A Game-Theoretic Interpretation of Organized Crime and Institutions

Andrés Romero

Players and Strategies

Two players interact in a simultaneous-move game:

- The State $E \in \{F, D\}$ chooses **Strong Institutions** (F) or **Weak Institutions** (D).
- Organized Crime $O \in \{N, X\}$ chooses **Non-confrontation** (N) or **Confrontation/Expansion** (X).

Parameters

Non-negative parameters:

- k: cost of maintaining F (enforcement, monitoring).
- λ : legitimacy/efficiency premium for the State under (F, N).
- D: institutional damage to the State if (D, X).
- d: analogous damage under (F, X) $(d \leq D)$.
- $\rho \in [0,1]$: effectiveness of repression under F.
- m: extra operational cost for F under confrontation.
- r_F, r_D : O's rents under non-confrontation with F or D $(r_D \ge r_F)$.
- R_F, R_D : O's rents under confrontation with F or D $(R_D \ge R_F)$.
- c: organizational cost of confrontation for O.
- s: sanction if repressed; under F the effective sanction is $s\rho$.
- $\theta \ge 0$: legitimacy loss from choosing D even without confrontation.

Payoff Matrix

$$\begin{array}{c|c|c} N & X \\ \hline F & (\lambda - k, r_F) & (-k - m - d(1 - \rho), R_F - c - s\rho) \\ \hline D & (-\theta, r_D) & (-\theta - D, R_D - c) \\ \end{array}$$

First entry: State; second: Organized Crime.

Best Responses (summary)

Organized Crime O:

Under
$$F: X \succ N \iff R_F - r_F \ge c + s\rho$$
,
Under $D: X \succ N \iff R_D - r_D \ge c$.

State E:

Given
$$N: F \succ D \iff \lambda \ge k - \theta$$
,
Given $X: F \succ D \iff D - d(1 - \rho) - m + \theta \ge k$.

Pure Strategy Nash Equilibria

- (F, N) iff $\lambda \geq k \theta$ and $R_F r_F \leq c + s\rho$.
- (D, N) iff $\lambda < k \theta$ and $R_D r_D < c$.
- (F,X) iff $D-d(1-\rho)-m+\theta \ge k$ and $R_F-r_F > c+s\rho$.
- (D, X) iff $D d(1 \rho) m + \theta < k$ and $R_D r_D \ge c$.

Mixed Strategy Equilibrium (summary)

Let p be the probability that O plays X, and q the probability that E plays F. Indifference yields

$$p = \frac{k - \theta - \lambda}{D - d(1 - \rho) - m - \lambda}, \qquad q = \frac{c - (R_D - r_D)}{(R_F - R_D) - (r_F - r_D) - s\rho}.$$

A mixed equilibrium exists if $p, q \in (0, 1)$ and denominators are nonzero.

Comparative Statics (intuition)

- Higher $\rho \Rightarrow$ larger $s\rho$ under F; X becomes less attractive; (F, N) expands.
- Higher $k \Rightarrow F$ becomes costlier; (F, \cdot) regions shrink; p rises in the mixed equilibrium.
- Higher D or lower $d \Rightarrow$ strengthens F when confrontation is likely; shifts mass from (D, X) toward (F, X) or (F, N).
- Larger $R_D r_D \Rightarrow$ increases the likelihood of (D, X) (collapse zone).

Interpretation

- 1. With effective institutions, governance coordinates on low confrontation (F, N).
- 2. With weak institutions, low confrontation (D, N) prevails until $R_D r_D \ge c$, after which confrontation dominates.
- 3. Collapse arises under (D, X) when the State avoids F and criminal returns to confrontation exceed costs.

Signalling Extension (Perfect Bayesian Equilibrium)

Nature first draws the State's type: **Strong** (S) with probability π , or **Weak** (W) with probability $1 - \pi$. The State observes its type and chooses a signal $s \in \{s_{strong}, s_{weak}\}$. Organized Crime O observes s (but not the type) and then chooses $a \in \{N, X\}$.

Type-dependent payoffs (mapping to baseline)

When O chooses N:

$$U_E^S(N) = \lambda - k, \quad U_E^W(N) = -\theta; \qquad U_O^S(N) = r_F, \quad U_O^W(N) = r_D.$$

When O chooses X:

$$U_{E}^{S}(X) = -k - m - d(1 - \rho), \quad U_{E}^{W}(X) = -\theta - D; \quad U_{O}^{S}(X) = R_{F} - c - s\rho, \quad U_{O}^{W}(X) = R_{D} - c.$$

Beliefs and O's best response to a signal

Let $\mu \equiv \Pr(S \mid s)$ be O's belief after seeing s. The expected gain from X over N is

$$\Delta_O(\mu) = \mu [(R_F - r_F) - (c + s\rho)] + (1 - \mu) [(R_D - r_D) - c].$$

O chooses X iff $\Delta_O(\mu) \geq 0$. Define the belief threshold μ^* by $\Delta_O(\mu^*) = 0$:

$$\mu^* = \frac{c - (R_D - r_D)}{(R_F - R_D) - (r_F - r_D) - s\rho} .$$

Hence O plays X after s iff $\mu \ge \mu^*$ (given the denominator > 0).

Separating PBE (deterrence via strong signal)

Consider a separating profile where S sends s_{strong} and W sends s_{weak} ; O's beliefs are $\mu(s_{strong}) = 1$, $\mu(s_{weak}) = 0$. O's best replies:

after
$$s_{strong}$$
: $\Delta_O(1) = (R_F - r_F) - (c + s\rho) \stackrel{!}{<} 0 \Rightarrow a = N;$ after s_{weak} : $\Delta_O(0) = (R_D - r_D) - c \stackrel{!}{\geq} 0 \Rightarrow a = N$

Let the cost of sending s_{strong} be τ_S for type S and τ_W for type W; normalize the cost of s_{weak} to zero for both types. Incentive compatibility (IC):

IC-S:
$$(\lambda - k) - \tau_S \ge -k - m - d(1 - \rho), \iff \tau_S \le \lambda + m + d(1 - \rho);$$

IC-W:
$$(-\theta - D) - 0 \ge (-\theta) - \tau_W$$
, $\iff \tau_W \ge D$.

Thus a separating PBE with deterrence exists if

$$R_F - r_F < c + s\rho$$
, $R_D - r_D \ge c$, $\tau_S \le \lambda + m + d(1 - \rho)$, $\tau_W \ge D$.

Pooling on strong signal

Suppose both types send s_{strong} , so $\mu(s_{strong}) = \pi$. O chooses N after s_{strong} iff $\Delta_O(\pi) < 0$. IC for types (no profitable deviation to s_{weak} which would induce X):

IC-S (no dev.):
$$(\lambda - k) - \tau_S \ge -k - m - d(1 - \rho) \iff \tau_S \le \lambda + m + d(1 - \rho),$$

IC-W (no dev.): $(-\theta) - \tau_W \ge (-\theta - D) \iff \tau_W \le D.$

Pooling is sustainable when

$$\Delta_O(\pi) < 0, \qquad \tau_S \le \lambda + m + d(1 - \rho), \qquad \tau_W \le D$$

Note the complementarity with separation: separation requires $\tau_W \geq D$, while pooling requires $\tau_W \leq D$.

Discussion

Signalling rationalizes bluffing: weak states may mimic strong signals when τ_W is low, leading to pooling and potential "tests" by O. When strong signals are sufficiently costly for weak states $(\tau_W \geq D)$, only strong states can credibly send them, producing separation and deterrence.

Appendix A. Step-by-step derivations (simultaneous game)

A1. State's best response given N

$$u_E(F, N) = \lambda - k, \qquad u_E(D, N) = -\theta.$$

Prefer F iff

$$\lambda - k \ge -\theta \iff \lambda \ge k - \theta$$
.

A2. State's best response given X

$$u_E(F, X) = -k - m - d(1 - \rho), \qquad u_E(D, X) = -\theta - D.$$

Prefer F iff

$$-k - m - d(1 - \rho) \ge -\theta - D$$

$$\theta + D - m - d(1 - \rho) \ge k$$

$$\iff D - d(1 - \rho) - m + \theta \ge k$$

A3. O's best response under F

$$u_O(F, N) = r_F,$$
 $u_O(F, X) = R_F - c - s\rho.$

Prefer X iff

$$R_F - r_F \ge c + s\rho \ .$$

A4. O's best response under D

$$u_O(D, N) = r_D,$$
 $u_O(D, X) = R_D - c.$

Prefer X iff

$$R_D - r_D \ge c$$
.

A5. Mixed equilibrium: State indifferent (solve for p)

 $\mathbb{E}[u_E|F] = (1-p)(\lambda - k) + p[-k - m - d(1-\rho)], \quad \mathbb{E}[u_E|D] = (1-p)(-\theta) + p(-\theta - D).$ Indifference \Rightarrow

$$(1-p)(\lambda-k) + p[-k-m-d(1-\rho)] = (1-p)(-\theta) + p(-\theta-D)$$

$$p[D-d(1-\rho)-m-\lambda] = k-\theta-\lambda$$

$$\implies p\left[\frac{k-\theta-\lambda}{D-d(1-\rho)-m-\lambda}\right].$$

A6. Mixed equilibrium: O indifferent (solve for q)

$$\mathbb{E}[u_O|X] = q(R_F - c - s\rho) + (1 - q)(R_D - c), \quad \mathbb{E}[u_O|N] = q r_F + (1 - q)r_D.$$

Indifference \Rightarrow

$$q[(R_F - R_D) - s\rho - (r_F - r_D)] = c - (R_D - r_D)$$

$$\implies q = \frac{c - (R_D - r_D)}{(R_F - R_D) - (r_F - r_D) - s\rho}.$$

Equivalent form (multiply num/den by -1):

$$q = \frac{(R_D - r_D) - c}{(R_D - R_F) - (r_D - r_F) + s\rho}.$$

A7. Interior-existence checks

A mixed equilibrium with $p, q \in (0, 1)$ exists when denominators are nonzero and parameter values imply 0 . Otherwise, one of the pure equilibria obtains.