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# Assignment 4 Part 3 - Andrew Paul 100996250

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In the third section of this assignment a current source and capacitor were added to create noise in the system. The G and C matrices were redefined in order to accommodate these new components.

## Updated G matrix

	1	2	3	4	5	6	7	8	9
1	-1	1	1	0	0	0	0	0	0
2	1	0	-1.5000	0	0	0	-1	0	0
3	0	0	0	-0.1000	0	0	1	0	-1
4	0	0	1	-1	0	0	0	0	0
5	0	0	0	-1000	0	10	0	1	0
6	0	0	0	1000	0	-10.0010	0	0	0
7	1	0	0	0	0	0	0	0	0
8	0	0	0	-10	1	0	0	0	0
9	0	0	0	0	0	0	0	0	1

## Updated C matrix

	1	2	3	4	5	6	7	8	9
1	-0.2500	0	0.2500	0	0	0	0	0	0
2	0.2500	0	-0.2500	0	0	0	0	0	0
3	0	0	0	-1.0000e-05	0	0	0	0	0
4	0	0	0	0	0	0	-0.2000	0	0
5	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0	0
7	0	0	0	0	0	0	0	0	0
8	0	0	0	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	0

```
close all;
clear;

%Initialize variables and matrices

G = zeros(9,9);
C = zeros(9,9);
```

```
F = zeros(9,1);

R1 =1;
R2 = 2;
R3 = 10;
R4 = 0.1;
R0 = 1000;
cap = 0.25;
L = 0.2;
alpha = 100;
Cn = 0.00001;

G1 = 1/R1;
G2 = 1/R2;
G3 = 1/R3;
G4 = 1/R4;
G0 = 1/R0;

% Redefined G matrix rows [V1 Iin V2 V3 V4 V5 IL I4 Iin]
% IL and I3 are no longer the same value with the added components
% Updated C and G Matrix

G(1, 1) = -G1;
G(1, 2) = G1;
G(2, 1) = G1;
G(1, 3) = G1;
G(2, 3) = -G1-G2;
G(3, 4) = -G3;
G(2, 7) = -1;
G(3, 7) = 1;
G(4, 3) = 1;
G(4, 4) = -1;
G(5, 6) = G4;
G(5, 4) = -alpha*G4;
G(5, 8) = 1;
G(6, 6) = -G4-G0;
G(6, 4) = alpha*G4;
G(8,4) = -alpha*G3;
G(7, 1) = 1;
G(8, 5) = 1;
G(3,9) = -1;
G(9,9) = 1;

% Create C matrix
C(1,1)= -cap;
C(2,1)= cap;
C(1,3)= cap;
C(2,3)= -cap;
C(3,4) = -Cn;
C(4,7)= -L;
```

```
F = zeros(1,9);

time_step = 0.001;

Vsolp = zeros(9,1);
A = C/(time_step) + G;

Vt = @(t) exp(-(1/2)*((t-0.06)/(0.03))^2);
Vout = zeros(1000,1);
Vin = zeros(1000,1);

i = 1;
time = zeros(1000,1);

for t=0:time_step:1

    % Random noise generator
    In = randn(1)*0.001;

    time(i) = t;
    F(1,7) = Vt(t);
    F(1,9) = In;
    Vsol = inv(A)*(C*Vsolp/time_step + F');
    Vout(i) = Vsol(6);
    Vin(i) = Vsol(1);
    Vsolp = Vsol;
    i = i+1;

end

figure(1)
subplot(2,1,2)
plot(time,Vout)
title('Guass Function - Vout vs. Time w/ Noise')
grid on

subplot(2,1,1)
plot(time,Vin)
title('Guass Function - Vin vs. Time w/ Noise')
grid on

% Vout Frequency plots

freq = 1000;
freqOut = fft(Vout);
x = length(Vout);
y = fftshift(freqOut);
freqShift = (-x/2:x/2-1)*(freq/x);
shift = abs(y).^2/x;

figure(2)
semilogy(freqShift,shift)
title('Gauss frquecnny spectrum - Vout w/ Noise')
```

```
% Vin freq plots

freqIn = fft(Vin);
x = length(Vin);
t = (0:x-1)*(freq/x);
power = abs(freqIn).^2/x;
y=fftshift(freqIn);
freqShift = (-x/2:x/2-1)*(freq/x);
shift = abs(y).^2/x;

figure(3)
semilogy(freqShift,shift)
title('Gauss frequency spectrum - Vin w/ Noise')

%Change Cap value 1
Cn = 0.1;
C = zeros(9,9);

C(1,1)= -cap;
C(2,1)= cap;
C(1,3)= cap;
C(2,3)= -cap;
C(3,4) = -Cn;
C(4,7)= -L;

A = C/(time_step) + G;
Vsolp = zeros(9,1);
Vt=@(t) exp(-(1/2)*((t-0.06)/(0.03))^2);
Vout=zeros(500,1);
Vin=zeros(500,1);
i = 1;
time=zeros(500,1);

for t=0:time_step:0.5
    In = randn(1)*0.001;
    time(i)=t;
    F(1,7) = Vt(t);
    F(1,9) = In;
    Vsol = inv(A)*(C*Vsolp/time_step + F');
    Vout(i) = Vsol(6);
    Vin(i) = Vsol(1);
    Vsolp = Vsol;
    i = i+1;
end

figure(4)
subplot(2,1,2)
plot(time,Vout)
title('Gauss Function - Vout vs. Time w/ Noise - Cn = 0.1')
grid on
```

```
subplot(2,1,1)
plot(time,Vin)
title('Guass Function - Vin vs. Time w/ Noise - Cn = 0.1')
grid on

freq = 1000;
freqOut = fft(Vout);
x = length(Vout);
y = fftshift(freqOut);
freqShift = (-x/2:x/2-1)*(freq/x);
shift = abs(y).^2/x;

figure(8)
semilogy(freqShift,shift)
title('Guass Function - Freq domain w/ Noise - Cn = 0.1')

% %Change Cap value 2
Cn = 0.0000001;
C = zeros(9,9);

C(1,1)= -cap;
C(2,1)= cap;
C(1,3)= cap;
C(2,3)= -cap;
C(3,4) = -Cn;
C(4,7)= -L;

A = C/(time_step) + G;
Vsolp = zeros(9,1);
Vt = @(t) exp(-(1/2)*((t-0.06)/(0.03))^2);
Vout = zeros(500,1);
Vin = zeros(500,1);
i = 1;
time = zeros(500,1);

for t=0:time_step:0.5
    In = randn(1)*0.001;
    time(i)=t;
    F(1,7) = Vt(t);
    F(1,9) = In;
    Vsol = inv(A)*(C*Vsolp/time_step + F');
    Vout(i) = Vsol(6);
    Vin(i) = Vsol(1);
    Vsolp = Vsol;
    i = i+1;
end

figure(5)
subplot(2,1,2)
plot(time,Vout)
title('Guass Function - Vout vs. Time w/ Noise - Cn = 0.0000001')
grid on
```

```
subplot(2,1,1)
plot(time,Vin)
title('Guass Function - Vin vs. Time w/ Noise - Cn = 0.0000001')
grid on

freq = 1000;
freqOut = fft(Vout);
x = length(Vout);
y = fftshift(freqOut);
freqShift = (-x/2:x/2-1)*(freq/x);
shift = abs(y).^2/x;

figure(11)
semilogy(freqShift,shift)
title('Guass Function - Freq domain w/ Noise - Cn = 0.0000001')

%Change Cap value 3
Cn = 0.001;
C = zeros(9,9);

C(1,1)= -cap;
C(2,1)= cap;
C(1,3)= cap;
C(2,3)= -cap;
C(3,4) = -Cn;
C(4,7)= -L;

A = C/(time_step) + G;
Vsolp = zeros(9,1);
Vt=@(t) exp(-(1/2)*((t-0.06)/(0.03))^2);
Vout=zeros(500,1);
Vin=zeros(500,1);
i = 1;
time=zeros(500,1);

for t=0:time_step:0.5
    In = randn(1)*0.001;
    time(i)=t;
    F(1,7) = Vt(t);
    F(1,9) = In;
    Vsol = inv(A)*(C*Vsolp/time_step + F');
    Vout(i) = Vsol(6);
    Vin(i) = Vsol(1);
    Vsolp = Vsol;
    i = i+1;
end

figure(9)
subplot(2,1,2)
plot(time,Vout)
title('Guass Function - Vout vs. Time w/ Noise - Cn = 0.001')
grid on
```

```
subplot(2,1,1)
plot(time,Vin)
title('Guass Function - Vin vs. Time w/ Noise - Cn = 0.001')
grid on

freq = 1000;
freqOut = fft(Vout);
x = length(Vout);
y = fftshift(freqOut);
freqShift = (-x/2:x/2-1)*(freq/x);
shift = abs(y).^2/x;

figure(10)
semilogy(freqShift,shift)
title('Guass Function - Freq domain w/ Noise - Cn = 0.001')

freq = 1000;

% Vary the Time Step

% Time Step = 0.0001

time_step=0.0001;

Vsolp= zeros(9,1);

Cn = 0.0000001;
C = zeros(9,9);

C(1,1)= -cap;
C(2,1)= cap;
C(1,3)= cap;
C(2,3)= -cap;
C(3,4) = -Cn;
C(4,7)= -L;

A = C/(time_step) + G;

Vt=@(t) exp(-(1/2)*((t-0.06)/(0.03))^2);
Vout = zeros(10000,1);
Vin = zeros(10000,1);

i = 1;

time = zeros(10000,1);
for t=0:time_step:1

    % Random noise generator
    In = randn(1)*0.001;

    time(i) = t;
```

```
F(1,7) = Vt(t);
F(1,9) = In;
Vsol = inv(A)*(C*Vsolp/time_step + F');
Vout(i) = Vsol(6);
Vin(i) = Vsol(1);
Vsolp = Vsol;
i = i+1;

end

figure(6)
subplot(2,1,2)
plot(time,Vout)
title('Guass Function - Vout vs. Time w/ Noise - Time step = 0.0001')
grid on

subplot(2,1,1)
plot(time,Vin)
title('Guass Function - Vout vs. Time w/ Noise - Time step = 0.0001')
grid on

% Part (d

time_step=0.01;

Vsolp= zeros(9,1);

Cn = 0.0000001;
C = zeros(9,9);

C(1,1)= -cap;
C(2,1)= cap;
C(1,3)= cap;
C(2,3)= -cap;
C(3,4) = -Cn;
C(4,7)= -L;

A = C/(time_step) + G;

Vt=@(t) exp(-(1/2)*((t-0.06)/(0.03))^2);
Vout = zeros(10000,1);
Vin = zeros(10000,1);

i = 1;

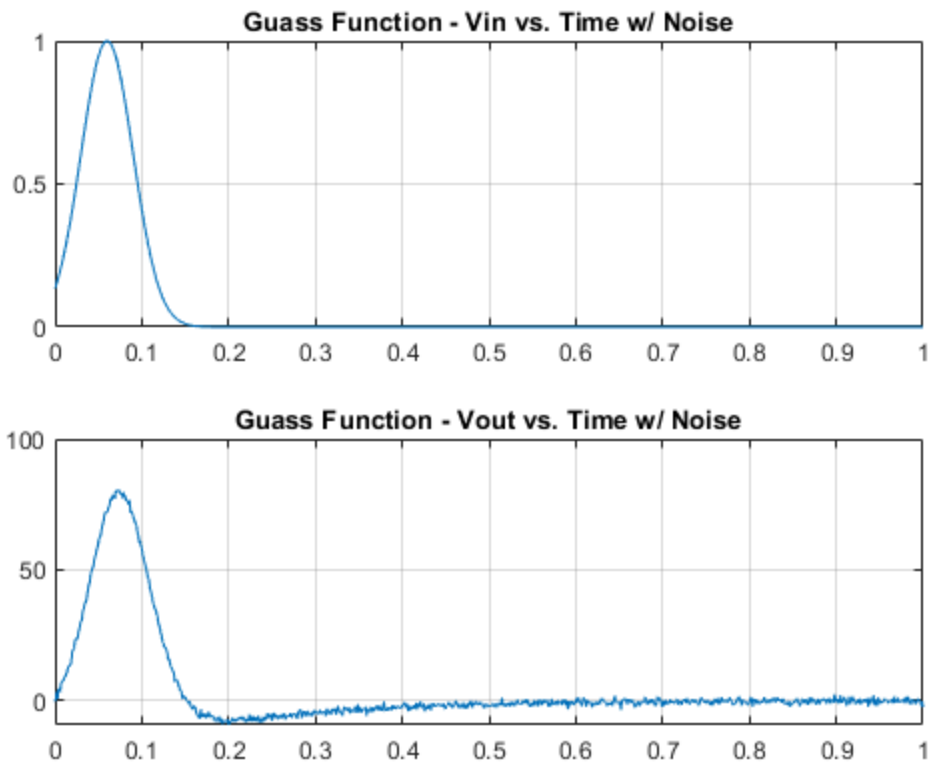
time = zeros(10000,1);
for t=0:time_step:1

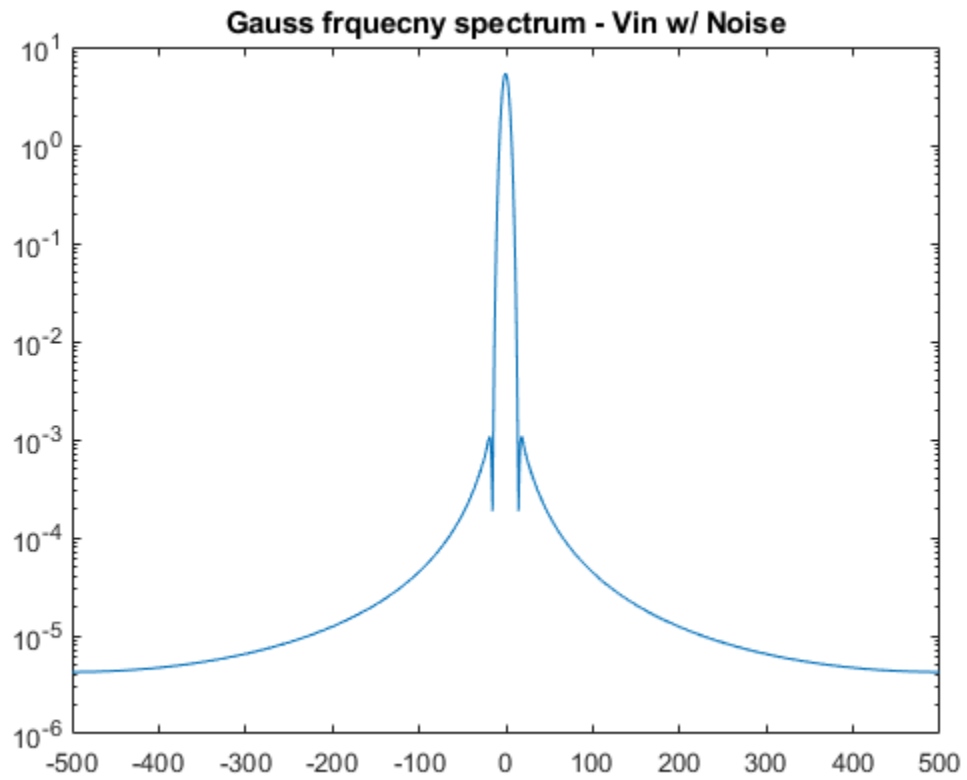
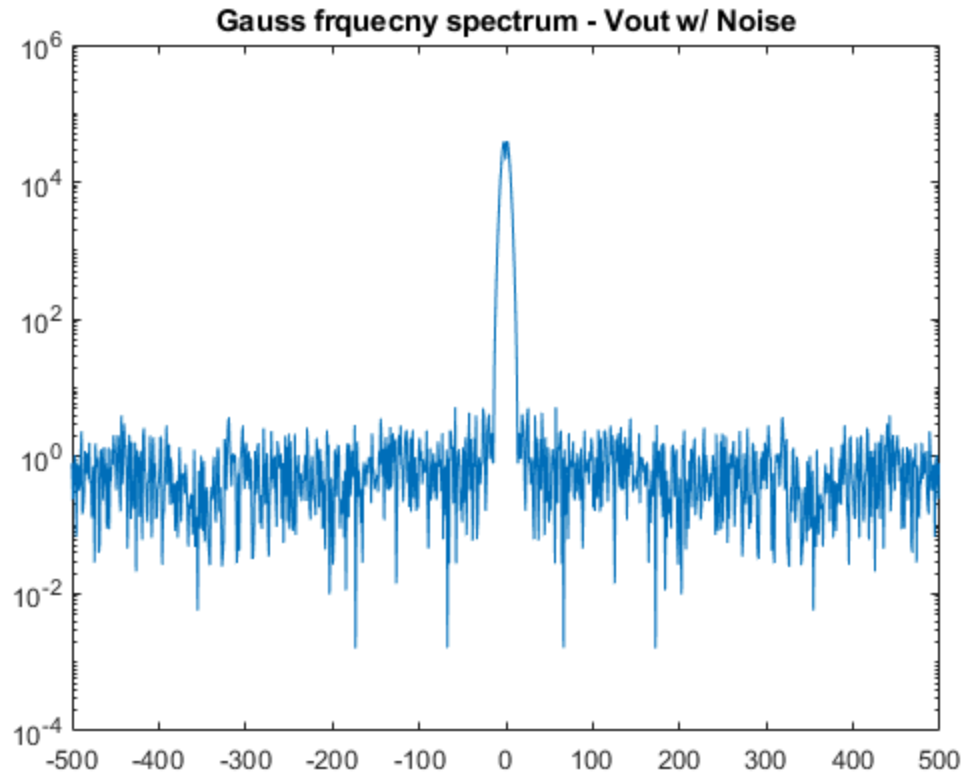
    % Random noise generation
    In = randn(1)*0.001;

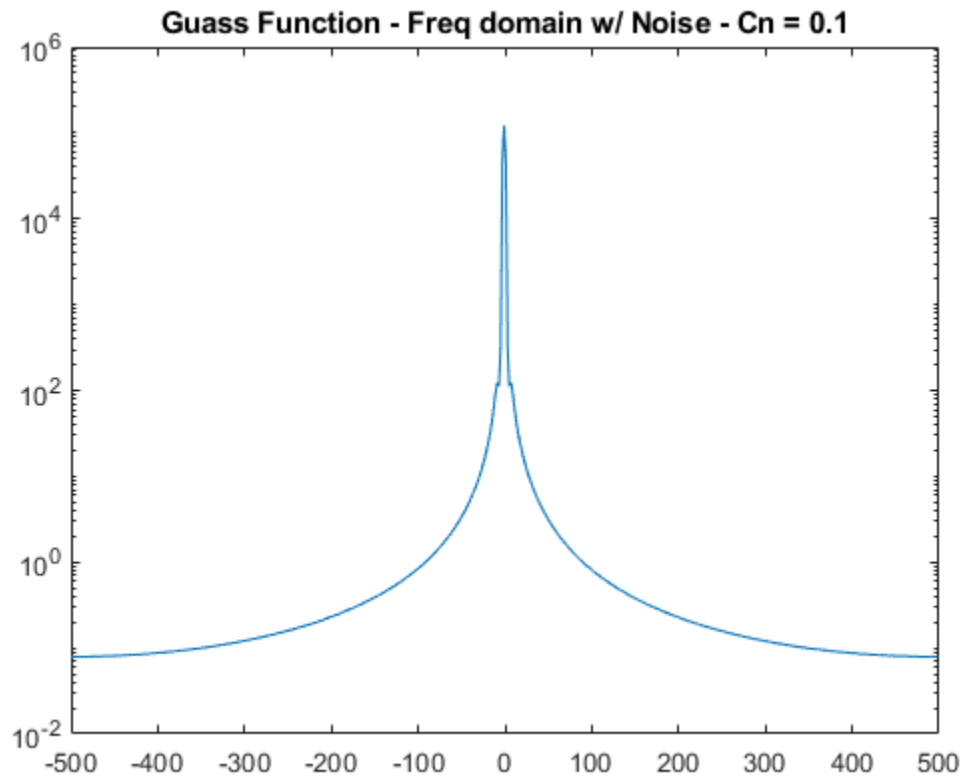
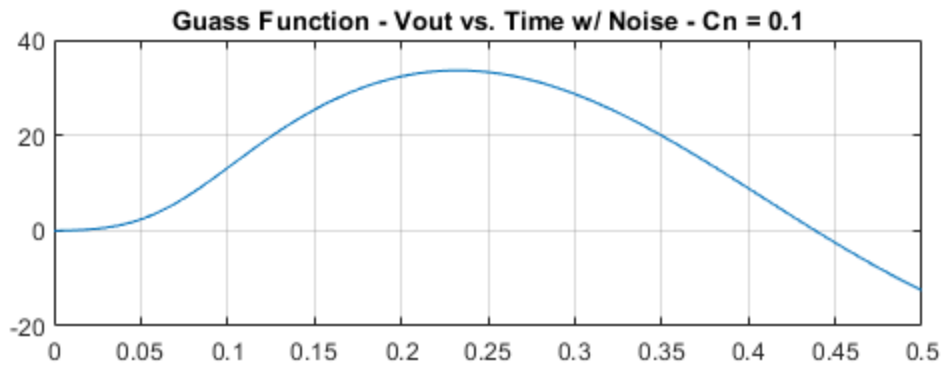
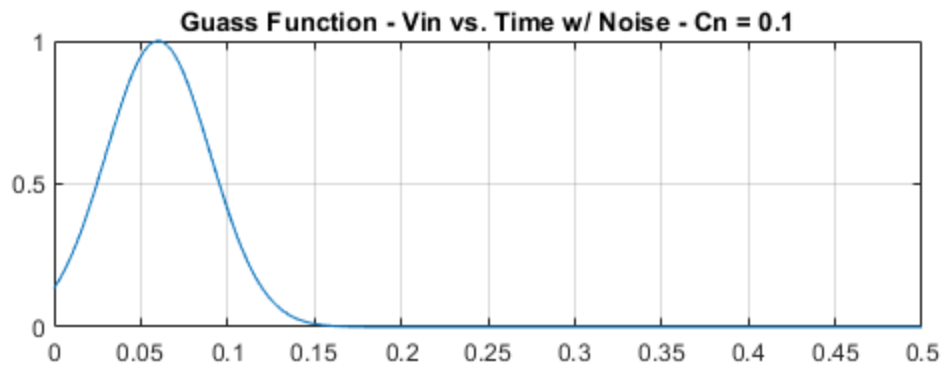
    time(i) = t;
    F(1,7) = Vt(t);
    F(1,9) = In;
```

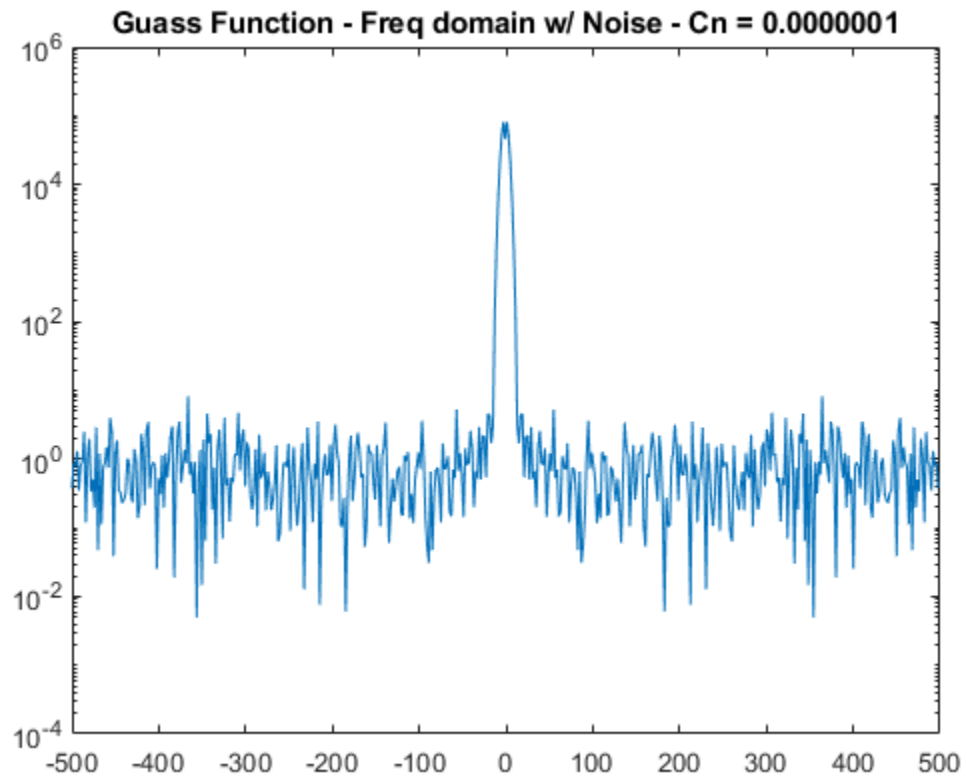
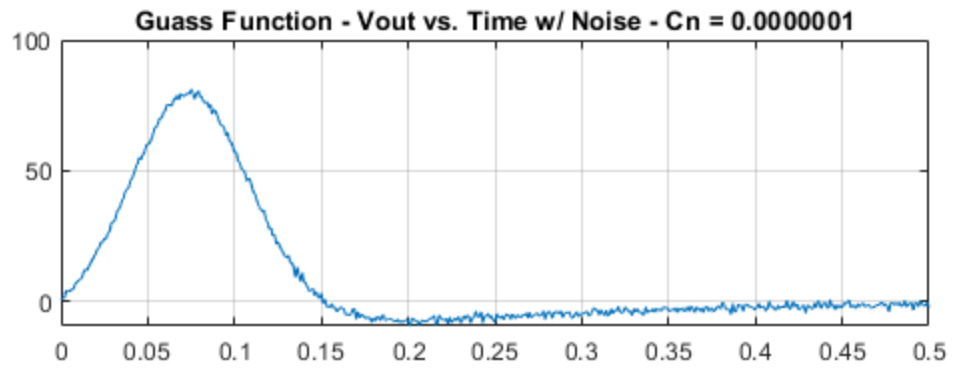
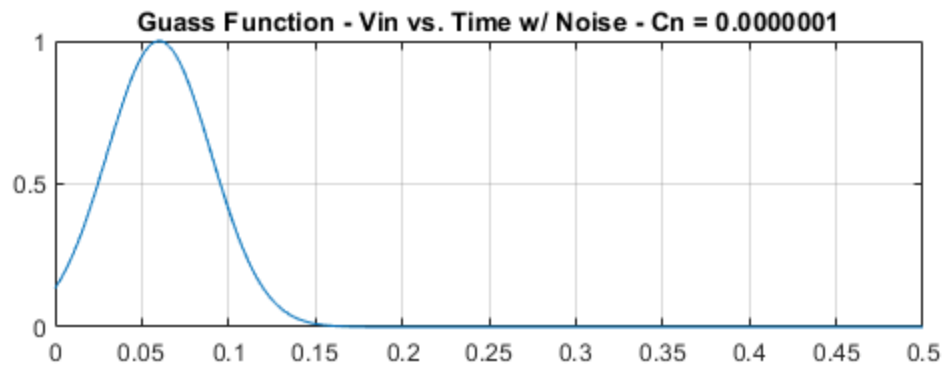


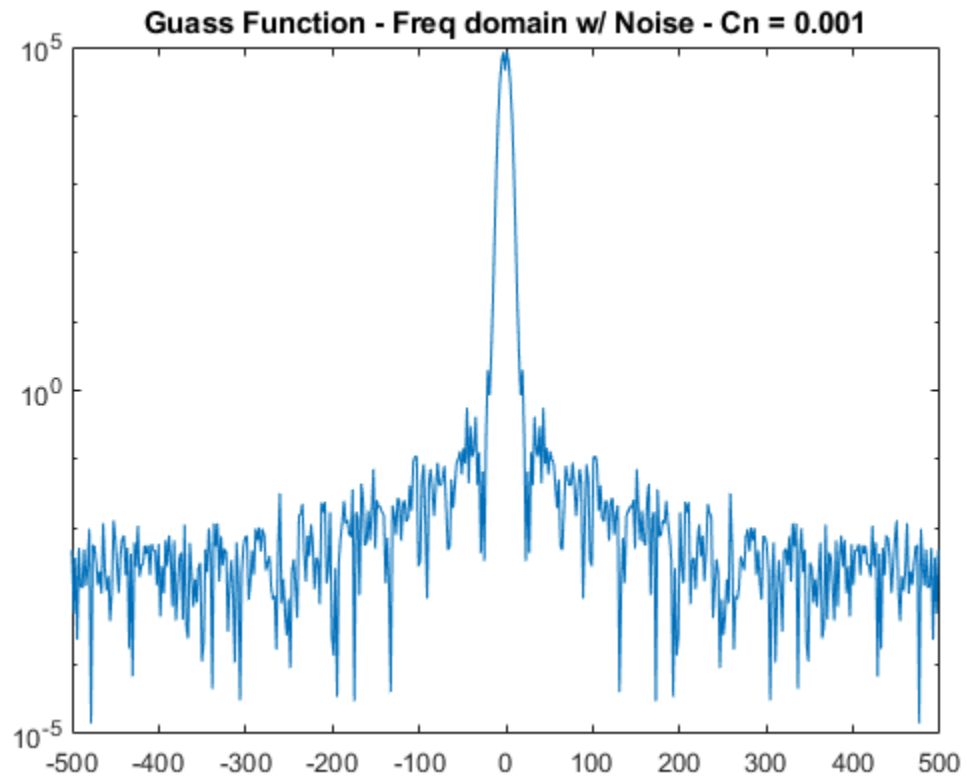
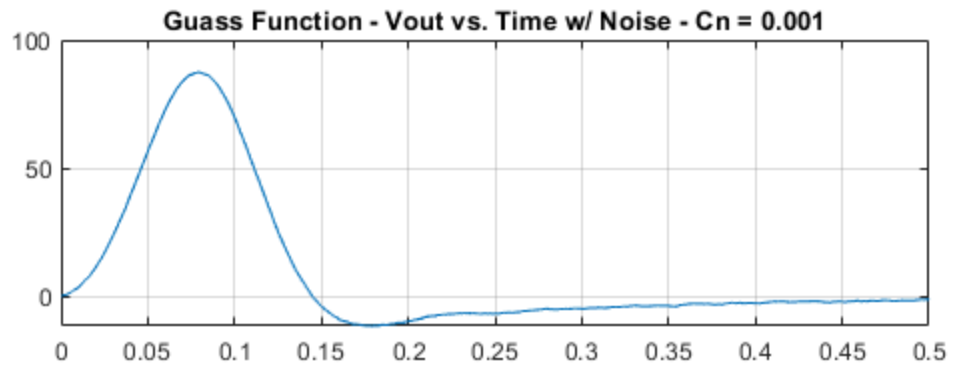
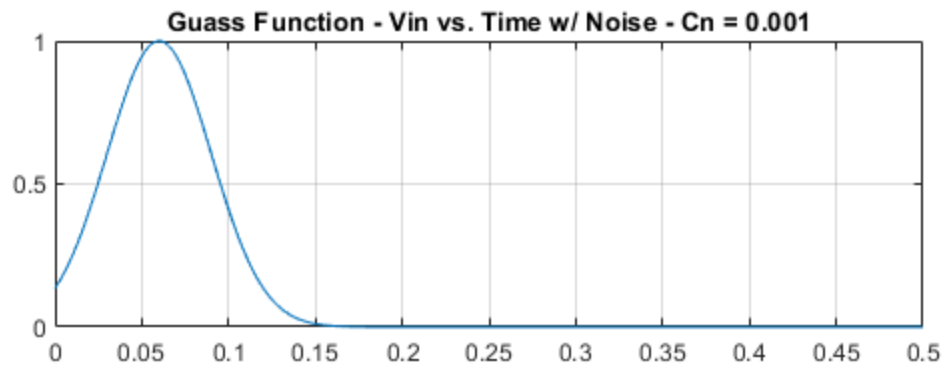
```
Vsol = inv(A)*(C*Vsolp/time_step + F');  
Vout(i) = Vsol(6);  
Vin(i) = Vsol(1);  
Vsolp = Vsol;  
i = i+1;  
  
end  
  
figure(7)  
subplot(2,1,2)  
plot(time,Vout)  
title('Guass Function - Vout vs. Time w/ Noise - Time step = 0.01')  
grid on  
  
subplot(2,1,1)  
plot(time,Vin)  
title('Guass Function - Vin vs. Time w/ Noise - Time step = 0.01')  
grid on
```

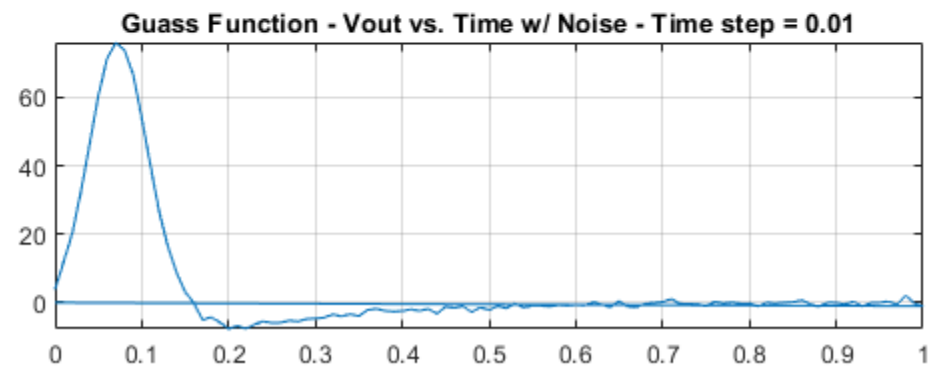
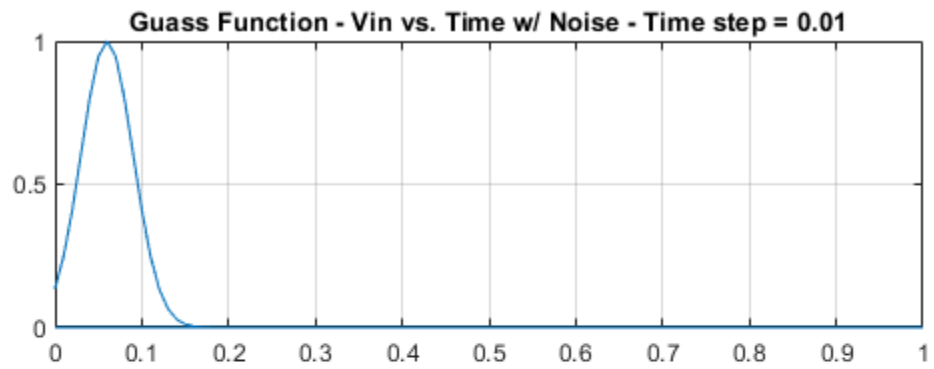
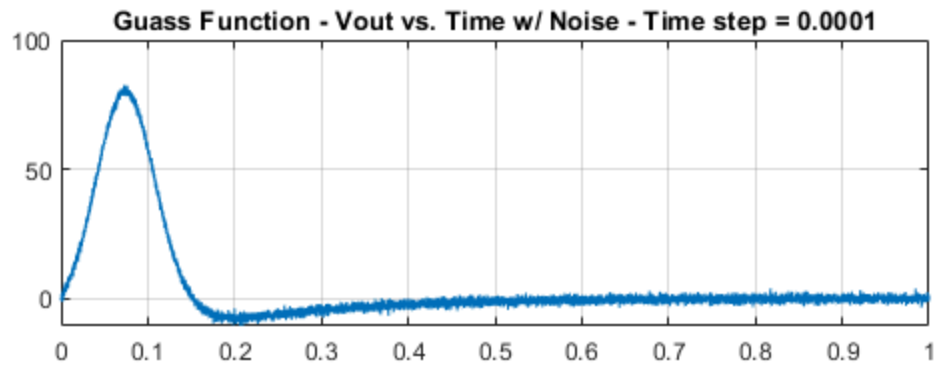
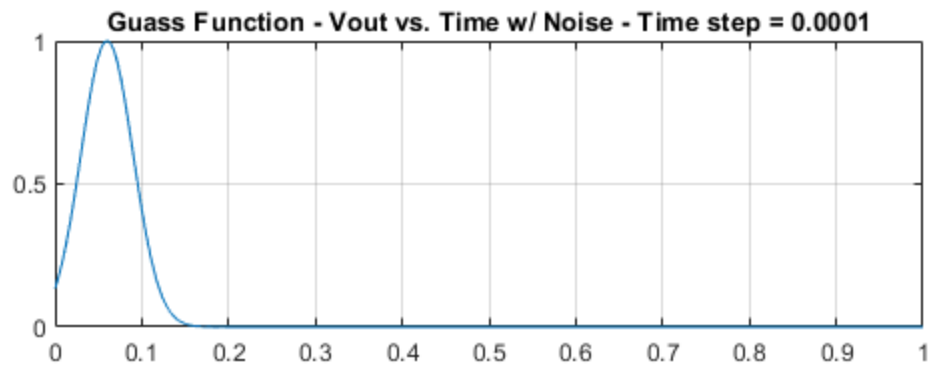












Increasing the value of  $C_n$  appears to decrease the bandwidth of the signal over the output.

## Assignment 4 Part 4 - Andrew Paul

The fourth section of this assignment discusses the implementation of non-linearity in the circuit.

Through research on the modelling of non-linearity in circuits it was found that the following method could be used to implement the given changes in the circuit. First, a Jacobian matrix could be created and solved to give the solution to the non-linear voltage generation which would be controlled by the current. The Newton-Raphson method could then be used to solve for the finite change in the value of the voltage generator. Similarly to previous procedures, a matrix defining the output voltage would then be solved for to give a good approximation of the final output values.

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