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### Geometry 3 Homework

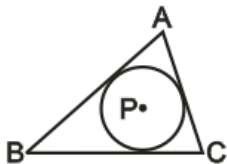
1. In  $\triangle ABC$ ,  $\overline{AD}$  is the perpendicular bisector of  $\overline{BC}$  and D lies on  $\overline{BC}$ . Which statement(s) must be true?

- (I)  $\triangle ABD \cong \triangle ACD$       (II)  $\triangle ABC$  is equilateral.      (III)  $\overline{AD}$  is the bisector of  $\angle BAC$ .  
 a) III only      b) I only      c) I and III only      d) II only      e) I, II, and III

2. X is a point inside triangle ABC. If X is equidistant from  $\overline{BC}$  and  $\overline{AC}$ , then X must lie on the  
 a) perpendicular bisector of  $\overline{AB}$       b) bisector of  $\angle C$       c) median of  $\overline{BC}$   
 d) altitude to side  $\overline{AB}$

3. The angle bisectors of  $\triangle ABC$  meet at point I,  $\overline{AB} : \overline{BC} : \overline{CA} = 4 : 5 : 8$ , and the area of  $\triangle ABC$  is 68. What is the area of  $\triangle BCI$ ?

4. In the figure, P is the incenter of  $\triangle ABC$ , the radius of the inscribed circle is 3 cm, and the perimeter of  $\triangle ABC$  is 42 cm. What is the area of  $\triangle ABC$ ?



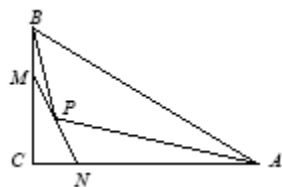
5.  $ABCD$  has perpendicular diagonals. If  $AB = 1$  cm,  $BC = 4$  cm, and  $CD = 8$  cm, determine the number of centimeters in  $AD$ .

6. The radius and height of a cylinder are integers. If the total surface area is numerically equal to the volume, determine the largest possible number of units in the height of the cylinder.

7. Each side of a square has the same length as the diagonal of a 5" x 12" rectangle. A circle is inscribed in the square. Exactly how many inches are in the circumference of the circle?

8. In a 5-12-13 triangle, a segment is drawn parallel to the hypotenuse and  $\frac{1}{3}$  the way from the hypotenuse to the opposite vertex. Another segment is drawn parallel to the first and  $\frac{1}{3}$  the way from the previous segment to the opposite vertex. Determine the number of square units in the trapezoid whose bases are the two drawn segments.

9. In  $\triangle ABC$ ,  $AC = 8$ ,  $BC = 6$ , and  $AB = 10$ . If  $\angle MNC = \angle ABC$  and  $P$  is the midpoint of  $MN$ , determine the length of  $MN$  so that the area of  $\triangle BPA$  is half the area of  $\triangle ABC$ .



10. In  $\triangle ABC$ ,  $BF$  bisects  $\angle ABC$  and  $\frac{BE}{EF} = \frac{BC}{BA}$ . If  $AB = 2$  and  $BC = 3$ , express the ratio  $\frac{AE}{ED}$  in the form  $\frac{a}{b}$  where  $a$  and  $b$  are relatively prime.

