Machine Learning from the ground up

aka: Demystifying ML

Writing a mock DNN from scratch using only numpy

My AGQ Lectures

Lecture 1: Embracing Python3 & Git

Intro, Intermediate Python3, Git

Getting Setup with Conda, Basics of Numpy & Pandas

Lecture 2: Machine Learning from the ground up

Building a simple **DNN** using **NumPy**, then the same again using **PyTorch**. Constructing a Simple **Classifier** using **PyTorch**.

Lecture 3: More complex Machine Learning models

Building more **complex graphs** using **PyTorch**. Building an **AutoEncoder** using **PyTorch**.

Lecture 4: Modern Machine Learning Concepts

DNN, **CNN**, **Attention** and model **Precision**. Building a **1-bit precision Classifier** using PyTorch

Demystifying ML

- Intro, what do ML experts and Scientists have in common
- Intro to ML model design
- Intro to Backpropagation
- How to write this into code
- Examples from writing and training a simple DNN from scratch
- Considerations around DNN models and some of their limitations

Training a model on data

- "Training a model on data" is the same as "fitting a PDF to a dataset".
- We want to tune free-parameters in the model(*PDF*) to find the set of parameters corresponding to the **maximum likelihood**.
- This is the same as saying we want to find the minima of

-log(Likelihood)

- This is the same as we want to minimize the loss of a model for a given dataset.
- To paraphrase a conversation, I once had:
 "Newton-Raphson the truth out of it until you're done"

"Training" according to a Scientist

- In science fitting is 'easy' I have ~10s of free parameters **p** and dataset **x** which I need to minimize such that:
- Best solution for that? Minuit(2)

$$-\frac{d\ln(\mathcal{L}(\boldsymbol{p};\boldsymbol{x}))}{d\boldsymbol{p}} = \frac{d\ln(PDF(\boldsymbol{p};\boldsymbol{x}))}{d\boldsymbol{p}} = 0$$

- 1. Take (2*parameter+1) "steps" for each **epoch**
 - Each step is evaluating $\mathcal{L}(p + \Delta p; x)$ for all x at 1 new point.
- 2. Calculate gradients using these steps and estimate distance to the minima
- 3. Adjust **p** and loop back to 1 until a 'true' minima has been reached

(no guarantee this is global)

- 4. Make sure Jacobian&Hessian are well defined
- For each parameter report final values and errors(uncertainty) at the minima.

All very scientific, all very 'simple'...

Training according to a Scientist

- Evaluating a complex PDF for the whole dataset is expensive.
- PDF is often effectively a custom written, complex piece of software considering many physical properties/relationships/theories. (For 99.999...% of the time also normalised to 1.0!)
- Automated tools like Minuit cope will with this by adjusting from our starting parameters and step-sizes to find a minima.
- Traditionally every time we evaluate our PDF in science, we typically must do this for the whole dataset.
- This is because our parameters have some physical interpretation.

Training according to a Scientist

PDFs are complex and fun:

 In PPE particles are distributed across all possible phase-space allowed by nature.

```
f_k \left( \vec{\Omega} = \{ \theta_{tr}, \psi_{tr}, \phi_{tr} \} \right)
                                                                                            g_k \left( \vec{\Omega} = \{ \theta_{\mu}, \theta_K, \phi_h \} \right)
  \frac{2\cos^2\psi_{tr}\left(1-\sin^2\theta_{tr}\cos^2\phi_{tr}\right)}{2\cos^2\psi_{tr}\left(1-\sin^2\theta_{tr}\cos^2\phi_{tr}\right)}
                                                                                                    2\cos^2\theta_K\sin^2\theta_\mu
                                                                                      \sin^2\theta_K \left(1 - \sin^2\theta_\mu \cos^2\phi_h\right)
     \sin^2 \psi_{tr} \left(1 - \sin^2 \theta_{tr} \sin^2 \phi_{tr}\right)
                     \sin^2 \psi_{tr} \sin^2 \theta_{tr}
                                                                                      \sin^2 \theta_K (1 - \sin^2 \theta_\mu \sin^2 \phi_h)
           -\sin^2\psi_{tr}\sin 2\theta_{tr}\sin\phi_{tr}
                                                                                             \sin^2 \theta_K \sin^2 \theta_\mu \sin 2\phi_h
      \frac{1}{2}\sqrt{2}\sin 2\psi_{tr}\sin^2\theta_{tr}\sin 2\phi_{tr}
                                                                                        \frac{1}{2}\sqrt{2}\sin 2\theta_K\sin 2\theta_\mu\cos\phi_h
       \frac{1}{2}\sqrt{2}\sin 2\psi_{tr}\sin 2\theta_{tr}\cos\phi_{tr}
                                                                                       -\frac{1}{2}\sqrt{2}\sin 2\theta_K\sin 2\theta_\mu\sin\phi_h
            \frac{2}{3}\left(1-\sin^2\theta_{tr}\cos^2\phi_{tr}\right)
                                                                                                            \frac{2}{3}\sin^2\theta_{\mu}
        \frac{1}{3}\sqrt{6}\sin\psi_{tr}\sin^2\theta_{tr}\sin2\phi_{tr}
                                                                                         \frac{1}{3}\sqrt{6}\sin\theta_K\sin2\theta_\mu\cos\phi_h
         \frac{1}{3}\sqrt{6}\sin\psi_{tr}\sin 2\theta_{tr}\cos\phi_{tr}
                                                                                       -\frac{1}{3}\sqrt{6}\sin\theta_K\sin2\theta_\mu\sin\phi_h
\frac{4}{3}\sqrt{3}\cos\psi_{tr}\left(1-\sin^2\theta_{tr}\cos^2\phi_{tr}\right)
                                                                                                 \frac{4}{2}\sqrt{3}\cos\theta_K\sin^2\theta_\mu
```

• Fitting/Training process isn't just about extracting signal features over background/noise. *PDF* must describe both, i.e. signal+background.

Training according to a Machine Learning expert

- I have millions of free parameters (or more). I don't care about their physical interpretations.
- I want to minimize these parameters to minimize a loss-function(\mathcal{L}) to most closely matches what I see in my training data.

 $-\frac{d\ln(\mathcal{L}(\boldsymbol{p};\boldsymbol{x}))}{d\boldsymbol{p}} = \frac{d\ln(loss(\boldsymbol{p};\boldsymbol{x}))}{d\boldsymbol{n}} = 0$

- 1. Batch up my data
- 2. Evaluate my loss function for a batch
- 3. Calculate the gradients of my parameters in n-dimensional fit-space
- 4. Update my parameters and move onto the next batch. After using all batches start again.
- 5. Repeat 2-4 until I've reached the number of epochs I'm interested in
- 6. Repeat steps 1-5 until I'm "happy"...

Happy here is subjective, it often changes depending on what the user is trying to do.

Yes, it's wishy-washy and full of soft-squishy stuff. IMHO: "it's not very clean or scientific"

Training according to a ML expert

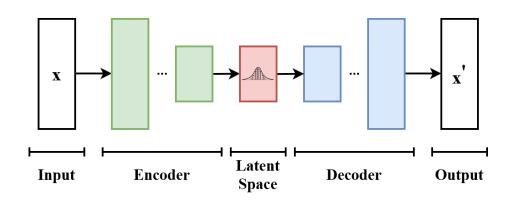
• This process needs to evaluate the gradient of all parameters p in n-dimensional fit-space, this is done via back-propagation.

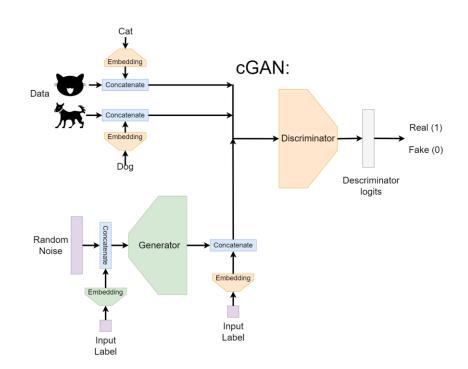
(NB: more on this later!)

- Actual **function being evaluated** is often described in terms of models with data flowing between layers. Often, **much simpler** than complex models used by a scientists.
- Compared to Minuit, less steps are involved, and the minimization can be much quicker.
- Unlike Minuit where we take an approach using all information we have; here we rely on
 a statistically guided tools to take us to the minima much quicker.
- We only need to evaluate small batches of data at a time. That is good because that's how computers tend to like to work ©

Training according to a ML expert

- Sample the input data
- Build a model as a graph
- Pass data forward and backward through model to evaluate
- Use backpropagation to differentiate
- Trained model <u>aims</u> to be *realistic*...





Training, according to different communities...

	Physics Analysis	ML model training
Minima	Well defined minima with a well-defined error	Minima is when training has given the 'best' outcome
Training/Free Parameters	Physical interpretation of each parameter makes fine-tuned, clear understanding of limits and constraints possible	Parameters are effectively random with only limits being statistical in nature
Fit-Space	Fit-space normally << 100 dimensions	Fit-space >> 1,000,000,000 dimensions (!)
PDF/Model	Well defined but complex . Normalised to 1. Whole dataset evaluated for every epoch. Intended to describe the real world. Almost never fully analytically differentiable. Every single event is evaluated against whole complex PDF to determine probabilities.	Loss function is simple . Models control complex flow of data during training. Normalisation often handled through training. Used to extract structure from real-world during training. Always analytically differentiable. Model designed to extract signal and remove/ignore background but often has no knowledge of how to best separate the 2.

So why now (now being 2020+)?

• OK, great ideas, Minuit was published in 1973, why did the latest round of ML/AI companies only launch 50yr later?

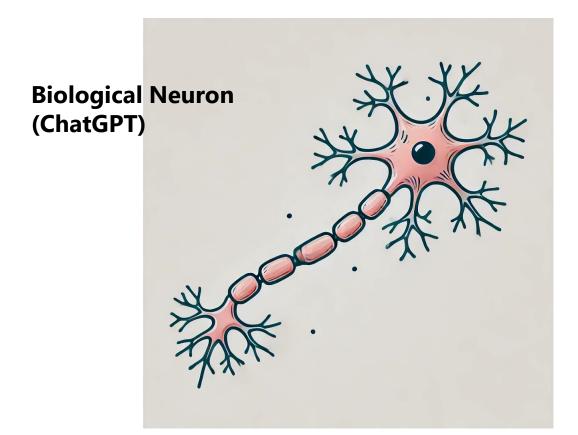
Bandwidth...

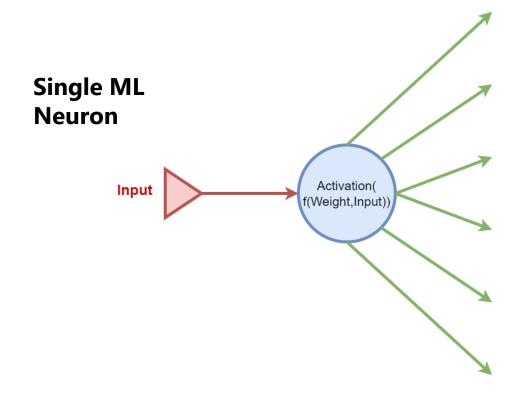
• ML/AI training shuffles data around at **huge** rates that have only been possible with <u>consumer-facing</u> tech for the past 5-10yr.

Neural Networks – The Neuron

Artificial Neural Networks are inspired by the way neurons work in nerve clusters in biological systems.

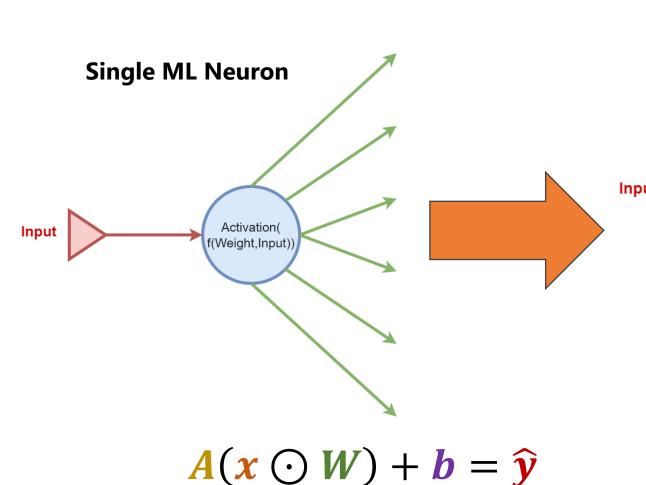


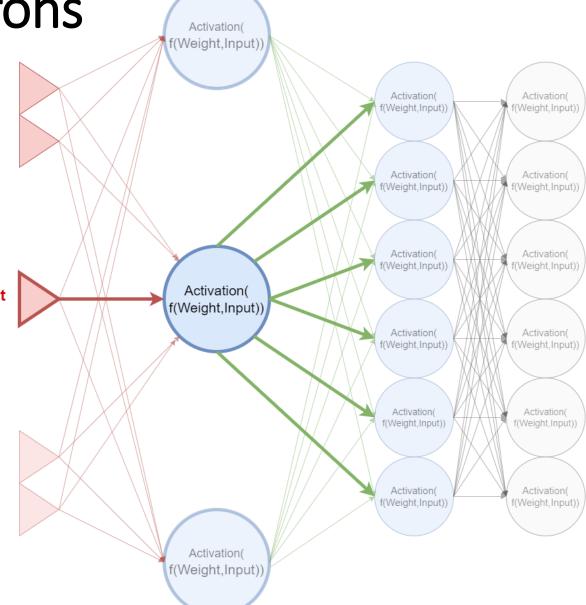




ML Neuron Network







Neural Networks – Neurons

• The behaviour of an **ANN** neuron is inspired by the biological equivalent:

$$A(x \odot W) + b = \hat{y}$$

- The input to the neuron is acted on by the weights in the neuron.
 (Simplest case is that the input is multiplied by the weight(s) and summed).
- After the neuron has acted on all the inputs the output of the neuron comes from applying an Activation function and optionally adding a Bias.
- Activation functions are required to allow the model to describe non-linear data.
- So far basic multi-dimensional (linear-) algebra(!)

ANN – Universal Approximation Theorem

```
"... with a single hidden layer can be shown to be universal approximators." ... "However, the required number of hidden units may be very large."
```

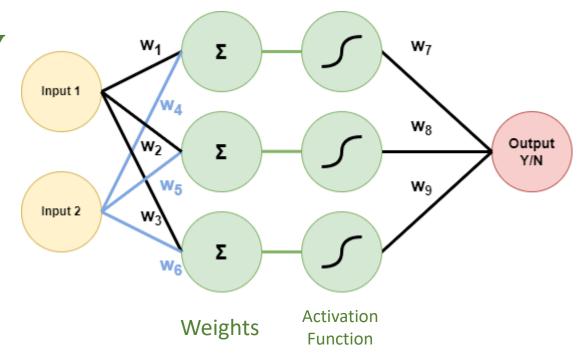
Ian Goodfellow et al.
 (Emphasis mine)

ML model design

• Looking at the simplest model, input passing through 1 Dense layer to give some output. (Most basic, slightly crap, classifier)

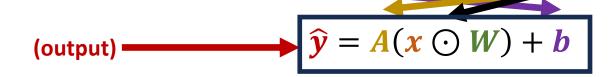
• Input x is operated on by Weights W

 We can also apply an activation function, but for the simple case let's ignore this. (only for now!)



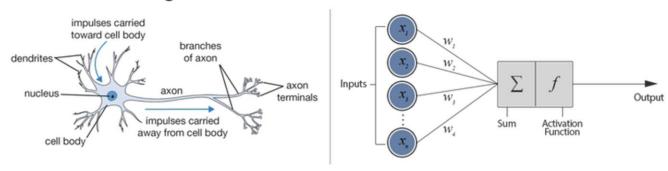
ML model design – Neurons

 Every single neuron in a normal Dense layer is made of a function, an activation and a bias.



• The activation function keeps the output of the operation on the input within a given range and the bias adjusts the output in a normal linear manner.

Biological Neuron versus Artificial Neural Network



ML model design

• Since we have a classifier, we are going to minimize the function which calculates the difference between the model output \hat{y} and the truth y.

$$L(y; \hat{y}) = loss(y; \hat{y}) = \frac{(\hat{y} - y)^2}{2}$$
, $\hat{y} = A(x \odot W) + b$

• For simplicity we're going to choose b = 0 and that A is a simple pass-through function.

*

- The free parameters we are left with for this example are: W
- Now we want to calculate: $\frac{\partial L}{\partial W} = 0$
- Using the chain rule: $\frac{\partial L}{\partial W} = \frac{\partial L}{\partial \widehat{y}} \times \frac{\partial \widehat{y}}{\partial W}$ $\frac{\partial L}{\partial \widehat{y}} = \frac{-2(y-\widehat{y})}{2} = (\widehat{y} y) \qquad , \qquad \frac{\partial \widehat{y}}{\partial W} = x$
- Therefore, we want to get:

$$\frac{\partial L}{\partial W} = x(\hat{y} - y) = 0$$
= layer input *(output gradient)

- For a given set of weights \mathbf{W} , we now know the gradient, based on a set of observables to be: $\frac{\partial L}{\partial \mathbf{W}} = \mathbf{x}(\hat{\mathbf{y}} \mathbf{y})$
- If we want to change W such that we end up at zero gradient, we can step down the gradient (in n-dimensions!) by some small step-size using the "Learning Rate" LR.
- Hence, we can adjust our parameters to \boldsymbol{W} be:

$$W' \Rightarrow W - LR \times x(\hat{y} - y)$$

OK, all sounds easy, why not just take a bigger steps and call it finished?

- The magnitude of the gradient of the weights can vary over n-dimensions.
- Taking a step in one dimension may be correlated with the gradient in another dimension.
- The gradient function is also expected to be highly non-linear.
- We are almost always starting from a random position in fit-space and don't know how far from the best minima we are.

Scientists shouldn't be surprised by this; this isn't yet anything "new".

- OK, let's go back to our 'simple' example and make it a bit more realistic.
- Assuming we add a bias to our dense layer:
- To first order we will assume the Weights(W) and biases(b) can be handled separately.
- Therefore, we can minimize the loss function separately for each:

$$\frac{\partial L}{\partial \hat{\mathbf{y}}} = \frac{-2(y - \hat{\mathbf{y}})}{2} = (\hat{\mathbf{y}} - y) \quad , \frac{\partial \hat{\mathbf{y}}}{\partial h} = 1 \quad \Rightarrow \quad \frac{\partial L}{\partial h} = (\hat{\mathbf{y}} - y)$$

 OK, let's go back to our 'simple' example and make it a bit more realistic.

• Assuming we use an Activation function: $A = \tanh(x)$

(NB: not a random function but chosen because of its mathematical properties!)

$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial A} \times \frac{\partial A}{\partial W} \Rightarrow \frac{\partial L}{\partial A} = 1 - A(W)^2, \quad \frac{\partial A}{\partial W} = x(\hat{y} - y)$$

• Hence:
$$\frac{\partial L}{\partial W} = \left(1 - A(W)^2\right) x(\hat{y} - y)$$

= layer input *(output gradient)

- So, for a more complete 1-Dense layer model what do we need:
- Gradient from previous layer: $\partial_{n-1} = (\hat{y} y)$
- Differential of Weights in layer: $(1 A(W)^2)x\partial_{l-1}$, this just depends on the output from this layer L_{n-1} .

So:
$$\frac{\partial L}{\partial W} = (1 - L_{n-1}^2) x \partial_{n-1}$$

NB: The (1-Output^2) only applies when using Tanh(!)

• Differential of Biases in a layer: $(\hat{y} - y)$ = Gradient from previous layer...

OK, so what if I apply more than 1 layer?

Chain rule saves us again:

$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial Layer_n} \times \frac{\partial Layer_n}{\partial W} , \quad \frac{\partial Layer_n}{\partial W} = \frac{\partial Layer_n}{\partial Layer_{n-1}} \times \frac{\partial Layer_{n-1}}{\partial W}$$

$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial Layer_n} \times \frac{\partial Layer_n}{\partial Layer_{n-1}} \times \frac{\partial Layer_{n-1}}{\partial W}$$

 When building a modern ML/AI model the requirement to be able to back-propagate means we're limited to functions we can analytically differentiate.

(Or analytically approximate the differentiation of if it's "good enough")

• This is a key difference to a lot of "scientific" numerical fitting where the gradient is almost never known analytically but is calculated purely numerically.

- Input data is passed as a **batch** to a model to be evaluated/train/make-predictions.
- For a Dense layer, a **batch** of **n** input elements is mapped to **m** neurons giving us a matrix of $(n \times m)$ dimensions. With a vector of length m biases.
- Connecting a 2^{nd} Dense layer with an output dimension y_n means we need a 2^{nd} matrix of dimension $(m \times y_n)$.
- We know to evaluate the differential at each layer we need to record the output from each layer and the input from each previous layer.

ML mode des class MyModel(): def __init__(

The model might look like this.

Layer1

Layer2

Need to start with the gradient at the end.

$$(1 - \boldsymbol{L}_n^2) \boldsymbol{x} \boldsymbol{\partial}_n$$
 "Undo" the Tanh Activator

$$W \Rightarrow W - LR \times \frac{\partial L}{\partial W}$$

```
def __init__(self, x, y):
                                             Let's use Tanh
   self.weights[0] = myMatrix(x, y)
   self.weights[1] = myMatrix(y, 1)
   self.biases[0] = myVector(y)
   self.biases[1] = 1
def forward(self, x):
   self.y[-1] = x
   self.y[0] = myActivation(x * self.weights[0]) + self.biases[0]
  self.y[1] = myActivation(self.y[0] * self.weights[1]) + self.biases[1]
   return self.y[1]
def backward(self, diff_y, learning_rate):
   previous gradient = diff y
    for i in reversed(range(2)):
       current gradient = (1 - self.y[i]^2) * previous gradient
       self.weights_diff[i] -= learning_rate * self.y[i-1].T @ current_gradient
       self.biases diff[i] -= learning rate * sum(current gradient)
        previous gradient = current gradient @ self.weights[i].T
```

Start with initial gradient and loop backwards through graph

'Undo' the gradient modification from our Activation function

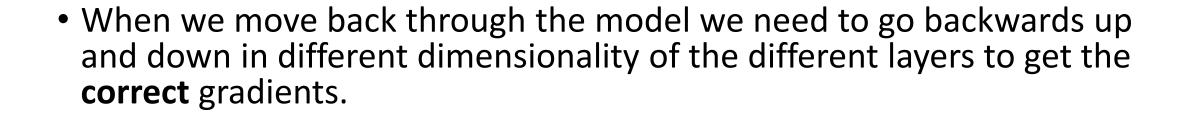
```
def backward(self, diff_y, learning_rate):
                                                  Now have gradient for weights[i] but
                                                 need to apply that to current model to
    previous gradient = diff y
                                                  get 'full' gradient at this part of graph
    for i in reversed(range(2)):
        current_gradient = (1 - self.y[i]^2) * previous_gradient
        self.weights_diff[i] -= learning_rate * self.y[i-1].T @ current_gradient
        self.biases diff[i] -= learning rate * sum(current gradient)
        previous_gradient = current_gradient @ self.weights[i].T
```

Input to step before this needs us to 'Undo' the gradient effect from our current set of weights

Saying 'undo' here is to help conceptualize what is going on.

What is really going on is the errors in the graph are being decomposed to individual components within the graph using the chain rule so the graph can be minimized to give the smallest total error.

 Following through the code there is an important subtlety which is lost when looking through the simplified algebra. Dimensionality.



• This is achieved by using the Transposed version of the "matrix" previously used when walking forward through the model.

(Hence why we use Weights.T rather than applying the weights again)

- In our example we have:
- 1. Input of dimension 1
- 2. connected to a dense layer of dimension (1, x)
- 3. connected to a dense layer of dimension (x, y)
- 4. connected to a 2^{nd} dense layer of dimension (y, 1)
- 5. giving an output of dimension 1.
- Moving backwards through our network we need to go from 1 to (y, 1) to (x, y) back to 1 we achieve this by transposing the original matrices to match the dimensions.

- There's a lot of matrices multiplied with potentially many calculations.
- When performing a matrix multiplication in Python with numpy:
 - np.matmul(x, W) is the same as using the matrix operator: x @ W
- There are some functional differences between np.dot and np.matmul which shouldn't impact us too much, but beware(!)
- Last week I demonstrated that matmul and @ can be much faster than pure Python.

ML model design – Writing Reading Code

 Here are some conventions when looking at ML related code (and to some extent algebra):

- \hat{y} this is often the **predicted** or **logits** value from a model
- x is often the batch of data being processed, y is labels/truth
- a is often the output of an activated layer
- z is often the output of non-activated layer

ML model design – Training

• OK, to train a model this is 'easy':

- 1. Move forwards through the model (save outputs as you go)
- 2. Move backwards through the model (to calculate gradients)
- 3. Step in fit-space —ve to the gradient
- 4. Repeat steps 1-3 until we are "happy"

ML model design – Training

- Minuit and other scientific based statistical minimizers often return the absolute likelihood for a whole fit function.
- This is due to the minimizer attempting to move along the surface of the likelihood function to reach a minima.

• Common tools such as **TensorFlow** or **PyTorch** tend to report the 'average' of the loss function for the last batch.

This is normally the mean of the logits but can technically differ.

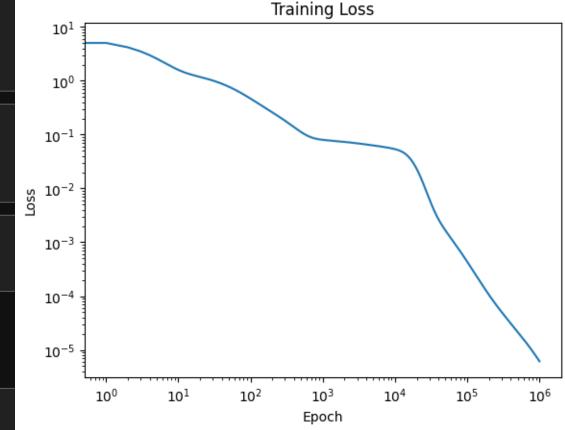
• Training a DNN to a sinusoid dataset allows it to learn the features of a dataset and give back the correct value when correctly trained.

In our simple case we won't bother to "batch-up" our dataset, we can
just evaluate it element by element on a CPU and O(1k) points isn't
too intensive.

• The "secret sauce" comes from our use of Activation Functions(!)

Construct our input dataset

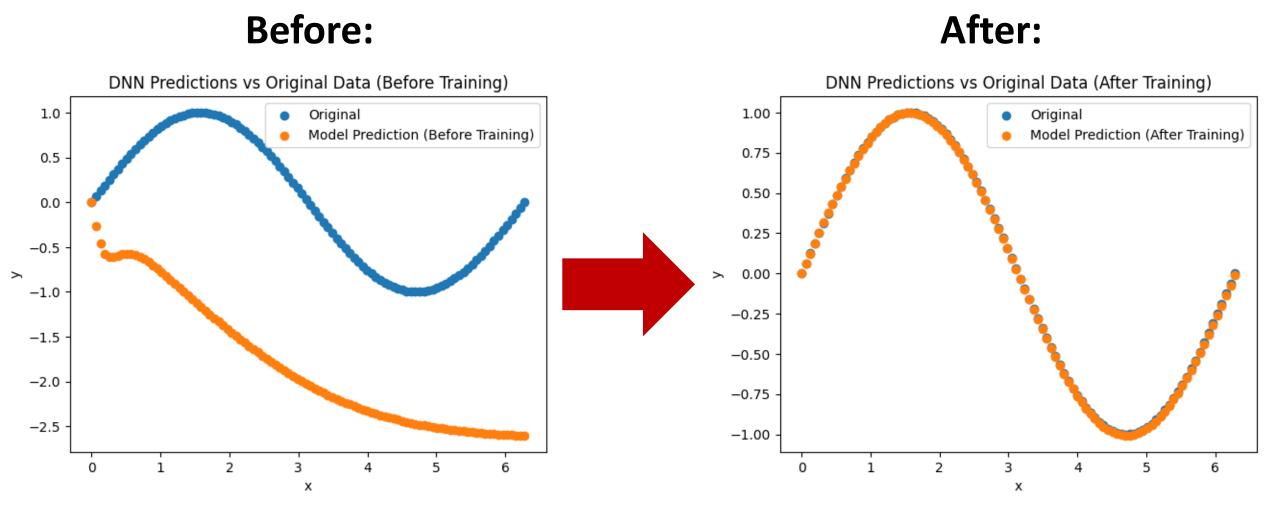
```
[4]:
      input_size = 1 # since we have only one feature (x)
      hidden size = 10 # number of neurons in the hidden Layers
      output_size = 1 # output is a single value (y)
[5]:
      # Generate sinusoidal data
      timesteps = 100 # number of timesteps in the data
      x = np.linspace(0, 2 * np.pi, timesteps)
      y = np.sin(x)
[6]:
      # Reshape x and y for training
      x_train = x.reshape(-1, 1)
      y_train = y.reshape(-1, 1)
      Build Our Model
      # Initialize and train the model
      model = SimpleDNN(hidden size)
[10]
      model.train(x train, y train, epochs=100000, learning rate=0.001)
```



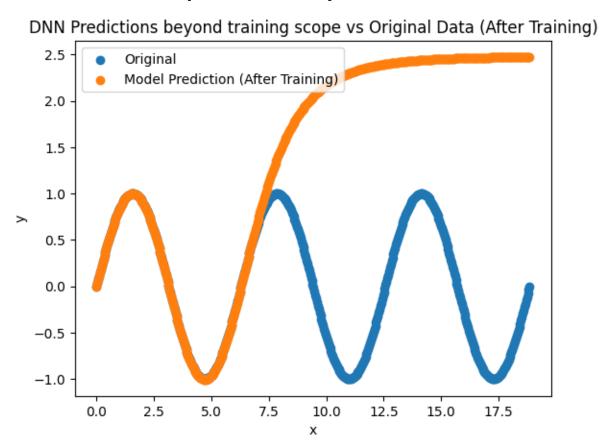
• Our (average) loss function is going down (huzzah!)

• This probably means it's "learning" something.

• If it's correctly trained our model can predict the value of y for a given input of x, i.e. it can mimic a sinusoid function



• OK, fantastic we've trained our model, now what happens if we predict beyond what it's previously seen:



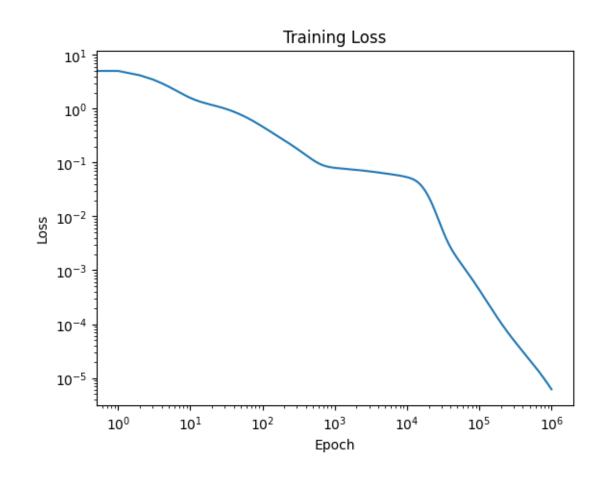
ML DNN model design

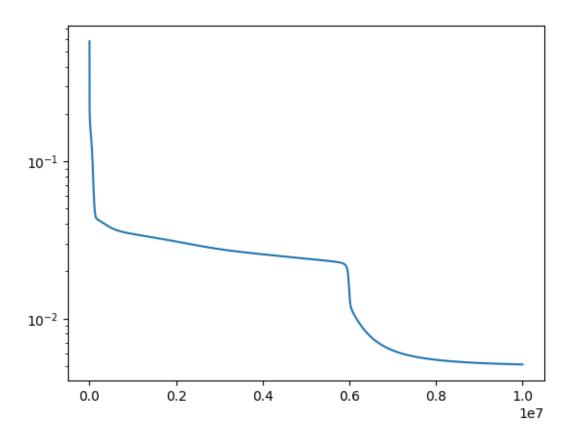
So why does it fail?

- DNN have no concept of time/positional-ordering, they memorize, and they spit the input back out.
- This is fine if we want to up/down-sample data between different input/output networks/models.
- Is powerful if we just want a quick/easy model to do something such as anomaly detection or classification.
- This is basically useless by itself for analysing a piece of music or extracting emotion from a sentence.

ML model design

When do we stop training?





ANN So Far – A Recap

- We've covered that an ANN composed of neurons and it is trained to describe a given dataset and perform a task.
- Neurons contain Weights, Biases and Activation functions
- To make this useful we want to know:
 - What is inside a model? (How are neurons connected?)
 - How do we evaluate this? (How is data read into the model?)
 - How do train/fit/tune this?

 (How is a model trained on data?)



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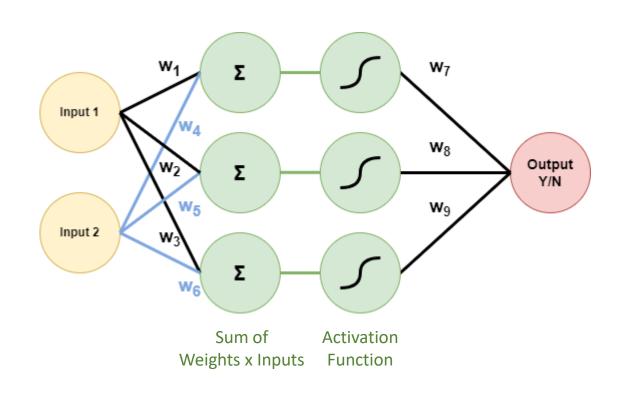
Shallow Neural Network – A Special Case

A Shallow Neural Network is an ANN which has a <u>single</u> hidden layer. This is typically taken to be a "special case" which isn't always practical to use.

Example of a SNN with 1 hidden layer.

In this case we have **9** free weights. (**9** model parameters)

This means to train this model on data we would need to find the combination of **9 weights** which best match the model to the training data.



Shallow Neural Network – A Special Case

To <u>evaluate</u> a **SNN/DNN** model, we need our data to be represented as <u>numerical input</u>.

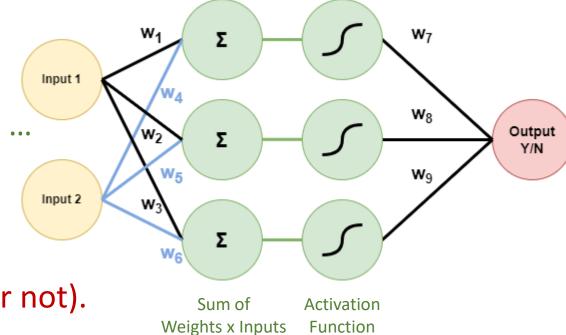
The numerical input is connected to (read by) the first layer in the model.

The output from this layer is passed to the next.

And the next. And the next. And the next ...

Finally, the *logits* are passed to the output layer which gives some output.

Output is then evaluated to be correct (or not).



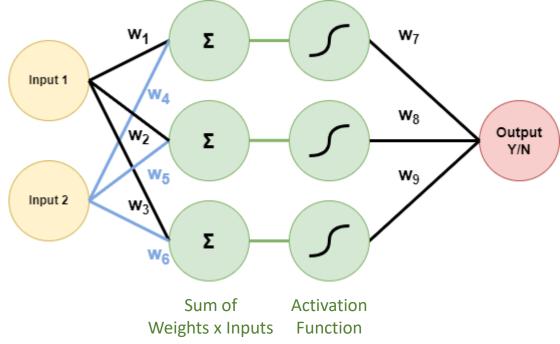
Shallow Neural Network – A Special Case

To **train** this model we need to calculate the full matrix of 9x9 partial derivatives to know what step size to take.

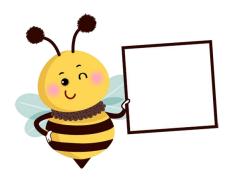
The size of the step we then take is controlled by the "learning rate".

Calculating the various parameters in this **Jacobian** is expensive, but there are mathematical tricks to reduce the steps required.

These tricks mean this is referred to as an O(nlog(n)) vs an $O(n^2)$ problem.



ANN – Activation Functions



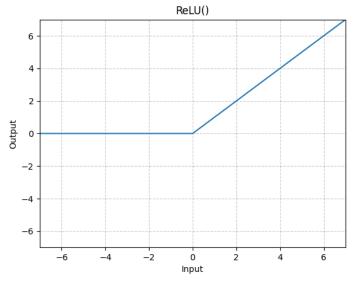
- Activation Functions in ANN give the network the ability to handle non-linear relationships.
- The choice of an activator can have an impact on how quickly a function can be trained on a dataset.
- The choice of activator can also impact model stability during training.
- Activators are also used to normalize or cap the distribution of model weights passed forward from each hidden layer.

ANN – Activators (Some Examples) ReLU

ReLU or **Rectified Linear Unit** activator is probably the most common function used in building and training ANN.

It is fast, simple, has many advantages but also has issues.

ReLU(x) = max(0, x)



ReLU from
PyTorch
documentation

This activation function effectively turns on/off nodes within an ANN during training.

One of the biggest problems with **ReLU** is that the function is discontinuous. This can cause instabilities in training which can be difficult to understand/control/rectify.

ANN – Activators (Some Examples) GELU

GELU or Gaussian Error Linear Unit is a a choice of activation function which is gaining significant traction.

Can be viewed as a 'smoother ReLU' function. This has the advantages of the **ReLU**, it is always continuous, but at the cost of being computationally more expensive.

GELU(approximate='none')

$$GELU(x) = x \times P(X \le x)$$

$$= x \times \Phi(x)$$

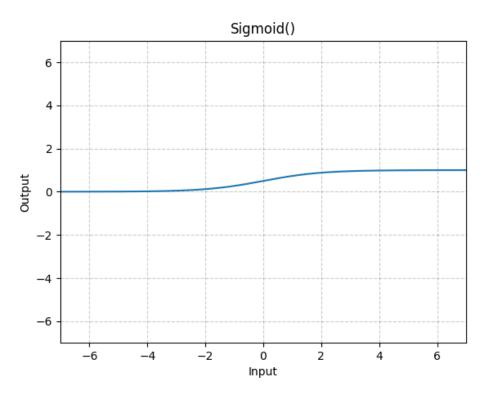
$$\approx \frac{x}{2} \left(1 + \tanh\left(\sqrt{\frac{2}{\pi}}(x + 0.044715x^3)\right) \right)^{\frac{1}{2}}$$
GELU from PyTorch documents

Where $\Phi(x)$ is the CDF for the Gaussian Distribution

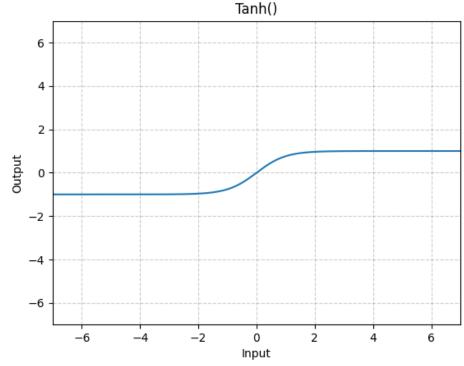
GELU from documentation

ANN – Activators (Some Examples) sigmoid/tanh

Other commonly used activation functions.



$$S(x) = \sigma(x) = \frac{1}{1 + e^{-x}}$$



Plots from PyTorch docs

$$tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

• The final "step" in a **DNN** network is the **Output** layer. (Also sometimes known as the **projection** layer)

 This layer maps the raw-hidden results from the network (logits) to the model output.

- If your model is a classifier the output may be a category-id.
- If your model is a generator the output may be an image.
- If your model is an **LLM** the output is **encoded text**.

- With DNN classifiers we want to be able to predict the class of some input data.
- Typically, this means that we need to identify the 'category' of our input using our model.
- We now need to consider:
 - a) What form should the output layer take?
 - b) What should the loss function attempt to calculate?

- Output for a classifier needs to make a prediction of a category.
- To be consistent all predictions *need to sum to 100%*
- It's possible to build an activation function which give a **one-hot result** when making predictions.

i.e. truth =
$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$
, prediction = $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$

Typically output layer looks similar to a hidden dense node layer.

The layer first includes a dense layer of *n* nodes. Here *n* is defined as the number of categories in the labels the model is trained on.

After this, the output from each node is normalized using an activator such as a Softmax function.

Softmax
$$(z) = \sigma(\tilde{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}}$$
 for $i = 1, ..., K$

DNN Classifier

• So, a simple DNN Classifier takes some inputs (of different types)

• It passes these inputs through some Neural Network

 The output from this network makes a guess at the classification of the input(s)

 By comparing to truth and using back-propagation we train our model to perform better.





• When training our model, we want to make sure that we are avoiding over-training on features only present in the training data.

This Photo by Unknown Author is licensed under CC BY-SA-NC

- We also want to not waste computing resources over-training a model which has effectively converged.
- The best way of doing this is to split our data into 3 datasets as with Decision Trees:

Training, Validation & Testing

More on this next week

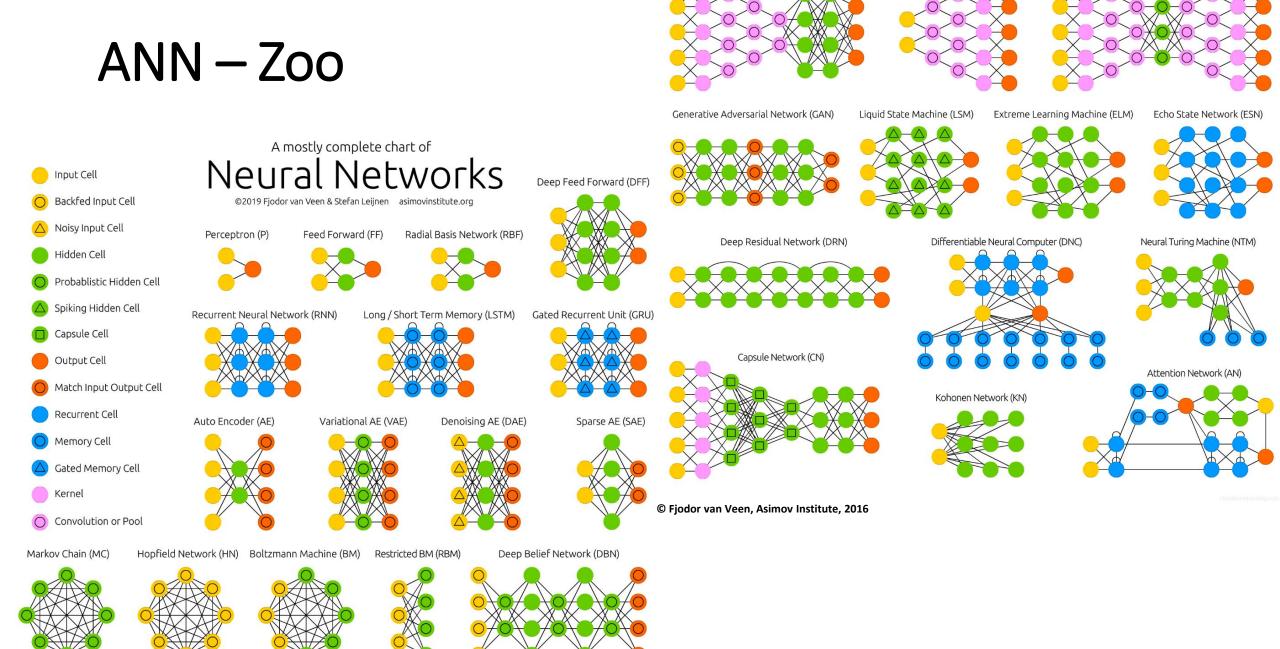
Training – Model Design

In the workshop following this lecture we will be building models which are designed to work with hundreds of input parameters.

In turn the **DNN** designed to work with this uses hundreds of thousands of free weights.

If it is possible to reduce the number of free weights by being clever in our nodes, then the model is mathematically simpler to work with.

This typically means that we need to do something more complex in our node than just 'summing' over the products...



Deep Convolutional Network (DCN)

Deconvolutional Network (DN)

Deep Convolutional Inverse Graphics Network (DCIGN)

Neural Networks – Deep NN

- In most cases we will be using multiple "hidden layers" within a NN.
- A network with more <u>layers</u> is defined as being deeper (depth)
- A network with more <u>nodes</u> per-layer is described as wider (width)
- ANN come in many shapes/sizes
- TensorFlow playground is an excellent online resource for playing with different CNN models and how they train to a given dataset: https://playground.tensorflow.org/

TensorFlow-Playground — (An Aside)

• Can be useful to 'get a feel' for how changing individual parts of the model can impact training.

I claim nodes on this page are best thought of as CNN neurons.
 (more on these in my next lecture)

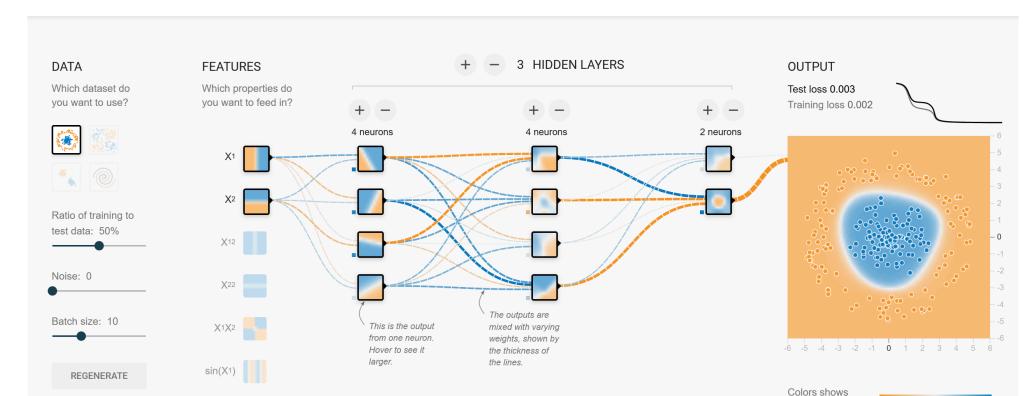
 Weight scales are a good comparator to 'how much of feature X' is in the dataset?

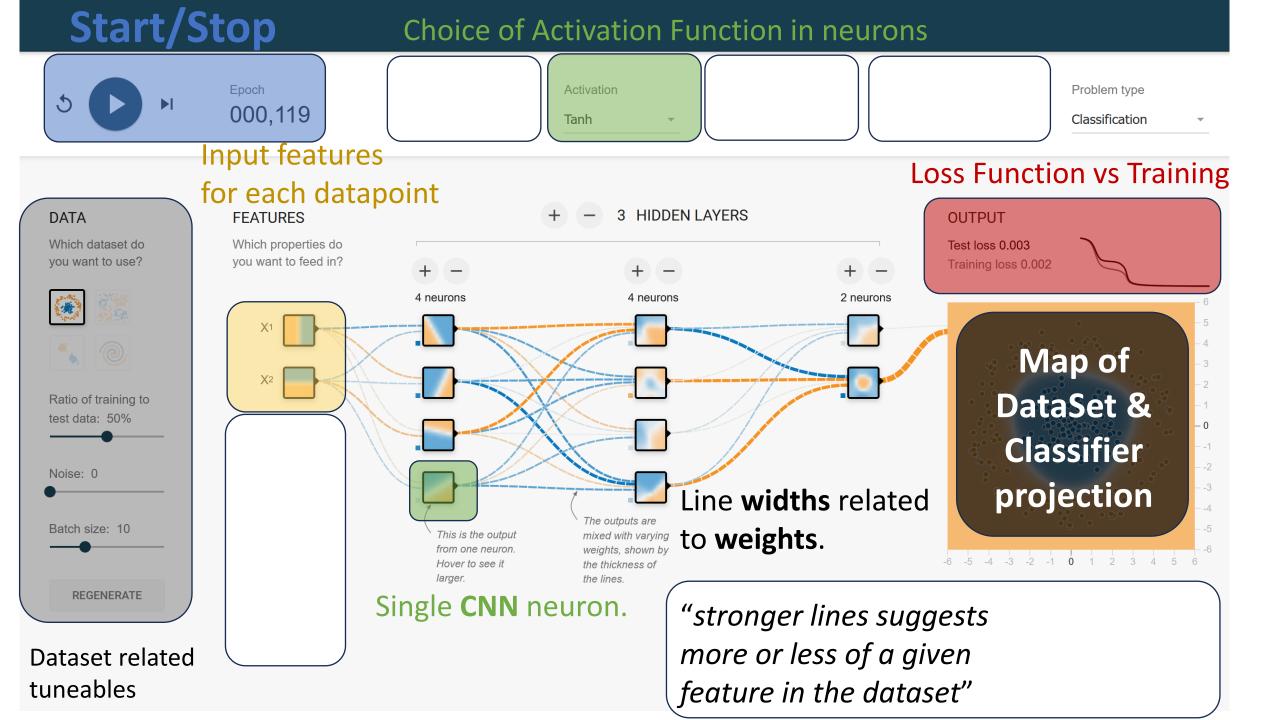
TensorFlow-Playground — (An aside)

Tinker With a **Neural Network** Right Here in Your Browser.

Don't Worry, You Can't Break It. We Promise.







Next Lecture

- My next lecture will introduce a few different topics:
- 1. Evaluating how well has a fit converged?
- 2. When should we decide to stop training?
- 3. How can I optimize/improve training?
- 4. Using more advanced nodes in a PyTorch model(graph)
- 5. Constructing more advanced models in PyTorch
- 6. Constructing an AutoEncoder for anomaly detection

Today's Workshop

PyTorch docs if you need them:

https://pytorch.org/docs/stable/nn.html

- Today's workshop starts a bit slower;
- 1. Start by build a Deep Neural Network or Multi-Layer Perceptron using just NumPY.

Getting hands dirty with Python code.

2. Second, building the same model again using PyTorch

Getting familiar with PyTorch's API

3. Building a Classifier using PyTorch

Using PyTorch to build a classifier for real data

4. Extending our DNN beyond it's training window