### Introduction to Causal Inference

Causal Inference using Machine Learning Master in Economics, UNT

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A causal question asks about the effect of a cause A on an outcome B.

A could be:



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  - $\bullet \ \, \mathsf{Policy} \ (\mathsf{e.g.}, \ \mathsf{a} \ \mathsf{new} \ \mathsf{transfer} \ \mathsf{policy} \ \mathsf{impacting} \ \mathsf{household} \ \mathsf{income} \ (\mathsf{AUH}))$



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  - Treatment (e.g., a drug trial reducing heart attack risk)



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  - Efficiency (e.g., speed of production or resource utilization)

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 Example: Eating more food can cause weight gain, but if food intake and exercise both increase proportionally, we may observe no correlation between food and weight in the data, even though causation exists.

### Causal Inference Tree

#### Two design traditions

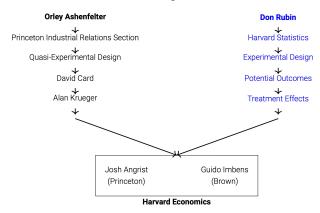


Figure: Source: Scott Cunningham Substack

## **Experimental Design Tradition**

Experimental design relies on randomized controlled trials (RCTs) to establish causality through direct manipulation of the treatment.

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### Esther Duflo (Nobel Prize 2019):

- Pioneered the use of randomized controlled trials in development economics to study policy interventions.
- Contribution: Applied RCTs to measure the effectiveness of educational and poverty interventions in developing countries.

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- Abadie, A., Diamond, A., and Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of california's tobacco control program. *American Economic Review*, 105(3):391–425.
- Snow, J. (1854). *On the Mode of Communication of Cholera*. London: John Churchill.
- Thistlethwaite, D. L. and Campbell, D. T. (1960). Regression-discontinuity analysis: An alternative to the ex post facto experiment. *Journal of Educational Psychology*, 51(6):309–317.
- Wright, P. G. (1928). The tariff on animal and vegetable oils. *Quarterly Journal of Economics*, 43(4):599–607.