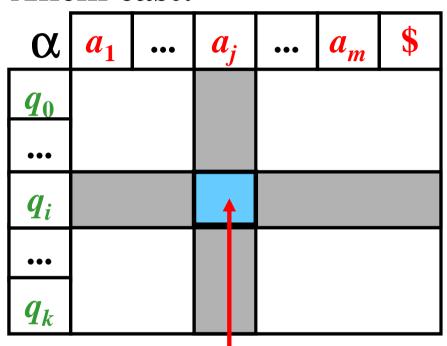
# Kapitola VIII. (Bonus) LR syntaktická analýza

# LR syntaktický analyzátor

- Necht' G = (N, T, P, S) je BKG, kde  $N = \{A_1, A_2, \dots, A_n\}, T = \{a_1, a_2, \dots, a_m\}$
- LR-syntaktický analyzátor je rozšířený zásobníkový automat M se stavy  $Q = \{q_0, q_1, ..., q_k\}$ , kde  $q_0$  je počáteční stav.
- Činnost *M* je založena na LR tabulce, která má následující dvě části:
  - 1) Akční část (tabulka akcí)
  - 2) Přechodová část (tabulka přechodů)

# Akční část & přechodová část

#### Akční část:



$$\alpha[q_i, a_i] = 1, 2, 3 \text{ nebo } 4$$

- 1) sq: s = shift,  $q \in Q$
- 2) rp:  $\mathbf{r} = r$ edukce,  $p \in P$
- 3) **:** úspěch
- 4) prázdné políčko: chyba

#### Přechodová část:

$$\beta[q_i, A_j] = 1 \text{ nebo } 2$$

- 1)  $q: q \in Q$
- 2) prázdné políčko

### LR syntaktický analyzátor: Algoritmus

- Vstup: LR tabulka pro  $G = (N, T, P, S); x \in T^*$
- Výstup: Pravý rozbor x, pokud  $x \in L(G)$ , jinak chyba
- Metoda:
- Vlož  $\langle \$, q_0 \rangle$  na zásobník;  $stav := q_0$ ;
- repeat
  - nechť  $a = aktuální znak na vstupu case <math>\alpha[stav, a]$  of:
    - sq: push( $\langle a, q \rangle$ ) & přečti další symbol a ze vstupu & stav := q;
    - rp: zaměň  $\langle ?, q \rangle \langle X_1, ? \rangle \langle X_2, ? \rangle ... \langle X_n, ? \rangle$  za  $\langle A, stav \rangle$  na vrcholu zásobníku & zapiš p na výstup, kde p:  $A \rightarrow X_1 X_2 ... X_n \in P$  and  $stav := \beta[q, A]$ ;
    - ©: úspěch
  - prázdné políčko: chyba until úspěch or chyba

```
G_{expr1} = (N, T, P, E), \text{ kde } N = \{E, F, T\}, T = \{i, +, *, (, )\}, P = \{1: E \to E + T, 2: E \to T, 3: T \to T * F, 4: T \to F, 5: F \to (E), 6: F \to i \}
```

LR-tabulka pro  $G_{expr1}$ :

α	i	+	*			<b>\$</b>		β	E	T	F
0	<b>S</b> 5			<b>S4</b>				0	1	2	3
1		<b>S</b> 6						1			
2		<b>r2</b>	<b>s</b> 7		<b>r2</b>	<b>r2</b>		2			
3		r4	r4		<b>r4</b>	<b>r4</b>	Akční část	3			
4	<b>S</b> 5			<b>s4</b>		\	$lacksquare$ pro $G_{expr1}$	4	8	2	3
5		r6	<b>r6</b>		<b>r6</b>	<b>r6</b>	r - expr1	5			
6	<b>S</b> 5			<b>s4</b>			Přechodová	6		9	3
7	<b>S</b> 5			<b>s</b> 4				7			10
8		<b>s6</b>			<b>s11</b>		část pro $G_{expr1}$	8			
9		r1	<b>s</b> 7		<b>r1</b>	<b>r1</b>		9			
<i>10</i>		<b>r3</b>	<b>r3</b>		<b>r3</b>	<b>r3</b>		<i>10</i>			
<i>11</i>		r5	<b>r5</b>		<b>r5</b>	<b>r5</b>		<i>11</i>			

Pravidla:  $1: E \to E+T, \quad 2: E \to T, \quad 3: T \to T*F, \\ 4: T \to F, \quad 5: F \to (E), \quad 6: F \to i$ 

Zásobník	St.	Vstup	Akce	Pravidlo

Pravidla:  $1: E \to E+T, \quad 2: E \to T, \quad 3: T \to T*F, \\ 4: T \to F, \quad 5: F \to (E), \quad 6: F \to i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	<i>i</i> * <i>i</i> \$	$\alpha[0, i] = s5$	

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$ $\langle \$, 0 \rangle \langle i, 5 \rangle$	<b>0 5</b>	i*i\$ *i\$	$\alpha[0, i] = s5$ $\alpha[5, *] = r6$	$6 \cdot F \rightarrow i$
\Ψ, •/\•, •/		ιψ		<b>U. 1</b>

Pravidla:  $1: E \to E+T, \quad 2: E \to T, \quad 3: T \to T*F, \\ 4: T \to F, \quad 5: F \to (E), \quad 6: F \to i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
Zásobník $\langle \$, 0 \rangle$ $\langle \$, 0 \rangle \langle i, 5 \rangle$	St. 0 5	*i\$ *i\$	Akce $\alpha[0, i] = s5$ $\alpha[5, *] = r6$ $\beta[0, F] = 3$	

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	<i>i*i</i> \$	$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$	$6: F \rightarrow i$
(d) (1) (2)		<b>₩</b> •Φ	$\beta[0, F] = 3$	4 70
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$	$4: T \to F$

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0		$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$	$6: F \rightarrow i$
		** <b>*</b>	$\beta[0, F] = 3$	4 65 5
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$	$4: T \to F$
			$\beta[0, T] = 2$	

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0		$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$	6: $F \rightarrow i$
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\beta[0, F] = 3$ $\alpha[3, *] = r4$	$4: T \to F$
\Φ, •/\1', •/	3	μφ	$\beta[0, T] = 2$	<b>→. 1</b> → 1
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$	$\alpha[2,*]=\$7$	

Pravidla:1:  $E \rightarrow E+T$ , 2:  $E \rightarrow T$ , 3:  $T \rightarrow T*F$ ,4:  $T \rightarrow F$ , 5:  $F \rightarrow (E)$ , 6:  $F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	<i>i*i</i> \$	$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$ $\beta[0, F] = 3$	$6: F \rightarrow i$
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$	$4: T \to F$
		<b></b> • ch	$\beta[0, T] = 2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$ i\$	$\alpha[2, *] = s7$	
$\langle\$,0\rangle\langle T,2\rangle\langle *,7\rangle$	7	15	$\alpha[7, i] = s5$	

Pravidla:  $1: E \to E+T, \quad 2: E \to T, \quad 3: T \to T*F, \\ 4: T \to F, \quad 5: F \to (E), \quad 6: F \to i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$ $\langle \$, 0 \rangle \langle i, 5 \rangle$	<b>0 5</b>	i*i\$ *i\$	$\alpha[0, i] = s5$ $\alpha[5, *] = r6$	$6: F \rightarrow i$
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\beta[0, F] = 3$ $\alpha[3, *] = r4$	$4: T \to F$
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$	$\beta[0, T] = 2$ $\alpha[2, *] = 57$	
$\langle\$,0\rangle\langle T,2\rangle\langle *,7\rangle \ \langle\$,0\rangle\langle T,2\rangle\langle *,7\rangle\langle i,5\rangle$	<b>7 5</b>	<i>i</i> \$ \$	$\alpha[7, i] = s5$ $\alpha[5, \$] = r6$	$6: F \rightarrow i$

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$ $\langle \$, 0 \rangle \langle i, 5 \rangle$	0 5	i*i\$ *i\$	$\alpha[0, i] = s5$ $\alpha[5, *] = r6$ $\beta[0, E] = 3$	$6: F \rightarrow i$
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$eta[0, F] = 3$ $\alpha[3, *] = r4$ $\beta[0, T] = 2$	$4: T \to F$
$\langle \$, 0 \rangle \langle T, 2 \rangle$ $\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	2 7	*i\$ i\$	$\alpha[2, *] = s7$ $\alpha[7, i] = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	\$	$\alpha[5, \$] = \mathbf{r6}$ $\beta[7, F] = 10$	

Pravidla:  $1: E \to E+T, \quad 2: E \to T, \quad 3: T \to T*F, \\ 4: T \to F, \quad 5: F \to (E), \quad 6: F \to i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	_	$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$	$6: F \rightarrow i$
/\$ 0\/T 2\	2	<b>*</b> -o	$\beta[0, F] = 3$	4. T . T
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$ $\beta[0, T] = 2$	$4: T \to F$
$\langle\$,0\rangle\langle T,2\rangle$	2	*i\$	$\alpha[2, *] = 57$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	7	<i>i</i> \$	$\alpha[7, i] = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	<i>i</i> \$	$\alpha[5, \$] = \mathbf{r}6$	$6: F \rightarrow i$
			$\beta[7, F] = 10$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle F, 10 \rangle$	10	\$	$\alpha[10, \$] = r3$	$3: T \rightarrow T^*F$

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0 5	i*i\$ *i\$	$\alpha[0, i] = \$5$	$6: F \rightarrow i$
$\langle \$, 0 \rangle \langle i, 5 \rangle$	3	·ιφ	$\alpha[5, *] = r6$ $\beta[0, F] = 3$	$0.\ \mathbf{F} \rightarrow \mathbf{t}$
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$ $\beta[0, T] = 2$	$4: T \to F$
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$	$\alpha[2, *] = 57$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	7	<i>i</i> \$ \$	$\alpha[7, i] = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	\$	$\alpha[5, \$] = \mathbf{r6}$ $\beta[7, F] = 10$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle F, 10 \rangle$	10	\$	$\alpha[10, \$] = r3$	
			$\beta[0, T] = 2$	

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	_	$\alpha[0,i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$ $\beta[0, F] = 3$	$6: F \rightarrow i$
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$	$4: T \rightarrow F$
		4	$\beta[0, T] = 2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$	$\alpha[2, *] = $7$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	7	<i>i</i> \$	$ \alpha[7, i]  = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	<b>\$</b>	$\alpha[5, \$] = r6$	
			$\beta[7, F] = 10$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle F, 10 \rangle$	10	\$	$\alpha[10, \$] = r3$	$3: T \to T^*F$
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	\$	eta[0, T] = 2 $\alpha[2, \$] = r2$	$2: E \rightarrow T$
(Ψ, ♥/\1, , 2/		Ψ	$[\omega_{L}^{2}, \psi] - L^{2}$	

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	<i>i</i> * <i>i</i> \$	$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = r6$	$6: F \rightarrow i$
(d) (1) (2)		<b>*</b> •ch	$\beta[0, F] = 3$	4 70 0
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = r4$	$4: T \to F$
$\langle\$,0\rangle\langle T,2\rangle$	2	*i\$	$\beta[0, T] = 2$ $\alpha[2, *] = 57$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	7	<i>i</i> \$	$\alpha[2, i] = s7$ $\alpha[7, i] = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	<b>\$</b>	$\alpha[5,\$] = \mathbf{r}6$	$6: F \rightarrow i$
		·	$\beta[7, F] = 10$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle F, 10 \rangle$	10	<b>\$</b>	$\alpha[10, \$] = r3$	$3: T \rightarrow T*F$
(4, 0) (5, 0)		<b>.</b>	$\beta[0, T] = 2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	\$	$\alpha[2, \$] = r^2$	$2: E \to T$
			$\beta[0, E] = 1$	

Pravidla:  $1: E \rightarrow E+T, 2: E \rightarrow T, 3: T \rightarrow T*F, 4: T \rightarrow F, 5: F \rightarrow (E), 6: F \rightarrow i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	<i>i</i> * <i>i</i> \$	$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = \mathbf{r6}$	$6: F \rightarrow i$
			$\beta[0, F] = 3$	
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$	$\alpha[3, *] = \mathbf{r4}$	$4: T \to F$
			$\beta[0,T]=2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$	$\alpha[2, *] = \$7$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	7	<i>i</i> \$	$ \alpha[7, i]  = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	\$	$\alpha[5,\$]=\mathbf{r}_{6}$	$6: F \rightarrow i$
			$[\beta[7, F] = 10]$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle F, 10 \rangle$	<b>10</b>	\$	$\alpha[10, \$] = r3$	$3: T \rightarrow T*F$
			$\beta[0,T]=2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	\$	$\alpha[2, \$] = r2$	$2: E \to T$
			$\beta[0, E] = 1$	
$\langle \$, 0 \rangle \langle E, 1 \rangle$	1	<b>\$</b>	$\alpha[1, \S] = \odot$	

Pravidla:  $1: E \to E+T, \quad 2: E \to T, \quad 3: T \to T*F, \\ 4: T \to F, \quad 5: F \to (E), \quad 6: F \to i$ 

Zásobník	St.	Vstup	Akce	Pravidlo
$\langle \$, 0 \rangle$	0	<i>i*i</i> \$	$\alpha[0, i] = s5$	
$\langle \$, 0 \rangle \langle i, 5 \rangle$	5	*i\$	$\alpha[5, *] = \mathbf{r}6$	$6: F \rightarrow i$
			$\beta[0, F] = 3$	
$\langle \$, 0 \rangle \langle F, 3 \rangle$	3	*i\$		$4: T \rightarrow F$
(4. 0) ( 0)		• • •	$\beta[0, T] = 2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	*i\$	$\alpha[2, *] = \$7$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle$	7	<i>i</i> \$	$\alpha[7, i] = s5$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle i, 5 \rangle$	5	\$	$\alpha[5,\$] = \mathbf{r}6$	
(A 0) (T 0) (T 10)		Φ.	$\beta[7, F] = 10$	
$\langle \$, 0 \rangle \langle T, 2 \rangle \langle *, 7 \rangle \langle F, 10 \rangle$	10	\$		$3: T \to T^*F$
/d		φ	$\beta[0, T] = 2$	
$\langle \$, 0 \rangle \langle T, 2 \rangle$	2	\$	$\alpha[2, \$] = r2$	
/d		ф	$ \beta[0, E]  = 1$	Üspěch
$\langle \$, 0 \rangle \langle E, 1 \rangle$	1	***	$[\alpha[1, \S] = \odot]$	Pravý rozbor: 646

# Konstrukce LR tabulky: Úvod

• Jeden algoritmus pro syntaktickou analýzu, ale spousta algoritmů pro konstrukci LR-tabulky.

#### Základní algoritmy pro konstrukci LR tabulky:

- 1) Simple LR (SLR): nejslabší, ale jednoduchý a vytvoří málo stavů
- 2) Canonical LR: více silný, ale vytvoří poměrně hodně stavů
- 3) Lookahead LR (LALR): nejlepší, protože nejsilnější a vytvoří stejný počet stavů jako SLR

### Rozšířená gramatika s "hloupým" pravidlem

Myšlenka: Gramatika se speciálním "startovacím pravidlem"

**Definice:** Necht' 
$$G = (N, T, P, S)$$
 je BKG,  $S' \notin N$ .  $Rozšířená gramatika$  pro  $G$  je gramatika  $G' = (N \cup \{S'\}, T, P \cup \{S' \rightarrow S\}, S')$ .

**Proč hloupé pravidlo?** Až je použito pravidlo  $S' \rightarrow S$  a vstupní token je ukončovač řetězce, potom je syntaktická analýza **úspěšně dokončena**.

#### Příklad:

$$K = (N, T, P, S)$$
, where  $N = \{S, A\}$ ,  $T = \{i, o, (,)\}$ ,  $P = \{1: S \rightarrow SoA, 2: S \rightarrow A, 3: A \rightarrow i, 4: A \rightarrow (S)\}$ 

#### Rozšířená gramatika pro K:

$$H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (, )\}, P = \{0: S' \to S, 1: S \to SoA, 2: S \to A, 3: A \to i, 4: A \to (S)\}$$

# Konstrukce LR tabulky: Položky

Myšlenka: Položka je pravidlo s tečkou • na pravé straně pravidla.

**Definice:** Necht' G = (N, T, P, S) je BKG,  $A \rightarrow x \in P, x = yz$ . Potom  $A \rightarrow y \cdot z$  je položka.

**Příklad:** Uvažujme  $S \rightarrow SoA$ 

Všechny položky pro pravidlo  $S \rightarrow SoA$  jsou:

 $S \rightarrow \bullet SoA, S \rightarrow S \bullet oA, S \rightarrow So \bullet A, S \rightarrow SoA \bullet$ 

**Význam:**  $A \rightarrow y \bullet z$  říká, že pokud y se vyskytuje na zásobníku a prefix zbytku vstupního řetězce se dá postupně zredukovat na z, potom yz = x může být zredukováno na A užitím pravidla  $A \rightarrow x$ .

# Uzávěr položek: Algoritmus

**Pozn.:** Uzávěr položky *I*, *Closure*(*I*) je množina položek definována pomocí následujícího algoritmu:

- Vstup: G = (N, T, P, S); položka I
- Výstup: Closure(I)
- Metoda:
- $Closure(I) := \{I\};$
- Používej následující pravidlo, dokud bude možné měnit množinu *Closure(I)*:
  - if  $A \to y \bullet Bz \in Closure(I)$  and  $B \to x \in P$ then přidej položku  $B \to \bullet x$  do Closure(I)

# Uzávěr položek: Příklad 1/2

```
H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (, )\}, P = \{0: S' \to S, 1: S \to SoA, 2: S \to A, 3: A \to i, 4: A \to (S)\}
```

**Určeme:** Closure(I) for  $I = S' \rightarrow \bullet S$ 

$$Closure(I) := \{S' \rightarrow \bullet S\}$$

- 1)  $S' \rightarrow \bullet S \in Closure(I) \& S \rightarrow SoA \in P$ : **přidej**  $S \rightarrow \bullet SoA$  **do** Closure(I) $Closure(I) = \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA\}$
- 2)  $S' \rightarrow \bullet S \in Closure(I) \& S \rightarrow A \in P$ : přidej  $S \rightarrow \bullet A$  do Closure(I) $Closure(I) = \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A\}$

### Uzávěr položek: Příklad 2/2

$$H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (, )\}, P = \{0: S' \to S, 1: S \to SoA, 2: S \to A, 3: A \to i, 4: A \to (S)\}$$

- 3)  $S \rightarrow \bullet A \in Closure(I) \& A \rightarrow i \in P$ : přidej  $A \rightarrow \bullet i$  do Closure(I) $Closure(I) = \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i\}$
- 4)  $S \rightarrow \bullet A \in Closure(I) \& A \rightarrow (S) \in P$ : **přidej**  $A \rightarrow \bullet (S)$  **do** Closure(I)

#### Celkově:

 $Closure(I) = \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \to yU \bullet z)$ ,  $kde A \to y \bullet Uz \in I$ .

**Definice:** Nechť G = (N, T, P, S) je BKG, I je množina položek a  $U \in T \cup N$ . Potom  $\Theta_U(I) = \{j: j \in Closure(A \rightarrow yU \bullet z), A \rightarrow y \bullet Uz \in I\}$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

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#### **Příklad:**

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Určeme:  $\Theta_{A}(I)$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

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#### Určeme: $\Theta_{A}(I)$

 $Closure(S \rightarrow SoA \bullet)$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

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Určeme:  $\Theta_{A}(I)$ 

 $Closure(S \rightarrow SoA \bullet)$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \to yU \bullet z)$ ,  $kde A \to y \bullet Uz \in I$ .

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Určeme:  $\Theta_{A}(I)$ 

 $Closure(S \rightarrow SoA \bullet) \cup Closure(S \rightarrow A \bullet)$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

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Definice: Nechť G = (N, T, P, S) je BKG, I je množina položek a U \in T \cup N. Potom \Theta_U(I) = \{j: j \in Closure(A \rightarrow yU \circ z), A \rightarrow y \circ Uz \in I\}
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#### **Příklad:**

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H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\},\
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I = \{S \rightarrow So \bullet A, S \rightarrow \bullet A, A \rightarrow \bullet (S)\}
```

Určeme:  $\Theta_{A}(I)$ 

 $Closure(S \to SoA \bullet) \cup Closure(S \to A \bullet) = \{S \to SoA \bullet, S \to A \bullet\}$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

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Definice: Nechť G = (N, T, P, S) je BKG, I je množina položek a U \in T \cup N. Potom \Theta_U(I) = \{j: j \in Closure(A \rightarrow yU \circ z), A \rightarrow y \circ Uz \in I\}
```

#### Příklad:

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H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\},\
P = \{0: S' \rightarrow S, 1: S \rightarrow SoA, 2: S \rightarrow A, 3: A \rightarrow i, 4: A \rightarrow (S)\},\
I = \{S \rightarrow So \bullet A, S \rightarrow \bullet A, A \rightarrow \bullet (S)\}
```

Určeme:  $\Theta_{A}(P)$ 

$$Closure(S \rightarrow SoA \bullet) \cup Closure(S \rightarrow A \bullet) = \{S \rightarrow SoA \bullet, S \rightarrow A \bullet\}$$

Určeme:  $\Theta(I)$ 

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

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Definice: Nechť G = (N, T, P, S) je BKG, I je množina položek a U \in T \cup N. Potom \Theta_U(I) = \{j: j \in Closure(A \rightarrow yU \circ z), A \rightarrow y \circ Uz \in I\}
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#### **Příklad:**

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H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\},

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I = \{S \rightarrow So \bullet A, S \rightarrow \bullet A, A \rightarrow \bullet (S)\}
```

Určeme:  $\Theta_{A}(\mathbf{P})$ 

$$Closure(S \to SoA \bullet) \lor Closure(S \to A \bullet) = \{S \to SoA \bullet, S \to A \bullet\}$$

Určeme: Θ(D)

## Množina $\Theta_U(I)$ pro G

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \to yU \bullet z)$ ,  $kde A \to y \bullet Uz \in I$ .

```
Definice: Nechť G = (N, T, P, S) je BKG, I je množina položek a U \in T \cup N. Potom \Theta_U(I) = \{j: j \in Closure(A \rightarrow yU \bullet z), A \rightarrow y \bullet Uz \in I\}
```

#### **Příklad:**

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H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\},

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I = \{S \rightarrow So \bullet A, S \rightarrow \bullet A, A \rightarrow \bullet (S)\}
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## Určeme: $\Theta_{A}(\mathbf{P})$

 $Closure(S \to SoA \bullet) \lor Closure(S \to A \bullet) = \{S \to SoA \bullet, S \to A \bullet\}$ 

#### Určeme: Θ(D)

 $Closure(A \rightarrow (\bullet S))$ 

## Množina $\Theta_U(I)$ pro G

Myšlenka: Pro symbol U a množinu položek I,  $\Theta_U(I)$  značí sjednocení všech uzávěrů tvaru  $Closure(A \rightarrow yU \bullet z)$ , kde  $A \rightarrow y \bullet Uz \in I$ .

**Definice:** Nechť G = (N, T, P, S) je BKG, I je množina položek a  $U \in T \cup N$ . Potom  $\Theta_{U}(I) = \{j: j \in Closure(A \rightarrow yU \bullet z), A \rightarrow y \bullet Uz \in I\}$ 

#### **Příklad:**

```
H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\},

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I = \{S \rightarrow So \bullet A, S \rightarrow \bullet A, A \rightarrow \bullet (S)\}
```

### Určeme: $\Theta_{A}(\mathbf{P})$

 $Closure(S \to SoA \bullet) \lor Closure(S \to A \bullet) = \{S \to SoA \bullet, S \to A \bullet\}$ 

#### Určeme: Θ(D)

 $Closure(A \rightarrow (\bullet S)) = \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}$ 

# Množina $\Theta_G$ pro gramatiku G

**Pozn.:** Množina  $\Theta_G$  pro gramatiku G je množina množin položek definovaných následujícím algoritmem:

- Vstup: Rozšířená G = (N, T, P, S')
- Výstup:  $\Theta_G$  pro gramatiku G
- Metoda:
- $\Theta_G := \{Closure(S' \rightarrow \bullet S)\};$
- for each  $I \in \Theta_G$  and  $U \in N \cup T$ if  $\Theta_U(I) \neq \emptyset$  then přidej  $\Theta_U(I)$  do  $\Theta_G$

```
H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\}, P = \{0: S' \to S, 1: S \to SoA, 2: S \to A, 3: A \to i, 4: A \to (S)\}
```

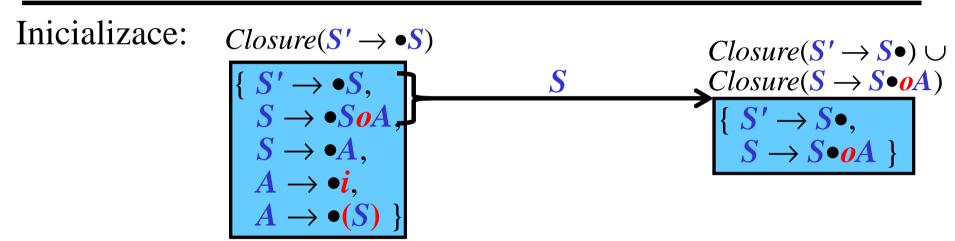
Inicializace:

```
H = (N, T, P, S'), \text{ kde } N = \{S', S, A\}, T = \{i, o, (,)\}, P = \{0: S' \to S, 1: S \to SoA, 2: S \to A, 3: A \to i, 4: A \to (S)\}
```

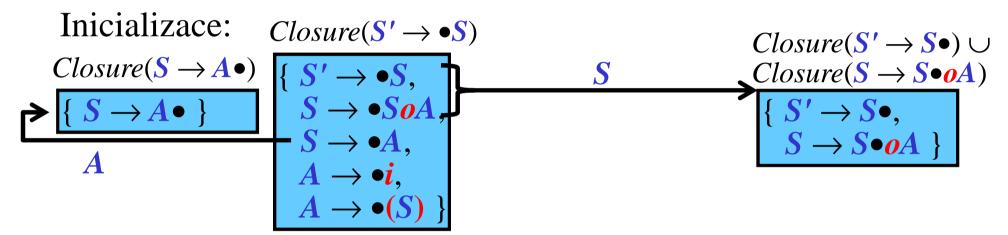
Inicializace:  $Closure(S' \rightarrow \bullet S)$ 

```
\{S' \rightarrow \bullet S, S \rightarrow \bullet S o A, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}
```

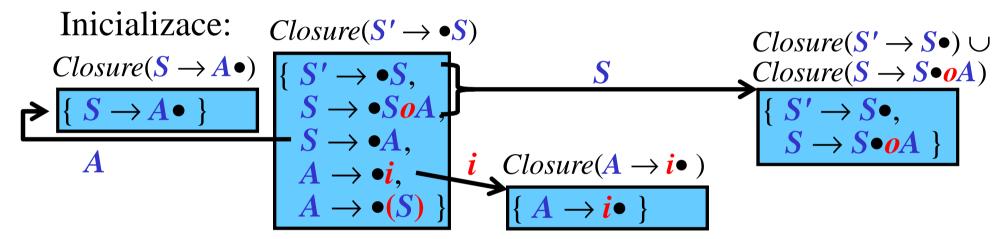
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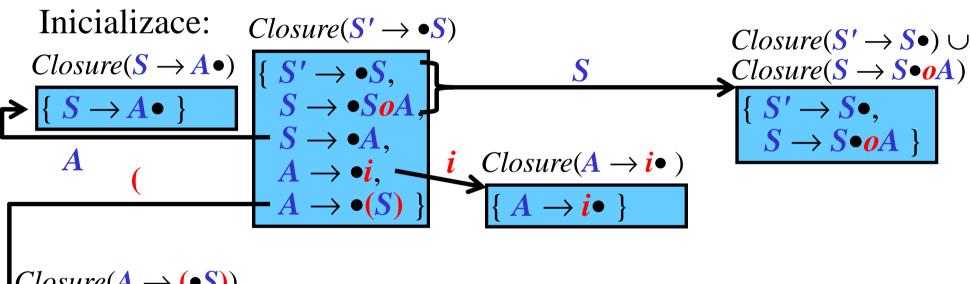
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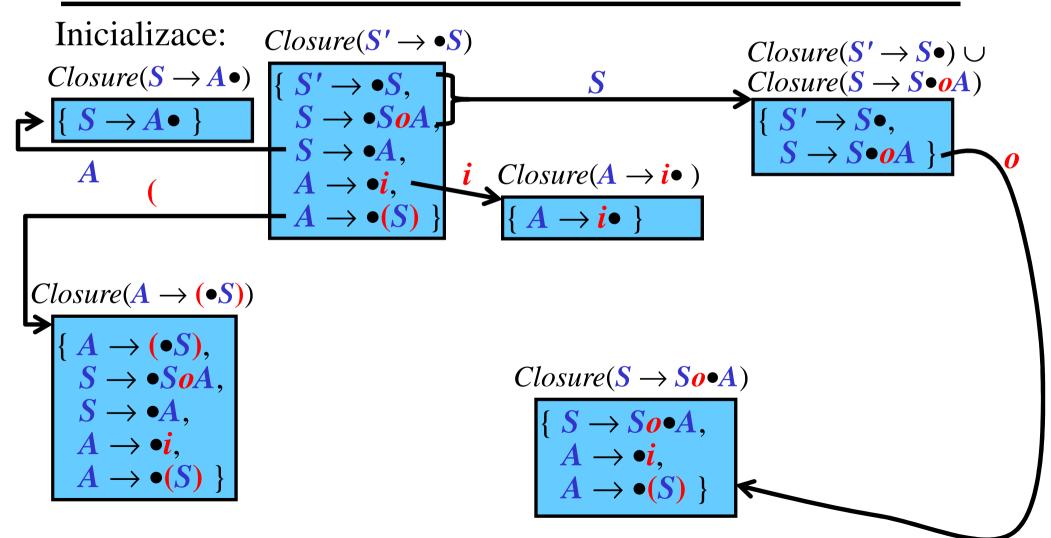


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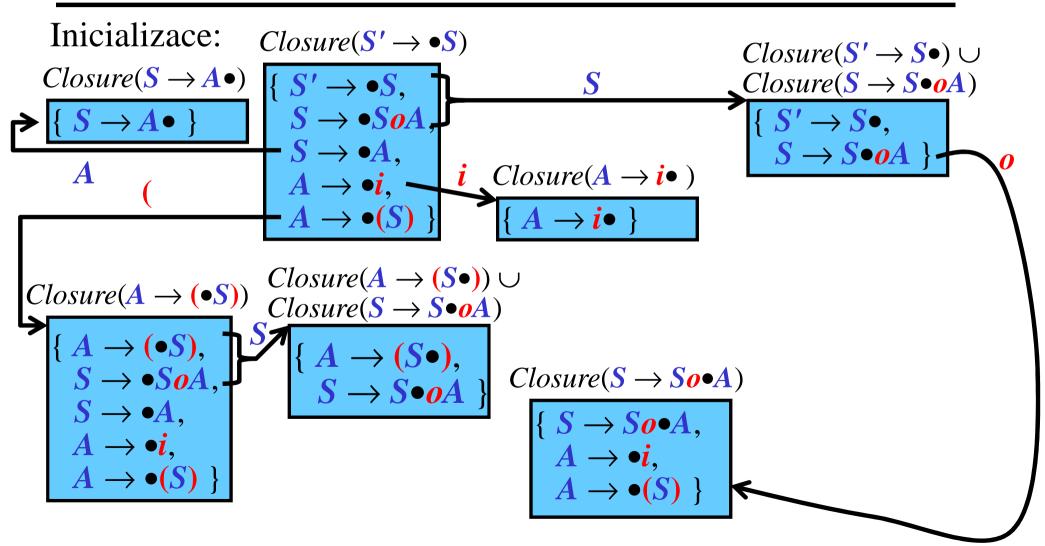


Closure( $A \rightarrow (\bullet S)$ )  $\begin{cases}
A \rightarrow (\bullet S), \\
S \rightarrow \bullet SoA, \\
S \rightarrow \bullet A, \\
A \rightarrow \bullet i, \\
A \rightarrow \bullet (S)
\end{cases}$ 

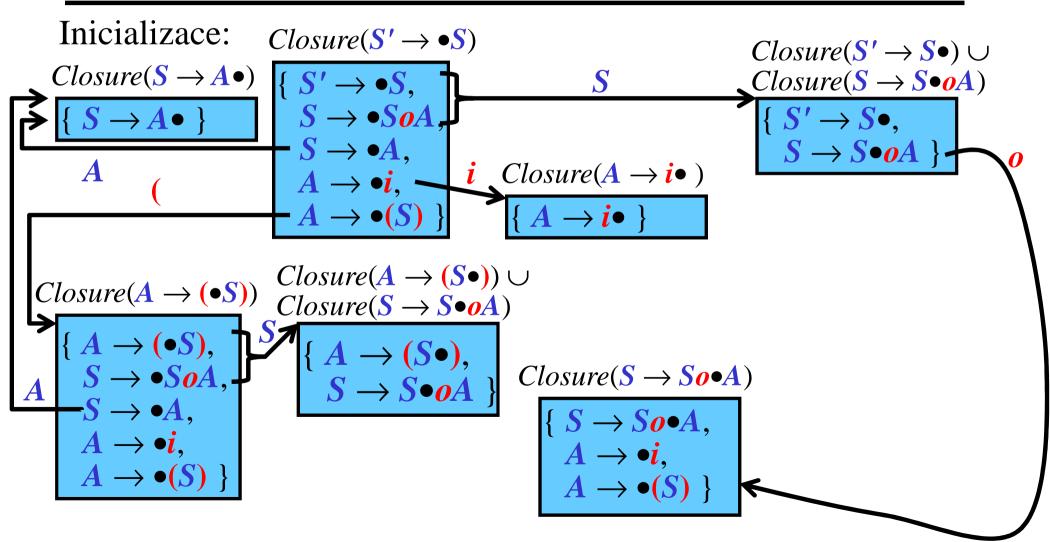
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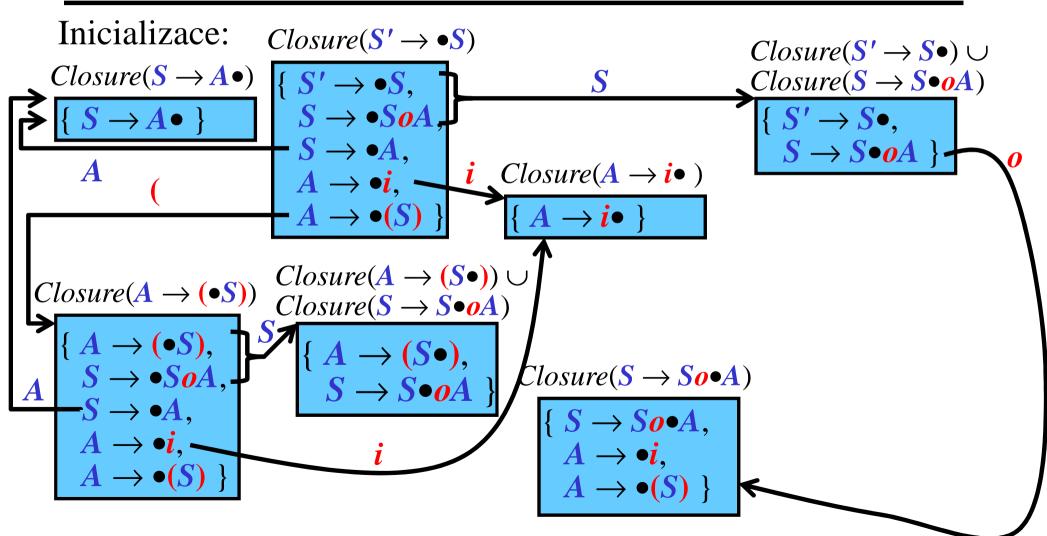
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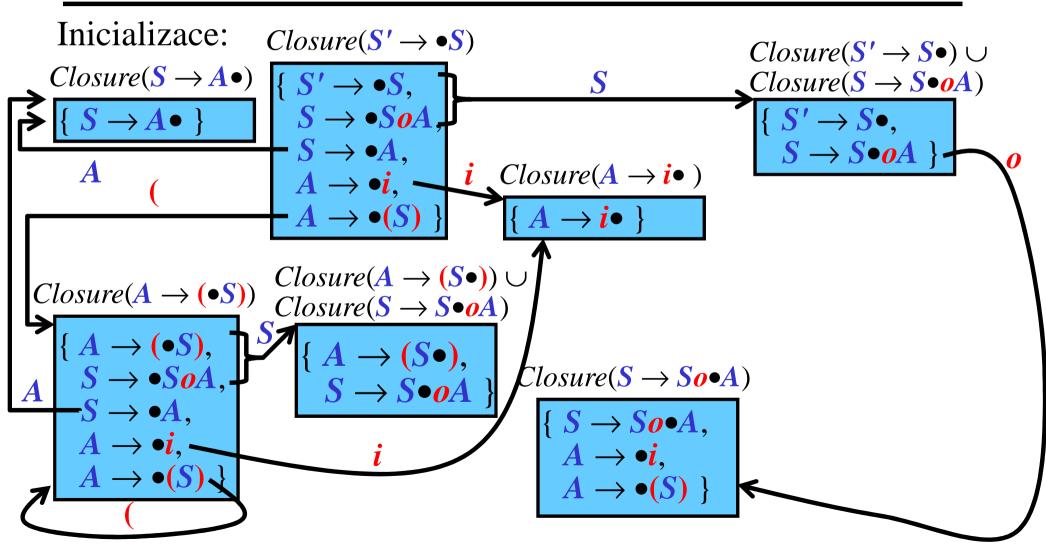
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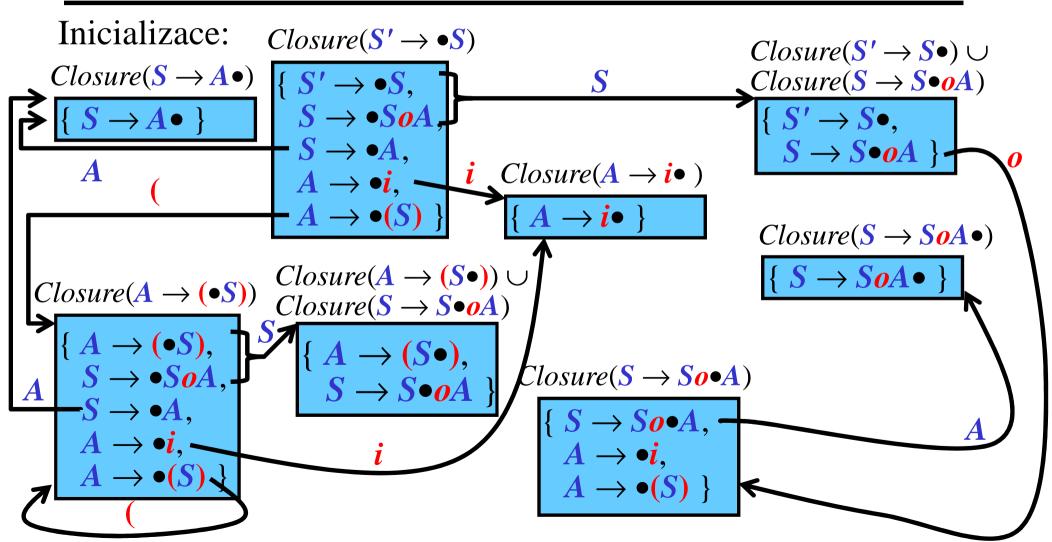
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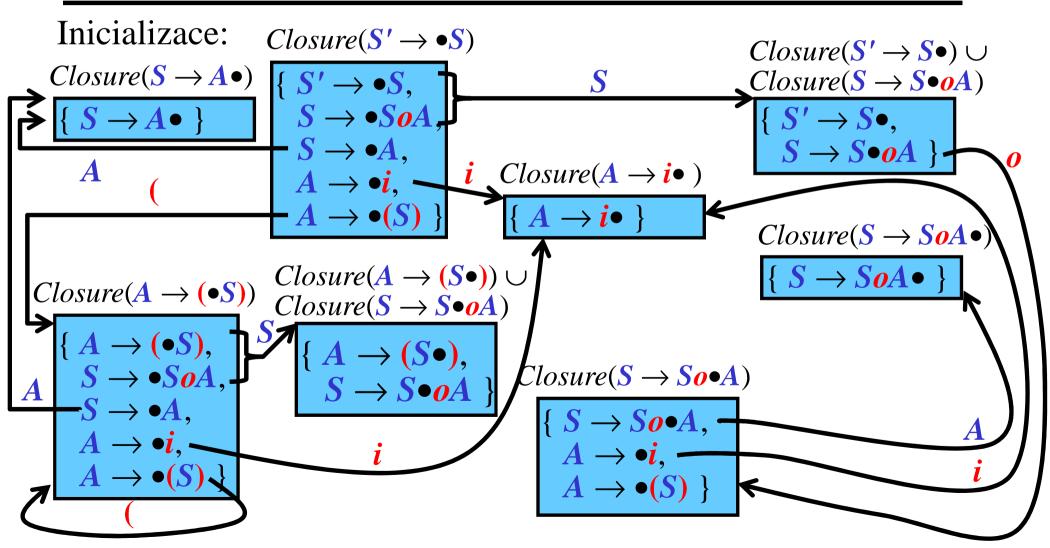
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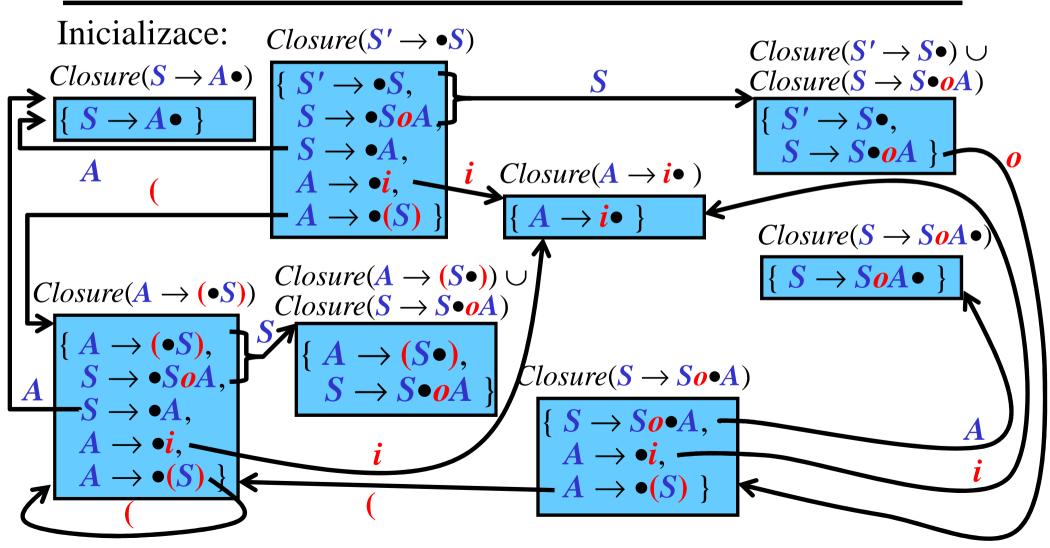
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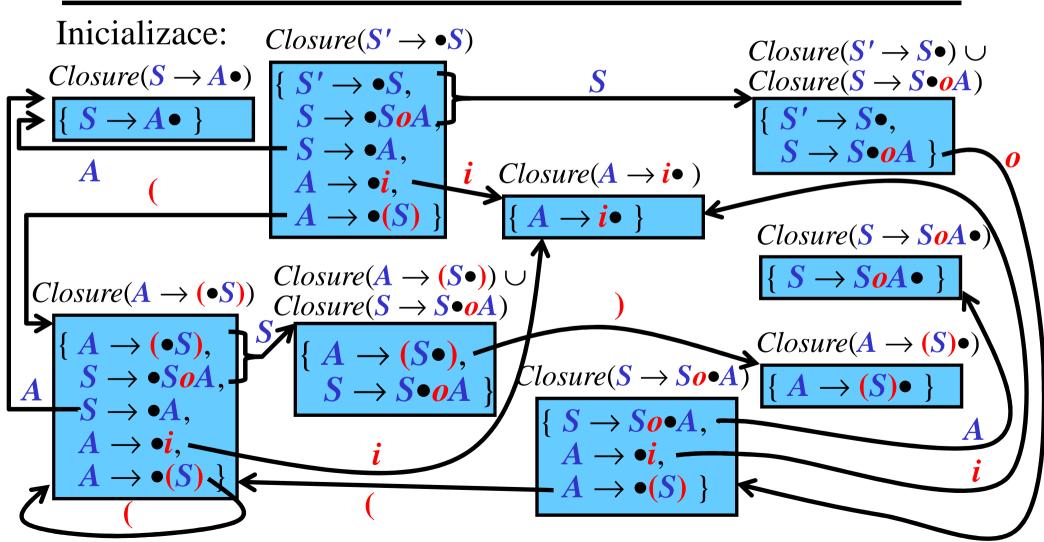
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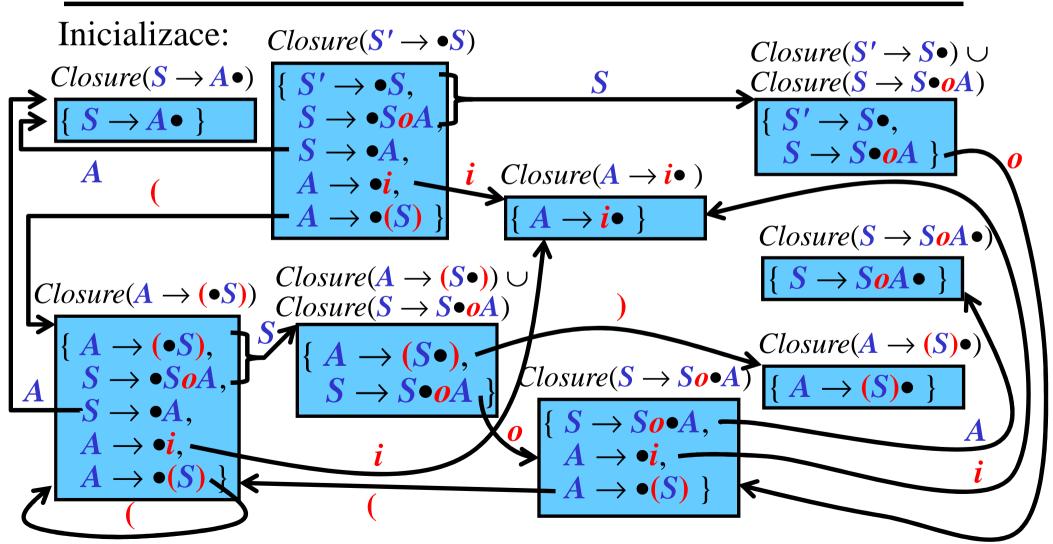
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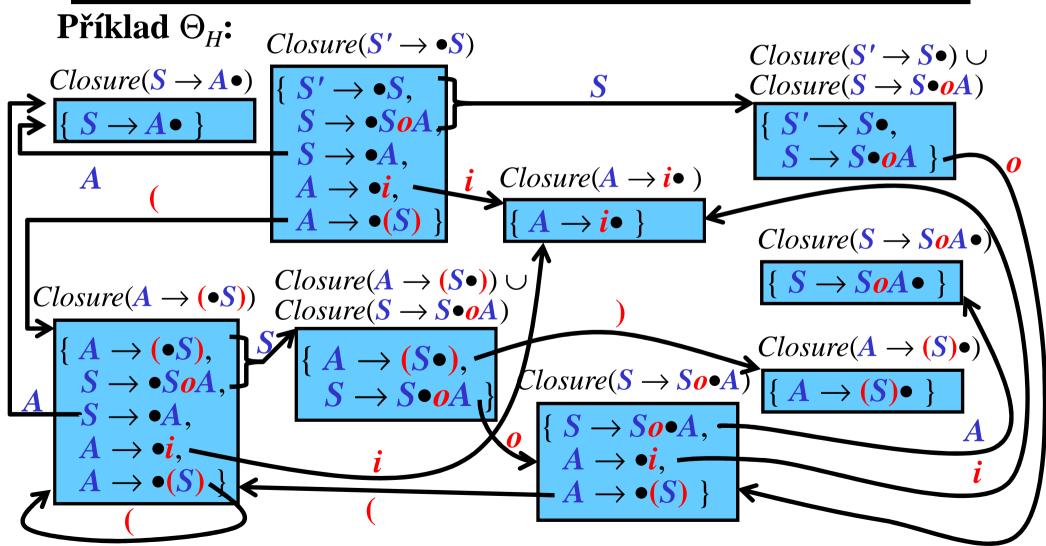
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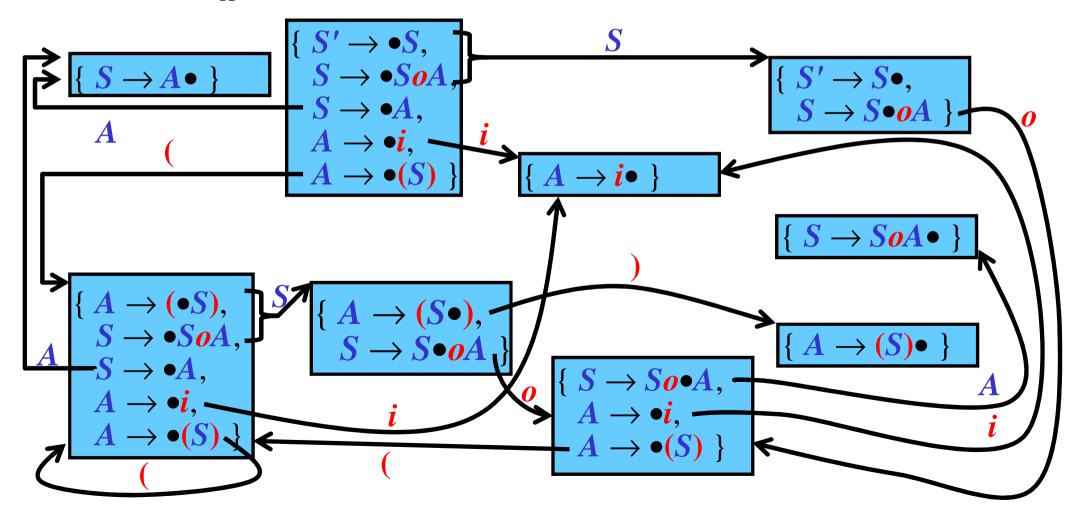


Pojmenujte prvky  $\Theta_G$  jako  $I_0$  až  $I_n$ , kde n+1 je počet prvků (množin) v  $\Theta_G$ . Množinu obsahující  $S' \to \bullet S$  označme  $I_0$ .

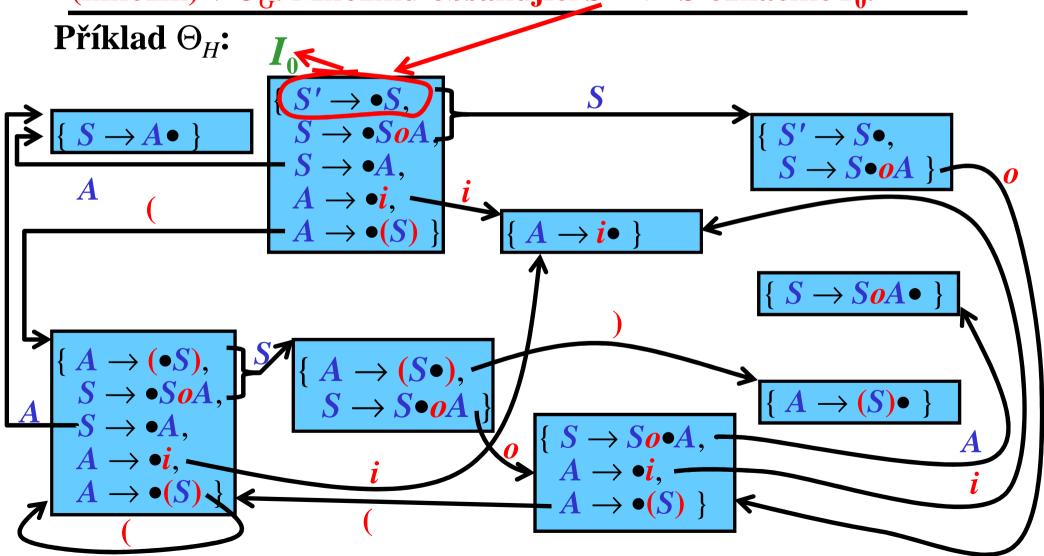


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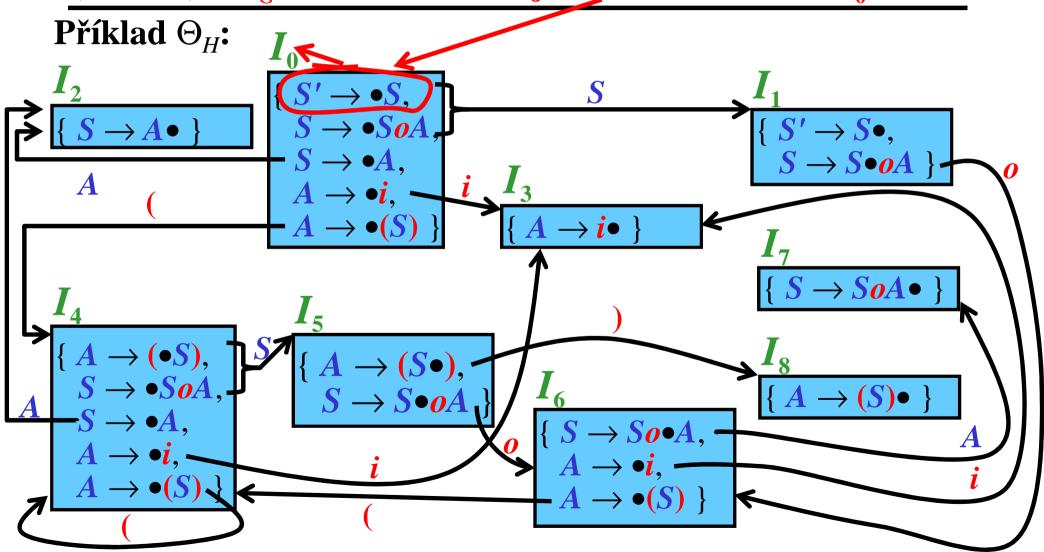
**Příklad**  $\Theta_H$ :



Pojmenujte prvky  $\Theta_G$  jako  $I_0$  až  $I_n$ , kde n+1 je počet prvků (množin) v  $\Theta_G$ . Množinu obsahující  $S' \to \bullet S$  označme  $I_0$ .



Pojmenujte prvky  $\Theta_G$  jako  $I_0$  až  $I_n$ , kde n+1 je počet prvků (množin) v  $\Theta_G$ . Množinu obsahující  $S' \to \bullet S$  označme  $I_0$ .



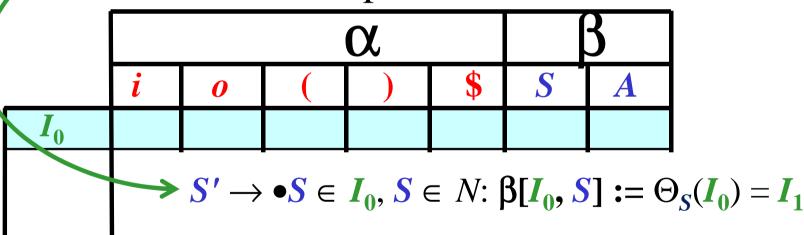
## Konstrukce LR tabulky: SLR Algoritmus

- Vstup: Rozšířená gramatika  $G = (N, T, P, S'); \Theta_G;$  Follow(A) pro všechna  $A \in N$
- Výstup: LR tabulka pro G ( $\alpha$  = akční č.,  $\beta$  = přechodová č.)
- Metoda:
- StatesOfTable :=  $\Theta_G$ ; StartState := Closure( $S' \to \bullet S$ );
- for each  $x \in \Theta_G$  do
- for each  $I \in x$  do
  - case I of
    - $I = A \rightarrow y \bullet Xz$ , kde  $X \in N$ :  $\beta[x, X] := \Theta_X(x)$
    - $I = A \rightarrow y \bullet Xz$ ,  $kde X \in T$ :  $\alpha[x, X] := s\Theta_X(x)$
    - $I = S' \rightarrow S \bullet : \alpha[x, \$] := \bigcirc$
    - $I = A \rightarrow y$   $(A \neq S')$ : for each  $a \in Follow(A)$  do  $\alpha[x, a] := rp$ , kde p je návěští pravidla  $A \rightarrow y$

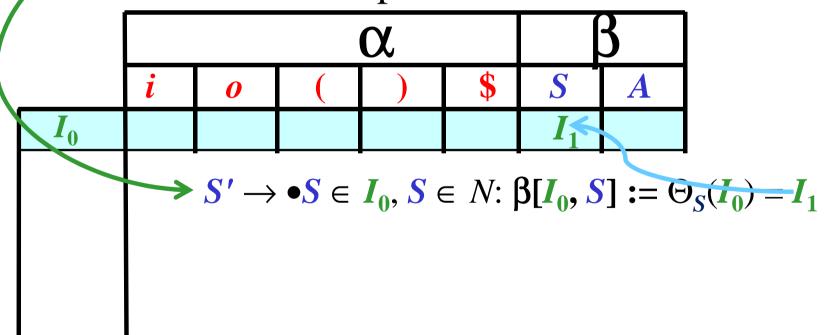
```
\begin{split} &\Theta_{H} = \{I_{0} : \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1} : \{S' \rightarrow S \bullet, S \rightarrow S \bullet oA\}, I_{2} : \{S \rightarrow A \bullet\}, I_{3} : \{A \rightarrow i \bullet\}, \\ &I_{4} : \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5} : \{A \rightarrow (S \bullet), S \rightarrow S \bullet oA\}, I_{6} : \{S \rightarrow So \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7} : \{S \rightarrow SoA \bullet\}, I_{8} : \{A \rightarrow (S) \bullet\}\} \end{split}
```

			β							
	i	0	(	)	\$	S	$\boldsymbol{A}$			
$I_0$										
				•			•			

```
\begin{split} &\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ &I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```

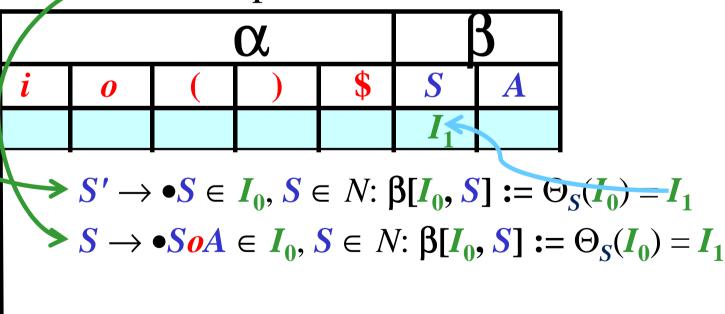


```
\begin{split} &\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ &I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
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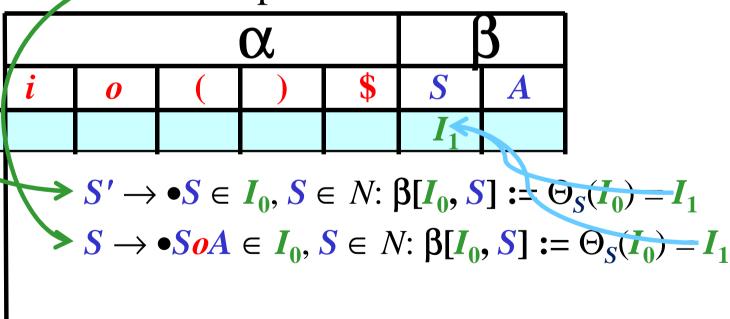


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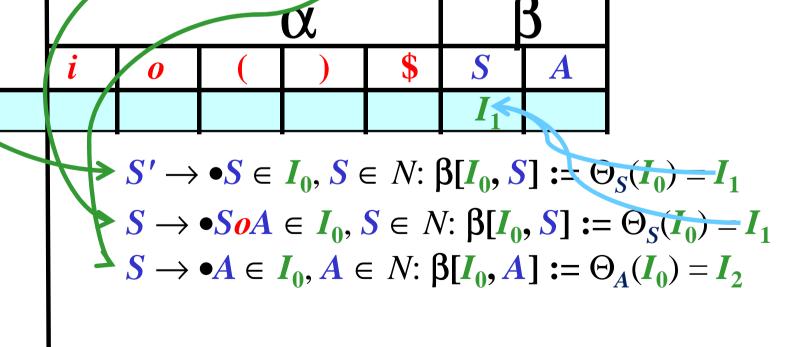
#### **Vrčeme:** L<del>R ta</del>bulku pro *K*



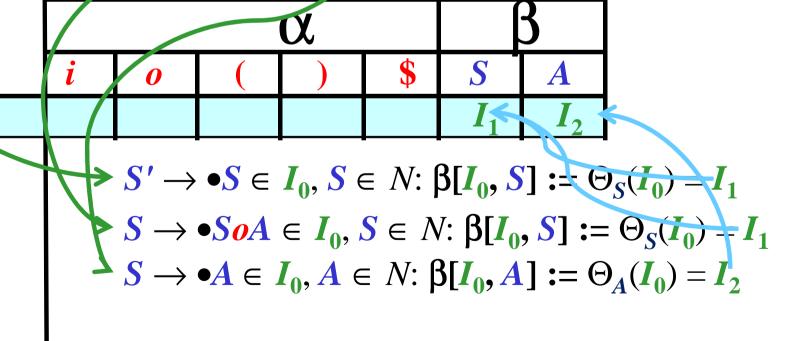
```
\begin{split} &\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bulletoA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ &I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bulletoA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```



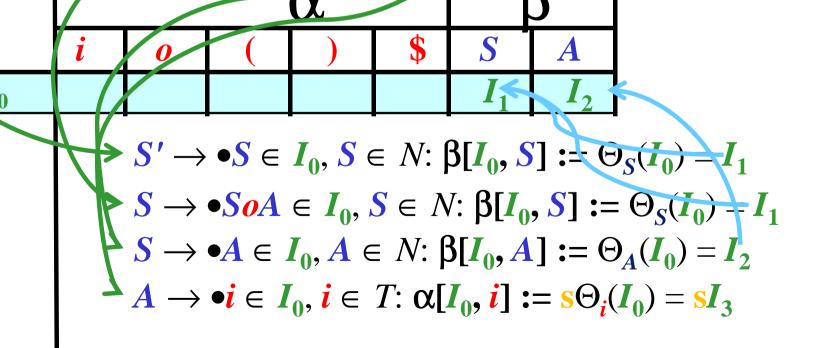
```
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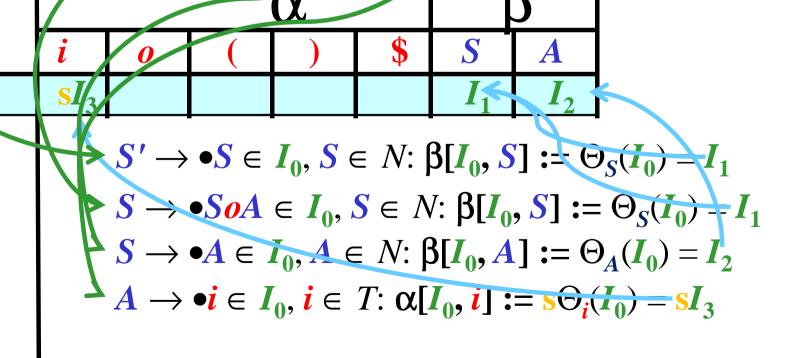
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```



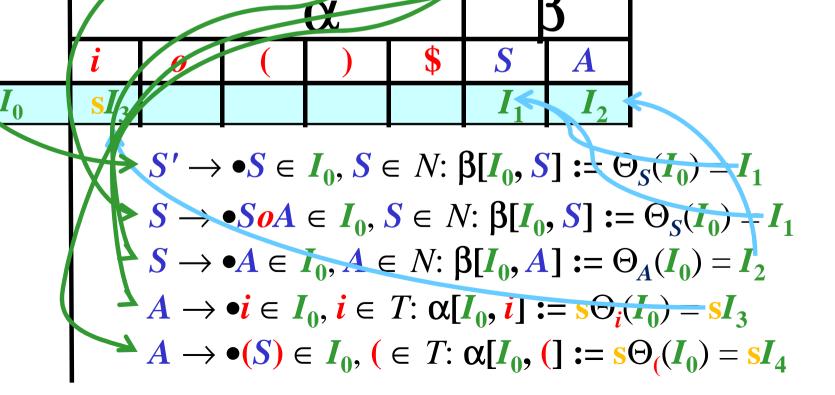
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```



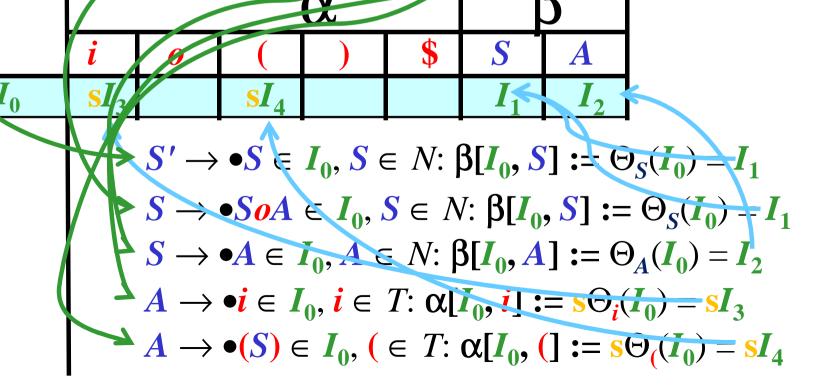
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```
\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{1}: \{S' \rightarrow S \bullet, S \rightarrow S \bullet oA\}, I_{2}: \{S \rightarrow A \bullet\}, I_{3}: \{A \rightarrow i \bullet\}, I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{5}: \{A \rightarrow (S \bullet), S \rightarrow S \bullet oA\}, I_{6}: \{S \rightarrow So \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{7}: \{S \rightarrow SoA \bullet\}, I_{8}: \{A \rightarrow (S) \bullet\}\}
```



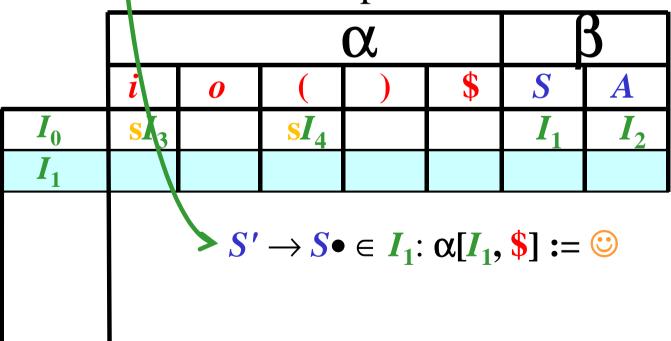
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\begin{split} \Theta_{H} &= \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bulletoA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bulletoA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
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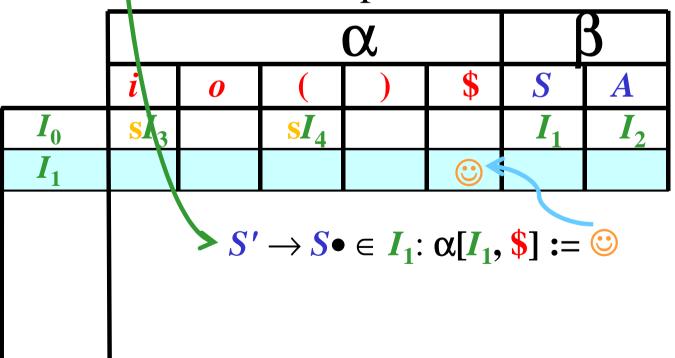
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```

			β				
	i	0	(	)	\$	S	$\boldsymbol{A}$
$I_0$	$SI_3$		$\mathbf{s}I_4$			$I_1$	$I_2$
$I_1$							

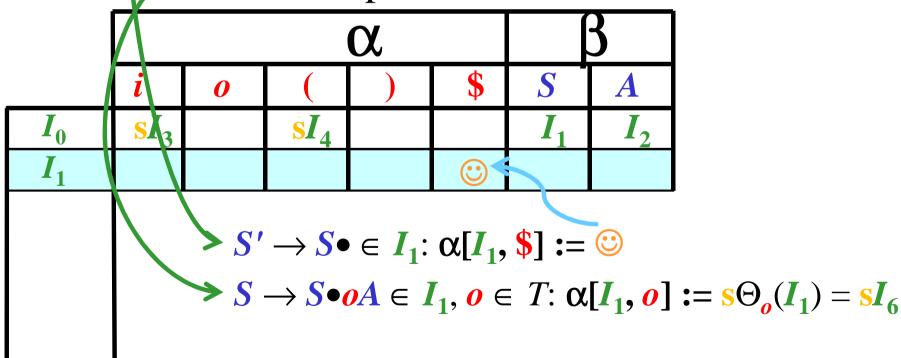
```
\begin{split} \Theta_{H} &= \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```



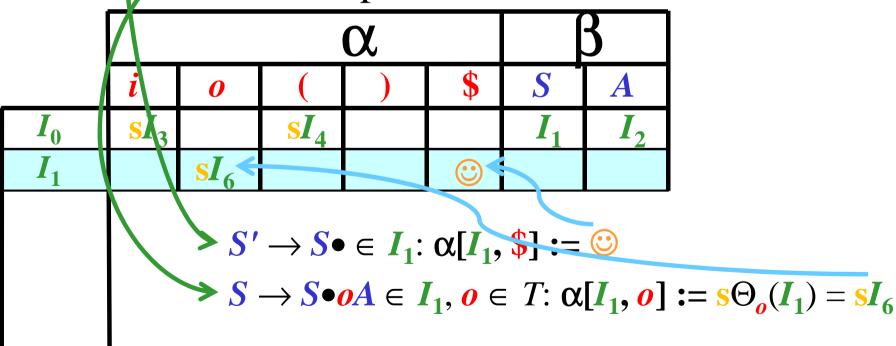
```
\begin{split} \Theta_{H} &= \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```



```
\begin{split} &\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ &I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```



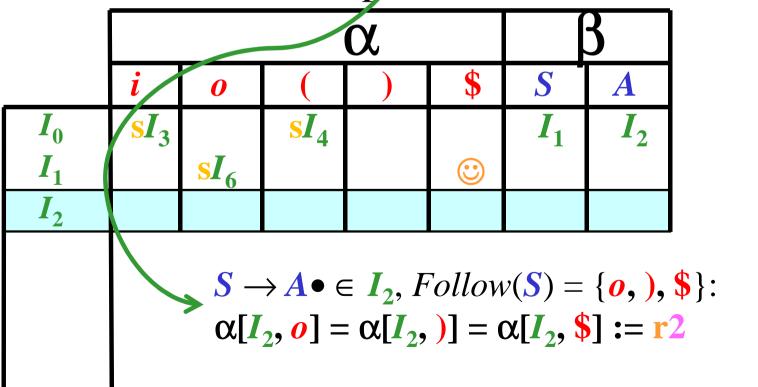
```
\begin{split} &\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ &I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```



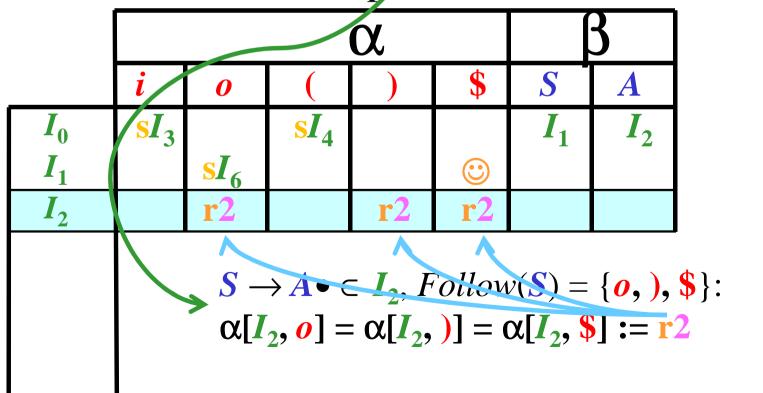
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\begin{split} &\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bullet oA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ &I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bullet oA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ &I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
```

	α				β		
	i	0	(	)	\$	S	$\boldsymbol{A}$
$I_0$	$SI_3$		$SI_4$			$I_1$	$I_2$
$I_1$		$\mathbf{SI}_{6}$					
$I_2$							
-2							

$$\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{1}: \{S' \rightarrow S \bullet, S \rightarrow S \bullet oA\}, I_{2}: \{S \rightarrow A \bullet\}, I_{3}: \{A \rightarrow i \bullet\}, I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{5}: \{A \rightarrow (S \bullet), S \rightarrow S \bullet oA\}, I_{6}: \{S \rightarrow So \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{7}: \{S \rightarrow SoA \bullet\}, I_{8}: \{A \rightarrow (S) \bullet\}\}$$



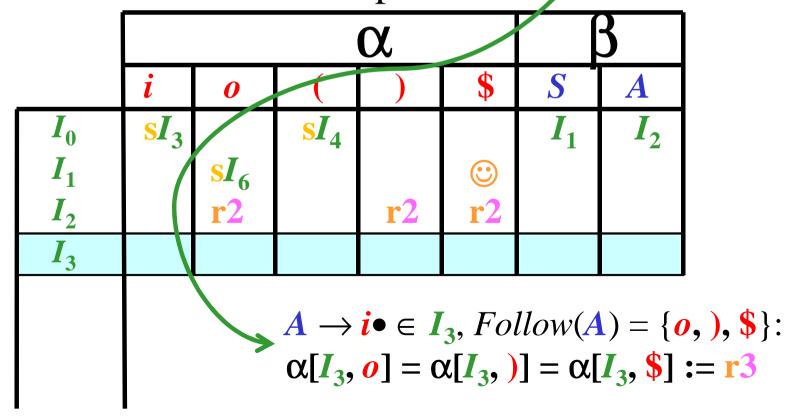
$$\Theta_{H} = \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{1}: \{S' \rightarrow S \bullet, S \rightarrow S \bullet oA\}, I_{2}: \{S \rightarrow A \bullet\}, I_{3}: \{A \rightarrow i \bullet\}, I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{5}: \{A \rightarrow (S \bullet), S \rightarrow S \bullet oA\}, I_{6}: \{S \rightarrow So \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, I_{7}: \{S \rightarrow SoA \bullet\}, I_{8}: \{A \rightarrow (S) \bullet\}\}$$



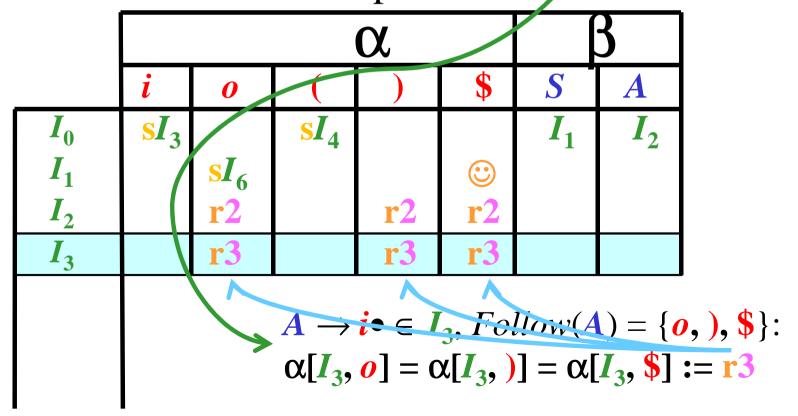
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```

	α				β		
	i	0	(	)	\$	S	$\boldsymbol{A}$
$I_0$	$SI_3$		$\mathbf{s}I_4$			$I_1$	$I_2$
$I_1$		sI <sub>6</sub> r2					
$I_2$		r2		r2	r2		
$I_3$							

```
\begin{split} \Theta_{H} &= \{I_{0}: \{S' \rightarrow \bullet S, S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{1}: \{S' \rightarrow S\bullet, S \rightarrow S\bulletoA\}, I_{2}: \{S \rightarrow A\bullet\}, I_{3}: \{A \rightarrow i\bullet\}, \\ I_{4}: \{A \rightarrow (\bullet S), S \rightarrow \bullet SoA, S \rightarrow \bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{5}: \{A \rightarrow (S\bullet), S \rightarrow S\bulletoA\}, I_{6}: \{S \rightarrow So\bullet A, A \rightarrow \bullet i, A \rightarrow \bullet (S)\}, \\ I_{7}: \{S \rightarrow SoA\bullet\}, I_{8}: \{A \rightarrow (S)\bullet\}\} \end{split}
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#### **Určeme:** LR tabulku pro *K*

			I	α			3
	i	0			\$	S	$\boldsymbol{A}$
$I_0$	$SI_3$		$\mathbf{s}I_4$			$I_1$	$I_2$
$I_1$		$\mathbf{S}I_6$			$\odot$		
$I_2$		r2		r2	r2		
$I_3$		r3		r3	r3		

Zbytek tabulky sestrojte analogicky.

$$A \rightarrow i \in I_3$$
,  $Fellow(A) = \{o, \},$ \$:  
 $\alpha[I_3, o] = \alpha[I_3, ] = \alpha[I_3,$ \$] := r3

#### **Výsledná** LR tabulka pro *K*

	α				β		
	i	0	(	)	\$	S	$\boldsymbol{A}$
$I_0$	$SI_3$		$SI_4$			$I_1$	$I_2$
$I_1$		sI <sub>6</sub> r2					
$I_2$		r2		r2	<b>r2</b>		
$I_3$		r3		r3	r3		
$I_4$	$SI_3$		$SI_4$			$I_5$	$I_2$
$egin{array}{c} I_4 \ I_5 \end{array}$		$\mathbf{SI}_{6}$		$SI_8$			
$I_6$	$SI_3$		$SI_4$				$I_7$
$egin{array}{c} I_6 \ I_7 \end{array}$		r1		r1	r1		
$I_8$		r4		r4	r4		

# Přejmenování stavů

# Přejmenovat stavy:

Old	New
$I_0$	0
$I_1$	1
$I_2$	2
$I_3$	3
$I_4$	4
$I_5$	5
$I_6$	6
$I_7$	7
$I_8$	8

### LR tabulka pro Ks přejmenovanými stavy:

α	i	0			\$
0	<b>s</b> 3		<b>s4</b>		
1		<b>s6</b>			
2		<b>r2</b>		r2	r2
3		r3		r3	r3
4	<b>s</b> 3		<b>s4</b>		
5		<b>s6</b>		<b>s8</b>	
6	<b>s</b> 3		<b>s4</b>		
7		r1		r1	r1
8		r4		r4	r4

β	S	$\overline{A}$
0	1	2
1		
2		
1 2 3 4 5		
4	5	2
5		
6		7
6 7 8		
8		