

Contract Regulation in Selection Markets

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Roadmap

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Motivation 1

- ▶ Selection markets are often tightly regulated
 - ▶ mandatory purchase / non-purchase fees (health insurance in US, Germany)
 - ▶ minimal coverage (most markets)
 - ▶ maximal coverage (US exchanges, “platinum” plans)
- ▶ How do these affect equilibrium and welfare?

In this paper

- ▶ Tractable model of a competitive selection market
 - ▶ continuum of types
 - ▶ realistic regulation:
 - ▶ minimum and maximum coverage
 - ▶ non-purchase fee
 - ▶ special cases: Akerlof 70 and Rothschild-Stiglitz 76
- ▶ Equilibrium typically exhibits partial pooling
 - ▶ depends non-trivially on the type distribution (unlike in RS)
- ▶ Equilibrium is unique if the type distribution is log-concave.
- ▶ Increasing the non-purchase fee increases welfare if the density of cost types is decreasing.
- ▶ The optimal level of the minimum coverage is positive, below full insurance and induces some pooling at the minimum coverage.
- ▶ The optimal level of the maximum coverage is full insurance (even in an extension that allows for moral hazard).

Literature

- ▶ **Theory of regulation in markets for lemons**
 - ▶ Weyl Veiga 2016, Veiga 2023, Einav Finkelstein Tebaldi 2016, Handel Hendel Whinston 2015, Gemmo Kubitz Rothschild 2020, etc
- ▶ **Theory of regulation in RS settings**
 - ▶ Veiga Weyl 2016, Azevedo Gottlieb 2017, Neudeck Podcizek 1996, Encinosa 2001, Noton Olivella 2015, Farinha Luz et al 2022
- ▶ **Empirics of regulation in markets for lemons**
 - ▶ Finkelstein 2004, Einav Finkelstein Schrimpf 2010, Saltzman 2021, Landais et al 2021, Geruso et al 2021, Marone Sabety 2022

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Types

- ▶ Type $\mu > 0$ captures expected cost
- ▶ Types $\Theta = [\underline{\mu}, \bar{\mu}]$
- ▶ PDF $f(\mu) > 0$, CDF $F(\mu)$
- ▶ We will assume f log-concave: $\frac{\partial^2}{\partial \mu^2} \ln[f(\mu)] \leq 0$

Contracts

- ▶ If an individual buys coverage x , the insurer covers a share x of the loss
- ▶ Allowed contracts are

$$x \in X = \{0\} \cup [\underline{x}, \bar{x}] \subseteq [0, 1]$$

- ▶ Not buying: $x = 0$
- ▶ Minimal coverage: $\underline{x} \geq 0$
- ▶ Maximal coverage: $\bar{x} \leq 1$
- ▶ Full insurance: $x = 1$

Cost

- ▶ (Endogenous) price of coverage x is

$$p(x) \geq 0$$

- ▶ A contract is a pair

$$(x, p)$$

- ▶ If type μ buys (x, p) , the expected cost to the insurer is

$$x\mu$$

Utility

$$u(\mu, x, p) = x\mu + g(\mu, x) - p - T \cdot \mathbb{I}\{x = 0\}$$

- ▶ Even if buyers were risk neutral, they would transfer to the insurer the expected cost $x\mu$
- ▶ Risk aversion surplus $g(\mu, x)$
- ▶ Non-purchase fee $T \geq 0$
- ▶ We assume

$$\frac{\partial g}{\partial x} > 0, \quad \frac{\partial^2 g}{\partial x^2} < 0, \quad \frac{\partial g}{\partial \mu} \geq 0.$$

$$\text{and } g(\mu, 0) \equiv 0, \quad \frac{\partial g}{\partial x}(\mu, 1) \equiv 0$$

- ▶ Quasi-linearity in p consistent with CARA
- ▶ If $T > 0$, assume $\underline{x} > 0$ to preserve continuity

Timing

1. Regulator chooses $(\underline{x}, \bar{x}, T)$
2. Insurers compete and individuals make choices, with the outcome given by an AG equilibrium (described later)

Assumptions

- ▶ Quasi-linearity in p (no wealth effects)
- ▶ No insurance loads
- ▶ Exclusive contracts
- ▶ No moral hazard
 - ▶ but included in an extension

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AG Equilibrium, intuition

- ▶ Equilibrium concept from Azevedo Gottlieb 2017 (AG)
- ▶ Intuitively: in equilibrium
 - ▶ individuals optimize
 - ▶ each contract breaks even
 - ▶ the price of non-traded contracts is robust to small perturbations in the economy

AG Equilibrium, more formally

- ▶ An allocation α is a distribution on $\Theta \times X$
 - ▶ e.g, $\alpha(\{\mu, x\})$ is mass of types μ purchasing contract x
- ▶ A **weak equilibrium** is a price $p(x)$ and an allocation α such that
 - ▶ individuals choose x to maximize utility
 - ▶ each contract breaks even: $p(x) = x \cdot \mathbb{E}_\alpha[\mu \mid x]$
- ▶ Typically, there exist many weak equilibria
- ▶ An economy is a triple $[\Theta, X, f]$
- ▶ An **equilibrium** is the limit of a sequence of weak equilibria of perturbed economies, where there is a vanishing mass of “behavioral” zero-cost individuals who purchase every contract.

Theorem (AG)

Every economy has an equilibrium. In equilibrium, $p(x)$ is continuous and almost everywhere differentiable. Equilibrium need not be unique

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Equilibrium Regimes

- ▶ An equilibrium “regime” is defined by whether or not there a positive mass of individuals choosing x in...

$$x > \underline{x}, \quad x = \underline{x}, \quad x = 0$$

- ▶ EG, all equilibria where individuals buy $x \in \{0, \underline{x}\}$ have the same structure, uniqueness properties, etc

Some regimes are not possible

Lemma

In any equilibrium, if there is a mass of individuals choosing $x = 0$, then there is also a mass of individuals choosing $x = \underline{x}$.

Equilibrium regimes

Some choose $x > \underline{x}$	Some choose $x = \underline{x}$	Some choose $x = 0$	Regime
Y	Y	Y	Dispersive
Y	-	-	RS
-	Y	-	boring
-	-	Y	not possible
Y	Y	-	Perfect Purchase, Partial Pooling (PPPP)
-	Y	Y	Lemons
Y	-	Y	not possible

When does each regime happen?

- ▶ Some sufficient conditions:
 - ▶ If \underline{x} is sufficiently low \rightarrow RS
 - ▶ If $\bar{x} - \underline{x}$ is sufficiently small \rightarrow Lemons
- ▶ More conditions in the paper

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Dispersive Equilibrium

some buy

$$x > \underline{x}$$

some buy

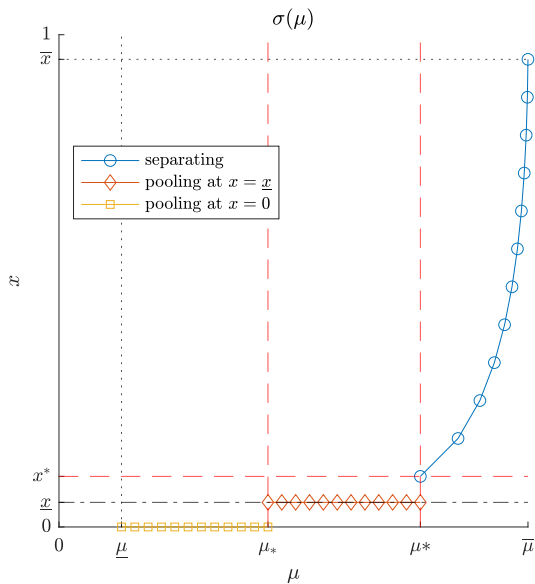
$$x = \underline{x}$$

some buy

$$x = 0$$

- ▶ Requires $\bar{x} > \underline{x} > 0$
- ▶ Let $\sigma(\mu)$ be the contract that type μ chooses (almost surely) in equilibrium.

Dispersive Equilibrium: graphically



Equilibrium characterization

Proposition (Dispersive Equilibrium)

1. *There is an $x^* \in [\underline{x}, \bar{x}]$ and a $\mu^* < \bar{\mu}$ such that types $\mu \in [\mu^*, \bar{\mu}]$ buy $x \in [x^*, \bar{x}]$. For these types, let $\tau = \sigma^{-1}$. Then, for these types, σ satisfies*

$$\bar{\mu} - \mu = \int_{\sigma(\mu)}^{\bar{x}} \frac{1}{x} \frac{\partial g}{\partial x}(\tau(x), x) dx, \quad \forall \mu \in [\mu^*, \bar{\mu}] \quad (1)$$

These contracts break even:

$$p(\sigma(\mu)) = \sigma(\mu)\mu, \quad \forall \mu \in [\mu^*, \bar{\mu}]$$

2. *For $x \in [\underline{x}, x^*)$, price $p(x)$ makes type μ^* indifferent between $(x^*, p(x^*))$ and any $(x, p(x))$*
3. *There is a $\mu_* \in (\underline{\mu}, \mu^*)$ such $\mu \in [\mu_*, \mu^*)$ buys $x = \underline{x}$. This contracts breaks even:*

$$p(\underline{x}) = \underline{x} \cdot \mathbb{E}[\mu \mid \mu \in [\mu_*, \mu^*)].$$

4. *Type μ_* is indifferent between $(\underline{x}, p(\underline{x}))$ and $(0, 0)$*
5. *Types $\mu \in [\underline{\mu}, \mu_*)$ purchase $x = 0$ and it breaks even: $p(0) = 0$.*

Intuition 1: shape of σ in the region of full separation

- ▶ Type $\bar{\mu}$ buys $x = \bar{x}$:
 - ▶ $p'(x) \leq \bar{\mu}$
 - ▶ For $x < \bar{x}$, for type $\bar{\mu}$, $\frac{\partial u}{\partial x} = \bar{\mu} + g'(\bar{\mu}, x) - p'(x) > 0$
- ▶ For types in the region of full separation, utility satisfies the FOC

$$\mu + \frac{\partial g}{\partial x}(\mu, x) - p'(x) = 0$$

- ▶ Price is differentiable (from AG), so

$$p'(x) = \tau(x) + x \cdot \tau'(x)$$

- ▶ Use $\mu = \tau(x)$. Combine these to get

$$\mu + \frac{\partial g}{\partial x}(\mu, x) - [\tau(x) + x \cdot \tau'(x)] = 0 \Leftrightarrow \tau'(x) = \frac{1}{x} \frac{\partial g}{\partial x}(\tau(x), x)$$

- ▶ Boundary condition $\bar{x} = \sigma(\bar{\mu})$. Integrating $\int_{\sigma}^{\bar{x}}$ yields the result

Corollary

Corollary

In the region of full separation, the allocation $\sigma(\mu)$ is independent of f, \underline{x}, T .

- ▶ (\underline{x}, T) affect μ^* , but not $\sigma(\mu)$
- ▶ \bar{x} does directly affect $\sigma(\mu)$
- ▶ In this region, things behave as in RS76

Intuition 2: Why is $x \in (\underline{x}, x^*)$ not purchased?

- ▶ Suppose the set of non-purchased contracts is small ($x^* \approx \underline{x}$)
- ▶ If indeed this was a dispersive equilibrium
 - ▶ type μ^* chooses x^* at a price $p = \mu^* x^*$
 - ▶ The price of \underline{x} is determined by all the types who choose \underline{x} , who are all less costly than μ^* .
- ▶ If μ^* switches to purchasing the minimum coverage, she obtains approximately the same level of coverage but a discretely lower price
→ a contradiction.

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- ▶ All individuals choose $x > \underline{x}$
- ▶ Everyone is in the region of full separation
- ▶ This is the equilibrium structure in RS76
- ▶ Sufficient condition: \underline{x} sufficiently small (indeed, in RS76, there is no minimum coverage)

RS, graphically

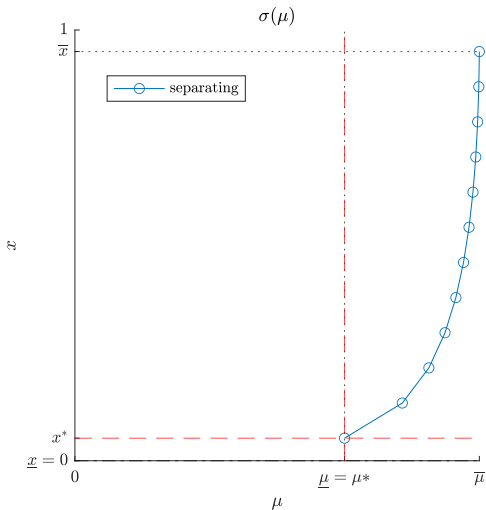


Figure 1: An illustration of an RS equilibrium (with $\underline{x} = 0$).

Proposition

If the equilibrium regime is RS, it is described by Proposition 1, with

$$\mu^* = \mu_* = \underline{\mu}$$

However, nobody buys the minimum coverage, so its price is not determined by the break-even condition (but by the indifference curve of type $\underline{\mu}$). Also, type $\underline{\mu}$ strictly prefers x^ to $x = 0$*

PPPP equilibrium

- ▶ All individuals choose $x > \underline{x}$ or $x = \underline{x}$
- ▶ Some individuals pool at the minimum coverage
- ▶ Tends to occur if T is large

PPPP, graphically

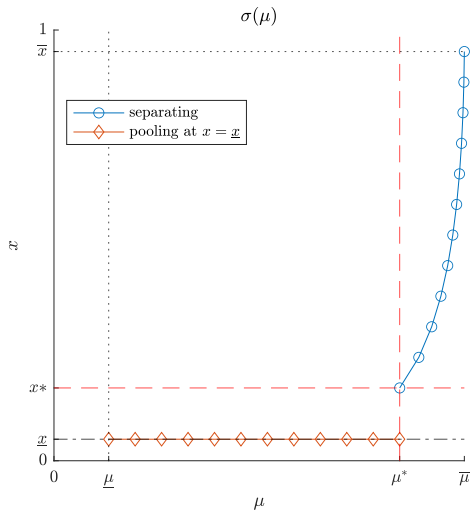


Figure 2: Illustration of a “PPPP” equilibrium.

PPPP equilibrium

Proposition

If the equilibrium regime is PPPP, it is described by Proposition 1, with

$$\mu_* = \underline{\mu}$$

Moreover, type $\underline{\mu}$ strictly prefers \underline{x} to zero.

Lemons equilibrium

- ▶ All individuals buy $x \in \{0, \underline{x}\}$
- ▶ No mass in the region of full separation
- ▶ As in Akerlof 1970 and EFC 2010
- ▶ Occurs if \bar{x}, \underline{x} sufficiently similar
- ▶ AG equilibria are Nash equilibria

Proposition

If the equilibrium regime is Lemons, it is described by Proposition 1, with

$$\mu^* = \bar{\mu}.$$

Since there is no one in the region of full separation, (1) is vacuous.

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Uniqueness

- ▶ If the regime is RS, it is unique
- ▶ If the regime is PPP, it is the unique PPP equilibrium

Proposition

If f is log-concave, equilibrium is unique.

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Comparative Statics

- ▶ Consider small changes in $(\underline{x}, \bar{x}, T)$
- ▶ Assume f log-concave. This will be used in two ways:
 - ▶ uniqueness
 - ▶ sign some effects
- ▶ For tractability, henceforth assume $g(\mu, x) = g(x), \forall \mu$

Welfare

- Welfare is

$$W = [F(\mu^*) - F(\mu_*)]g(\underline{x}) + \int_{\mu^*}^{\bar{\mu}} g(\sigma(\mu))f(\mu)d\mu.$$

First Best

- ▶ First best: everyone buys full insurance
- ▶ Achievable with $T = \infty$ and $\underline{x} = \bar{x} = 1$
- ▶ Two potential problems:
 - ▶ politically difficult
 - ▶ suppose that instead of a tax on non-buyers there is a subsidy to buyers. Government must subsidize all individuals to buy. If there is a shadow cost of public funds, “full insurance for all” is not socially optimal (because $g'(1) = 0$)

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Adjusting T

- ▶ RS, PPPP: nobody choosing $x = 0$, so changes in T have no effect
- ▶ Lemons: increasing T shifts some non-buyers into buying \rightarrow increases W

Adjusting T

Lemma

If the regime is dispersive, and f log-concave,

$$\frac{\partial \mu_*}{\partial T} < 0, \quad \frac{\partial \mu^*}{\partial T} > 0.$$

1. T increases \rightarrow type μ_* shifts from $x = 0$ to $x = \underline{x}$
 2. This lowers $p(\underline{x})$
 3. Type μ^* shifts from $x = x^*$ to $x = \underline{x}$
 4. This raises $p(\underline{x})$. f log-concave signs the overall effect
- Welfare:
- rises proportionately to $f(\mu_*)(g(\underline{x}) - 0)$
 - falls proportionately to $f(\mu^*)(g(x^*) - g(\underline{x}))$

Adjusting T

Proposition

If the regime is dispersive with thresholds μ_, μ^* then*

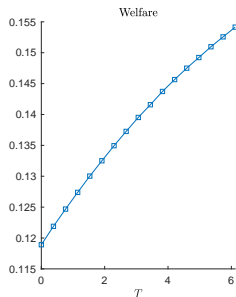
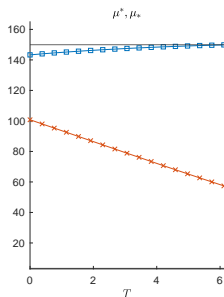
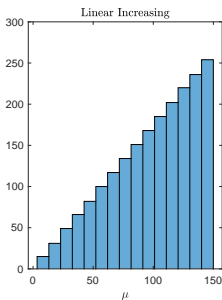
$$f(\mu_*) \geq f(\mu^*) \Rightarrow \frac{\partial W}{\partial T} > 0.$$

If f is weakly decreasing for all μ , then

$$\frac{\partial W}{\partial T} > 0, \forall T.$$

Adjusting T

- Condition is sufficient but not necessary:



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Adjusting \bar{x}

- ▶ Increasing \bar{x} (weakly) increases welfare if f log-concave
- ▶ Lemons: no effect
- ▶ RS / PPPP: welfare obviously increases (for any f)

Adjusting \bar{x}

Proposition

For dispersive equilibria, if f is log-concave,

$$\frac{\partial W}{\partial \bar{x}} > 0.$$

- ▶ Type $\bar{\mu}$ purchases greater coverage
- ▶ In the region of full separation, types $\mu > \mu^*$ purchase greater coverage
- ▶ Some individuals switch from \underline{x} to $x > \underline{x}$, which lowers $p(\underline{x})$
- ▶ Some individuals switch from 0 to \underline{x} , which also lowers $p(\underline{x})$
- ▶ Log-concavity: the fall in $p(\underline{x})$ does not cause too many of those who switched up from \underline{x} to $x > \underline{x}$ to “fall back down”

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Ambiguity

- ▶ Positive effects
 - ▶ When \underline{x} rises, those purchasing it become better off
 - ▶ This can induce some to raise their chosen coverage from 0 to \underline{x}
- ▶ Negative effects
 - ▶ Possibly some buyers of $x > \underline{x}$ now lower their choice to \underline{x}
 - ▶ This would increase $p(\underline{x})$, so it can also result in some individuals lowering their choice from \underline{x} to 0.

Optimal \underline{x} is > 0

- ▶ There is always a (small) level of \underline{x} which strictly increases welfare.
- ▶ Suppose $\underline{x} = 0$, so regime is RS
- ▶ Now consider a gradual increase in \underline{x}
- ▶ For some level of the minimum coverage (denoted \underline{x}_0), the equilibrium regime shifts from RS to PPPP.
 - ▶ why to PPPP? individuals cannot pool at $x = 0$ without pooling at $x = \underline{x}$
 - ▶ \underline{x}_0 solves $\bar{\mu} - \underline{\mu} = \int_{\underline{x}_0}^{\bar{x}} \frac{g(x)}{x} dx$.
- ▶ When $\underline{x} \approx \underline{x}_0$, then $x^* \approx \underline{x}_0$ and $\mu^* \approx \underline{\mu}$

Proposition

We have $\lim_{\underline{x} \rightarrow \underline{x}_0} \frac{\partial W}{\partial \underline{x}} = 0$ and $\lim_{\underline{x} \rightarrow \underline{x}_0} \frac{\partial^2 W}{\partial \underline{x}^2} = 0$. However, in a right-neighborhood of \underline{x}_0 ,

$$\frac{\partial^3 W}{\partial \underline{x}^3} > 0$$

and hence, in a right neighborhood of \underline{x}_0 , W is strictly increasing in \underline{x} .

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Adjusting \underline{x}

Lemma

If the equilibrium regime is Lemons, and f is log-concave, then

$$\frac{\partial \mu_*}{\partial \underline{x}} > 0, \forall \underline{x} < 1.$$

- ▶ Higher coverage \underline{x} (and the corresponding adjustment in price) shrinks the set of buyers due to adverse selection: the cost of infra-marginal types (i.e., $p(\underline{x})$) increases faster than the willingness to pay of marginal types

Adjusting \underline{x}

social planner's welfare maximizing choice of quantity \approx monopolists's profit maximizing choice of quantity

- ▶ Let quantity be $q(\underline{x}) = 1 - F(\mu_*(\underline{x}))$
- ▶ Then

$$\frac{\partial \underline{x}}{\partial q} = - \left(f(\mu_*) \frac{\partial \mu_*}{\partial \underline{x}} \right)^{-1} \leq 0.$$

Welfare

- ▶ Welfare is

$$W = q \cdot g(\underline{x}(q))$$

- ▶ Surplus $g(\underline{x}(q))$ behaves like an inverse demand function.
- ▶ FOC:

$$\frac{\partial W}{\partial q} = g(\underline{x}(q)) + q \cdot g'(\underline{x}(q)) \frac{d\underline{x}}{dq} = 0 \quad (2)$$

- ▶ Selling insurance to another marginal individual entails:
 - ▶ marginal gains: surplus of the marginal individual, $g(\underline{x}(q))$
 - ▶ infra-marginal losses: increasing q requires lowering the \underline{x} enjoyed by all q infra-marginal individuals: surplus falls proportionally to $q \cdot g'(\underline{x}(q))$

Optimal \underline{x} is < 1

- ▶ We've seen that it is optimal to choose $\bar{x} = 1$
- ▶ What is the optimal level of \underline{x} ? We know it is $> \underline{x}_0 \dots$
 - ▶ Is $\underline{x} = 1$ optimal?
 - ▶ Yes, if everyone buying full insurance is an equilibrium.
 - ▶ Suppose it is not (e.g., T cannot be set high enough)
 - ▶ Then, if $\underline{x} = \bar{x} = 1$, the equilibrium regime is Lemons.
 - ▶ We show that this is not optimal

Optimal \underline{x} is < 1

Proposition

If $\bar{x} = 1$, then

$$\frac{dW}{dq} \Big|_{\underline{x}=1} > 0 \quad \text{and} \quad \frac{dW}{d\bar{x}} \Big|_{\underline{x}=1} < 0$$

if and only if all individuals buying $\underline{x} = 1$ is not an equilibrium.

- ▶ At full insurance
 - ▶ marginal surplus from additional insurance vanishes, since $g'(1) = 0$
 - ▶ marginal lowering of q due to adverse selection does not
- ▶ Optimal minimum coverage is greater than \underline{x}_0 but below full insurance

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Moral Hazard (MH)

- ▶ MH = insurer cost increases disproportionately with coverage x
 - ▶ Eg, individuals use more healthcare when they receive better insurance, especially high-cost individuals
- ▶ Key question: in the presence of MH, can there be OVER-insurance in equilibrium?
 - ▶ if so, this would be a reason to impose $\bar{x} < 1$

Modeling MH

- Utility and cost are now

$$u(\mu, x, p) = \mu x + g(x) + w(\mu, x) - p, \quad c(\mu, x) = \mu x + k(\mu, x).$$

Assumption

$w(\cdot), k(\cdot)$ are twice continuously differentiable, increasing in μ and strictly increasing in x , with $k(, 0) \equiv w(, 0) \equiv 0$.

We assume $\frac{\partial k}{\partial x}(\mu, x) > \frac{\partial w}{\partial x}(\mu, x) > 0, \forall x > 0$ and $\forall \mu$.

Moreover,

$$\frac{\partial^2 k}{\partial x^2}(\mu, x) \geq \frac{\partial^2 w}{\partial x^2}(\mu, x), \quad \frac{\partial^2 k}{\partial \mu \partial x}(\mu, x) \geq \frac{\partial^2 w}{\partial \mu \partial x}(\mu, x).$$

- The wedge $k(\mu, x) - w(\mu, x)$ is increasing concave in x and increases more quickly in x for higher μ

Social Surplus

- Social surplus is

$$s(\mu, x) = g(x) + w(\mu, x) - k(\mu, x).$$

Equilibrium

Proposition

Suppose $X = [0, \bar{x}]$ and MH is present. There is a unique equilibrium. Either no individual purchases, or all purchase positive coverage as follows:

- 1. There is a cut-off coverage $x^* \in (0, \bar{x})$ and a maximal purchased coverage $\tilde{x} \in (x^*, \bar{x}]$, s.t. all types purchase contracts $x \in [x^*, \tilde{x}]$ and all such contracts are purchased.*
- 2. Type $\bar{\mu}$ buys the maximal purchased coverage \tilde{x}*
- 3. The allocation rule σ is strictly increasing and $\sigma \leq \tilde{x}$. Let $\tau = \sigma^{-1}$ be defined on $x \in [x^*, \tilde{x}]$. Then,*

$$\tau'(x) = \frac{1}{x + \frac{\partial k}{\partial \mu}(\tau(x), x)} \frac{\partial s}{\partial x}(\tau(x), x), \quad \forall x \in (x^*, \tilde{x}) \quad (3)$$

- 4. Each contract breaks even: $p(x) = c(\tau(x), x), \forall x \in [x^*, \tilde{x}]$.*

What is the maximal purchased coverage \tilde{x} ?

Proposition

In equilibrium, $\tilde{x} = \bar{x}$ if

$$\frac{\partial s}{\partial x}(\bar{\mu}, \bar{x}) \geq 0.$$

If $\tilde{x} < \bar{x}$, then \tilde{x} satisfies

$$\frac{\partial s}{\partial x}(\bar{\mu}, \tilde{x}) = 0.$$

- ▶ If information was symmetric, each type would obtain coverage such that $\frac{\partial s}{\partial x} = 0$
- ▶ Asymmetric information: coverage chosen by low risks distorted downwards but “no distortion at the top”

MH reduces equilibrium coverage

Corollary

Suppose $X = [0, \bar{x}]$. All else equal, for each type μ , equilibrium coverage is (weakly) higher if $w(\cdot) \equiv k(\cdot) \equiv 0$ than in a model with MH.

- ▶ But, under MH, the optimal amount of coverage is also lower

Excessive insurance?

- ▶ Let $x^{**}(\mu)$ be the coverage that maximizes surplus for type μ

Lemma

*If $x^{**}(\mu) > 0$, it is the unique value that satisfies*

$$\frac{\partial s}{\partial x}(\mu, x^{**}(\mu)) = 0. \quad (4)$$

*Moreover, $x^{**}(\mu) < 1$, and $x^{**}(\cdot)$ it is weakly decreasing in μ .*

- ▶ Full insurance is not optimal for any individual
- ▶ The optimal coverage is lower for higher cost types

Excessive insurance?

Proposition

In equilibrium, every type $\mu < \bar{\mu}$ obtains coverage that is strictly lower than what is socially optimal. Full insurance $\bar{x} = 1$ is not purchased even if it is offered.

- ▶ At most, type $\bar{\mu}$ buys \tilde{x} which is optimal for that type
- ▶ Equilibrium coverage is increasing in type
- ▶ Socially optimal coverage is decreasing in type
- ▶ MH leads to UNDER-insurance in equilibrium for every type (except perhaps $\bar{\mu}$)

Proposition

Suppose that $X = [0, \bar{x}]$, and MH is present. Suppose that, in equilibrium, positive coverage is purchased by all. If $\bar{x} > \tilde{x}$, then $\frac{\partial W}{\partial \bar{x}} = 0$. If $\tilde{x} = \bar{x}$, then $\frac{\partial W}{\partial \bar{x}} > 0$.

- ▶ The presence of MH does not provide a rational for $\bar{x} < 1$
 - ▶ best case scenario ($\bar{x} > \tilde{x}$): does not affect welfare.
 - ▶ if $\tilde{x} \geq \bar{x}$, then it reduces welfare.

Roadmap

- 1 Motivation
- 2 Model
- 3 Equilibrium
- 4 Possible Equilibrium Regimes
- 5 Equilibrium Characterization
 - Dispersive Equilibrium
 - Other Regimes
- 6 Uniqueness
- 7 Comparative Statics
 - Adjusting T
 - Adjusting \bar{x}
 - Adjusting \underline{x} , PPPP Regime
 - Adjusting \underline{x} , Lemons Regime
- 8 Moral Hazard
- 9 Conclusion

- ▶ Tractable model of a competitive selection market
 - ▶ includes common contract restrictions
 - ▶ nests, as special cases, Akerlof 1970 and RS76
- ▶ Equilibrium typically exhibits partial pooling
 - ▶ depends non-trivially on the type distribution (unlike in RS)
- ▶ Equilibrium is unique if the type distribution is log-concave.
- ▶ Increasing the non-purchase fee increases welfare if the density of types is decreasing.
- ▶ The optimal level of the minimum coverage is positive, below full insurance and induces some pooling at the minimum coverage contract.
- ▶ The optimal level of the maximum coverage is full insurance (even in an extension that allows for moral hazard).

THANK YOU!

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