
A crash course on LISP

Functional programming

- Definition From the "comp.lang.functional FAQ"

Functional programming is a style of programming that emphasizes the evaluation of expressions, rather than execution of commands.

The expressions in these language are formed by using functions to combine basic values.

A functional language is a language that supports and encourages programming in a functional style.

- Why functional programming matters?

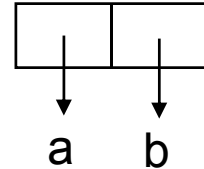
<http://www.cs.chalmers.se/~rjmh/Papers/whyfp.pdf>

Lisp resources

- CMU AI repository
<http://www-2.cs.cmu.edu/afs/cs.cmu.edu/project/ai-repository/ai/0.html>
- Reference book:
Common Lisp the Language, 2nd edition by **Guy L. Steele**, Thinking Machines, Inc. Digital Press 1990
paperbound 1029 pages ISBN 1-55558-041-6
<http://www-2.cs.cmu.edu/afs/cs.cmu.edu/project/ai-repository/ai/html/cltl/mirrors.html>
- Lisp FAQ
<http://www-2.cs.cmu.edu/afs/cs/project/ai-repository/ai/lang/lisp/faq/0.html>
- Lisp tutorials
<http://mypage.iu.edu/~colallen/lp/>
- Code taken from
ANSI Common Lisp, by Paul Graham.

Definitions

- **Cons:** A **cons** is a pair of pointers, the first of which is the **car** and the second one is the **cdr**.



- **Atom:**
 - » Basic lisp entity: the empty list, the constant atom t, a symbol, a number (real (rational (ratio integer) float) complex), a vector, an array, a character, a string
 - » Everything that is not a **cons**
(defun our-atomp (x) (not (consp x)))
- **List:**
 - » An ordered collection of atoms or lists (the elements of the list)
 - » A list is either **nil** or a **cons**
(defun our-listp (x) (or (null x) (consp x)))
- **Expression:** An atom or a list.
- **Form:** An expression to be evaluated by the Lisp interpreter.
- **Evaluation:**
 - » If the form is an atom: The value of the atom.
 - » If the form is a list: The value of a function evaluation
 - The first element of a list is interpreted as the name of the function to be evaluated.
 - The remaining elements are evaluated and given as the input to the function (prefix notation).

Definitions

- **Proper list:**

- » A lisp entity susceptible of being constructed with the **list** command.
- » A proper list is a list that is either **nil** or a **cons** whose **cdr** is a proper list

```
(defun our-proper-listp (x)
  (or (null x)
      (and (consp x)
            (our-proper-listp (cdr x)))))
```

- **Assoc-list (aka alist):**

- » A list of conses.
- » Each of these conses represents an association of a given key with a given value
 - the **car** of each cons is the key
 - the **cdr** is the value associated with that key

Warning: assoc-lists are slow (linear-time access)

Exercise: Write a function to determine whether an object is an assoc-list

```
(defun our-assoc-listp (x) ...)
```

Conses

cons, car, cdr, consp

» (setf x (cons 'a 'b))

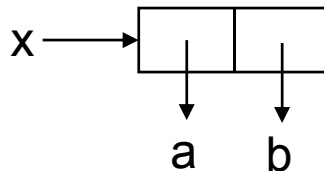
(a.b)

» (car x)

a

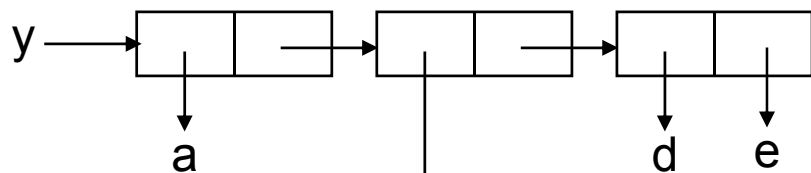
» (cdr x)

b



» (setf y (cons 'a (cons (cons 'b 'c) (cons 'd 'e))))

(A (B . C) D . E)



» (setf z (car (cdr y)))

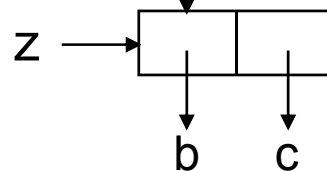
(b.c)

» (consp (cdr y))

T

» (consp (cdr z))

NIL

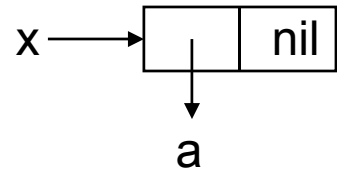


Lists

cons, car (first) , cdr (rest), list

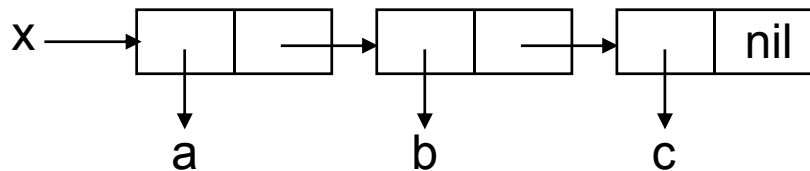
» (setf x (cons 'a nil))

(a)



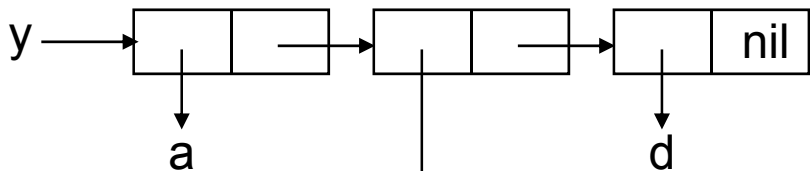
» (setf x (cons (car x) '(b c)))

(a b c)



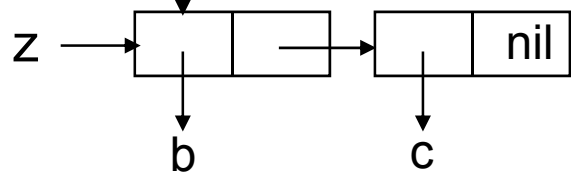
» (setf y (list 'a (list 'b 'c) 'd))

(a (b c) d)



» (setf z (car (cdr y)))

(b c)



» (eq z (cdr x))

NIL

» (equal z (cdr x))

T

» (eq z (car (cdr y)))

T

Commands for lists

- Constructing lists:
list, append, copy-tree
copy-list [! only copies cdr's of the elements]
nconc [! Destructive; macro]
- List properties:
null, listp [Boolean]
- Lists as conses:
car (first), cdr (rest), cadr, caddr, caaar, ..., cddddr, nthcdr
first, second, third, ..., tenth, nth, last, rest
- Lists as sets:
member, member-if, subsetp
adjoin, union, intersection, set-difference
- Lists as stacks
push, pop [! destructive; macros]
- Lists as sequences (sequences = vectors + lists)
length, count
find, find-if, position, position-if
merge
remove
delete [! destructive]
subseq, reverse
nreverse, sort [! destructive]
every, some [Boolean]
- Association lists
assoc

Example: Our-lisp-functions (1)

```
.....
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
;;; Home-made lisp functions.
....
;;;

(defun our-length (x)
  (if (null x)
      0
      (+ 1 (our-length (cdr x))))))

(defun our-copy-list (lst)
  (if (atom lst)
      lst
      ;; Watch out: you are only copying the cdr's
      (cons (car lst) (our-copy-list (cdr lst)))))

(defun our-assoc (key alist)
  (and (consp alist)
       (let ((pair (car alist)))
         (if (eql key (car pair))
             pair
             (our-assoc key (cdr alist))))))

....
;;;
;;; Note the use of recursion
;;; Do not forget the default case!
.....
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
```

Examples: Our-lisp-functions (2)

```
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;; More home-made lisp functions.
;;;

(defun our-member (obj lst)
  (cond ((atom lst) nil)
        ((eql (car lst) obj) lst)
        (t (our-member obj (cdr lst)))))
;;;
;;; Note the use of recursion
;;; Do not forget the default case!
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;

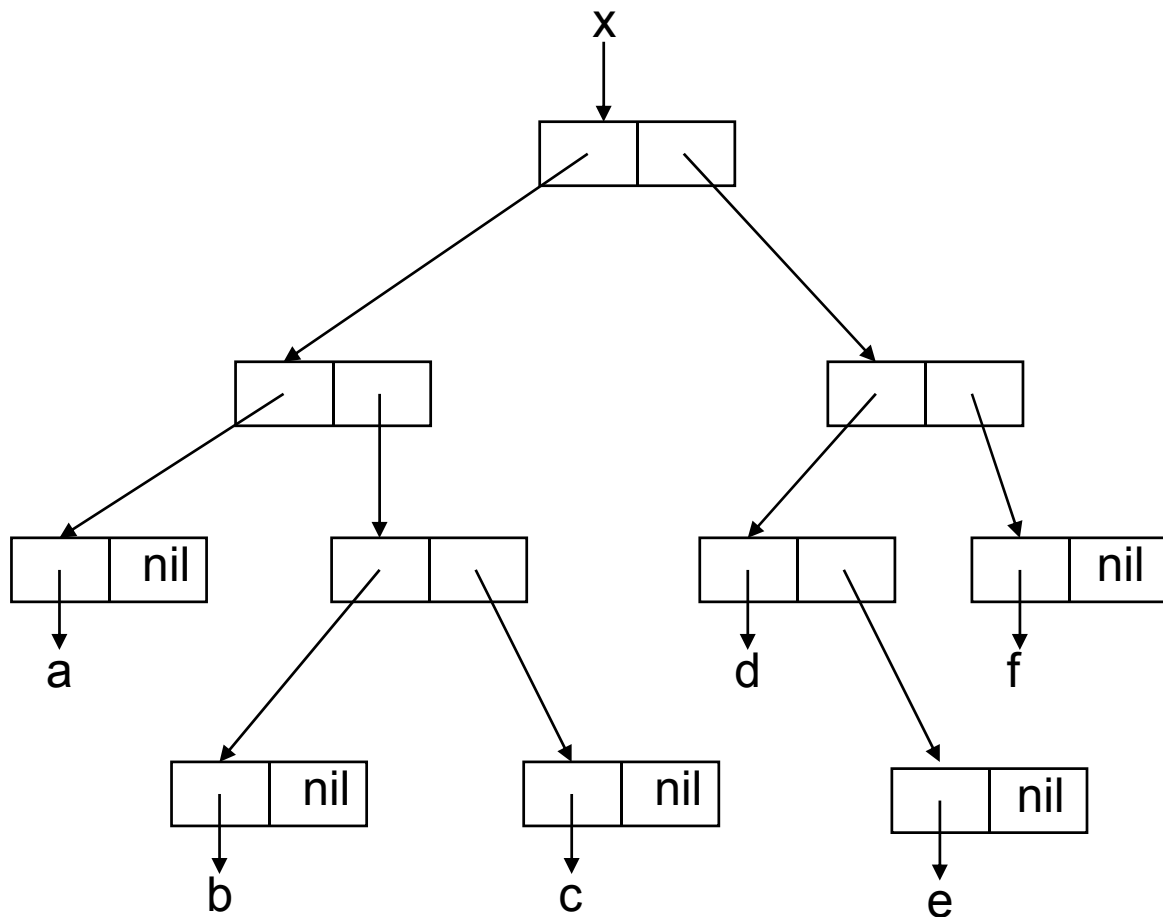
(defun lst-and (lst)
  (cond
    ((null lst) t)
    ((null (first lst)) nil)
    (t (lst-and (rest lst)))))

(defun lst-or (lst)
  (cond
    ((null lst) nil)
    ((null (first lst)) (lst-or (rest lst)))
    (t t)))
```

Conses and lists as trees

Conses can be thought of as binary trees with the **car** as the left subtree and the **cons** as the right subtree.

» (setf x '(((a) (b) c) (d e) f))



- Functions on trees
 - copy-tree**
 - tree-equal**
 - subst**

.....
 ,,,,,,,,,,,,,,


```
(defun our-copy-tree (tr)
  (if (atom tr)
      tr
      (cons (our-copy-tree (car tr))
            (our-copy-tree (cdr tr))))))
```

```

;;; Compare with our-copy-list:
;;; copy-tree copies the car and the cons.
;;; copy-list only copies the cons.
;;; If some car of the list elements is not an atom,
;;; changing (e.g. with setf) some value inside
;;; that car in the copy modifies original!

```

```
(defun our-substitute (new old tr)
  (if (eql tr old)
      new
      (if (atom tr)
          tr
          (cons (our-substitute new old (car tr))
                  (our-substitute new old (cdr tr)))))))
```

.....
 ,,,,,,,,,,,,,,


```
(defun same-shape-tree (tr1 tr2)
  (tree-equal tr1 tr2 :test #'our=true))
```

```
(defun our-true (&rest ignore) t)
```

```

::: (same-shape-tree '(((A) ((B) (C))) ((D (E)) F))
:::                               '((((A)) ((B) (C))) ((D (E)) F)))
:::
:::
::: (same-shape-tree '(((A) ((B) (C))) ((D (E)) F))
:::                               '(((1) ((2) (3))) ((4 (5)) 6)))
:::
:::
.....
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
```

Example: Quicksort on vectors

```
;;; Quick sort on vectors (vector = one-dimensional array)
(defun quicksort (vec l r)
  (let ((i l)
        (j r)
        (p (svref vec (round (+ l r) 2)))) ; middle element as pivot
    ;;
    ;; Partition vector by swapping elements until all
    ;; elements of the vector lower than the pivot are to the
    ;; to the left of those greater than the pivot
    (while (<= i j)
      (while (< (svref vec i) p) (incf i))
      (while (> (svref vec j) p) (decf j))
      (when (<= i j)
        (rotatef (svref vec i) (svref vec j))
        (incf i)
        (decf j)))
    ;;
    ;; If either of the partitions has two or more elements,
    ;; apply quicksort recursively to the partitions.
    (when (> (- j l) 1) (quicksort vec l j))
    (when (> (- r i) 1) (quicksort vec i r)))
  vec)
;; Example: (quicksort (vector 1 -2 3 -4) 0 3)
```

Exercise: Implement quicksort with lists

Some LISP functions (1)

Consider the following LISP functions:

- » COUNT / COUNT-IF / COUNT-IF-NOT
- » FIND / FIND-IF / FIND-IF-NOT
- » REMOVE / REMOVE-IF / REMOVE-IF-NOT

- REMOVE / REMOVE-IF

- » (remove <elmnt> <list> [:test <equality-test>] [:key <key>])
 - (remove 2 '(1 2 3 4 2 4 5 2))
(1 3 4 4 5)
 - (remove 2 '((1 a) (2 b) (3 c) (4 d) (2 f)))
((1 A) (2 B) (3 C) (4 D) (2 F))
 - (remove 2 '((1 a) (2 b) (3 c) (4 d) (2 f)) :key #'car)
((1 A) (3 C) (4 D))
 - (remove '(2 b) '((1 a) (2 b) (3 c) (4 d) (2 f)))
((1 A) (2 B) (3 C) (4 D) (2 F))
 - (remove '(2 b) '((1 a) (2 b) (3 c) (4 d) (2 f)) :test #'eql)
((1 A) (2 B) (3 C) (4 D) (2 F))
 - (remove '(2 b) '((1 a) (2 b) (3 c) (4 d) (2 f)) :test
#'equal)
((1 A) (3 C) (4 D) (2 F))
- » (remove-if[-not] <predicate><list>)
 - (remove-if #'oddp '(1 2 3 4 2 4 5 2))
(2 4 2 4 2)

Some LISP functions (2)

- FIND / FIND-IF

» (find <element> <list> [:test <equality-test>] [:key <key>])

– (find 2 '(1 2 3 4 2 4 5 2))
2

– (find 2 '((1 a) (2 b) (3 c) (4 d) (2 f)))
NIL

– (find 2 '((1 a) (2 b) (3 c) (4 d) (2 f)) :key #'car)
(2 b)

» (find-if[-not] <predicate><list>)

– (find-if #'oddp '(1 2 3 4 2 4 5 2))
1

- COUNT / COUNT-IF

» (count <elmnt> <list> [:test <equality-test>] [:key <key>])

– (count 4 '(1 2 3 4 2 4 5 2))
2

» (count-if[-not] <predicate><list>)

– (count-if #'oddp '(1 2 3 4 5 6))
3

Higer order functions (1)

- **# ' <fn>**: Reference to a function

- **apply**

Arguments: a function + a collection of arguments the last of which is a list

Evaluates to : Value of the function applied to the arguments

» (apply #' + '(1 2 3))

» (apply #' + 1 '(2 3))

» (apply #' + 1 2 3 '())

- **funcall**

Arguments: a function + a collection of arguments

Evaluates to : Value of the function applied to the arguments

» (funcall #' + 1 2 3)

Higer order functions (2)

- **mapcar**

Arguments: a function + one or more lists

Evaluates to: List of values resulting from applying the function to each of the elements of the list(s), until some list is exhausted

```
» (mapcar #'> '(1 2 3) '(4 1 2 5))
(NIL T T)
» (mapcar #'sqrt '(1 4 9 16))
(1 2 3 4)
```

- **mapcan:** (mapcar ...) = (apply #'nconc (mapcar ...))

```
(setf lst '(NIL 2 NIL 4 NIL 6))

(apply #'nconc (mapcar #'(lambda (x)
                           (if (null x)
                               NIL
                               (list x)))
              lst))

(mapcan #'(lambda (x)
              (if (null x)
                  NIL
                  (list x)))
        lst)
```

- **maplist**

Arguments: a function + one or more lists

Evaluates to: List of values resulting from applying the function to the list(s) and to each of the **cdrs** of the list(s), until some list is exhausted

```
» (maplist #'(lambda (x y) (append x y)) '(a b c) '(e f))
((A B C E F) (B C F))
```

The lambda function (anonymous functions)

- Notation used by Whitehead y Russell in *Principia Mathematica*.
- Evolution of notation
 - » $\lambda x(x + x)$ (Alonzo Church, 1941: definition of *lambda calculus*)
 - » $\Lambda x(x + x)$
 - » $\lambda x(x + x)$
 - » `(lambda (x) (+ x x))` (McCarthy 1958)
- Usage in LISP
 - » `(funcall #'(lambda (x) (+ x x)) 3)`
6
 - » `(mapcar #'(lambda (x) (* x x))
 '(1 2 3))`
(1 4 9)
 - » `(mapcar #'(lambda (x y) (list x y))
 '(a b c d) '(1 2 3))`
((a 1) (b 2) (c 3))

Variable visibility:

Lexical scope

- Scope determined by the structure of the code

```
>(let ((x 10)) (defun foo () x))  
>(let ((x 20)) foo)  
10
```

- **Lexical closure:** Section of the code where a variable with lexical scope is *visible*

```
> (defun main (z)  
  (example-of-scope z 3))
```

```
> (defun example-of-scope (x y)  
  (append (let ((x (car x)))  
            (list x y)))  
  x  
  z))
```

z is lexically invisible

Variable visibility:

Dynamic scope

- The LISP keyword `special` is used to denote that a variable has dynamic scope.
- In this example `x` in function `foo` does not refer to the lexically defined variable. It makes reference to any variable `x` declared as `special` when the function is evaluated.

```
>(let ((x 10)) (defun foo ()  
  (declare (special x)) x))  
>(let ((x 20))  
  (declare (special x))  
  (foo))  
20
```

- Usage: give a global variable `global` a new value only temporarily.
- very few programming languages have dynamic scope (Lisp, Tcl,...)
- It is difficult to use and debug

Use of let

- Use let to avoid repeating evaluations

WITH REPEATED CODE:

```
(defun foo(x)
  (if (> (* x x) 4)
      x
      (* x x)))
```

WITHOUT REPEATED CODE (**preferable**):

```
(defun foo(x)
  (let ((aux (* x x)))
    (if (> aux 4)
        x
        aux))))
```

Structures

A structure is a composite object that groups related data.

Example: Binary search tree

A binary search tree (BST) is either **nil** or a node whose left and right children are BST's

```
» (defstruct node
    elt
    (l nil)
    (r nil))
```

The following functions are immediately defined

make-node	(constructor)
node-p	(is ... a node?)
copy-node	(copy structure)
node-elt	(value of elt field)
node-l	(value of l field)
node-r	(value of r field)

```
» (setf nd1 (make-node :elt 0 ))
» (setf root (make-node :elt 1 :l nd1))
```

[illegible]

;;; Binary search trees.

```
(defstruct (node (:print-function
                  (lambda (n stream depth)
                    (format stream "#<~A>" (node-elt n))))))
  elt (l nil) (r nil))
```

```
(defun bst-insert (obj bst <)  
  (if (null bst)  
      (make-node :elt obj)  
      (let ((elt (node-elt bst)))  
        (if (eql obj elt)  
            bst  
            (if (funcall #'< obj elt)  
                (make-node  
                  :elt elt  
                  :l (bst-insert obj (node-l bst) <)  
                  :r (node-r bst))  
                (make-node  
                  :elt elt  
                  :l (node-l bst)  
                  :r (bst-insert obj (node-r bst) <))))))))))
```


Example: Binary-search-trees (2)

```
(defun print-tree (n)
  (if (null n)
      ()
      (progn
        (format t "~A" (node-elt n))
        (print-tree (node-l n))
        (format t "r")
        (print-tree (node-r n))))))
```

```
(defun bst-find (obj bst <)
  (if (null bst)
      nil
      (let ((elt (node-elt bst)))
        (if (eql obj elt)
            bst
            (if (funcall #'< obj elt)
                (bst-find obj (node-l bst) <)
                (bst-find obj (node-r bst) <)))))))
```

Example: Binary-search-trees (3)

```
(defun bst-min (bst)
  (and bst
    (or (bst-min (node-l bst)) bst)))
```

```
(defun bst-max (bst)
  (and bst
    (or (bst-max (node-r bst)) bst)))
```

```
(defun bst-remove (obj bst <)
  (if (null bst)
    nil
    (let ((elt (node-elt bst)))
      (if (eql obj elt)
        (percolate bst)
        (if (funcall #'< obj elt)
          (make-node
            :elt elt
            :l (bst-remove obj (node-l bst) <)
            :r (node-r bst))
          (make-node
            :elt elt
            :l (node-r bst)
            :r (bst-remove obj (node-r bst) <))))))))
```

[illegible]

Recursive programming (1)

- Lists are recursive data structures.
- Recursion is preferred to iteration in LISP
 - » Intuitive and elegant implementation.
- Example: Power of a number

```
(defun our-power (x n)
  (if (= n 0)
      1
      (* x (our-power x (- n 1)))))
```

- Example: Count atoms

```
(defun count-atoms (expr)
  (cond ((null expr) 0)
        ((atom expr) 1)
        (t (+ (count-atoms (first expr))
               (count-atoms (rest expr))))))
```

```
» (count-atoms '(a (b c) ((d (e)) f)))
```

Recursive programming (2)

- Example: Flatten list

```
(defun flatten (lst)
  (cond
    ((null lst) NIL)
    ((atom (first lst))
     (cons
      (first lst)
      (flatten (rest lst))))
    (t (append
         (flatten (first lst))
         (flatten (rest lst))))))

>> (flatten '(a (b c) ((d (e)) f)))
(a b c d e f)
```

Recursive programming (3)

- Example: Number of sublists in a list (number of times a parenthesis is opened minus 1)

```
(defun number-of-sublists (expression)
  (if (or (null expression) (atom expression))
      0
      (+ (if (atom (first expression)) 0 1)
         (number-of-sublists (first expression))
         (number-of-sublists (rest expression)))))
```

```
>> (number-of-sublists '(a (b c) ((d (e)) f)))
4
```

Recursion vs. Iteration (1)

- Recursive version

```
(defun scalar-product (v1 v2)
  (if (or (null v1) (null v2))
      0
      (+ (* (first v1) (first v2))
          (scalar-product (rest v1) (rest v2))))))
```

- Iterative version with mapcar

```
defun scalar-product (v1 v2)
  (apply #' + (mapcar #' * v1 v2)))
```

ERRONEOUS USE: Iterative version with dolist

```
(defun scalar-product (v1 v2)
  (let ((sum 0))
    (dotimes (i (length v1))
      (setf sum
              (+ sum (* (nth i v1)
                          (nth i v2)))))
    sum))
```

```
(scalar-product '(2 3) '(4 5))
```

Recursion vs. Iteration (2)

Our version of remove-if

- Mapcar version:

```
(defun our-remove-if (predicate lst)
  (remove NIL
    (mapcar #'(lambda (element)
      (unless
        (funcall predicate element)
        element))
      lst)))
```

- Mapcan version:

```
(defun our-remove-if (predicate lst)
  (mapcan #'(lambda (element)
    (unless
      (funcall predicate element)
      (list element)))
    lst))
```

```
>> (our-remove-if #'evenp '(1 2 3 4))
(1 3)
```


Recursion vs. Iteration (3)

- Recursive version:

```
(defun our-remove-if (predicate lst)
  (cond
    ((null lst) nil)
    ((funcall predicate (first lst))
     (our-remove-if predicate (rest lst)))
    (t (cons (first lst)
              (our-remove-if predicate (rest lst))))))
```

```
>> (our-remove-if #'evenp '(1 2 3 4))
```

- Iterative version (DO NOT USE):

```
(defun our-remove-if (predicate lst)
  (let (aux)
    (dolist (i lst aux)
      (unless (funcall predicate i)
        (setf aux (append aux (list i)))))))
```

```
(our-remove-if #'evenp '(1 2 3 4))
```

Mapcar + recursion

- Maximum depth of a list

```
(defun max-depth (expression)
  (cond
    ((null expression) 0)
    ((atom expression) 1)
    (t (+ 1
          (apply #'max (mapcar #'max-depth
                                expression))))))
```

```
>> (max-depth '1)
1
>> (max-depth '(1))
2
>> (max-depth '((1 (2 (3))) 4))
5
```

Tail recursion (1)

Recursion is sometimes not efficient

Example: Program to generate Fibonacci numbers

$\text{fibonacci}(0) = 0$

$\text{fibonacci}(1) = 1$

$\text{fibonacci}(n) = \text{fibonacci}(n-1) + \text{fibonacci}(n-2); \quad n \geq 2$

;;; Recursive: clear but inefficient

```
(defun fibonacci-recursive (n)
  (cond
    ((<= n 0) 0)
    ((= n 1) 1)
    (t (+ (fibonacci-recursive (- n 1))
          (fibonacci-recursive (- n 2))))))
```

;;; Iterative: efficient but unclear

```
(defun fibonacci-iterative (n)
  (if (<= n 0)
      0
      (do ((i n (- i 1))
          (f1 1 (+ f1 f2))
          (f2 1 f1))
          ((<= i 2) f1))))
```

Tail recursion (2)

- **Tail recursion** is a special case of **recursion** that can be transformed into an **iteration**.
- **Tail call optimization:**
 - » If the function is tail recursive, the result of the last call can be returned directly to the original caller.
 - » This reduces the amount of stack space used and improves efficiency.

Example: Factorial

```
;;; Recursive
(defun factorial-recursive (n)
  (if (<= n 1)
      1
      (* n (factorial-recursive (- n 1)))))

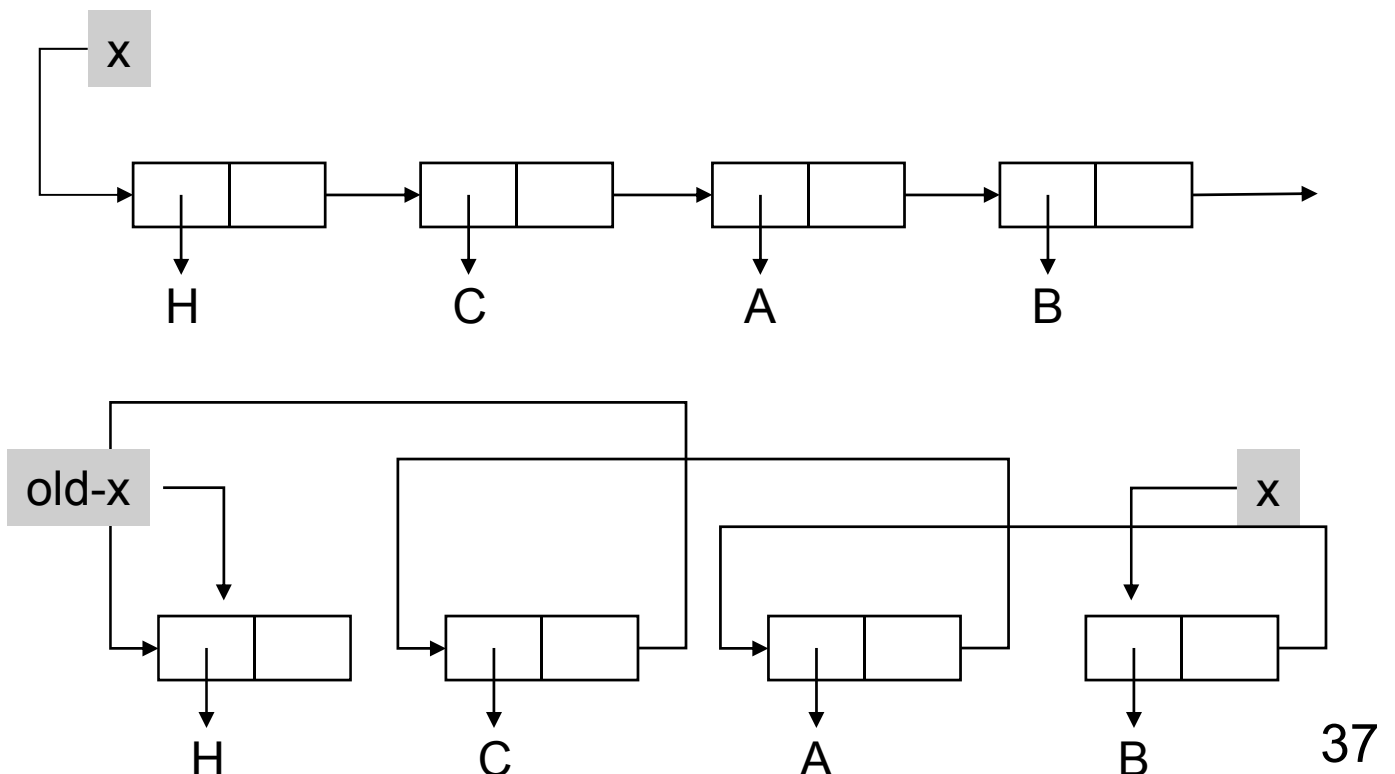
;;; Tail recursive: More efficient
(defun factorial-tail-recursive (n)
  (if (<= n 1)
      1
      (factorial-aux n 1)))
(defun factorial-aux (n accumulator)
  (if (<= n 1)
      accumulator
      (factorial-aux (- n 1) (* n accumulator))))
```

Destructive operations

- Consider the example

```
> (setf x '(H C A B))  
      (H C A B)  
> (setf old-x x)  
      (H C A B)  
> (setf x (nreverse old-x))  
      (B A C H)  
> x  
      (B A C H)  
>old-x  
      (H)
```

- NREVERSE destroys the list pointed at by `old-x`.
Pointers are reassigned in order not to generate garbage.



NREVERSE redefined

```
(defun our-nreverse (n)
  (our-nreverse-1 nil n))

(defun our-nreverse-1 (head tail)
  (let ((residual (cdr tail)))
    (our-nreverse-2 (setf (cdr tail) head)
                     residual
                     tail)))

(defun our-nreverse-2 (drop residual tail)
  (if (null residual)
      tail
      (our-nreverse-1 tail residual)))
```

Example: delete (destructive) / remove (non-destructive)

```
>> (setf lst '(a b c d))
(a b c d)
>> (delete 'a lst)
(b c d)
>> lst
(a b c d)
>> (delete 'b lst)
(a c d)
>> lst
(a c d)
```

Repeat operations using `remove` instead of `delete`

Age Group	Percentage
18-24	10%
25-34	15%
35-44	20%
45-54	25%
55-64	30%
65-74	35%
75-84	40%
85+	45%

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```
(defun compr (elt n lst)
  (if (null lst)
      (list (n-elts elt n))
      (let ((next (car lst)))
        (if (eql next elt)
            (compr elt (+ n 1) (cdr lst))
            (cons (n-elts elt n)
                  (compr next 1 (cdr lst))))))))
```

39

Age Group	Percentage
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65-74	35%
75-84	40%
85+	45%

```
(defun list-of (n elt)
  (if (zerop n)
      nil
      (cons elt (list-of (- n 1) elt))))
```

;;; Note the use of recursion + top-down design

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Page 10 of 10

[illegible]

### ;;; Breadth-first-search in graphs

```
(defun shortest-path (start end net)
  (bfs end (list (list start)) net))
```

```
(defun bfs (end queue net)
  (if (null queue)
      nil
      (let ((path (car queue)))
        (let ((node (car path)))
          (if (eql node end)
              (reverse path)
              (bfs end
                   (append (cdr queue)
                           (new-paths path node net))
                   net)))))))
```

```
(defun new-paths (path node net)
  (mapcar #'(lambda(n)
               (cons n path))
          (cdr (assoc node net)))))
```

□ □ □  
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```
;;; recursion + top-down design (new-paths) + use of queue
```

[illegible]