

# Question 4: Volatility Comparison

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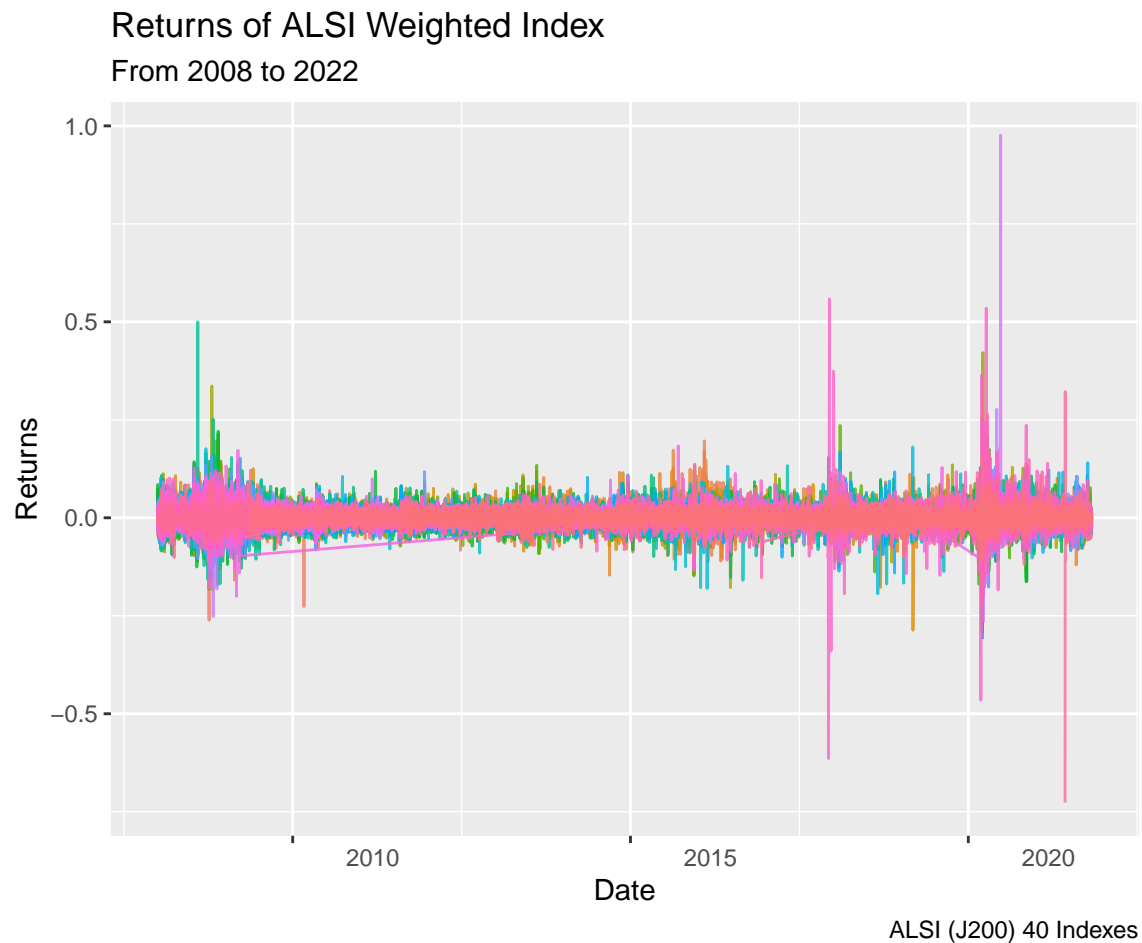
2022-11-26

## Introduction

In this section I run a Principal Component Analysis to understand the concentration and commonality of returns within the Top 40 indexes.

## Data

I begin testing the data for missing values (NA) and then plotting the data to see if there are any significant outliers.

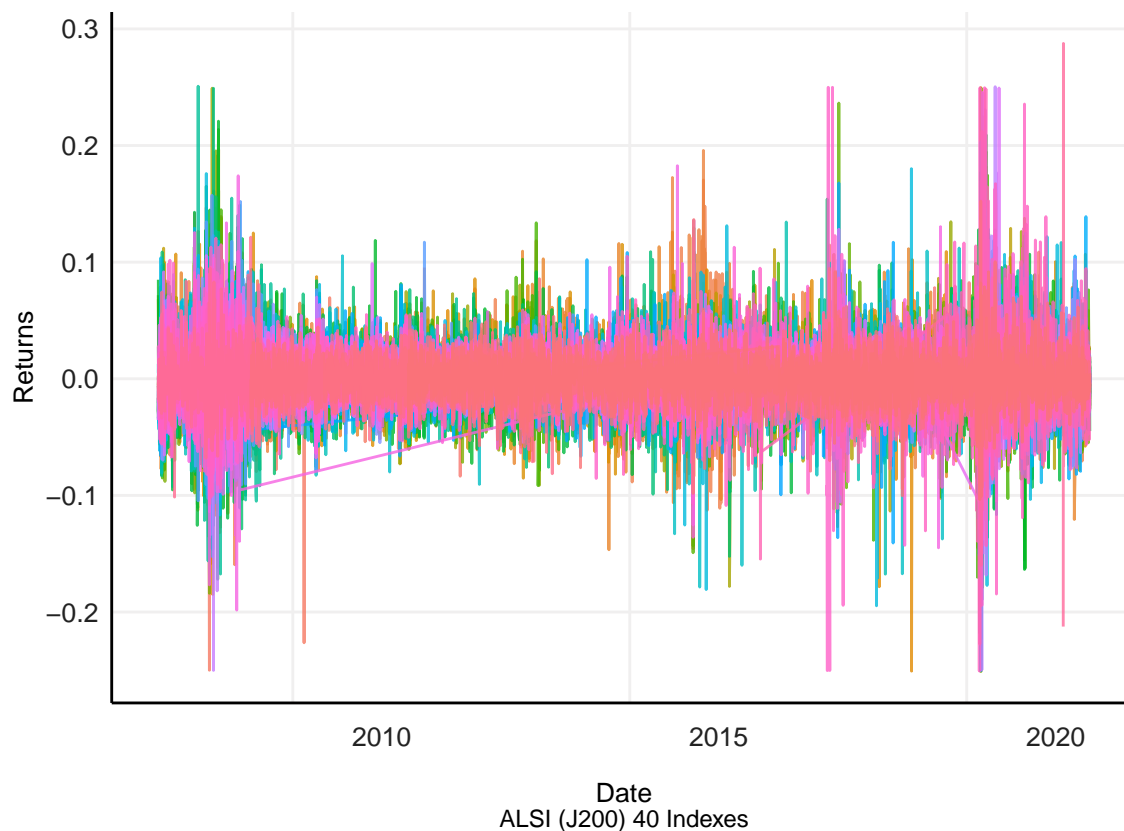


Now I winsorize the data by setting any return above 0.25% equal to 0.25% and create a weighted return column based on the J200 weights. I also determine if there are missing values that will effect the results of my analysis and then the data is mean-centered.

The index weight column J200 and Index\_Name column both have missing values, however this is nothing to be concerned about as this just implies that some stocks don't have weights as they were included in the Top 40 or will be in the future but are not included at present. Therefore, I remove missing values from the weights column.

## Returns of ALSI Weighted Indexes

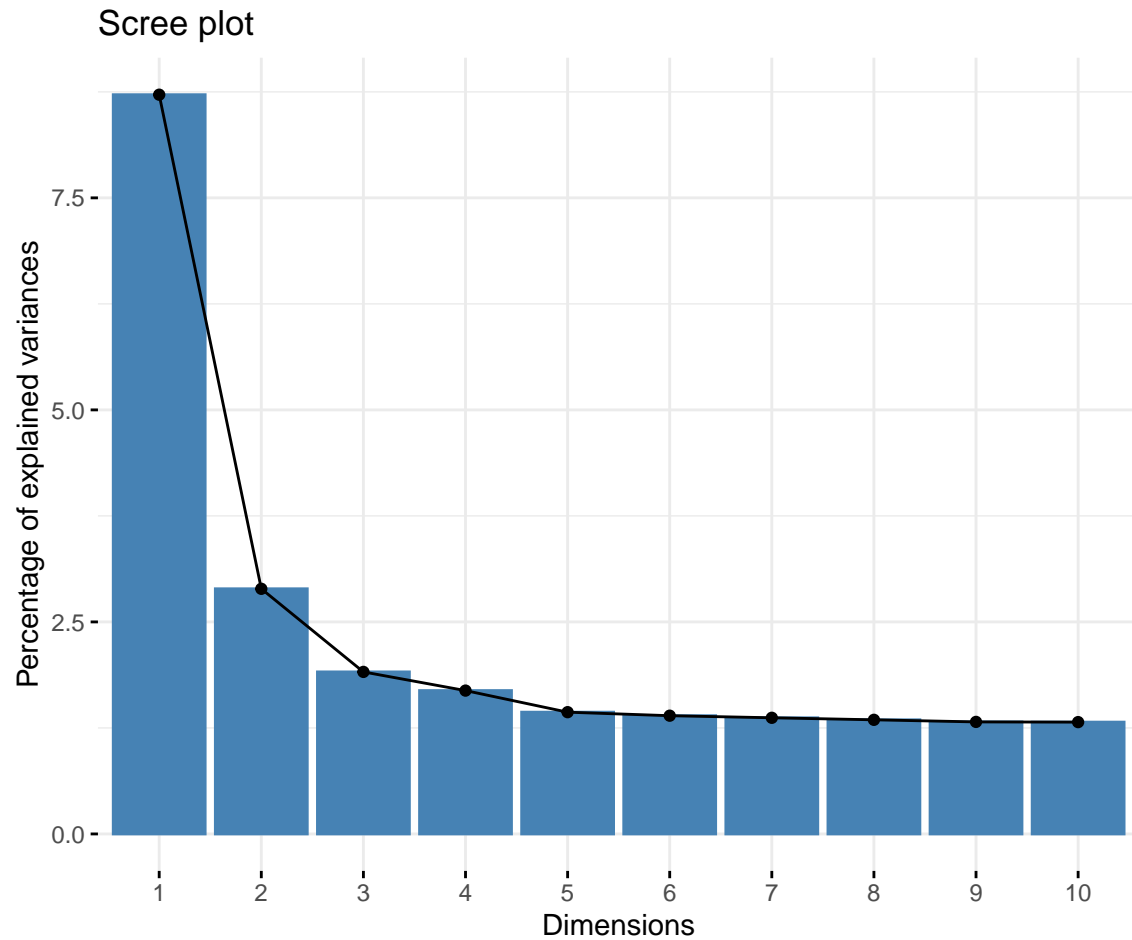
From 2008 to 2022



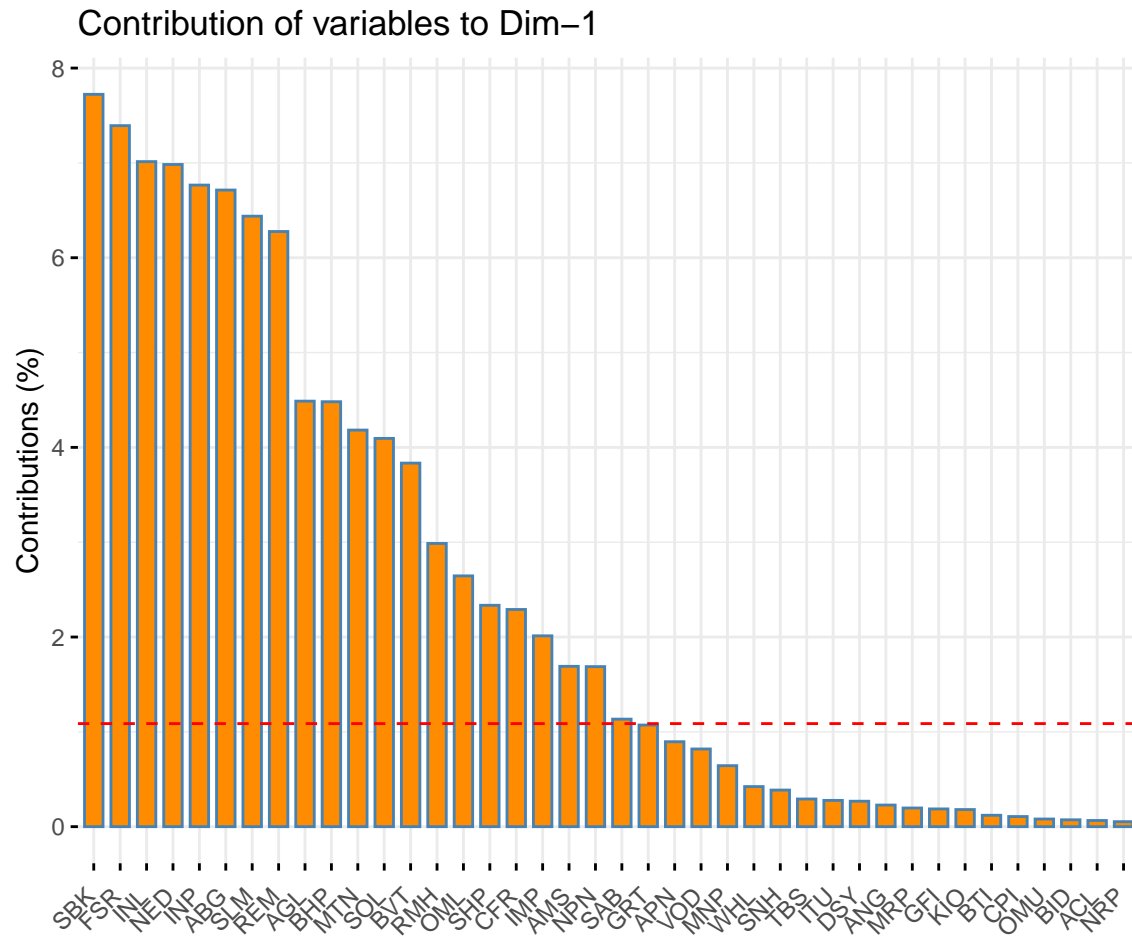
## PCA

Now that the data has been cleaned I begin the principal component analysis.

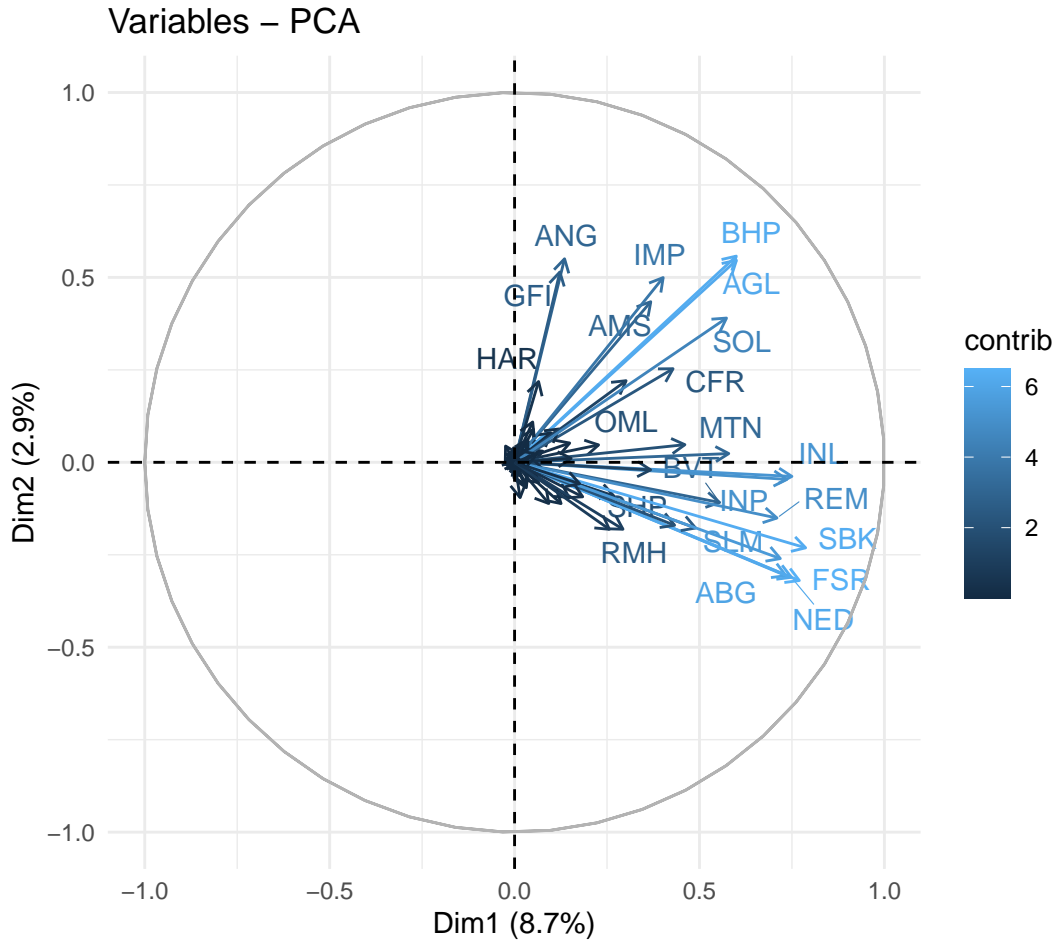
I make use of the FactoMineR package to run my first PCA, however once I made the data wide missing values for the returns of certain equities in the index at specific dates. This may be because of listing and de-listing on a public exchange. I now use the impute function to replace missing values with using "Drawn\_Distribution\_Own" method, however this did not work and then moved on to replacing the missing values with the "Drawn\_Distribution\_Collective" method.



From the scree plot above one can see the first 10 or 10 largest principal components. Each component (1-10) display's it's contribution to explaining the variation in the Top 40 data set. The first component explains approximately 8.5% of the variation. Components 2 through 10, each explain roughly between 2.6% and 2% of the variation.



The graph above provides the contribution each stop makes to the first component. The largest contributors to the are financials such as Standard Bank, First Rand, Invested, Nedbank, ABSA and Sanlam. Given the commonality of sector among the largest contributors to the first principal component. It is likely that the first principal competent is interest rates, given financial equities relationship to interest rates i.e. changing interest rates would significantly change financials share prices



## calc rolling contributions with PerformanceAnalytics

or starification from prac 2 bonus

The co-efficient of variation shows the extent of variability of data in a sample in relation to the mean of the population.

Table 1: Summary of Mean Application Statistics per Categyory

Tickers	High_Ratio	SD_High	FULL_SD_High	Low_Ratio	SD_Low	FULL_SD_LOW
IPL	0.00	0.00	0.00	0.93	0.00	0.00
TRU	0.92	0.00	0.00	0.99	0.00	0.00
LHC	1.04	0.00	0.00	1.01	0.00	0.00
MRP	1.05	0.00	0.00	0.76	0.00	0.00
MSM	1.08	0.00	0.00	1.03	0.00	0.00
SHP	1.09	0.00	0.00	0.87	0.00	0.00
NTC	1.12	0.00	0.00	0.72	0.00	0.00
WHL	1.13	0.00	0.00	0.88	0.00	0.00
MTN	1.15	0.02	0.02	0.95	0.02	0.02
APN	1.19	0.00	0.00	0.69	0.00	0.00
SOL	1.20	0.02	0.02	0.85	0.01	0.02

Tickers	High_Ratio	SD_High	FULL_SD_High	Low_Ratio	SD_Low	FULL_SD_LOW
CFR	1.21	0.03	0.02	0.74	0.02	0.02
AGL	1.21	0.04	0.04	0.88	0.03	0.04
VOD	1.21	0.00	0.00	0.78	0.00	0.00
DSY	1.22	0.00	0.00	0.54	0.00	0.00
BHP	1.24	0.05	0.04	0.87	0.04	0.04
EXX	1.24	0.00	0.00	0.78	0.00	0.00
REM	1.25	0.01	0.00	0.77	0.00	0.00
INP	1.25	0.00	0.00	0.77	0.00	0.00
NED	1.25	0.00	0.00	0.72	0.00	0.00
BVT	1.25	0.00	0.00	0.84	0.00	0.00
INL	1.25	0.00	0.00	0.81	0.00	0.00
REI	1.26	0.00	0.00	0.76	0.00	0.00
SBK	1.27	0.01	0.01	0.82	0.01	0.01
TBS	1.27	0.00	0.00	0.77	0.00	0.00
MND	1.27	0.00	0.00	0.60	0.00	0.00
ABG	1.28	0.01	0.00	0.65	0.00	0.00
RMH	1.28	0.00	0.00	0.82	0.00	0.00
GRT	1.28	0.00	0.00	0.64	0.00	0.00
MUR	1.30	0.01	0.00	0.90	0.00	0.00
AMS	1.30	0.01	0.01	0.73	0.00	0.01
SLM	1.30	0.01	0.01	0.66	0.00	0.01
IMP	1.31	0.02	0.01	0.74	0.01	0.01
BTI	1.31	0.01	0.01	0.65	0.00	0.01
MDC	1.31	0.00	0.00	0.78	0.00	0.00
OML	1.32	0.01	0.01	0.72	0.01	0.01
FSR	1.33	0.01	0.01	0.67	0.01	0.01
SAB	1.34	0.03	0.02	0.80	0.02	0.02
AEG	1.35	0.01	0.00	0.95	0.00	0.00
PPC	1.36	0.00	0.00	0.57	0.00	0.00
MNP	1.37	0.01	0.00	0.45	0.00	0.00
SAP	1.37	0.00	0.00	0.87	0.00	0.00
ITU	1.38	0.00	0.00	0.70	0.00	0.00
CCO	1.39	0.00	0.00	0.45	0.00	0.00
LON	1.40	0.00	0.00	0.63	0.00	0.00
NPN	1.41	0.06	0.04	0.42	0.02	0.04
ANG	1.42	0.01	0.01	0.74	0.01	0.01
LBH	1.43	0.00	0.00	0.64	0.00	0.00
ASR	1.44	0.00	0.00	0.84	0.00	0.00
KIO	1.47	0.00	0.00	0.84	0.00	0.00
PIK	1.48	0.00	0.00	0.74	0.00	0.00
SNH	1.48	0.01	0.01	0.60	0.00	0.01
TKG	1.48	0.01	0.00	0.54	0.00	0.00
GFI	1.50	0.01	0.01	0.67	0.01	0.01
ACL	1.55	0.01	0.00	0.61	0.00	0.00
LGL	1.57	0.00	0.00	0.79	0.00	0.00
HAR	1.64	0.01	0.00	0.63	0.00	0.00
AXL	1.73	0.00	0.00	0.73	0.00	0.00
ARI	1.76	0.00	0.00	0.73	0.00	0.00