

Built-In Data Structures

Array based list

C++: `std::vector`

Java: `ArrayList`

Python: `list`

Add element at end: amortized $O(1)$

Delete last element: $O(1)$

Access element by index: $O(1)$

Insert element at arbitrary position: $O(N)$

Delete element at arbitrary position: $O(N)$

Amortized complexity

“Insert operation is amortized $O(f(n))$ ” means it takes $O(M \cdot f(n))$ time to perform M insert operations in total (in this case since the array is created).

It is necessary to say that it's amortized $O(1)$ and not simply $O(1)$ because a single operation could be $O(N)$ if the array size needs to be doubled.

Sorted array based list

Construct from an unsorted list: $O(N \log N)$

Insert element: $O(N)$

Access element by value: $O(\log(N))$

Delete element: $O(N)$

Linked list

C++: `std::list`

Java: `LinkedList`

Python: doesn't exist

Access element by index: $O(N)$

Add element at start, end, or before/after a known element: $O(1)$

Unordered set

C++: `std::unordered_set`

Java: `HashSet`

Python: `set`

Insert element: amortized $O(1)$

Access element by value: $O(1)$

Delete element: $O(1)$

Hashing

A hash function is a function that:

- Takes in some input
- Returns a fixed size integer
- Is deterministic (always returns the same output for a given input)
- Tries to “scramble” the input. Ideally, the output should appear random (other than the fact that the same input always gives the same output) and should not be feasible to reverse (if you know the output of a hash function there should be no easy way to determine its input)

Examples of hash functions:

https://en.wikipedia.org/wiki/Hash_function#Hashing_integer_data_types

Problems

Some introductory problems:

<https://dmoj.ca/problem/ccc18j2>

<https://dmoj.ca/problem/ccc15j3>

<https://dmoj.ca/problem/ccc18s2>

<https://dmoj.ca/problem/ioi94p1>

Some problems more relevant to today's lesson:

<https://dmoj.ca/problem/ccc08s2>

<https://dmoj.ca/problem/ccc22s2>

<https://dmoj.ca/problem/valentines19s2>