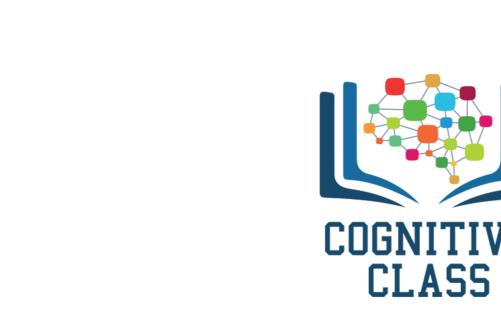


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In this lab, you will learn the basics of differentiation. Derivatives

Differentiation in PyTorch

```
Partial Derivatives
```

Estimated Time Needed: 25 min

Preparation

import torch

In [3]: # Create a tensor x

The tensor x: tensor(2., requires_grad=True)

y = x ** 2

In []:

is_leaf: True

requires grad: True Let us try to calculate the derivative for a more complicated function. In [8]: # Calculate the $y = x^2 + 2x + 1$, then find the derivative

 $\frac{\mathrm{dy}(x)}{\mathrm{dx}} = 2x + 2$

Practice

The derivative at x=1: tensor(7.) Double-click **here** for the solution.

In the forward pass we receive a Tensor containing the input and return a Tensor containing the output. ctx is a context object that can be used to stash information for backward computation. You can cache arbitrary result=i**2

@staticmethod

Out[11]: tensor(4.)

This is equivalent to the following:

the expression is given by:

 $\frac{\partial f(u,v)}{\partial u} = v + 2u$

 $\frac{\partial f(u=1, v=2)}{\partial u} = 2 + 2(1) = 4$

The partial derivative with respect to u: tensor(1.) The equation is given by:

gradient: Y = x ** 2

y = torch.sum(x ** 2)

We can plot the function and its derivative

In [16]: # Take the derivative with respect to multiple value. Plot out the function and its derivative

function derivative

10.0

7.5

plt.plot(x.detach().numpy(), Y.detach().numpy(), label = 'function')

plt.plot(x.detach().numpy(), x.grad.detach().numpy(), label = 'derivative') plt.xlabel('x')

y.backward()

In [18]: # Take the derivative of Relu with respect to multiple value. Plot out the function and its derivative

Y = torch.relu(x)

plt.xlabel('x')

function

plt.legend() plt.show()

10

In [19]: y.grad_fn

Practice

y = Y.sum()y.backward()

Try to determine partial derivative u of the following function where u=2 and v=1: $f=uv+(uv)^2$ In [8]: # Practice: Calculate the derivative of f = u * v + (u * v) ** 2 at u = 2, v = 1u = torch.tensor(2., requires_grad=True) v = torch.tensor(1., requires_grad=True) f = u*v + (u*v)**2

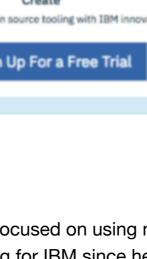
Out[19]: <SumBackward0 at 0x7f0e12dc52b0>

The partial derivative with respect to v: tensor(10.) Double-click here for the solution.

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The partial derivative with respect to u: tensor(5.)

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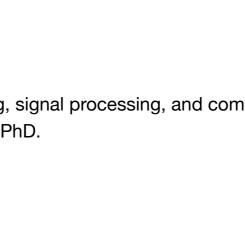


Table of Contents

The following are the libraries we are going to use for this lab. In [2]: # These are the libraries will be useing for this lab.

import matplotlib.pylab as plt

Derivatives

Let us create the tensor x and set the parameter requires_grad to true because you are going to take the derivative of the tensor. x = torch.tensor(2.0, requires_grad = True)

print("The tensor x: ", x)

Then let us create a tensor according to the equation $y = x^2$. In [4]: # Create a tensor y according to $y = x^2$ print("The result of $y = x^2$: ", y)

The result of $y = x^2$: tensor(4., grad_fn=<PowBackward0>)

Then let us take the derivative with respect x at x = 2

In [5]: # Take the derivative. Try to print out the derivative at the value x = 2

y.backward() print("The dervative at x = 2: ", x.grad) The dervative at x = 2: tensor(4.)

The preceding lines perform the following operation: $\frac{\mathrm{dy}(x)}{\mathrm{dx}} = 2x$ $\frac{dy(x=2)}{dx} = 2(2) = 4$

In [6]: print('data:',x.data) print('grad_fn:',x.grad_fn) print('grad:',x.grad) print("is_leaf:",x.is_leaf) print("requires grad:",x.requires grad) data: tensor(2.) grad_fn: None grad: tensor(4.)

requires_grad: True In [7]: print('data:',y.data) print('grad fn:',y.grad fn) print('grad:',y.grad) print("is_leaf:",y.is_leaf) print("requires_grad:",y.requires_grad) data: tensor(4.) grad_fn: <PowBackward0 object at 0x7f0e12dc31d0> grad: None is_leaf: False

x = torch.tensor(2.0, requires grad = **True**)

print("The result of $y = x^2 + 2x + 1$: ", y) y.backward() print("The dervative at x = 2: ", x.grad) The result of $y = x^2 + 2x + 1$: tensor(9., grad_fn=<AddBackward0>) The dervative at x = 2: tensor(6.) The function is in the following form: $y = x^2 + 2x + 1$ The derivative is given by:

 $\frac{dy(x=2)}{dx} = 2(2) + 2 = 6$

y = x ** 2 + 2 * x + 1

Determine the derivative of $y = 2x^3 + x$ at x = 1In [9]: # Practice: Calculate the derivative of $y = 2x^3 + x$ at x = 1x = torch.tensor(1.0, requires_grad=True) $y = 2 \times x \times 3 + x$ print('The result of y=2*x^3+x: ', y) y.backward() print('The derivative at x=1: ', x.grad)

Type your code here

The result of y=2*x^3+x: tensor(3., grad_fn=<AddBackward0>)

In the backward pass we receive a Tensor containing the gradient of the loss with respect to the output, and we need to compute the gradient of the loss

We can implement our own custom autograd Functions by subclassing torch.autograd. Function and implementing the forward and backward passes which operate on Tensors In [10]: class SQ(torch.autograd.Function):

def forward(ctx,i):

objects for use in the backward pass using the ctx.save_for_backward method. ctx.save for backward(i) return result **@staticmethod** def backward(ctx, grad_output):

with respect to the input.

<torch.autograd.function.SQBackward object at 0x7f0ea50bd668>

The result of v * u + u^2: tensor(3., grad_fn=<AddBackward0>)

i, = ctx.saved_tensors

grad_output = 2*i

return grad_output We can apply it the function In [11]: x=torch.tensor(2.0,requires_grad=True) sq=SQ.apply y=sq(x)print(y.grad_fn) y.backward() x.grad

Partial Derivatives We can also calculate **Partial Derivatives**. Consider the function: $f(u, v) = vu + u^2$ Let us create u tensor, v tensor and f tensor In [12]: # Calculate $f(u, v) = v * u + u^2$ at u = 1, v = 2

f = u * v + u ** 2

 $f(u = 1, v = 2) = (2)(1) + 1^2 = 3$ Now let us take the derivative with respect to u:

In [13]: # Calculate the derivative with respect to u

u = torch.tensor(1.0, requires_grad=True) v = torch.tensor(2.0, requires grad=True)

print("The result of v * u + u^2: ", f)

f.backward() print("The partial derivative with respect to u: ", u.grad) The partial derivative with respect to u: tensor(4.)

Now, take the derivative with respect to v: In [14]: # Calculate the derivative with respect to v print("The partial derivative with respect to u: ", v.grad)

Calculate the derivative with respect to a function with multiple values as follows. You use the sum trick to produce a scalar valued function and then take the In [15]: # Calculate the derivative with multiple values x = torch.linspace(-10, 10, 10, requires_grad = True)

plt.legend() plt.show() 100 80

60

40

20

0

-10.0 -7.5 -5.0

-20

The orange line is the slope of the blue line at the intersection point, which is the derivative of the blue line. The method detach() excludes further tracking of operations in the graph, and therefore the subgraph will not record operations. This allows us to then convert the tensor to a numpy array. To understand the sum operation Click Here The **relu** activation function is an essential function in neural networks. We can take the derivative as follows: In []:

-2.5

2.5

x = torch.linspace(-10, 10, 1000, requires_grad = True)

plt.plot(x.detach().numpy(), Y.detach().numpy(), label = 'function')

plt.plot(x.detach().numpy(), x.grad.detach().numpy(), label = 'derivative')

derivative 8 6 2 -10.0 -7.5 -5.0 -2.5 2.5 5.0 7.5 10.0 0.0

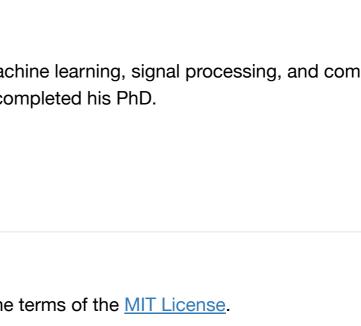
f.backward() print("The partial derivative with respect to u: ", u.grad) print("The partial derivative with respect to v: ", v.grad)

Type the code here

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About the Authors:

Sign Up For a Free Trial Joseph Santarcangelo has a PhD in Electrical Engineering, his research focused on using machine learning, signal processing, and computer vision to determine how videos impact human cognition. Joseph has been working for IBM since he completed his PhD. Other contributors: Michelle Carey, Mavis Zhou



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