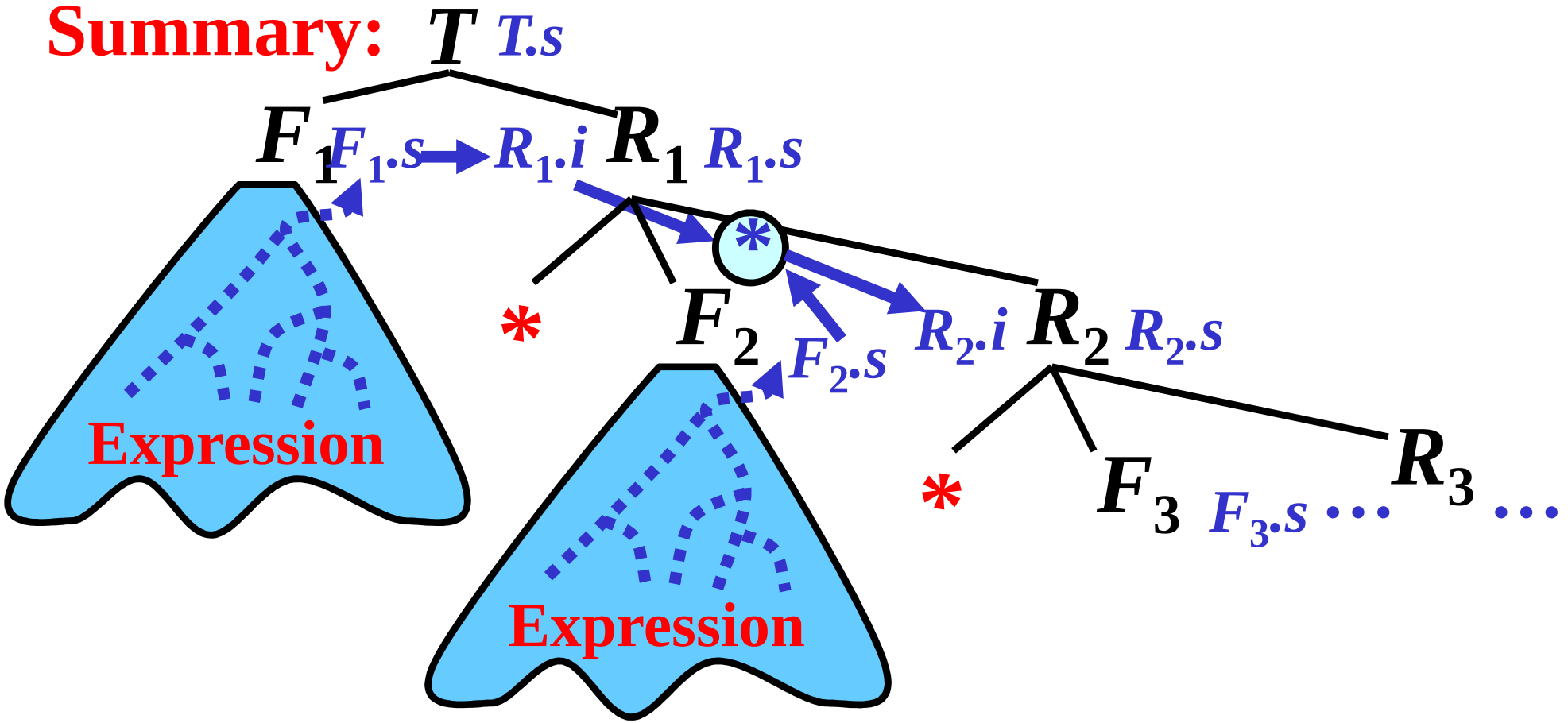
Expressions: Multiplication 4/4

Summary:



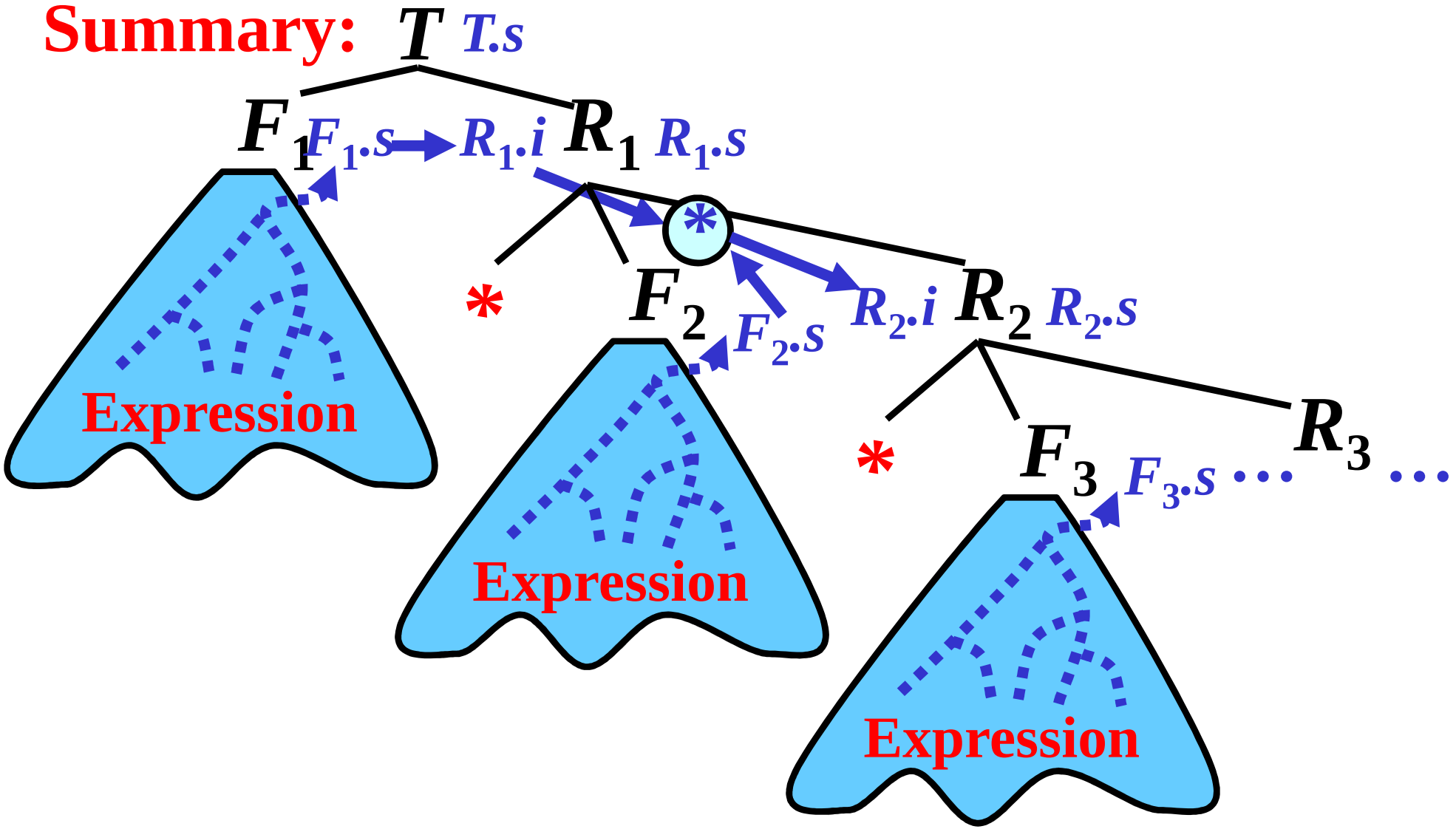
Expressions: Multiplication 4/4

Summary:



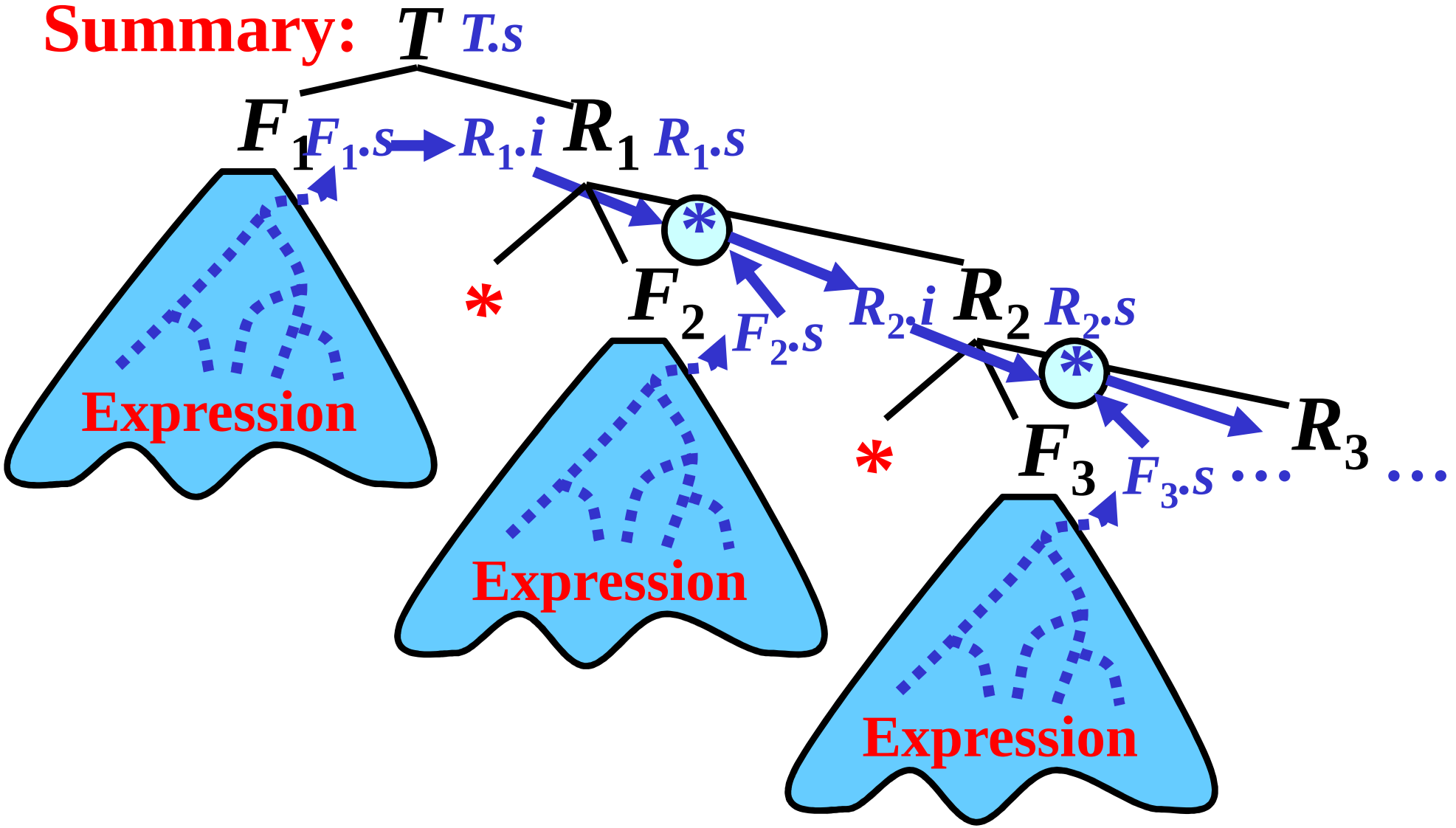
Expressions: Multiplication 4/4

Summary:



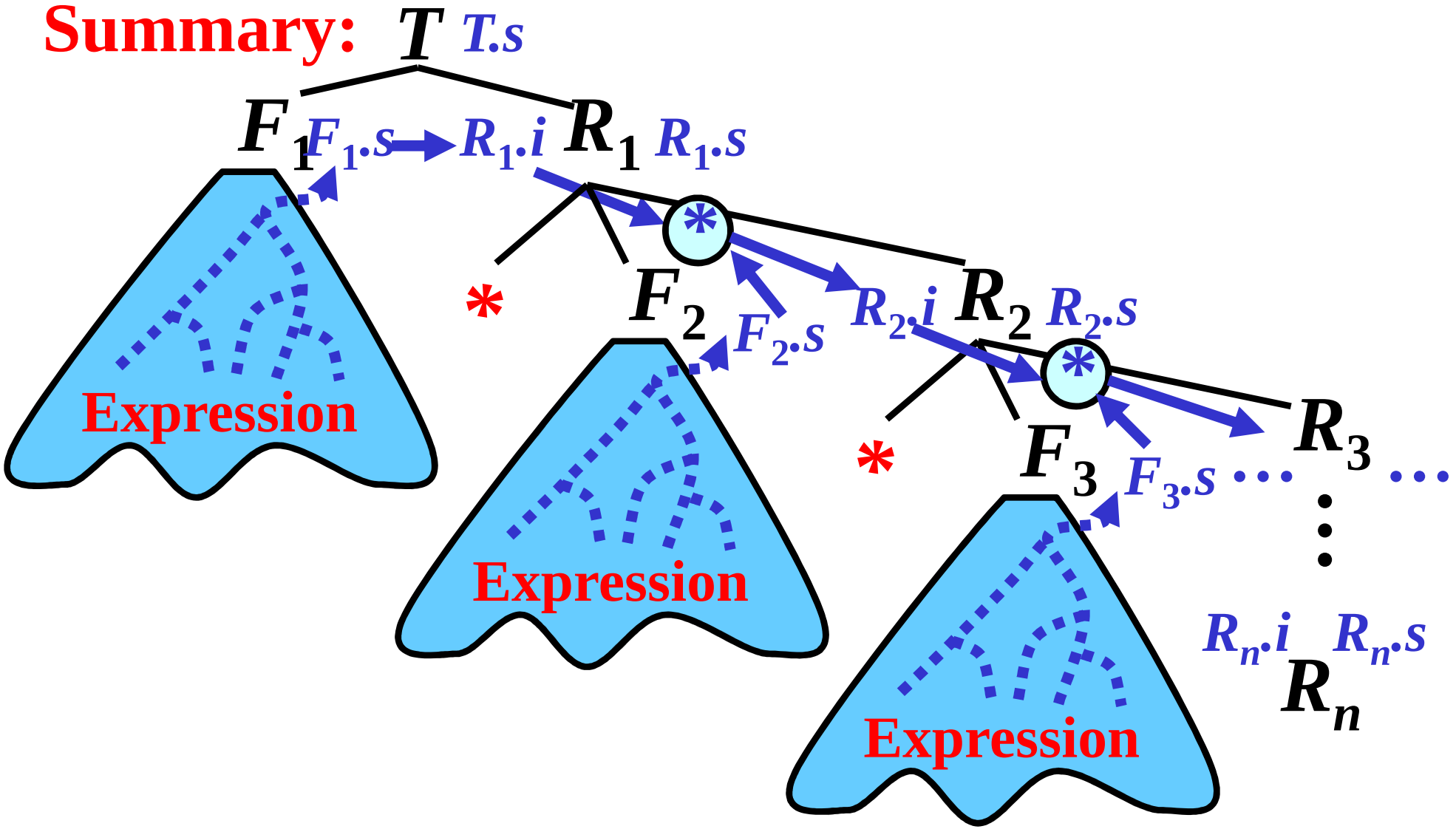
Expressions: Multiplication 4/4

Summary:

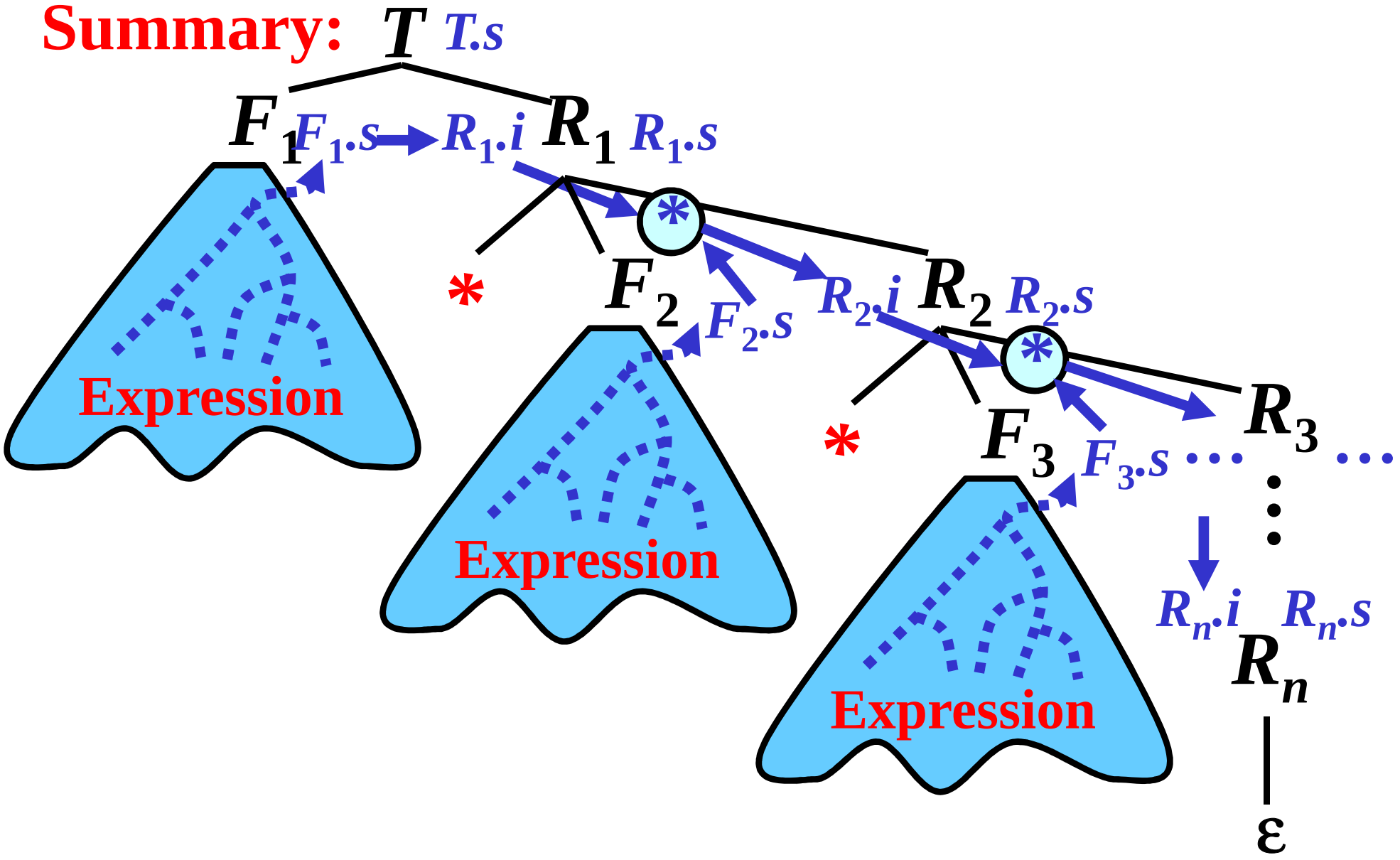


Expressions: Multiplication 4/4

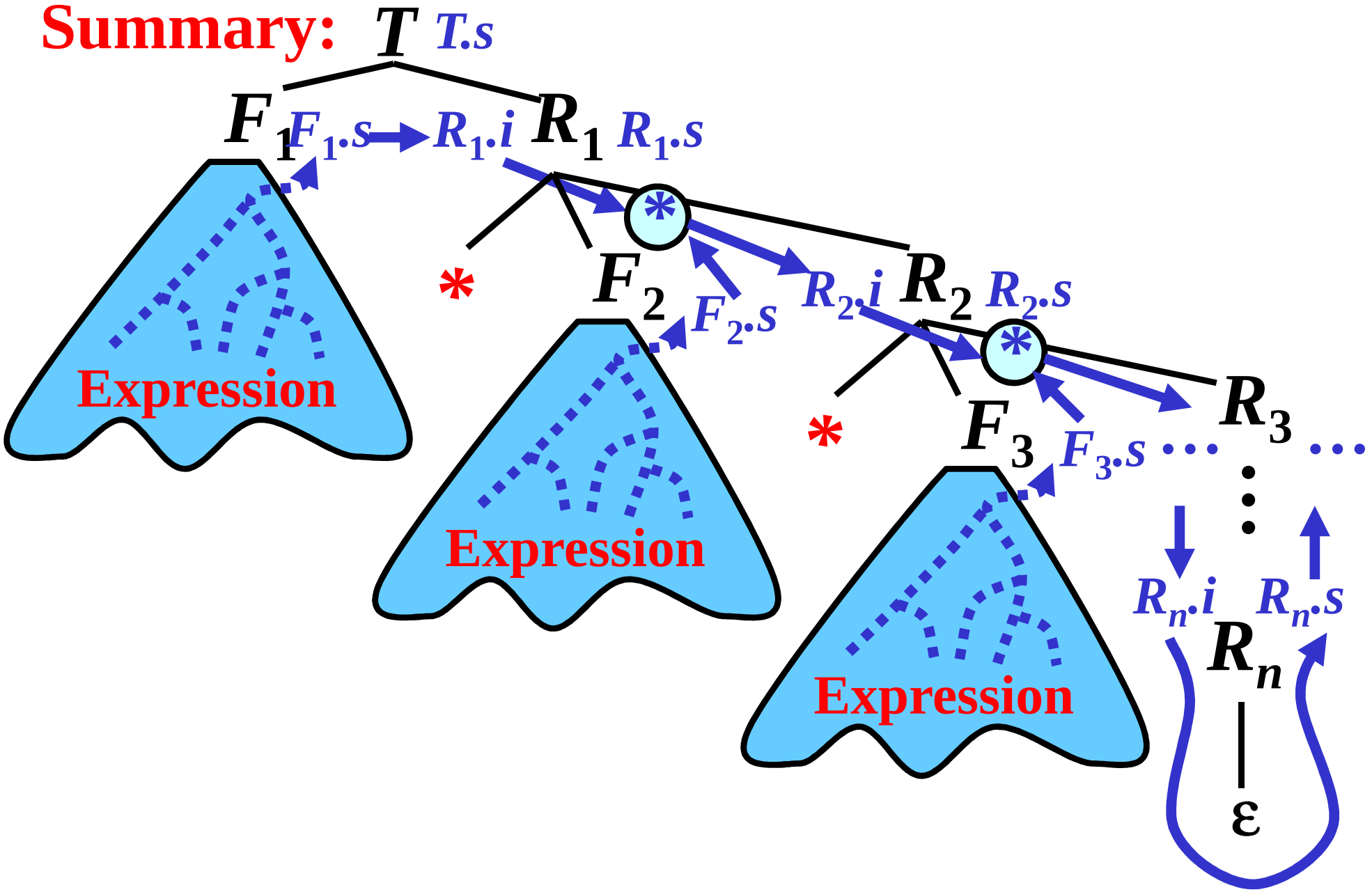
Summary:



Expressions: Multiplication 4/4

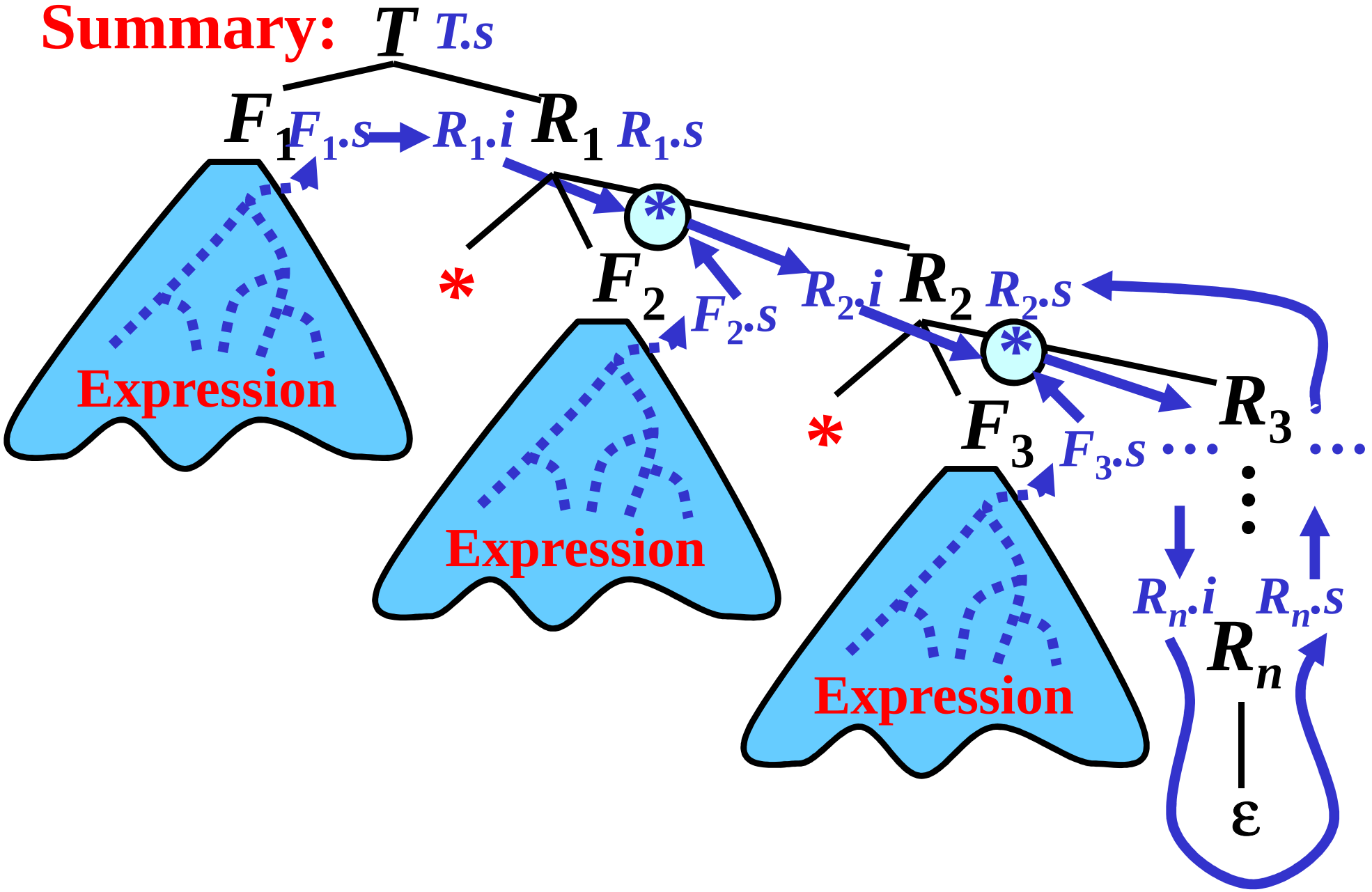


Expressions: Multiplication 4/4



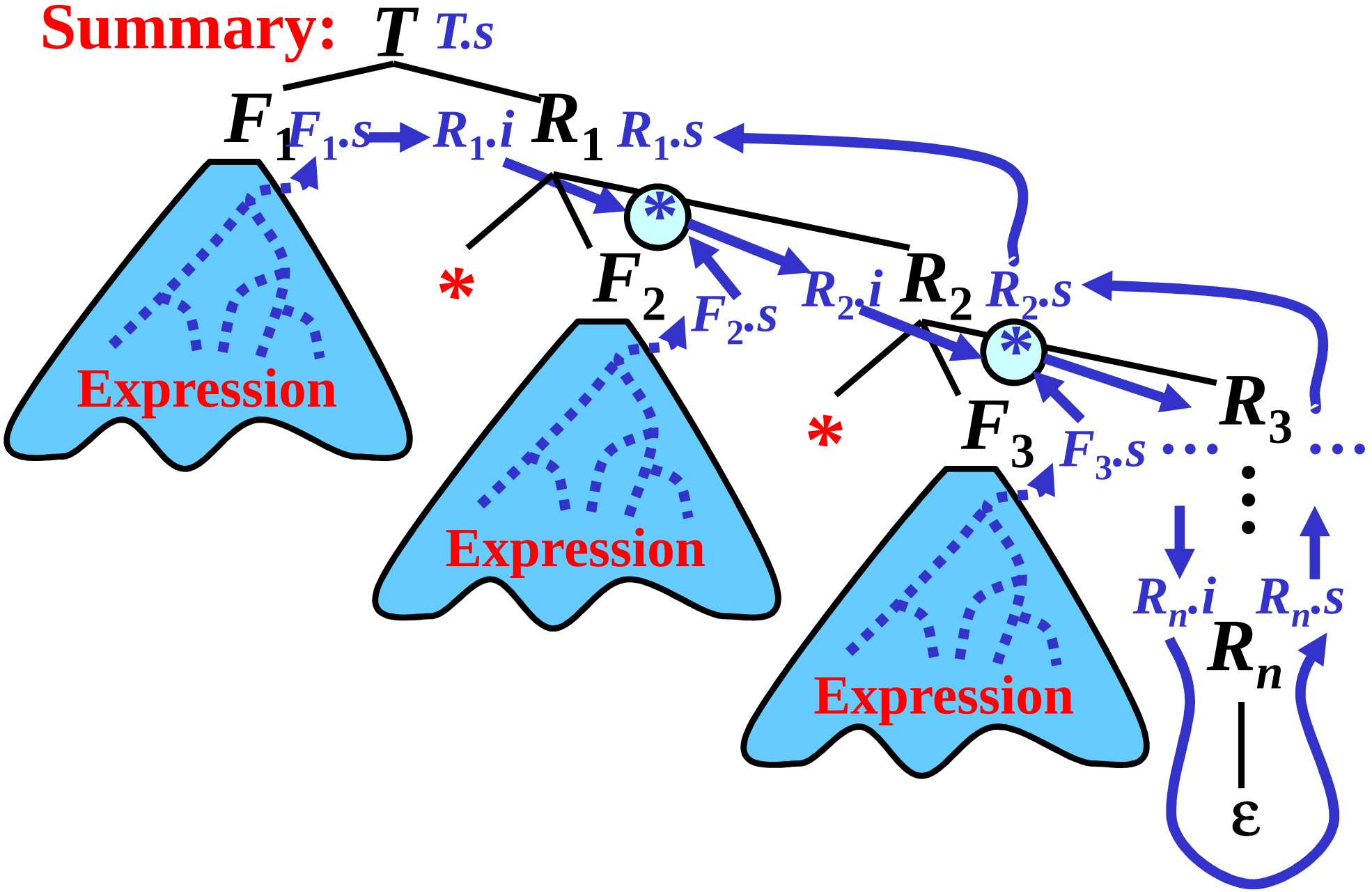
Expressions: Multiplication 4/4

Summary:

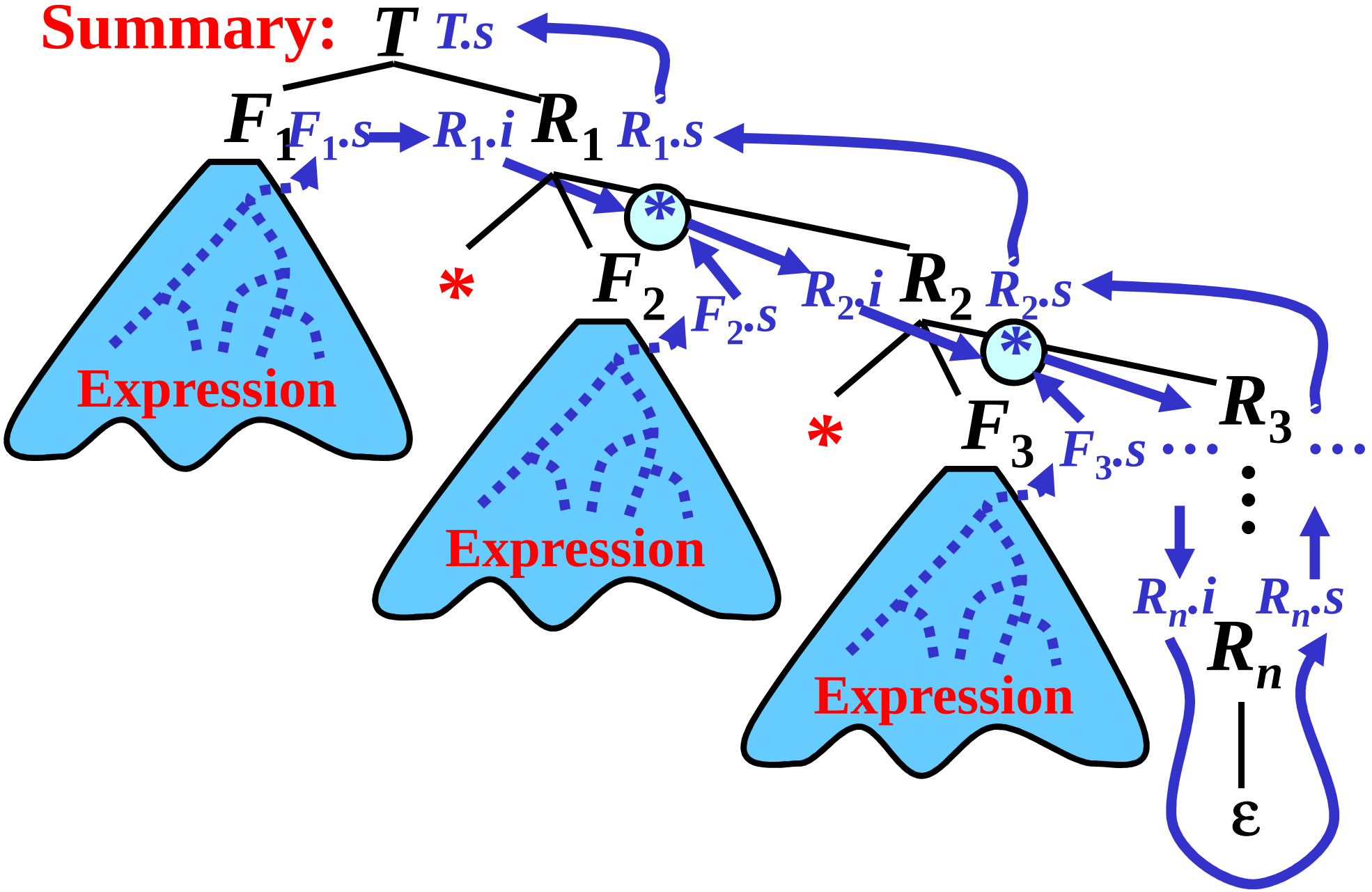


Expressions: Multiplication 4/4

Summary:



Expressions: Multiplication 4/4



Grammar for Expressions: Summary

1. $E \rightarrow T \; \{Q.i := T.s\} \; Q \; \{E.s := Q.s\}$
2. $Q_1 \rightarrow +T \; \{Q_2.i := Q_1.i + T.s\} \; Q_2 \; \{Q_1.s := Q_2.s\}$
3. $Q \rightarrow \varepsilon \; \{Q.s := Q.i\}$
4. $T \rightarrow F \; \{R.i := F.s\} \; R \; \{T.s := R.s\}$
5. $R_1 \rightarrow *F \; \{R_2.i := R_1.i * F.s\} \; R_2 \; \{R_1.s := R_2.s\}$
6. $R \rightarrow \varepsilon \; \{R.s := R.i\}$
7. $F \rightarrow (E \; \{F.s := E.s\} \;)$
8. $F \rightarrow i \; \{F.s := i.value\}$

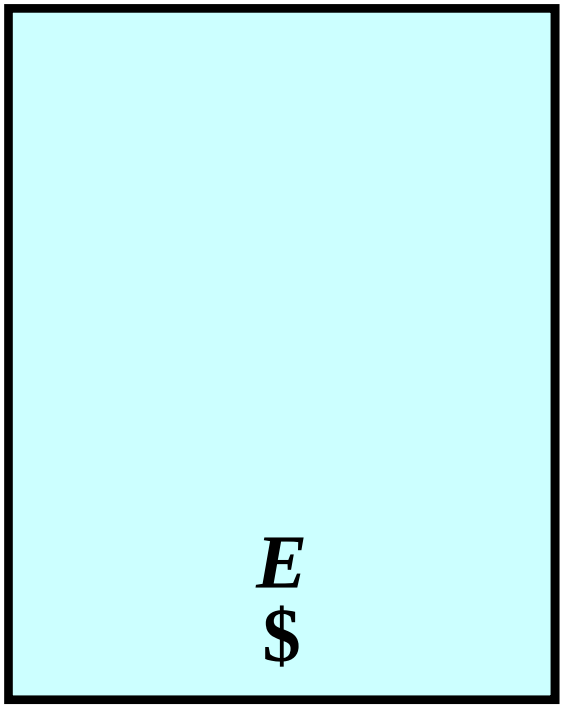
Evaluation of Expressions: Example 1/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2$ \$

Rule: $E \rightarrow T_1 \{Q_1.i := T_1.s\}\ Q_1\ \{E.s := Q_1.s\}$

Parser pushdown:



Semantic pushdown:

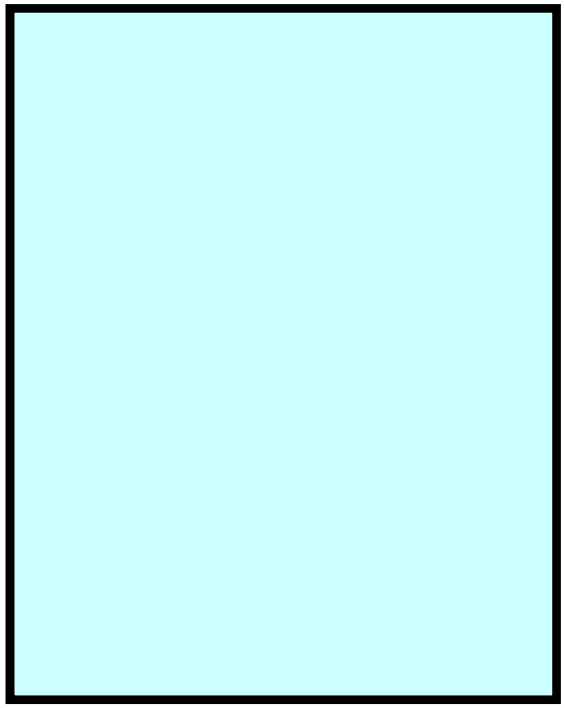
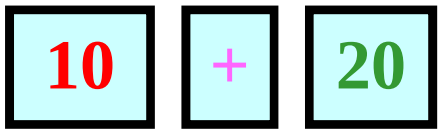


Illustration:



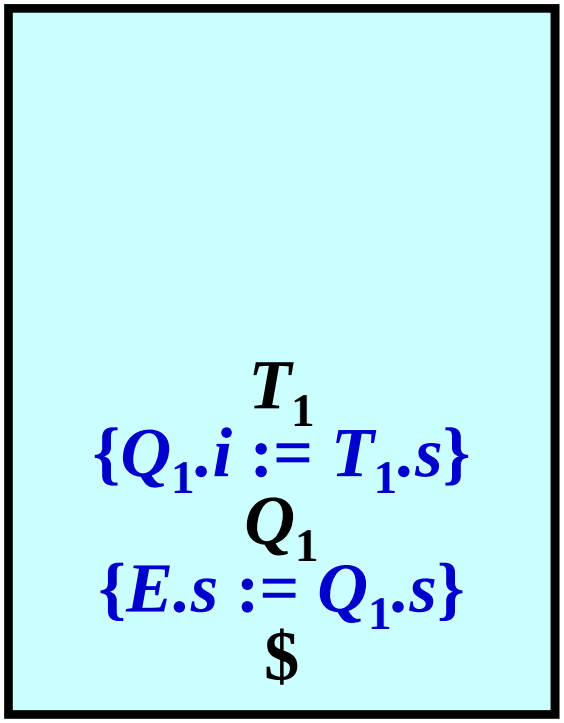
Evaluation of Expressions: Example 2/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2$ \$

Rule: $T_1 \rightarrow F_1 \{R_1.i := F_1.s\} R_1 \{T_1.s := R_1.s\}$

Parser pushdown:



Semantic pushdown:

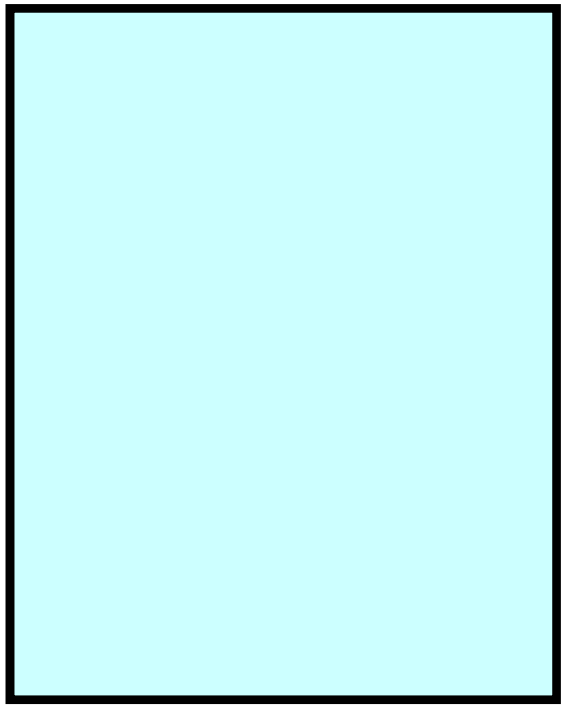
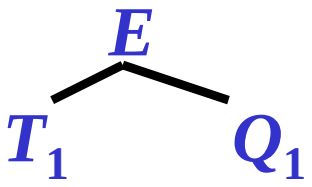
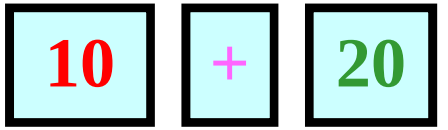


Illustration:





Evaluation of Expressions: Example 3/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $i_1 + i_2$ \$

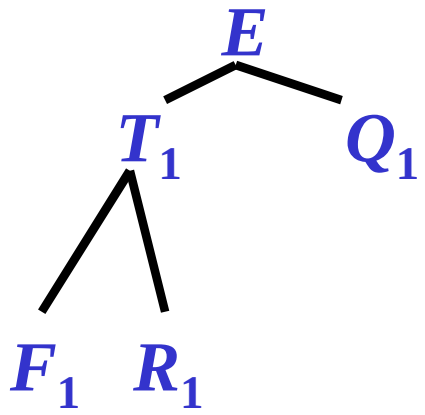
Rule: $F_1 \rightarrow i_1$ $\{F_1.s := i.value\}$

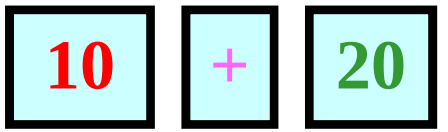
Parser pushdown:

F_1
$\{R_1.i := F_1.s\}$
R_1
$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
\$

Semantic pushdown:

Illustration:





Evaluation of Expressions: Example 4/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $i_1 + i_2$ \$

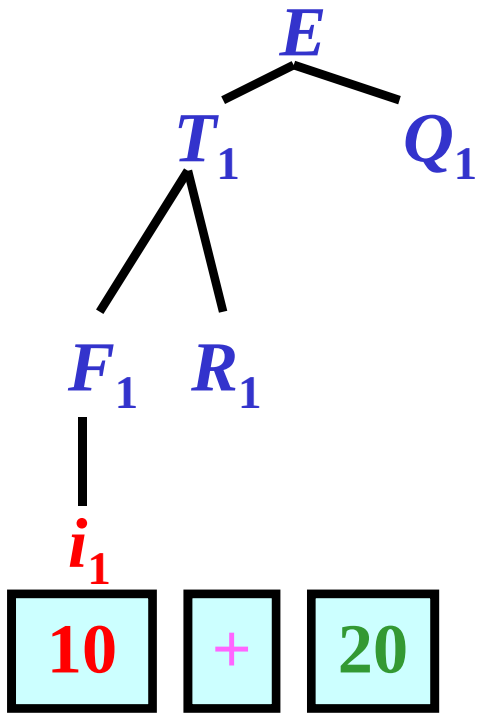
Rule:

Parser pushdown:

i_1
$\{F_1.s := i.value\}$
$\{R_1.i := F_1.s\}$
R_1
$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
\$

Semantic pushdown:

Illustration:



Evaluation of Expressions: Example 5/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $+ \; i_2 \; \$$

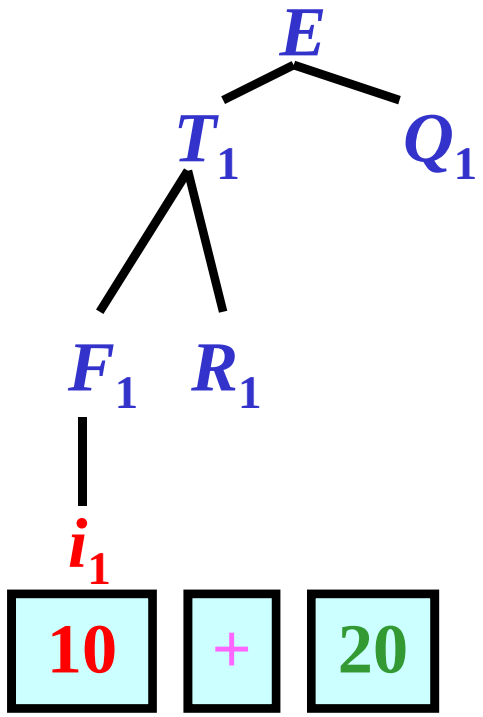
Rule:

Parser pushdown:

$\{F_1.s := i.value\}$
$\{R_1.i := F_1.s\}$
R_1
$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

Illustration:



Evaluation of Expressions: Example 6/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ \; i_2 \; \$$

Rule:

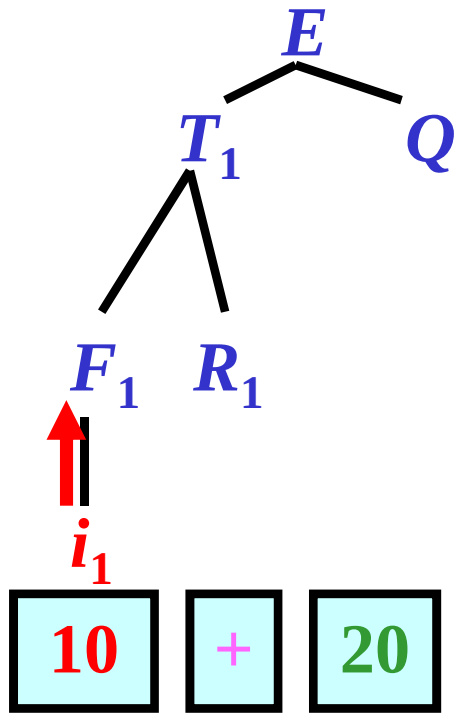
Parser pushdown:

$\{R_1.i := F_1.s\}$
R_1
$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

$F_1.s = 10$

Illustration:



Evaluation of Expressions: Example 6/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ \; i_2 \; \$$

Rule: $R_1 \rightarrow \varepsilon \; \{R_1.s := R_1.i\}$

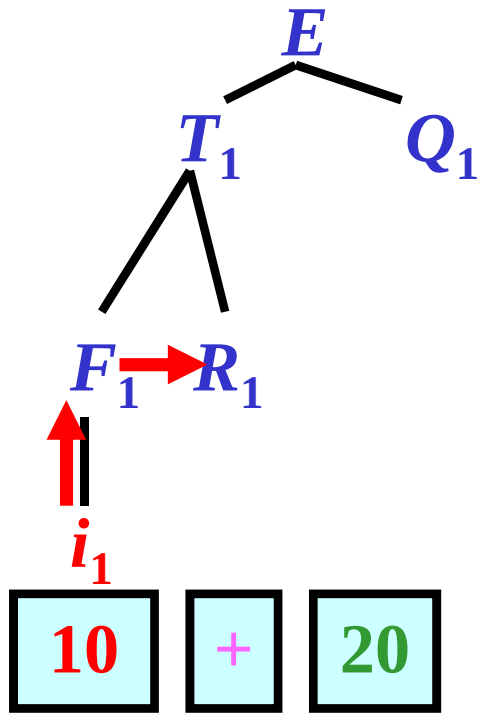
Parser pushdown:

R_1
$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

$R_1.i = 10$

Illustration:



Evaluation of Expressions: Example 7/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ \; i_2 \; \$$

Rule:

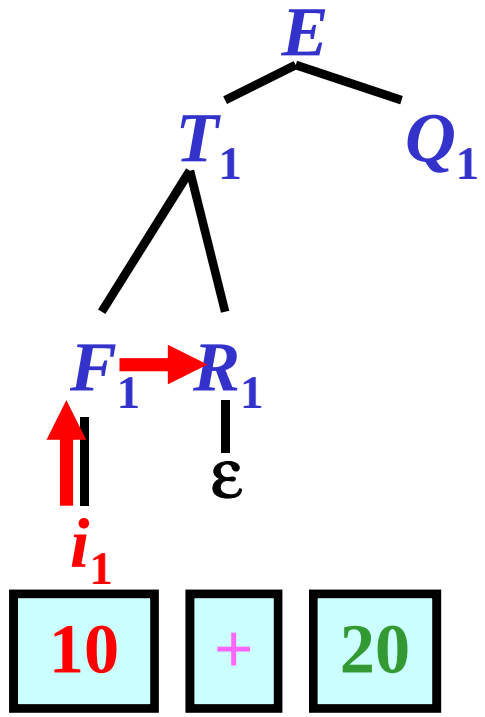
Parser pushdown:

$\{R_1.s := R_1.i\}$
$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

$R_1.i = 10$

Illustration:



Evaluation of Expressions: Example 7/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $+ \; i_2 \; \$$

Rule:

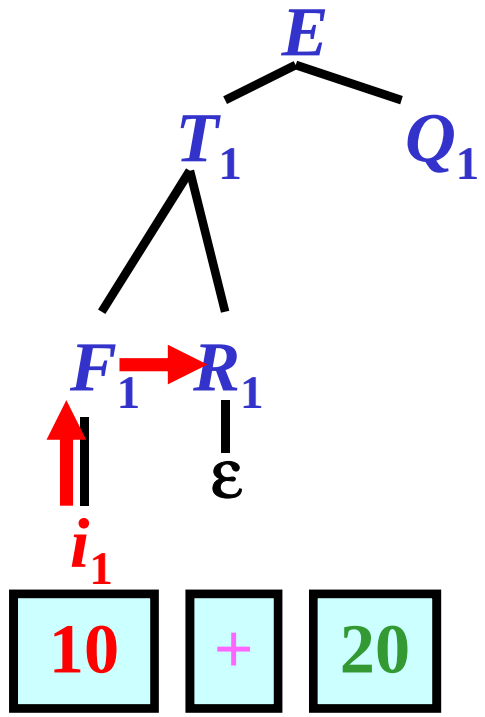
Parser pushdown:

$\{T_1.s := R_1.s\}$
$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

$R_1.s = 10$

Illustration:



Evaluation of Expressions: Example 7/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ \; i_2 \; \$$

Rule:

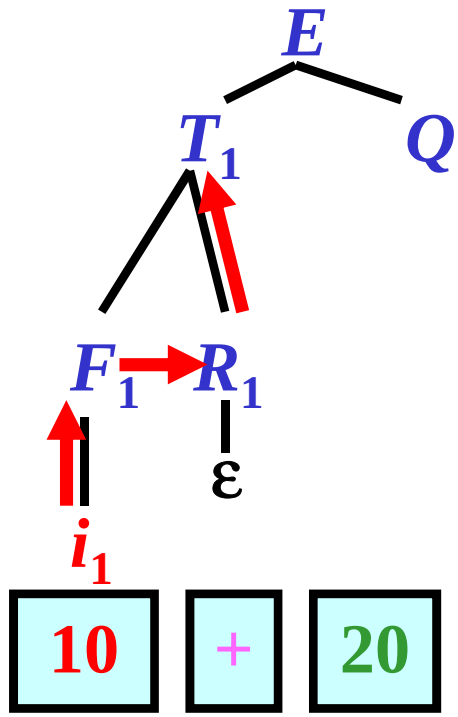
Parser pushdown:

$\{Q_1.i := T_1.s\}$
Q_1
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

$T_1.s = 10$

Illustration:



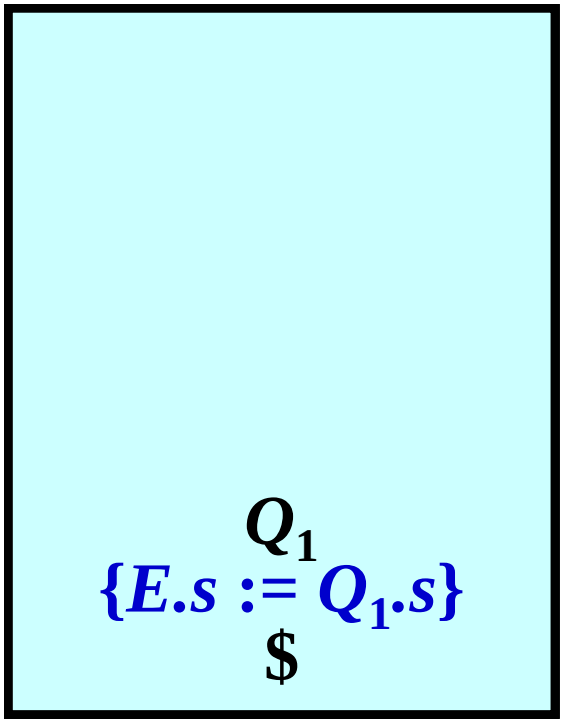
Evaluation of Expressions: Example 7/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+ \; i_2 \; \$$

Rule: $Q_1 \rightarrow +T_2 \; \{Q_2.i := Q_1.i + T_2.s\} \; Q_2 \; \{Q_1.s := Q_2.s\}$

Parser pushdown:



Semantic pushdown:

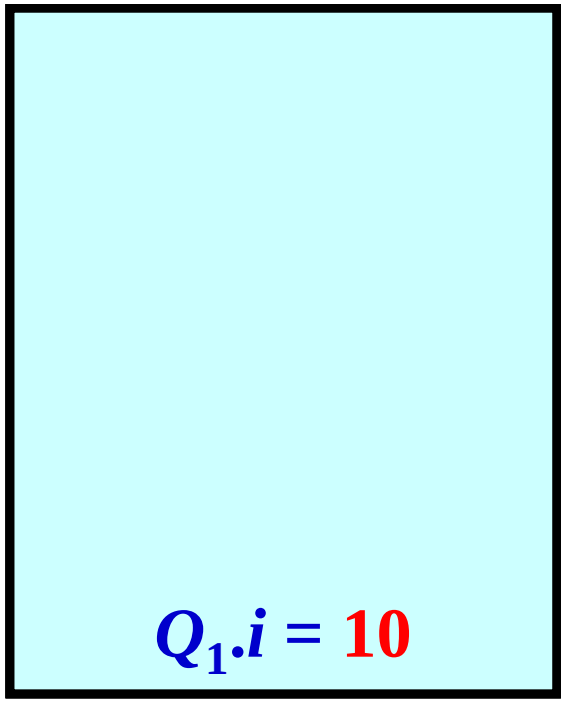
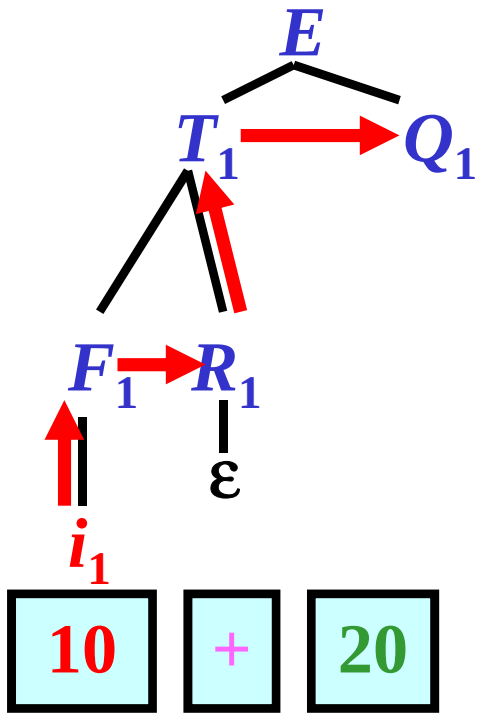


Illustration:



Evaluation of Expressions: Example 8/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: $+\ i_2\ \$$

Rule:

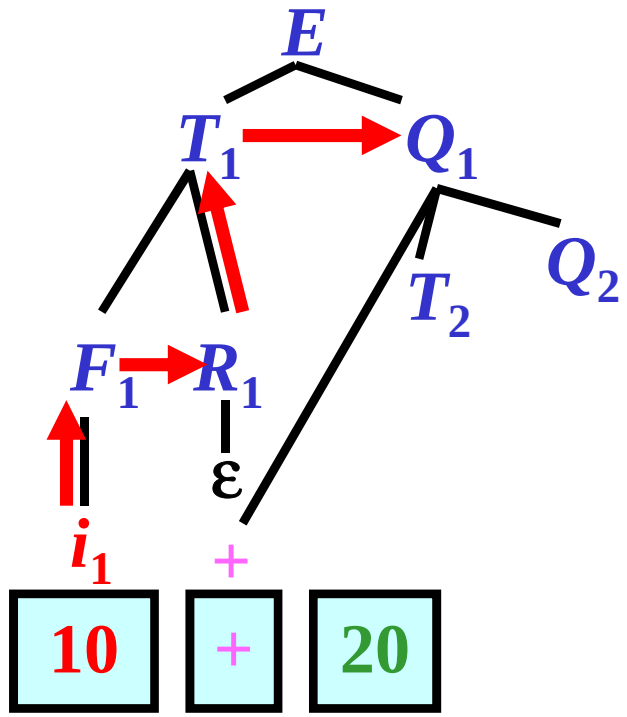
Parser pushdown:

$+$
T_2
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$\$$

Semantic pushdown:

$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 9/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: i_2 \$

Rule: $T_2 \rightarrow F_2\ \{R_2.i := F_2.s\}\ R_2\ \{T_2.s := R_2.s\}$

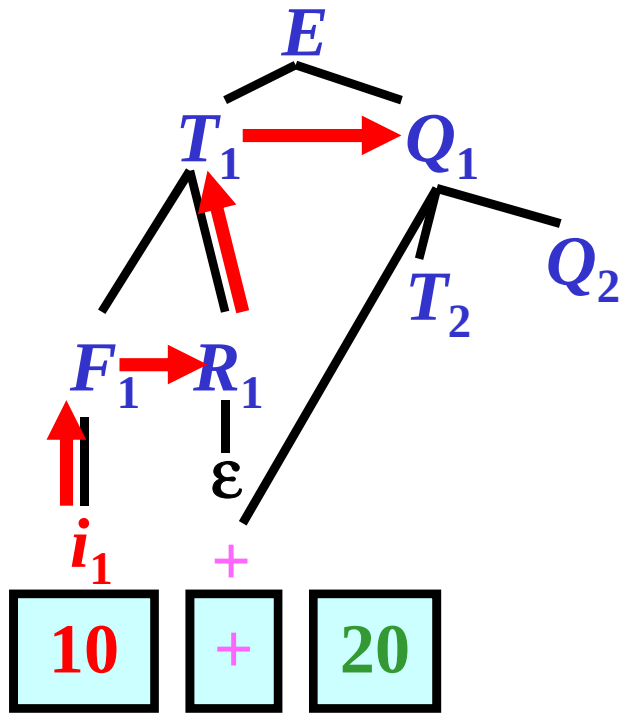
Parser pushdown:

T_2
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
\$

Semantic pushdown:

$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 10/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: i_2 \$

Rule: $F_2 \rightarrow i_2$ $\{F_2.s := i.value\}$

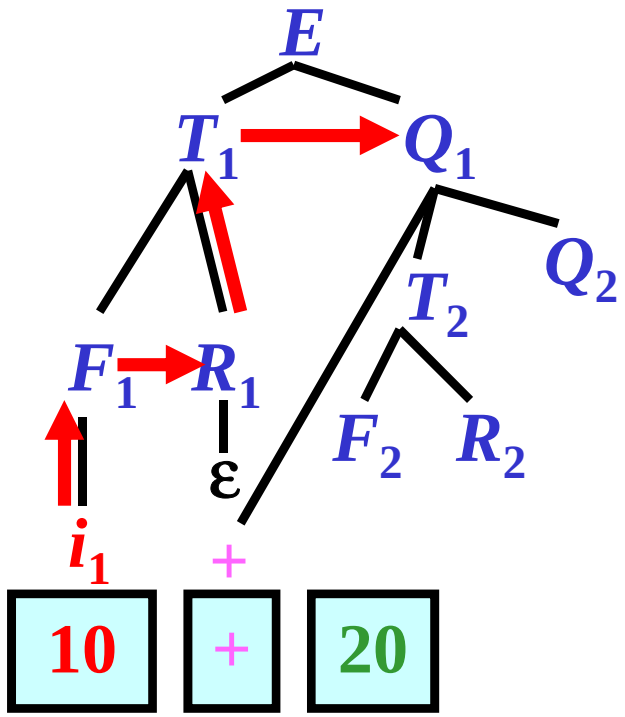
Parser pushdown:

F_2
$\{R_2.i := F_2.s\}$
R_2
$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
\$

Semantic pushdown:

$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 11/16

Example for $a + b$, where $a.value = 10$, $b.value = 20$

Input: i_2 \$

Rule:

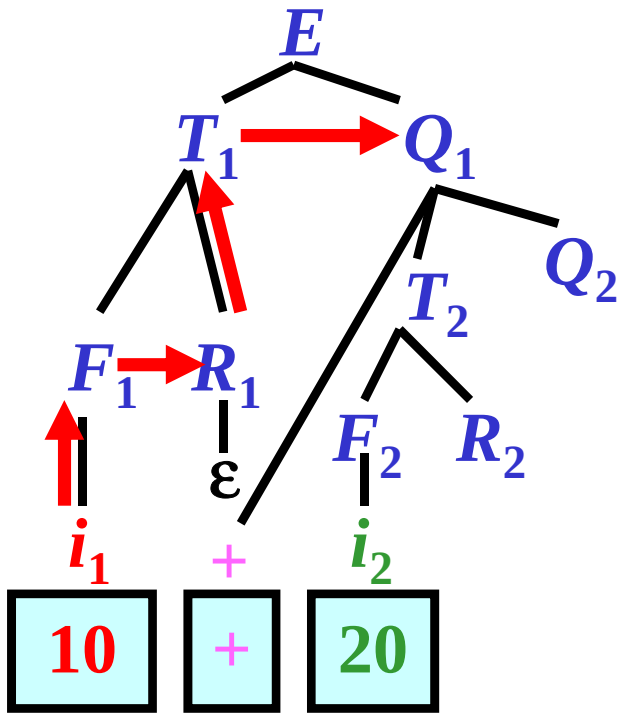
Parser pushdown:

i_2
$\{F_2.s := i.value\}$
$\{R_2.i := F_2.s\}$
R_2
$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
\$

Semantic pushdown:

$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 12/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

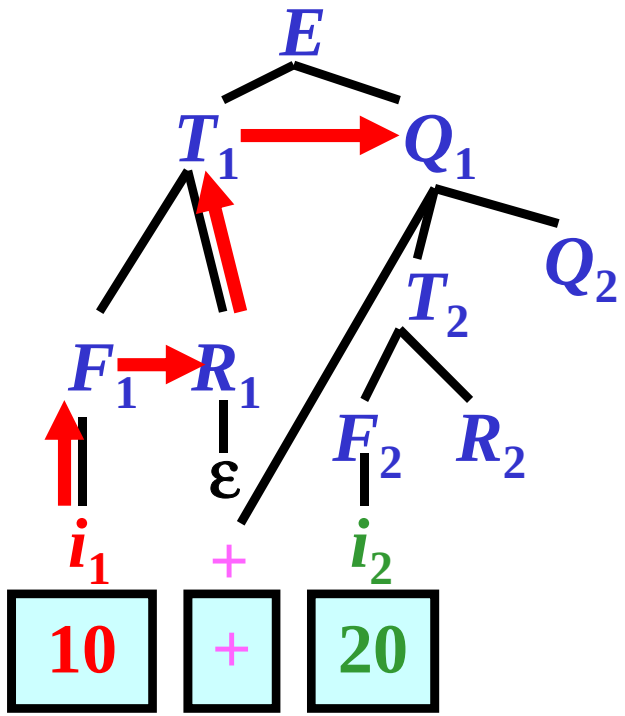
Parser pushdown:

$\{F_2.s := i.value\}$
$\{R_2.i := F_2.s\}$
R_2
$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 13/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

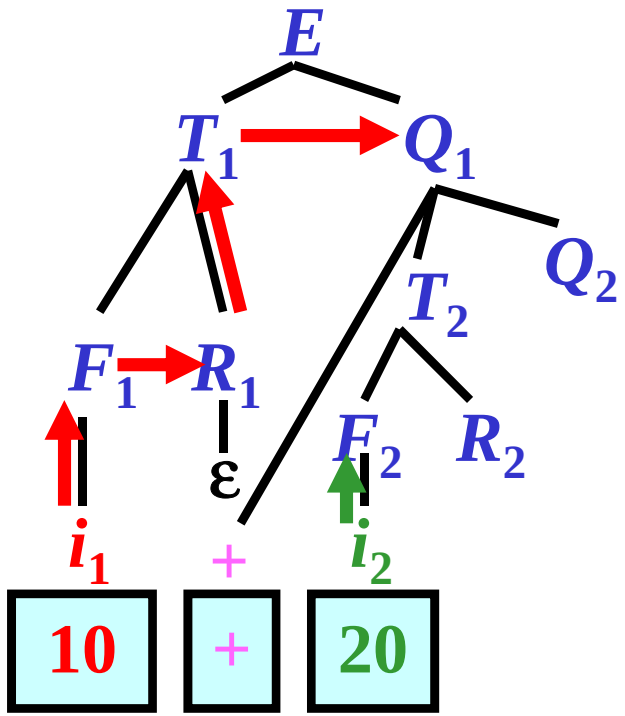
Parser pushdown:

$\{R_2.i := F_2.s\}$
R_2
$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$F_2.s = 20$
$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 13/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule: $R_2 \rightarrow \varepsilon \; \{R_2.s := R_2.i\}$

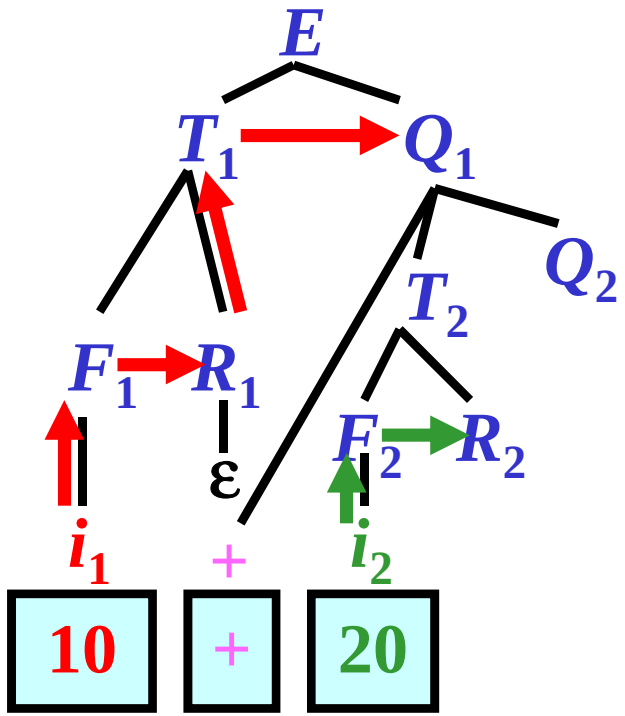
Parser pushdown:

R_2
$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$R_2.i = 20$
$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 14/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

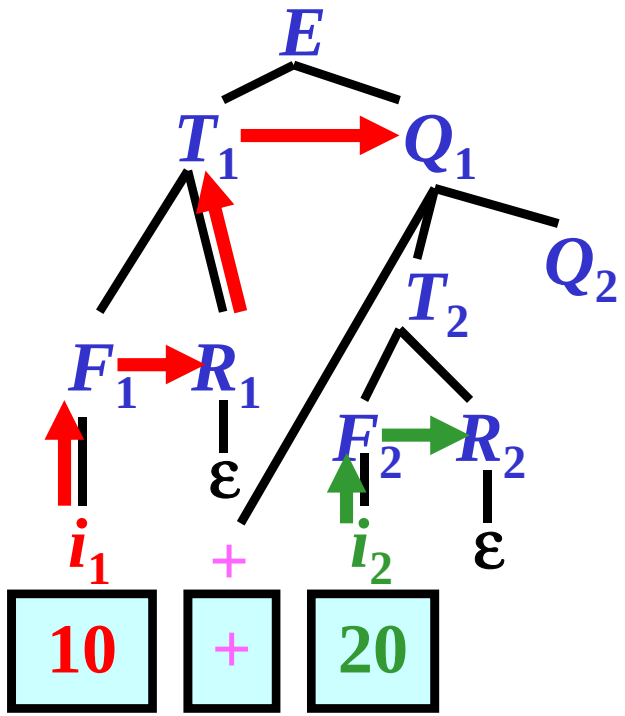
Parser pushdown:

$\{R_2.s := R_2.i\}$
$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$R_2.i = 20$
$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 14/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

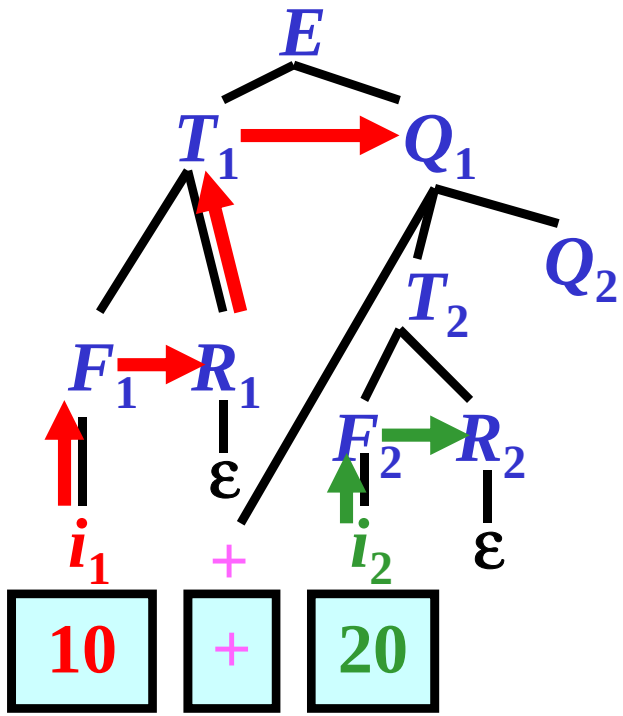
Parser pushdown:

$\{T_2.s := R_2.s\}$
$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$R_2.s = 20$
$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 14/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

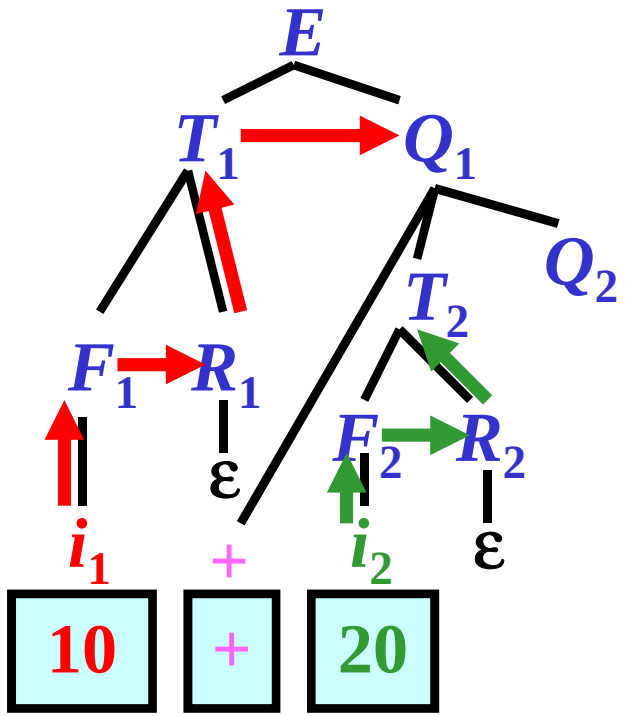
Parser pushdown:

$\{Q_2.i := Q_1.i + T_2.s\}$
Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$T_2.s = 20$
$Q_1.i = 10$

Illustration:



Evaluation of Expressions: Example 15/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule: $Q_2 \rightarrow \varepsilon \{Q_2.s := Q_2.i\}$

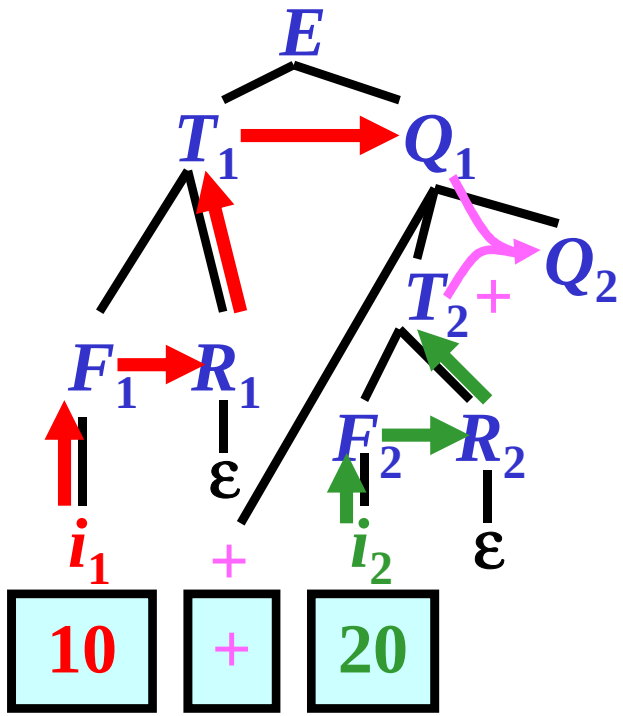
Parser pushdown:

Q_2
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$Q_2.i = 30$

Illustration:



Evaluation of Expressions: Example 16/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

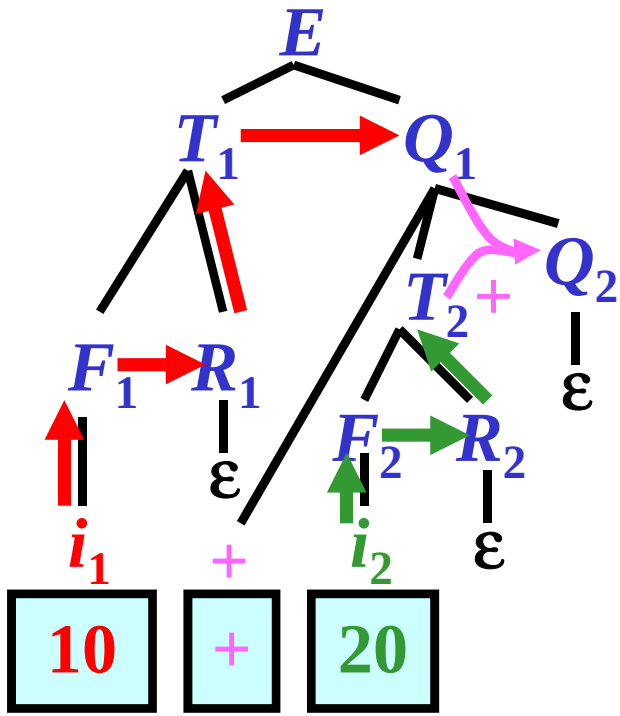
Parser pushdown:

$\{Q_2.s := Q_2.i\}$
$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$Q_2.i = 30$

Illustration:



Evaluation of Expressions: Example 16/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

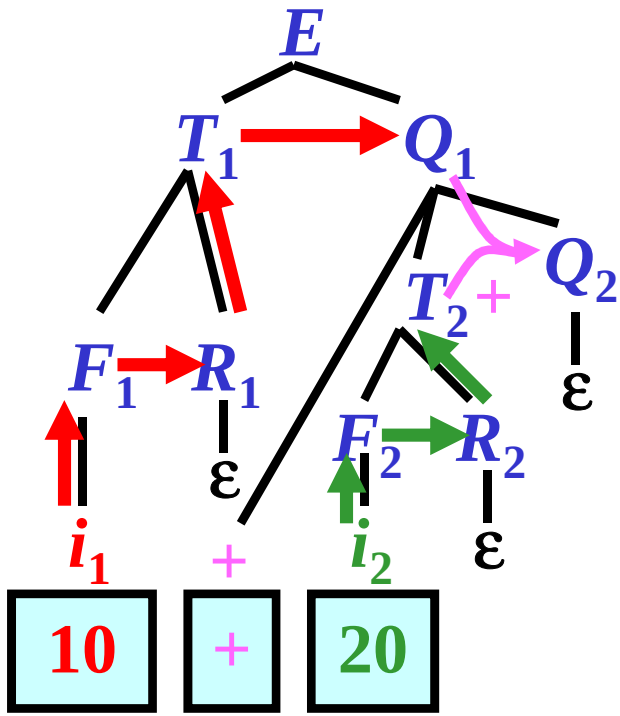
Parser pushdown:

$\{Q_1.s := Q_2.s\}$
$\{E.s := Q_1.s\}$
$

Semantic pushdown:

$Q_2.s = 30$

Illustration:



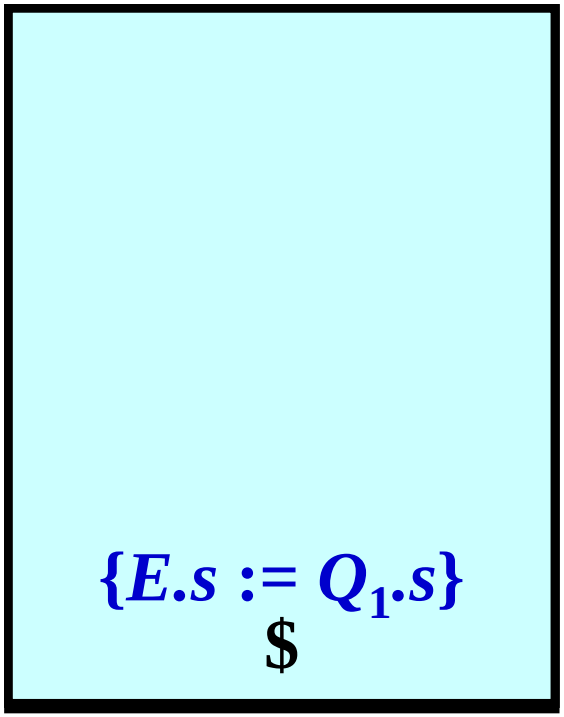
Evaluation of Expressions: Example 16/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

Parser pushdown:



Semantic pushdown:

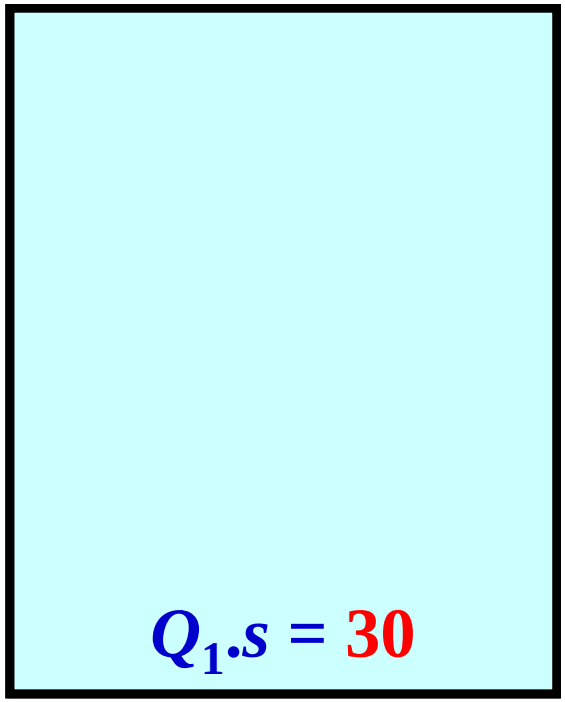
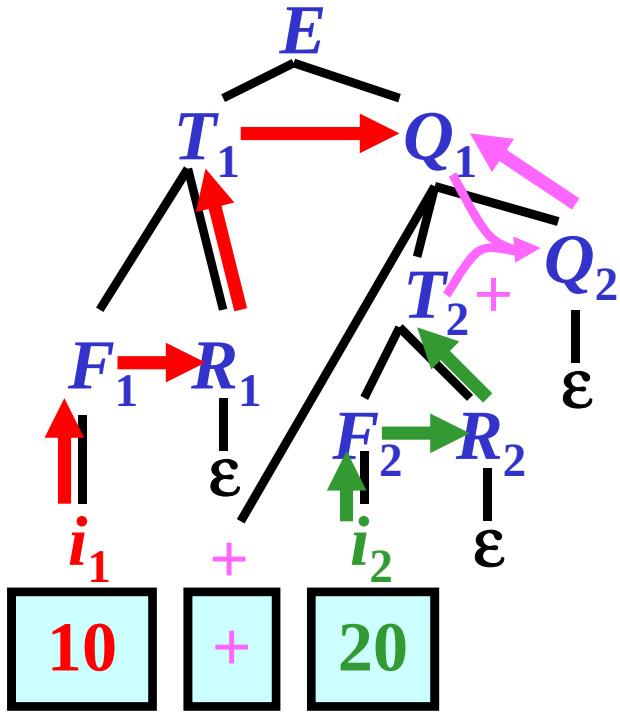


Illustration:



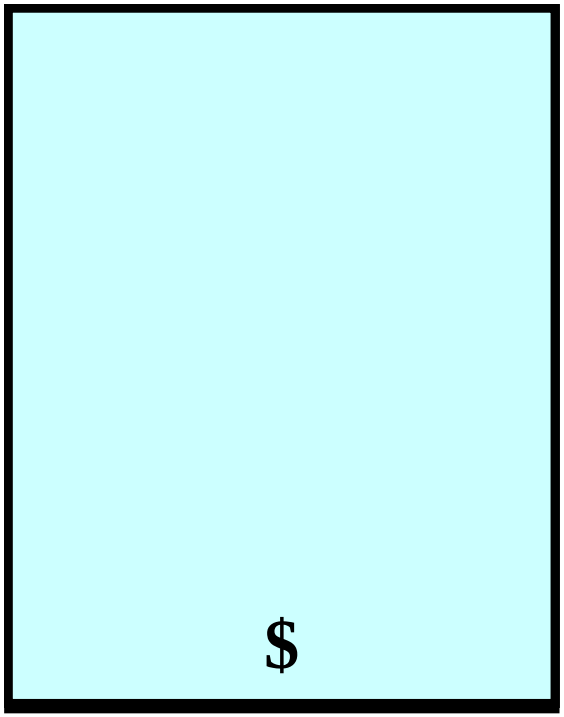
Evaluation of Expressions: Example 16/16

Example for *a* + *b*, where *a.value* = 10, *b.value* = 20

Input: $

Rule:

Parser pushdown:



Semantic pushdown:

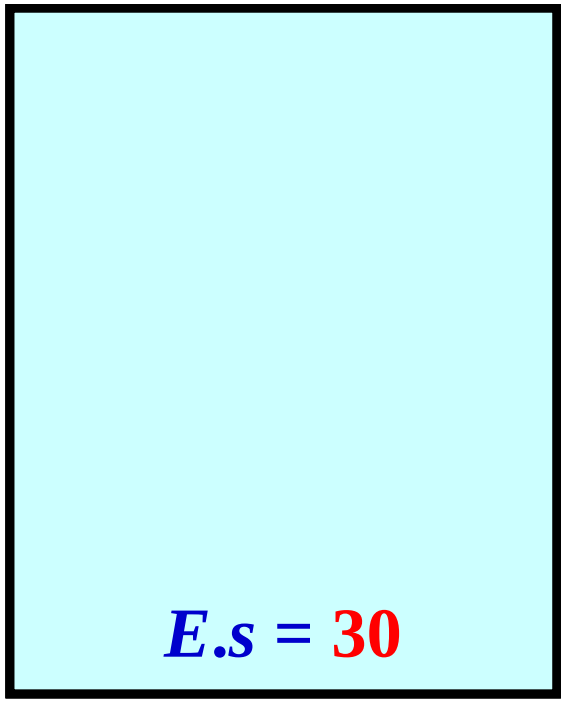
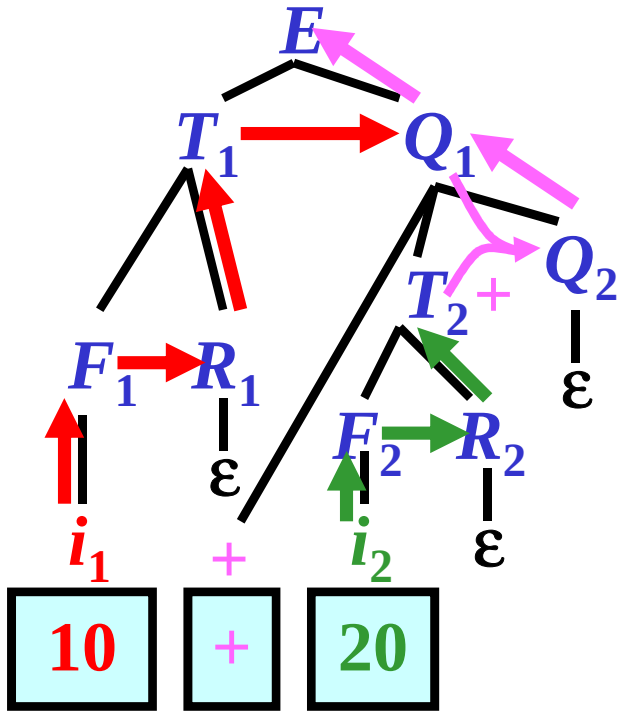
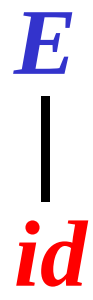


Illustration:



Semantic Analysis: Type Checking

1) **Rule:**

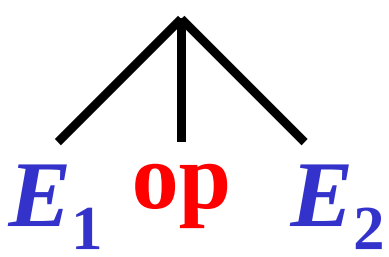


Action:

***E*.type := *id*.type**

---

2) **Rule:**



Operation op is defined over types:

$$t_1 \ \mathbf{op} \ t_2 \rightarrow t_3$$

Action:

if (*E*$_1$.type = t_1 **or**
E$_1$.type is convertable to t_1)
and
(*E*$_2$.type = t_2 **or**
E$_2$.type is convertable to t_2)
then
E.type := t_3
else
Semantic Error.

Type Checking: Example 1/3

- **Make a type-checking for a grammar:**
- $G_{expr1} = (N, T, P, E)$, where $N = \{E, F, T\}$, $T = \{i, +, *, (,)\}$,
  $P = \{ E \to E+T, E \to T, T \to T*F, T \to F, F \to (E), F \to i \}$

- **Operators *, + are defined as:**
  - **int * int → int**
  - **int + int → int**
  - **real * real → real**
  - **real + real → real**

Possible Conversion:

- **From int to real**

Rule: $F \to i$	{*F.type* := *i.type*; generate(:=, *i.loc*, ,*F.loc*) }
Rule: $F_i \to (E_j)$	{F_i.*type* := E_j .*type*}
Rule: $T_i \to F_j$	{T_i.*type* := F_j .*type*}
Rule: $E_i \to T_j$	{E_i.*type* := T_j .*type*}

Type Checking: Example 2/3

Rule: $E_i \rightarrow E_j + T_k$ { **if** E_j **.type** = T_k**.type then begin**
E_i**.type** := E_j**.type**
generate(+, E_j**.loc**, T_k**.loc**, E_i**.loc**)
end
else begin
generate(***new.loc***, h, ,)
if E_j **.type** = ***int*** **then begin**
generate(***int-to-real***, E_j**.loc** , , h)
generate(+, h, T_k**.loc**, E_i**.loc**)
end
else begin
generate(***int-to-real***, T_k**.loc** , , h)
generate(+, E_j**.loc**, h, E_i**.loc**)
end
E_i**.type** := ***real***
end
}

Type Checking: Example 3/3

Rule: $T_i \rightarrow T_j * F_k$ {

```
if Tj.type = Fk.type then begin
    Ti.type := Tj.type
    generate(*, Tj.loc, Fk.loc, Ti.loc)
end
else begin
    generate(new.loc, h, , )
    if Tj.type = int then begin
        generate(int-to-real, Tj.loc , , h)
        generate(*, h, Fk.loc, Ti.loc)
    end
    else begin
        generate(int-to-real, Fk.loc , , h)
        generate(*, Tj.loc, h, Ti.loc)
    end
    Ti.type := real
 end
}
```

Short Evaluation (Jumping Code)

Idea:

- ***a*** **=** ***true*** **implies** ***a*** **or (… ? …) =** ***true***
- ***a*** **=** ***false*** **implies** ***a*** **and (… ? …) =** ***false***

Note: (… ? …) is <u>not evaluated</u>.

---

1) (*a* and *b*) = *p*:

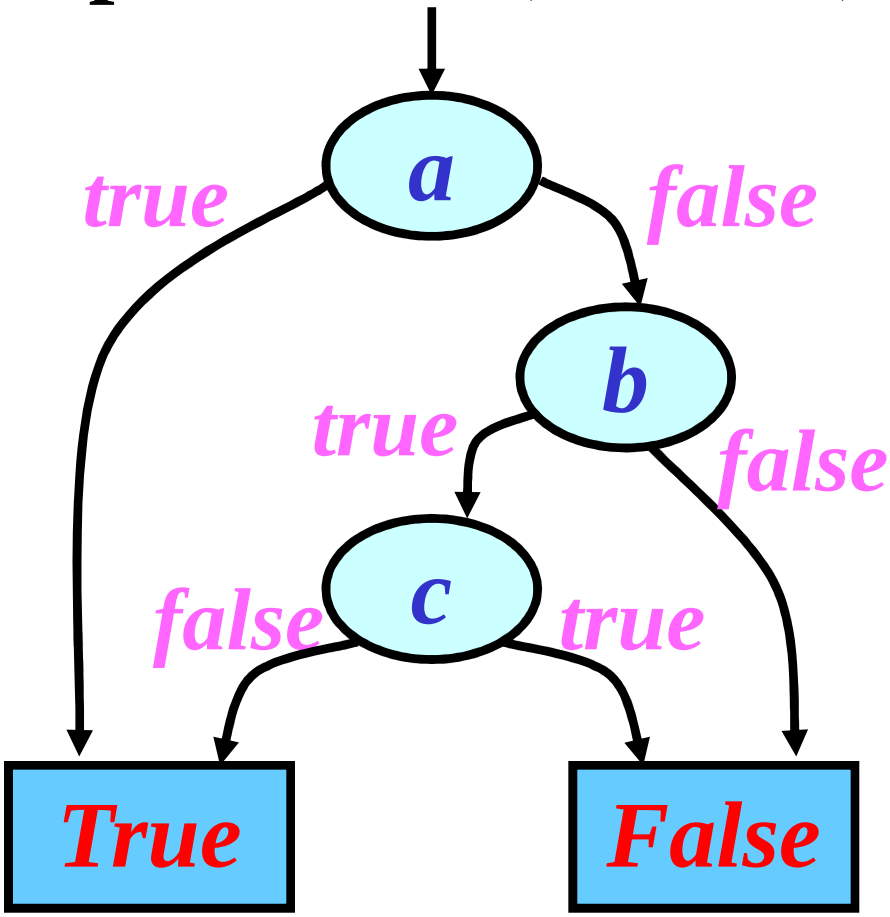
if ***a*** **=** ***false*** **then** ***p*** **=** ***false***
else ***p*** **=** ***b***

2) (*a* or *b*) = *p*:

if ***a*** **=** ***true*** **then** ***p*** **=** ***true***
else ***p*** **=** ***b***

Short Evaluation: Graphic Representation

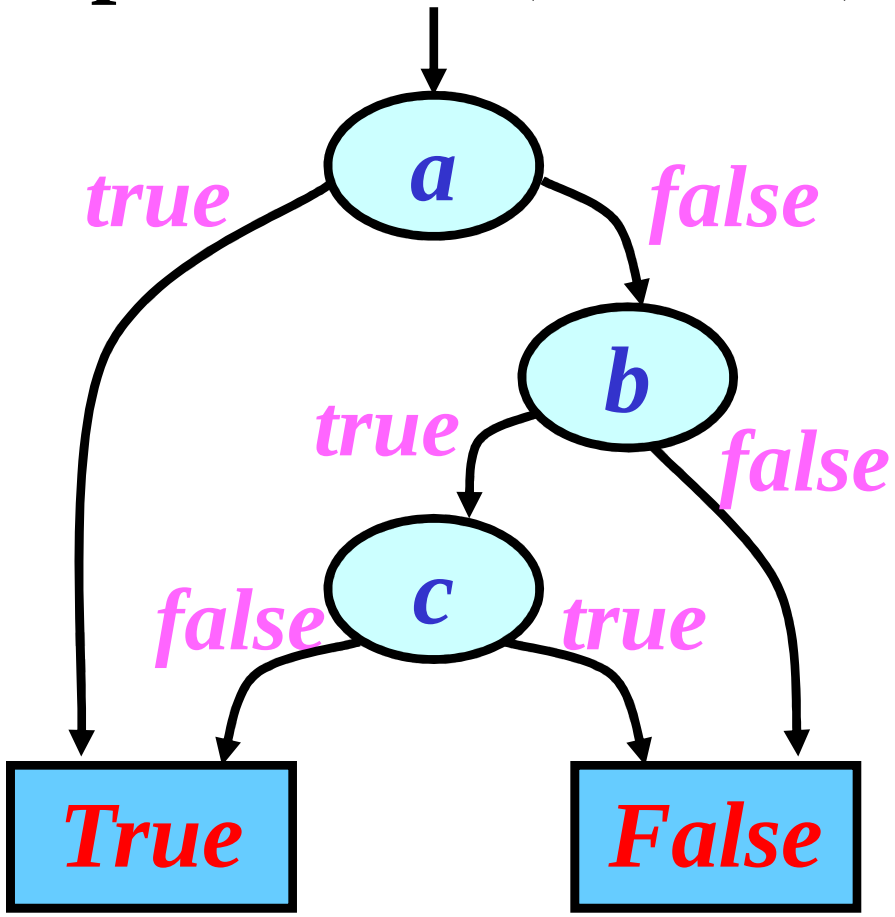
Example: *a* or (*b* and (not *c*)):



- Simulation of this graphic representation by 3AC jumps

Short Evaluation: Graphic Representation

Example: *a* or (*b* and (not *c*)):



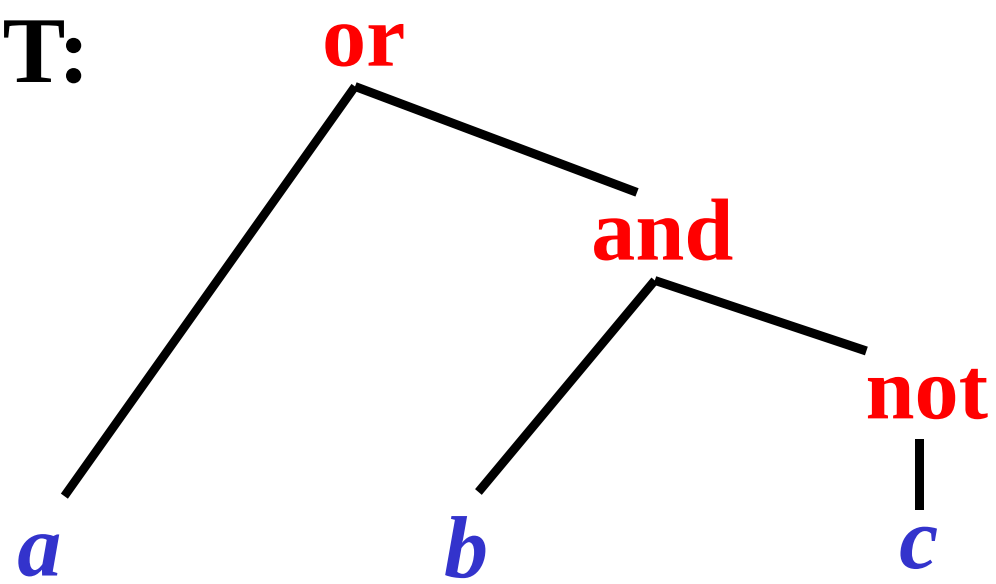

```
if a goto True
goto X
X:
if b goto Y
goto False
Y:
if c goto False
goto True
True: …
False: …
```

- Simulation of this graphic representation by 3AC jumps

Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b* and (not *c*)):**

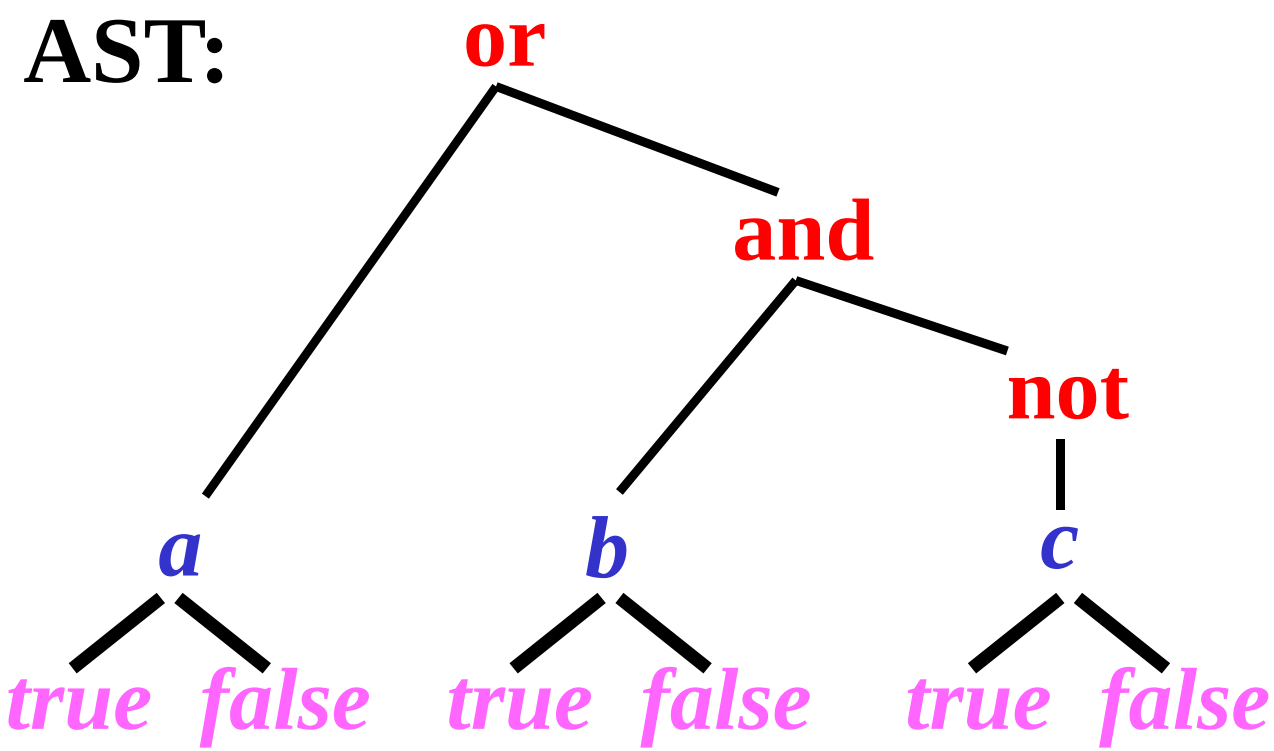
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b*** **and (not** ***c*****)):**

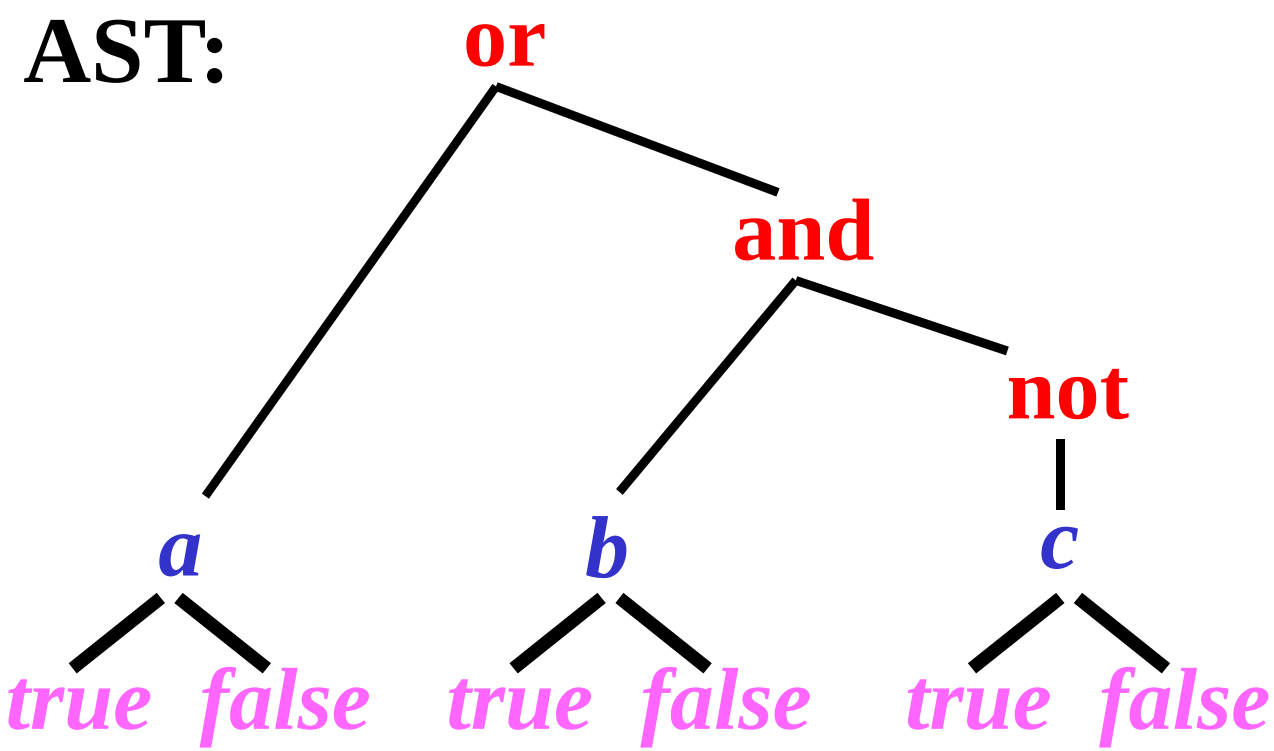
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b*** **and (not *c*)):**

AST:



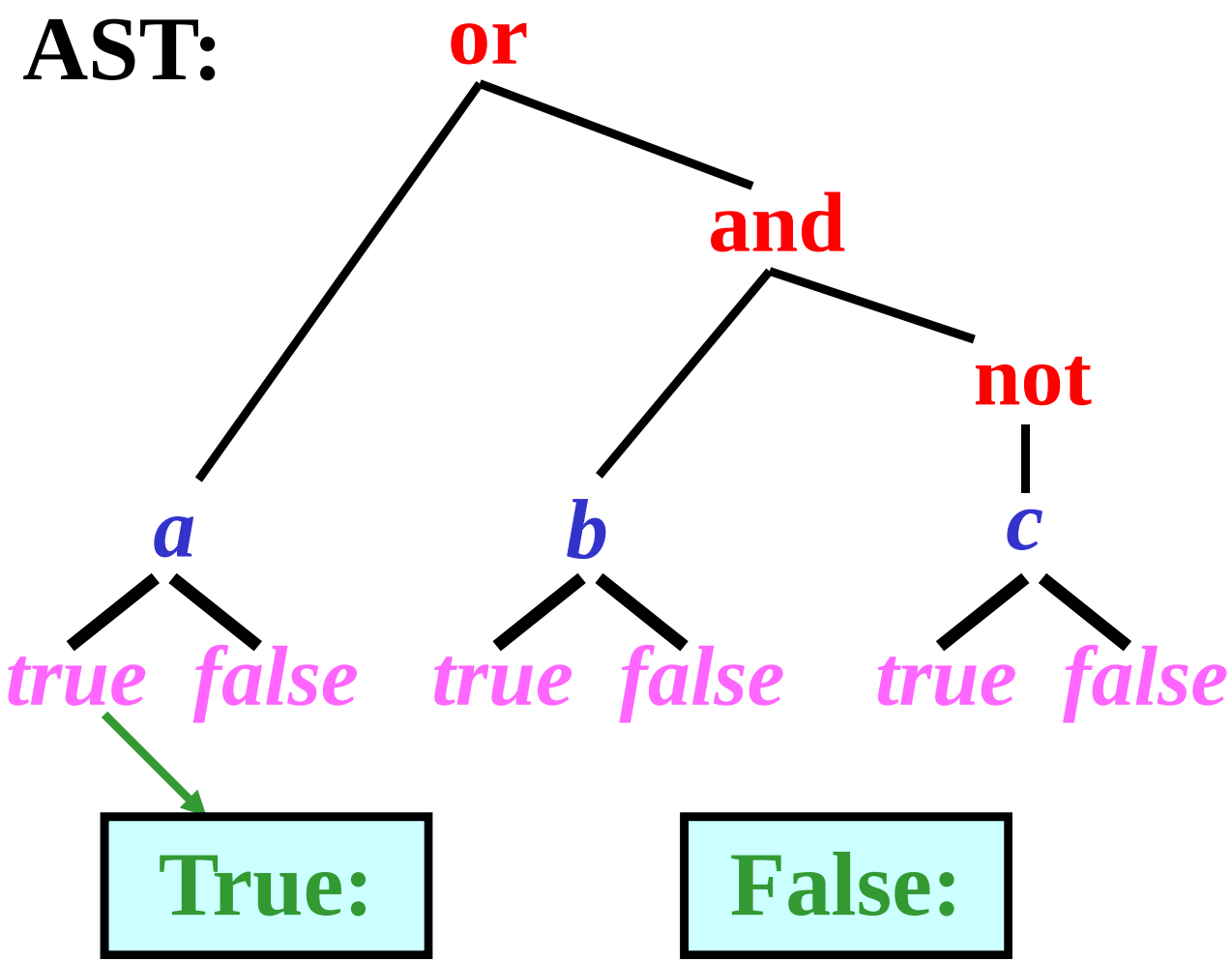
True:

False:

Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b*** **and (not** ***c*****)):**

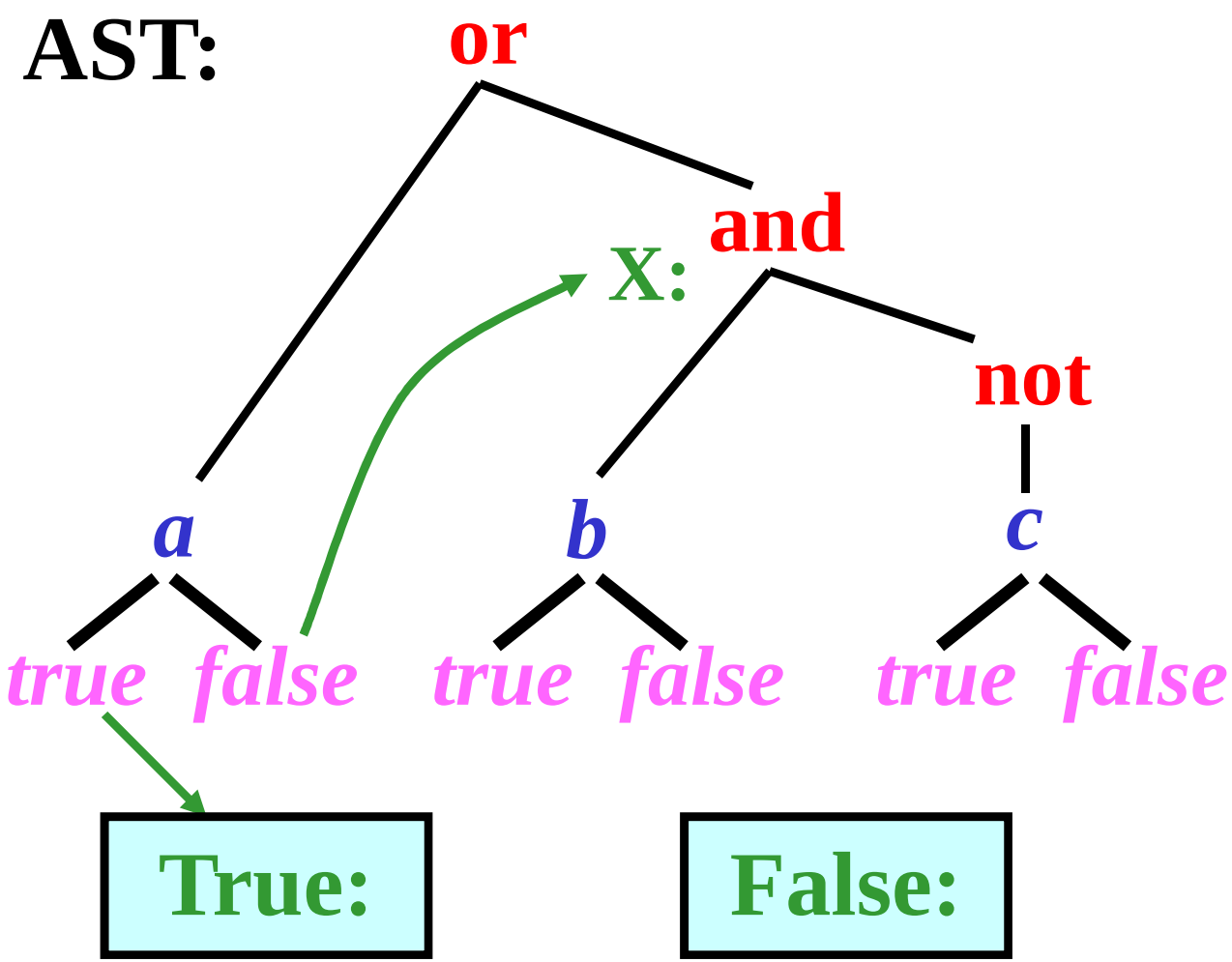
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b*** **and (not** ***c*****)):**

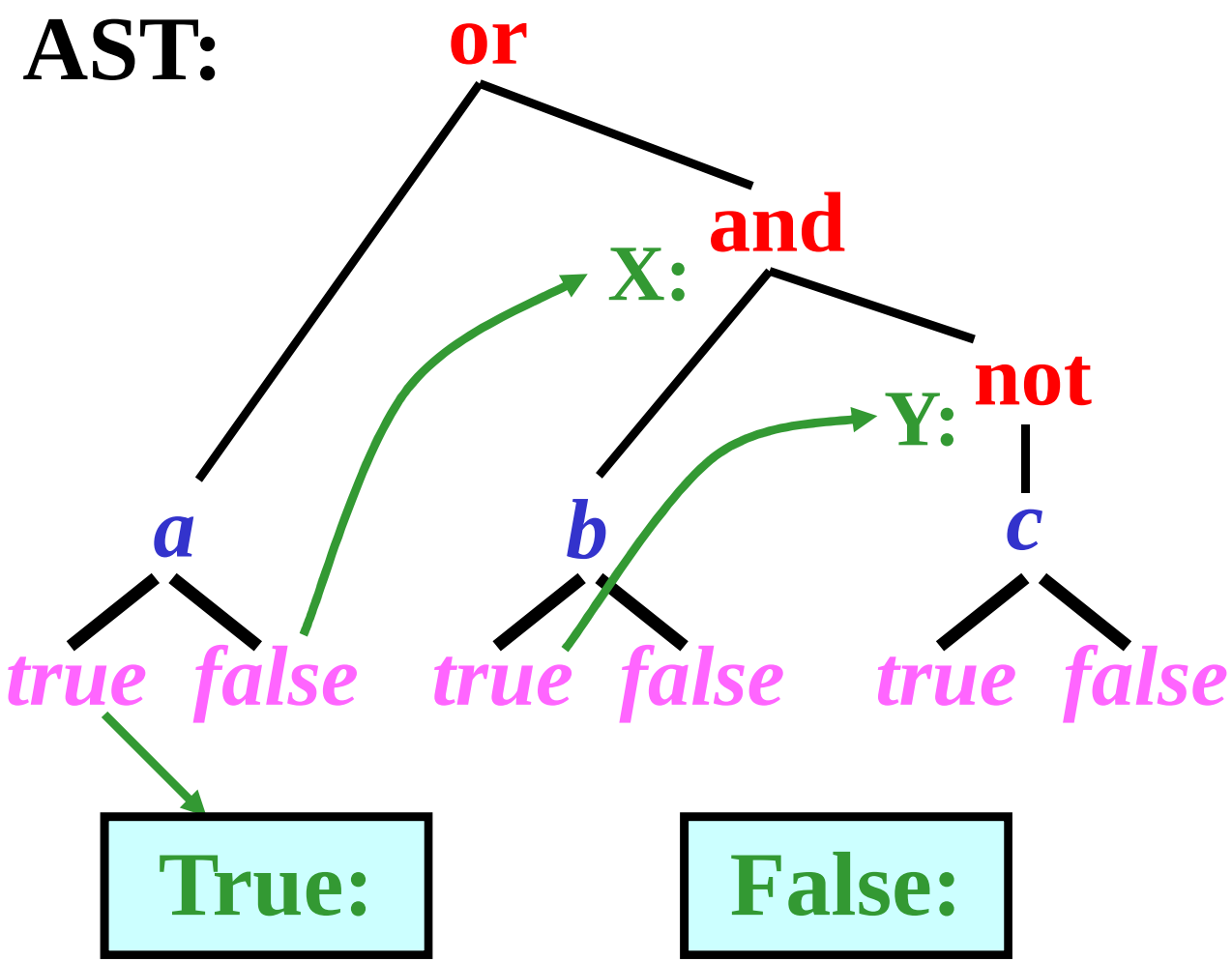
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b*** **and (not** ***c*****)):**

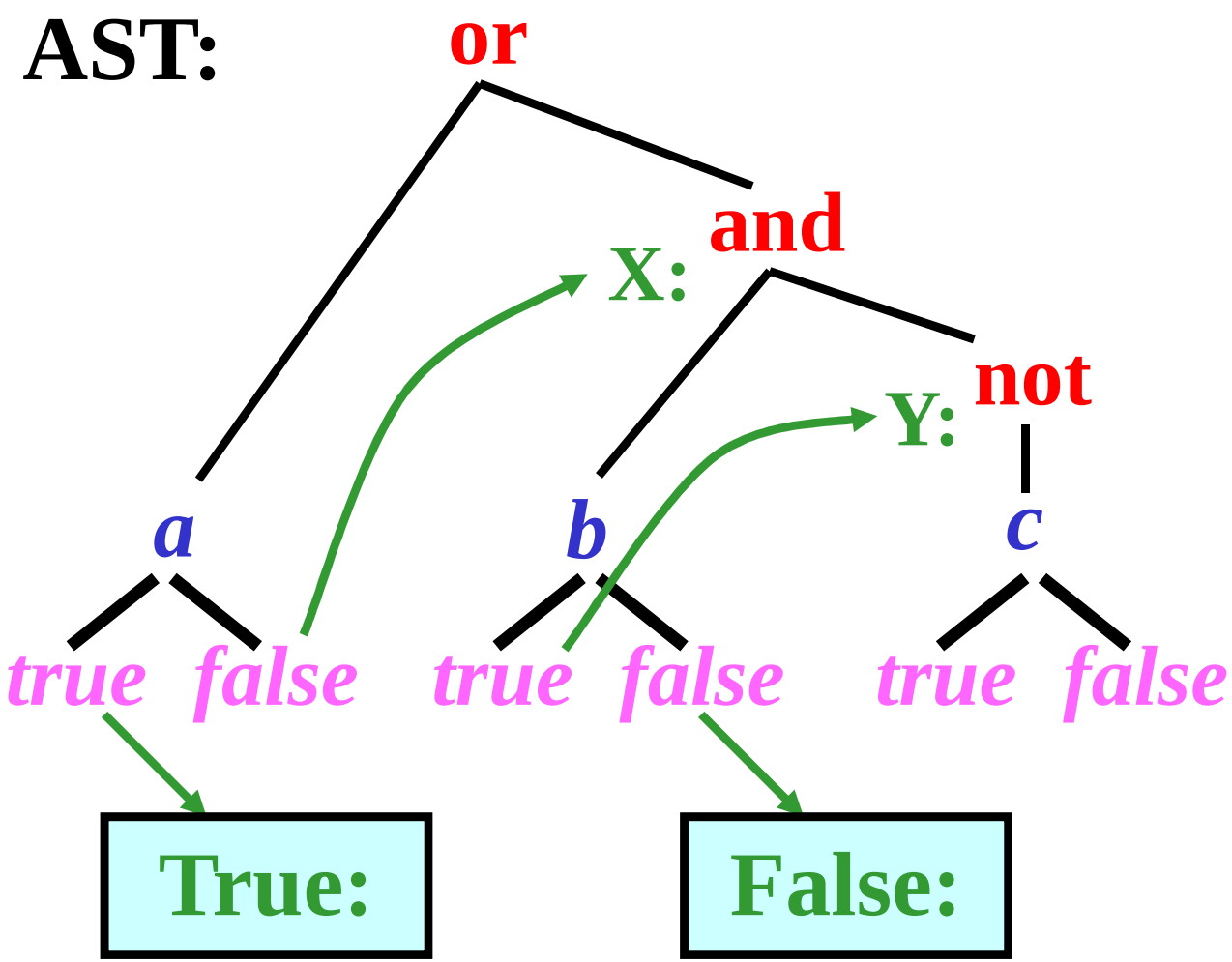
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b*** **and (not** ***c*****)):**

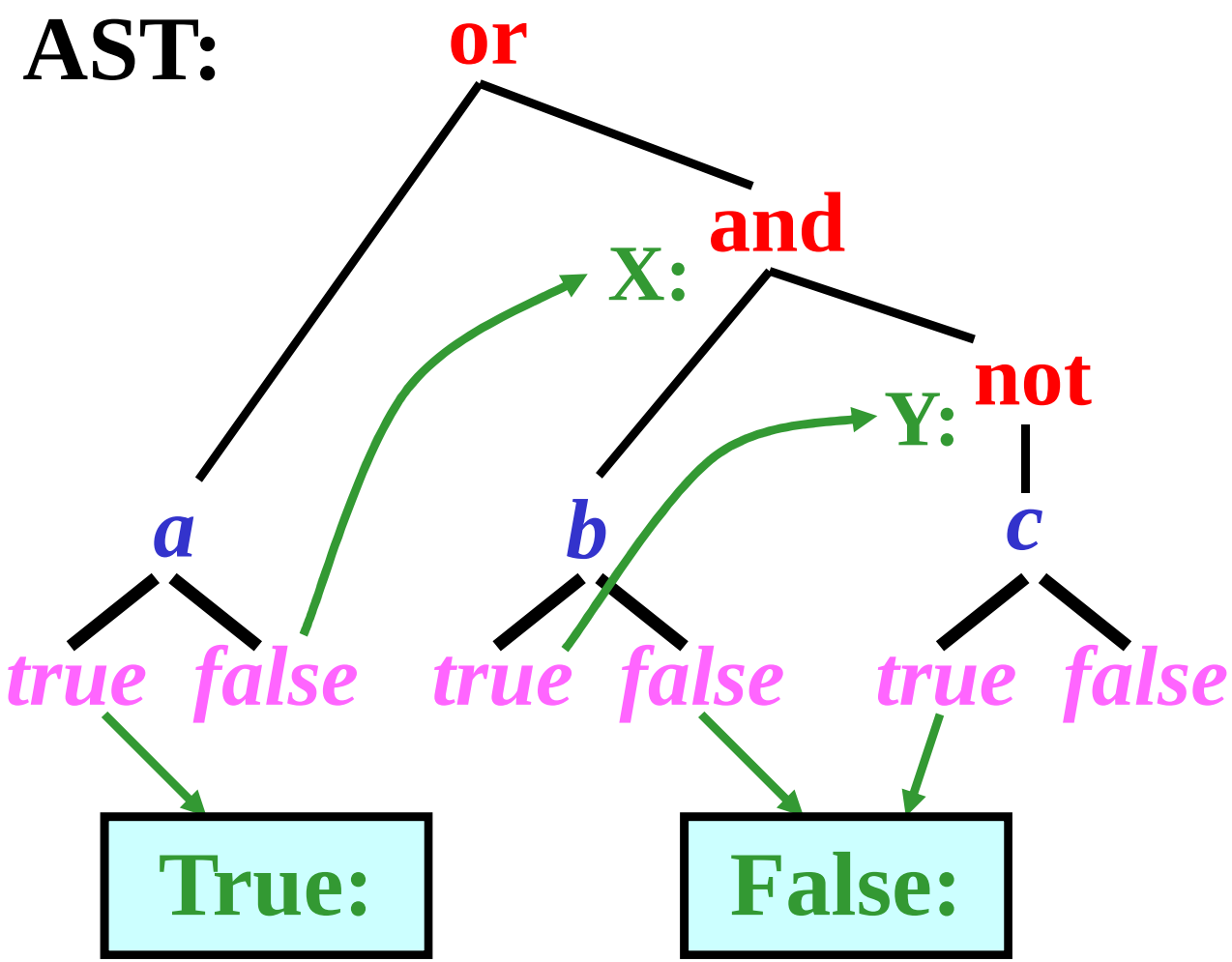
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (*b* and (not *c*)):**

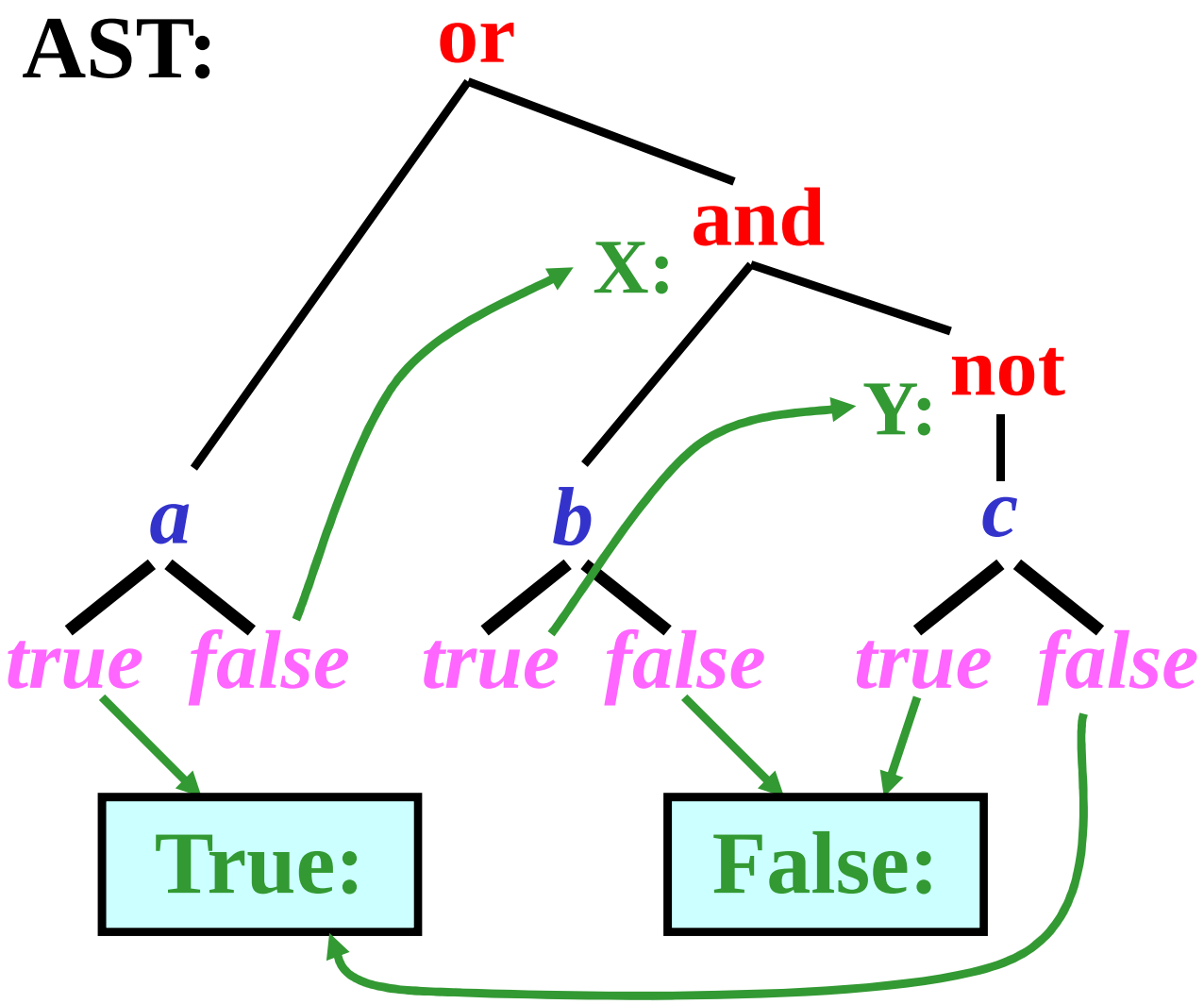
AST:



Short Evaluation Using AST: Introduction

Example: ***a*** **or (** ***b*** **and (not** ***c*****)):**

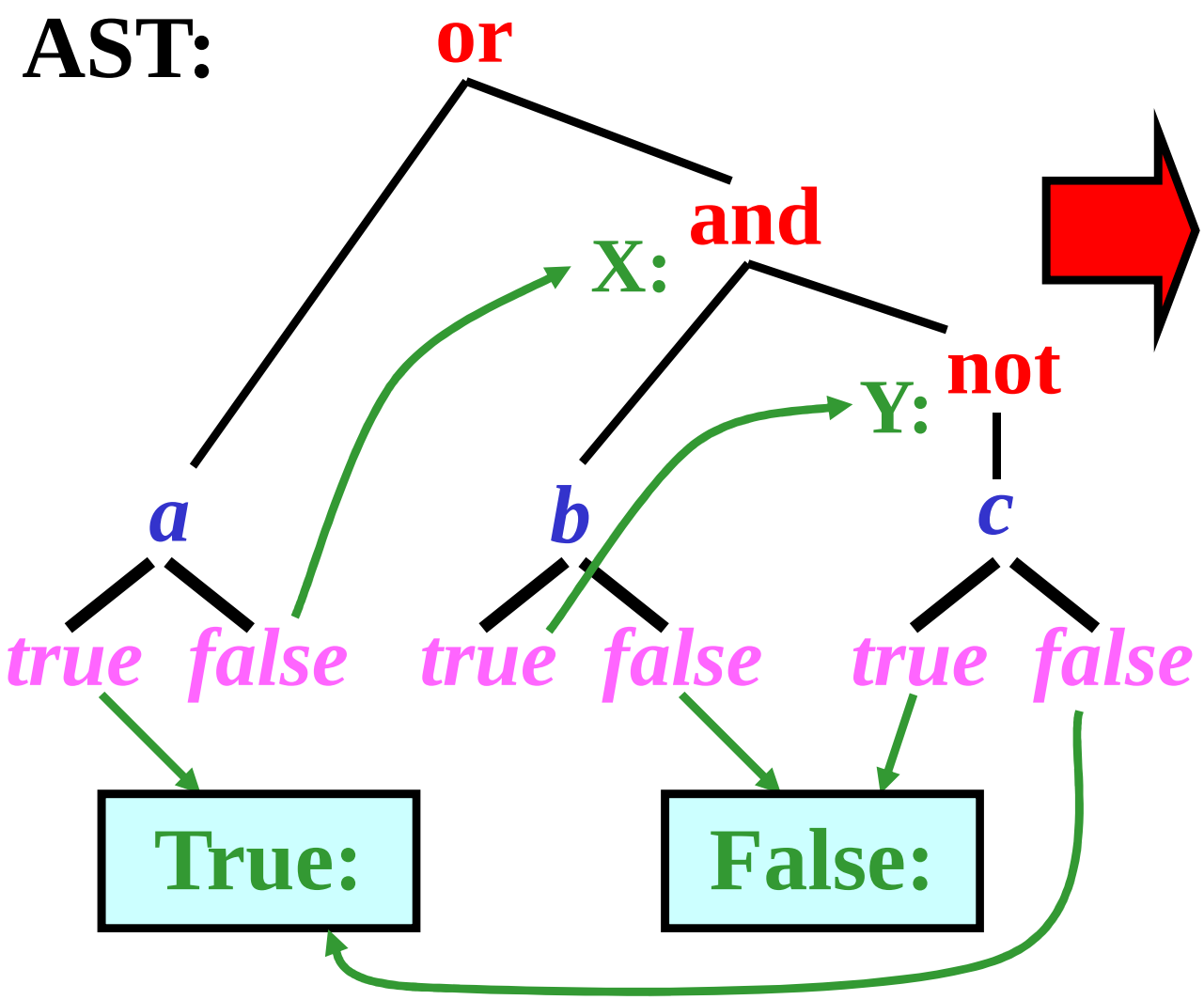
AST:



Short Evaluation Using AST: Introduction

Example: *a* or (*b* and (not *c*)):

AST:



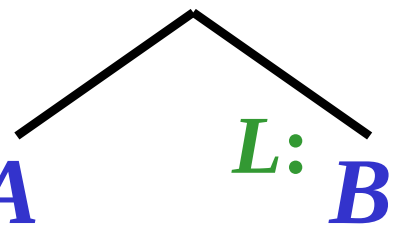

```
if a goto True
goto X
X:
if b goto Y
goto False
Y:
if c goto False
goto True
True: …
False: …
```

Short Evaluation Using AST: Implementation

• Every AST node, ***X***, has assigned two attributes ***X.t***, ***X.f***

Elementary ASTs:

1)

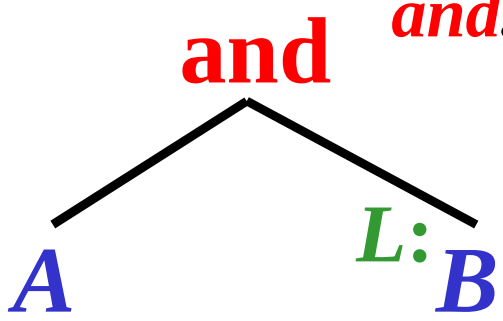


or.t
or.f

A.t := ***or.t*** ***B.t*** := ***or.t***
A.f := ***L*** ***B.f*** := ***or.f***

• **Note:** ***L*** = a new label

2)



and.t
and.f

A.t := ***L*** ***B.t*** := ***and.t***
A.f := ***and.f*** ***B.f*** := ***and.f***

• **Note:** ***L*** = a new label

3)

not.t
not.f

A.t := ***not.f***
A.f := ***not.t***

• **Initialization:** Let ***R*** is the root of AST, then:

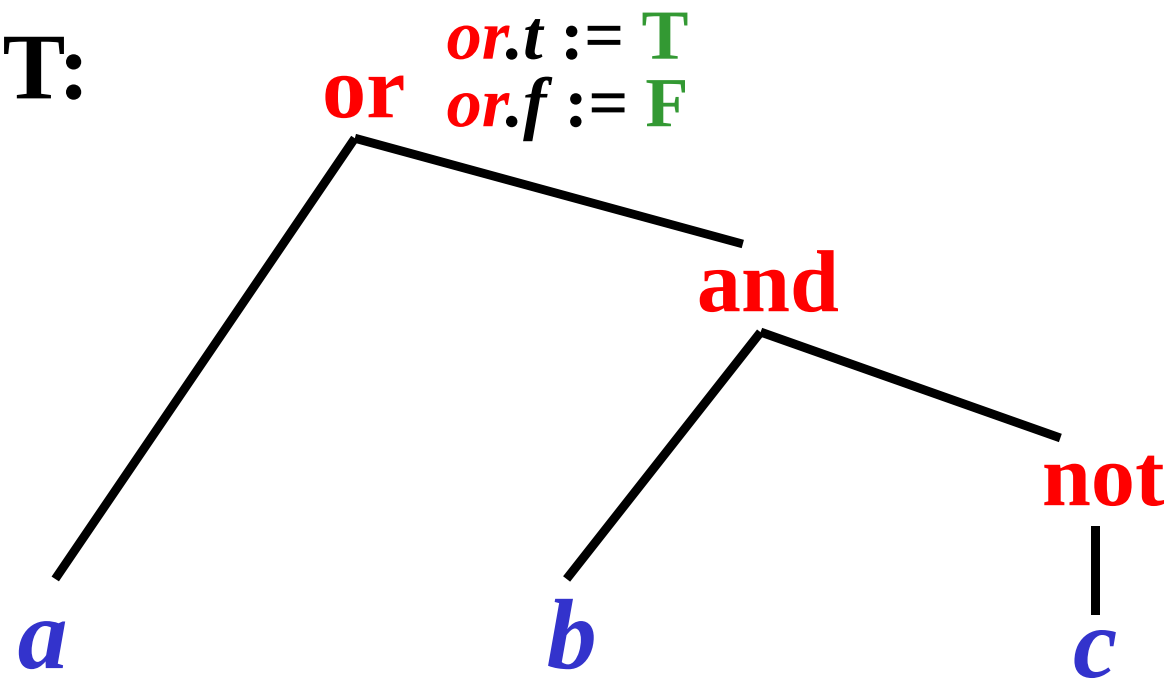
R.t := **True**, ***R.f*** := **False** (**True** & **False** are labels)

• **Propagation:** Attributes are propagated from root to leaves in AST using rules **1)**, **2)** and **3)**.

Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:

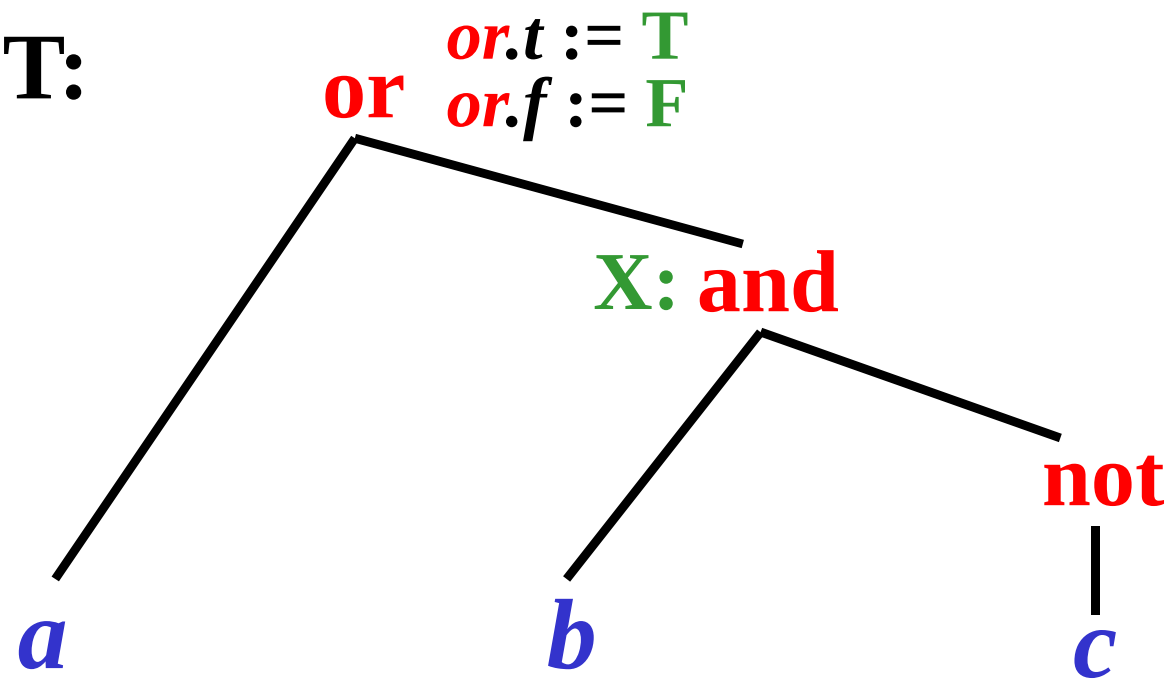


Note:
- **T** = ***True***
- **F** = ***False***

Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:

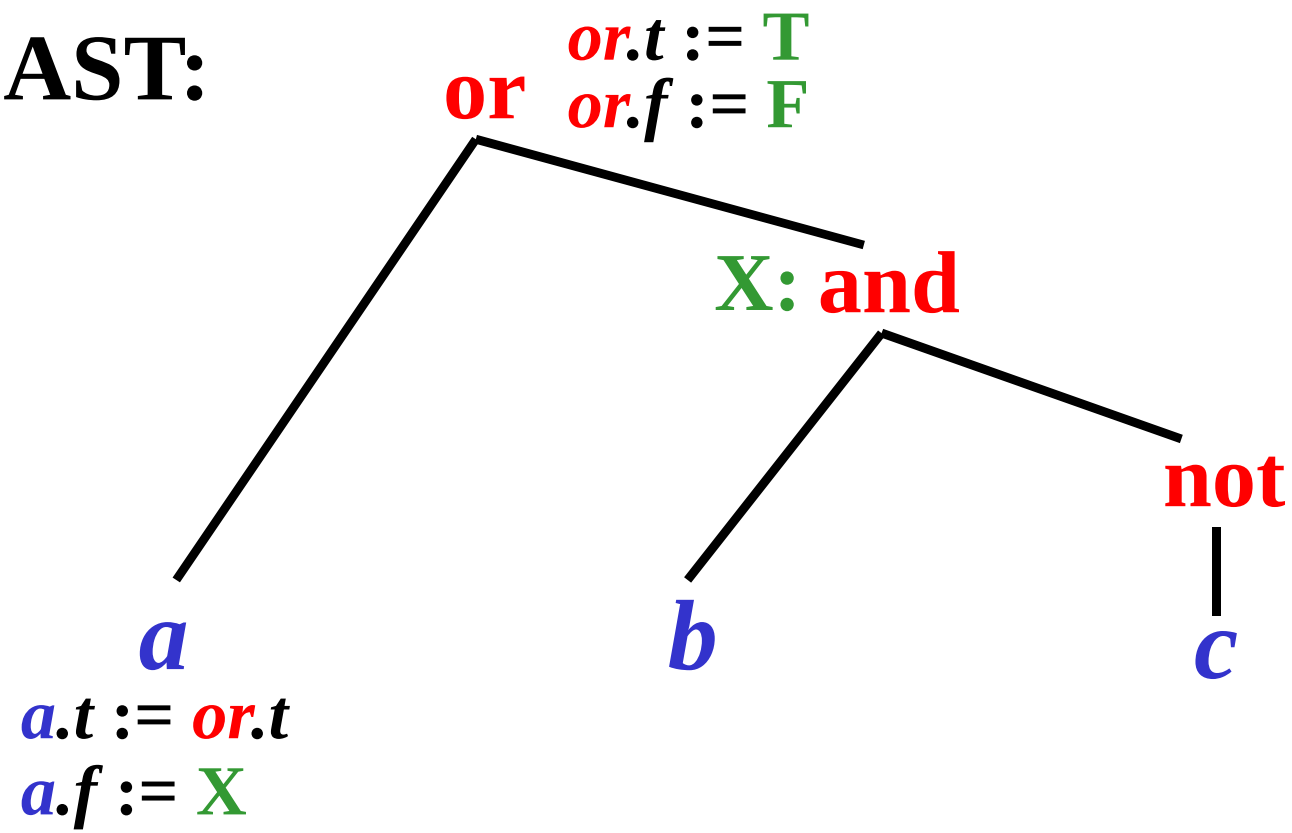


Note:
- **T** = ***True***
- **F** = ***False***

Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:
- **T** = ***True***
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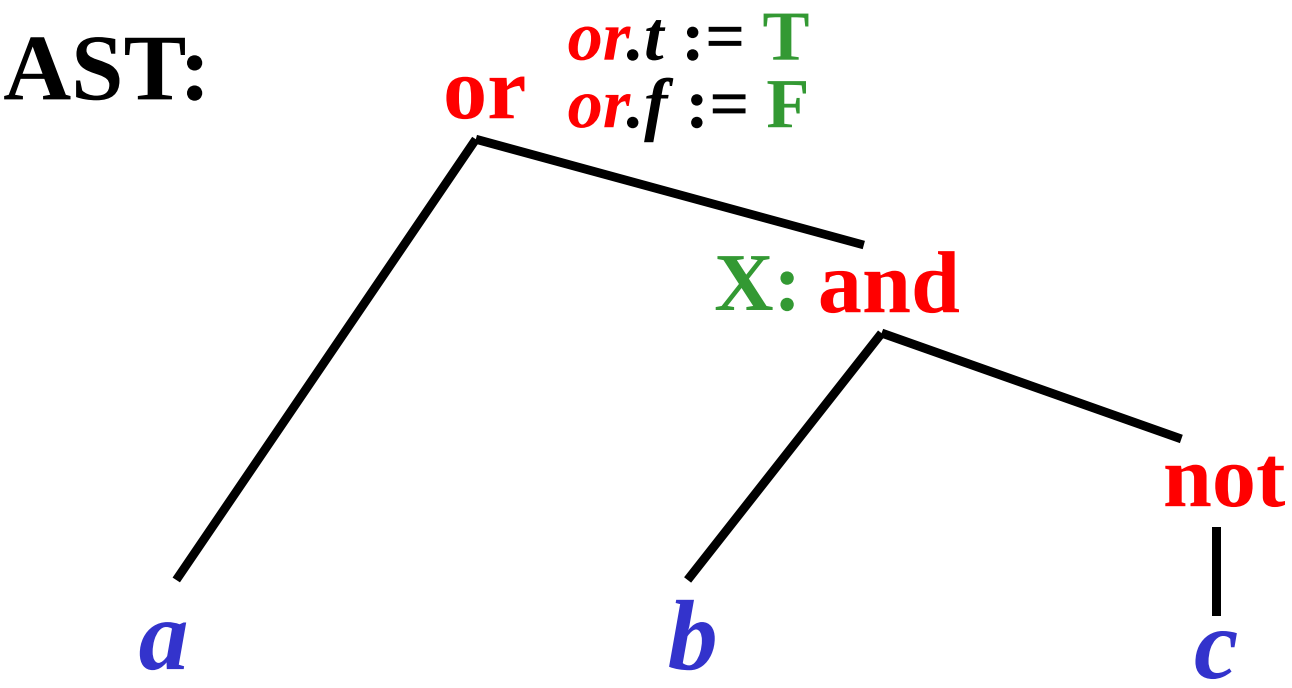
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:
- **T** = ***True***
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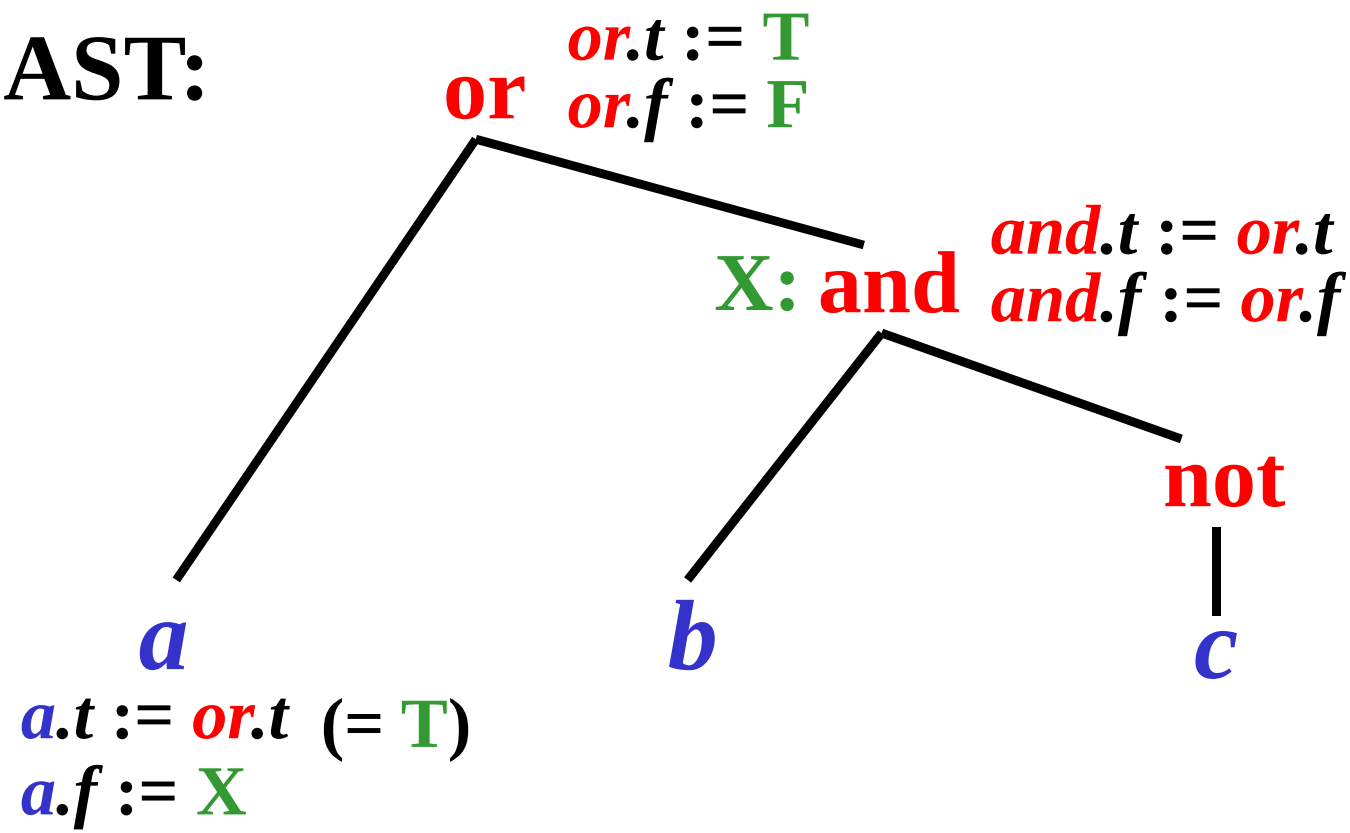
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:

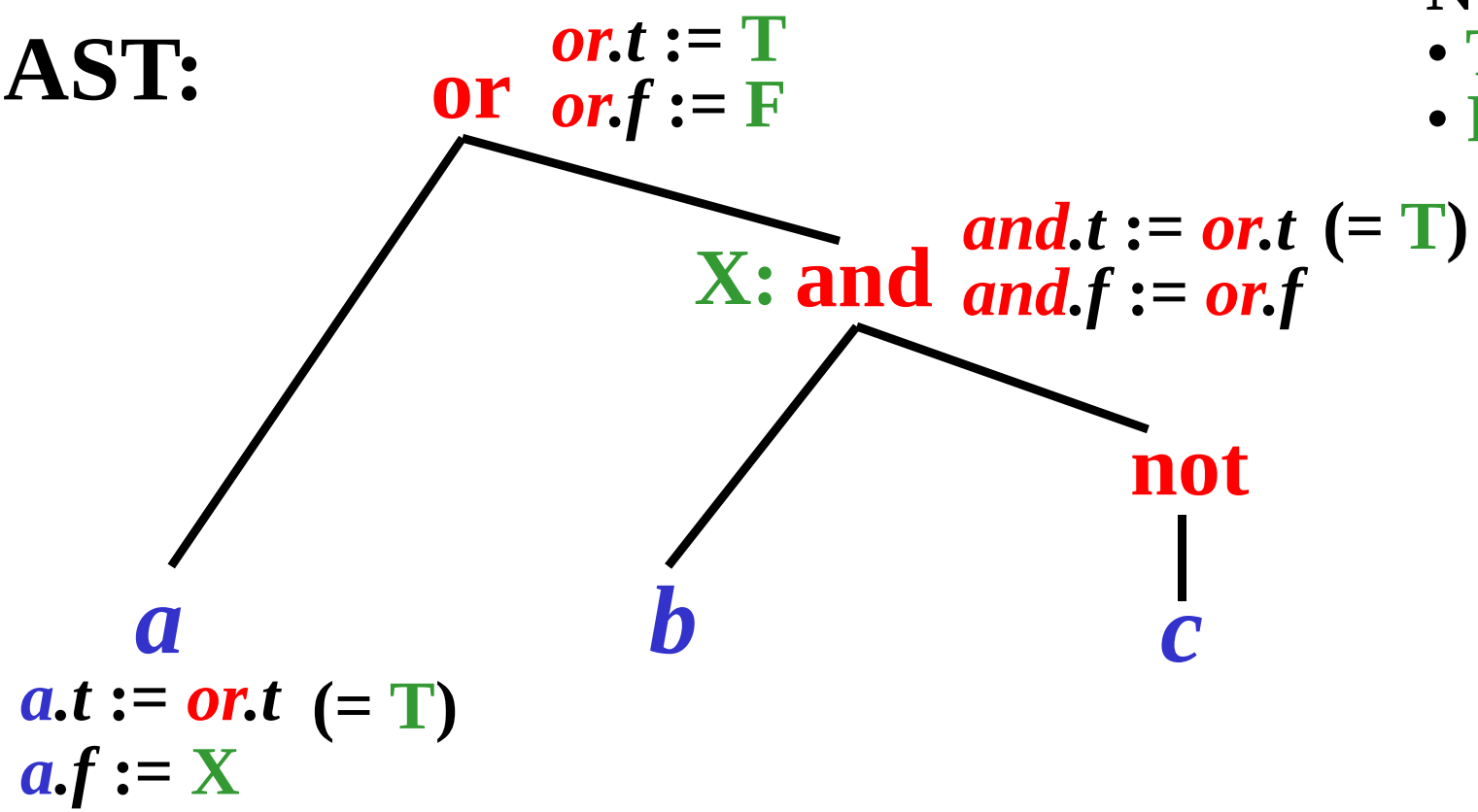


Note:
- **T** = ***True***
- **F** = ***False***

Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:
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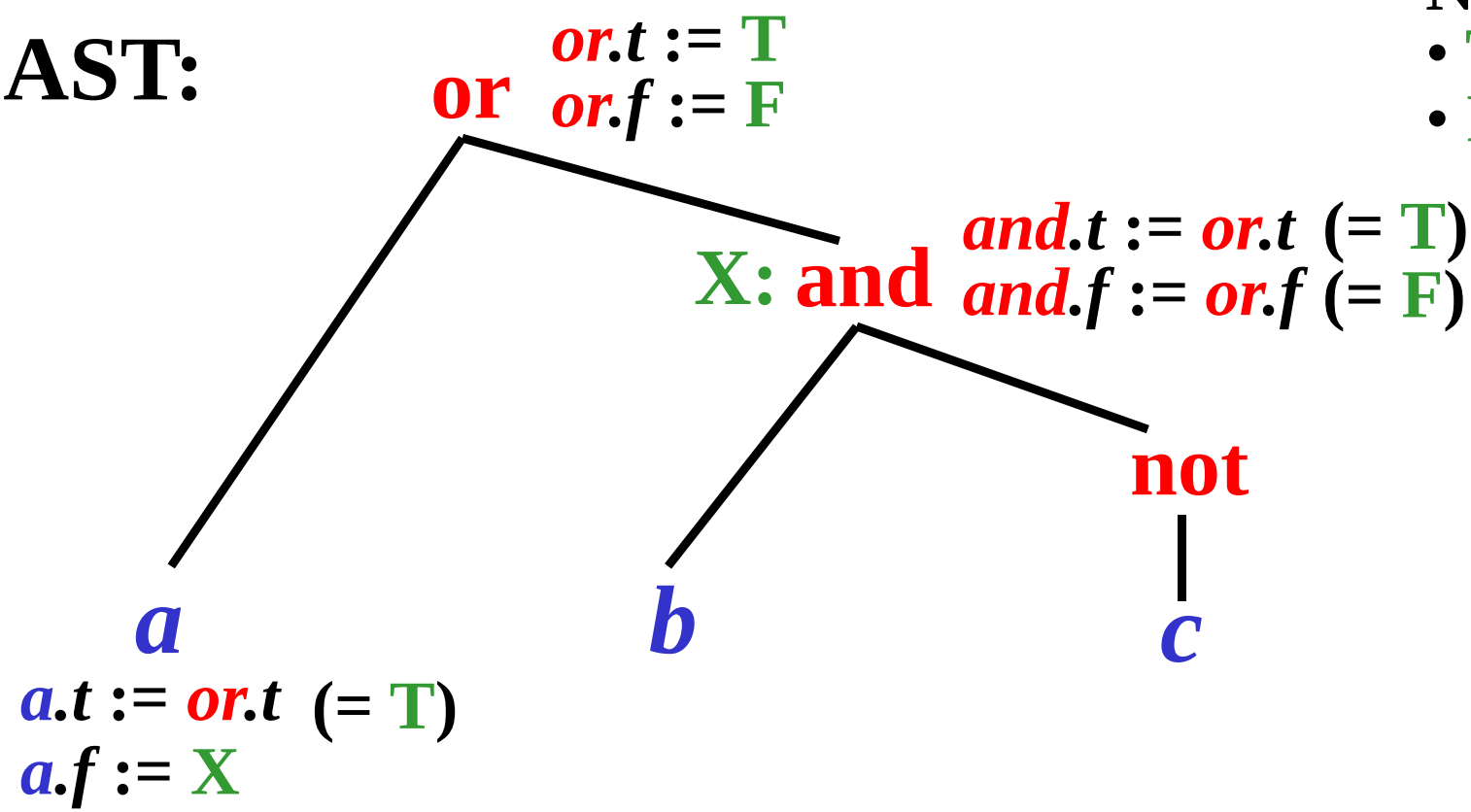
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:
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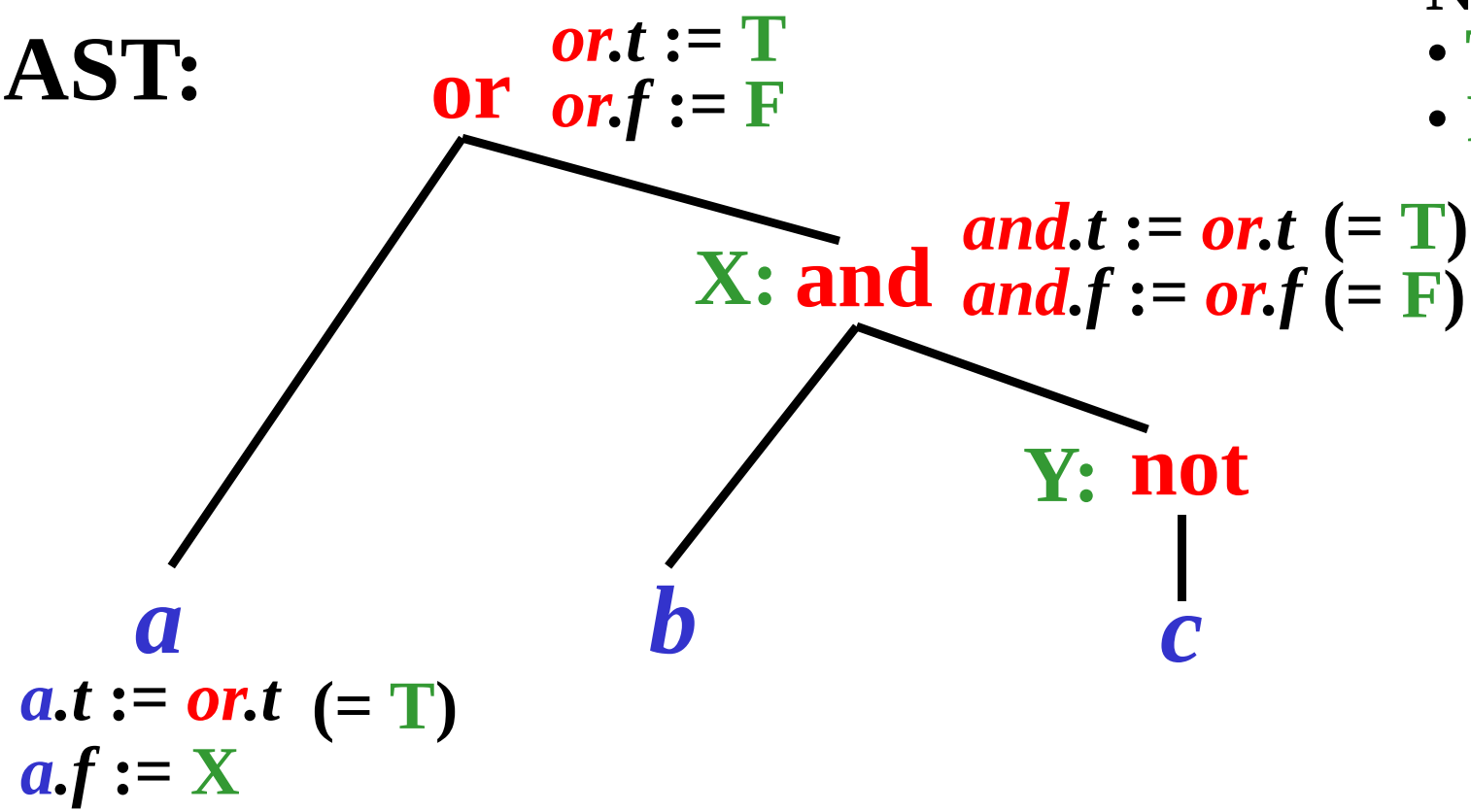
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:
- **T** = ***True***
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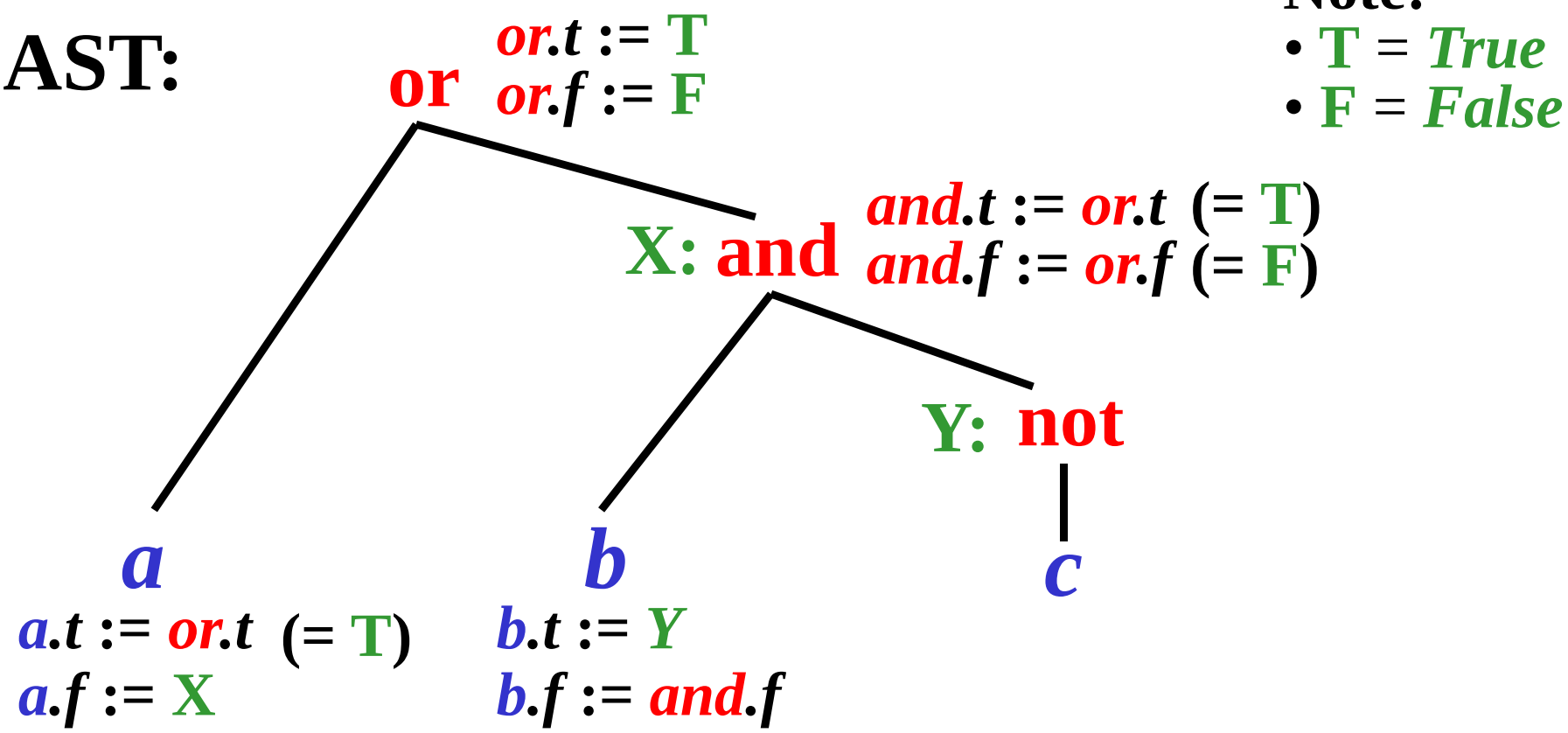
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:
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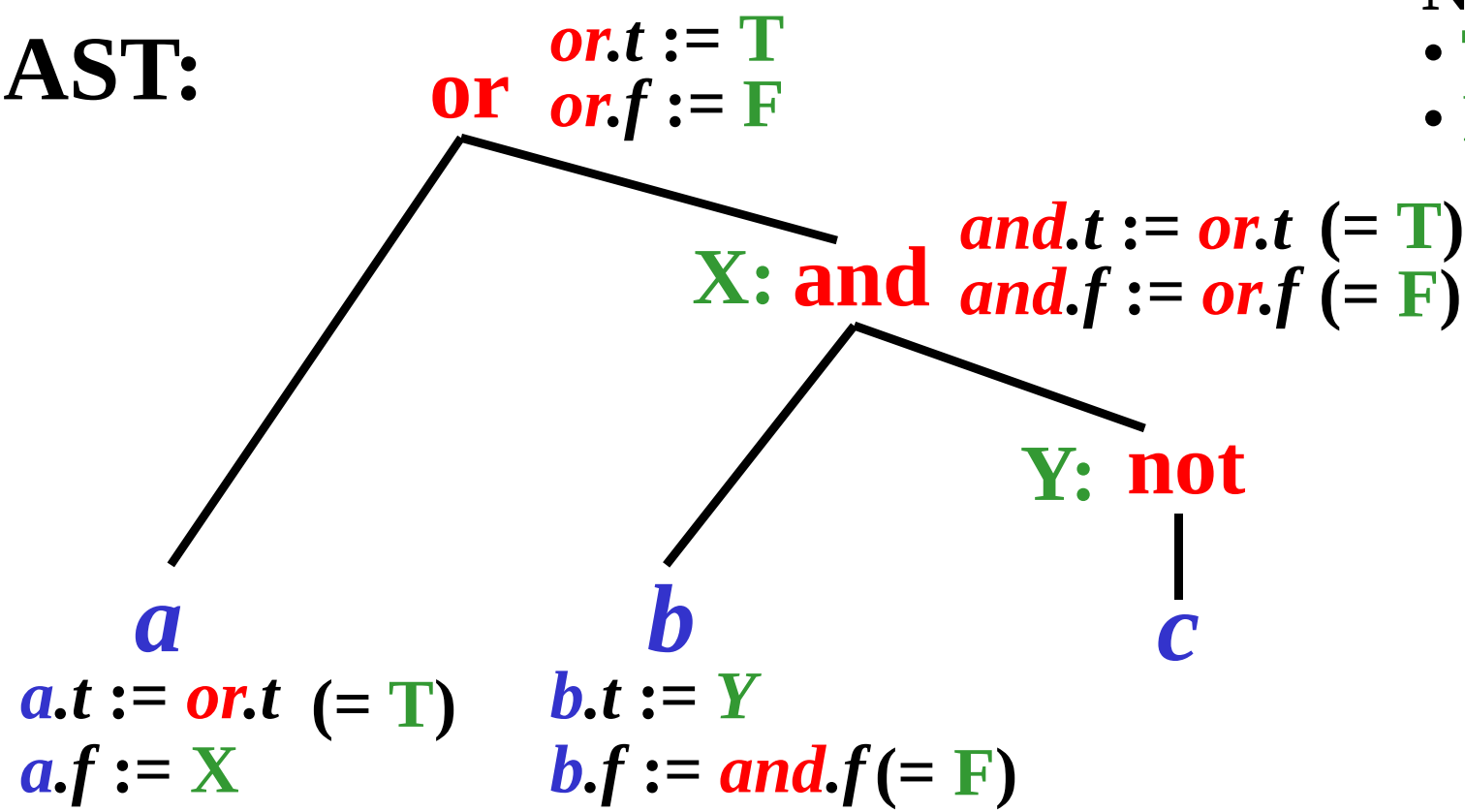
- **F** = ***False***

Short Evaluation Using AST: Example

Example: ***a*** **or (** ***b*** **and (not** ***c*****)):**

AST:



Note:
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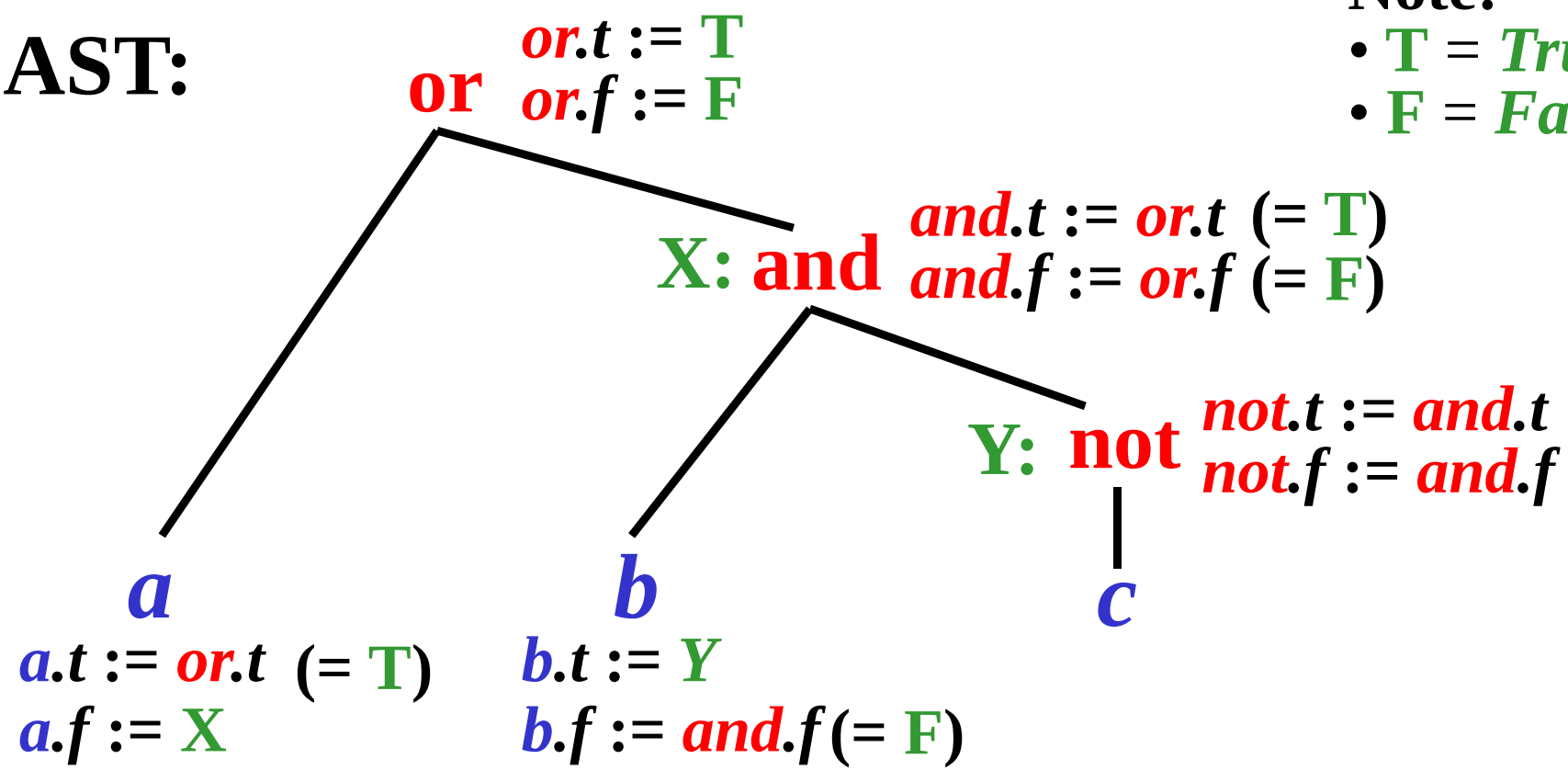
Short Evaluation Using AST: Example

Example: ***a*** **or (** ***b*** **and (not** ***c*****)):**

AST:



Note:

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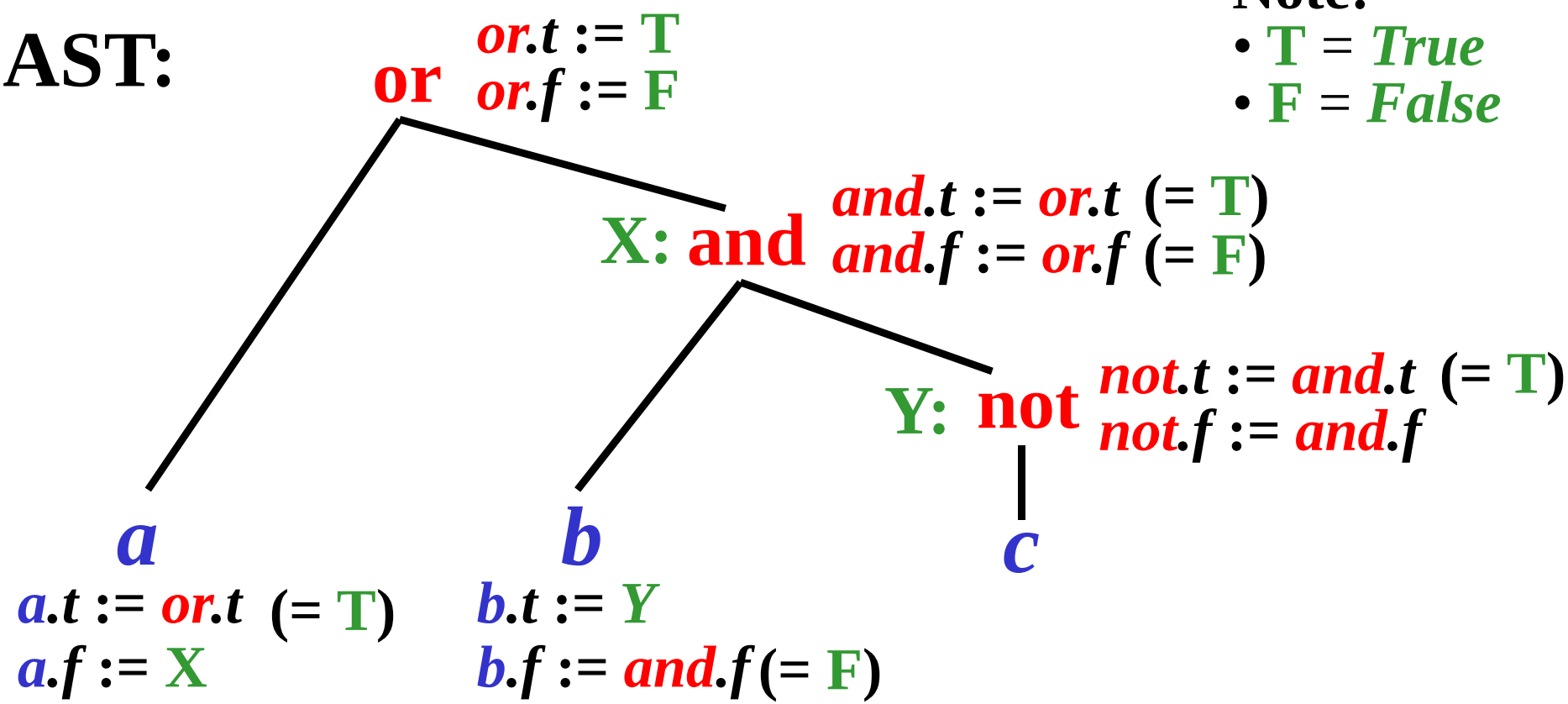
Short Evaluation Using AST: Example

Example: ***a*** **or (** ***b*** **and (not** ***c*****)):**

AST:



Note:

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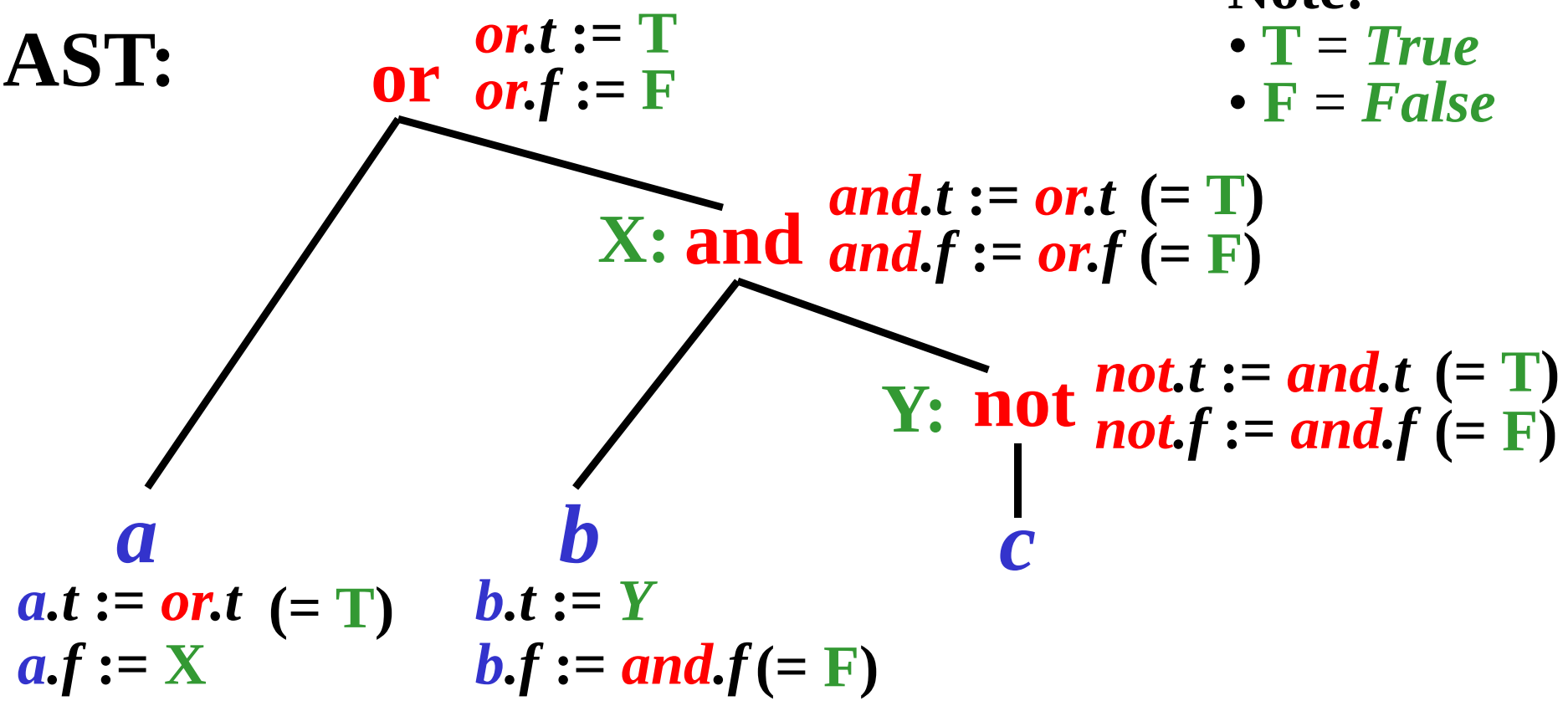
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



Note:

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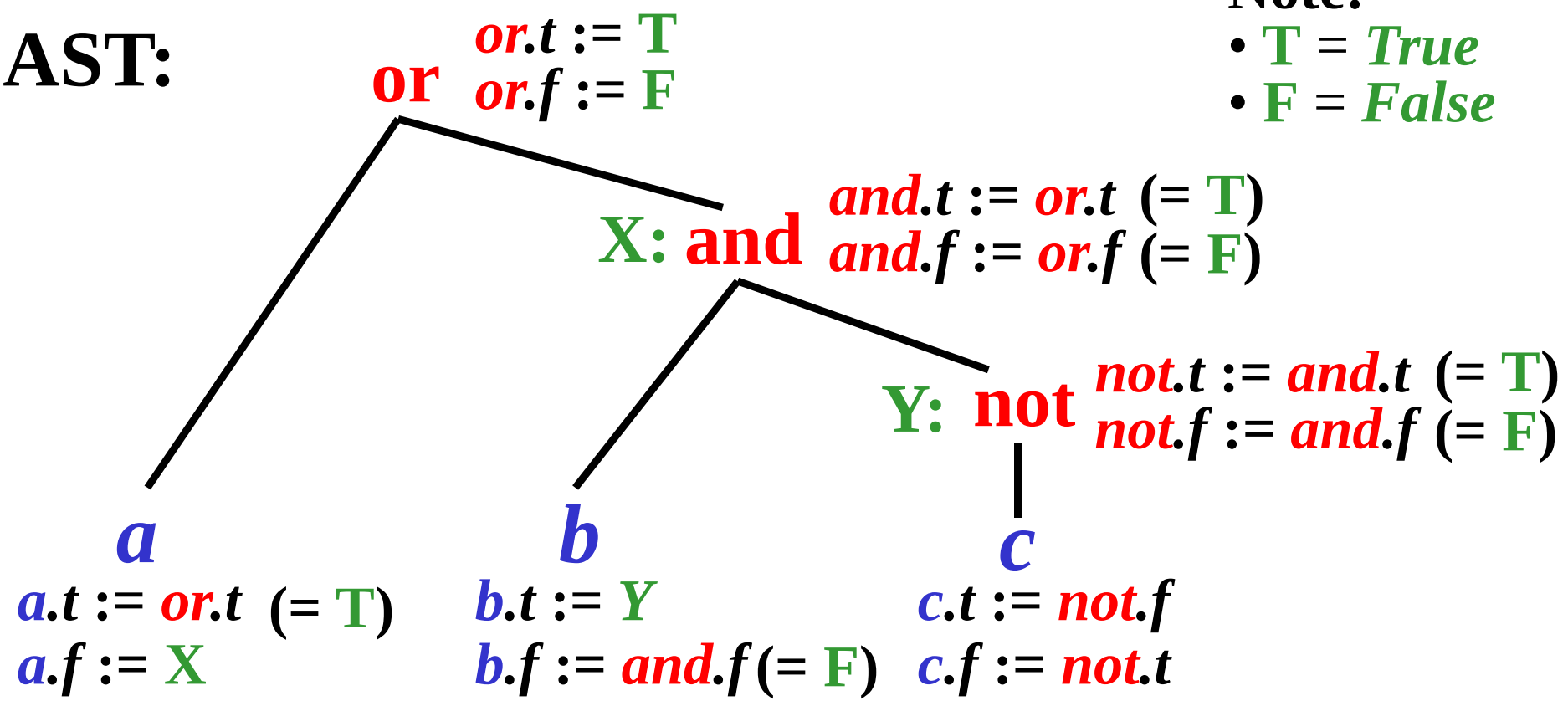
Short Evaluation Using AST: Example

Example: ***a*** **or (** ***b*** **and (not** ***c*****)):**

AST:



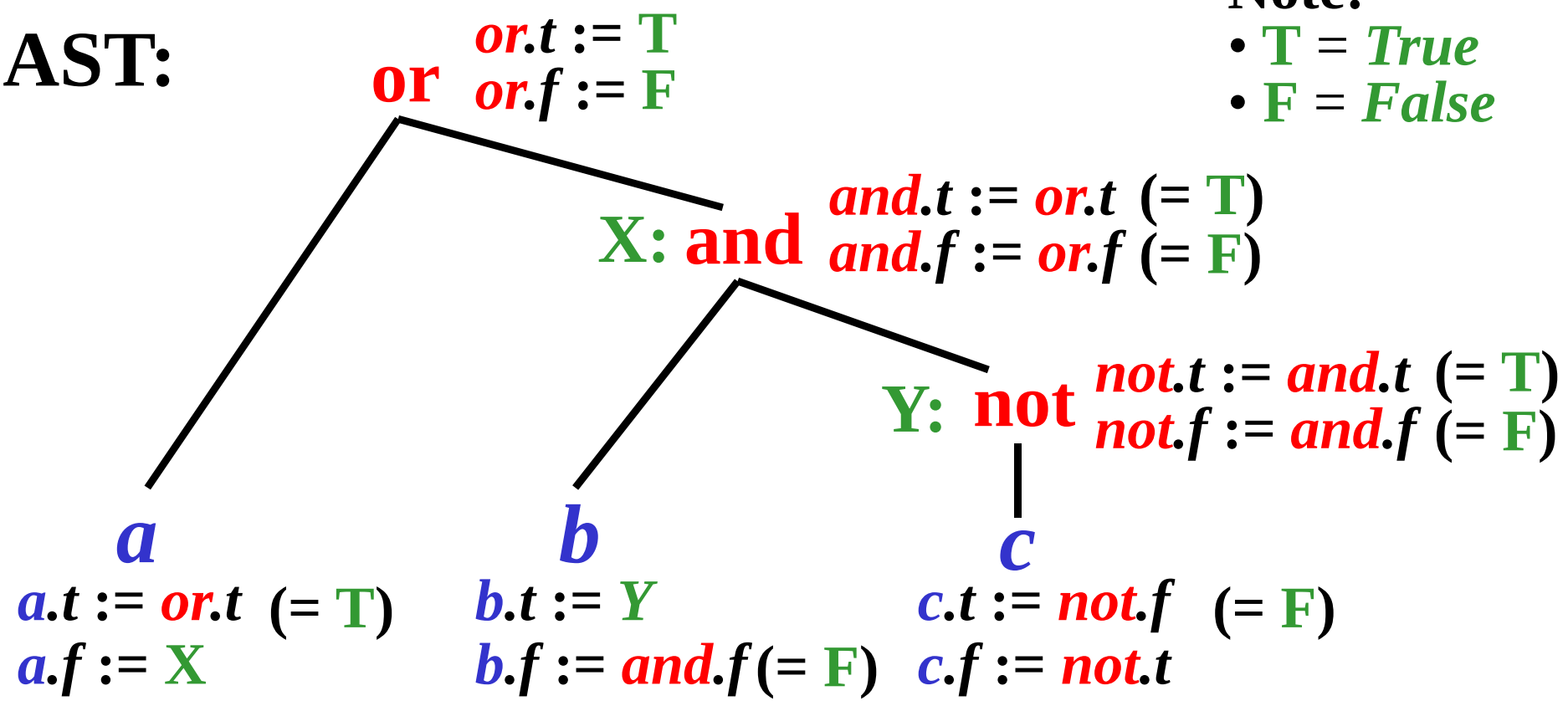
Note:

- **T** = ***True***
- **F** = ***False***

Short Evaluation Using AST: Example

Example: ***a*** **or (** ***b*** **and (not** ***c*****)):**

AST:



Note:

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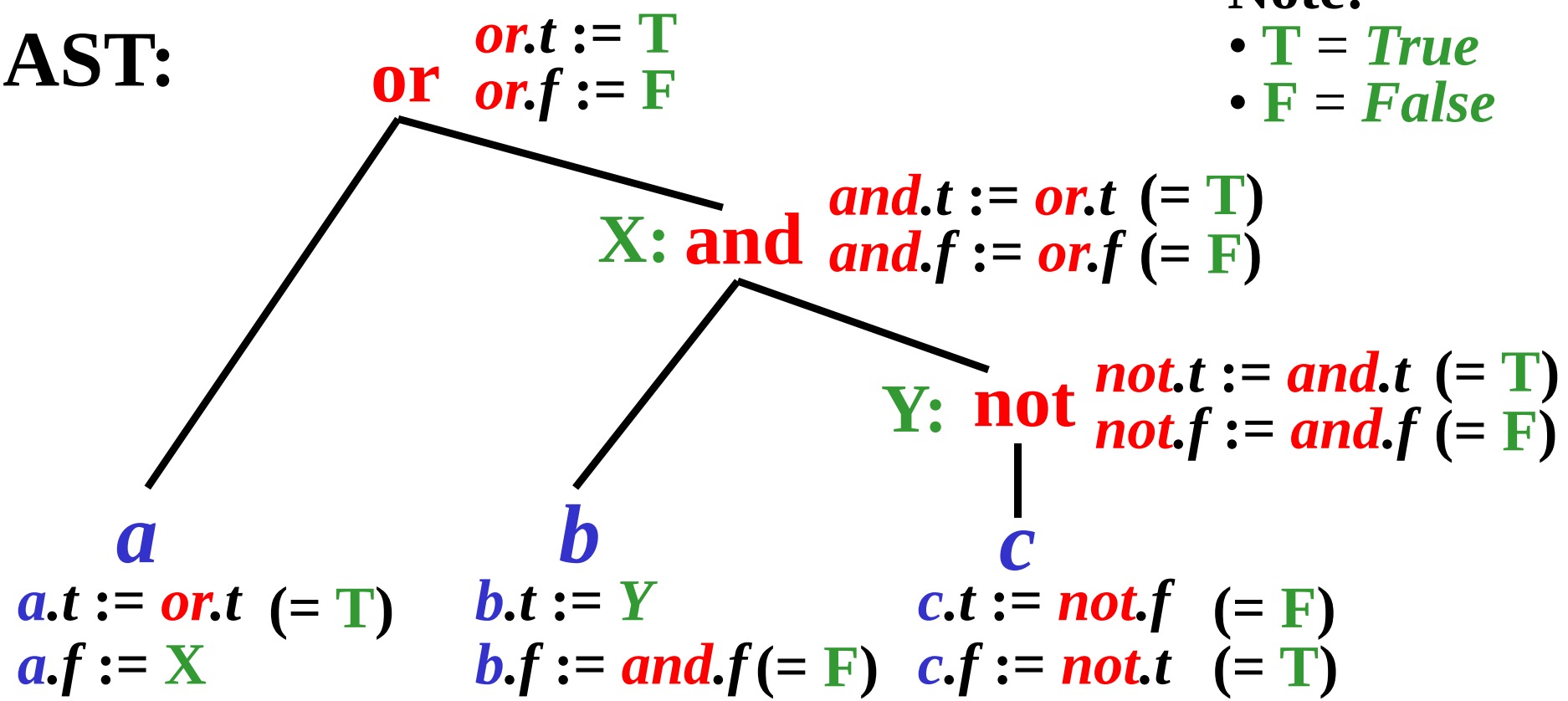
Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



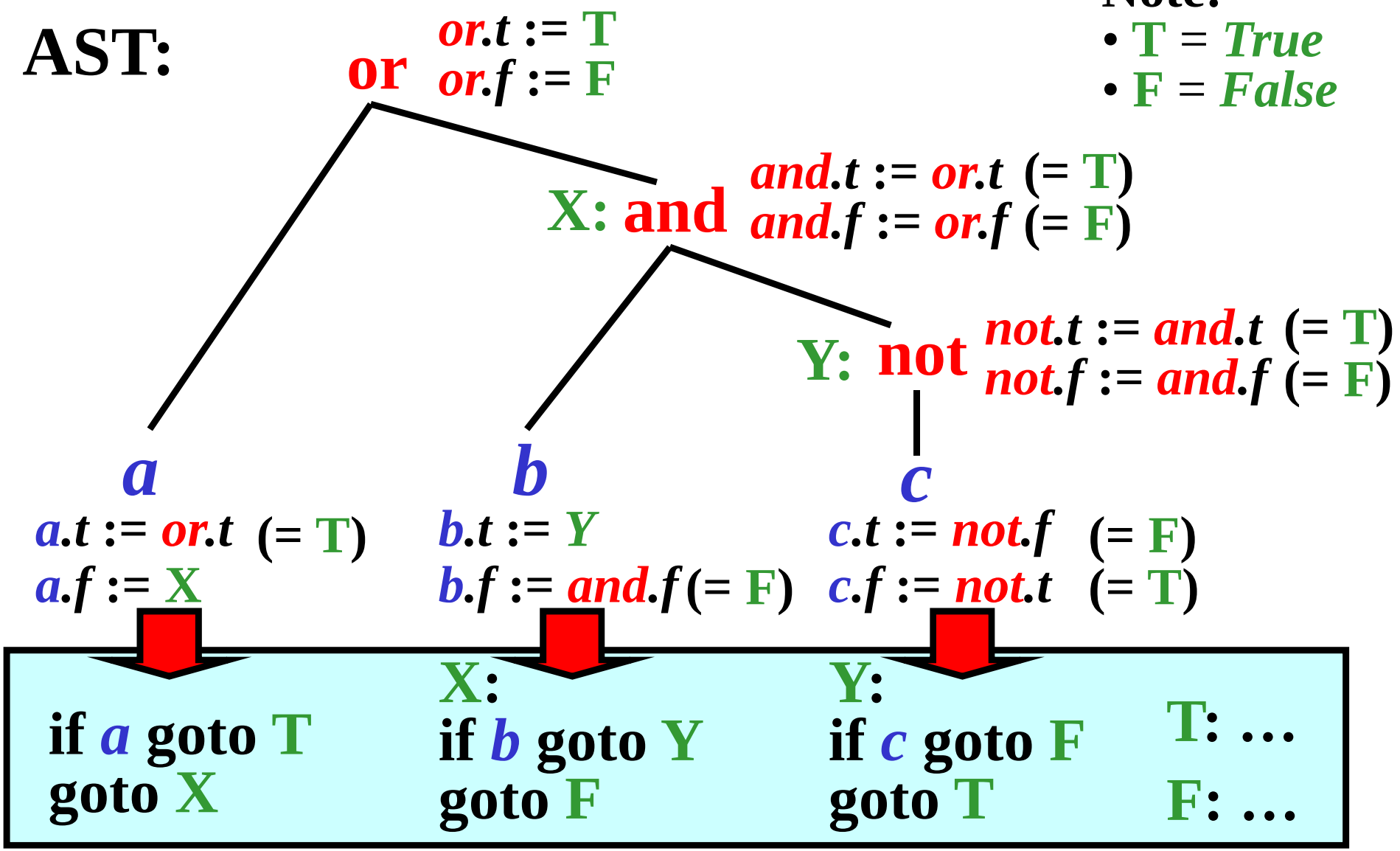
Note:

- **T** = ***True***
- **F** = ***False***

Short Evaluation Using AST: Example

Example: ***a*** **or (*b* and (not *c*)):**

AST:



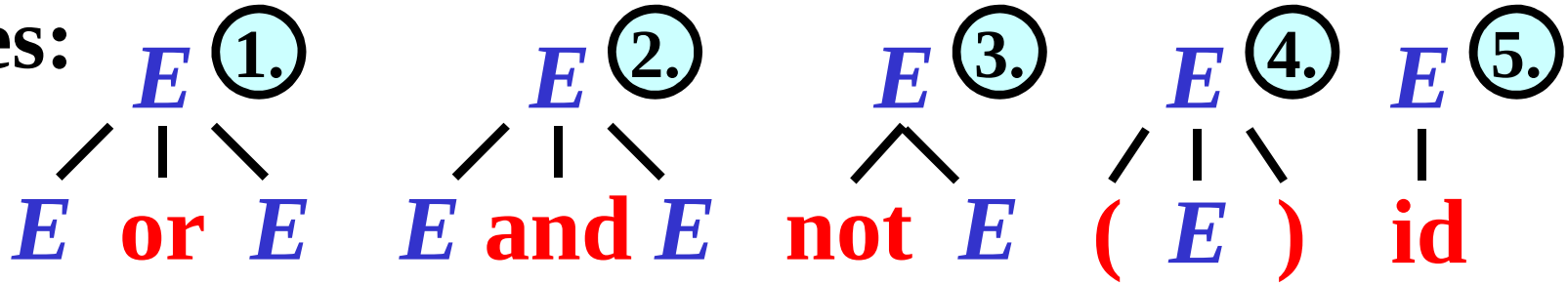
Note:

- **T** = ***True***
- **F** = ***False***

Short Evaluation: Direct Code Generation 1/5

- **Grammar for boolean expressions:**

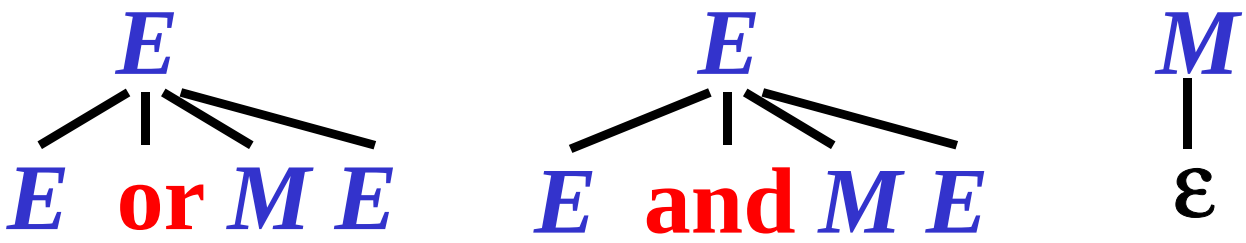
Rules:



Note: **Ambiguity!**

- **Modification of grammar:**

1) Replace rules ① & ② with:



2) Assign to each rule the following semantic action

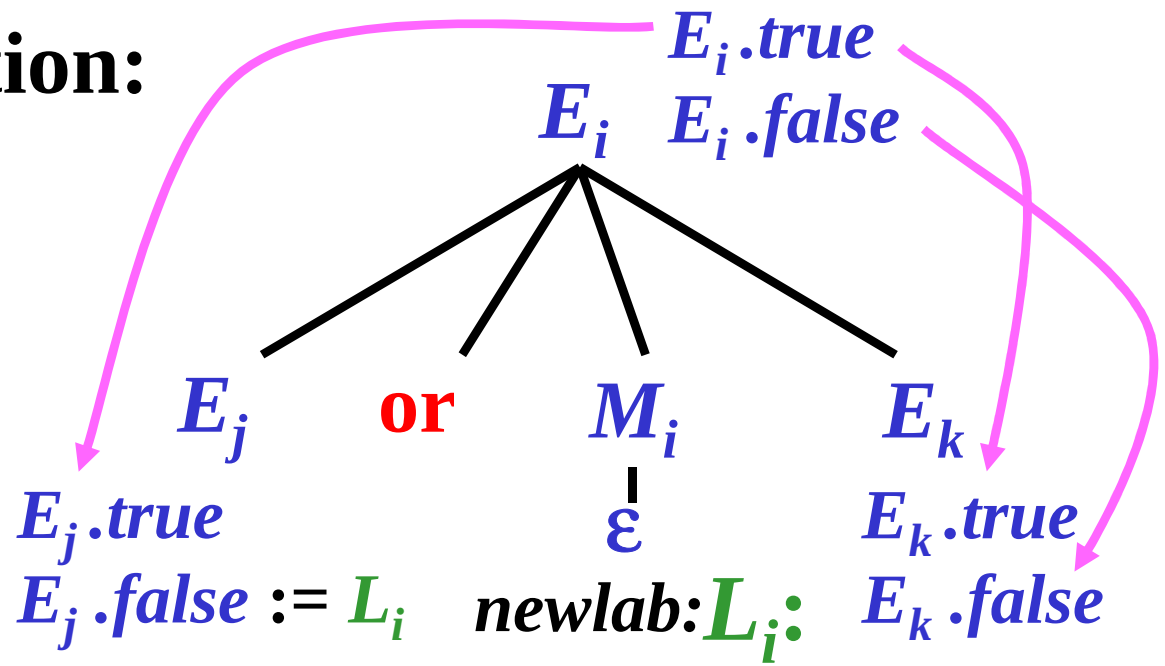
Short Evaluation: Direct Code Generation 2/5

$M_i \rightarrow \varepsilon$ {generate "M_i . ***lab:***"} // Generation of a new label

---

$E_i \rightarrow E_j$ **or** $M_i\ E_k$ {$M_i.lab$:= *GenerateNewLab*;
$E_j.true := E_i.true$; $E_j.false := M_i.lab$
$E_k.true := E_i.true$; $E_k.false := E_i.false$ }

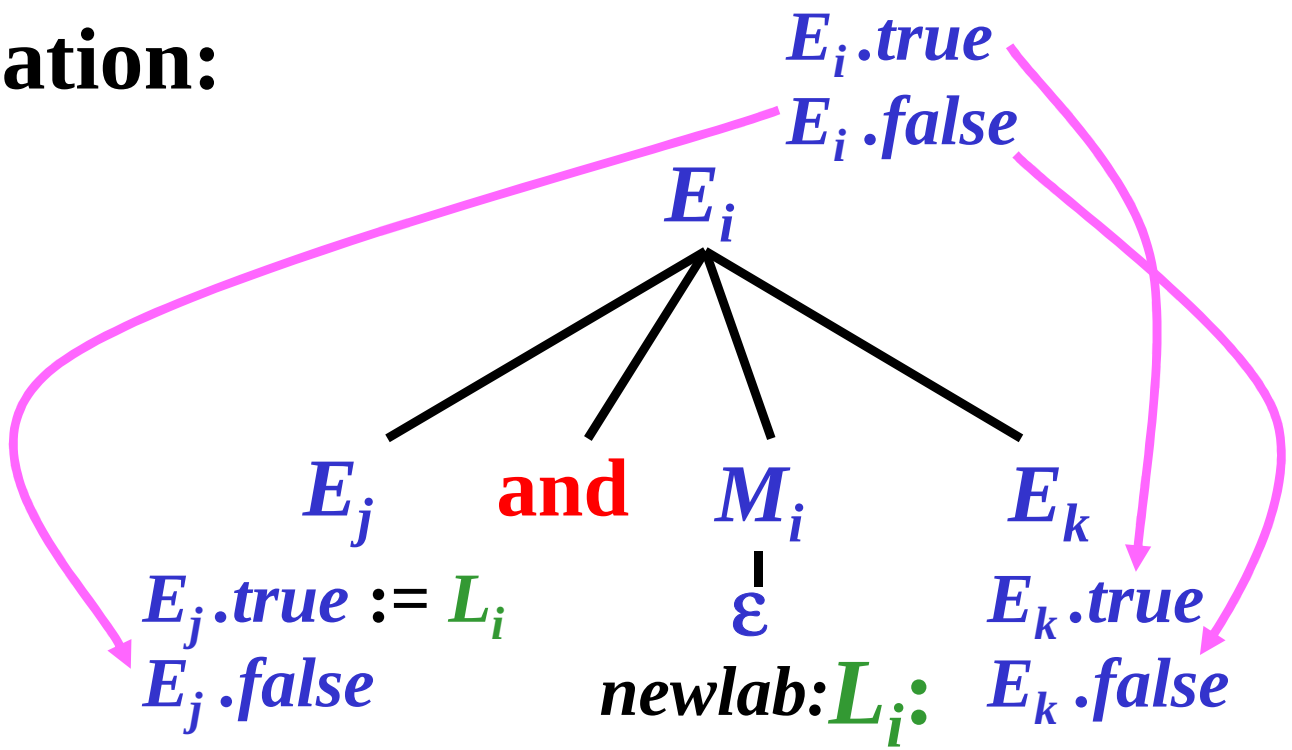
Illustration:



Short Evaluation: Direct Code Generation 3/5

$E_i \rightarrow E_j$ **and** $M_i\ E_k$ {$M_i.lab$:= *GenerateNewLab*;
$E_j.true := M_i.lab$; $E_j.false := E_i.false$
$E_k.true := E_i.true$; $E_k.false := E_i.false$ }

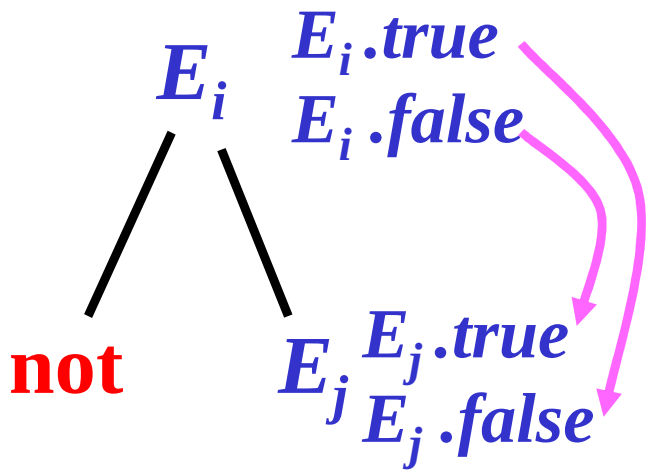
Illustration:



Short Evaluation: Direct Code Generation 4/5

$E_i \rightarrow$ **not** E_j { $E_j.true$:= $E_i.false$;
$E_j.false$:= $E_i.true$ }

Illustration:



$E_i \rightarrow (E_j)$ {$E_j.true$:= $E_i.true$;
$E_j.false$:= $E_i.false$ }

$E_i \rightarrow id_j$ { generate "**if** $id_j.val$ **goto** $E_i.true$";
generate "**goto** $E_i.false$" }

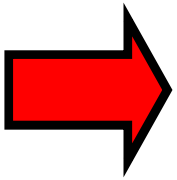
Short Evaluation: Direct Code Generation 5/5

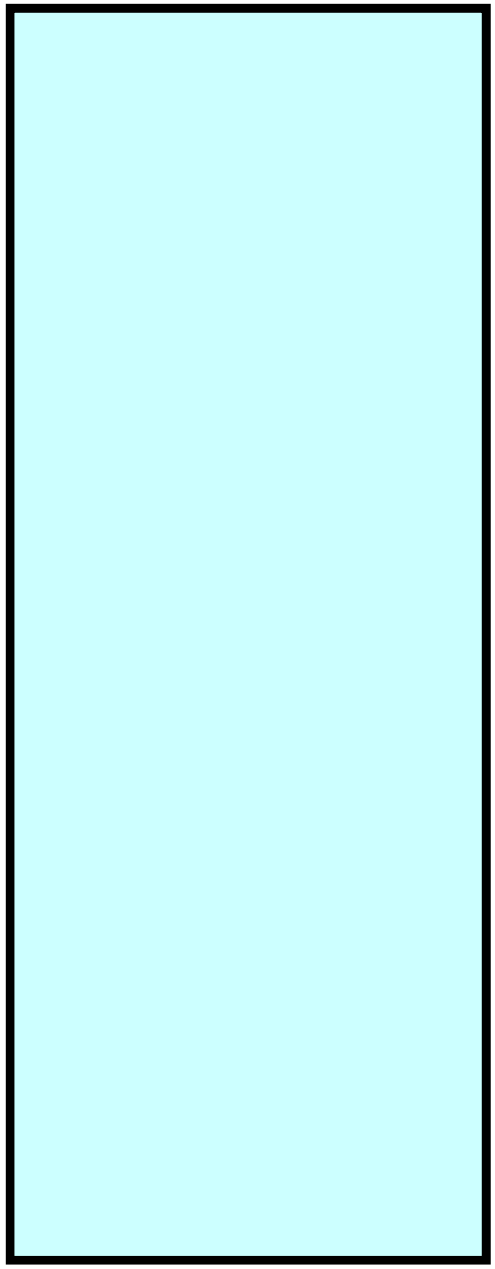
Example: *a* and *b* or *c* and *d*:

$E_0 . t := L_{true}$

$E_0 . f := L_{false}$

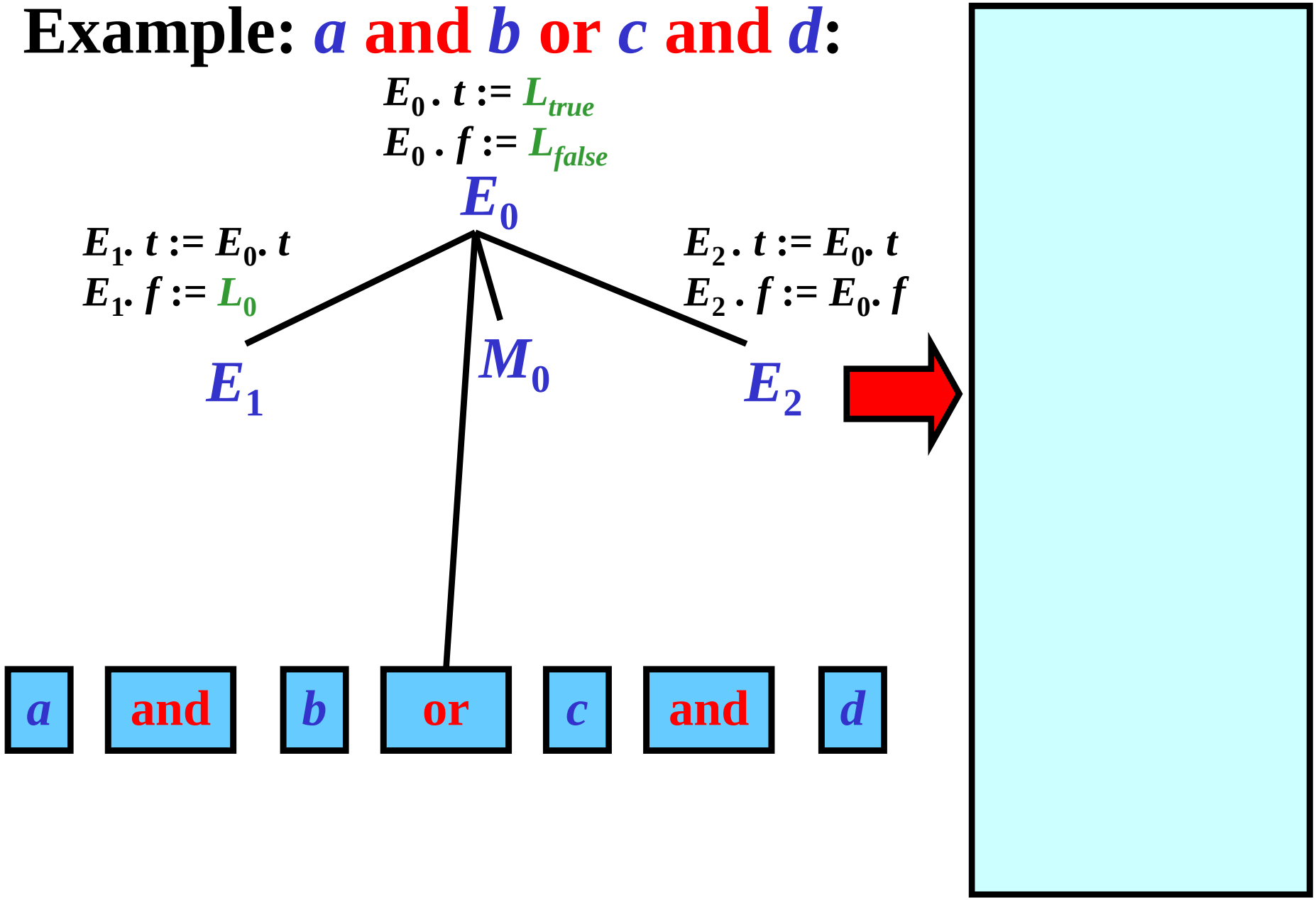
E_0





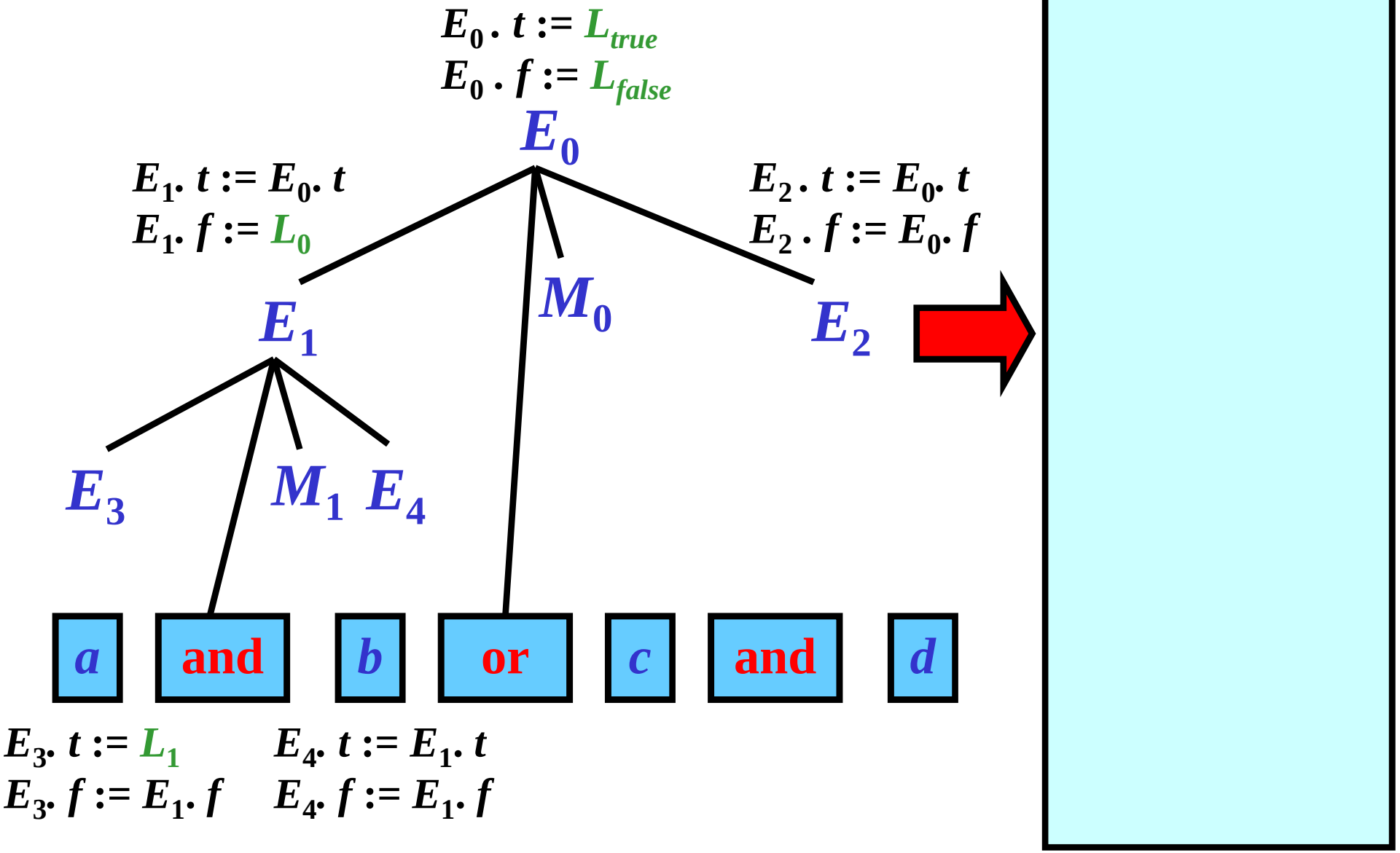
Short Evaluation: Direct Code Generation 5/5

Example: *a* and *b* or *c* and *d*:



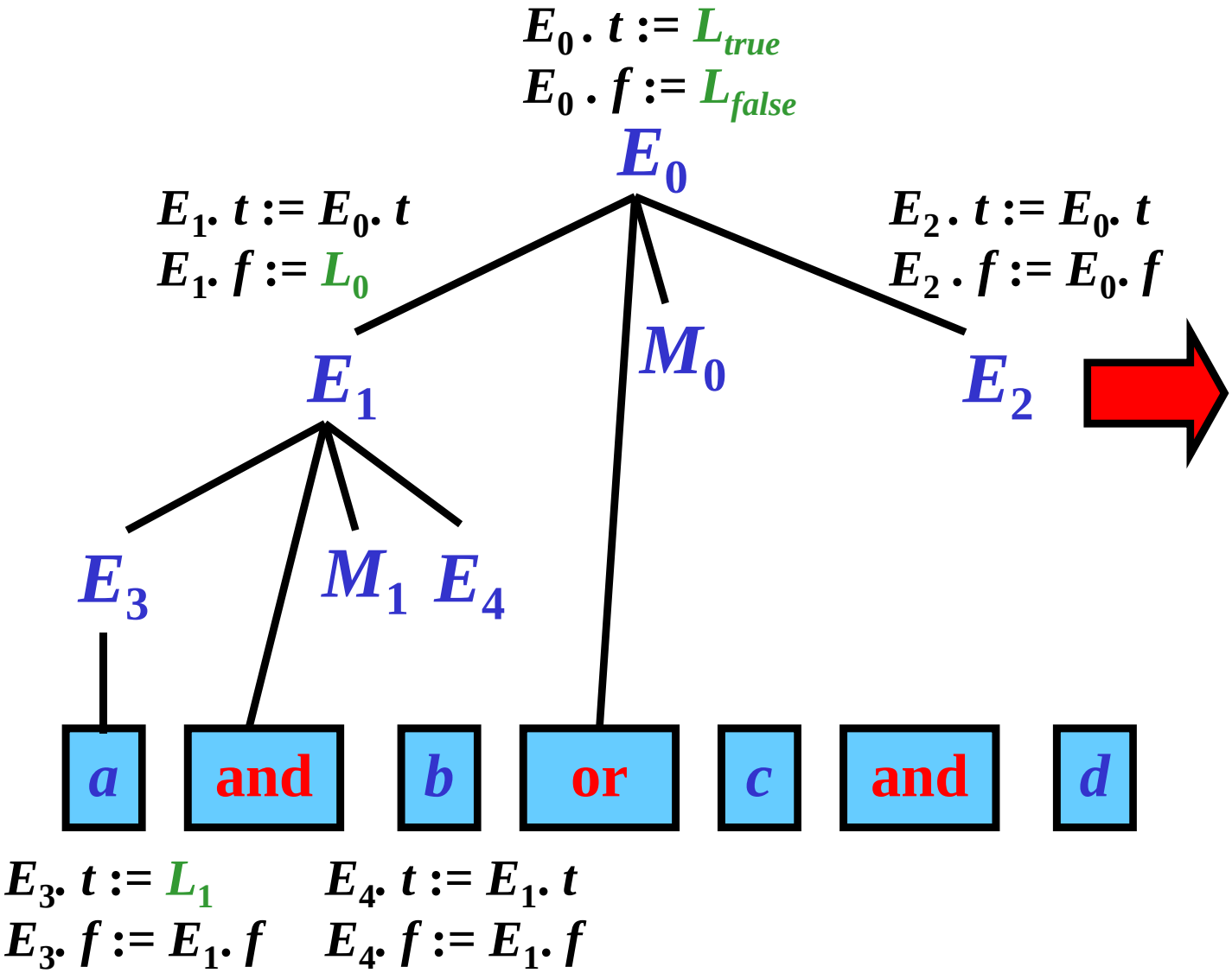
Short Evaluation: Direct Code Generation 5/5

Example: *a* and *b* or *c* and *d*:



Short Evaluation: Direct Code Generation 5/5

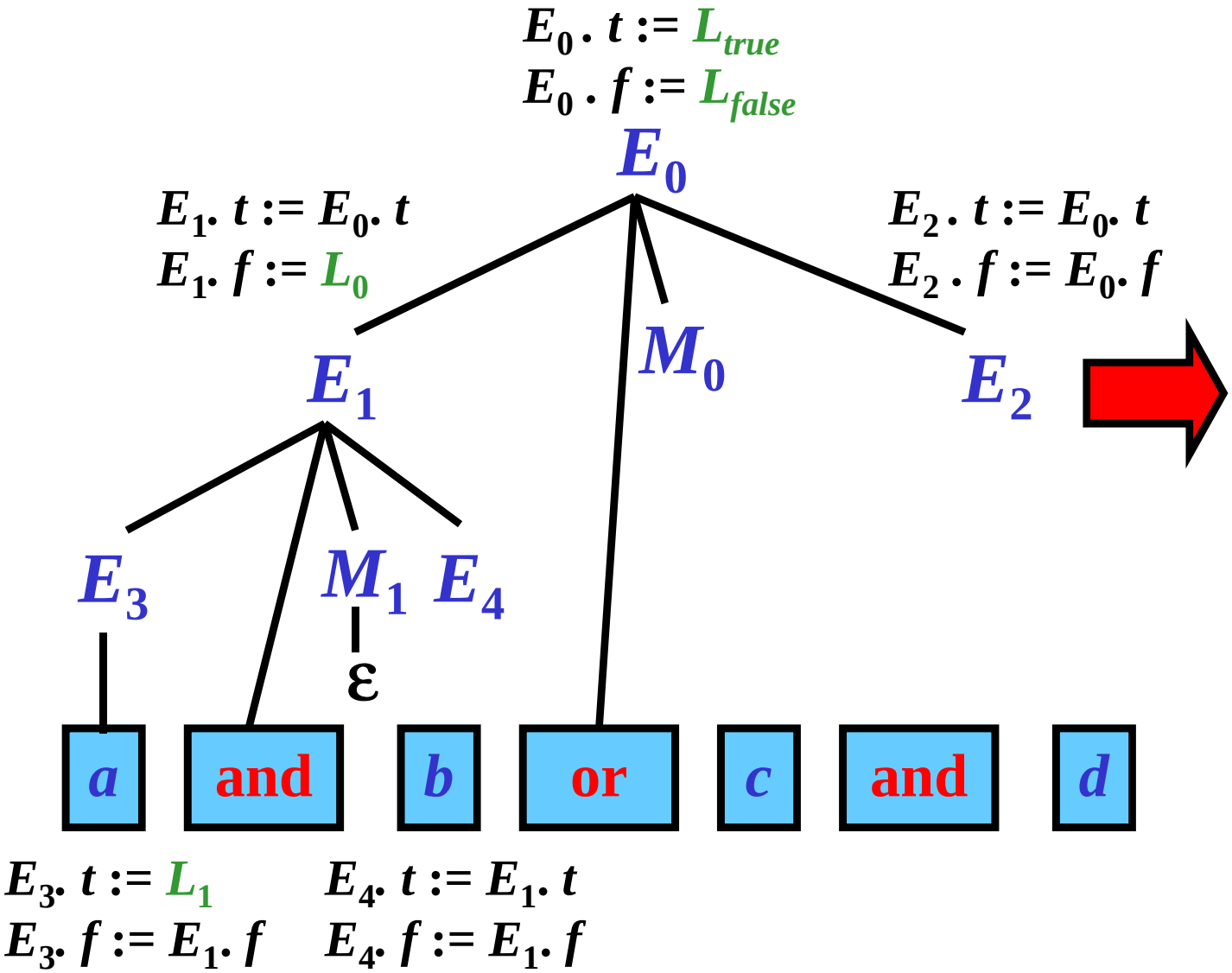
Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0

Short Evaluation: Direct Code Generation 5/5

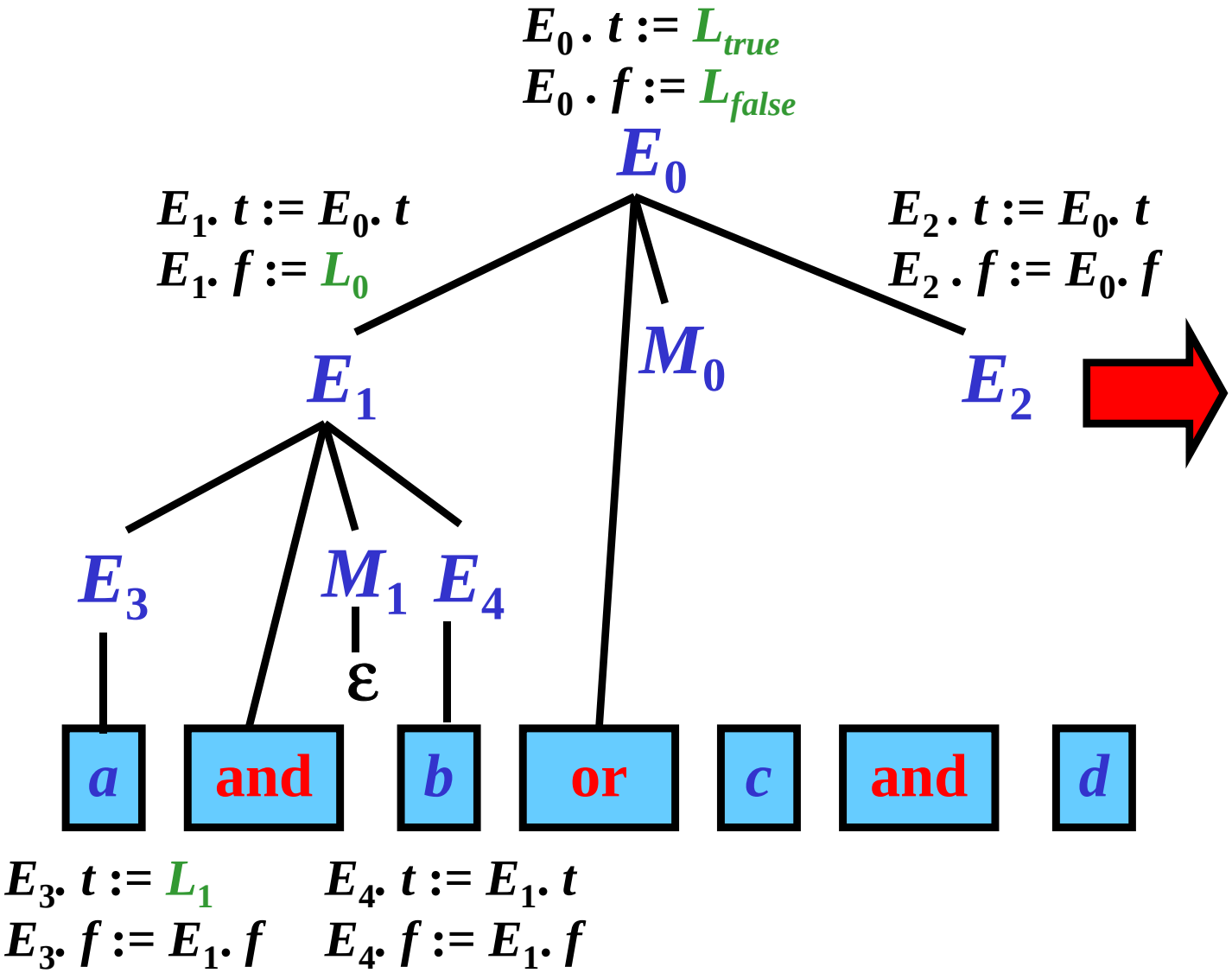
Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0
L_1:

Short Evaluation: Direct Code Generation 5/5

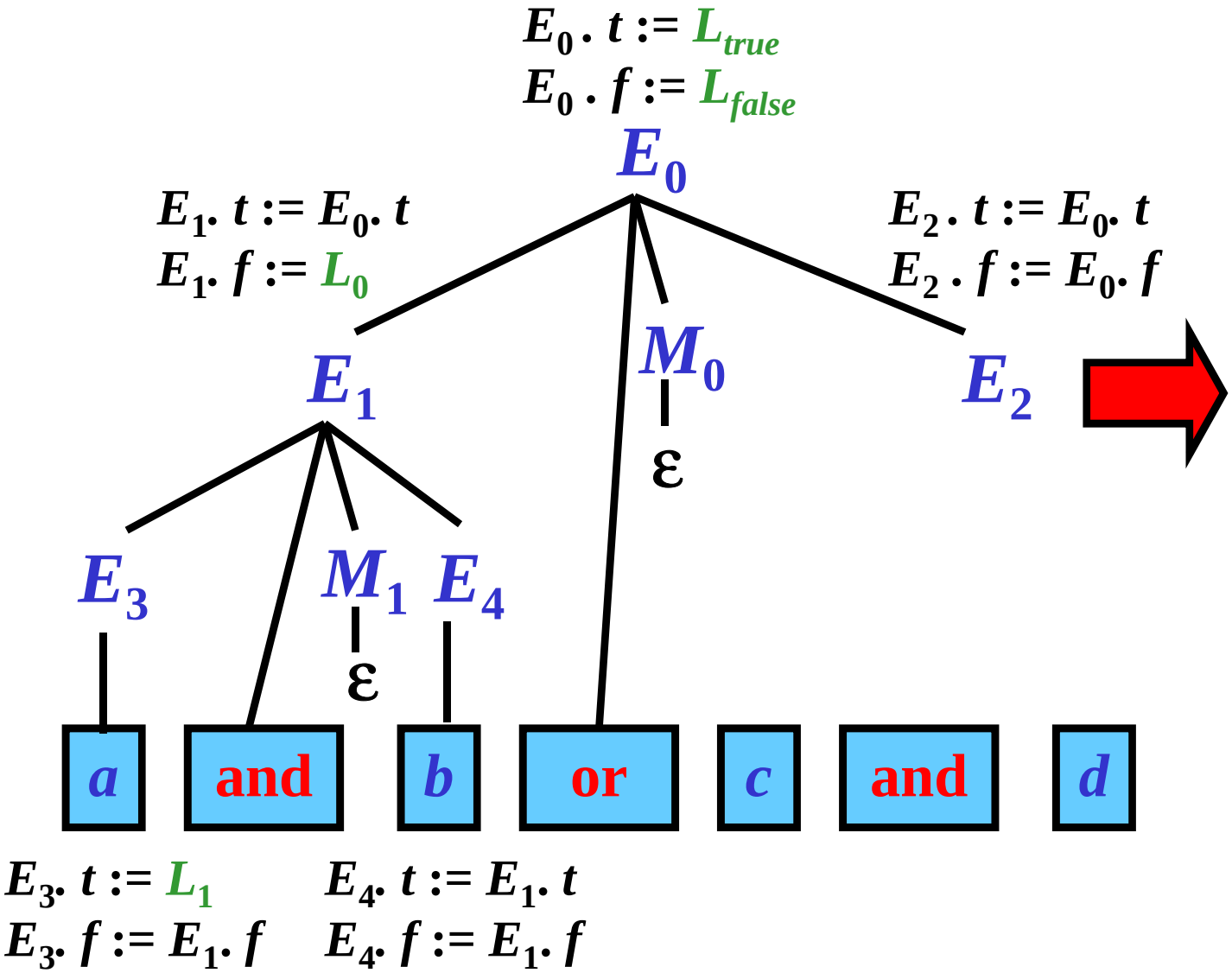
Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0
L_1:
if ***b*** *goto* L_{true}
goto L_0

Short Evaluation: Direct Code Generation 5/5

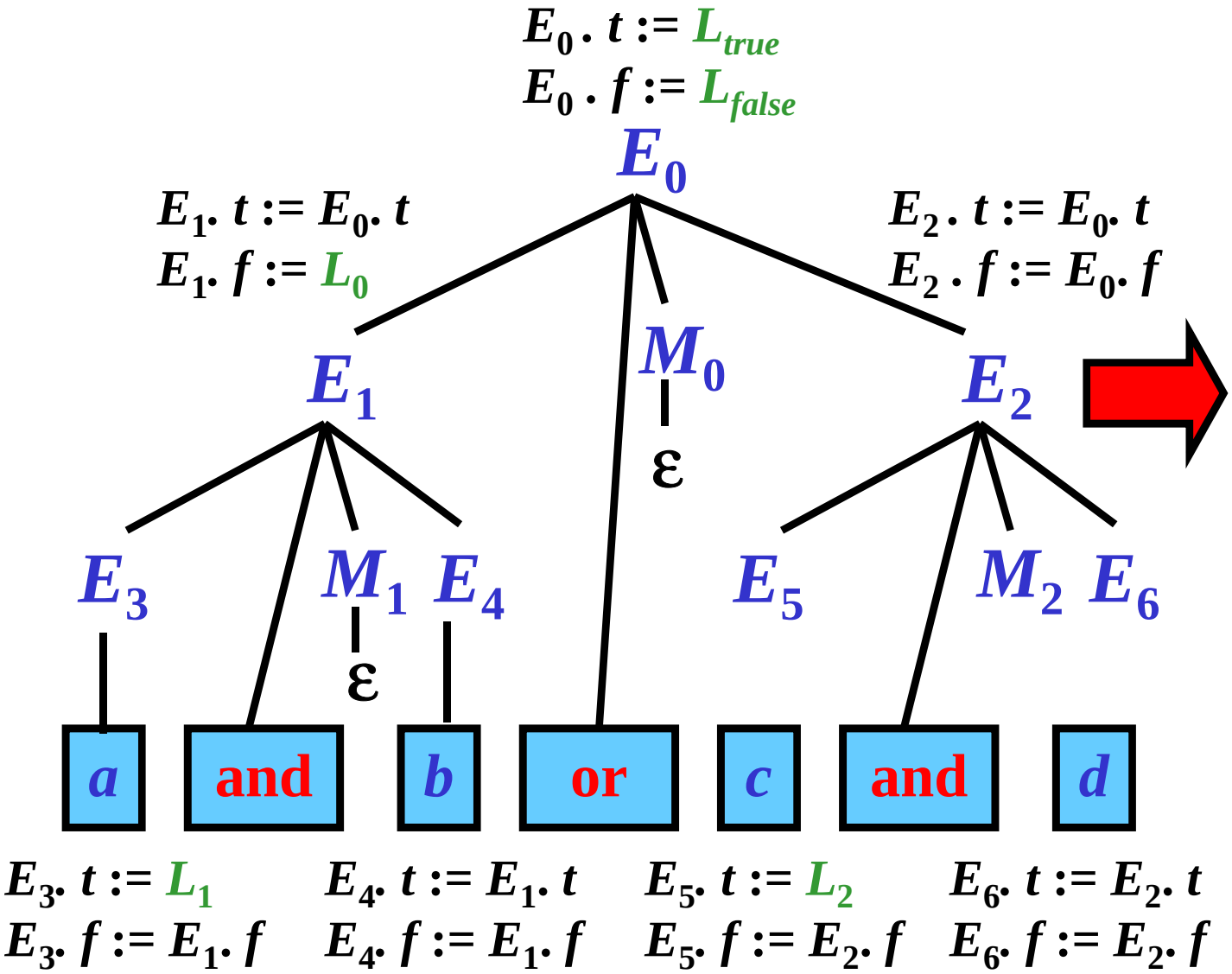
Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0
L_1:
if ***b*** *goto* L_{true}
goto L_0
L_0:

Short Evaluation: Direct Code Generation 5/5

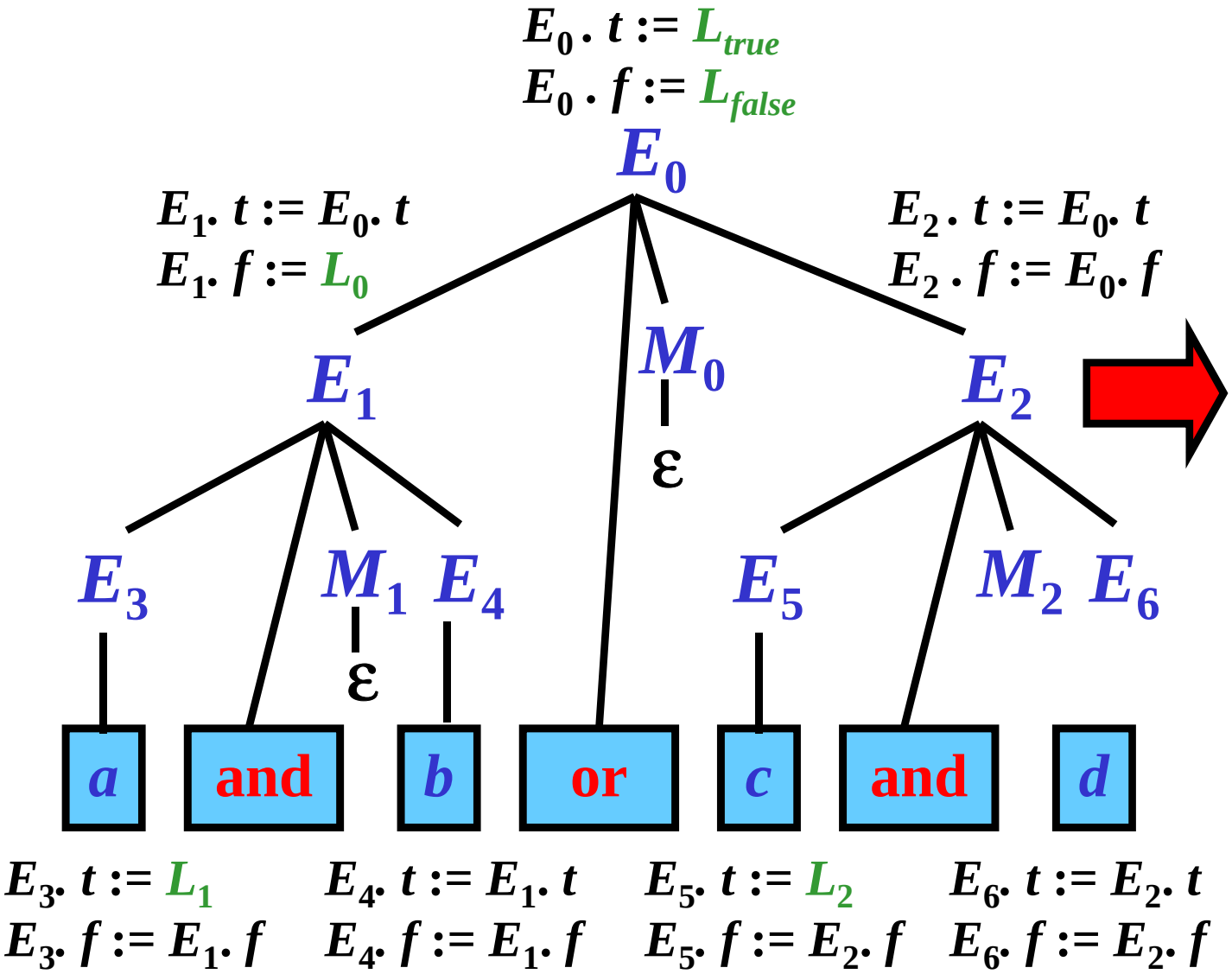
Example: *a* and *b* or *c* and *d*:



if a goto L_1
goto L_0
L_1:
if b goto L_{true}
goto L_0
L_0:

Short Evaluation: Direct Code Generation 5/5

Example: *a* and *b* or *c* and *d*:



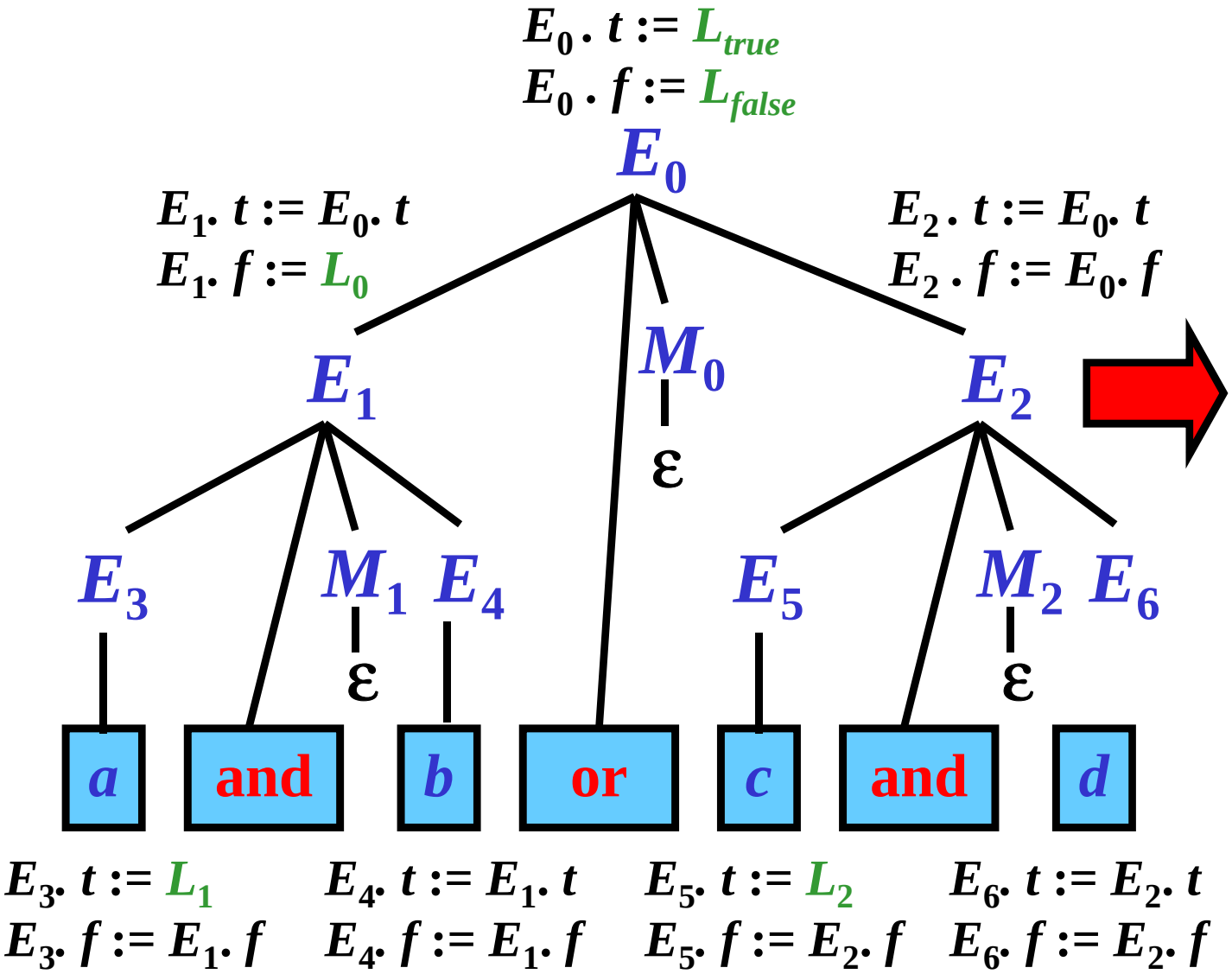
if a goto L_1
goto L_0

L_1:
if b goto L_{true}
goto L_0

L_0:
if c goto L_2
goto L_{false}

Short Evaluation: Direct Code Generation 5/5

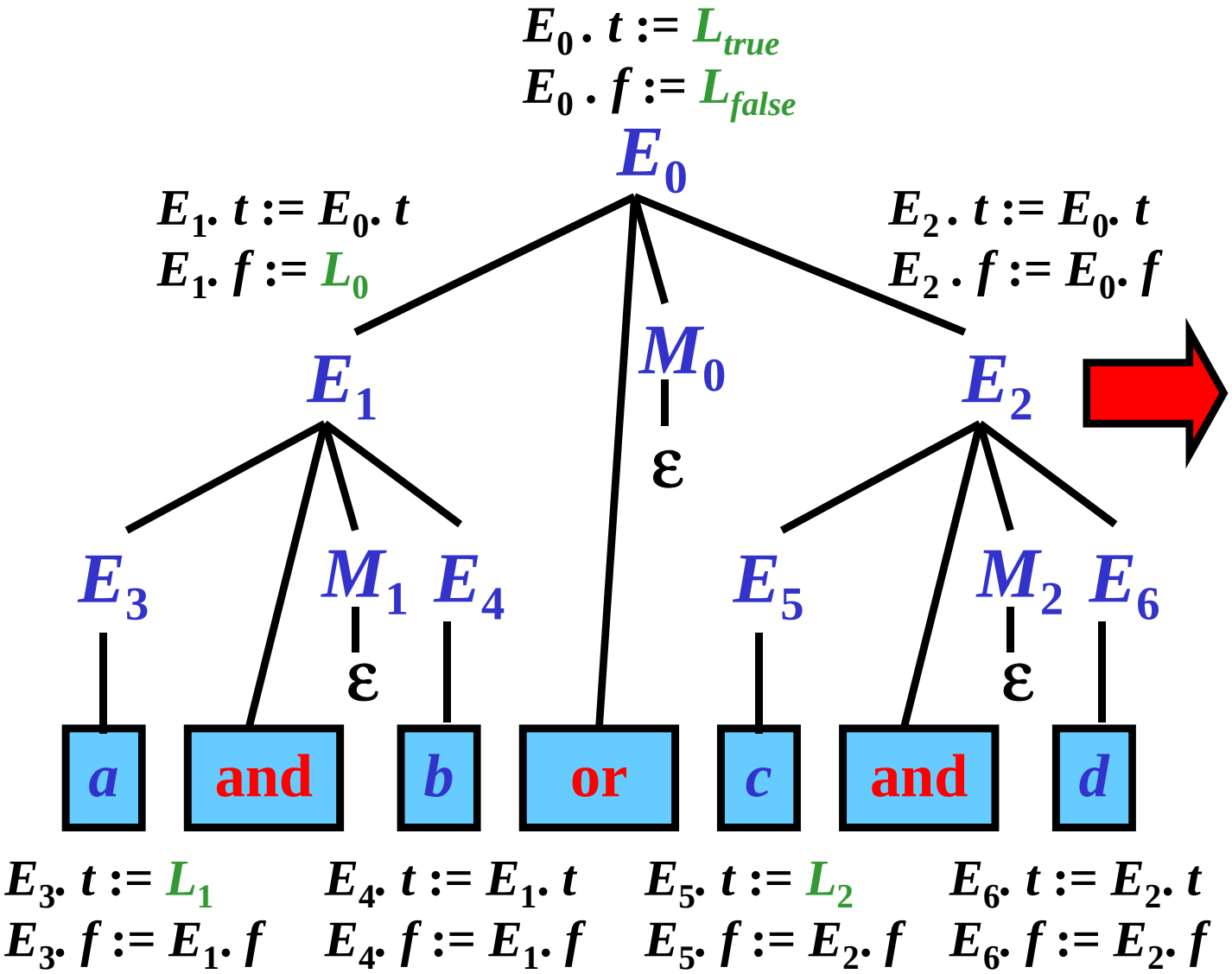
Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0
L_1:
if ***b*** *goto* L_{true}
goto L_0
L_0:
if ***c*** *goto* L_2
goto L_{false}
L_2:

Short Evaluation: Direct Code Generation 5/5

Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0

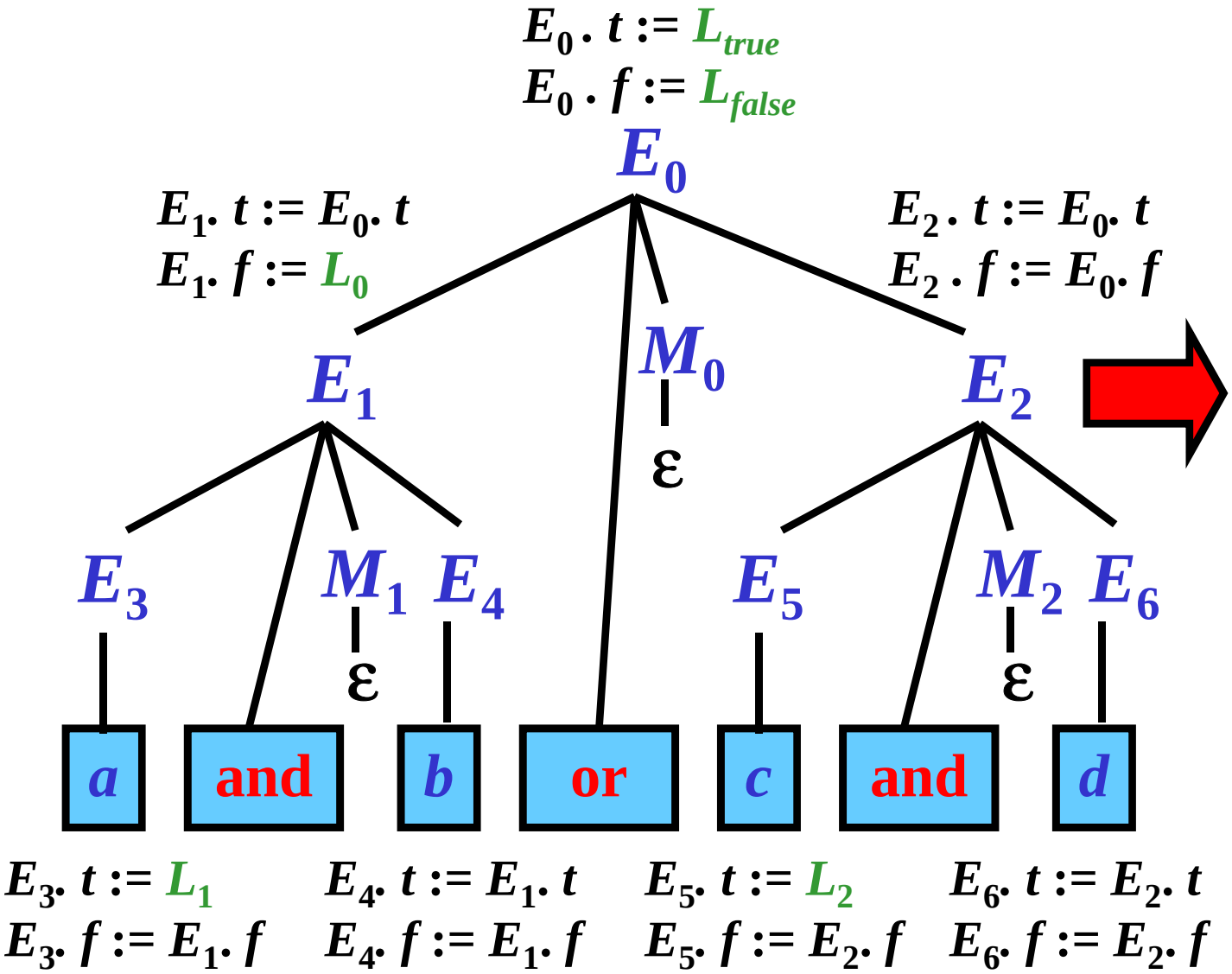
L_1:
if ***b*** *goto* L_{true}
goto L_0

L_0:
if ***c*** *goto* L_2
goto L_{false}

L_2:
if ***d*** *goto* L_{true}
goto L_{false}

Short Evaluation: Direct Code Generation 5/5

Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0

L_1:
if ***b*** *goto* L_{true}
goto L_0

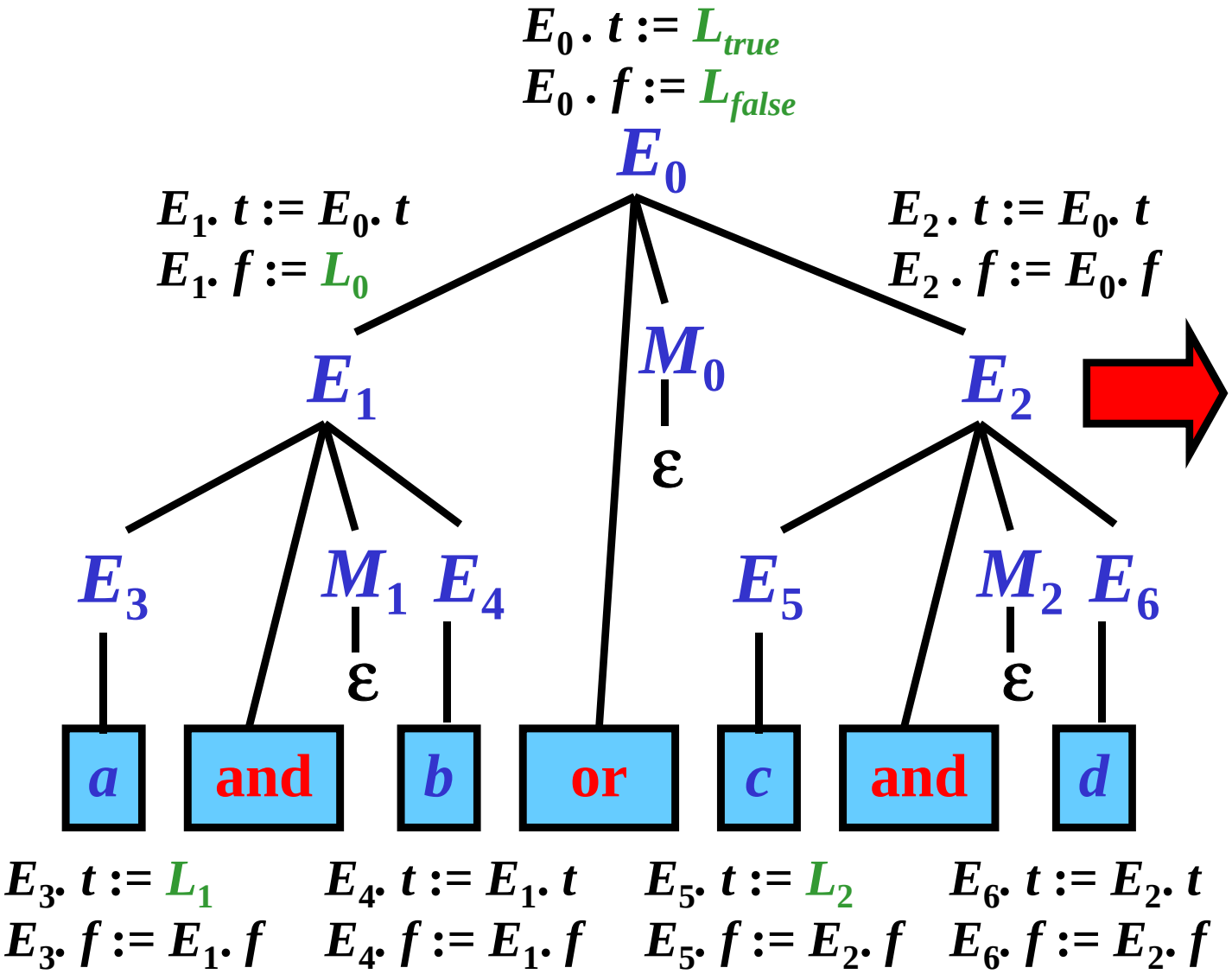
L_0:
if ***c*** *goto* L_2
goto L_{false}

L_2:
if ***d*** *goto* L_{true}
goto L_{false}

L_{true}: …

Short Evaluation: Direct Code Generation 5/5

Example: *a* and *b* or *c* and *d*:



if ***a*** *goto* L_1
goto L_0

L_1:
if ***b*** *goto* L_{true}
goto L_0

L_0:
if ***c*** *goto* L_2
goto L_{false}

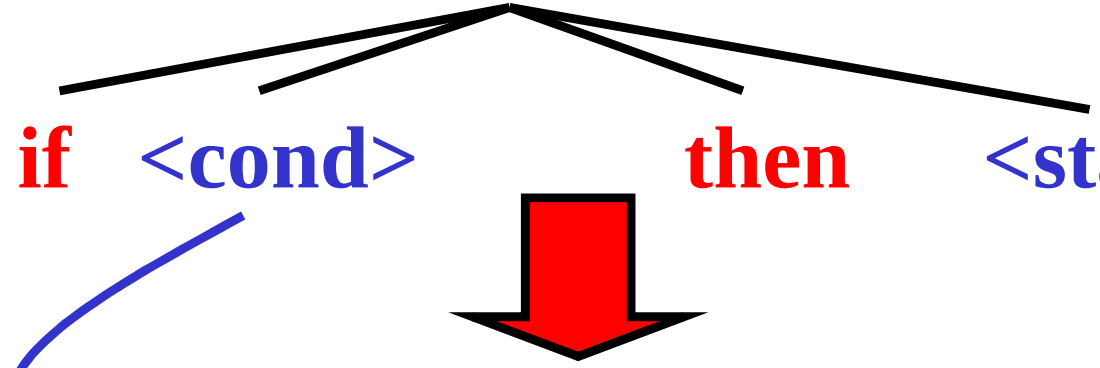
L_2:
if ***d*** *goto* L_{true}
goto L_{false}

L_{true}: …

L_{false}: …

Branching: If-Then

Rule: <if-then>

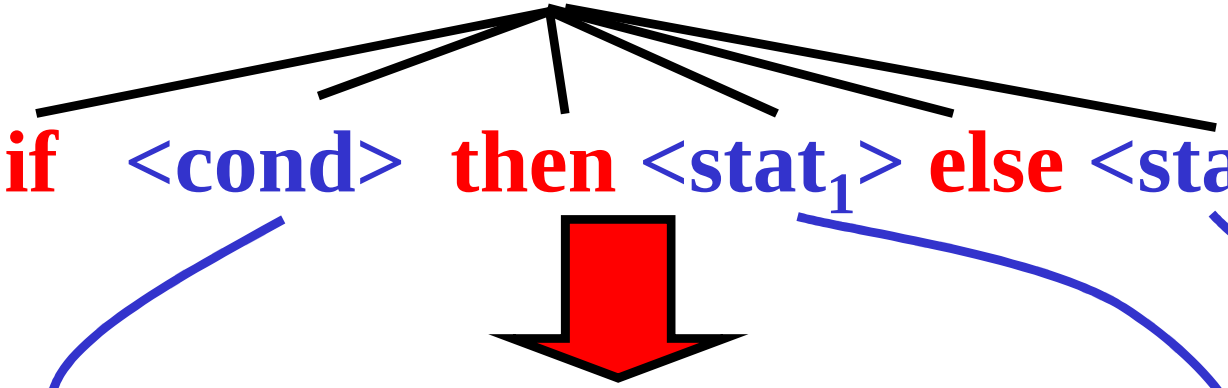


Semantic action:

```
{ // evaluation of cond
  // to c.val
(not , c.val, , c.val)
(goto, c.val, , L1   )
 // code of stat1      }
(lab , L1   , ,       )
```

Branching: If-Then-Else

Rule: **<if-then-else>**



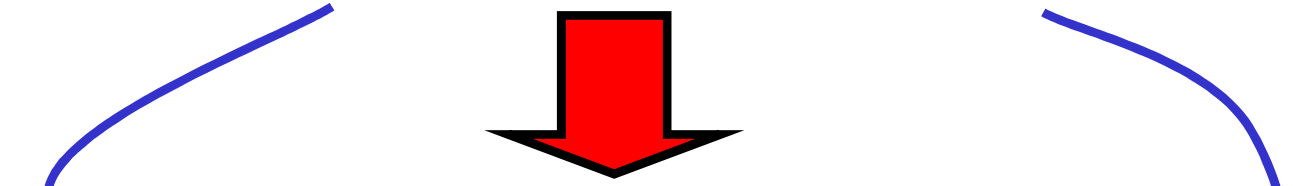
Semantic action:

```
{ // evaluation of cond
  // to c.val
(not , c.val, , c.val)
(goto, c.val, , L1   )
 // code of stat1      }
(goto,       , , L2   )
(lab , L1    , ,      )
 // code of stat2      }
(lab , L2    , ,      )
```

While Loop

Rule: **<while-loop>**

while **<cond>** **do** **<stat>**

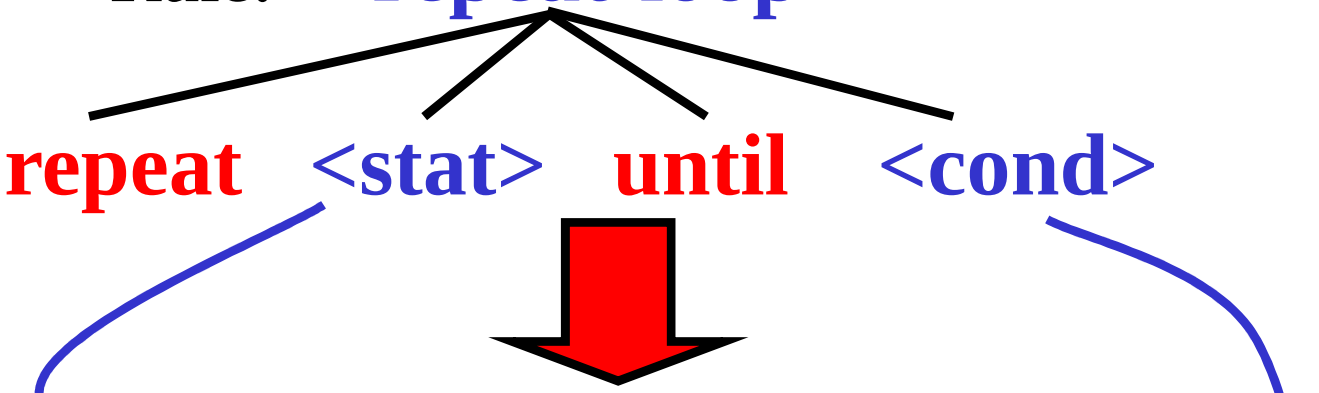


Semantic action:

```
(lab , L1    , ,          )
// evaluation of cond
// to c.val
(not , c.val, , c.val)
(goto, c.val, , L2    )
 // code of stat
(goto,       , , L1    )
(lab ,  L2   , ,          )
```

Repeat Loop

Rule: <repeat-loop>



Semantic action:

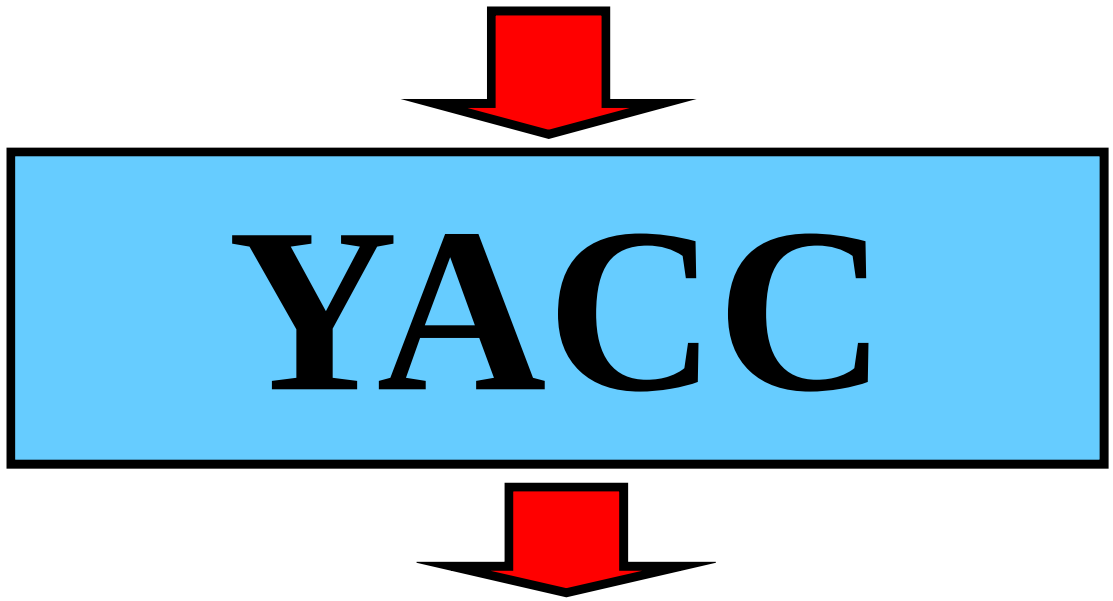
```
(lab , L1    , ,          )
{// code of stat

 // evaluation of cond
 // to c.val
(not , c.val, , c.val)
(goto, c.val, , L1   )
```

Yacc: Basic Idea

- Automatic construction of **parser** from **CFG**
- Yacc compiler × Yacc language
- *Yacc* from *Y*et *a*nother *c*ompiler *c*ompiler

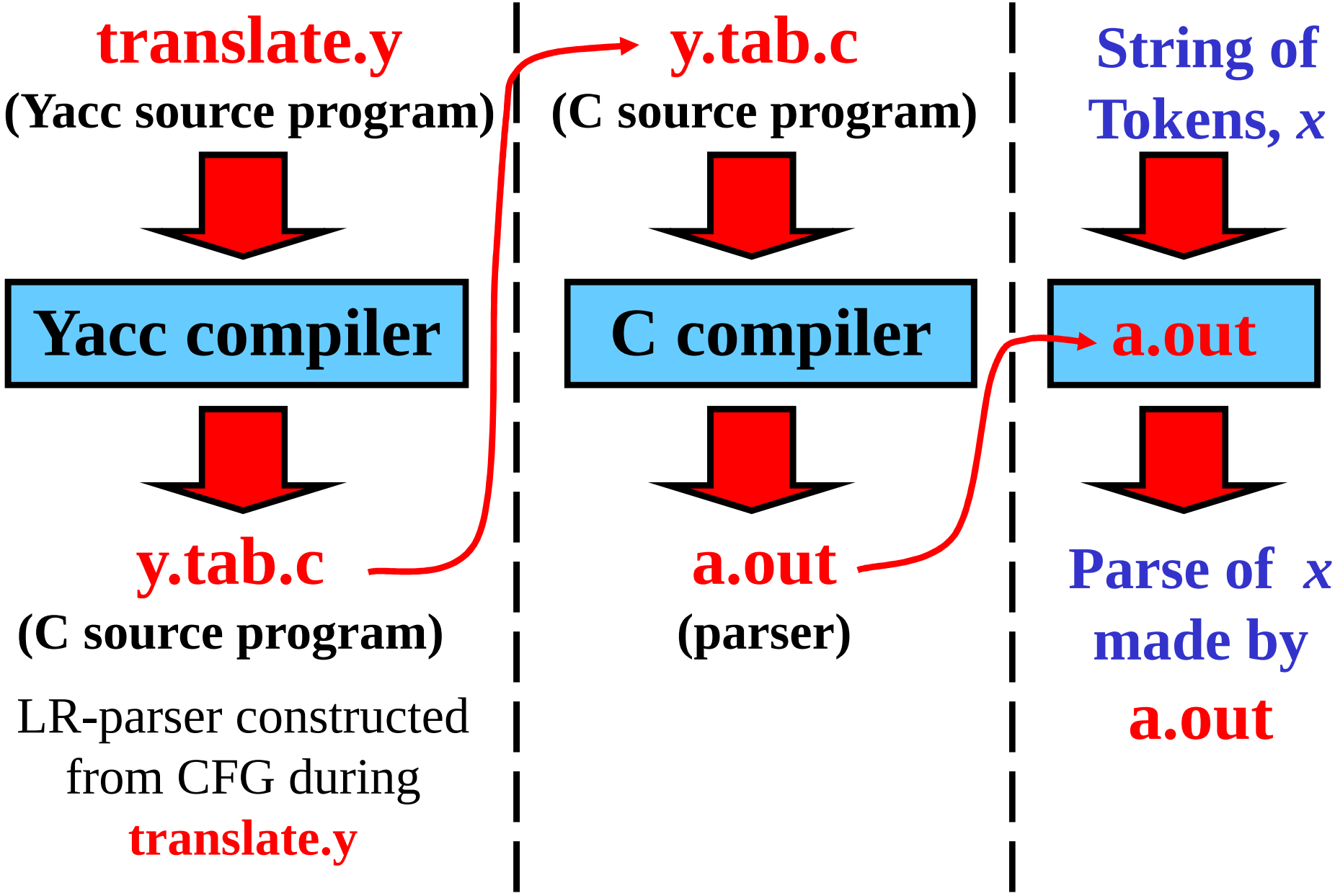
Ilustrace:

Context-free grammar, *G*



Parser for *G*

Yacc: Phases of Compilation



Structure of Yacc Source Program

/* Section I: Declaration */

$d_1, d_2, \ \ldots \ , d_i$

%% **/* End of Section I*/**

/* Section II: Translation rules */

$r_1, r_2, \ \ldots \ , r_j$

%% **/* End of Section II*/**

/* Section III: Auxiliary procedures*/

$p_1, p_2, \ \ldots \ , p_k$

Description of Grammar in Yacc

- **Nonterminals:** names (= strings)
- **Example:** `prog`, `stat`, `expr`, …

- **Terminals:** Characters in quotes or declared tokens
- **Example:** `'+'`, `'*'`, `'('`, `')'`, `ID`, `INTEGER`

- **Rules:** Set of *A*-rules { $A \to x_1$, $A \to x_2$, … $A \to x_n$ }

  is written as

```
A : x1
  | x2
  …
  | xn
```

- **Example:**

```
expr : expr '+' expr
     | ID
```

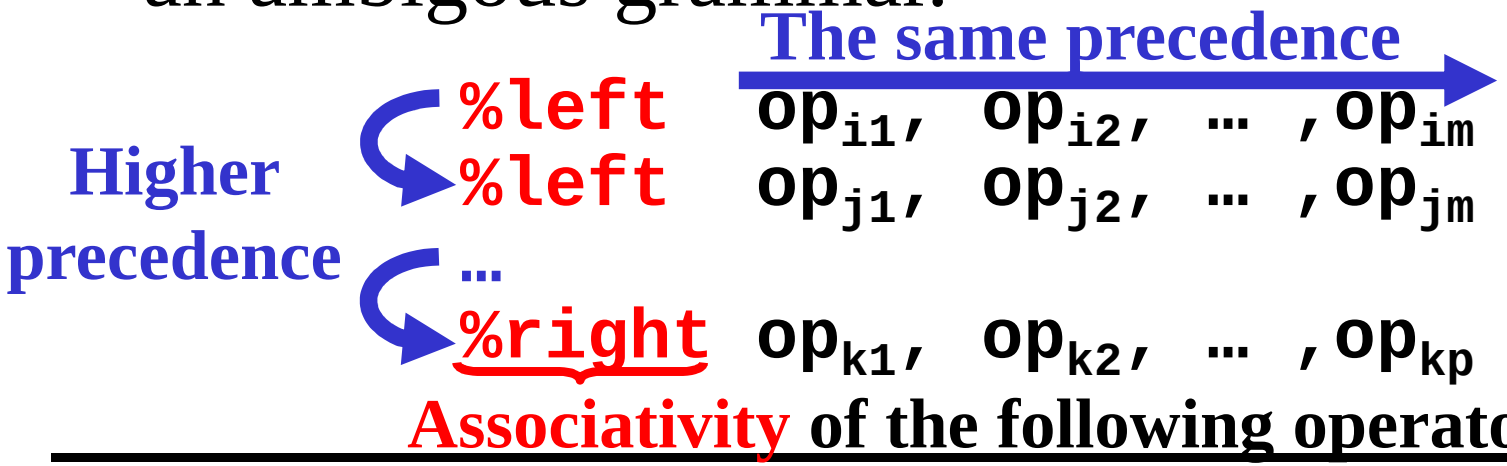
- **Start Nonterminal:** A left side of the first rule.

Section I: Declaration

1) Declaration of tokens

```
%token TYPE_OF_TOKEN
```

2) Specification of asociativity & precedence in an ambigous grammar.



Example:

```
%token INTEGER
%token ID
%left '+'
%left '*'
```

Section II: Translation Rules

- Translation rules are in the form:

```
Rule    Semantic_Action
```

- `Semantic_Action` is a program routine that specifies what to do if `Rule` is used.

Special symbols for a rule, *r*:

`$$` = attribute of *r*'s left-hand side

`$i` = attribute of the *i*-th symbols on *r*'s right-hand side

---

Example:

```
expr : expr '+' expr {$$ = $1 + $3}
     | expr '*' expr {$$ = $1 * $3}
     | '(' expr ')'  {$$ = $2}
     | INTEGER
     | ID
```

Section III: Auxiliary Procedures

- Auxiliary procedures used by translation rules

Note: If the Yacc-parser do not cooperate with a scanner (e.g. Lex), then there is **yylex()** implemented in this section.

Example:

```
int yylex() {
      /* Get the next token */
      &yylval = attribute;
      return TYPE_OF_TOKEN;
}
```

Complete Source Program in Yacc

```
%token INTEGER
%token ID
%left ‘+’
%left ‘*’

%%

expr : expr ‘+’ expr {$$ = $1 + $3}
     | expr ‘*’ expr {$$ = $1 * $3}
     | ‘(’ expr ‘)’  {$$ = $2}
     | INTEGER
     | ID

%%

int yylex () { …}
```