

$$\bullet \chi^2(a_0, a_1) = \sum_{i=1}^n (y_i - (a_0 + a_1 x_i))^2$$

→ Mínimo debe estar en (a_0, a_1) que haga $\nabla \chi^2_{(a_0, a_1)} = 0$

$$\begin{aligned} \nabla \chi^2_{(a_0, a_1)} &= \left(\frac{\partial \chi^2_{(a_0, a_1)}}{\partial a_0}, \frac{\partial \chi^2_{(a_0, a_1)}}{\partial a_1} \right) = \left[-2 \sum (y_i - (a_0 + a_1 x_i)) \left(\frac{\partial (a_0 + a_1 x_i)}{\partial a_0}, \frac{\partial (a_0 + a_1 x_i)}{\partial a_1} \right) \right] \\ &= \left[-2 \sum (y_i - (a_0 + a_1 x_i)) (1, x_i) \right] \end{aligned}$$

$$\bullet \nabla \chi^2_{(a_0, a_1)} = 0 \begin{cases} \sum (y_i - (a_0 + a_1 x_i)) = 0 & 1) \\ \sum (y_i - (a_0 + a_1 x_i)) x_i = 0 & 2) \end{cases}$$

⇒ de 1)

$$\begin{aligned} \sum y_i - \sum a_0 - \sum a_1 x_i &= 0 \Rightarrow \sum y_i = n a_0 + a_1 \sum x_i \\ \Rightarrow a_0 &= \frac{\sum y_i}{n} - a_1 \frac{\sum x_i}{n} \Rightarrow \boxed{a_0 = \bar{y} - a_1 \bar{x}} \end{aligned}$$

⇒ Sustituir en 2)

$$\begin{aligned} \sum (y_i - (a_0 + a_1 x_i)) x_i &= \sum x_i y_i - \left(\frac{\sum y_i \sum x_i}{n} - \frac{a_1 \sum x_i \sum x_i}{n} \right) - a_1 \sum x_i^2 \\ \Rightarrow \sum x_i y_i - \frac{\sum y_i \sum x_i}{n} &+ \frac{a_1 (\sum x_i)^2}{n} - a_1 \sum x_i^2 = 0 \end{aligned}$$

$$\Rightarrow \boxed{a_1 = \frac{\sum x_i y_i - \frac{\sum y_i \sum x_i}{n}}{\sum x_i^2 - \frac{(\sum x_i)^2}{n}}}$$

- $\chi^2(a_0, a_1, a_2) = \sum_{\bar{i}=1}^n (y_{\bar{i}} - (a_0 + a_1 x_{\bar{i}} + a_2 x_{\bar{i}}^2))^2$

$$\nabla \chi^2(a_0, a_1, a_2) = 0 \quad \begin{cases} \sum_{\bar{i}=1}^n (y_{\bar{i}} - (a_0 + a_1 x_{\bar{i}} + a_2 x_{\bar{i}}^2)) = 0 & EC|0 \\ \sum_{\bar{i}=1}^n (y_{\bar{i}} - (a_0 + a_1 x_{\bar{i}} + a_2 x_{\bar{i}}^2)) x_{\bar{i}} = 0 & EC|1 \\ \sum_{\bar{i}=1}^n (y_{\bar{i}} - (a_0 + a_1 x_{\bar{i}} + a_2 x_{\bar{i}}^2)) x_{\bar{i}}^2 = 0 & EC|2 \end{cases}$$

$$\begin{cases} \sum_{\bar{i}=1}^n (a_0 + a_1 x_{\bar{i}} + a_2 x_{\bar{i}}^2) = \sum_{\bar{i}=1}^n y_{\bar{i}} & EC|0 \\ \sum_{\bar{i}=1}^n (a_0 x_{\bar{i}} + a_1 x_{\bar{i}}^2 + a_2 x_{\bar{i}}^3) = \sum_{\bar{i}=1}^n y_{\bar{i}} x_{\bar{i}} & EC|1 \\ \sum_{\bar{i}=1}^n (a_0 x_{\bar{i}}^2 + a_1 x_{\bar{i}}^3 + a_2 x_{\bar{i}}^4) = \sum_{\bar{i}=1}^n y_{\bar{i}} x_{\bar{i}}^2 & EC|2 \end{cases}$$

- Cada ecuación (j) se puede escribir como:

$$\sum_{\bar{i}=1}^n y_{\bar{i}} x_{\bar{i}}^j - \sum_{K=0}^{J+N} \left(\sum_{\bar{i}=1}^n d_{K-j} x_{\bar{i}}^K \right) = 0$$

- donde N es el grado Polinomial del modelo del ajuste,