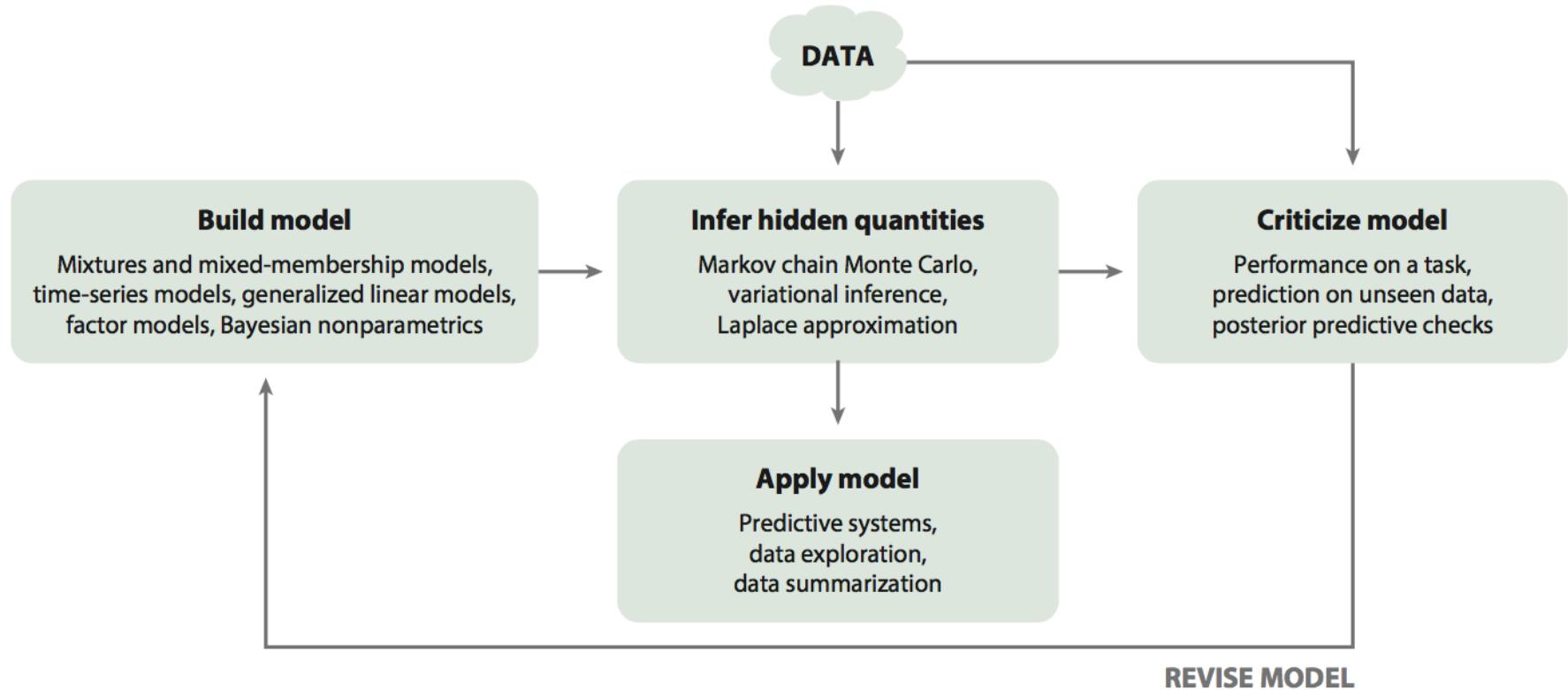


ΛMiDST TOOLBOX

Latent Variable Models

Andrés R. Masegosa

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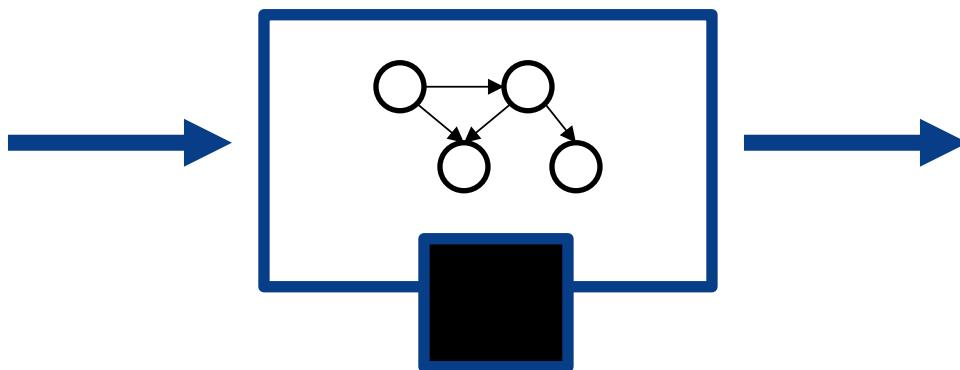


Blei, David M. "Build, compute, critique, repeat: Data analysis with latent variable models." *Annual Review of Statistics and Its Application* 1 (2014): 203-232.

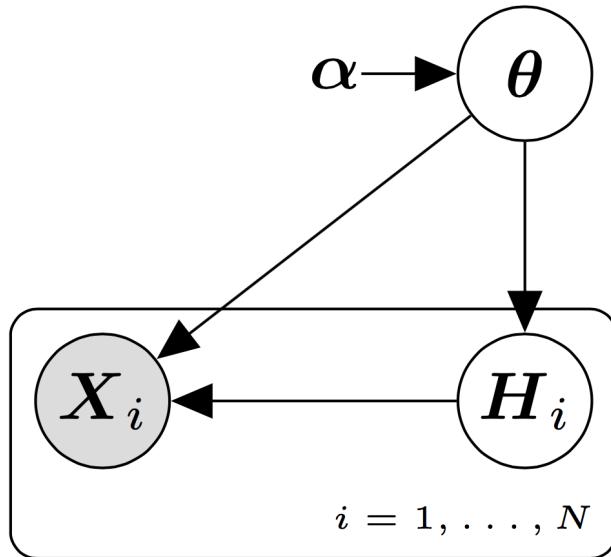
Openbox Models

[Probabilistic Graphical Models]

[Big] Data
[+Prior Information]



[Scalable] Bayesian Inference Engine
(Powered by Variational Methods)



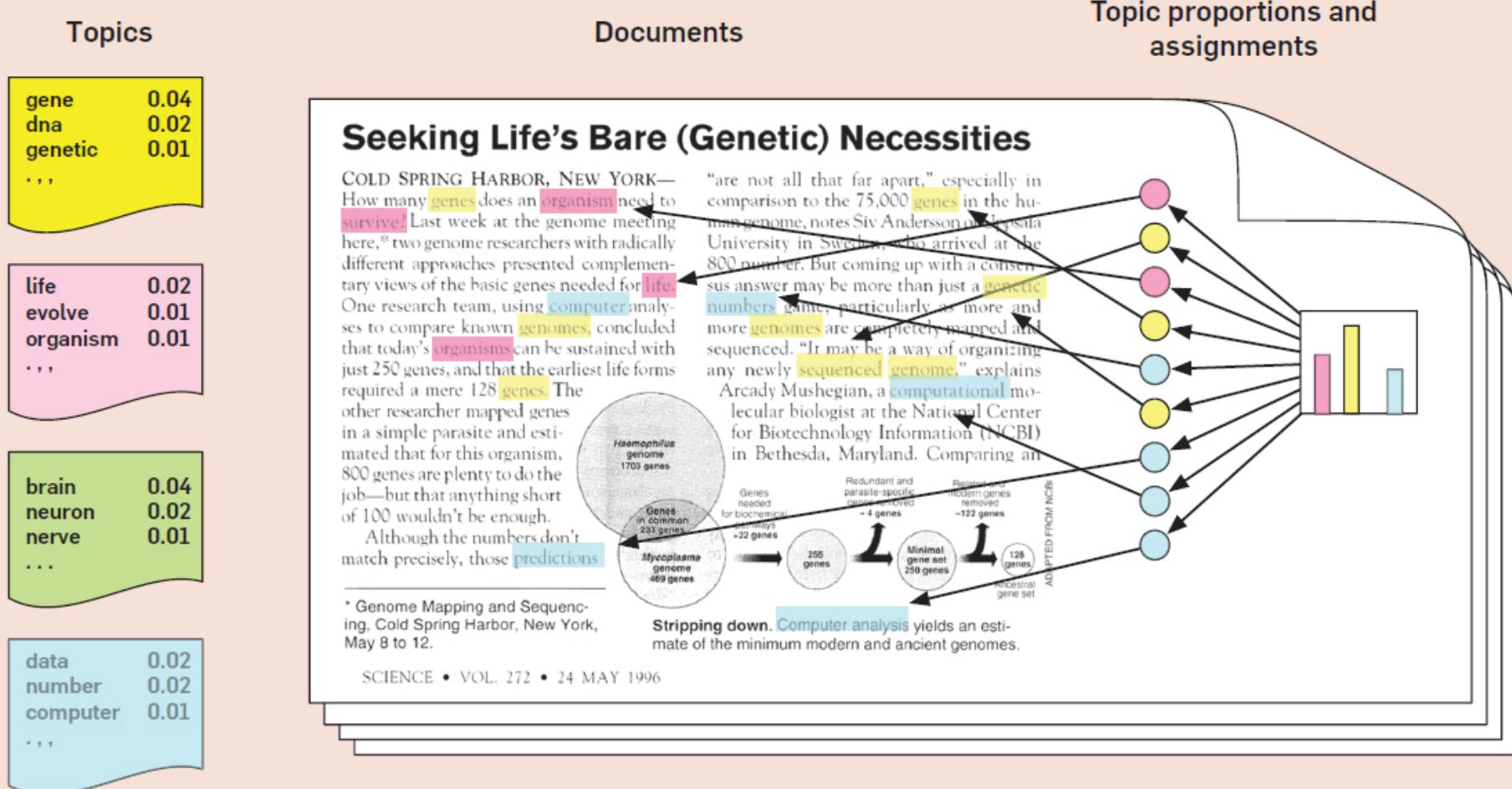
$$p(\theta, \mathbf{H}|D)$$

Latent Variable Models

Modeling non-observable mechanisms.

TEXT MODELING

AMIDST
TOOLBOX



David Blei, Probabilistic Topic Models, Communications of the ACM, Vol. 55 No. 4, Pages 77-84



TEXT MODELLING

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TOOLBOX



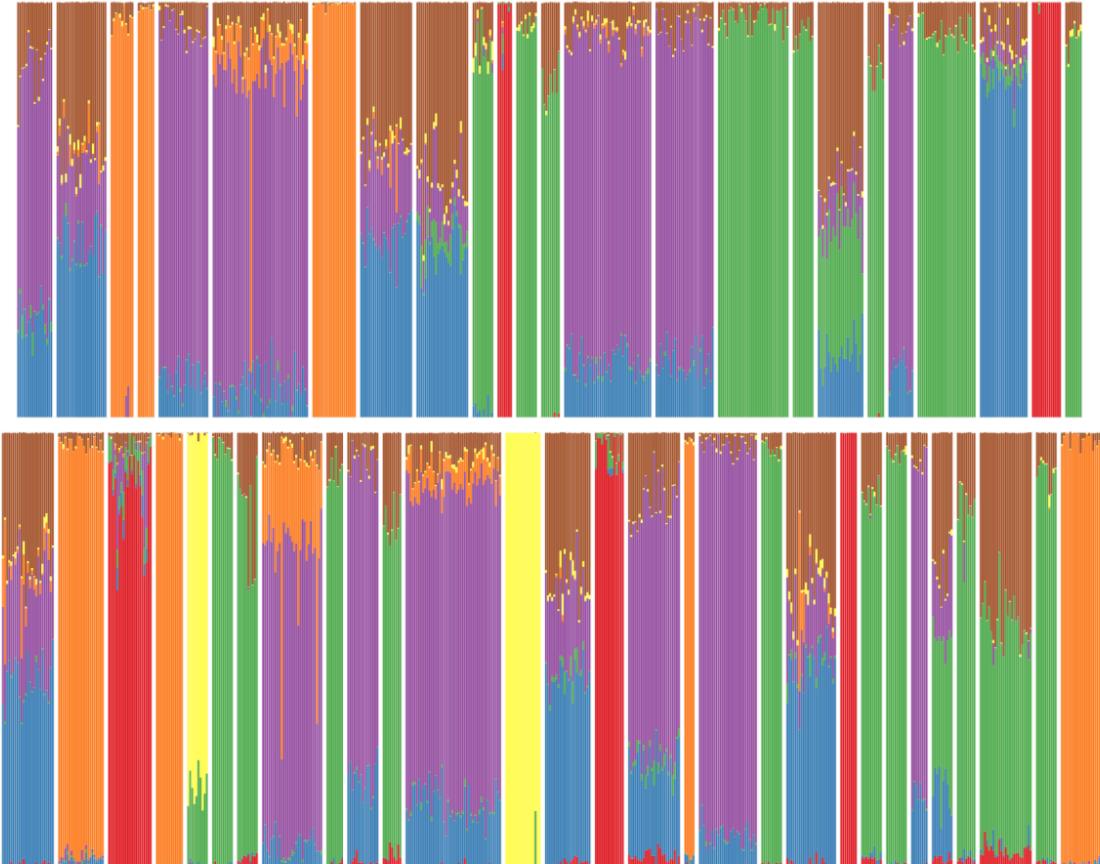
Topics found in 1.8M articles from the New York Times

[Hoffman, Blei, Wang, Paisley, JMLR 2013]



POPULATION GENETICS

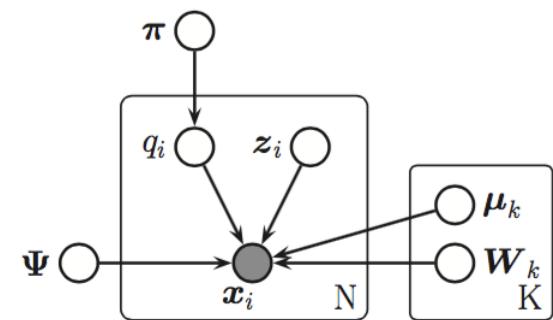
AMIDST
TOOLBOX



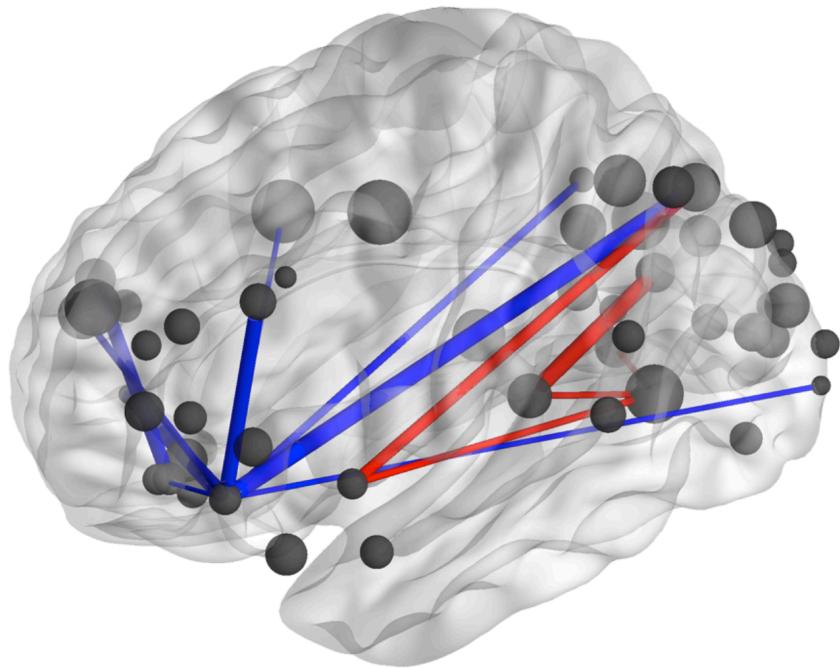
$$\begin{aligned}\beta_{k,\ell} &\sim \text{Beta}(a, b) \\ \theta_i &\sim \text{Dirichlet}(c) \\ x_{i,l} &\sim \text{Binomial}(2, \sum_k \theta_{i,k} \beta_{k,\ell})\end{aligned}$$

Gopalan, Prem, et al. Scaling probabilistic models of genetic variation to millions of humans.
Nature Research, 2016.





Trun et al. Automatic Differentiation Variational Inference. JMLR, 2016.



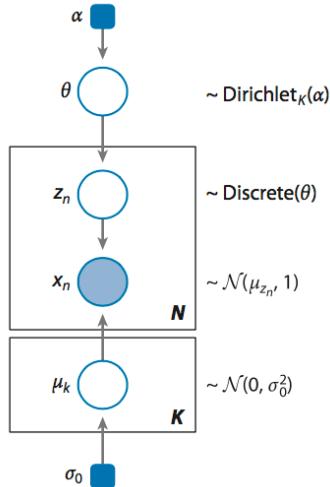
Neuroscience analysis of 220 million fMRI measurements

[Manning et al., PLOS ONE 2014]

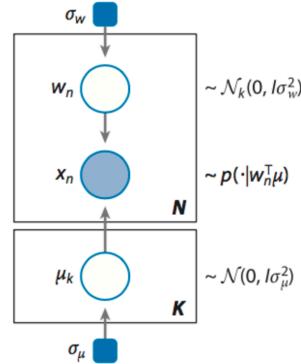
LATENT VARIABLE MODELS

AMIDST
TOOLBOX

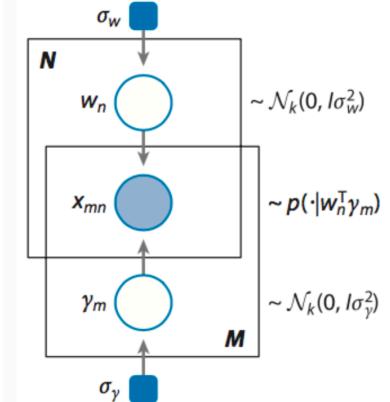
Blei, David M. "Build, compute, critique, repeat: Data analysis with latent variable models." *Annual Review of Statistics and Its Application* 1 (2014): 203-232.



Gaussian Mixture



Principal Component Analysis



Matrix Factorization

Latent Variable Models

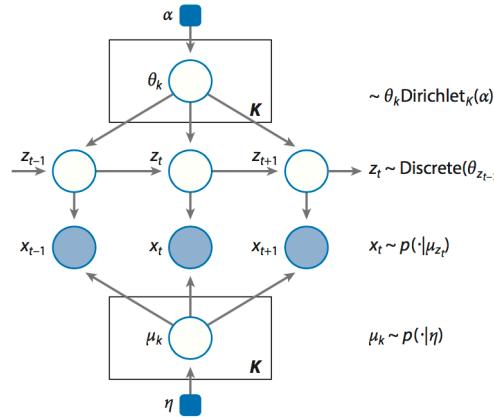
Gaussian Mixture Models, Principal Component Analysis, Factor Analyzers, Latent Dirichlet Allocation, etc.



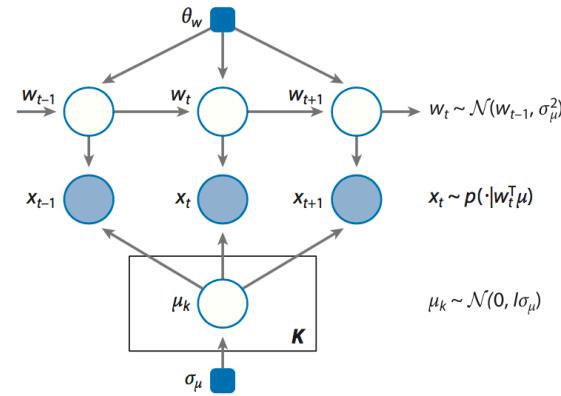
LATENT VARIABLE MODELS

AMIDST
TOOLBOX

Blei, David M. "Build, compute, critique, repeat: Data analysis with latent variable models." *Annual Review of Statistics and Its Application* 1 (2014): 203-232.



Hidden Markov Model

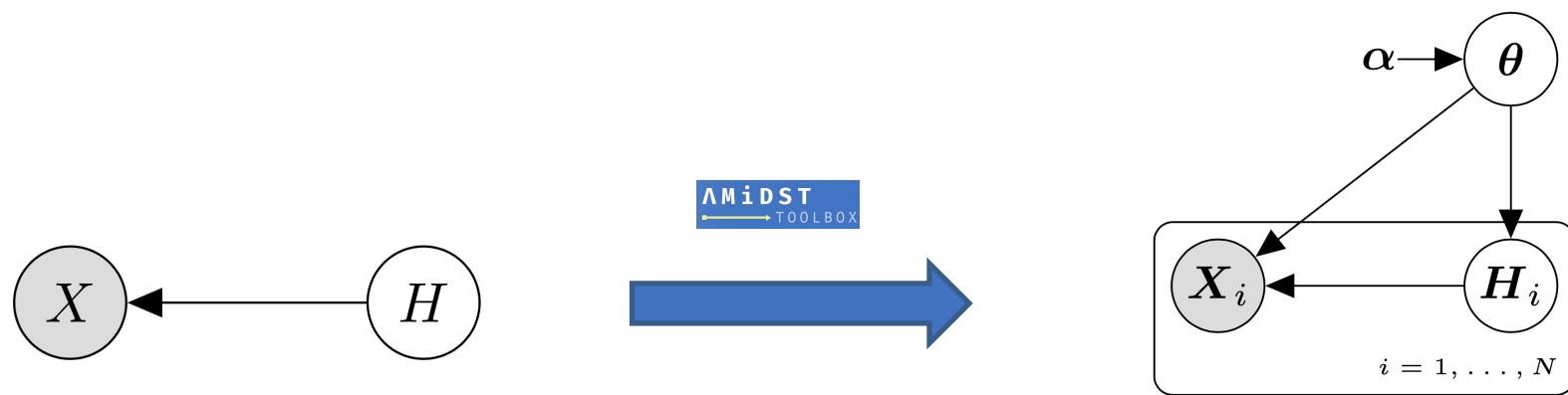


Kalman Filter

Dynamic/Temporal Models

Hidden Markov Models, Linear Dynamical Systems, State Space Models, Input-Output HMM, etc.





Automatic Bayesian Treatment

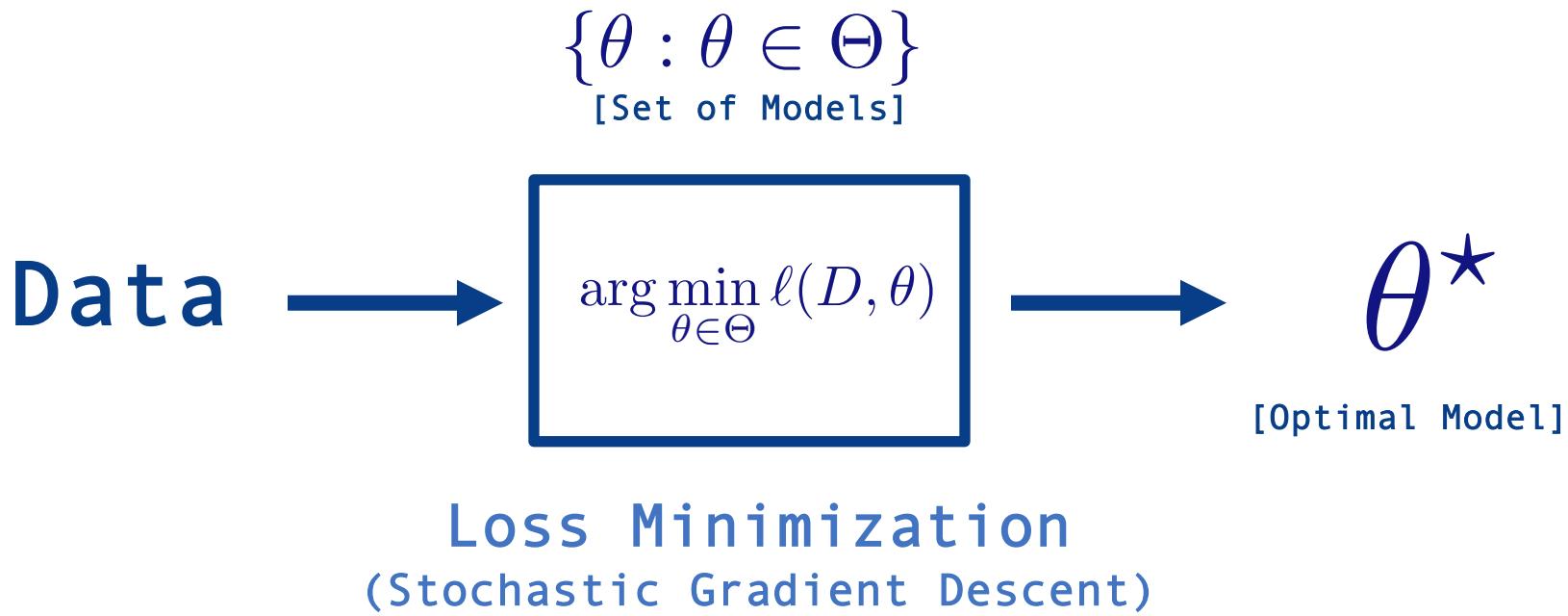
Modeling non-observable mechanisms.





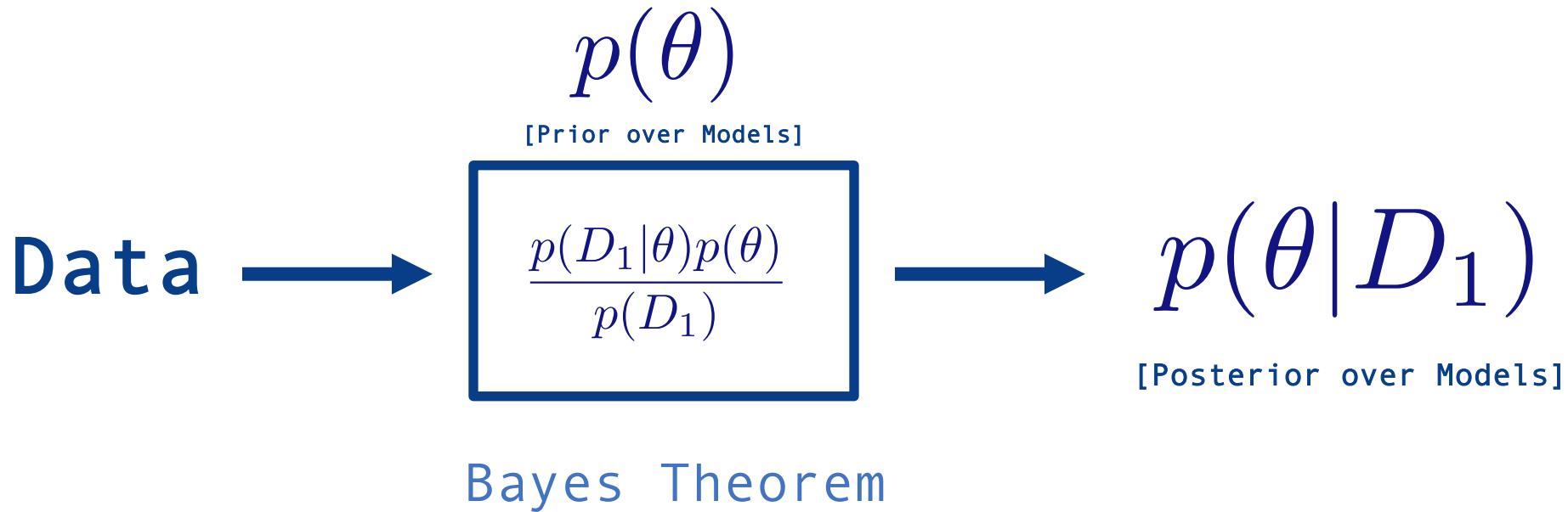
$$P(\theta | \mathbf{D})$$

Bayesian Learning



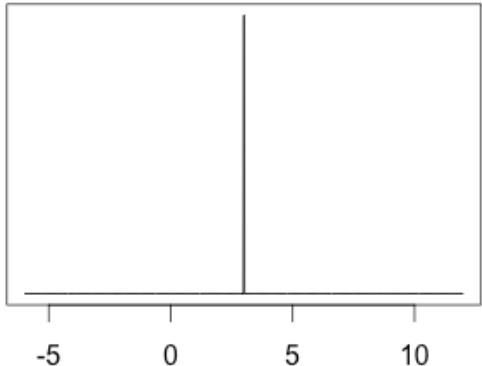
Example: $y = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_k \cdot x_k$



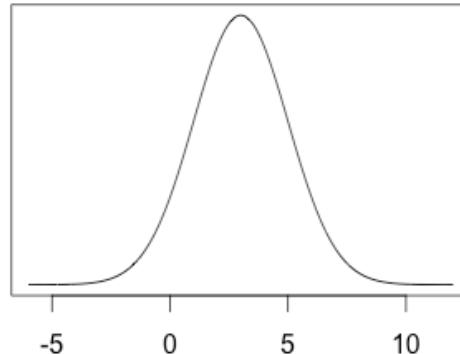


Learning as an inference Problem





VS



θ^*

[Point Estimate]

$p(\theta|D)$

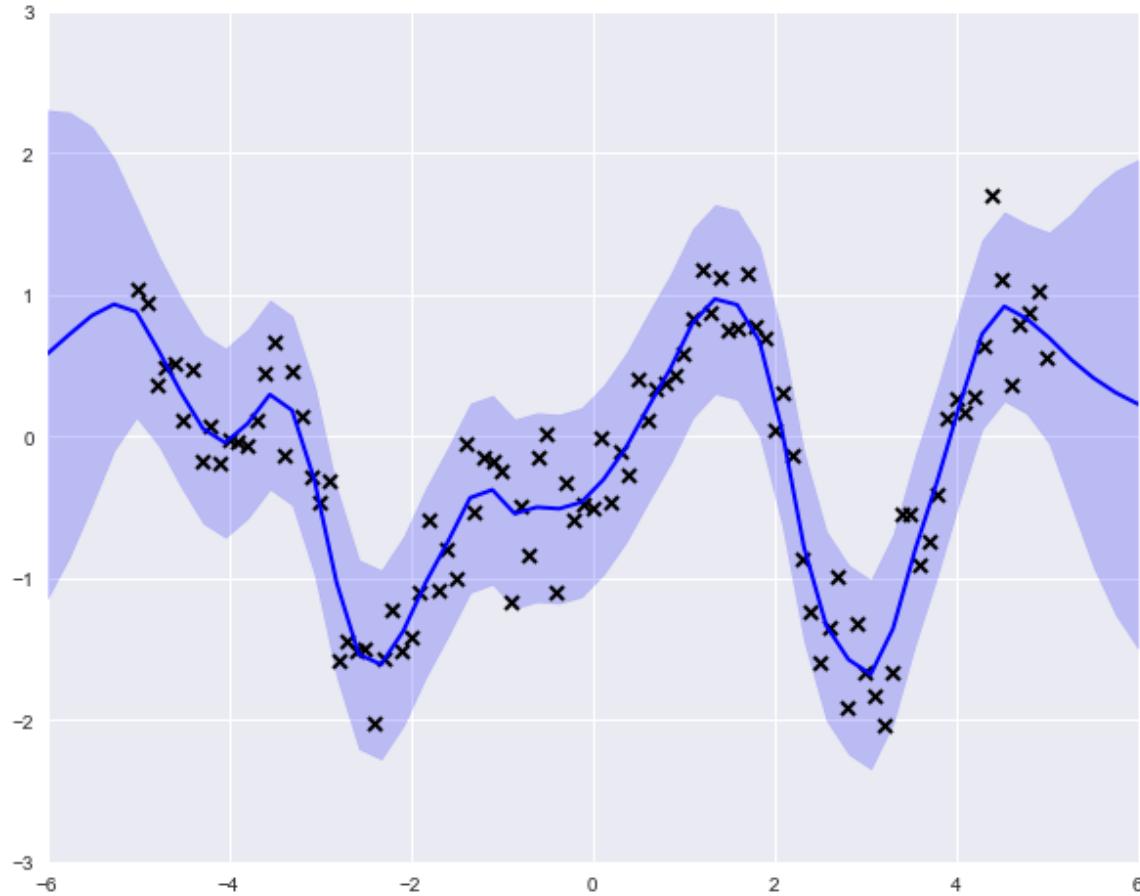
[Bayesian Estimate]

Example: $y = \theta_0 + \theta_1 \cdot x_1 + \dots + \theta_k \cdot x_k$



GAUSSIAN PROCESSES

AMIDST
TOOLBOX

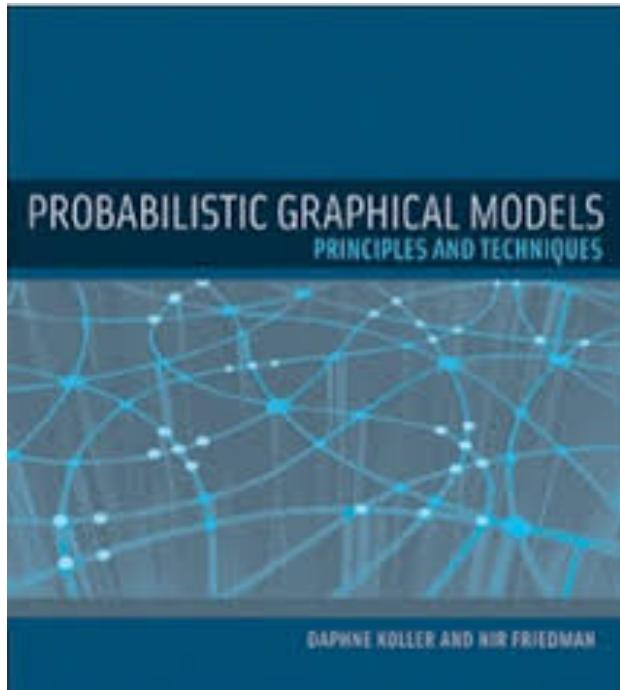


ID	S1_MaxTradeline	S2_BadLoans	S3_DeviceFirstSeen
841328	300	NA	11/16/2013
262927	500	0	10/1/2012
197305	750	0	NA
176415	NA	NA	NA
228986	0	3	NA
390908	800	NA	8/9/2013
846257	600	0	6/30/2012
254885	400	0	NA
833798	NA	0	3/9/2012
147660	900	2	NA

Probabilistic approach naturally deals with missing data

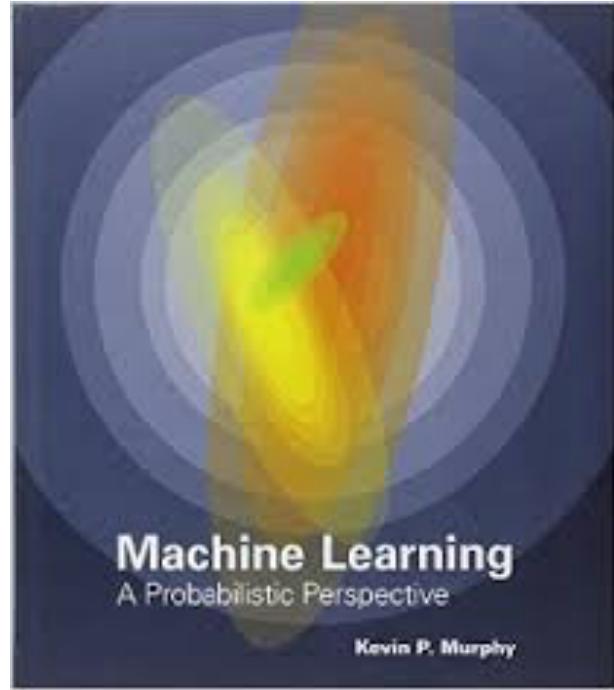
Everything is a random variable.





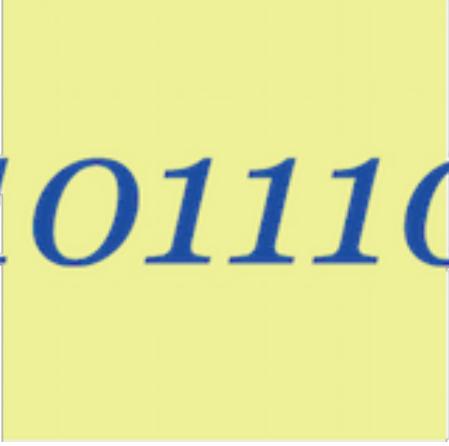
Probabilistic Graphical Models

+



Probabilistic Machine Learning



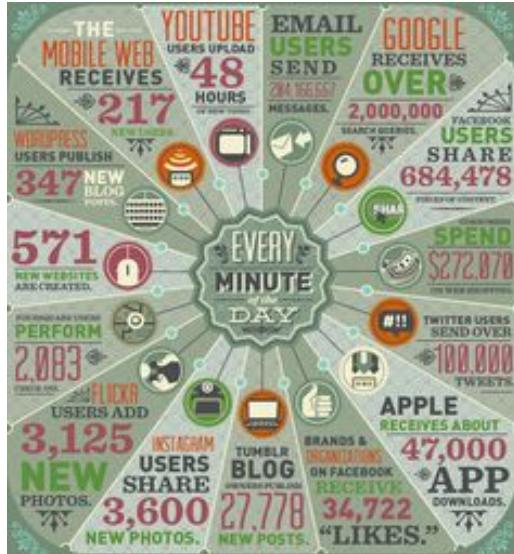
A large binary sequence "01011100" is displayed in blue text. It is overlaid on a yellow square, which is itself centered on a white rectangular background.

01011100

Data Streams

Update your models when new data is available.





- Unbounded Flows of Data are generated daily:
 - Social Networks, sensors, network monitoring, finance, etc.
 - Continuous Model Updating.



$$\{\theta : \theta \in \Theta\}$$

[Set of Models]

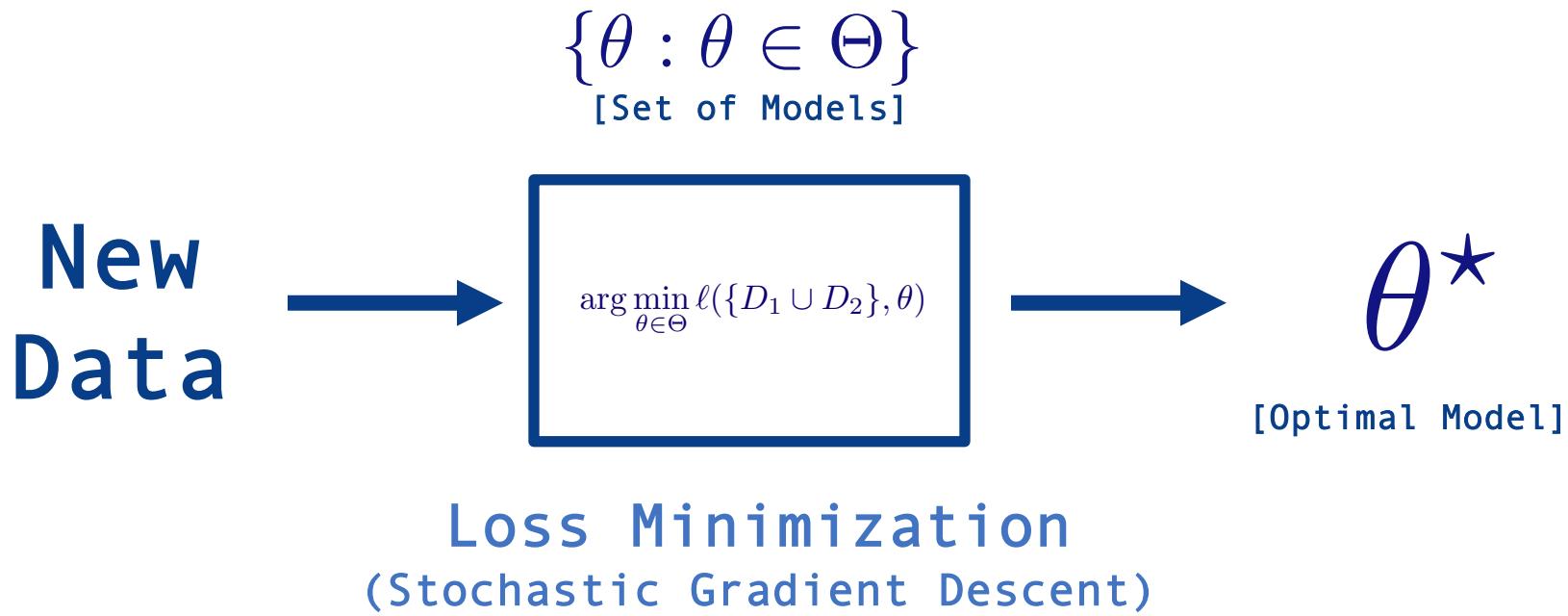
Data →

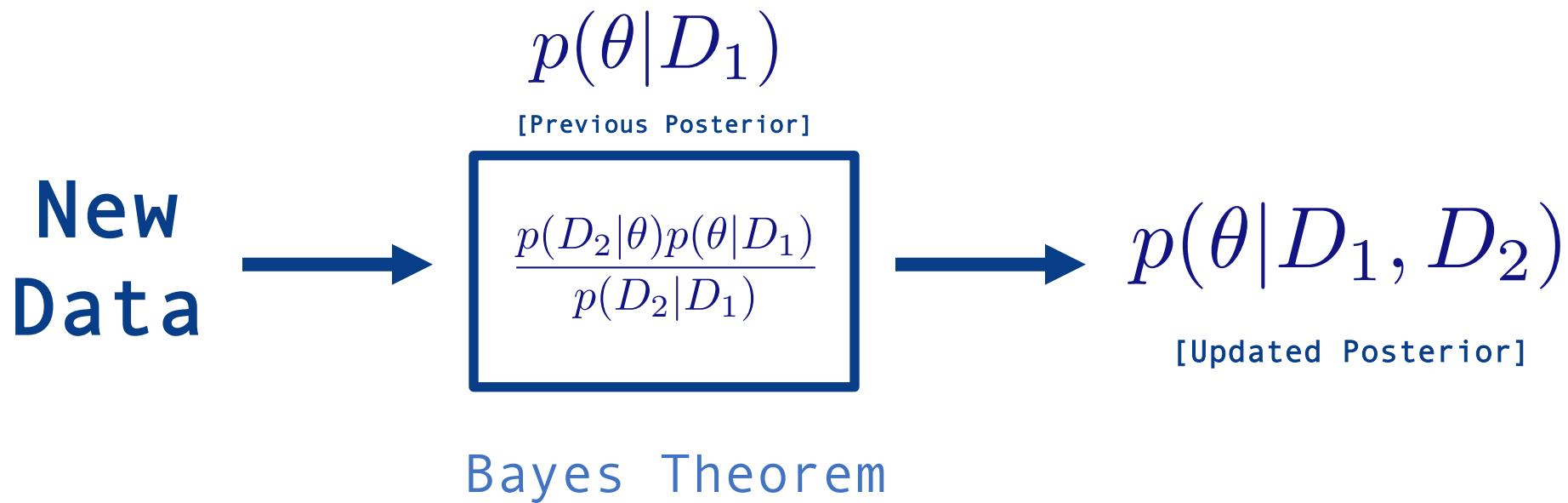
$$\arg \min_{\theta \in \Theta} \ell(D_1, \theta)$$

$$\theta^*$$

[Optimal Model]

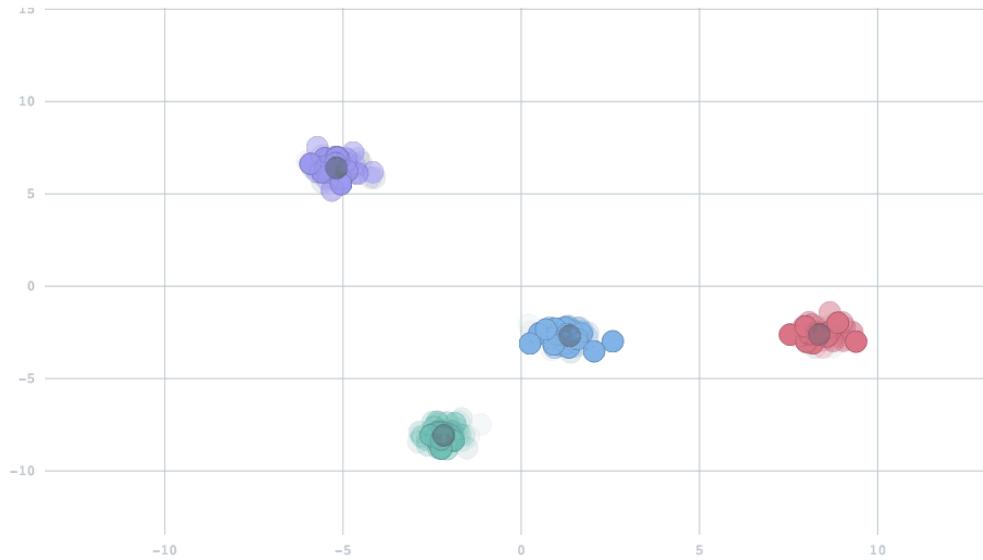
Loss Minimization
(Stochastic Gradient Descent)





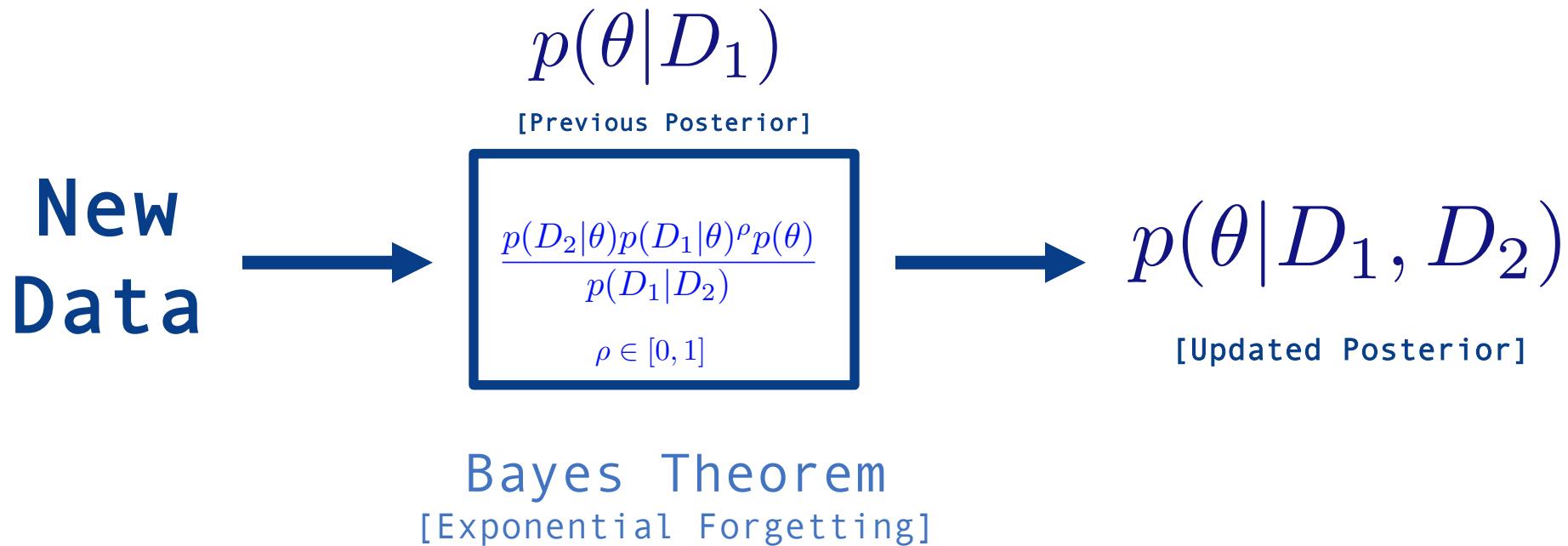
Freeman J. Introducing streaming k-means in Apache Spark 1.2.

<https://databricks.com/blog/2015/01/28/introducing-streaming-k-means-in-spark-1-2.html>



- Data may change from one time step to another.





- Old-data is exponentially down-weighted.
 - Forgetting Mechanism. Focus on the present.



$$P(\theta | \mathbf{D})$$

Scalable Learning

Perform Bayesian inference on your probabilistic models with powerful approximate and scalable algorithms.



$$p(\theta, H|D) = \frac{p(D|H, \theta)p(H|\theta)p(\theta)}{\int p(D|H, \theta)p(H|\theta)p(\theta) d\theta dH}$$

Highly Dimensional

Intractable Posterior

- Problem solving a highly multidimensional integral.
- Closed-form solution under very restrictive assumptions.
- Complex functional forms.



$$\arg \min_{\lambda} KL(q(\theta, H|\lambda) || p(\theta, H|D))$$

Approximation True Posterior

$$q(\theta, \mathbf{H}) = \prod_{k=1}^M q(\theta_k) \prod_{i=1}^N \prod_{j=1}^J q(H_{i,j})$$

Variational Methods

- The inference problem is casted as an optimization problem.
- Deterministic approximation.

Hoffman, Matthew D., et al. "Stochastic variational inference." *Journal of Machine Learning Research* 14.1 (2013): 1303-1347.



$$\ln p(D) = \mathcal{L}(\lambda) + KL(q(\theta, H|\lambda); p(\theta, H|D))$$

Constant

Maximize

Minimize

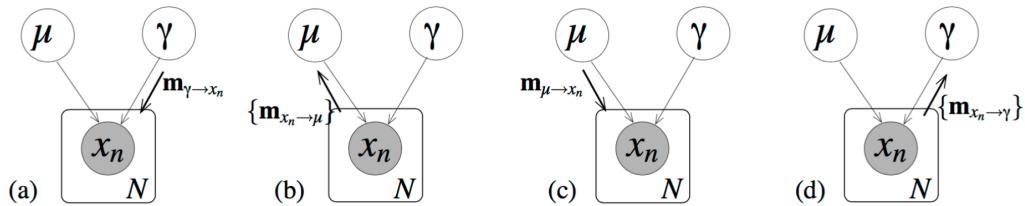
Optimization Problem

- The inference problem is casted as an optimization problem.
- Deterministic approximation.

Hoffman, Matthew D., et al. "Stochastic variational inference." *Journal of Machine Learning Research* 14.1 (2013): 1303-1347.



$$\frac{\partial \mathcal{L}}{\partial \lambda} =$$



Variational Message Passing

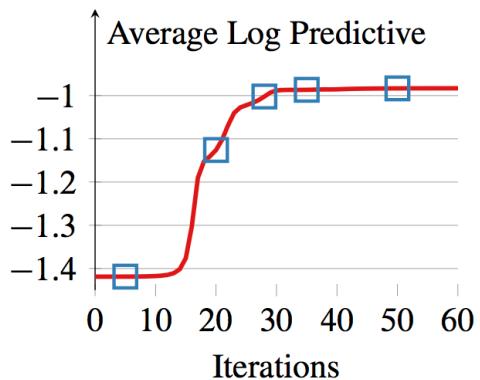
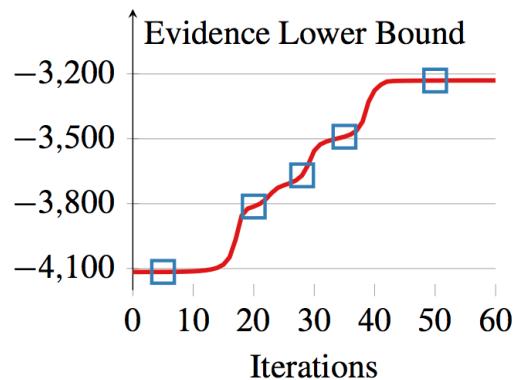
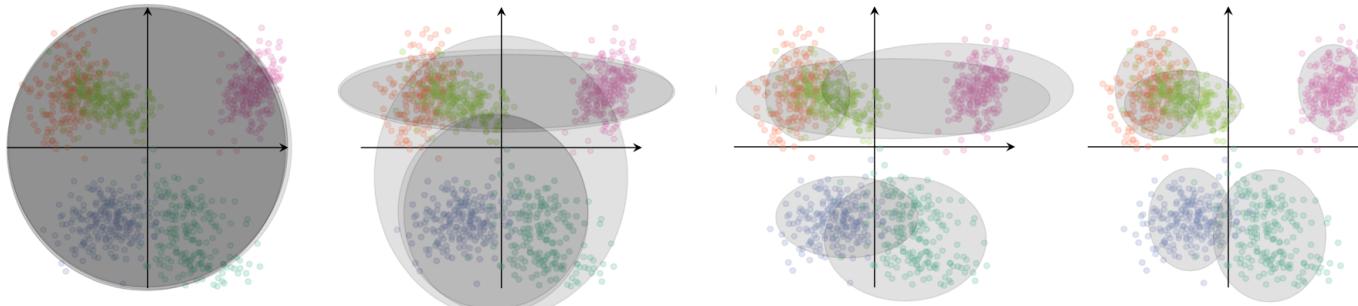
- Automatic Gradient Computation
- Coordinate Ascent Algorithm

Winn, J., & Bishop, C. M. (2005). Variational message passing. *Journal of Machine Learning Research*, 6(Apr), 661-694.



VARIATIONAL LEARNING

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Winn, J., & Bishop, C. M. (2005). Variational message passing. *Journal of Machine Learning Research*, 6(Apr), 661-694.



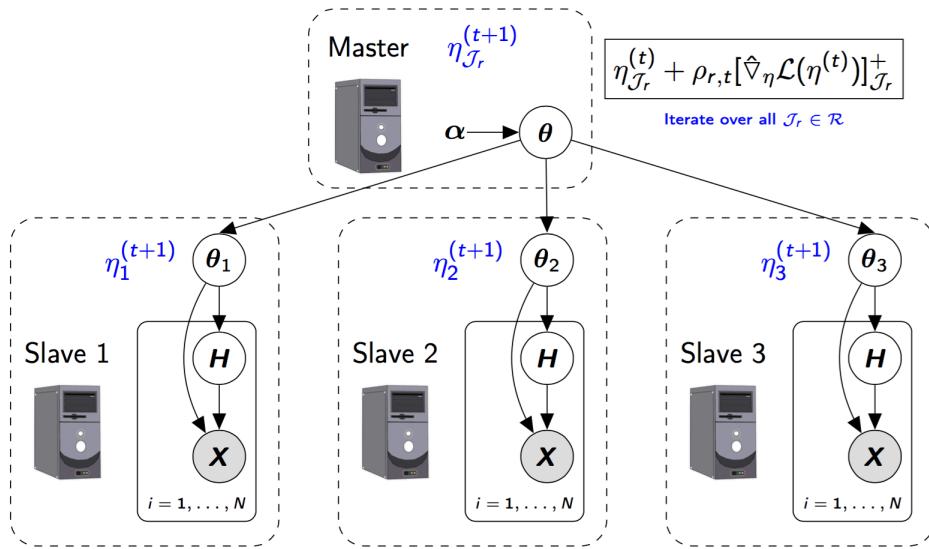
$$\lambda^{(t+1)} = \lambda^{(t)} + \rho \cdot N \cdot \frac{\partial \mathcal{L}(d_t, \lambda^{(t)})}{\partial \lambda}$$

Stochastic Gradient Ascent

- Estimate the gradient over a sub-sample of the data set

Hoffman, Matthew D., et al. "Stochastic variational inference." *Journal of Machine Learning Research* 14.1 (2013): 1303-1347.



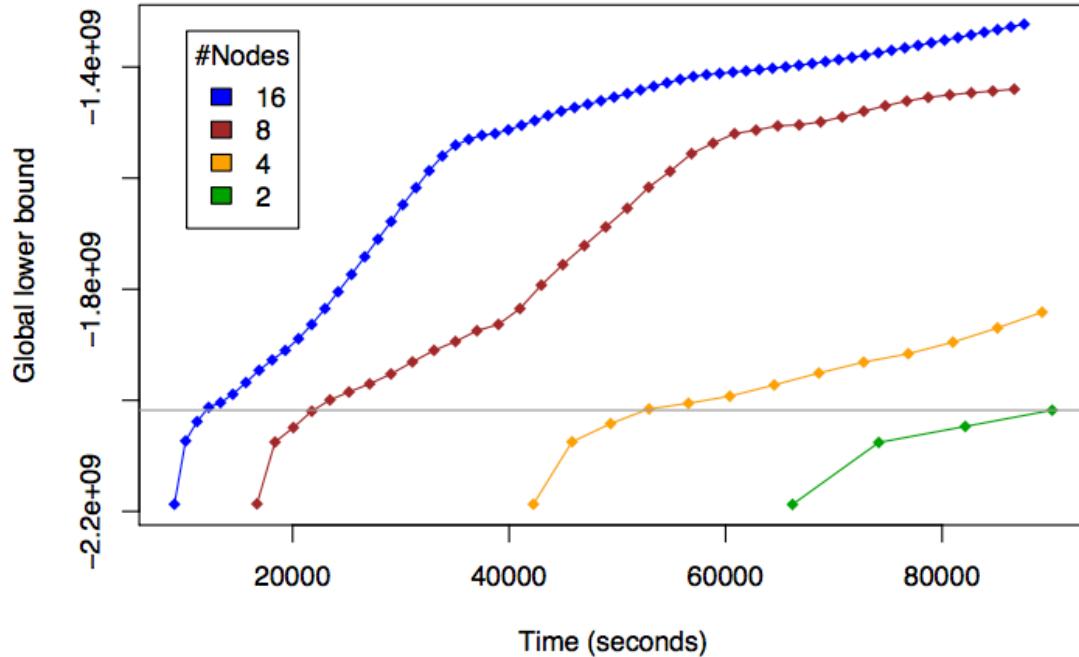


d-VMP Algorithm

A state-of-the-art distributed Variational Message Passing algorithm.

Masegosa, Andrés R., et al. "d-VMP: Distributed Variational Message Passing." *Proceedings of the Eighth International Conference on Probabilistic Graphical Models*. 2016.





Masegosa, Andrés R., et al. "d-VMP: Distributed Variational Message Passing." *Proceedings of the Eighth International Conference on Probabilistic Graphical Models*. 2016.

One billion node probabilistic model

Experiment on a Flink cluster with 16 nodes on AWS.



Thanks for your attention

www

www.amidsttoolbox.com

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contact@amidsttoolbox.com



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