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**Algebra 2 Homework****1. Solve each equation by factoring.**

1. $3x^2 + 11x - 20 = 0$	2. $x^2 + 14x + 24 = 0$	3. $8x^2 - 55x = -42$
4. $x^2 + 16x + 55 = 0$	5. $x^2 + 8x + 7 = 0$	6. $x^2 + 4x = 60$

**2. Solve each equation by factoring**

1. $-2x^2 + 14x - 6 = 14$	4. $x^2 + 3x - 4 = 0$	3. $x^2 - 2x - 8 = 0$
4. $4x^2 = 3x^2 + 4x + 5$	5. $x^2 + 8x = -12$	6. $x^2 - x - 10 = 2$
7. $6x^2 - 24x - 48 = 18x$	8. $x^2 + 8x + 7 = 0$	9. $x^2 + 4x - 5 = 0$

### Challenge problems

1. Let the operation  $*$  be defined by  $a * b = a^2 + 3^b$ . What is the value of  $(2 * 0) * (0 * 1)$ ?
2. Let  $N = 999,999,999,999,999,999$ . How many 9's are in the decimal expansion of  $N^2$ ?
3. Which is the largest of the following:  $1^{48}$ ,  $2^{42}$ ,  $3^{36}$ ,  $4^{30}$ ,  $5^{24}$ ,  $6^{18}$ ,  $7^{12}$ ,  $8^6$ ,  $9^0$ ? (Write the exponential expression, not the large integer which it equals.)
4. What is the largest possible value for the sum of two fractions such that each of the four 1-digit prime numbers occurs as one of the numerators or denominators?
5. How many integers  $x$  in  $\{1, 2, 3, \dots, 99, 100\}$  satisfy that  $x^2 + x^3$  is the square of an integer?

6. How many pairs  $(x, y)$  of positive integers satisfy  $2x + 7y = 1000$ ?

7. What is the sum of the three smallest prime numbers each of which is two more than a positive perfect cube?

8. How many 9's are in the decimal expansion of  $99999989999^2$ ? (This is the square of an 11-digit number.)

9. Simplify  $\sqrt{3+2\sqrt{2}} - \sqrt{3-2\sqrt{2}}$ .

10. What is the smallest positive integer  $k$  for which there exist integers  $a > 1$  and  $b > 1$  for which the correct simplification of  $\sqrt{k}$  is  $a\sqrt{b}$ , and the correct simplification of  $\sqrt[3]{k}$  is  $b\sqrt[3]{a}$ ?