

# Contour Plot

*# Script for OF1 : Description of Re=10 part*

```
import numpy as np
import matplotlib.pyplot as plt

U = r"OF1\data\cavity.original\0.5\U"

with open(U, 'r') as file:
    lines = file.readlines()

velocity_data = []
reading = False

for line in lines:
    line_stripped = line.strip()
    if reading:
        if line_stripped.startswith("("):
            break
        if line_stripped.startswith("(") and line_stripped.endswith(")"):
            line_no_paren = line_stripped[1:-1]

            parts = line_no_paren.split()
            if len(parts) >= 2:
                u_val = float(parts[0])
                v_val = float(parts[1])
                velocity_data.append((u_val, v_val))
        if line_stripped.isdigit():
            reading = True

velocity_array = np.array(velocity_data)
print("Number of velocity points:", velocity_array.shape[0])

u_values = velocity_array[:, 0]
v_values = velocity_array[:, 1]

grid_size = (20, 20)
if velocity_array.shape[0] != grid_size[0] * grid_size[1]:
    raise ValueError("The number of data points does not match a 20x20 grid.")
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u_grid = u_values.reshape(grid_size)
v_grid = v_values.reshape(grid_size)

x = np.linspace(0, 1, grid_size[0])
y = np.linspace(0, 1, grid_size[1])
X, Y = np.meshgrid(x, y)

plt.figure(figsize=(6, 5))
contour_u = plt.contour(X, Y, u_grid, levels=20, cmap="coolwarm")
plt.xlabel("x")
plt.ylabel("y")
plt.title("Contour Line Plot of u-velocity (~u)")
plt.colorbar(contour_u, label="u velocity")
plt.show()

# Contour line plot for v-velocity (vertical component)
plt.figure(figsize=(6, 5))
contour_v = plt.contour(X, Y, v_grid, levels=20, cmap="coolwarm")
plt.xlabel("x")
plt.ylabel("y")
plt.title("Contour Line Plot of v-velocity (~v)")
plt.colorbar(contour_v, label="v velocity")
plt.show()

center_index = grid_size[0] // 2
u_profile = u_grid[:, center_index] # u at x = 0.5 for all y
v_profile = v_grid[:, center_index] # v at x = 0.5 for all y
plt.figure(figsize=(6, 5))
plt.plot(u_profile, y, label="u/U", color="blue")
plt.plot(v_profile*100, y, label="v/U * 100", color="red")
plt.xlabel("Velocity")
plt.ylabel("y")
plt.title("Velocity Profiles at x = 0.5")
plt.legend()
plt.grid()
plt.show()

```

# Refining the Solution

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# Script for OF1 : Refining the Solution part

#-----#

import numpy as np
import matplotlib.pyplot as plt

#-----#

gridsize = [20,40,80,160]

i = 0

L = 0.1 #m
nu = 0.01 #m^2/s
U = 1 #m/s
Re = L*U/nu

for k in range(len(gridsize)):
    Nx = Ny = gridsize[k]

    file_path = f'OF1\\code\\U\\verticalmidline_U_{Nx}.xy'

    y = []
    u = []
    v = []

    with open(file_path, 'r') as f:
        for l in f:
            k = l.split(" ")
            y.append(k[1])
            u.append(k[3])
            v.append(k[4])

    y = np.array(y,dtype=float)
    u = np.array(u,dtype=float)
    v = np.array(v,dtype=float)

    figk = plt.figure(i,figsize=(8,6))
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figk.canvas.manager.set_window_title(f"Velocity Component Plot for gridsize
{Nx}x{Ny}")

c=100

plt.plot(u,y/L,'-o',label=r"$u/U$")
plt.plot(v*c,y/L,'-s',label=r"$v/U \times \{c\}$")
plt.title(r"$\tilde{u}$, $\tilde{v}$ vs. $y/L$ ($x/L = 0.5$)", fontsize=16)
plt.ylabel(r"$\tilde{y}$",fontsize=12)
plt.xlabel(r"$\tilde{u}$, $\tilde{v}$",fontsize=12)
plt.grid()
plt.legend(loc='lower right',fontsize = 12)

i+=1

# times in seconds
EndTime = 0.5
ExecutionTimes = [0.13,0.58,5.93,91.66]
dt = [0.005,0.0025,0.00125,0.000625]
iterations = []
C = [] # execution time per step
N = []
for i in range(len(dt)):
    iterations.append(EndTime/dt[i])
    C.append(ExecutionTimes[i]/iterations[i])
    N.append(gridsize[i]**2)

# fit
a, b = np.polyfit(np.log10(N),np.log10(C),deg=1) # linear log fitting
b = 10**b

figNC = plt.figure(i+1,figsize=(8,6))
figNC.canvas.manager.set_window_title("Refinement Measure")

plt.loglog(N,C,'r-s')
plt.plot(N,b*N**a,'k',linewidth = 1.5, label = r"$C = \beta N^{\alpha}$")
plt.title(r"$C$ vs. $N$" '\n' r"$\beta = $" f"{b:.3e}", " r"$\alpha = $" f"
{round(a,3)}", fontsize=16)
plt.ylabel("C (seconds/step)",fontsize=12)
plt.xlabel("N (gridpoints)",fontsize=12)
plt.grid()
plt.legend(loc='lower right',fontsize = 12)
plt.show()

```

# Force on the Lid

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# Script for OF1 : Force on the Lid part

#-----#

import numpy as np
import matplotlib.pyplot as plt
from scipy.integrate import trapezoid

#-----#

Re = [10,50,100,250,500]
endtime = [0.5, 1.5, 2.5, 3, 4]
F = []

for r in range(len(Re)):
    Ufile = rf"OF1\data\DeltaRe\cavityRe{Re[r]}\{endtime[r]}\U"
    print(f"Reading {Ufile}")

    Nx = Ny = 80 # gridsize

    L = 0.1 # 0.1m
    U = 1 #m/s

    u = []

    with open(Ufile, 'r') as f:
        lines = f.readlines()

    for i in lines:
        if i.startswith("("):
            k = i.split()[0][1:]
            u.append(k)

    # all x-component velocities from y=0 to y=1
    u = u[1:]
    u = np.array(u, dtype=float)

    Ux = np.zeros([Nx, Ny])

    # Mean x-component velocity in each row starting from row y=1 to y=0
```

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for i in range(Nx):
    for j in range(Ny):
        Ux[i,j] = u[(Nx*Ny-80*(i+1))+j]

x = np.linspace(0,L,Ny)/L
dx=dy=1/Nx

tau = np.zeros(Nx)

n = 4 #rows to fit over
y=1 #evaluate derivative at this point

#polynomial fitting
for i in range(Nx):
    a,b,c = np.polyfit(x[0:n],Ux[0:n,i],2)
    tau[i] = 2*a*(y) + b

figRe = plt.figure(0,figsize=(8,6))
figRe.canvas.manager.set_window_title("Nondimensional Stress vs. x")

plt.plot(x,tau,linewidth=2,label=f"Re = {Re[r]}")
plt.title("$\\tilde{\\tau}$ vs. $\\tilde{x}$, Meshsize = " f"{Nx}x{Ny}",
fontsize = 16)
plt.ylabel(r"$\\tilde{\\tau}$",fontsize=14,rotation=0)
plt.xlabel(r"$\\tilde{x}$",fontsize=14)
plt.grid()
plt.legend(loc="lower left")

F.append(trapezoid(tau,x,dx=dx))

figRe = plt.figure(1,figsize=(8,6))
figRe.canvas.manager.set_window_title("Nondimensional Force vs. Re")
plt.plot(Re,F,'r-s',markersize=7)
plt.title("$\\tilde{F}$ vs. Re, Meshsize = " f"{Nx}x{Ny}", fontsize = 16)
plt.ylabel(r"$\\tilde{F}$",fontsize=14,rotation=0)
plt.xlabel(r"Re",fontsize=14)
plt.grid()

plt.show()

```