

What to do  
when the  
world splits in  
two

Andrew  
Bacon

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time and  
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# What to do when the world splits in two

Andrew Bacon

Oxford University

January 25, 2010

- 1 Introduction
- 2 Self-locating uncertainty
- 3 Branching time and indeterminacy
- 4 Vagueness and uncertainty
- 5 Decision theoretic formulation indifference

## What to do when the world splits in two

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## Introduction

## 1 Introduction

## What to do when the world splits in two

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## Introduction

- Decision problem from the film “The Prestige”

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  - Choice 1: get into duplication machine. One of your duplicates becomes rich magician, other dies horrible death in a tank of water.

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  - Choice 2: don’t get into machine. remain not so good magician.

- Decision problem from the film “The Prestige”
  - Choice 1: get into duplication machine. One of your duplicates becomes rich magician, other dies horrible death in a tank of water.
  - Choice 2: don’t get into machine. remain not so good magician.
- Prudential rationality. Angier doesn’t care if someone dies unless it’s him.

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## Introduction

- Was Angier's decision rational?



- Was Angier's decision rational?
- How should decisions of this shape be made?

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- Was Angier's decision rational?
- How should decisions of this shape be made?
- Should Angier be uncertain, before he gets into the machine, whether he'll end up at the other end of the stage, or drowning in a tank?

- Was Angier's decision rational?
- How should decisions of this shape be made?
- Should Angier be uncertain, before he gets into the machine, whether he'll end up at the other end of the stage, or drowning in a tank?
- Applications to the literature on Everettian quantum mechanics.

# No uncertainty

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- Should Angier be uncertain?

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- Should Angier be uncertain?
  - Hard to make sense of this uncertainty: Angier knows all the objective facts.

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- Should Angier be uncertain?
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- Maximin

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- Maximin
  - Counterexample.

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- Maximin
  - Counterexample.
- Minimax regret
  - Violates dominance

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## 2 Self-locating uncertainty

# Uncertainty

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- The challenge, then, is to make sense of uncertainty in scenarios like Ruperts, where one knows all the 'objective facts'.

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- The approach of Saunders and Wallace combines the following two ideas

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- The challenge, then, is to make sense of uncertainty in scenarios like Ruperts, where one knows all the 'objective facts'.
- The approach of Saunders and Wallace combines the following two ideas
  - A Lewisian approach to the metaphysics of persistence, worms, and personal fission. (This characterisation is near enough for our purposes.)

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- The approach of Saunders and Wallace combines the following two ideas
  - A Lewisian approach to the metaphysics of persistence, worms, and personal fission. (This characterisation is near enough for our purposes.)
  - The idea that one can have irreducibly self-locating uncertainty, even if one knows all the facts (in the sense that one knows exactly which possible world one inhabits.)

# Problems

- 1 Suppose, instead of drowning, Rupert's second duplicate is instantaneously obliterated.

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- 1 Suppose, instead of drowning, Rupert's second duplicate is instantaneously obliterated.
  - There is only one worm: should he then be certain that he won't be obliterated, and end up at the other end of the stage?
- 2 Secondly, we could give up on Lewisian metaphysics and go for life long colocated people.

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- 2 Secondly, we could give up on Lewisian metaphysics and go for life long colocated people.
  - But a second worry comes up: this account potentially creates too much uncertainty, for example if there are many different objects colocated with me with different modal profiles (for statue lump type reasons.)

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  - But a second worry comes up: this account potentially creates too much uncertainty, for example if there are many different objects colocated with me with different modal profiles (for statue lump type reasons.)
- 3 (Williams): To have a complete story of uncertainty we need to account for uncertainty about things that might happen long after I cease to exist - it is hard to see how being uncertain which branch I am located in can generate this, since that uncertainty can only be responsible for uncertainty in events up until my death.

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- S+W's ultimate project is to set the foundations for a decision theoretic derivation of the Born rule for EQM.

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- S+W's ultimate project is to set the foundations for a decision theoretic derivation of the Born rule for EQM.
- This requires **Measurement Neutrality**. This principle is equivalent to saying that you should set your credence's according to the Born rule (against the background of an appropriate Savage style decision theory.)

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- This requires **Measurement Neutrality**. This principle is equivalent to saying that you should set your credence's according to the Born rule (against the background of an appropriate Savage style decision theory.)
- Ignoring the details, MN implies we must have situations where we assign successors different probabilities or the project won't get off the ground. [Draw a picture.]

# The principle of indifference

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“Dear Sir,  
(Forgive the impersonal nature of this communication – our purpose prevents us from addressing you by name.)  
We have just created a duplicate of Dr. Evil. The duplicate – call him ‘Dup’ – is inhabiting a replica of Dr. Evil’s battlestation that we have installed in our skepticism lab. At each moment Dup has experiences indistinguishable from those of Dr. Evil. For example, at this moment both Dr. Evil and Dup are reading this message. We are in control of Dup’s environment. If in the next ten minutes Dup performs actions that correspond to deactivating the battlestation and surrendering, we will treat him well. Otherwise we will torture him.  
Best regards, The PDF”

# Elga's principle of indifference

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- Elga proposes the following principle



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- Elga proposes the following principle
- Call two centred worlds **similar** iff they have the same world coordinate, and the person coordinate's are in subjectively indistinguishable states. (I.e. have the same memories, are receiving the same sensory stimulus etc etc.)

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- **Self-locating Indifference** You should distribute your credence's equally over similar centred worlds.

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- Elga proposes the following principle
- Call two centred worlds **similar** iff they have the same world coordinate, and the person coordinate's are in subjectively indistinguishable states. (I.e. have the same memories, are receiving the same sensory stimulus etc etc.)
- **Self-locating Indifference** You should distribute your credence's equally over similar centred worlds.
- (In particular, if you are certain that you are in one of two centred worlds, like we may suppose Dr. Evil is, you should give credence  $\frac{1}{2}$  to each.)

# Problem

- The problem is: the pre-fission worms, at  $t$ , have identical  $t$ -slices - which means their internal mental states must be identical.

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- The problem is: the pre-fission worms, at  $t$ , have identical  $t$ -slices - which means their internal mental states must be identical.
- Also, they are part of the same possible world - the two centred worlds are *similar* in Elga's terminology.

# Problem

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- Thus in the two branch scenario you must distribute your credence's equally over being the right and the left branch, violating measurement neutrality.

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- Note: it might be vague how many duplicates there are (due to vagueness in the decoherence basis.)

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- Also, they are part of the same possible world - the two centred worlds are *similar* in Elga's terminology.
- Thus in the two branch scenario you must distribute your credence's equally over being the right and the left branch, violating measurement neutrality.
- Note: it might be vague how many duplicates there are (due to vagueness in the decoherence basis.)
- But in most cases, it'll be supertrue that you ought not set your credence's according to the Born rule. (E.g. if the mod amplitude squared is an irrational number. Elga's principle never recommends an irrational credence.)



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- The proposal: the uncertainty in question exists because you are certain that it's indeterminate whether when you measure  $x$ -spin you'll get up or down.

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- The proposal: the uncertainty in question exists because you are certain that it's indeterminate whether when you measure  $x$ -spin you'll get up or down.
- The claim: you may know exactly which possible world you inhabit, and even know exactly where you are located in that world and yet still be uncertain about some things.

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- The proposal: the uncertainty in question exists because you are certain that it's indeterminate whether when you measure  $x$ -spin you'll get up or down.
- The claim: you may know exactly which possible world you inhabit, and even know exactly where you are located in that world and yet still be uncertain about some things.
- In particular, suppose you can see that Cedric is clearly bordering on the bald. Even if you know all the relevant facts (such as how many hairs he has on his head, how people use the term 'bald', etc...) you can still be uncertain whether Cedric is bald.

# How does indeterminacy come about?

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- Indeterminacy comes about when there are multiple equally good candidate interpretations of our language.

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- Indeterminacy comes about when there are multiple equally good candidate interpretations of our language.
- A world where time is branching, but the language users speak as if there were exactly one branch seems like a world where there are many good candidate interpretations for the language: each a linear branch.

# Preserving the logic

- Supervaluationism about vagueness keeps the logic fixed. For example the law of excluded middle is valid.

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# Preserving the logic

- Supervaluationism about vagueness keeps the logic fixed. For example the law of excluded middle is valid.
  - Famously, it allows you to keep classical logic, and still have truth value gaps.

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  - But there's nothing special about classical logic - you could have intuitionistic precisifications, or 3-valued precisifications, etc...

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  - The logic imposes constraints on what the interpretations must look like.

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- Notice that English seems to have a tense logic of linear time:

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- Notice that English seems to have a tense logic of linear time:
  - $\triangleleft \triangleright p \rightarrow (\triangleleft p \vee p \vee \triangleright p)$

# Frames, branches, models

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## Definition

A **frame** is a partial order  $\langle P, \leq \rangle$

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## Definition

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## Definition

Given a frame,  $\langle P, \leq \rangle$ , the set of **branches** over that frame is  $\mathcal{B} := \{b \mid b \text{ is a maximal chain in } \langle P, \leq \rangle\}$ . (Requires Choice.)

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## Definition

A **model** is a triple  $\langle P, \leq, V \rangle$ , where  $\langle P, \leq \rangle$  is a frame, and  $V : \mathcal{SL} \times P \times \mathcal{B} \rightarrow 2$ .

# Truth

- We define truth at a model  $\mathcal{M}$  with respect to a branch and a time in that branch as follows:

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# Truth

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- $\mathcal{M}, b, t \models \triangleright \phi$  iff there is a  $t' \in b$  such that  $t < t'$  and  $\mathcal{M}, b, t' \models \phi$

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- The clauses for  $\neg$ ,  $\wedge$ ,  $\vee$ ,  $\rightarrow$  and sentence letters are standard.
- A sentence is **supertrue** in  $\mathcal{M}$  at a time  $t$  iff  $\mathcal{M}, b, t \models \phi$  for every branch  $b$  such that  $t \in b$ .

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- Logic:  $\triangleleft \triangleright p \rightarrow (\triangleleft p \vee p \vee \triangleright p)$  is supertrue in every model at every time. (It's valid.)

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- Indifference: there is no self locating uncertainty when (it's supertrue that) there's only one person worm.

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- Obliteration: on one branch I get obliterated, on another I live on so it's indeterminate whether I get obliterated. So I should be uncertain whether I'll get obliterated.



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- Obliteration: on one branch I get obliterated, on another I live on so it's indeterminate whether I get obliterated. So I should be uncertain whether I'll get obliterated.
- Uncertainty about the distant future: the uncertainty due to indeterminacy has nothing to do with the length of your worms. Will still be indeterminate whether robots take over the earth, whether we live long enough to see it or not.

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# Vagueness and uncertainty

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- Suppose you know everything there is to know that's relevant to whether Cedric is bald: how many hairs he has, their distribution, colour, etc... and suppose you're certain he's a borderline case of baldness. Suppose, in fact, that you're omniscient, in the sense that you know exactly which possible world you inhabit.

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- Should you be uncertain about whether Cedric is bald?

# Some other views

- Epistemicism: you should be certain once you have learnt all the facts about how language is used.

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- Epistemicism: you should be certain once you have learnt all the facts about how language is used.
- Field: your credence in  $p$  and in  $\neg p$  should drop to 0.

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- Dorr: if you know all the relevant facts, and  $p$  is vague, then it will be indeterminate whether you know  $p$  (but supertrue that you're not ignorant/uncertain.)

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- Dorr: if you know all the relevant facts, and  $p$  is vague, then it will be indeterminate whether you know  $p$  (but supertrue that you're not ignorant/uncertain.)
- Schiffer: you end up in some *sui generis* state, which is somehow not the same as uncertainty.



# Rational behaviour

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- Someone who is certain that it is vague whether Cedric is bald will typically act *as if* they were uncertain about  $p$ :

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- Someone who is certain that it is vague whether Cedric is bald will typically act *as if* they were uncertain about  $p$ :
  - Won't accept or reject  $p$ , if queried.

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- Someone who is certain that it is vague whether Cedric is bald will typically act *as if* they were uncertain about  $p$ :
  - Won't accept or reject  $p$ , if queried.
  - Won't be willing to assert or deny  $p$ .

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  - Won't accept or reject  $p$ , if queried.
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  - Won't be willing to accept bets with high odds for  $p$ , or against  $p$ .

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- Premise: intuitively this behaviour is appropriate in the situation.

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  - Won't accept or reject  $p$ , if queried.
  - Won't be willing to assert or deny  $p$ .
  - Won't be willing to accept bets with high odds for  $p$ , or against  $p$ .
- Premise: intuitively this behaviour is appropriate in the situation.
- Premise: intuitively, this kind of behaviour is only ever appropriate when you are uncertain about  $p$ .

# Comparative judgements of uncertainty

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- Suppose you see two greeny/bluey patches.

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- Suppose you see two greeny/bluey patches.
  - They're both clearly borderline green.



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- Suppose you see two greeny/bluey patches.
  - They're both clearly borderline green.
  - The second one is greener than the other.

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- Suppose you see two greeny/bluey patches.
  - They're both clearly borderline green.
  - The second one is greener than the other.
  - You should be more sure the second one is green, than the first one.

# Comparative judgements of uncertainty

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- Suppose you see two greeny/bluey patches.
  - They're both clearly borderline green.
  - The second one is greener than the other.
  - You should be more sure the second one is green, than the first one.
- You should be at least as certain that the patch is green or Cedric is bald, than you are that the patch is green.

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- Suppose you pick a ball out of a bag containing 10 marbles: 9 are clearly red, one of them is borderline red.

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- Suppose you pick a ball out of a bag containing 10 marbles: 9 are clearly red, one of them is borderline red.
- You're holding a marble but you have not yet looked: what's your credence that you're holding a red marble?

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- Suppose you pick a ball out of a bag containing 10 marbles: 9 are clearly red, one of them is borderline red.
- You're holding a marble but you have not yet looked: what's your credence that you're holding a red marble?
- Should be between 90% and 100%.

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- Stipulate that  $n$  denotes the largest small number modulo 100 (i.e. the last two digits of the largest small number.)

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- Stipulate that  $n$  denotes the largest small number modulo 100 (i.e. the last two digits of the largest small number.)
  - $n$  is a vague name.



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- Stipulate that  $n$  denotes the largest small number modulo 100 (i.e. the last two digits of the largest small number.)
  - $n$  is a vague name.
  - It's supertrue that:  $0 \leq n \leq 99$

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- Stipulate that  $n$  denotes the largest small number modulo 100 (i.e. the last two digits of the largest small number.)
  - $n$  is a vague name.
  - It's supertrue that:  $0 \leq n \leq 99$
  - For each  $0 \leq k \leq 99$  it is vague whether  $n = k$  (assuming there are at least 100 borderline cases of smallness.)

# Mixed uncertainty

- Suppose you have 100 balls in a bag numbered from 0 to 99 and you have just picked one but have not yet looked at it's number.

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- Suppose you have 100 balls in a bag numbered from 0 to 99 and you have just picked one but have not yet looked at it's number.
- By the reasoning on the last slide you are certain that it is vague whether I am holding the  $n$ th ball.

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- By the reasoning on the last slide you are certain that it is vague whether I am holding the  $n$ th ball.
- What should your credence be that you are not holding the  $n$ th ball?
- Surely you should be 99% sure! It's (determinately) true that there are 99 marbles which aren't the  $n$ th ball, and only one which is.

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- By the reasoning on the last slide you are certain that it is vague whether I am holding the  $n$ th ball.
- What should your credence be that you are not holding the  $n$ th ball?
- Surely you should be 99% sure! It's (determinately) true that there are 99 marbles which aren't the  $n$ th ball, and only one which is.
- (Contrast: Field predicts it should be 0%).

# Uncertainty and ersatz uncertainty

- Consider a Sorites sequence:

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- Consider a Sorites sequence:
  - My credence that  $n$  is small is an 'ordinary' credence.

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- Consider a Sorites sequence:
  - My credence that  $n$  is small is an 'ordinary' credence.
  - If my credence that  $n$  is small is an ordinary credence my credence that  $n + 1$  is small is an ordinary credence.

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- Consider a Sorites sequence:
  - My credence that  $n$  is small is an 'ordinary' credence.
  - If my credence that  $n$  is small is an ordinary credence my credence that  $n + 1$  is small is an ordinary credence.
- Upshot: if we are to deny that in vague cases you ought to have ordinary credence's, you must allow there to be cases where it is vague whether your credence is an ordinary one, or a weird vagueness related one.

# Uncertainty and ersatz uncertainty

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  - If my credence that  $n$  is small is an ordinary credence my credence that  $n + 1$  is small is an ordinary credence.
- Upshot: if we are to deny that in vague cases you ought to have ordinary credence's, you must allow there to be cases where it is vague whether your credence is an ordinary one, or a weird vagueness related one.
- But it seems like vagueness over whether something is  $F$  or  $G$  only arises when  $F$  and  $G$  are very 'close'. (Like being red, and being orange - not like being red and being fluorescent green.) So vagueness related uncertainty must be 'close' to ordinary uncertainty.

# Functionalism

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- Uncertainty is just whatever fills the uncertainty role.

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- Naïve functionalism:  $Cr$  is just whatever satisfies the equation above.
- Representation theorems: if your desires are well behaved,  $Cr$  should be a probability function (and it's unique.)

# Bets and borderline cases

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- It seems that the conditions required for the representation theorems retain intuitive appeal in settings involving vagueness. For example

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- Dominance appears to explain our intuitions about about finding it more likely that the greener patch is green.
- But would you prefer a bet on the second patch being green over the first?

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- The problem is, it's hard to find cases where you're certain the person offering the bet is such that it is determinately the case that [they'll pay up iff you bet on the second patch being green.]

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- Suggestion. Suppose the person offering me the bet will write in their will: 'Andrew will get £100 iff the patch is green.' if I take the bet.



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- Suppose that legally, when they die, it will be indeterminate whether I own the £100 or the state does.
- Suppose all I care about is owning money.

# Caring about being green

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- Suppose I care intrinsically about owning green things. I'm offered a choice between being given the first borderline green patch and the second (greener) borderline green patch.

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- Suppose I care intrinsically about owning green things. I'm offered a choice between being given the first borderline green patch and the second (greener) borderline green patch.
- Every precisification that makes the first patch green makes the second patch green, but some precisifications make the second patch green but not the first.

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- Every precisification that makes the first patch green makes the second patch green, but some precisifications make the second patch green but not the first.
- Here it seems like dominance kicks in: I should go for the greener borderline green patch.

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# Preference indifference

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If this principle is remotely plausible then we have a problem for the decision theoretic defence of the Born rule.



# Branching Newcomb scenarios

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**picture** ■ Suppose that choosing *A* involves pressing a button that connects a circuit that drops £100 into the left box.

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- Suppose that choosing  $A$  involves pressing a button that connects a circuit that drops £100 into the left box.
- suppose that choosing  $B$  involves pressing a dummy button - it does nothing. However, an infallible predictor has put £100 in the right box just in case she's predicted you'll choose  $B$ .

# Branching Newcomb scenarios

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- suppose that choosing  $B$  involves pressing a dummy button - it does nothing. However, an infallible predictor has put £100 in the right box just in case she's predicted you'll choose  $B$ .
- My two boxer intuitions say I should definitely prefer  $A$  to  $B$ , thus violating preference indifference.

# Tentative thought

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- Perhaps branch weight is just a measure of how much causal influence your current actions have on what happens in the succeeding branches.